

Genetic cartography reveals ancestral relationships of human pathogenic viruses

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[Sravani Nanduri comments] [Alli Black comments] [Trevor Bedford comments] [John Huddleston comments]

Abstract

[285 words, limit is 300] Public health studies commonly infer phylogenies from viral genome sequences to understand transmission dynamics and identify clusters of genetically-related samples. However, viruses that reassort or recombine violate phylogenetic assumptions and require more sophisticated methods. Even when phylogenies are appropriate, they can be unnecessary. For example, pairwise distances between sequences can be enough to identify clusters of related samples or assign new samples to existing phylogenetic clusters. In this work, we tested whether dimensionality reduction methods could capture known genetic groups within two human pathogenic viruses that cause substantial human morbidity and mortality and frequently reassort or recombine, respectively: seasonal influenza A/H3N2 and SARS-CoV-2. We applied principal component analysis (PCA), multidimensional scaling (MDS), t-distributed stochastic neighbor embedding (t-SNE), and uniform manifold approximation and projection (UMAP) to sequences with well-defined

phylogenetic clades and either reassortment (H3N2) or recombination (SARS-CoV-2). For each low-dimensional embedding of sequences, we calculated the correlation between pairwise genetic and Euclidean distances in the embedding and applied a hierarchical clustering method to identify clusters in the embedding. We measured the accuracy of these clusters compared to previously defined phylogenetic clades, reassortment clusters, or recombinant lineages. We found that MDS maintained the strongest correlation between pairwise genetic and Euclidean distances between sequences, best captured the intermediate placement of recombinant lineages between parental lineages, and most accurately identified reassortment groups. Clusters from t-SNE most accurately recapitulated known phylogenetic clades. We show that simple statistical methods without a biological model can accurately represent known genetic relationships for relevant human pathogenic viruses. Our open source implementation of these methods for analysis of viral genome sequences can be easily applied when phylogenetic methods are either unnecessary or inappropriate.

Author summary

TBD.

Introduction

Tracking the evolution of human pathogenic viruses in real time enables epidemiologists to respond quickly to emerging epidemics and local outbreaks [1]. Real-time analyses of viral evolution typically rely on phylogenetic methods that can reconstruct the evolutionary history of viral populations from their genome sequences and estimate states of inferred ancestral viruses from the resulting trees including their most likely genome sequence, time of circulation, and geographic location [2–4]. Importantly, these methods assume that all sequence data share an evolutionary history represented by the clonal replication of genomes. In practice, the evolutionary histories of many human pathogenic viruses violate this assumption through processes of reassortment or recombination, as seen in seasonal influenza [5, 6] and seasonal coronaviruses [7], respectively. Researchers account for these evolutionary mechanisms by limiting their

analyses to individual genes [8, 9], combining multiple genes despite their different evolutionary histories [10], or developing more sophisticated models to represent the joint likelihoods of multiple co-evolving lineages with ancestral reassortment or recombination graphs [11, 12]. However, several key questions in genomic epidemiology do not require full phylogenetic inference of ancestral relationships and states. For example, genomic epidemiologists commonly need to 1) identify clusters of closely-related genomes that represent regional outbreaks or new variants of concern [13–16], 2) place newly sequenced viral genomes in the evolutionary context of other circulating samples [17–19], and 3) visualize the genetic relationships among closely related virus samples [20, 21]. Given that these common use cases rely on genetic distances between samples, tree-free statistical methods that operate on pairwise distances could be sufficient to address each case. As these tree-free methods lack a formal biological model of evolutionary relationships, they make weak assumptions about the input data and therefore should be applicable to pathogen genomes that violate phylogenetic assumptions.

Common statistical approaches to analyzing variation from genome alignments start by transforming alignments into a matrix that codes each distinct nucleotide character as an integer or a distance matrix representing the pairwise distances between sequences. The first of these transformations is the first step prior to performing a principal component analysis (PCA) to find orthogonal representations of the inputs that explain the most variance [22]. The second transformation calculates the number of mismatches between each pair of aligned genome sequences, also known as the Hamming distance, to create a distance matrix. Most phylogenetic methods begin by building a distance matrix for all sequences in a given multiple sequence alignment. Dimensionality reduction algorithms such as multidimensional scaling (MDS) [23], t-distributed stochastic neighbor embedding (t-SNE) [24], and uniform manifold approximation and projection (UMAP) [25] accept such distance matrices as an input and produce a corresponding low-dimensional representation or “embedding” of those data. Both types of transformation allow us to reduce high-dimensional genome alignments ($M \times N$ values for M genomes of length N) to low-dimensional embeddings where clustering algorithms and visualization are more tractable. Additionally, distance-based methods can reflect the presence or absence of insertions and deletions in an alignment that

phylogenetic methods ignore.

Each of the embedding methods mentioned above has been applied previously to genomic data to identify clusters of related genomes and visualize relationships between individuals. Although PCA is a generic linear algebra algorithm that optimizes for an orthogonal embedding of the data, the principal components from single nucleotide polymorphisms (SNPs) represent mean coalescent times and therefore recapitulate broad phylogenetic relationships [26]. PCA has been applied to SNPs of human genomes [26–29] and to multiple sequence alignments of viral genomes [30]. MDS attempts to embed input data into a lower-dimensional representation such that each pair of data points are as far apart in the embedding as they are in the original data. MDS has been applied to multiple gene segments of seasonal influenza viruses to visualize evolutionary relationships between segments [31]. Both t-SNE and UMAP build on manifold learning methods like MDS to find low-dimensional embeddings of data that place similar points close together and dissimilar points far apart [32]. These methods have been applied to SNPs from human genomes [33] and single-cell transcriptomes [34, 35].

Although these methods are commonly used for qualitative studies of evolutionary relationships, few studies have attempted to quantify patterns observed in the resulting embeddings and no studies have investigated the value of applying these methods to human pathogenic viruses. To this end, we tuned and validated the performance of PCA, MDS, t-SNE, and UMAP with genomes from simulated influenza-like and coronavirus-like populations and then applied these methods to natural populations of seasonal influenza virus A/H3N2 and SARS-CoV-2. These natural viruses are highly relevant as major causes of global human mortality, common subjects of real-time genomic epidemiology, and representatives of reassortant and recombinant human pathogens. For each combination of virus and embedding method, we quantified the relationship between pairwise genetic and Euclidean embedding distances, identified clusters of closely-related genomes in embedding space, and evaluated the accuracy of clusters compared to genetic groups defined by experts and biologically-informed models. Finally, we tested the ability of these methods to identify reassortment of seasonal influenza virus hemagglutinin (HA) and neuraminidase (NA) segments and recombination in SARS-CoV-2 genomes. These results inform our recommendations for

future applications of these methods including which are most effective for specific
77 problems in genomic epidemiology and which parameters researchers should use for each
78 method.
79

Materials and methods

[This placement of methods before results breaks with PLoS's default organization.
80 This organization follows that used by the TreeKnit paper which seemed to be a useful
81 model for this paper.]
82

Embedding methods

We selected four standard and common dimensionality reduction (or “embedding”)
83 methods to apply to human pathogenic viruses: PCA, MDS, t-SNE, and UMAP. PCA
84 operates on a matrix with samples in rows, “features” in columns, and numeric values
85 in each cell [22]. To apply PCA to multiple sequence alignments, we transformed each
86 nucleotide value into a corresponding integer (A to 1, G to 2, C to 3, T to 4, and all
87 other values to 5) and applied scikit-learn’s PCA implementation to the resulting
88 numerical matrix with the “full” singular value decomposition solver and 10
89 components [36].
90

The remaining three methods operate on a distance matrix. We constructed a
91 distance matrix from a multiple sequence alignment by calculating the pairwise
92 Hamming distance between nucleotide sequences. By default, the Hamming distance
93 only counted mismatches between pairs of standard nucleotide values (A, C, G, and T),
94 ignoring other values including gaps. We implemented an optional mode that
95 additionally counted each occurrence of consecutive gap characters in either input
96 sequence as individual insertion/deletion (“indel”) events.
97

We applied scikit-learn’s MDS implementation to a given distance matrix, with an
100 option to set the number of components in the resulting embedding [36]. Similarly, we
101 applied scikit-learn’s t-SNE implementation, with options to set the “perplexity” and
102 the “learning rate”. The perplexity controls the number of neighbors the algorithm uses
103 per input sample to determine an optimal embedding [24]. This parameter effectively
104 determines the balance between maintaining “local” or “global” structure in the
105

embedding [35]. The learning rate controls how rapidly the t-SNE algorithm converges 106 on a specific embedding [24, 37] and should scale with the number of input samples [38]. 107 We initialized t-SNE embeddings with the first two components of the corresponding 108 PCA embedding, as previously recommended to obtain more accurate global 109 structure [32, 35]. Finally, we applied the *umap-learn* Python package written by 110 UMAP’s authors, with options to set the number of “nearest neighbors” and the 111 “minimum distance” [25]. As with t-SNE’s perplexity parameter, the nearest neighbors 112 parameter determines how many adjacent samples the UMAP algorithm considers per 113 sample to find an optimal embedding. The minimum distance sets the lower limit for 114 how close any two samples can map next to each other in a UMAP embedding. Lower 115 minimum distances allow tighter groups of samples to form. For both t-SNE and 116 UMAP, we used the default number of components of 2. 117

Simulation of influenza-like and coronavirus-like populations 118

Given the relative lack of prior application of dimensionality reduction methods to 119 human pathogenic viruses, we first attempted to understand the behavior and optimal 120 parameter values for these methods when applied to simulated viral populations with 121 well-defined evolutionary parameters. To this end, we simulated populations of 122 influenza-like and coronavirus-like viruses using SANTA-SIM [39]. These simulated 123 populations allowed us to identify optimal parameters for each embedding method, 124 without overfitting to the limited data available for natural viral populations. For each 125 population type described below, we simulated five independent replicates with fixed 126 random seeds for over 55 years, filtered out the first 10 years of each population as a 127 burn-in period, and analyzed the remaining years. 128

We simulated influenza-like populations as previously described with 1,700 bp 129 hemagglutinin sequences [40]. As in that previous study, we scaled the number of 130 simulated generations per real year to 200 per year to match the observed mutation rate 131 for natural H3N2 HA sequences, and we sampled 10 genomes every 4 generations for 132 12,000 generations (or 60 years of real time). 133

We simulated coronavirus-like populations as previously described for human 134 seasonal coronaviruses with genomes of 21,285 bp [12]. For the current study, we 135

assigned 30 generations per real year to obtain mutation rates similar to the 8×10^{-4}
136 substitutions per site per year estimated for SARS-CoV-2 [41]. To account for the effect
137 of recombination on optimal method parameters, we simulated populations with a
138 recombination rate of 10^{-5} events per site per year based on human seasonal
139 coronaviruses for which recombination rates are well-studied [12, 42]. We calibrated the
140 overall recombination probability in SANTA-SIM such that the number of observed
141 recombination events per year matched the expected number for human seasonal
142 coronaviruses (0.3 per year) [12]. To assist with this calibration of recombination events
143 per year, we modified the SANTA-SIM source code to emit a boolean status of “is
144 recombinant” for each sampled genome. This change allowed us to identify recombinant
145 genomes by their metadata in downstream analyses and calculate the number of
146 recombination events observed per year. For each replicate population, we sampled 15
147 genomes every generation for 1,700 generations (or approximately 56 years of real time).
148

Optimization of embedding method parameters

149

We identified optimal parameter values for each embedding method with time series
150 cross-validation of embeddings based on simulated populations [43]. To increase the
151 interpretability of embedding space, we defined parameters as “optimal” when they
152 maximized the linear relationship between pairwise genetic distance of viral genomes
153 and the corresponding Euclidean distance between those same genomes in an
154 embedding. This optimization approach allowed us to also determine the degree to
155 which each method could recapitulate this linear relationship.
156

For each simulated population replicate, we created 10 training and test datasets
157 that each consisted of 4 years of training data and 4 years of test data preceded by a
158 1-year gap from the end of the training time period. These settings produced
159 training/test data with 2000 samples each for influenza-like populations and 1800
160 samples each for coronavirus-like populations. For each combination of training/test
161 dataset, embedding method, and method parameters, we applied the following steps.
162 We created an embedding from the training data with the given parameters, fit a linear
163 model to estimate pairwise genetic distance from pairwise Euclidean distance in the
164 embedding, created an embedding from the test data, estimated the pairwise genetic
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distance for genomes in the test data based on their Euclidean distances and the linear
166 model fit to the training data, and calculated the mean absolute error (MAE) between
167 estimated and observed genetic distances in the test data. We summarized the error for
168 a given population type, method, and method parameters across all population
169 replicates and training/test data by calculating the median of the MAE. For all method
170 parameters except those controlling the number of components used for the embedding,
171 we selected the optimal parameters as those that minimized the median MAE for a
172 given embedding method. Since increasing the number of components used by PCA and
173 MDS allows these methods to overfit to available data, we selected the optimal number
174 of components for these methods as the number beyond which the median MAE did not
175 decrease by at least 1 nucleotide. This approach follows the same concept from the
176 MDS algorithm itself where optimization occurs iteratively until the algorithm reaches a
177 predefined error threshold [23].
178

With the approach described above, we tested each method across a range of
179 relevant parameters with all combinations of parameter values. For PCA, we tested the
180 number of components between 2 and 6. For MDS, we tested the number of
181 components between 2 and 10. [The difference in number of components between PCA
182 and MDS sticks out here. We should use the same number for both or justify using
183 different numbers.] For t-SNE, we tested perplexity values of 15, 30, 100, 200, and 300,
184 and we tested learning rates of 100, 200, and 500. For UMAP, we tested nearest
185 neighbor values of 25, 50, and 100, and we tested values for the minimum distance that
186 points can be in an embedding of 0.05, 0.1, and 0.25.
187

Selection of natural virus population data

188

We selected recent publicly available genome sequences and metadata for seasonal
189 influenza H3N2 HA and NA genes and SARS-CoV-2 genomes from INSDC
190 databases [44]. For both viruses, we divided the available data into “early” and “late”
191 datasets to use as training and test data, respectively, for identification of virus-specific
192 clustering parameters. [First mention of clustering happens here before we define what
193 clustering is later on. Maybe ok as long as we reference the “later on” bit here
194 parenthetically?]
195

For analyses that focused only on H3N2 HA data, we defined the early dataset 196
between January 2016 and January 2018 and the late dataset between January 2018 to 197
January 2020. These datasets reflected two years of recent H3N2 evolution up to the 198
time when the SARS-CoV-2 pandemic disrupted seasonal influenza circulation. For both 199
early and late datasets, we evenly sampled 25 sequences per country, year, and month, 200
excluding known outliers. With this sampling scheme, we selected 1,523 HA sequences 201
for the early dataset and 1,073 for the late dataset. For analyses that combined H3N2 202
HA and NA data, we defined a single dataset between January 2016 and January 2018, 203
keeping 1,607 samples for which both HA and NA have been sequenced. 204

For SARS-CoV-2 data, we defined the early dataset between January 1, 2020 and 205
January 1, 2022 and the late dataset between January 1, 2022 and November 3, 2023. 206
For the early dataset, we evenly sampled 1,736 SARS-CoV-2 genomes by geographic 207
region, year, and month, excluding known outliers. For the late dataset, we used the 208
same even sampling by space and time to select 1,309 representative genomes. In 209
addition to these genomes, we sampled at most 20 genomes per Nextclade pango lineage 210
for 10 known recombinant lineages (XAY, XBB, XBB.1, XBC, XBF, XBL, XC, XD, 211
XE, XF, and XG) and their corresponding parental lineages (AY.29, AY.4, AY.45, 212
B.1.1.7, B.1.617, BA.1, BA.2, BA.2.75, BA.4, BA.5, BA.5.2.3, BJ.1, BM.1.1.1, and 213
CJ.1) as defined by <https://libguides.mskcc.org/SARS2/recombination>. [At this point, 214
we haven't defined "Pango lineages" yet, but I don't know that it makes sense to define 215
lineages in this section. Curious what other people think.] With these additional 216
genomes, the late SARS-CoV-2 dataset included 1,668 total genomes. 217

Evaluation of linear relationships between genetic distance and 218 Euclidean distance in embeddings 219

To evaluate the biological interpretability of distances between samples in 220
low-dimensional embeddings, we plotted the pairwise Euclidean distance between 221
samples in each embedding against the corresponding genetic distance between the same 222
samples. We calculated Euclidean distance using all components of the given embedding 223
(e.g., 2 components for PCA, t-SNE, and UMAP and 3 components for MDS). For each 224
embedding, we fit a linear model between Euclidean and genetic distance and calculated 225

the squared Pearson’s correlation coefficient, R^2 . The distance plots provide a
226 qualitative assessment of each embedding’s local and global structure relative to a
227 biologically meaningful scale of genetic distance, while the linear models and correlation
228 coefficients quantify the global structure in the embeddings.
229

Phylogenetic analysis

For each natural population described above, we created an annotated, time-scaled
231 phylogenetic tree. For seasonal influenza H3N2 HA and NA sequences, we aligned
232 sequences with MAAFT (version 7.486) [45, 46] using the *augur align* command (version
233 22.0.3) [47]. For SARS-CoV-2 sequences, we used existing reference-based alignments
234 provided by the Nextstrain team
235
(https://docs.nextstrain.org/projects/ncov/en/latest/reference/remote_inputs.html) and
236 generated with Nextalign (version 2.14.0) [19]. We inferred a phylogeny with IQ-TREE
237 (version 2.1.4-beta) [48] using the *augur tree* command and inferred a time tree with
238 TreeTime (version 0.10.1) [4] using the *augur refine* command. We visualized
239 phylogenies with Auspice [49], after first converting the trees to Auspice JSON format
240 with *augur export*.
241

Definitions of genetic groups by experts or biologically-informed 242 models

We annotated phylogenetic trees with genetic groups previously identified by experts or
244 assigned by biologically-informed models. For seasonal influenza H3N2, the World
245 Health Organization assigns “clade” labels to clades in HA phylogenies that appear to
246 be genetically or phenotypically distinct from other recently circulating H3N2 samples.
247 We used the latest clade definitions for H3N2 maintained by the Nextstrain team as
248 part of their seasonal influenza surveillance efforts [50].
249

As seasonal influenza clades only account for the HA gene and lack information
250 about reassortment events, we assigned joint HA and NA genetic groups using a
251 biologically-informed model, TreeKnit [11]. TreeKnit infers ancestral reassortment
252 graphs from two gene trees, finding groups of samples for which both genes share the
253 same history. These groups, also known as maximally compatible clades (MCCs),
254

represent samples whose HA and NA genes have reassorted together. TreeKnit attempts
255 to resolve polytomies in one tree using information present in the other tree(s). Input
256 trees for TreeKnit must contain the same samples and root on the same sample. Because
257 of these TreeKnit expectations, we inferred HA and NA trees with IQ-TREE with a
258 custom argument to collapse near-zero-length branches ('-czb'). We rooted the resulting
259 trees on the same sample that we used as an alignment reference, A/Beijing/32/1992,
260 and pruned this sample prior to downstream analyses. We applied TreeKnit to the
261 rooted HA and NA trees with a gamma value of 2.0 and the '-better-MCCs' flag, as
262 previously recommended for H3N2 analyses [11]. Finally, we filtered the MCCs
263 identified by TreeKnit to retain only those with at least 10 samples and to omit the root
264 MCC that represented the most recent common ancestor in both HA and NA trees.
265

For SARS-CoV-2, we used both expert-defined "Nextstrain clades" [51–53] and
266 computationally-defined Pangolin lineages [17] provided by Nextclade as "Nextclade
267 pango" annotations. Nextstrain clade definitions represent the World Health
268 Organization's variants of concern and other phylogenetic clades that have reached
269 minimum global and regional frequencies and growth rates. Pangolin lineages represent
270 a combination of lineages assigned by a machine learning model (pangoLEARN) and
271 expert-curated lineages (<https://github.com/cov-lineages/pango-designation>) and must
272 contain at least 5 samples with an unambiguous evolutionary event. As such, Nextstrain
273 clades represent a much coarser genetic resolution than Pangolin lineages. Additionally,
274 Pangolin lineages produced by recombination receive a lineage name prefixed by an "X",
275 while Nextstrain clades do not explicitly reflect recombination events.
276

Since Pangolin lineages can represent much smaller genetic groups than are
277 practically useful, we collapsed lineages with fewer than 10 samples in our analysis into
278 their parental lineages using the pango_aliasor tool
279 (https://github.com/corneliusroemer/pango_aliasor). Specifically, we counted the
280 number of samples per lineage, sorted lineages in ascending order by count, and
281 collapsed each lineage with a count less than 10 into its parental lineage in the
282 count-sorted order. This approach allowed small lineages to aggregate with other small
283 parental lineages and meet the 10-sample threshold. We used these "collapsed
284 Nextclade pango" lineages for subsequent analyses.
285

Clustering of samples in embeddings

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To understand how well embeddings of genetic data could capture previously defined genetic groups, we applied an unsupervised clustering algorithm, HDBSCAN [54], to each embedding. HDBSCAN identifies initial clusters from high-density regions in the input space and merges these clusters hierarchically. This algorithm allowed us to avoid defining an arbitrary or biased expected number of clusters *a priori*. HDBSCAN provides parameters to tune the minimum number of samples required to seed an initial cluster (“min samples”), the minimum size for a final cluster (“min size”), and the minimum distance between initial clusters below which those clusters are hierarchically merged (“distance threshold”). We hardcoded the min samples to 5 to minimize the number of spurious initial clusters and min size to 10 to reflect our interest in genetic groups with at least 10 samples throughout our analyses. HDBSCAN calculates the distance between clusters on the Euclidean scale of each embedding. To account for embedding-specific distances, we performed a coarse grid search of distance threshold values for each virus type and embedding method.

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We performed the grid search on the early datasets for both seasonal influenza H3N2 HA and SARS-CoV-2. For each dataset and embedding method, we applied HDBSCAN clustering with a distance threshold between 0 and 7 inclusive with steps of 0.5 between values. For a given threshold, we obtained sets of samples assigned to HDBSCAN clusters from the embedding. We evaluated the accuracy of these clusters with variation of information (VI) which calculates the distance between two sets of clusters of the same samples [55]. When two sets of clusters are identical, VI equals 0. When the sets are maximally different, VI is $\log N$ where N is the total number of samples. To make VI values comparable across datasets, we normalized each value by dividing by $\log N$, following the pattern used to validate TreeKnit’s MCCs [11]. Unlike other standard metrics like accuracy, sensitivity, or specificity, VI distances do not favor methods that tend to produce more, smaller clusters. For each virus dataset and embedding method, we identified the distance threshold that minimized the normalized VI between HDBSCAN clusters and genetic groups defined by experts or biologically-informed models (“Nextstrain clade” for seasonal influenza and both “Nextstrain clade” and “collapsed Nextclade pango lineage” for SARS-CoV-2). HDBSCAN allows samples to not

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belong to a cluster and assigns these samples a numeric label of -1. We intentionally
317 included all unassigned samples in the normalized VI calculation thereby penalizing
318 cluster parameters that increased the number of unassigned samples by increasing their
319 VI values. Finally, we used these optimal distance thresholds to identify clusters in
320 out-of-sample data from the late datasets for both viruses and calculate the normalized
321 VI between those clusters and previously defined genetic groups.
322

Evaluating robustness of embedding cluster accuracy

323

The cluster accuracies we estimated for late H3N2 HA and SARS-CoV-2 datasets
324 represented a single VI measurement for a single pathogen dataset. To understand how
325 robust these accuracies were across different datasets, we generated alternate random
326 samples from both late pathogen datasets using the same geographic and temporal
327 grouping but with different numbers of sequences per group and different random seeds.
328 Specifically, we sampled 5, 10, 15, 20, or 25 sequences per group for five replicates per
329 pathogen (random seeds of 0, 1, 2, 3, and 4), embedded these sequences with each
330 method, identified clusters in embeddings, and calculated the VI distance between those
331 clusters and Nextstrain clade assignments. We plotted the distribution of the resulting
332 VI distances, to estimate the variance of these values caused by sampling bias.
333

Identification of cluster-specific mutations

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To better understand the genetic basis of embedding clusters, we identified
335 cluster-specific mutations for all HDBSCAN clusters. First, we found all mutations
336 between each sample's sequence and the reference sequence used to produce the
337 alignment, considering only A, C, G, T, and gap characters. Within each cluster, we
338 identified mutations that occurred in at least 10 samples and in at least 50% of samples
339 in the cluster. We recorded the resulting mutations per cluster in a table with columns
340 for the embedding method, the position of the mutation, the derived allele of the
341 mutation, and a list of the distinct clusters the mutation appeared in. From this table,
342 we could identify mutations that only occurred in specific clusters and mutations that
343 distinguished sets of clusters from each other.
344

Assessment of HA/NA reassortment in seasonal influenza

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populations

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To assess the ability of embedding methods to detect reassortment in seasonal influenza populations, we applied each method to either HA alignments only or concatenated alignments of HA and NA sequences from the same samples, performed HDBSCAN clustering with the optimal distance threshold for the given method, and calculated the normalized VI between the resulting clusters and TreeKnit MCCs. To minimize the effects of missing data on the PCA embeddings, we dropped all columns with N characters from the HA and HA/NA alignments prior to producing PCA embeddings. We used the original alignments to calculate distance matrices for all other methods, since distance-based methods can ignore N characters in pairwise comparisons. We compared normalized VI values for the HA-only clusters of each method to the corresponding VI values for the HA/NA clusters. Lower VI values in the HA/NA clusters than HA-only clusters indicated better clustering of samples into known reassortment groups.

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Assessment of recombination in SARS-CoV-2 populations

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To assess the ability of embedding methods to detect recombination in late SARS-CoV-2 populations (2022-2023), we calculated the Euclidean distances in low-dimensional space between the 10 known recombinant lineages and their respective parental lineages described in “Selection of natural virus population data” above. Given that we optimized each method’s parameters to maximize a linear relationship between genetic and Euclidean distance, we expected embeddings to place recombinant lineages between their parental lineages, reflecting the intermediate genetic state of the recombinants. For a recombinant lineage X and its parental lineages A and B , we calculated the average pairwise Euclidean distance, D , between samples in A and B , A and X , and B and X . We identified lineages that mapped properly as those for which $D(A, X) < D(A, B)$ and $D(B, X) < D(A, B)$. We also identified lineages for which the recombinant lineage placed closer to at least one parent than the distance between the parents. Note that we used the original uncollapsed “Nextclade pango” annotations to identify samples in each lineage, as these were the lineage names used to include recombinant samples in the

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analysis and define known relationships between recombinant and parental lineages.

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Data and software availability

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The entire workflow for our analyses was implemented with Snakemake [56]. We have
377 provided all source code, configuration files, and datasets at
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<https://github.com/blab/cartography>. Interactive phylogenetic trees and corresponding
379 embeddings for natural populations are available at <https://nextstrain.org/groups/blab/>
380 under the “cartography” keyword. The *pathogen-embed* Python package, available at
381 <https://pypi.org/project/pathogen-embed/>, provides command line utilities to calculate
382 distance matrices (*pathogen-distance*), calculate embeddings per method
383 (*pathogen-embed*), and apply hierarchical clustering to embeddings (*pathogen-cluster*).
384

Results

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Simulated populations enable tuning of embedding method parameters

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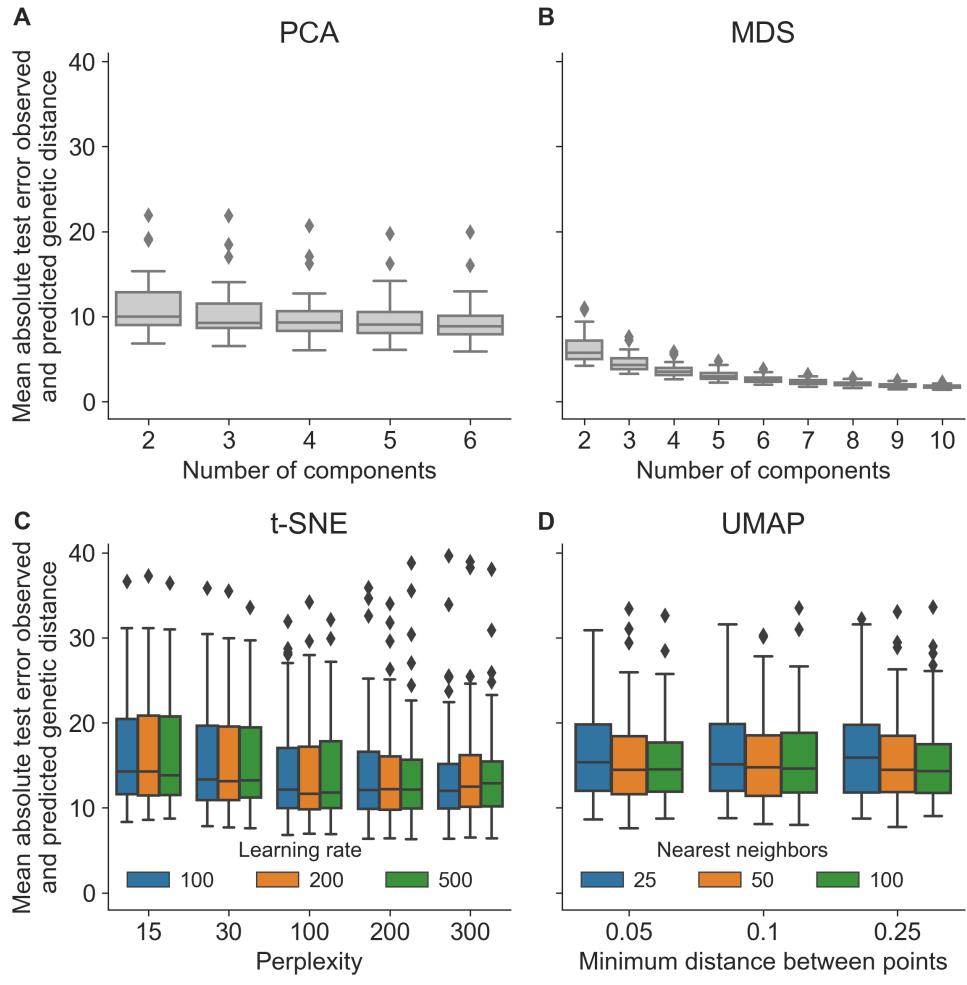
To understand how well PCA, MDS, t-SNE, and UMAP could represent genetic
388 relationships between samples of human pathogen viruses under well-defined
389 evolutionary conditions, we simulated influenza-like and coronavirus-like populations,
390 created embeddings for each population across a range of method parameters, and
391 identified optimal parameters as those that maximized a linear relationship between
392 genetic distance and Euclidean distance in low-dimensional space (see Methods).
393 Specifically, we selected parameters that minimized the median of the mean absolute
394 error (MAE) between observed pairwise genetic distances of simulated genomes and
395 predicted genetic distances for those genomes based on their Euclidean distances in each
396 embedding. For methods like PCA and MDS where increasing the number of
397 components available to the embedding could lead to overfitting, we selected the
398 maximum number of components beyond which the median MAE did not decrease by
399 more than 1 nucleotide.
400

For influenza-like populations, the optimal parameters were 2 components for PCA,
401 3 components for MDS, perplexity of 100 and learning rate of 200 for t-SNE, and
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nearest neighbors of 100 and minimum distance of 0.25 for UMAP. As expected, 403
increasing the number of components for PCA and MDS gradually decreased the 404
median MAEs of their embeddings (S1 Fig A and B). However, beyond 2 and 3 405
components, respectively, the reduction in error did not exceed 1 nucleotide. This result 406
suggests that there were diminishing returns for the increased complexity of additional 407
components. Both t-SNE and UMAP embeddings produced a wide range of errors (the 408
majority between 10 and 20 average mismatches) across all parameter values (S1 Fig C 409
and D). Embeddings from t-SNE appeared robust to variation in parameters, with a 410
slight improvement in median MAE associated with perplexity of 100 and little benefit 411
to any of the learning rate values (S1 Fig C). [Based on these results, we should consider 412
setting the learning rate to the default for scikit-learn which scales the rate with the 413
input sample size.] Similarly, UMAP embeddings were robust across the range of tested 414
parameters, with the greatest benefit coming from setting the nearest neighbors greater 415
than 25 and no benefit from changing the minimum distance between points (S1 Fig D). 416

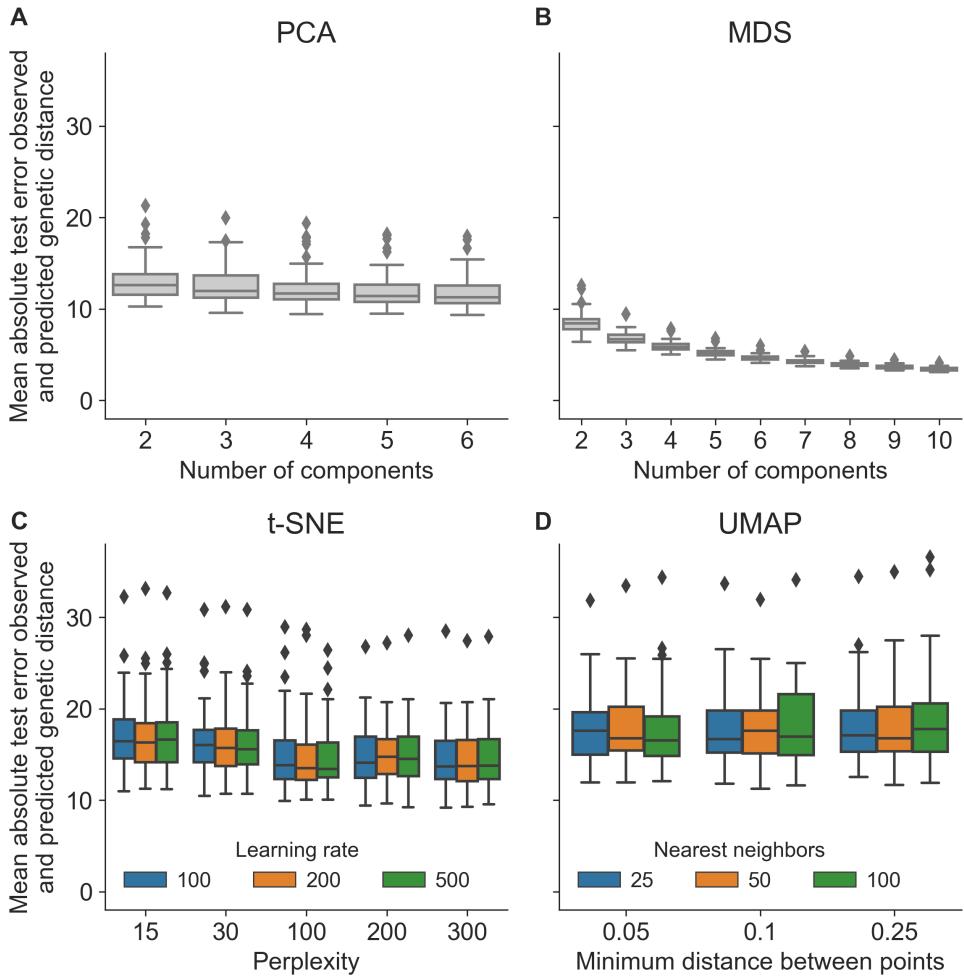
The optimal parameters for coronavirus-like populations were nearly the same as 417
those for the influenza-like populations. The optimal parameters were 2 components for 418
PCA, 3 for MDS, perplexity of 100 and learning rate of 500 for t-SNE, and nearest 419
neighbors of 100 and minimum distance of 0.05 for UMAP. As with influenza-like 420
populations, both PCA and MDS showed diminishing benefits of increasing the number 421
of components (S2 Fig A and B). Similarly, we observed little improvement in MAEs 422
from varying t-SNE and UMAP parameters (S2 Fig C and D). The most noticeable 423
improvement came from setting t-SNE's perplexity to 100 (S2 Fig C). These results 424
indicate the limits of t-SNE and UMAP to represent global genetic structure, at least 425
across the parameter regimes considered here. [An obvious follow-up question would be 426
whether we can improve MAEs for these methods by increasing components available to 427
them, too.] 428

We inspected representative embeddings based on the optimal parameters above for 429
the first four years of influenza- and coronavirus-like populations. Simulated sequences 430
collected from the same time period tended to map closer in embedding space, 431
indicating the maintenance of “local” genetic structure in the embeddings (Fig. 1). 432
Most embeddings also represented some form of global structure, with later generations 433
mapping closer to intermediate generations than earlier generations. MDS maintained 434



S1 Fig. Distribution of mean absolute errors (MAE) between observed and predicted pairwise genetic distances per embedding method parameters for simulated influenza-like populations.

the greatest continuity between generations for both population types (S3 Fig). In contrast, PCA, t-SNE, and UMAP all demonstrated tighter clusters of samples separated by potentially arbitrary space. The UMAP embedding for the coronavirus-like samples was most extreme in this respect, with a tight cluster of early samples placing far away from all other samples in the embedding including those from nearby generations. These qualitative results matched our expectations based on how well each method maximized a linear relationship between genetic and Euclidean distances during parameter optimization (S1 Fig and S2 Fig).



S2 Fig. Distribution of mean absolute errors (MAE) between observed and predicted pairwise genetic distances per embedding method parameters for simulated coronavirus-like populations.

Embedding clusters recapitulate phylogenetic clades for seasonal influenza H3N2

Seasonal influenza H3N2's hemagglutinin (HA) sequences provide an ideal positive control to test embedding methods and clustering in low-dimensional space. H3N2's HA protein evolves rapidly, accumulating amino acid mutations that enable escape from adaptive immunity in human populations [57]. These mutations produce distinct phylogenetic clades that represent potentially different antigenic phenotypes. The World Health Organization (WHO) Global Influenza Surveillance and Response System (GISRS) regularly sequences genomes of circulating influenza lineages [58] and submits

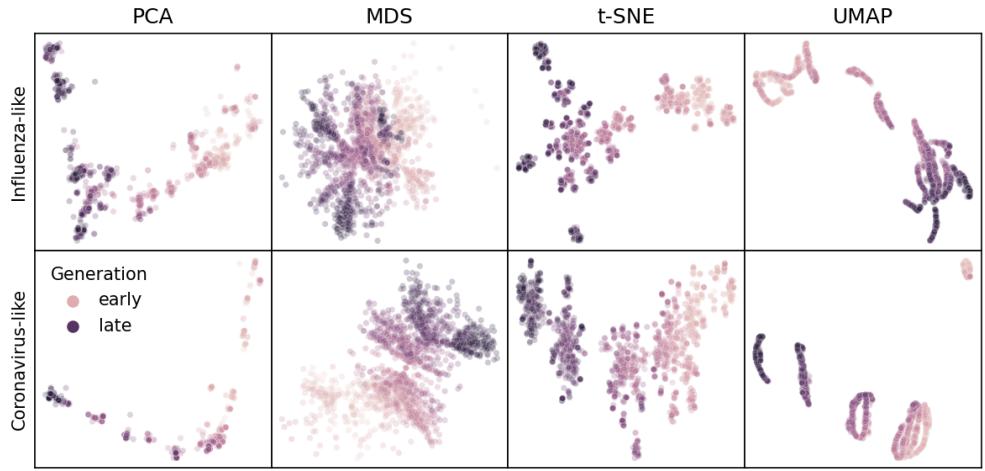
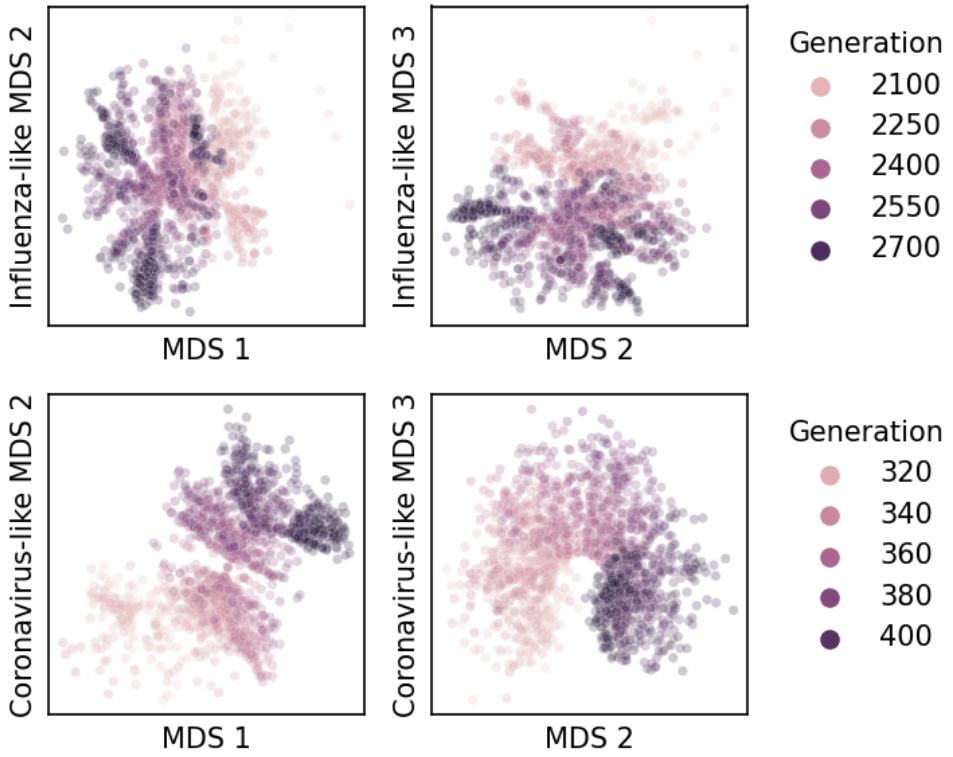


Fig 1. Representative embeddings for simulated populations using optimal parameters per pathogen (rows) and embedding method (columns). Each panel shows the embedding for sequences from the first four years of a single replicate population for the corresponding pathogen type. Each point represents a simulated viral sequence colored by its generation with darker values representing later generations. The MDS embedding shows the first two of three total components. S3 Fig shows the full MDS embedding for all components.

these sequences to public INSDC databases like NCBI's GenBank [44]. These factors, coupled with HA's relatively short gene size of 1,701 nucleotides, facilitate real-time genomic epidemiology of H3N2 [50] and rapid analysis by the embedding methods we wanted to evaluate.

We first applied each embedding method to the early H3N2 HA sequences collected from 2016 through 2018, colored samples by previously defined phylogenetic clades, and inspected the placement of these samples in the embeddings and corresponding phylogeny. All four embedding methods qualitatively recapitulated clade-level groupings observed in the phylogeny (Fig 2 and S4 Fig). Samples from the same clade generally grouped tightly together. Most embedding methods also clearly delineated larger phylogenetic clades, placing clades A1, A2, A3, A4, and 3c3.A into separate locations in the embeddings. One exception to this pattern was the PCA embedding which grouped samples from clades A3 and A4 into the same space. Despite maintaining local and broader global structure, not all embeddings captured intermediate genetic structure. For example, clade A1b descended from clade A1 and diversified into the smaller subclades A1b/131K, A1b/135K, and A1b/135N. All methods placed A1b far from its ancestor A1, but all methods also placed descendants of A1b into tight clusters together.



S3 Fig. Representative MDS embeddings for simulated populations using optimal parameters per pathogen (rows) and showing all three components.

The t-SNE embedding created separate clusters of the three descendant clades, but these clusters all placed so close together in the embedding space that, without previously defined clade labels, we would have visually grouped these samples into a single cluster. These results qualitatively replicate the patterns we observed in embeddings for simulated influenza-like populations (Fig 1).

To quantify the apparent maintenance of local and global structure by all four embedding methods, we calculated the relationship between pairwise genetic and Euclidean distance of samples in each embedding. All four methods maintained a linear relationship between genetic and Euclidean distances for samples that differed by no more than ≈ 10 nucleotides (Fig 3). However, only MDS consistently maintained that linearity as genetic distance increased (Pearson's $R^2 = 0.94$). Values of Euclidean distances in MDS corresponded nearly perfectly with values of genetic distances. In contrast, we observed a nonlinear relationship for samples with more genetic differences in PCA (Pearson's $R^2 = 0.67$), t-SNE (Pearson's $R^2 = 0.37$), and UMAP (Pearson's

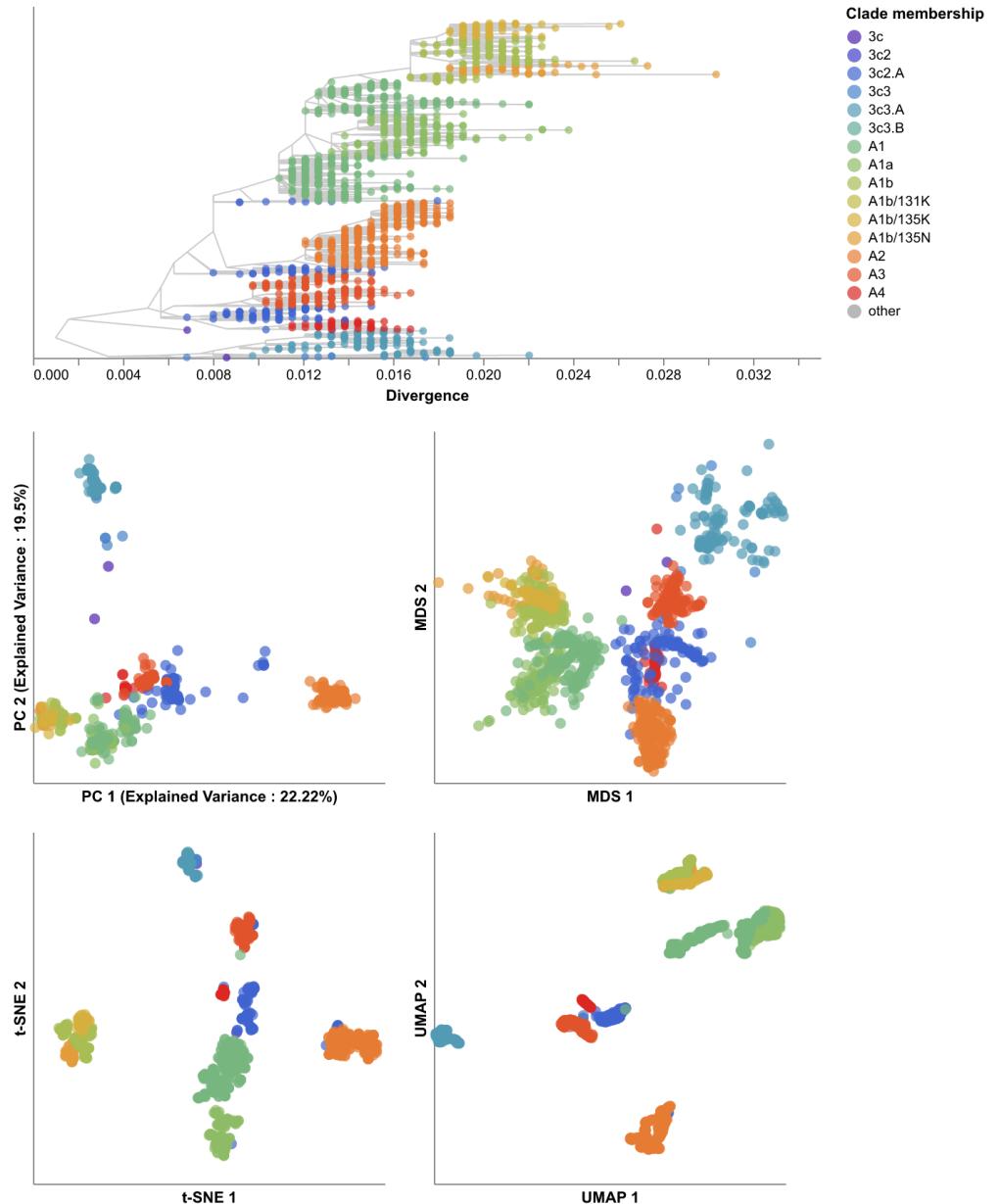
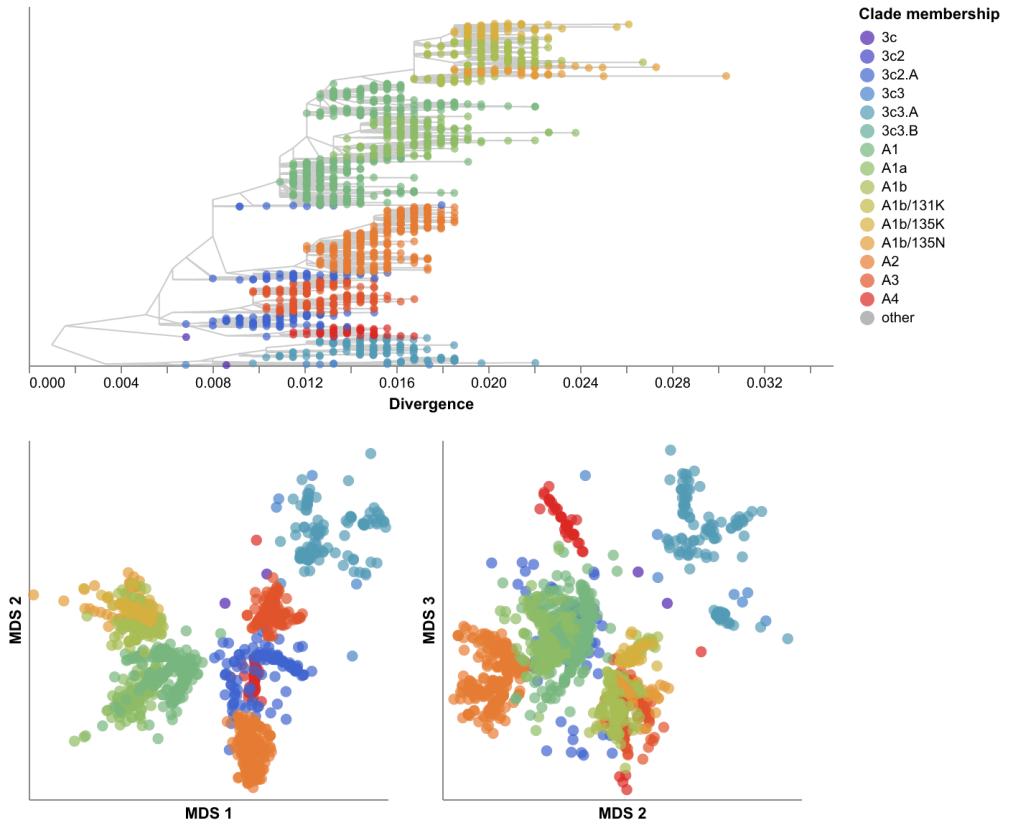


Fig 2. Phylogeny of early (2016–2018) influenza H3N2 HA sequences plotted by nucleotide substitutions per site on the x-axis (top) and low-dimensional embeddings of the same sequences by PCA (middle left), MDS (middle right), t-SNE (bottom left), and UMAP (bottom right). Tips in the tree and embeddings are colored by their Nextstrain clade assignment.

$R^2 = 0.48$) embeddings. Although the most genetically distant samples mapped far from each other in all of these embeddings, samples with intermediate distances could map much closer or farther than expected by a linear model. In t-SNE and UMAP embeddings, some pairs of samples with intermediate distances of 30–40 nucleotides



S4 Fig. MDS embeddings for early (2016–2018) influenza H3N2 HA sequences showing all three components.

mapped farther apart than pairs of samples with much greater genetic distances. 487

Next, we measured how well clusters of H3N2 HA samples in each embedding 488 corresponded to previously defined genetic groups. For each embedding, we assigned 489 cluster labels to each sample with the hierarchical clustering algorithm, HDBSCAN, 490 which does not require an expected number of clusters as input [54]. HDBSCAN does 491 require definition of a minimum distance that its initial clusters must be from each 492 other to avoid being merged into the same cluster. This distance corresponds to the 493 Euclidean distance between clusters in embedding space which varies by method (Fig 3). 494 To find the optimal minimum distance for HDBSCAN clusters of H3N2 HA data, we 495 assigned clusters to each embedding for a range of distance values (0-7) with a step size 496 of 0.5 and calculated the accuracy of clusters at each distance value compared to the 497 Nextstrain clade assignments shown in Fig 2. We selected the minimum distance value 498 per method that minimized the difference between HDBSCAN clusters and clade 499 assignments as measured by the normalized variation of information (VI) metric [55] 500

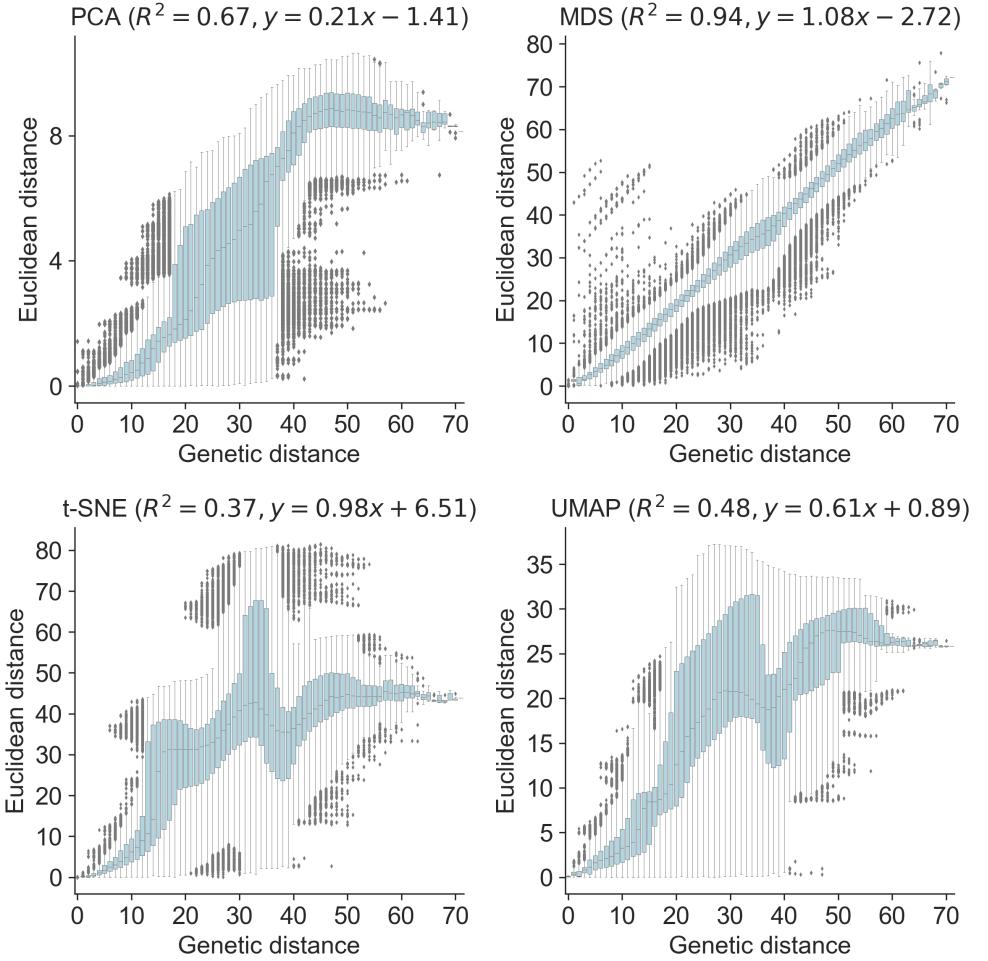


Fig 3. Relationship between pairwise genetic and Euclidean distances in embeddings of early (2016–2018) influenza H3N2 HA sequences by PCA (upper left), MDS (upper right), t-SNE (lower left), and UMAP (lower right). Each boxplot represents the distribution of pairwise Euclidean distances at a given genetic distance.

(see Methods). The optimal minimum distances were 0.5 for PCA, 3.5 for MDS, 2.0 for t-SNE, and 1.0 for UMAP (Table 1). Since Euclidean distances for MDS correspond directly to genetic distances, these results show that clusters must be at least 3.5 nucleotides apart to be considered distinct. 501
502
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As expected, the clusters for each method generally corresponded to larger phylogenetic clades (Fig 4). Clusters from t-SNE most accurately captured expert clade assignments (normalized VI=0.04) with nine clusters. These clusters captured broader phylogenetic clades (A1, A1b, A2, A3, A4, 3c2.A, and 3c3.A) but failed to distinguish between A1b and its descendants. Clusters from UMAP performed nearly as well 505
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508
509

Table 1. Accuracy of embedding methods per human pathogenic virus sorted by normalized variation of information (VI) distance. Smaller VI values indicate smaller distances between HDBSCAN clusters and known genetic groups with 0 indicating identical clusters and 1 indicating maximally different clusters. Threshold refers to the distance threshold used to assign clusters with HDBSCAN.

Pathogen	Method	VI	Threshold
Influenza H3N2	t-SNE	0.04	2.0
	UMAP	0.08	1.0
	MDS	0.10	3.5
	PCA	0.19	0.5
SARS-CoV-2 (Nextstrain clade)	t-SNE	0.07	1.0
	MDS	0.15	0.0
	UMAP	0.16	0.5
	PCA	0.36	4.5
SARS-CoV-2 (Nextclade pango)	t-SNE	0.12	1.0
	MDS	0.23	0.0
	UMAP	0.25	0.5
	PCA	0.42	4.5

(normalized VI=0.08) with six clusters. These clusters captured broader clades, but 510
they failed to distinguish among A1 and A1a, A1b and its subclades, and 3c2.A and A4. 511
The nine MDS clusters were more than twice as far from expert clades as t-SNE clusters 512
(normalized VI=0.10), but this difference in accuracy appeared to be driven primarily 513
by the cost of more samples that HDBSCAN failed to assign to clusters in the MDS 514
embedding. MDS clusters captured most of the larger clades (A1, A2, A3, A4, 3c2.A, 515
and 3c3.A), but they also collected A1 and its descendants into two large clusters. The 516
PCA embedding produced the lowest accuracy (normalized VI=0.19) and fewest 517
clusters (N=3). PCA's three clusters corresponded to some of the most distantly-related 518
and ancestral clades (3c2.A, 3c3.A, and A2). We identified 30 cluster-specific mutations 519
for all three PCA clusters, 34 for seven of the nine MDS clusters, 32 for six of nine 520
t-SNE clusters, and 25 for four of the six UMAP clusters (S1 Table). We also found 521
that pairwise genetic distances between sequences in the same MDS, t-SNE, or UMAP 522
clusters matched the genetic distances between sequences in the same Nextstrain clades 523
(S5 Fig). These results indicate that nonlinear embeddings of t-SNE and UMAP could 524
be better-suited for clustering and classification than linear embeddings from PCA and 525
MDS. 526

To understand whether these embedding methods and optimal cluster parameters 527
could effectively cluster previously unseen sequences, we applied each method to the 528

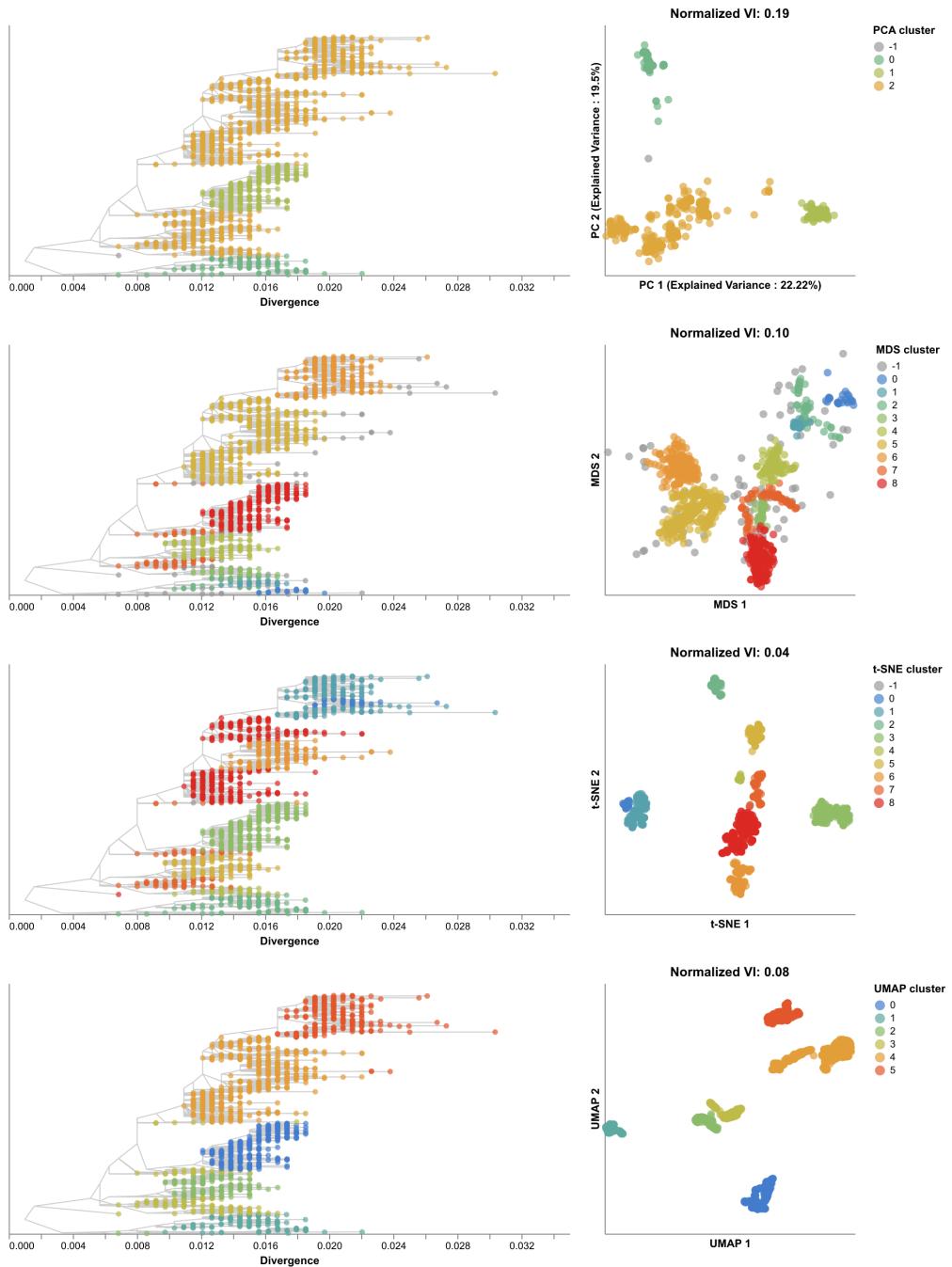
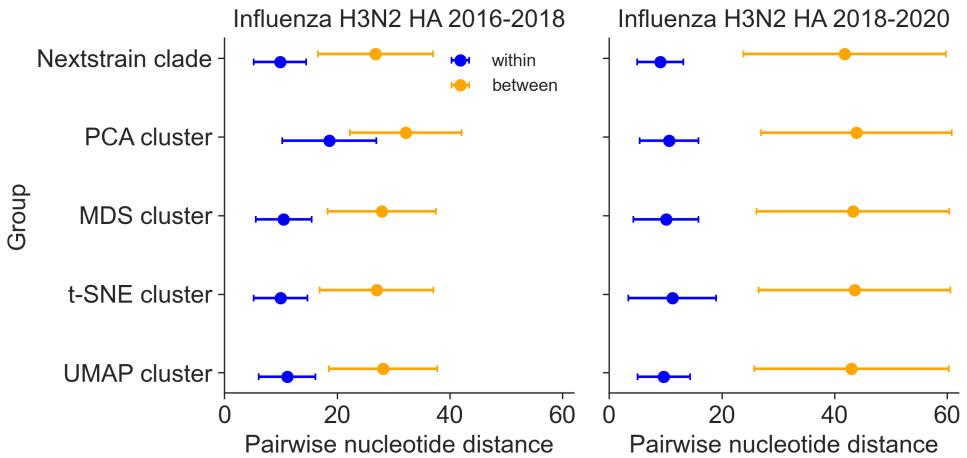


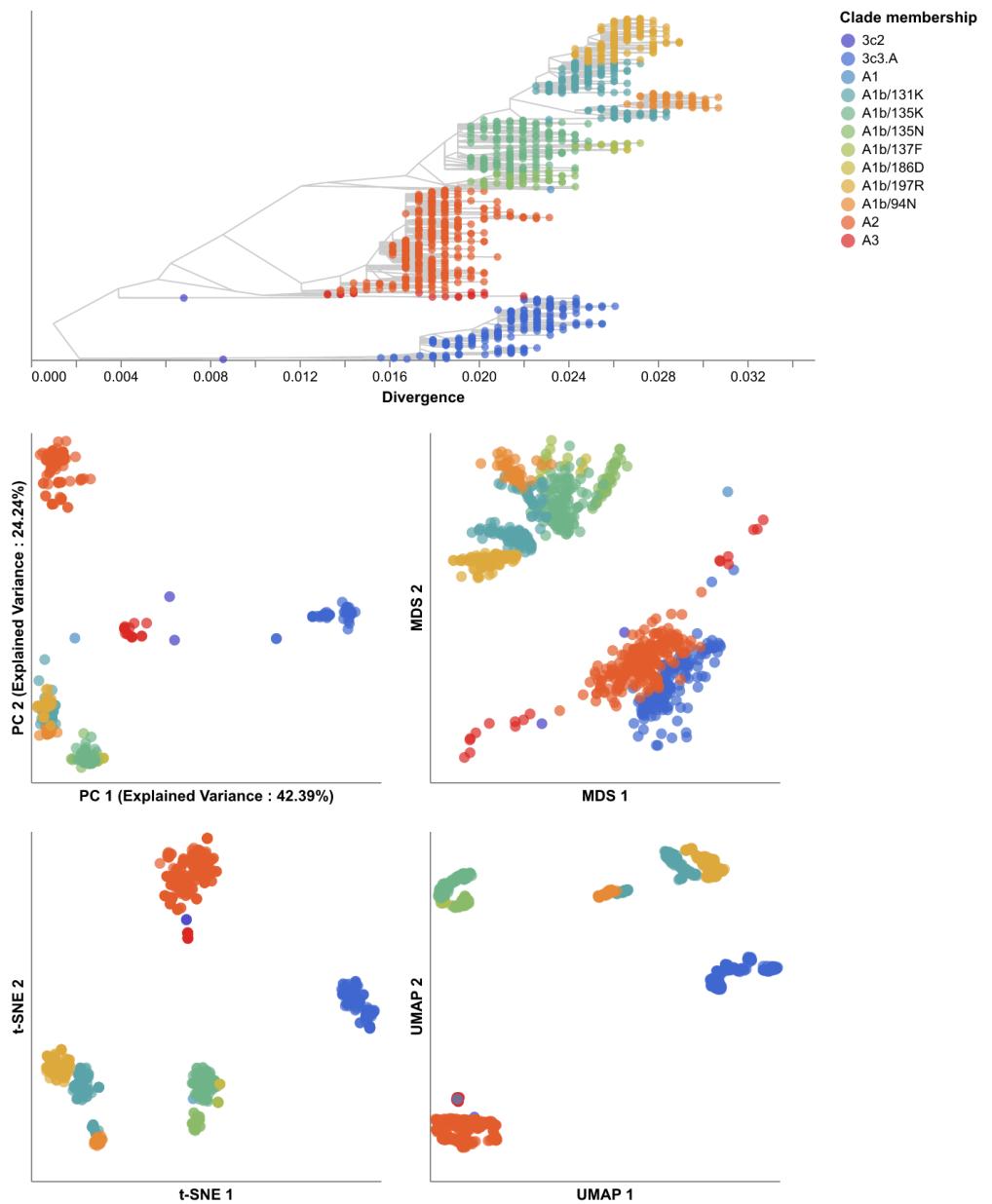
Fig 4. Phylogenetic trees (left) and embeddings (right) of early (2016–2018) influenza H3N2 HA sequences colored by HDBSCAN cluster. Normalized VI values per embedding reflect the distance between clusters and known genetic groups (Nextstrain clades).

late H3N2 HA dataset (2018–2020), clustered sequences in the embedding space with HDBSCAN using the optimal minimum distance threshold from the early dataset, and calculated the accuracy of the cluster assignments based on previously defined clades.



S5 Fig. Pairwise nucleotide distances for early (2016–2018) and late (2018–2020) influenza H3N2 HA sequences within and between genetic groups defined by Nextstrain clades and clusters from PCA, MDS, t-SNE, and UMAP embeddings.

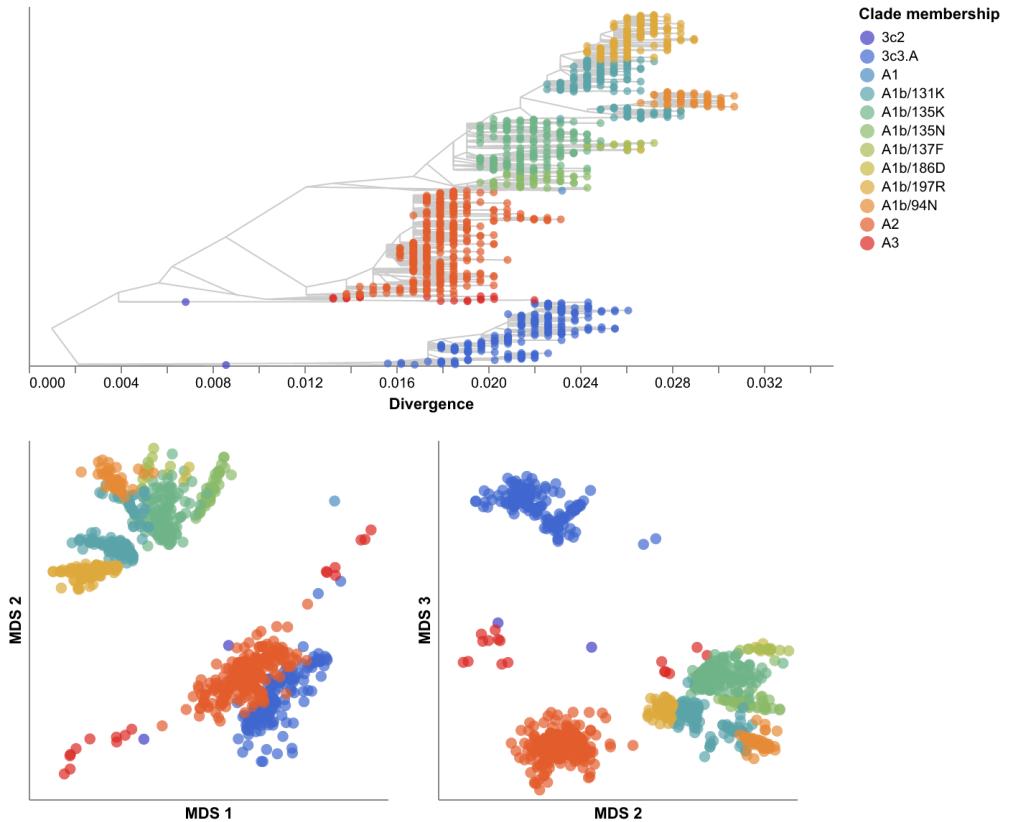
Unlike the early H3N2 HA dataset, the late dataset contained fewer clades (S6 Fig) and a greater genetic distance between samples in clades (S5 Fig). Clusters from all four methods generally captured phylogenetic clades (Fig. 5 and S6 Fig). The MDS clusters most accurately captured expert clades (normalized VI=0.07) with six clusters corresponding to the largest clades (Fig. 5 and S7 Fig). MDS split A3 samples into two widely separated groups in its Euclidean space, indicating substantial within-clade genetic differences. On inspection of this clade, we found recurrent HA1 substitutions of 135K, 142G, and 193S in multiple subclades that MDS could not effectively represent. Clusters from t-SNE, UMAP, and PCA followed closely in accuracy (normalized VI=0.08, 0.08, and 0.09) with 5, 7, and 6 clusters, respectively. We identified 25 cluster-specific mutations for four of the six PCA clusters, 51 for all six MDS clusters, 53 for all five t-SNE clusters, and 30 for five of the seven UMAP clusters (S1 Table). Pairwise genetic distances within clusters generally matched the diversity within Nextstrain clades (S5 Fig). Cluster accuracies remained robust to sampling density and composition (S8 Fig). These results show that all four methods can produce well-supported clusters that accurately capture known genetic groups when applied to previously unseen H3N2 HA samples.



S6 Fig. Phylogeny of late (2018–2020) influenza H3N2 HA sequences plotted by nucleotide substitutions per site on the x-axis (top) and low-dimensional embeddings of the same sequences by PCA (middle left), MDS (middle right), t-SNE (bottom left), and UMAP (bottom right). Tips in the tree and embeddings are colored by their Nextstrain clade assignment.

Joint embeddings of hemagglutinin and neuraminidase genomes identify seasonal influenza virus H3N2 reassortment events

Given that clusters from embedding methods could recapitulate expert-defined clades, we measured how well the same methods could capture reassortment events between



S7 Fig. MDS embeddings for late (2018–2020) influenza H3N2 HA sequences showing all three components.

multiple gene segments as detected by biologically-informed computational models. 553
Evolution of HA and NA surface proteins contributes to the ability of influenza viruses 554
to escape existing immunity [57] and HA and NA genes frequently reassort [5, 6, 59]. 555
Therefore, we focused our reassortment analysis on HA and NA sequences, sampling 556
1,607 viruses collected between January 2016 and January 2018 with sequences for both 557
genes. We aligned these sequences to a common reference (A/Beijing/32/1992), inferred 558
HA and NA phylogenies, and applied TreeKnit to both trees to identify maximally 559
compatible clades (MCCs) that represent reassortment events [11]. Of the 191 560
reassortment events identified by TreeKnit, 15 (8%) contained at least 10 samples 561
representing 1,062 samples (66%). 562

We created PCA, MDS, t-SNE, and UMAP embeddings from the HA alignments 563
and from merged HA and NA alignments. We identified clusters in both HA-only and 564
HA/NA embeddings and calculated the VI distance between these clusters and the 565
MCCs identified by TreeKnit. We expected that clusters from HA-only embeddings 566

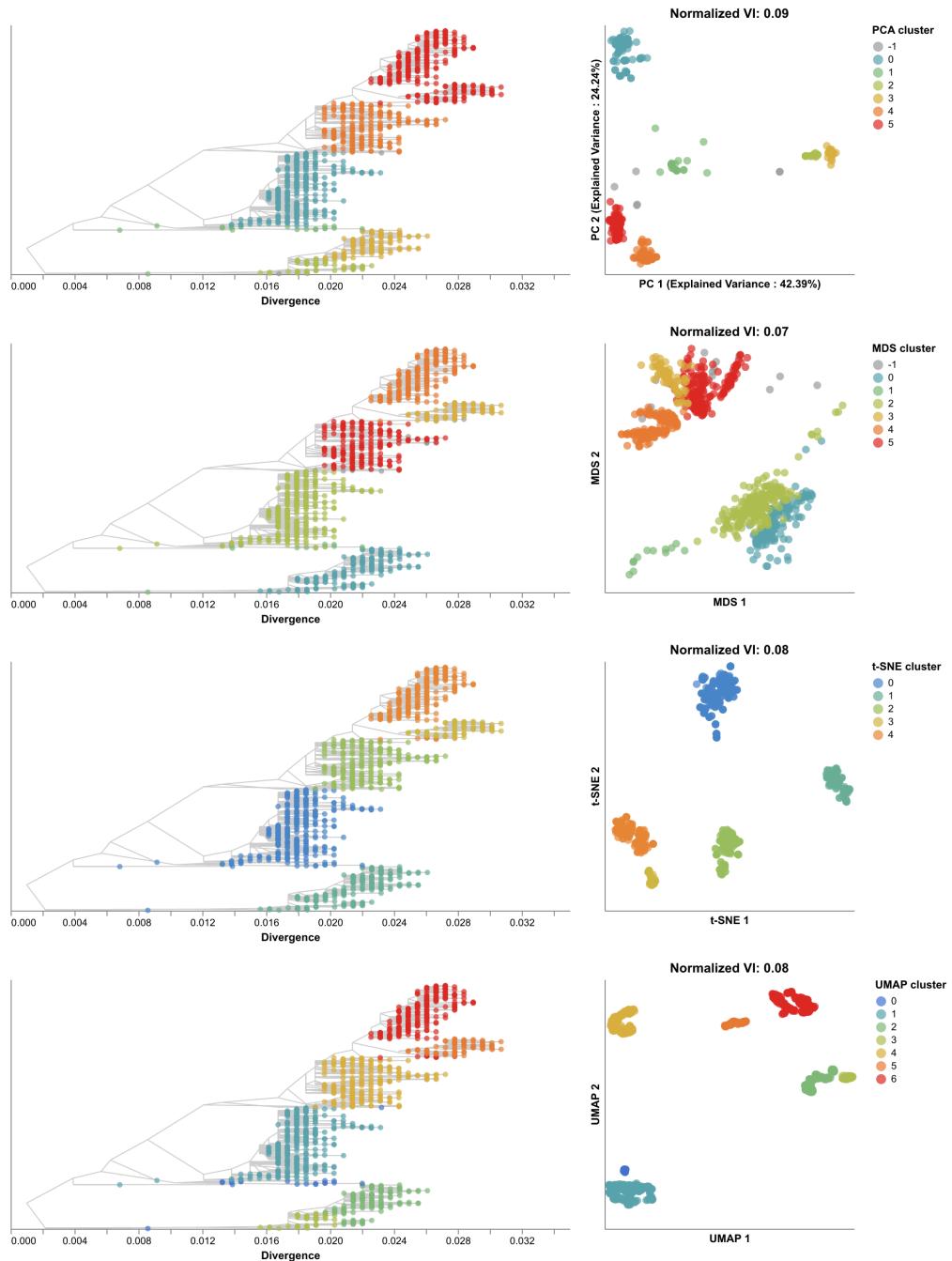
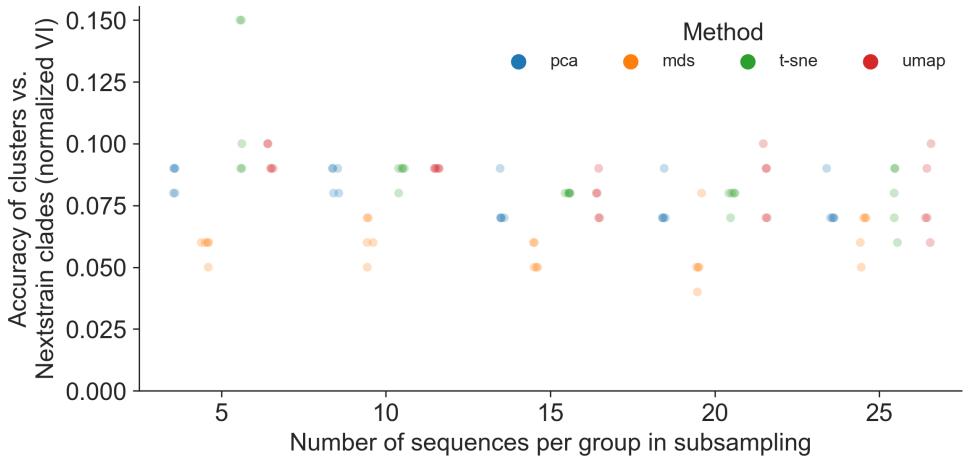


Fig 5. Phylogenetic trees (left) and embeddings (right) of late (2018–2020) H3N2 HA sequences colored by HDBSCAN cluster. Normalized VI values per embedding reflect the distance between clusters and known genetic groups (Nextstrain clades).

could only reflect reassortment events when the HA clade involved in reassortment happened to carry characteristic nucleotide mutations. We expected that the VI distances for clusters from HA/NA embeddings would improve on the baseline distances



S8 Fig. Replication of cluster accuracy per embedding method for late (2018–2020) influenza H3N2 HA sequences across different sequences per group sampled from the original dataset and five replicates per sampling density.

calculated with the HA-only clusters.

All embedding methods produced more accurate clusters from the HA/NA alignments than the HA-only alignments (Fig. 6). HA/NA clusters from MDS reduced the distance to known reassortment events by 69% from a normalized VI value of 0.16 with HA only to 0.05. Adding NA to HA only modestly improved PCA, t-SNE, UMAP clusters, reducing distances by 0.05, 0.04, and 0.03, respectively. Embeddings with both genes also produced more clusters than the HA-only embeddings with one additional cluster in PCA (S10 Fig), 11 in MDS (S11 Fig), five in t-SNE (S12 Fig), and one in UMAP (S13 Fig). With the exception of PCA, all embeddings of HA/NA alignments produced distinct clusters for the known reassortment event within clade A2 [59] as represented by MCCs 14 and 11 (S9 Fig). Other larger events like those represented by MCCs 9 and 13 mapped far apart in all HA/NA embeddings except PCA. Smaller events like the reassortment represented by MCCs 10 and 6 only received separate clusters in the MDS embedding of HA and NA (S11 Fig). We noted that some of the additional clusters in HA/NA embeddings likely also reflected genetic diversity in NA that was independent of reassortment between HA and NA. These results suggest that a single embedding of multiple gene segments could identify biologically meaningful clusters within and between all genes.

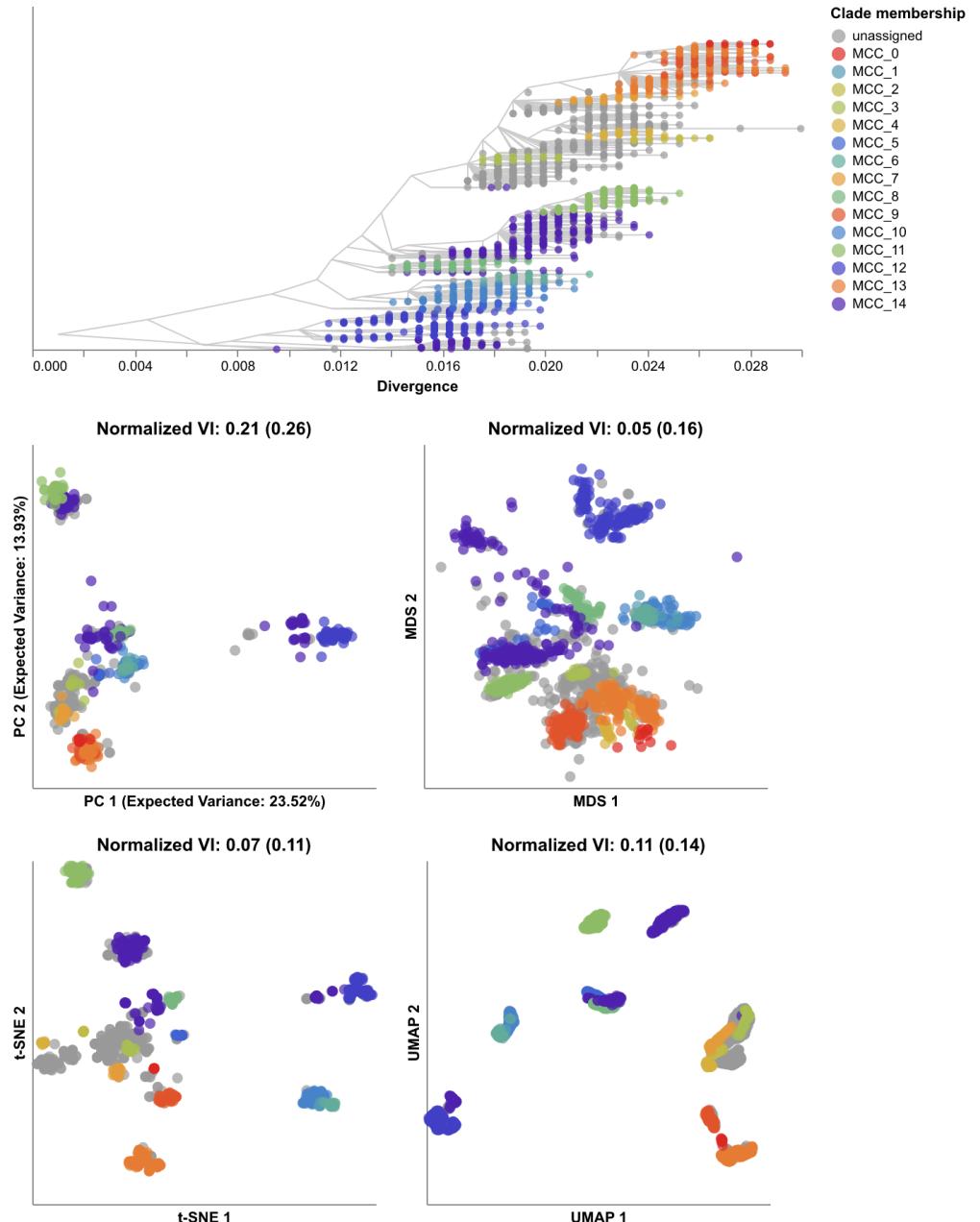
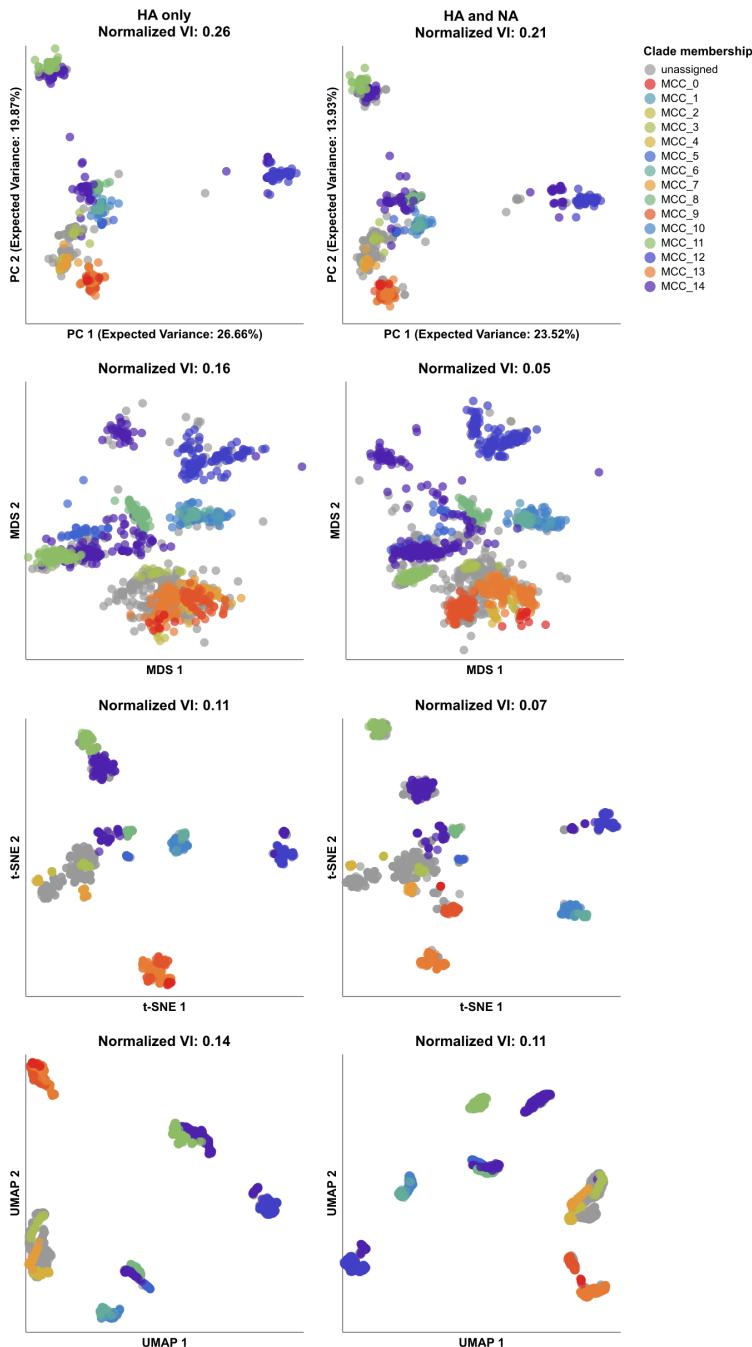


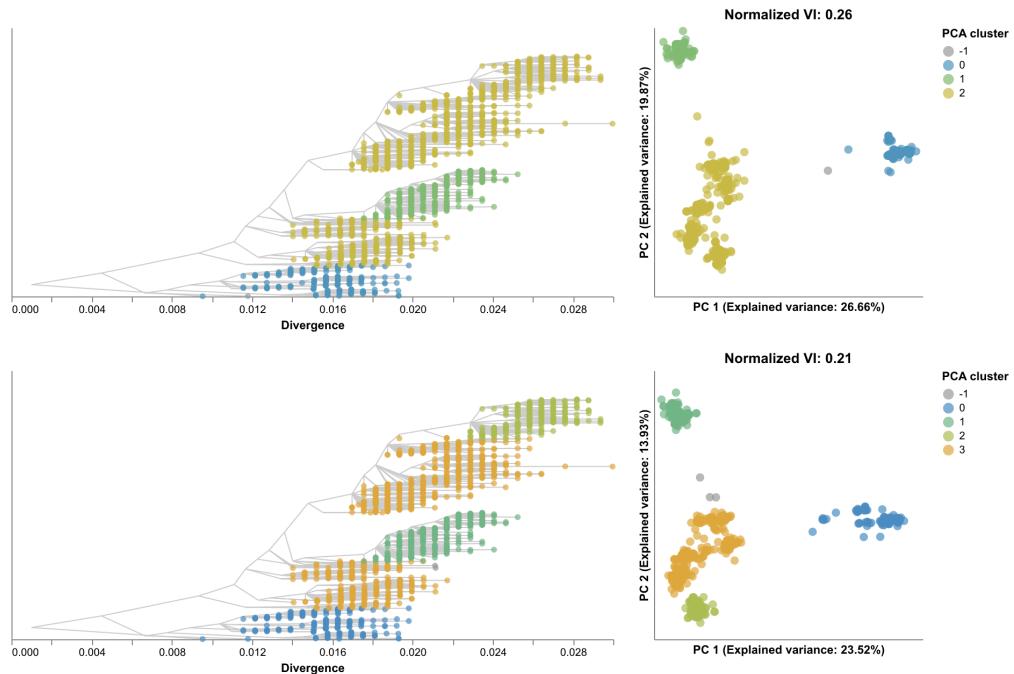
Fig 6. Phylogeny of early (2016–2018) influenza H3N2 HA sequences plotted by nucleotide substitutions per site on the x-axis (top) and low-dimensional embeddings of the same HA sequences concatenated with matching NA sequences by PCA (middle left), MDS (middle right), t-SNE (bottom left), and UMAP (bottom right). Tips in the tree and embeddings are colored by their TreeKnit Maximally Compatible Clades (MCCs) label which represents putative HA/NA reassortment groups. The first normalized VI values per embedding reflect the distance between HA/NA clusters and known genetic groups (MCCs). VI values in parentheses reflect the distance between HA-only clusters and known genetic groups.



S9 Fig. Embeddings influenza H3N2 HA-only (left) and combined HA/NA (right) showing the effects of additional NA genetic information on the placement of reassortment events detected by TreeKnit (MCCs).

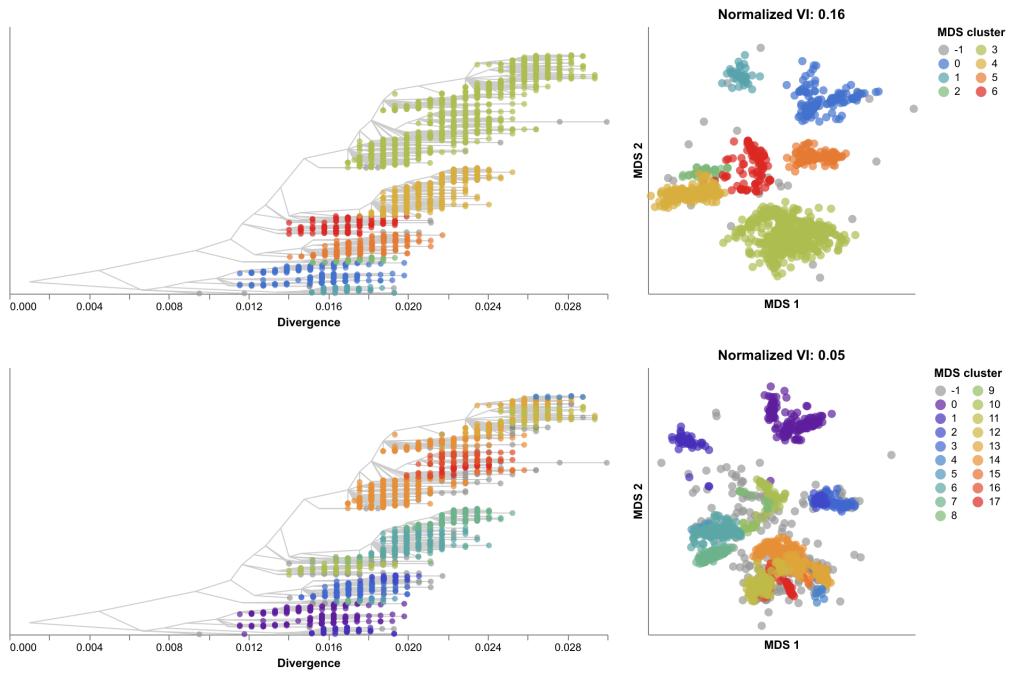
SARS-CoV-2 clusters recapitulate broad genetic groups corresponding to Nextstrain clades

SARS-CoV-2 poses a greater challenge to embedding methods than seasonal influenza, with an unsegmented genome an order of magnitude longer than influenza's HA or



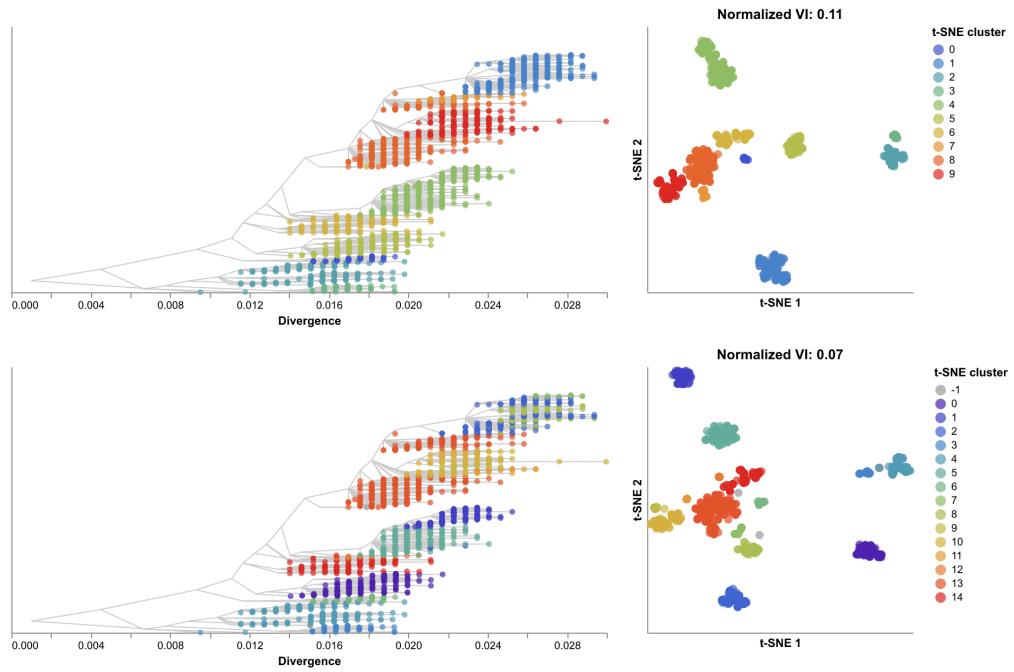
S10 Fig. PCA embeddings for influenza H3N2 HA sequences only (top row) and HA/NA sequences combined (bottom row) showing the HA trees colored by clusters identified in each embedding (left) and the corresponding embeddings colored by cluster (right).

NA [60], a mutation rate in the spike surface protein subunit S1 that is four times higher than influenza H3N2's HA rate [61], and increasingly common recombination [62, 63]. However, multiple expert- and model-based clade definitions exist for SARS-CoV-2, enabling comparison between clusters from embeddings and known genetic groups. These definitions span from broad genetic groups named by the WHO as “variants of concern” (e.g., “Alpha”, “Beta”, etc.) [64] or systematically defined by the Nextstrain team [51–53] to smaller, emerging genetic clusters defined by Pangolin [17]. As with seasonal influenza, we defined an early SARS-CoV-2 dataset spanning from January 2020 to January 2022, embedded genomes with the same four methods, and identified HDBSCAN clustering parameters that minimized the VI distance between embedding clusters and previously defined genetic groups as defined by Nextstrain clades and collapsed “Nextclade pango” lineages (see Methods). Using these optimal cluster parameters, we produced clusters from embeddings of a late SARS-CoV-2 dataset spanning from January 2022 to November 2023 and calculated the VI distance between those clusters and known genetic groups.



S11 Fig. MDS embeddings for influenza H3N2 HA sequences only (top row) and HA/NA sequences combined (bottom row) showing the HA trees colored by clusters identified in each embedding (left) and the corresponding embeddings colored by cluster (right).

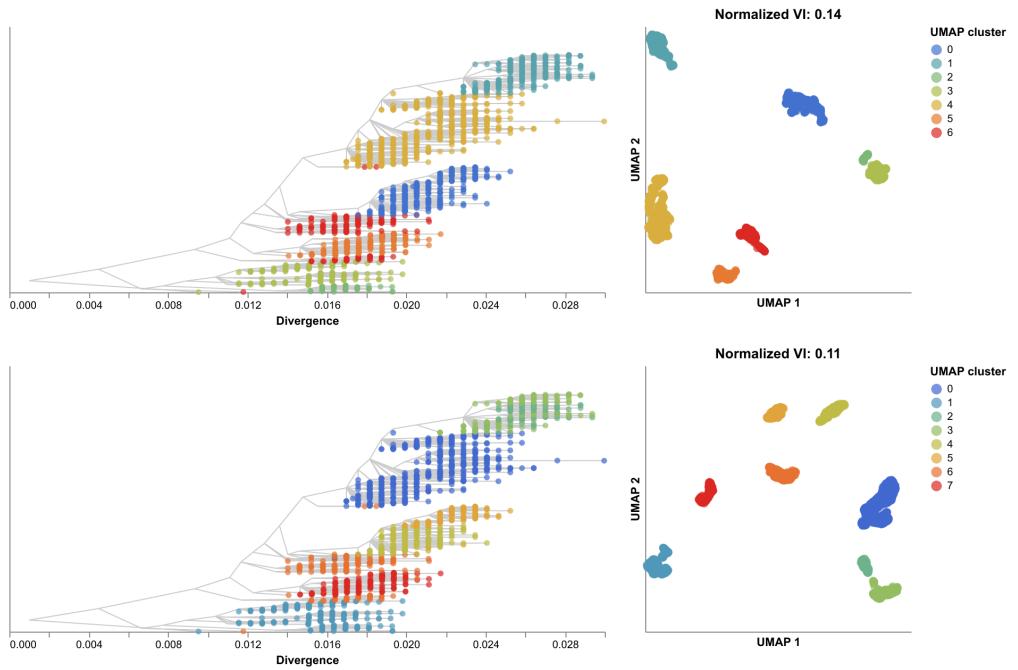
The early SARS-CoV-2 dataset represented 24 Nextstrain clades and 35 collapsed Nextclade pango lineages. With the exception of PCA, all other embedding methods placed samples from the same Nextstrain clades closer together and closely related Nextstrain clades near each other (Fig. 7). For example, the most genetically distinct clades like 21J (Delta) and 21K (Omicron) placed farthest from other clades, while all Delta clades (21A, 21I, and 21J) placed close together (Fig. 7, S14 Fig). As we saw with embeddings of H3N2 HA sequences, MDS placed related clades closer together on a continuous scale, while t-SNE and UMAP produced more clearly separate groups of samples. Unlike the H3N2 HA analysis, the PCA embedding of SARS-CoV-2 sequences failed to create any genetically meaningful clusters. We suspected that PCA components reflected variation in missing ("N") or gap ("–") characters that we represented with a separate character state than the standard nucleotide characters of A, C, G, and T. We plotted the PC1 value of each sample against the number of missing bases in its alignment and confirmed that missing data explained a substantial proportion of variation in PC1 but not all (S15 Fig, Pearson's $R^2 = 0.304$). When we compared embedding clusters to Nextclade pango lineages, we did not observe the same



S12 Fig. t-SNE embeddings for influenza H3N2 HA sequences only (top row) and HA/NA sequences combined (bottom row) showing the HA trees colored by clusters identified in each embedding (left) and the corresponding embeddings colored by cluster (right).

clear grouping as we did with Nextstrain clades. For example, the Nextstrain clade 21J (Delta) contained 11 pango lineages that all appeared to map into the same overlapping space in MDS, t-SNE, and UMAP embeddings (S16 Fig). These results suggest that distance-based embedding methods can recapitulate broader genetic groups of SARS-CoV-2, but that these methods lack the resolution of finer groups defined by Pangolin.

We quantified the maintenance of local and global structure in early SARS-CoV-2 embeddings by fitting a linear model between pairwise genetic and Euclidean distances of samples. As we expected from the qualitative evaluation of the PCA embedding above, we found no relationship between Euclidean distance in PCA and genetic distance in alignments (Fig. 8). In contrast, the MDS embedding produced a strong linear mapping across the range of observed genetic distances (Pearson's $R^2 = 0.92$). Both t-SNE and UMAP maintained intermediate degrees of linearity (Pearson's $R^2 = 0.63$ and $R^2 = 0.55$, respectively). These embeddings placed the most genetically similar samples close together and the most genetically distinct farther apart. However, these embeddings did not consistently place pairs of samples with intermediate genetic



S13 Fig. UMAP embeddings for influenza H3N2 HA sequences only (top row) and HA/NA sequences combined (bottom row) showing the HA trees colored by clusters identified in each embedding (left) and the corresponding embeddings colored by cluster (right).

distances at an intermediate distance in Euclidean space. The linear relationship for genetically similar samples in t-SNE remained consistent up to a genetic distance of approximately 30 nucleotides. The corresponding relationship for UMAP only remained consistent up to a genetic distance of approximately 10 nucleotides.

We identified clusters in embeddings from early SARS-CoV-2 data using cluster parameters that minimized the normalized VI distance between clusters and known genetic groups. Since Nextstrain clades and Nextclade pango lineages represented different resolutions of genetic diversity, we identified separate optimal parameters for clusters compared to each of these known genetic groups. When comparing clusters to Nextstrain clades, the t-SNE embedding produced the most accurate clusters with a normalized VI of 0.07 (N=19 clusters, minimum distance of 1.0) (Fig. 9, Table 1). MDS and UMAP produced similarly accurate clusters with normalized VIs of 0.15 (N=16) and 0.16 (N=6) at minimum distances of 0 and 0.5, respectively. As expected, PCA produced the least accurate clusters with a normalized VI of 0.36 (N=2, minimum distance of 4.5). We found 18 cluster-specific mutations for one of the two PCA clusters, 232 for nine of 16 MDS clusters, 363 for 15 of 19 t-SNE clusters, and 155 for five of six

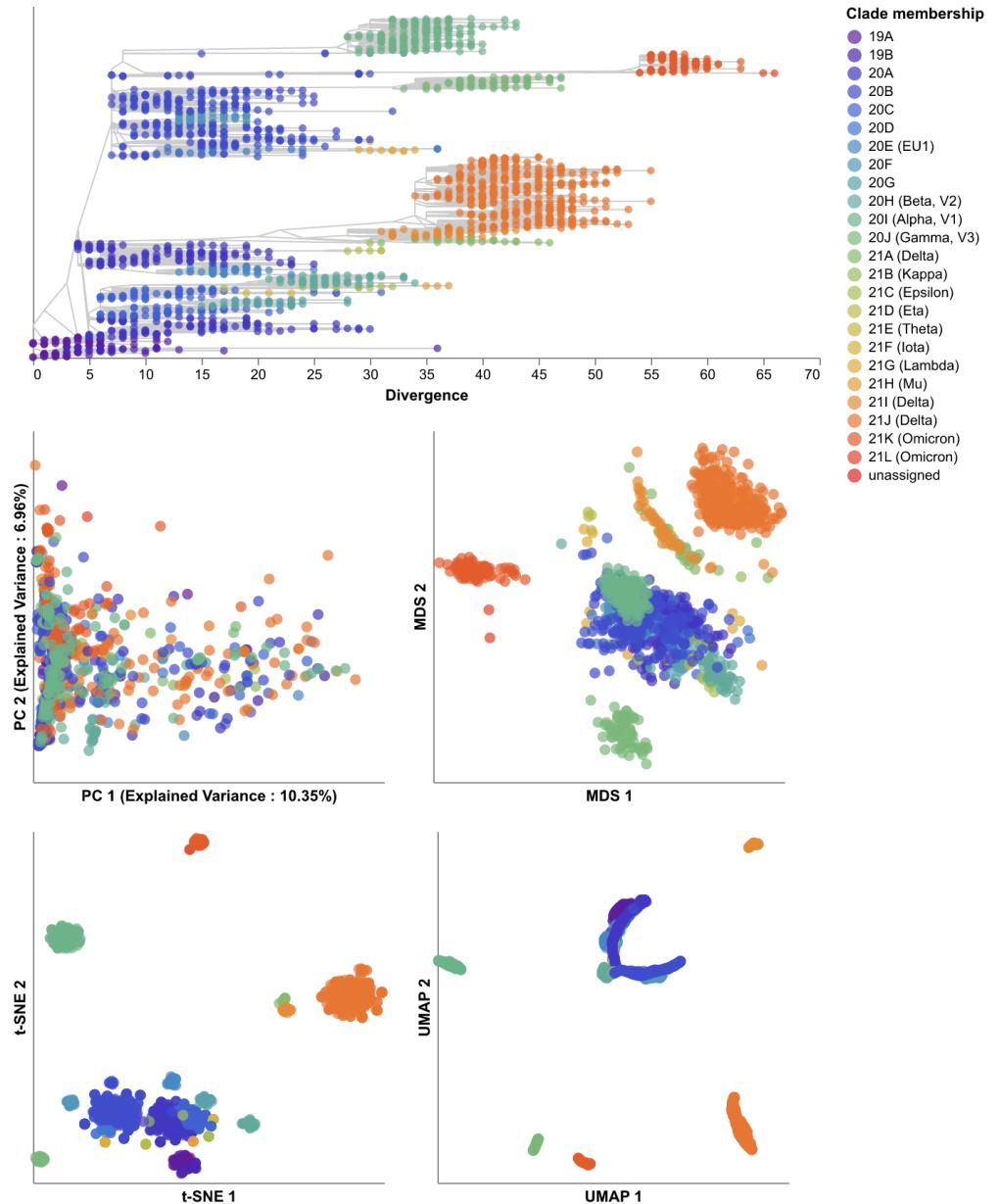
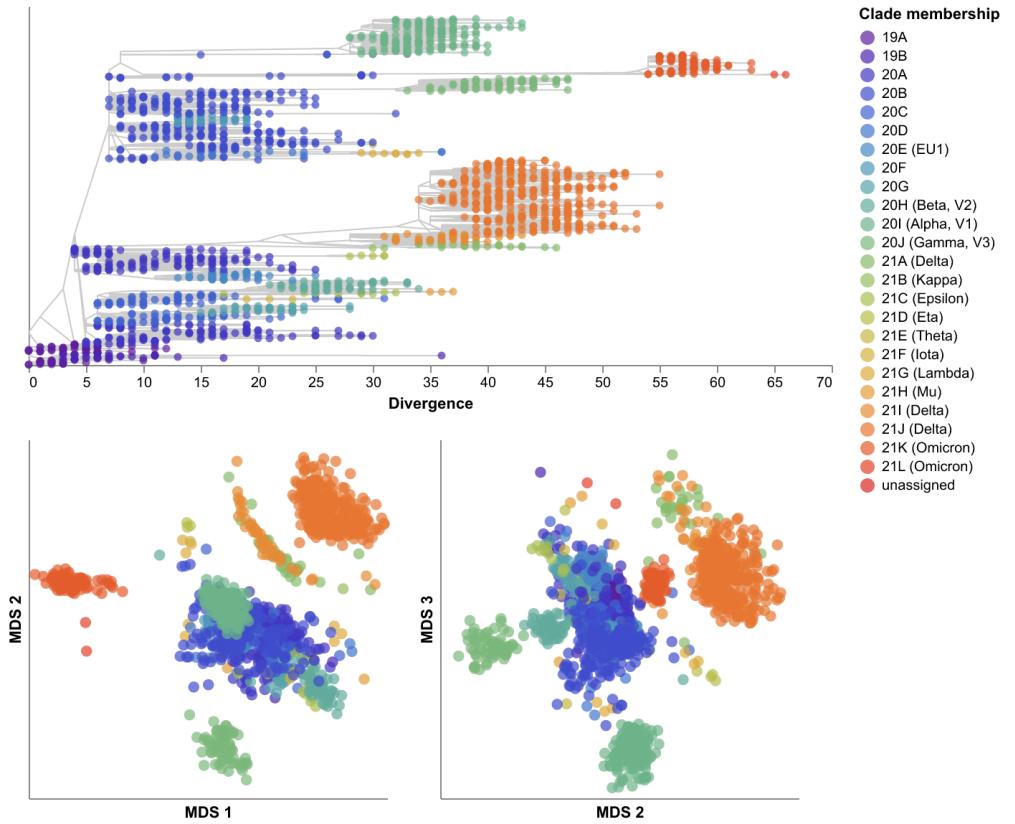


Fig 7. Phylogeny of early (2020–2022) SARS-CoV-2 sequences plotted by number of nucleotide substitutions from the most recent common ancestor on the x-axis (top) and low-dimensional embeddings of the same sequences by PCA (middle left), MDS (middle right), t-SNE (bottom left), and UMAP (bottom right). Tips in the tree and embeddings are colored by their Nextstrain clade assignment.

UMAP clusters (S1 Table). Clusters from t-SNE produced within-group genetic distances that were most similar to distances within Nextstrain clades (S17 Fig).

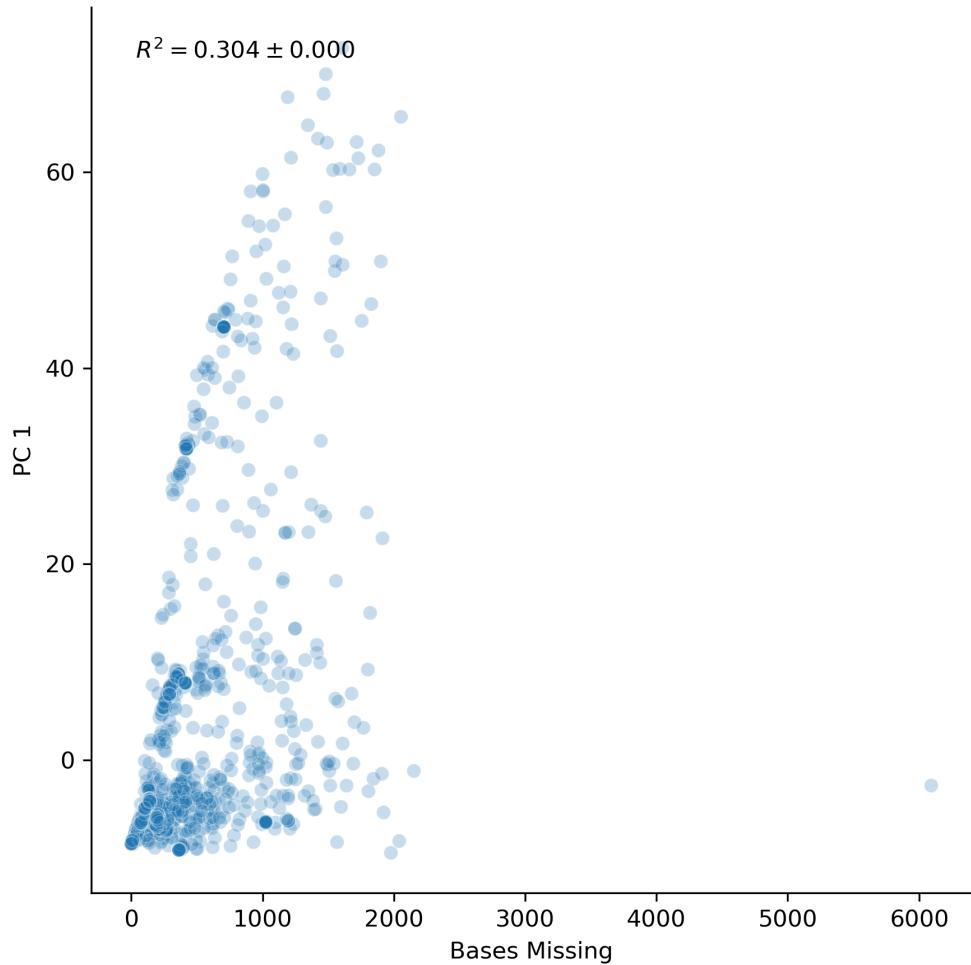
When comparing clusters to Nextclade pango lineages, all four methods produced less accurate clusters (S18 Fig). Clusters from t-SNE were the most accurate with a VI



S14 Fig. MDS embeddings for early SARS-CoV-2 sequences showing all three components.

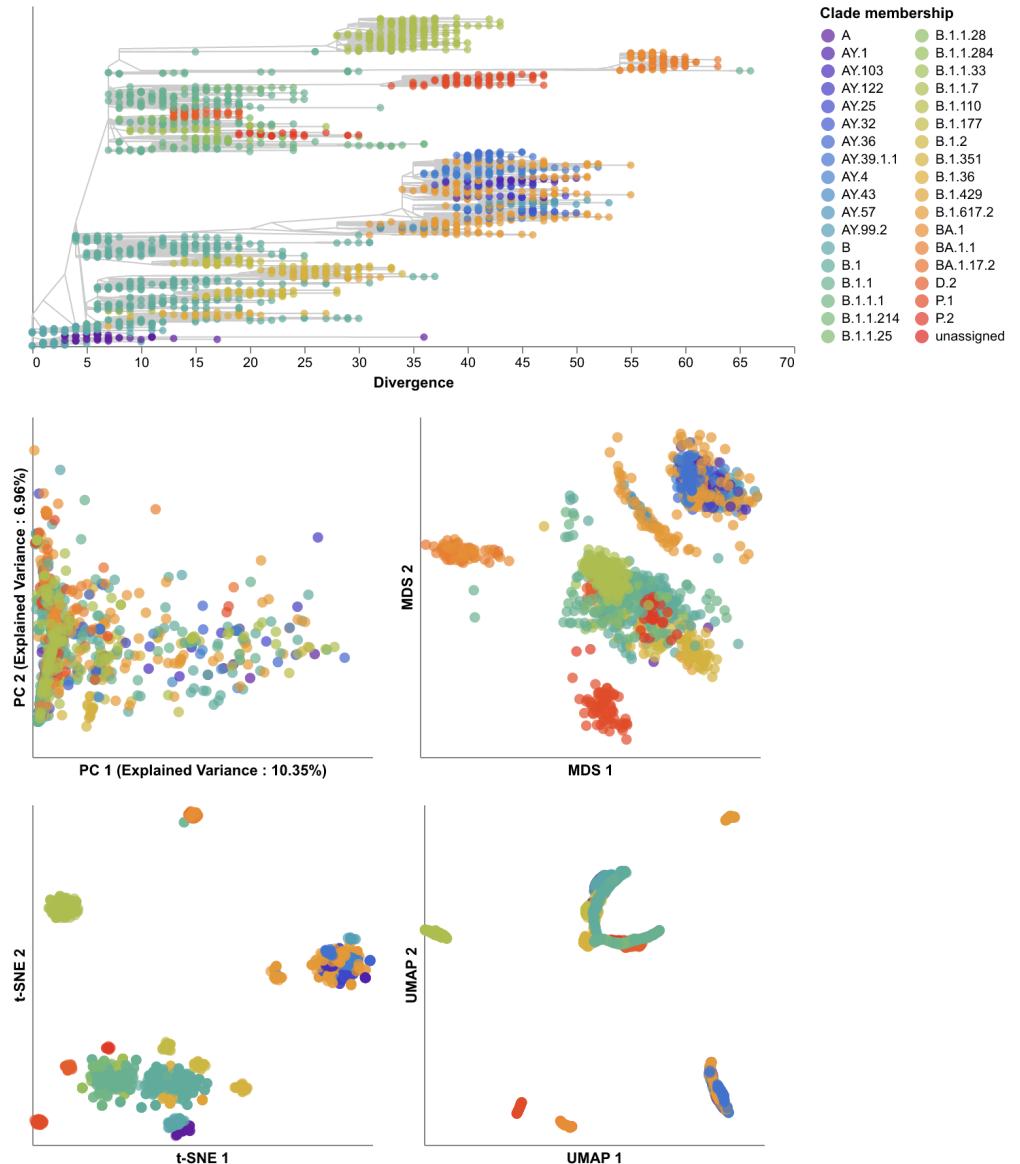
of 0.12. MDS and UMAP clusters performed similarly with VIs of 0.23 and 0.25. PCA clusters remained the least accurate with a VI of 0.42. The optimal minimum distances for all four methods remained the same with Nextclade pango lineages as when trained with Nextstrain clades. These results confirm quantitatively that these embeddings methods can accurately capture broader genetic diversity of SARS-CoV-2, but most methods cannot distinguish between fine resolution genetic groups identified by Pangolin. However, we observed greater pairwise genetic distances within collapsed Nextclade pango lineages than within Nextstrain clades, suggesting that Pangolin lineages were not as tightly scoped as we originally expected (S17 Fig).

To test the optimal cluster parameters identified above, we applied embedding methods to late SARS-CoV-2 data and compared clusters from these embeddings to known genetic groups. Of the 17 Nextstrain clades defined during this time period, 14 (82%) descended from Omicron and represented 1,495 (90%) of all samples in the dataset. Of the 51 Nextclade pango lineages, 20 originated from a recombination event



S15 Fig. Principal component 1 (PC1) of the PCA embedding for early SARS-CoV-2 data plotted by the number of missing (“N”) or gap (“-”) characters in the corresponding sample’s aligned sequence. Pearson’s R^2 estimates the variation in PC1 explained by missing data.

and corresponded to 521 (31%) of all samples. The clusters from embeddings of these more recent SARS-CoV-2 sequences performed as well or better than the clusters from earlier SARS-CoV-2 sequences (Fig. 10). Clusters from t-SNE most accurately matched Nextstrain clades (normalized VI=0.08) with 22 clusters. Clusters from UMAP followed (normalized VI=0.13) with nine clusters and MDS produced 10 clusters (normalized VI=0.15). We found 50 cluster-specific mutations for two of three PCA clusters, 75 for nine of 10 MDS clusters, 93 for 16 of 22 t-SNE clusters, and 112 for eight of nine UMAP clusters (S1 Table). Clusters from t-SNE remained the most consistently accurate across different random samples of sequences from the same time period and different total



S16 Fig. Phylogeny of early (2020–2022) SARS-CoV-2 sequences plotted by number of nucleotide substitutions from the most recent common ancestor on the x-axis (top) and low-dimensional embeddings of the same sequences by PCA (middle left), MDS (middle right), t-SNE (bottom left), and UMAP (bottom right). Tips in the tree and embeddings are colored by their collapsed Nextclade pango lineage assignment.

samples (S19 Fig). UMAP clusters became more accurate and less variable as we added more sequences per group to the embeddings. 682

All methods produced less accurate representations of Nextclade pango lineages (S20 Fig). Clusters from t-SNE were twice as far from Nextclade pango lineages than Nextstrain clades (normalized VI=0.16). UMAP's clusters were nearly two times farther 683
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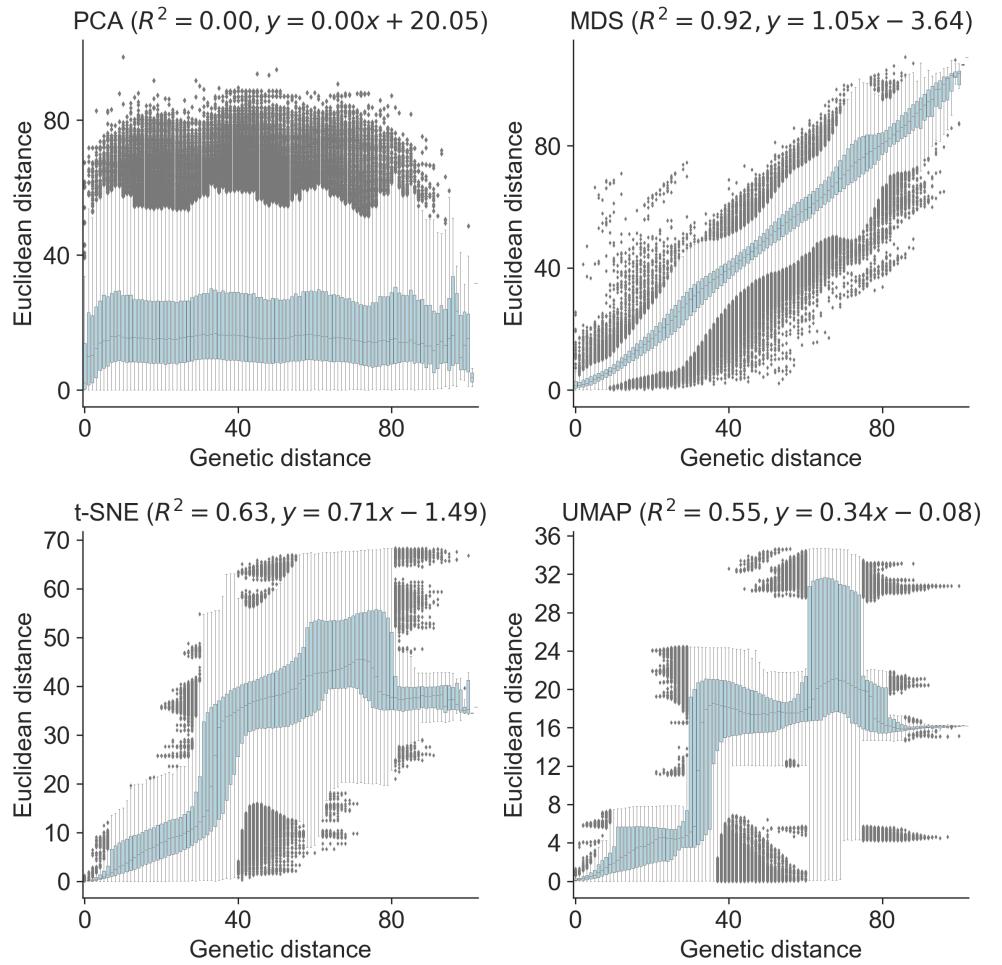


Fig 8. Relationship between pairwise genetic and Euclidean distances in embeddings for early (2020–2022) SARS-CoV-2 sequences by PCA (upper left), MDS (upper right), t-SNE (lower left), and UMAP (lower right). Each boxplot represents the distribution of pairwise Euclidean distances at a given genetic distance.

from pango lineages than Nextstrain clades (normalized VI=0.23). Clusters from MDS were 1.6 times as far from pango lineages as Nextstrain clades (normalized VI=0.24). These results replicate the patterns we observed with early SARS-CoV-2 data where clusters from embeddings more effectively represented broader genetic diversity than the finer resolution diversity labeled by Pangolin. Unlike the Nextclade pango lineages in the early SARS-CoV-2 data, the lineages from the later data exhibited fewer pairwise genetic distances between samples in each lineage than samples in Nextstrain clades or any embedding cluster (S17 Fig).

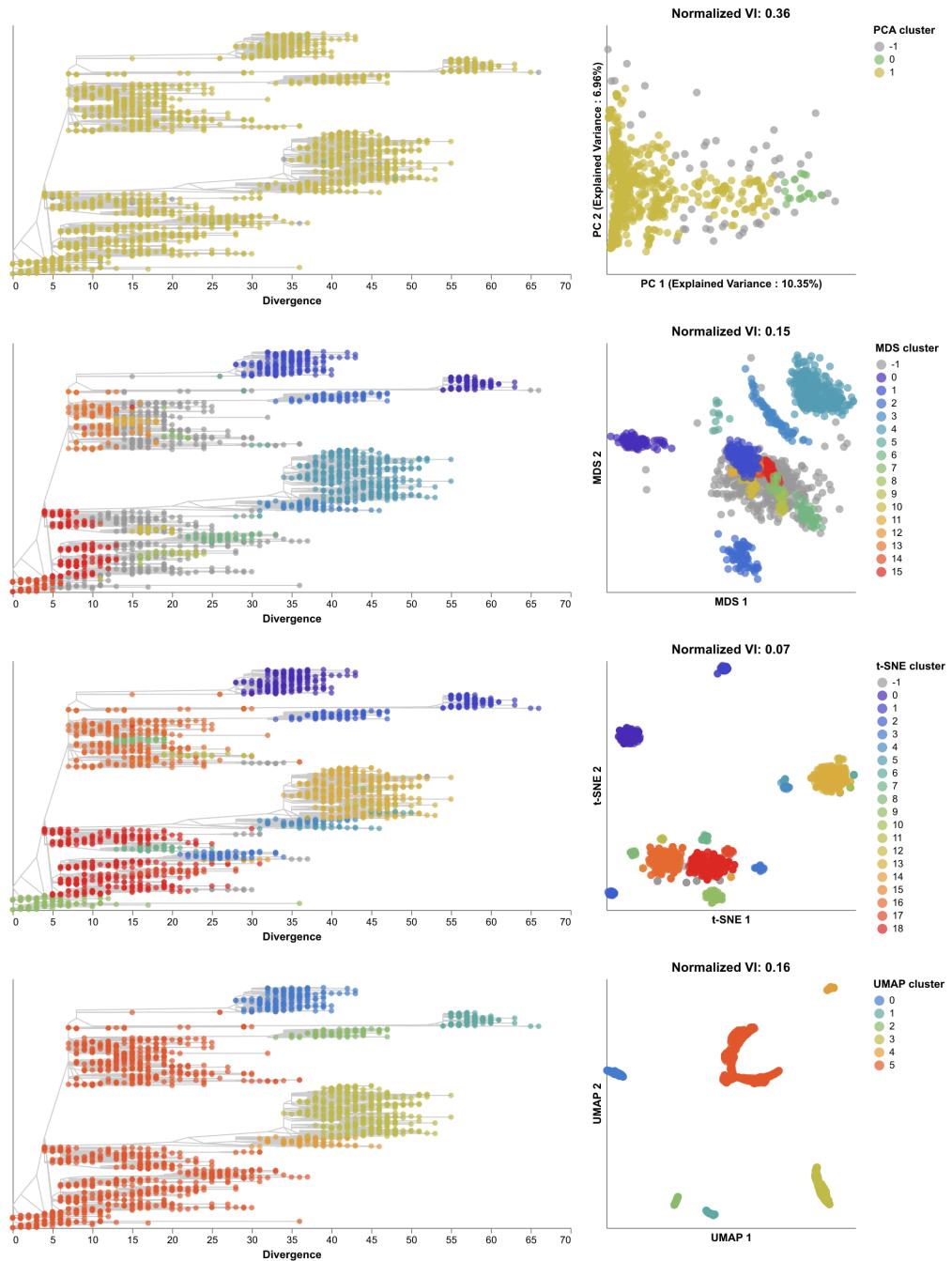
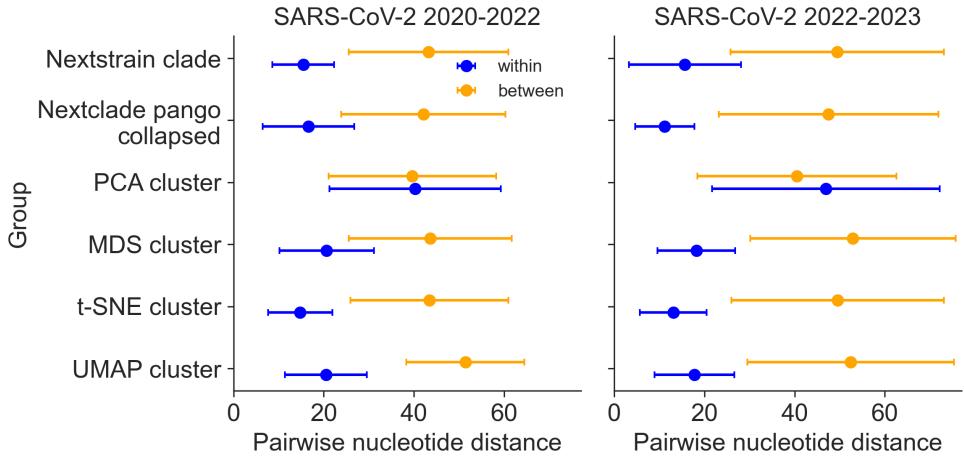


Fig 9. Phylogenetic trees (left) and embeddings (right) of early (2020–2022) SARS-CoV-2 sequences colored by HDBSCAN cluster. Normalized VI values per embedding reflect the distance between clusters and known genetic groups (Nextstrain clades).

Distance-based embeddings reflect SARS-CoV-2 recombination events

Finally, we tested the ability of sequence embeddings to capture patterns of recombination between known parental lineages of SARS-CoV-2. We reasoned that each



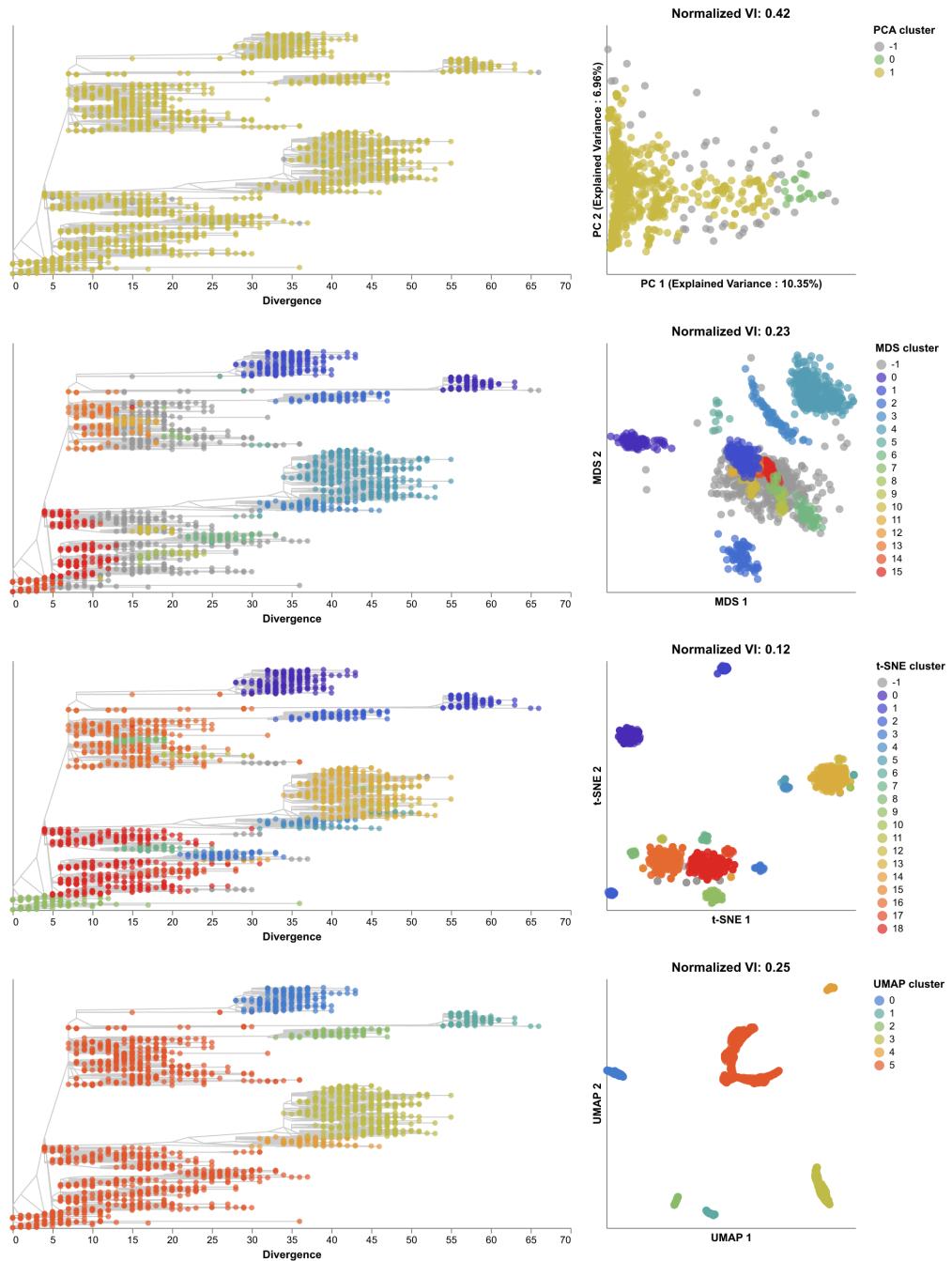
S17 Fig. Pairwise nucleotide distances for early (2020-2022) and late (2022-2023) SARS-CoV-2 sequences within and between genetic groups defined by Nextstrain clades, collapsed Nextclade pango lineages, and clusters from PCA, MDS, t-SNE, and UMAP embeddings.

recombinant lineage, X , should always place closer to its parental lineages A and B than the parental lineages place to each other. Based on this logic, we calculated the average Euclidean distance between pairs of samples in lineages A and B , A and X , and B and X for each embedding method (see Methods). We identified recombinant lineages that mapped closer to both of their parental lineages and those that mapped closer to at least one of the parental lineages.

Seven of the ten recombinant lineages that we inspected had enough samples in both parental and recombinant lineages to calculate average pairwise distances (XD, XE, XF, XG, XBB, XBF, and XBL). MDS embeddings consistently placed recombinant lineages between the parental lineages in all seven cases (S2 Table). Embeddings from t-SNE and UMAP performed nearly as well, placing five of seven recombinant lineages between parentals. PCA performed the worst with only three recombinant lineages of seven placed between parentals. However, all recombinant lineages mapped closer to at least one parent in all embeddings.

Discussion

We applied four standard dimensionality reduction methods to simulated and natural genome sequences of two relevant human pathogenic viruses and found that the



S18 Fig. Phylogenetic trees (left) and embeddings (right) of early (2020–2022) SARS-CoV-2 sequences colored by HDBSCAN cluster.
Normalized VI values per embedding reflect the distance between clusters and known genetic groups (collapsed Nextclade pango lineages).

resulting embeddings could reflect pairwise genetic relationships between samples and capture previously identified genetic groups. From our analysis of simulated influenza-
716 and coronavirus-like sequences, we found that each method produced consistent
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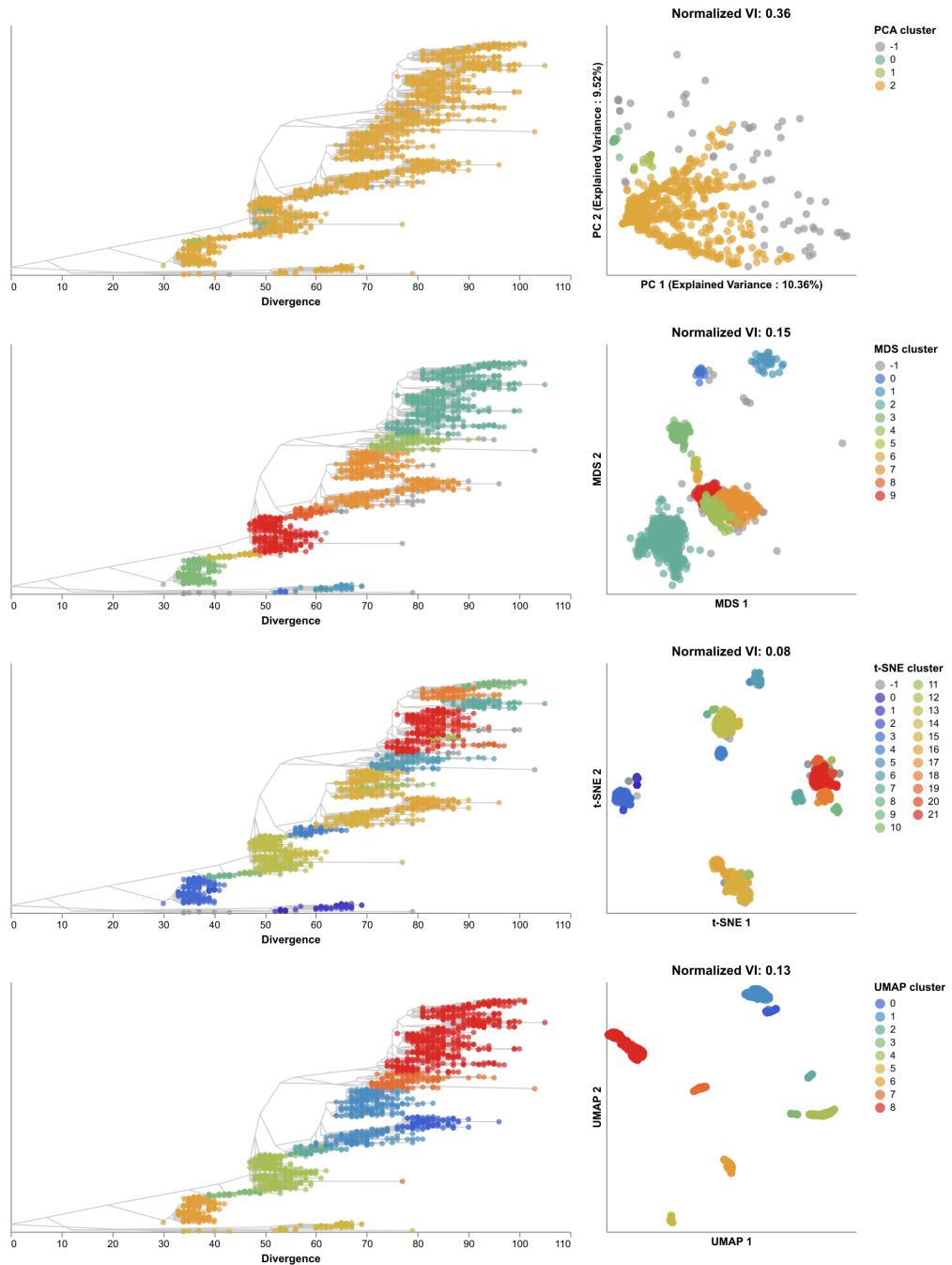
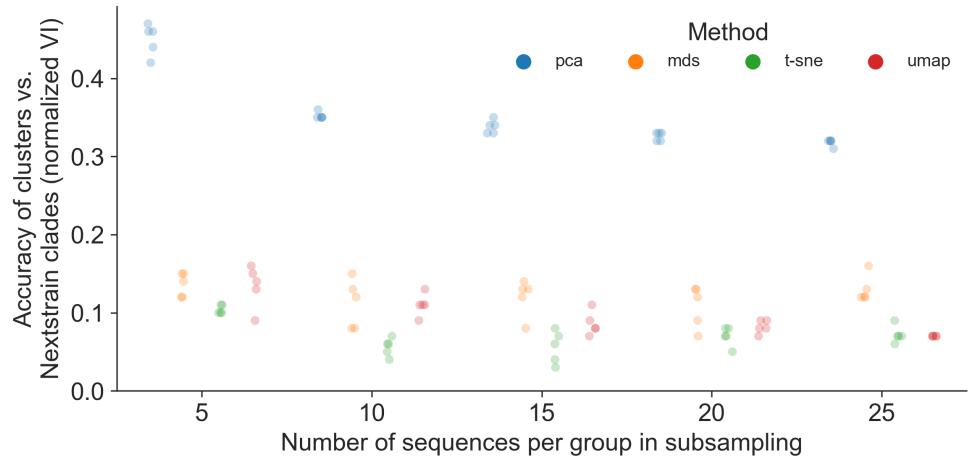


Fig 10. Phylogenetic trees (left) and embeddings (right) of late (2022–2023) SARS-CoV-2 sequences colored by HDBSCAN cluster. Normalized VI values per embedding reflect the distance between clusters and known genetic groups (Nextstrain clades).

embeddings of genetic sequences for two distinct pathogens, more than 55 years of evolution, and a wide range of practical method parameters. These results suggest that researchers could apply these biologically-uninformed methods to a broad range of

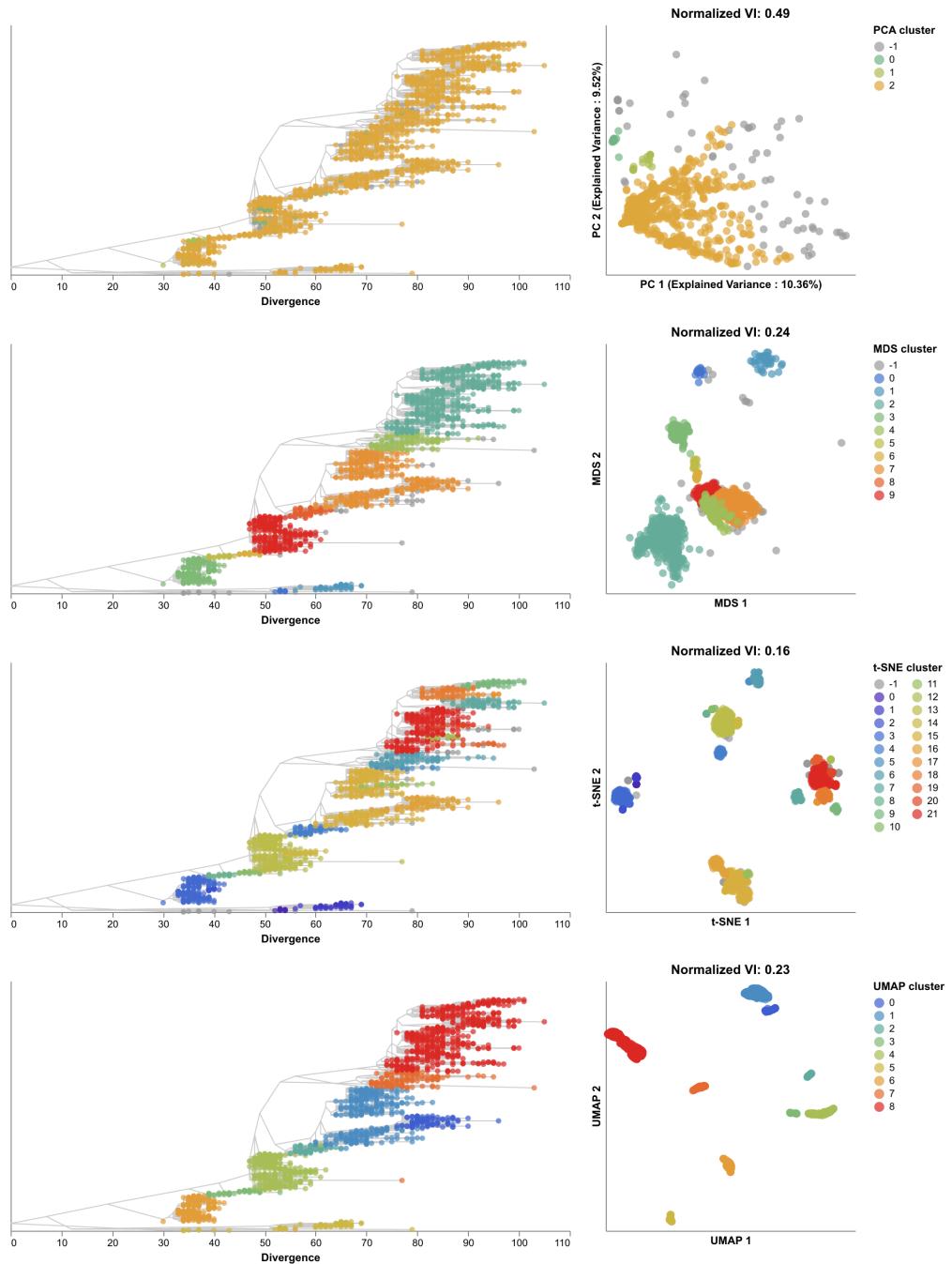


S19 Fig. Replication of cluster accuracy per embedding method for late (2022–2023) SARS-CoV-2 sequences across different sequences per group sampled from the original dataset and five replicates per sampling density.

S2 Table. Average Euclidean distances between each known recombinant, X , and its parental lineages A and B per embedding method. Distances include average pairwise comparisons between A and B , A and X , and B and X . Additional columns indicate whether each recombinant lineage maps closer to both parental lineages (or at least one) than those parents map to each other.

parental_A	parental_B	recombinant_X	method	distance_A_B	distance_A_X	distance_B_X	X_maps_closer_to_both_parents	X_maps_closer_to_any_parental
AY.4	BA.1	XD	PCA	14.14	7.51	15.17	False	True
BA.1	BA.2	XE	PCA	28.30	15.02	24.33	True	True
AY.4	BA.1	XF	PCA	14.14	9.16	16.51	False	True
BA.1	BA.2	XG	PCA	28.30	13.41	23.30	True	True
BJ.1	BM.1.1.1	XBB	PCA	23.28	17.44	24.87	False	True
BA.5.2.3	CJ.1	XBF	PCA	18.72	17.55	20.27	False	True
XBB.1	BA.2.75	XBL	PCA	22.95	20.43	20.52	True	True
AY.4	BA.1	XD	MDS	78.98	43.29	50.74	True	True
BA.1	BA.2	XE	MDS	48.67	32.41	21.46	True	True
AY.4	BA.1	XF	MDS	78.98	74.38	6.72	True	True
BA.1	BA.2	XG	MDS	48.67	39.75	13.91	True	True
BJ.1	BM.1.1.1	XBB	MDS	35.98	20.30	28.46	True	True
BA.5.2.3	CJ.1	XBF	MDS	43.51	39.39	9.68	True	True
XBB.1	BA.2.75	XBL	MDS	32.50	12.82	30.95	True	True
AY.4	BA.1	XD	t-SNE	6.65	1.66	5.35	True	True
BA.1	BA.2	XE	t-SNE	37.63	34.31	6.30	True	True
AY.4	BA.1	XF	t-SNE	6.65	9.33	2.83	False	True
BA.1	BA.2	XG	t-SNE	37.63	36.46	5.34	True	True
BJ.1	BM.1.1.1	XBB	t-SNE	27.56	4.87	31.21	False	True
BA.5.2.3	CJ.1	XBF	t-SNE	56.13	55.38	1.52	True	True
XBB.1	BA.2.75	XBL	t-SNE	31.98	4.21	31.26	True	True
AY.4	BA.1	XD	UMAP	12.19	0.88	11.54	True	True
BA.1	BA.2	XE	UMAP	15.83	11.93	4.83	True	True
AY.4	BA.1	XF	UMAP	12.19	11.80	0.77	True	True
BA.1	BA.2	XG	UMAP	15.83	12.48	4.02	True	True
BJ.1	BM.1.1.1	XBB	UMAP	13.71	1.33	14.76	False	True
BA.5.2.3	CJ.1	XBF	UMAP	17.82	17.87	0.38	False	True
XBB.1	BA.2.75	XBL	UMAP	14.81	1.75	13.46	True	True

human pathogenic viruses with minimal tuning of the method parameters. Of the four methods, MDS most accurately reflected pairwise genetic distances between simulated samples in its embeddings. From our analysis of natural populations of seasonal influenza H3N2 HA and SARS-CoV-2 sequences, we confirmed that MDS most reliably reflected pairwise genetic distances and we found that clusters from t-SNE embeddings most accurately recapitulated previously defined genetic groups at the resolution of WHO and Nextstrain clades. Clusters from both MDS and t-SNE embeddings of H3N2



S20 Fig. Phylogenetic trees (left) and embeddings (right) of late (2022–2023) SARS-CoV-2 sequences colored by HDBSCAN cluster.
Normalized VI values per embedding reflect the distance between clusters and known genetic groups (collapsed Nextclade pango lineages).

HA and NA sequences accurately matched reassortment clades identified by a biologically-informed model based on ancestral reassortment graphs. MDS embeddings consistently placed known recombinant lineages of SARS-CoV-2 between their parental

lineages. From these results, we conclude that tree-free dimensionality reduction
732 methods can provide valuable biological insights for human pathogenic viruses through
733 easily interpretable visualizations of genetic relationships and the ability to account for
734 genetic variation that phylogenetic methods cannot including indels, reassortment, and
735 recombination.
736

Despite the promise of these simple methods to answer important public health
737 questions about human pathogenic viruses, these methods and our analyses suffer from
738 inherent limitations. The lack of an underlying biological model is both a strength and
739 the clearest limitation of the dimensionality reduction methods we considered here. For
740 example, embeddings of SARS-CoV-2 genomes cannot capture the same fine-grained
741 genetic resolution as Pangolin lineage annotations. Each method provides only a few
742 parameters to tune its embeddings and these parameters have little effect on the
743 qualitative outcome. Each method also suffers from specific issues in our analysis. PCA
744 performs poorly with missing data and requires researchers to impute the missing values
745 prior to analysis, as previously shown for Zika virus [30]. Neither t-SNE nor UMAP
746 maintain a linear relationship between pairwise Euclidean and genetic distances across
747 the observed range of genetic distances. As a result, viewers cannot know that samples
748 mapping far apart in a t-SNE or UMAP embedding are as genetically distant as they
749 appear. In maintaining a linear relationship between Euclidean and genetic distances,
750 MDS sacrifices the ability to form more accurate genetic clusters for viruses with large
751 genomes like SARS-CoV-2. Given these limitations of these methods, we do not expect
752 them to replace biologically-informed methods that provide more meaningful
753 parameters to tune their algorithms. Instead, we expect that researchers can use these
754 methods for rapid visualization and clustering of their genome sequences as the first
755 step prior to analysis with more sophisticated and computationally intensive algorithms.
756

We note that our analysis reflects a small subset of human pathogen viruses and
757 dimensionality reduction methods. We focused on analysis of two respiratory RNA
758 viruses that contribute dramatically to seasonal human morbidity and mortality, but
759 numerous alternative pathogens would also have been relevant subjects. For example,
760 HIV represents a canonical example of a highly recombinant and bloodborne virus,
761 while Zika, dengue, and West Nile viruses represent pathogens with multiple host
762 species in a transmission chain. Similarly, we selected only four dimensionality
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reduction methods from myriad options that are commonly applied to genetic data [65].
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We chose these methods based on their wide use and availability in tools like
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scikit-learn [36] and to limit the dimensionality of our analyses.
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Some limitations noted above suggest future directions for this line of research. We
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provide optimal settings for each pathogen and embedding method in this study and
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open source tools to apply these methods to other pathogens. Researchers can easily
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integrate these tools into existing workflows for the genomic epidemiology of viruses and
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visualize the results with Nextstrain. Alternately, researchers may choose to apply
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similar existing tools developed for metagenomic analysis [66–69] to the analysis of viral
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populations. In the short term, researchers can apply the methods we describe here to
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seasonal influenza and SARS-CoV-2 genomes to identify biologically relevant clusters
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including reassortment events or recombinant lineages. In the long term, we expect
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researchers will benefit from expanding the breadth of dimensionality reduction
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methods applied to viruses and the breadth of viral diversity assessed by these methods.
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Conclusion

We showed that simple dimensionality reduction methods operating on pairwise genetic
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differences can capture biologically-relevant clusters of phylogenetic clades, reassortment
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events, and patterns of recombining lineages for human pathogenic viruses. The
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conceptual and practical simplicity of these tools should enable researchers to more
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readily visualize and compare samples for human pathogenic viruses when phylogenetic
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methods are either unnecessary or inappropriate.
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Supporting information

**S1 Fig. Distribution of mean absolute errors (MAE) between observed and
predicted pairwise genetic distances per embedding method parameters for
simulated influenza-like populations.** Each panel shows boxplots of MAEs for a
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specific embedding method (PCA, MDS, t-SNE, and UMAP) and a given combination
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of method parameters. Boxplots reflect median, upper and lower quartiles, and the
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range of values.
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- S2 Fig.** Distribution of mean absolute errors (MAE) between observed and predicted pairwise genetic distances per embedding method parameters for simulated coronavirus-like populations. Each panel shows boxplots of MAEs for a specific embedding method (PCA, MDS, t-SNE, and UMAP) and a given combination of method parameters. Boxplots reflect median, upper and lower quartiles, and the range of values. 792
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- S3 Fig.** Representative MDS embeddings for simulated populations using optimal parameters per pathogen (rows) and showing all three components. 798
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- S4 Fig.** MDS embeddings for early (2016–2018) influenza H3N2 HA sequences showing all three components. 800
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- S5 Fig.** Pairwise nucleotide distances for early (2016–2018) and late (2018–2020) influenza H3N2 HA sequences within and between genetic groups defined by Nextstrain clades and clusters from PCA, MDS, t-SNE, and UMAP embeddings. 802
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- S6 Fig.** Phylogeny of late (2018–2020) influenza H3N2 HA sequences plotted by nucleotide substitutions per site on the x-axis (top) and low-dimensional embeddings of the same sequences by PCA (middle left), MDS (middle right), t-SNE (bottom left), and UMAP (bottom right). Tips in the tree and embeddings are colored by their Nextstrain clade assignment. 806
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- S7 Fig.** MDS embeddings for late (2018–2020) influenza H3N2 HA sequences showing all three components. 811
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- S8 Fig.** Replication of cluster accuracy per embedding method for late (2018–2020) influenza H3N2 HA sequences across different sequences per group sampled from the original dataset and five replicates per sampling density. 813
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- S9 Fig.** Embeddings influenza H3N2 HA-only (left) and combined HA/NA (right) showing the effects of additional NA genetic information on the 817
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placement of reassortment events detected by TreeKnit (MCCs).

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S10 Fig. PCA embeddings for influenza H3N2 HA sequences only (top
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row) and HA/NA sequences combined (bottom row) showing the HA trees
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colored by clusters identified in each embedding (left) and the
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corresponding embeddings colored by cluster (right).
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S11 Fig. MDS embeddings for influenza H3N2 HA sequences only (top
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row) and HA/NA sequences combined (bottom row) showing the HA trees
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colored by clusters identified in each embedding (left) and the
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corresponding embeddings colored by cluster (right).
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S12 Fig. t-SNE embeddings for influenza H3N2 HA sequences only (top
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row) and HA/NA sequences combined (bottom row) showing the HA trees
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colored by clusters identified in each embedding (left) and the
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corresponding embeddings colored by cluster (right).
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S13 Fig. UMAP embeddings for influenza H3N2 HA sequences only (top
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row) and HA/NA sequences combined (bottom row) showing the HA trees
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colored by clusters identified in each embedding (left) and the
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corresponding embeddings colored by cluster (right).
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S14 Fig. MDS embeddings for early SARS-CoV-2 sequences showing all
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three components.
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S15 Fig. Principal component 1 (PC1) of the PCA embedding for early
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SARS-CoV-2 data plotted by the number of missing (“N”) or gap (“-”)
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characters in the corresponding sample’s aligned sequence. Pearson’s R^2
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estimates the variation in PC1 explained by missing data.
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S16 Fig. Phylogeny of early (2020–2022) SARS-CoV-2 sequences plotted
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by number of nucleotide substitutions from the most recent common
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ancestor on the x-axis (top) and low-dimensional embeddings of the same
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sequences by PCA (middle left), MDS (middle right), t-SNE (bottom left),
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and UMAP (bottom right). Tips in the tree and embeddings are colored by
their collapsed Nextclade pango lineage assignment.

S17 Fig. Pairwise nucleotide distances for early (2020–2022) and late
(2022–2023) SARS-CoV-2 sequences within and between genetic groups
defined by Nextstrain clades, collapsed Nextclade pango lineages, and
clusters from PCA, MDS, t-SNE, and UMAP embeddings.

S18 Fig. Phylogenetic trees (left) and embeddings (right) of early
(2020–2022) SARS-CoV-2 sequences colored by HDBSCAN cluster.
Normalized VI values per embedding reflect the distance between clusters
and known genetic groups (collapsed Nextclade pango lineages).

S19 Fig. Replication of cluster accuracy per embedding method for late
(2022–2023) SARS-CoV-2 sequences across different sequences per group
sampled from the original dataset and five replicates per sampling density.

S20 Fig. Phylogenetic trees (left) and embeddings (right) of late
(2022–2023) SARS-CoV-2 sequences colored by HDBSCAN cluster.
Normalized VI values per embedding reflect the distance between clusters
and known genetic groups (collapsed Nextclade pango lineages).

S1 Table. Mutations observed per embedding cluster relative to a
reference genome sequence for each pathogen. Each row reflects the
alternate allele identified at a specific position of the given pathogen genome
or gene sequence, the pathogen dataset, the embedding method, the number
of clusters in the embedding with the observed mutation, and the list of
distinct cluster labels with the mutation. Mutations must have occurred in
at least 10 samples of the given dataset with an allele frequency of at least
50%.

S2 Table. Average Euclidean distances between each known recombinant,
 X , and its parental lineages A and B per embedding method. Distances
include average pairwise comparisons between A and B , A and X , and B and X .

X. Additional columns indicate whether each recombinant lineage maps closer to both parental lineages (or at least one) than those parents map to each other.	874 875 876
S3 Table. Accessions and authors from originating and submitting laboratories of seasonal influenza and SARS-CoV-2 sequences from INSDC databases.	877 878 879

Acknowledgments

We thank members of the Bedford Lab for constructive feedback on this project over the course of many years. We gratefully acknowledge the originating and submitting laboratories of seasonal influenza and SARS-CoV-2 sequences from INSDC databases without whom this work would not be possible (S3 Table). JH was supported by NIH F31AI140714. AB was supported by the National Science Foundation Graduate Research Fellowship Program under Grant No. DGE-1256082. TB is a Howard Hughes Medical Institute Investigator. This work was supported by NIH NIGMS award R35 GM119774 to TB, BMGF award INV-018979 to TB and NIH NIAID contract 75N93021C00015.

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