

Unravelling higher order chromatin organisation through statistical analysis

Benjamin L. Moore

Doctor of Philosophy
The University of Edinburgh
2015



DECLARATION

This thesis presents my own work, wherever the contributions of others were involved this is clearly indicated. It has not been submitted for any other degree or professional qualification.

—Benjamin L. Moore (2015)

ACKNOWLEDGEMENTS

ABSTRACT

Recent technological advances underpinned by high throughput sequencing have given new insights into the three-dimensional structure of mammalian genomes. Chromatin conformation assays have been the critical development in this area, particularly Hi-C, which ascertains genome-wide patterns of intra and inter-chromosomal contacts. However many open questions remain concerning the functional relevance of such higher order structure, the extent to which it varies, and how it relates to other features of the genomic and epigenomic landscape.

Current knowledge of nuclear architecture describes a hierarchical organisation ranging from small loops between individual loci, to megabase-sized self-interacting topological domains (TADs), encompassed within large multimegabase chromosome compartments. In parallel with the discovery of these strata, the ENCODE project has generated vast amounts of data through ChIP-seq, RNA-seq and other assays applied to a wide variety of cell types, forming a comprehensive bioinformatics resource.

In this work we combine Hi-C datasets describing physical genomic contacts with a large and diverse array of chromatin features derived at a much finer scale in the same mammalian cell types. These features include levels of bound transcription factors, histone modifications and expression data. These data are then integrated in a statistically rigorous way, through a predictive modelling framework from the machine learning field. These studies were extended, within a collaborative project, to encompass a dataset of matched Hi-C and expression data collected over a murine neural differentiation timecourse.

We compare higher order chromatin organisation across a variety of human cell types and find pervasive conservation of chromatin organisation at multiple scales. We also identify structurally variable regions between cell types, that are rich in active enhancers and contain loci of known cell-type specific function. We show that broad aspects of higher order chromatin organisation, such as nuclear compartment domains, can be accurately predicted in a variety of human cell types, using models based upon underlying chromatin features. We dissect these quantitative models and find them to be generalisable to novel cell types, presumably reflecting fundamental biological rules linking compartments with key activating and repressive signals. These models describe the strong interconnectedness between locus-level patterns of local histone modifications and bound factors, on the order of hundreds or thousands of basepairs, with much broader compartmentalisation of large, multi-megabase chromosomal regions.

Finally, boundary regions are investigated in terms of chromatin features and co-localisation with other known nuclear structures, such as association with the nuclear lamina. We find boundary complexity to vary between cell types and link TAD aggregations to previously described lamin-associated domains, as well as exploring the concept of super-boundaries that span multiple levels of organisation. Together these analyses lend quantitative evidence to a model of higher order genome organisation that is largely stable between cell types, but can selectively vary locally, based on the activation or repression of key loci.

LAY SUMMARY

Each human cell contains DNA that would extend for two metres if fully straightened. Instead, this same length of DNA is highly compacted into micrometre-sized cell nuclei. Recently experimental methods such as Hi-C have been developed which allow the inspection of this folded state, generating counts of how frequently chromosomal regions are interacting with each other. These counts can be statistically analysed to reveal different levels of structures, including loops between two distant locations, knot-like domains of self-interacting regions, and broad stretches of mostly active or inactive regions.

In this work, we bring together Hi-C datasets from several different publications and combine these with a large number of chromatin datasets that quantify, for example, levels different DNA-binding proteins as well as modifications to DNA packing histone proteins. We used these datasets to build predictive models of active and inactive states across each human chromosome in three different cell types, and achieved high predictive accuracy. We then compare and contrast these models, and use them to identify the key features which define active and inactive states.

We also analyse the boundaries between domains and compare these across cell types. We find the domains themselves are highly conserved between cell types, but observe different chromatin features marking domain boundaries. Further collaborative work involved analysis of boundaries from Hi-C data taken over successive time points, where boundary markings were found to persist as cells differentiate from stem cells.

Overall we find the three-dimensional DNA structures within cells are highly similar even between human embryonic stem cells and cells derived from blood. Where there are differences, these areas tend to highlight biological activity specific to that cell type.

CONTENTS

Declaration **ii**

Acknowledgements **iv**

Abstract **vi**

Lay summary **ix**

Contents **xi**

List of Figures **xv**

List of Tables **xix**

List of Acronyms **xx**

Published material **xxiii**

1 INTRODUCTION 1

1.1	Genome organisation	1
1.1.1	C-methods and Hi-C	1
1.1.2	Hi-C variants	2
1.1.3	Chromosome compartments	4
1.1.4	Topological domains	6
1.1.5	Other proposed structures	7
1.2	Models of chromatin folding	8
1.2.1	Fractal globule	9
1.2.2	Strings and binders switch	9
1.2.3	Looping and CTCF	10
1.3	Criticisms of C-methods	11
1.3.1	Cell populations	11
1.3.2	Ploidy	12
1.3.3	Resolution	12
1.3.4	Biological interpretation	12
1.3.5	Other considerations	13
1.4	Machine learning in genomics	13
1.4.1	ENCODE	14
1.4.2	Related work	15

1.5	Aims	15
2	METHODS	17
2.1	Hi-C data	17
2.1.1	Mapping	17
2.1.2	Filtering	17
2.1.3	Correction	18
2.1.4	Eigenvector calculation	18
2.1.5	TAD calling	19
2.2	ENCODE features	20
2.2.1	Clustering input features	20
2.3	Modelling compartment eigenvectors	20
2.3.1	Random Forest	20
2.3.2	Model performance	21
2.3.3	Hidden Markov models	22
2.3.4	Stepwise regression	23
2.3.5	LASSO	24
2.3.6	Other modelling approaches	25
2.4	Variable regions	25
2.4.1	Stratification by variability	25
2.4.2	Chromatin state enrichment	25
2.4.3	Gene ontology analysis	26
2.5	Boundaries	26
2.5.1	TAD boundaries	26
2.5.2	Compartments	27
2.6	Predicting TAD boundaries	27
2.6.1	AUC-RF	27
2.6.2	Gini importance	28
2.7	MetaTAD analysis	29
2.7.1	Size selection	29
2.7.2	Collaborator datasets	29
2.7.3	LAD coincidence	30
2.8	Giems band comparison	30
2.9	Nuclear positioning	31
2.10	Modelling transcriptional output	31
2.10.1	Reproducing a published study	31
2.10.2	Predicting FANTOM5 data	32
2.11	4C analysis	32
2.11.1	Normalisation	33
2.11.2	Significance estimation	33
2.12	Scripts and other analyses	34

3 REANALYSIS OF HI-C DATASETS	35
3.1 Introduction	35
3.2 Hi-C reprocessing	35
3.3 Compartment profiles	37
3.4 Domain calls	37
3.4.1 Compartments	37
3.4.2 TADs	42
3.5 Domain epigenomics	44
3.5.1 A/B compartments	44
3.5.2 TAD classes	45
3.6 Variable regions	47
3.6.1 Chromatin state enrichment	50
3.6.2 Gene ontology enrichment	52
3.6.3 Contact changes	52
3.7 Nuclear positioning	54
4 INTEGRATIVE MODELLING AS A TOOL TO EXPLORE BIOLOGICAL SYSTEMS	55
4.1 Introduction	55
4.2 Extending Dong <i>et al.</i>	56
4.2.1 <i>Bestbin</i> method	57
4.2.2 Model adjustments	59
4.3 Modelling FANTOM5 expression data	60
4.3.1 <i>Bestbin</i> analysis	61
4.4 Modelling higher order chromatin	61
4.4.1 Predictive model	63
4.4.2 Cross-application	64
4.4.3 Between-cell variability	64
4.4.4 Variable importance	66
4.4.5 Correlating input features	70
4.5 Technical considerations	70
4.5.1 Resolution	70
4.5.2 Other modelling approaches	73
4.5.3 Non-independence	74
4.6 Parsimonious models from expanded feature sets	75
4.6.1 Stepwise regression	75
4.6.2 LASSO regression	76
4.6.3 Regularised Random Forest	77
5 CHROMATIN DOMAIN BOUNDARIES	79
5.1 Introduction	79
5.2 TAD and compartment boundaries	80

5.2.1	CTCF and YY1	85
5.2.2	Repeats	86
5.3	De novo boundary prediction	88
5.3.1	Learning boundary classification	88
5.4	MetaTAD boundaries	91
5.4.1	MetaTAD / TAD boundary comparison	92
5.4.2	Lamina associated domains	94
5.4.3	Boundaries over a time series	96
5.5	Other boundaries	99
5.5.1	Giemsa bands	99
6	LOCAL CHROMATIN CONFORMATION	103
6.1	Introduction	103
6.2	4C at the SHH locus	103
6.2.1	4C pipeline	104
6.2.2	Analysis of ZRS interactions	105
6.2.3	Assay diagnostics	105
6.3	3D modelling of chromatin fibre	109
6.3.1	AutoChrom3D method	109
6.3.2	Modelling the <i>Shh</i> region with 5C	110
6.3.3	Repeat simulations	110
7	DISCUSSION	115
7.1	Modelling higher order chromatin organisation	115
7.2	Domain boundaries	116
7.3	Domain evolution	117
7.4	A note on causality	117
7.5	Insights into genome organisation	118
7.6	Conclusion	118
	APPENDICES	121
	References	141

LIST OF FIGURES

Figure 1	Steps in the Hi-C assay.	3
Figure 2	Derivation of A/B compartment profile from Hi-C data.	5
Figure 3	Dixon <i>et al.</i> pipeline for calling topological associating domains (TADs).	7
Figure 4	Levels of higher order chromatin organisation.	8
Figure 5	Comparison of theoretical models of chromatin folding.	9
Figure 6	Random Forests overview.	21
Figure 7	Random Forest parameters are largely insensitive.	22
Figure 8	Iterative correction converts raw counts to normalised interaction frequencies.	36
Figure 9	Compartment profiles are observably well-correlated between human cell types and across all chromosomes	38
Figure 10	Compartment eigenvectors are highly correlated between human cell types	39
Figure 11	Overview of HMM method for compartment calls.	40
Figure 12	Univariate Gaussian emission distributions for A and B unobserved HMM states.	41
Figure 13	Compartment calls by simple thresholding method or context-aware HMMs.	41
Figure 14	Size distributions of compartment calls in three human cell types.	42
Figure 15	Compartment boundaries are shared between cell types.	43
Figure 16	The number of called TADs per cell type under study.	43
Figure 17	TAD boundaries are shared between cell types.	44
Figure 18	Concordance of chromatin structure at multiple scales over three human cell types.	45
Figure 19	The chromatin signatures of A/B compartments.	46
Figure 20	TADs reflect epigenomic domains.	48
Figure 21	Structurally variable regions indicate cell type specific biology.	49
Figure 22	Regions of variable structure are enriched for cell type specific enhancers.	50
Figure 23	Distributions of features across all predicted chromatin states in regions of variable higher order structure.	51

- Figure 24 Regions of variable higher order structure change their genome-wide contact profiles to favour active compartments. 53
- Figure 25 Nuclear positioning of chromosomes relative to compartment eigenvectors. 54
- Figure 26 Highly accurate models of expression were built following Dong *et al.* 56
- Figure 27 Comparison of two-step classification-regression model of transcription with a simple linear regression model. 57
- Figure 28 Average input feature profiles over transcription start sites. 58
- Figure 29 Relative importance metrics for variables in both stages of a reimplementation of a published model for predicting transcriptional output. 59
- Figure 30 Random Forest predictions of FANTOM5 expression data. 60
- Figure 31 Distributions of bestbin locations relative to the TSS. 62
- Figure 32 Compartment eigenvector model predictions are highly correlated with observed values. 63
- Figure 33 Models of higher order chromatin structure learned in one cell type can be cross-applied to others. 65
- Figure 34 Genomic regions that vary across cell types are modelled less successfully than static regions. 66
- Figure 35 Variable importance per cell type specific model. 67
- Figure 36 Intersections of the top 10 ranked variables in the cell type specific models. 67
- Figure 37 Correlations of individual features with compartment eigenvector in the H1 hESC cell type. 68
- Figure 38 Comparison of variable importance between three cell type specific Random Forest models. 69
- Figure 39 Correlation heatmaps of the 35 features used to model compartment eigenvectors. 71
- Figure 40 Models learned at 1 Mb resolution can be applied to higher resolution datasets. 72
- Figure 41 Comparison of Random Forest performance with other modelling approaches. 73
- Figure 42 Circle of correlations of variables compared with PLS axes. 74
- Figure 43 Ten largest LASSO model coefficients from expanded feature sets. 77
- Figure 44 TAD boundary enrichments and depletions. 81
- Figure 45 Compartment boundary enrichments and depletions. 82

Figure 46	Compartment and TAD boundary enrichment summary in three human cell types.	84
Figure 47	Distinct enrichments of CTCF and YY1 boundaries.	85
Figure 48	Repeat class average-o-grams over all TAD and compartment boundaries.	87
Figure 49	Significance and effect sizes of repeat class enrichments/depletions over boundaries.	88
Figure 50	Significance and effect sizes of repeat family enrichments/depletions over boundaries.	89
Figure 51	The AUC-RF stepwise algorithm finds that variable subset which maximises the AUROC on out-of-bag data.	90
Figure 52	Receiver operating characteristics for TAD boundary classifications.	90
Figure 53	Variable importance for boundary classification Random Forest models.	91
Figure 54	Calibration of metaTAD size selection bounds.	92
Figure 55	Large metaTADs show greater enrichments for an array of boundary features.	93
Figure 56	MetaTADs align with lain associated domains.	94
Figure 57	MetaTADs align with lamin associated domains.	95
Figure 58	MetaTAD boundaries much LAD boundaries much more often than expected by chance.	96
Figure 59	MetaTAD–LAD coincidence increases at higher levels of the metaTAD hierarchy.	97
Figure 60	Observed enrichments persist over a time series.	98
Figure 61	Genome-wide agreement between Giemsa bands and A/B compartments..	100
Figure 62	Giemsa-stain bands correspond to A/B compartments.	101
Figure 63	SHH–ZRS contacts occur within a stable TAD.	104
Figure 64	TSA treatment induces a strong ZRS–SHH interaction.	106
Figure 65	A stable ZRS–SHH interaction is coupled with reduced extraneous contacts.	107
Figure 66	The bait chromosome is enriched for 4C sequencing reads.	108
Figure 67	Inferred polymer trajectories of the ZRS–SHH region following TSA treatment in two cell lines.	111
Figure 68	Repeat simulations of 3D polymer trajectories in the <i>Shh</i> –ZRS region.	113
Figure 69	<i>Shh</i> –ZRS distance measurements from repeated 3D polymer simulations.	114

LIST OF TABLES

Table 1	Public Hi-C data used in this work.	17
Table 2	ChIP-seq and other public datasets used in this work.	20
Table 3	ENCODE datasets generated in the H1 hESC cell line and used in models of transcriptional output.	32
Table 4	Performance comparison of different modelling techniques.	73
Table 5	Performance comparison of full and optimised RF and ML models.	76
Table 6	4C sequencing library statistics.	108
Table 7	Measurement distances between ZRS and SHH in each inferred 3D structure.	110
Table A1	Gm12878 functional enrichments in regions of variable structure.	122
Table A2	H1 hESC functional enrichments in regions of variable structure.	123
Table A3	K562 functional enrichments in regions of variable structure.	124

LIST OF ACRONYMS

3C	Chromosome conformation capture (derivatives: 4C, 5C, Hi-C)
AUROC	Area under the receiver operating characteristic
CAGE	Cap analysis of gene expression
ChIP-seq	Chromatin immunoprecipitation following by high-throughput sequencing
DI	Directionality index
ENCODE	The encyclopaedia of DNA elements
ESC	Embryonic stem cell
FDR	False discovery rate
FISH	Fluorescent <i>in-situ</i> hybridisation
GC	Guanine and cytosine (content of a DNA sequence)
GO	Gene ontology
Hi-C	Genome-wide 3C experiment using high-throughput sequencing
HMM	Hidden Markov Model
ICE	Iterative correction and eigenvector expansion
IF	Interaction frequency
LAD	Lamin associated domain
MAD	Median absolute deviation
MSE	Mean squared error
NAD	Nucleolus associated domain
OOB	Out-of-bag
PCC	Pearson correlation coefficient
PCR	Polymerase chain reaction
PLS	Partial least squares

RF	Random Forest
RMSE	Root mean-squared error
RVS	Regions of variable structure
TAD	Topologically-associating domains
TSS	Transcription start site

PUBLISHED MATERIAL

Some materials contained in this thesis have previously been published in:

Moore BL, Aitken S and Semple CA (2015) Integrative modeling reveals the principles of multi-scale chromatin boundary formation in human nuclear organization. *Genome Biology*, **16**:100.
doi:[10.1186/s13059-015-0661-x](https://doi.org/10.1186/s13059-015-0661-x)

Parts of Section 5.4 are used in a submitted manuscript:

Fraser J, Ferrai C, Chiariello AM, Schueler M, Rito T, Laudanno G, Barbieri M, Moore BL, Aitken S, Morris KJ, Itoh M, Kawaji H, Jaeger I, Hayashizaki Y, Carninci P, Forrest ARR, FANTOM Consortium, Semple CA, Dostie J, Pombo A, Nicodemi M (2015) Hierarchical organization of chromosome folding and its re-organization underlies transcriptional changes in cellular differentiation. *Submitted*

I | INTRODUCTION

1.1 GENOME ORGANISATION

It's oft-stated that the DNA within each human cell would extend for two metres fully extended. Instead that same length of DNA packs into a cell nucleus with a diameter in the order of micrometers (μm). This is achieved through a complex organisation hierarchy, ranging from how chromosomes are arranged in the nucleus in territories, to nuclear interactions with the nucleolus or periphery, down to how DNA is wrapped around nucleosomes (for recent reviews, see [1,2](#)). While the biophysics of the latter level of organisation may be well understood, more broadly there is much still to learn about the guiding principles and functional importance of higher order chromatin organisation.

This introductory section will describe the current state-of-the-art in chromosome conformation capture experimental methods, as well as criticisms and considerations when interpreting these data, and discuss what is currently understood or theorised about the structure and function of higher order genome organisation. We compare competing models which attempt to recapitulate mechanisms of chromatin folding, and also explore some of the best understood organisational strata in mammalian higher order genome organisation.

1.1.1 C-methods and Hi-C

Classical studies of chromosome conformation relied on microscopy techniques to visualise nuclear architecture, most commonly fluorescence *in situ* hybridisation (FISH). These techniques led to the discovery of "chromosome territories", regions of the nucleus wherein distinct chromosomes were thought to occupy, and more broadly identified the non-random arrangement of loci in three-dimensional space.[\[3,4\]](#) Finer details of chromatin organisation, such as the proposed 30 nm fibre, were also introduced through microscopy-based techniques. Techniques such as FISH are powerful for precise inspection of single genes, but are low-throughput and offer limited resolution.[\[3\]](#)

With the advent DNA sequencing technology, new experimental methods emerged. Chromosome conformation capture (3C), introduced by Dekker *et al.*[\[5\]](#) was the first sequencing-based method of assaying nuclear architecture. The method uses formaldehyde to cross-link nuclear proteins in place, trapping genomic regions that were physically co-located through bound proteins, then to apply a frequent restriction

enzyme to shear the sample into fragments. Next, under dilute conditions, DNA fragments are ligated together. The dilute conditions favour ligations between fixed fragments, with the aim of generating hybrid fragments from two genomic regions which were close together in the original preparation. Cross-linking can then be reversed and, in the case of the original 3C method, measured by quantitative PCR using pre-designed primers for your fragments of interest. The end result is a relative measure of interaction frequency between any two regions of interest, in theory directly proportional to their distance in three-dimensional space.

The rapid advancement of sequencing, allowed the original 3C method to be further developed, first through microarray technology, then using high-throughput sequencing. Two protocols were proposed for a 3C-inspired one-to-many assay^[6,7] (both named 4C), whereby interactions were measured for a specific “viewpoint” fragment against all other restriction fragments genome-wide. The same year a many-to-many assay (5C) allowed measurements for all restriction fragments within a specified region.^[8]

The final step was an all-versus-all assay, capable of assaying pairwise interaction frequencies between all restriction fragments of a genome. This assay was published by Lieberman Aiden *et al.*^[9] and named Hi-C (Fig. 1). The Hi-C method added biotin tagging to pull-down only ligated fragments for sequencing. At the time of publication, resolution of Hi-C data for analysis was limited by sequencing depth, given the huge number of restriction fragments produced by a 6-cutter enzyme (HindIII and NcoI were used in^[9]) but the falling costs of sequencing and proven utility of the assay meant subsequent Hi-C papers incrementally increased their sequencing depth, to a point where analysis could be performed at the level of individual restriction fragments, genome-wide.^[10–13]

1.1.2 Hi-C variants

The interaction maps produced by Hi-C were found to exhibit several inherent biases. Fragment properties, such as their length, GC content and mappability, were confounding interaction frequency estimates and therefore needed to be normalised-away before subsequent analysis.^[14,15] A range of statistical techniques were developed to correct for these latent variables,^[16–19] while experimentalists instead looked to improve on the experimental procedure itself.

Tethered chromosome capture (TCC)^[20] was the first attempt to increase the signal to noise ratio of Hi-C contacts. In this method, ligations take place on a fixed surface, with the aim of preventing spurious ligations between fragments in solution which were not cross-linked. Kalhor *et al.*^[20] reported a large decrease in observed interchromosomal contacts in their tethered library, suggesting many of those originally observed were caused by spurious ligation of non-crosslinked fragments.

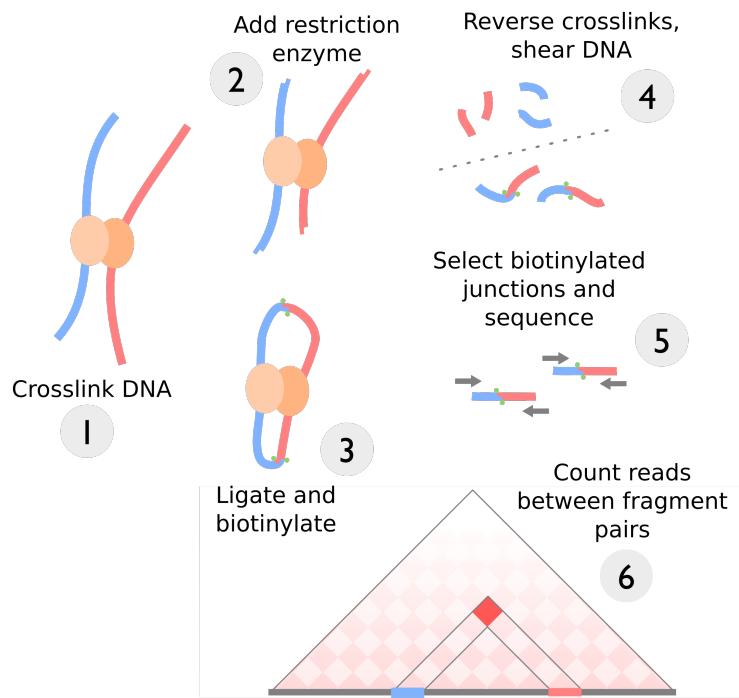


Figure 1: Steps in the Hi-C assay. Schematic of the Hi-C experimental procedure as described in Lieberman Aiden *et al.* [9]

Hi-C is a population-level assay, as the retrieved interaction counts are from a huge number of different cells. As well as building population-averaged models of genome structure, it is also of interest to probe cell-to-cell variability through single-cell approaches. For instance, it's been estimated that long-range contacts identified with C-methods may occur in as few as 10% of cells at any one time. [4]

In the first single-cell Hi-C study, Nagano *et al.* [21] aimed to explore this cell-to-cell variability by performing the Hi-C assay on single, hand-selected nuclei. An obvious limitation this Hi-C variant is that a single restriction fragment can ligate to at most one other fragment, meaning even if 100% yield were to be achieved, any $n \times n$ restriction fragment interaction matrix could at most populate $\frac{n}{2}$ cells; in practice, the realised yield of this first single cell Hi-C experiment was just 2.5%. [21] Nevertheless, single-cell Hi-C was able to reproduce findings from population-based (or “ensemble”) Hi-C, such as preferential interactions between active domains, but also was able to dissect *trans* interactions, suggesting high cell-to-cell variability leads to their relatively uniform appearance in normal Hi-C interaction maps. [21] Combined with observations from TCC which gave evidence that interchromosomal contacts were disproportionately the result of spurious ligation, [20] the functional significance of these *trans* interactions seems at best unclear in the general case.

Capture-C is a C-method variant which attempts to address resolution problems associated with the Hi-C genome-wide pairwise assay by enriching for functional

interactions using *a priori* selection of target loci.^[22] Indeed, a suggestion in the original Hi-C paper was that resolution could be improved by either increased sequencing or using hybrid capture.^[9] Since then, Hi-C variants with a target enrichment step have been developed, including Capture Hi-C (CHi-C)^[23] and HiCap.^[24] These methods have been applied to genome-wide target sets (e.g. CHi-C assayed 22,000 human promoters^[25]) and so it could be said that they are to Hi-C as exome-capture is to a whole-genome sequencing, in the contexts of conformation capture and variant discovery respectively.

In-situ Hi-C was a recent refinement of the Hi-C method, from the publisher of the original method.^[13] The principle difference is that fixation and ligation now happen in place, within intact cell nuclei, the result of which is a greatly improved noise profile with many fewer *trans* contacts.^[26]

1.1.3 Chromosome compartments

In the paper describing the Hi-C technique,^[9] Lieberman-Aiden *et al.* described low-resolution structures they name “A” and “B” nuclear compartments. These are regions with a median size of around 5 megabases which showed properties typical of euchromatin and heterochromatin, respectively. A compartments were observed through 3D-FISH to be centrally-positioned in the nucleus and ChIP-seq data showed several hallmarks of transcriptional activity. B compartments, conversely, were heterochromatic and lamina-associated regions, with little transcription and repressive histone modifications such as H3k9me3.^[3,9] As expected from positioning data, the co-location of compartment types is also visible in their contact maps.

These compartments were identified through a continuous eigenvector profile, derived from a normalised Hi-C contact matrix^[9] (Fig. 2). This approach can be intuitively understood as formulated by Lajoie *et al.*^[27]:

1. A tartan pattern on normalised Hi-C matrices indicates two preferentially-contacting compartments (Fig. 2).
2. Assume a function (c) that maps a given genomic bin to its compartment, using a positive number for compartment A and a negative for compartment B.
3. The interaction frequency between bins i and j is thus $c(i) \cdot c(j)$. (This is enough to generate a tartan pattern: if i and j are in the same compartment, the product will be positive.^[27])
4. Our symmetric Hi-C matrix thus contains $c(i)c(j)$ and in this formulation, principle components analysis is finding the basis that minimises the mean-squared error between $c(i)c(j)$ and $c(i)$.

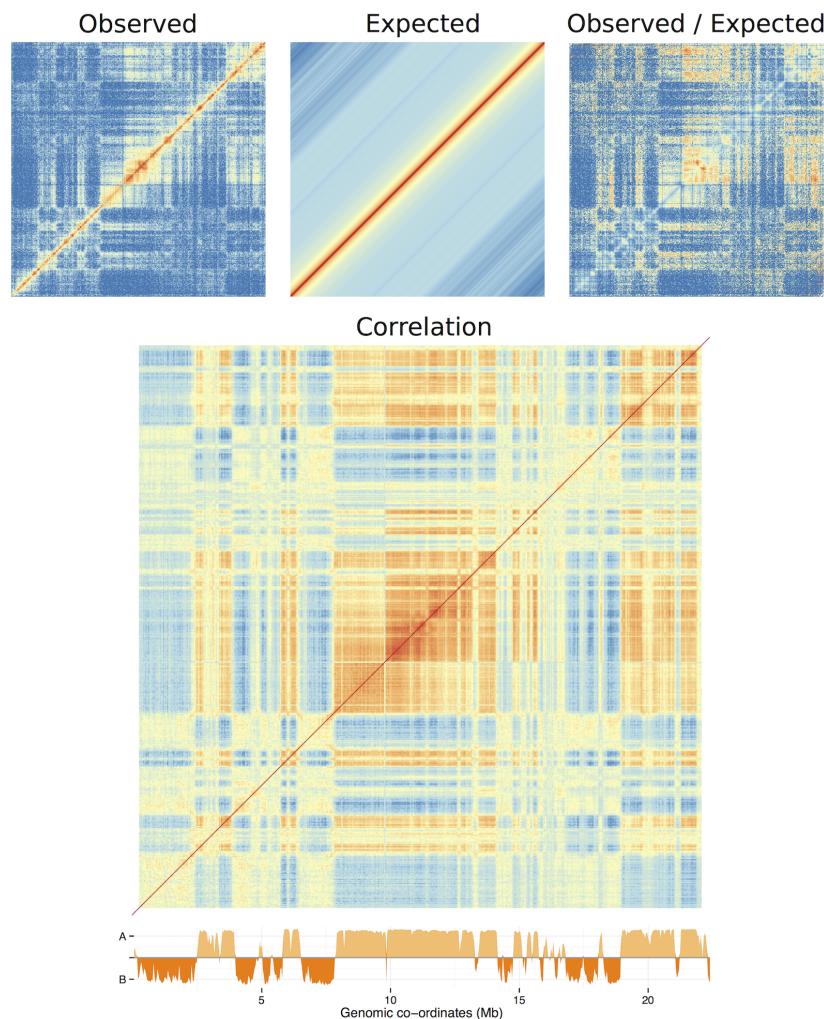


Figure 2: Derivation of A/B compartment profile from Hi-C data. Observed interaction frequencies (O) are averaged along super-diagonals to give a distance-normalised expected matrix (E). The Pearson correlation of the O/E matrix then can undergo eigenvector expansion; in most cases eigenvector v with the largest eigenvalue, λ , then reflects A/B compartmentalisation.^[9]

Importantly, this measure holds more information than a simple two-state classification, rather the continuous values can be interpreted as relative levels of compaction or activity.^[16,17]

1.1.4 Topological domains

The falling cost of high-throughput sequencing enabled increasingly deep sequencing of Hi-C experiments. Sequencing is the main resolution-limiting resource for this assay, as to increase the analysis resolution and maintain the level of coverage requires an exponential increase in the total amount of sequencing required.^[9,28]

In experiments totalling around two billion total sequencing reads, Dixon *et al.*^[10] produced Hi-C contact maps in human and mouse cell lines at 40 kb resolution. At the same time, Nora *et al.*^[29] published an even higher-resolution 5C dataset covering a 4.5 Mb region of the mouse X chromosome. In both of these studies, the authors note "topological associative domains" (or TADs) which were observable as self-interacting, off-diagonal blocks of higher-than-expected self-interaction frequency. With a mean size of around 1 Mb, TADs were recognised as a novel layer of higher order chromatin organisation at a level below the larger A/B compartments (Section 2.5.2). TADs have since been reported in a variety of metazoan organisms including dog,^[30] *Drosophila*^[31,32] and *C. elegans*^[33] yet comparable structures are not found in higher plants such as *Arabidopsis*^[34,35] or in yeast.^[36,37]

Dixon *et al.*^[10] defined a TAD calling algorithm based on the directional bias of a genomic region's contacts, and used a Hidden Markov Model to infer blocks of strongly up- or downstream-biased, reasoning that domain boundaries are present when a strongly upstream biased region is adjacent to a region of opposite bias (Fig. 3). These boundaries themselves were investigated and were found to display suggestive functional enrichments for DNA binding proteins including CTCF, long thought to act as an insulator of chromatin state (Section 1.2.3). Deletion of a CTCF site has been found to disrupt the corresponding TAD border, while removal of some other enriched factors had little effect.^[29,38,39] The authors also performed some comparative analysis, reporting large and significant overlap of domain boundary positions both within species and between human and mouse cell lines.^[10]

Since then, several studies have investigated the functional implications of TADs. A simple biological explanation is that TADs—by definition—delimit functional contacts, such as those between enhancers and promoters, and so could inhibit spurious contacts with other nearby genetic elements.^[2,40] Hormonal treatment of human breast cancer cells reported coordinated expression responses within TADs, suggesting they function as domains of transcriptional co-regulation called "regulons".^[41] However the size of TADs means they often span multiple genes, commonly with unrelated functions, so it seems unlikely they can function as regulons in the general case.^[1]

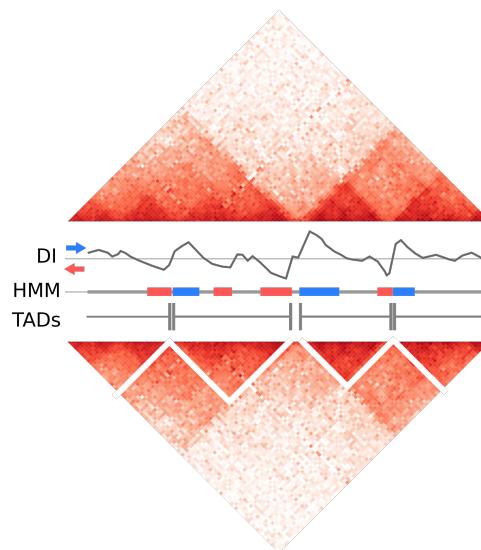


Figure 3: Dixon *et al.* pipeline for calling topological associating domains (TADs). First a directionality index (DI) is calculated for each bin based on the ratio of upstream:downstream contacts. Secondly a Hidden Markov Model (HMM) is used to infer the most likely state sequence that emitted the DI variable. Finally a simple rule is applied whereby a run of high-confidence upstream-biased state calls marks the end of a domain. New domains begin with any subsequent downstream-biased state. Gaps between TAD calls can be observed, and as labelled border regions up to a size threshold of 400 kb, whereafter those regions are unclassified.^[10]

1.1.5 Other proposed structures

Filippova *et al.*^[42] developed a tuneable algorithm which identifies "alternative topological domains". The authors use dynamic programming to search for an optimal set of non-overlapping boundary pairs that maximise intra-domain contacts. The algorithm includes a length scaling factor (γ) which is used to penalise domain size; by varying γ the authors define a subset of "multiscale domains" of heightened persistence across resolutions.^[42] These multiscale domains were found to be smaller, on average, than those previously reported by Dixon *et al.*^[10], despite being applied to the same Hi-C experimental data (mean size: 200 kb as opposed to \approx 1 Mb). However the domains of Filippova *et al.*^[42] show increased intra-domain contacts and stronger boundary enrichments relative to previously-described TADs, indicating this algorithm may generate a more accurate representation of topological domains in mammalian genome organisation. Intriguingly, this study also reports quantitative evidence for hierarchical genome organisation, finding that those domains called at large γ will then combine into larger meta-domains as the γ penalty decreases.

A study of *Drosophila* embryonic chromosomes found a similarly hierarchical organisation of physical domains, and also was able to relate these to "epigenomics domains" showing specific sets of enrichment signatures representing active, null, polycomb-associated and telomeric regions.^[31]

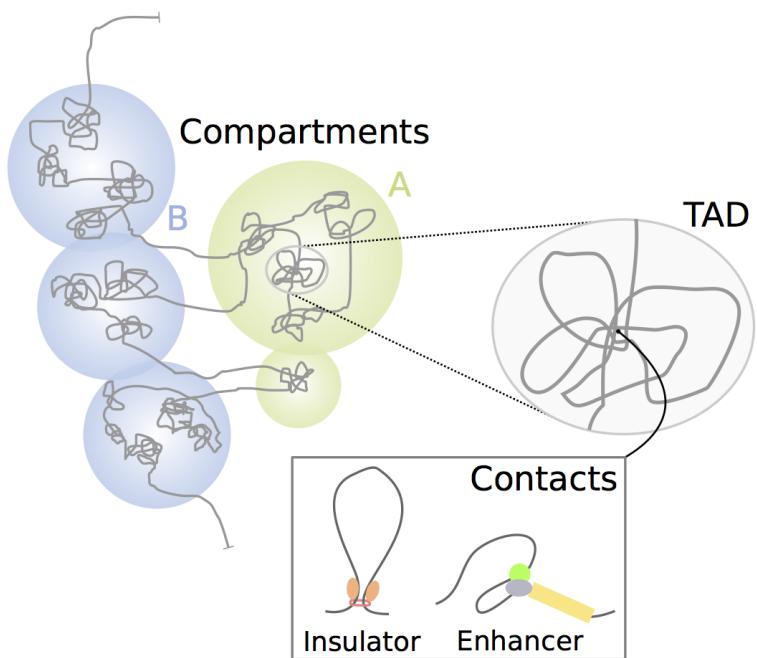


Figure 4: Levels of higher order chromatin organisation. Cartoon showing how functional contacts, such as loops between bound CTCF insulators (Section 1.2.3), occur within TADs (Section 1.1.4) which in turn are found within A or B compartments (Section 2.5.2).

Recent high-resolution studies have been able to resolve ever-smaller levels of sub-structure. Rao *et al.*^[13] refined the concept of chromosome compartments to “sub-compartments”, dividing simple A/B divisions into a total of 5 subtypes. The authors were also able to identify “contact domains” of median size 185 kb, many of which were associated with identifiable individual looping events (Section 1.2.3).^[13] This domain size is close to those of Filippova *et al.*^[42] (described above) and the authors here suggest that previously-observed large TADs may be the result of insufficient sequencing; that is, not all boundaries could be detected using 40 kb binned contact maps thus multiple contact domains were unintentionally combined into large domains.

1.2 MODELS OF CHROMATIN FOLDING

Theoretical mechanistic models of chromatin folding such as the “strings and binders switch” model^[43] and the “fractal globule” model^[9,44,45] have both produced simulated data that reflects empirical C-method observations and potentially describe the polymer dynamics of chromatin folding.

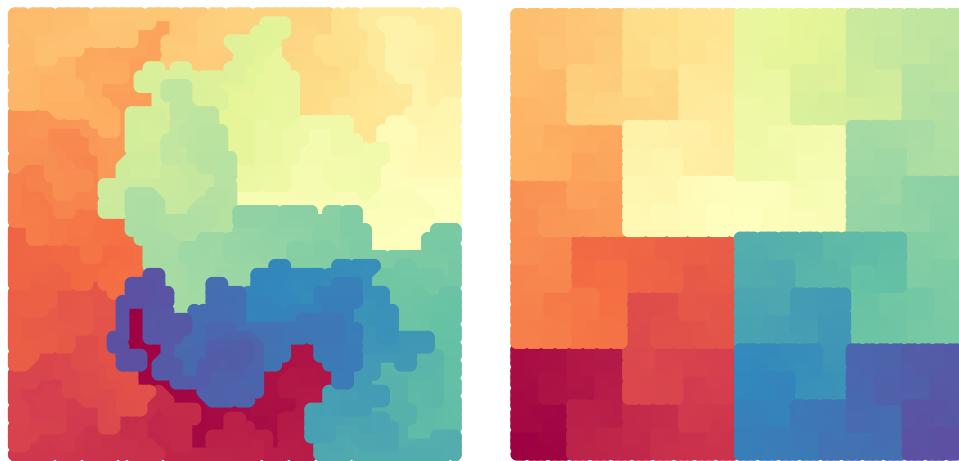


Figure 5: Comparison of theoretical models of chromatin folding. Two theoretical models of chromatin folding are shown simulated along a 2D polymer, coloured from start to finish as blue–green–red. An equilibrium globule is represented by a Hamiltonian path through a grid network (*left*) and is compared to a Fractal Globule, here represented by a Hilbert curve (*right*).

1.2.1 Fractal globule

Lieberman Aiden *et al.*^[9] tested a number of theoretical models of genome folding to see which best explained the observed power-law scaling between distance and observed contact frequency ($\text{IF} = \frac{1}{\text{dist}^{-\alpha}}$ where $\alpha \approx 1.08$). The authors sought to distinguish two previously-described models of genome organisation: the “fractal globule” and “equilibrium globule” (Fig. 5). The study found that a theoretical fractal globule, embodying scale-independent self-similar aggregate folding, better fit the observed data than an equilibrium globule null model where simulated polymer folding was allowed to proceed unchecked.

The fractal globule model was noted for its appealing functional properties. Under this model, for example, the polymer folds are knot-free hence could facilitate local dynamics of repression and activation without wider disruption. Despite this appeal, the authors were careful to state that while their simulations show good agreement with observed data, this does not preclude other organisational models from having similar or greater explanatory power.^[9]

1.2.2 Strings and binders switch

Subsequent modelling techniques integrated known biological phenomena as well as polymer models. This formed the basis of Barbieri *et al.*’s^[43] “strings and binders switch” (SBS) model, where the authors simulated polymer folding in the presence of DNA binding factors, such as the known genome organiser CTCF (Section 1.2.3).

This organisational model was developed in an attempt to consolidate global Hi-C measures of contact scaling with C-based experiments on smaller regions and FISH studies, which found a range of scaling parameters. The authors also explore the different values of α between cell lines and even chromosomes, and find that their mechanistic model can explain each case using variable concentrations of binders which causes phase-switching between open and compacted chromatin, with fractal globule existing at the phase transition boundary.

This model offers broad explanatory power for a range of observed power law coefficients (α) and from simple underpinnings, but critics point out that simulations were performed on a polymer composed of just 512 monomers so may not be broadly applicable.^[17]

1.2.3 Looping and CTCF

Examples have long been known of specific enhancer elements that are brought into close proximity with the promoter(s) they are regulating; under this model, these contacts form a "loop" structure between two potentially distal loci^[46,47] (Fig. 4). A model region, the β -globin locus and its locus control region (LCR) located 40-80 kb away,^[17] has been studied since the early 1980s,^[48–51] and is an interesting example of a well-characterised looping. Current knowledge suggests the β -globin forms loops with the multiple distal *cis*-enhancer elements which make up the LCR, together forming an active chromatin hub (ACH).^[52] Within such a hub, regulatory signals could be efficiently integrated to dictate the overall activity of the target locus.^[1,3] It is now thought that the majority of active promoters are engaged with multiple, often cell type specific, regulatory looping events.^[12,53]

A notable component of many long-range looping events is the CCCTC-binding transcription factor (CTCF),^[54,55] already mentioned as a component of TAD boundaries (Section 1.1.4) and as a proposed looping factor in the SBS model (Section 1.2.2). CTCF is strongly conserved in higher eukaryotes,^[56] ubiquitously expressed and embryonic lethal, but it is not tied to a single biological function — instead CTCF has been described as a "multivalent factor",^[55] capable of regulating transcription, imprinting, dosage-compensation and acting as an insulator.

In the context of genome organisation, CTCF is of interest for its role of anchoring interactions between loci, forming loops. Experimental evidence has shown that interactions between CTCF sites stabilises the aforementioned loops linking the β -globin locus with its distal LCR.^[57] This looping role, potentially undertaken in combination with other architectural proteins such as Mediator and cohesion,^[47,58] can explain its previously-identified insulator behaviour: CTCF can block the spread of heterochromatin and contacts between enhancers and promoter through topological constraints by forming loops.^[55] It must be said, however, that the functional significance of

CTCF-mediated loops, and indeed the role of CTCF in even well-studied systems, remains only partially understood.^[59]

A recent Hi-C paper, that of Rao *et al.*^[13], again brought CTCF and looping to the fore of chromatin conformation research. This study identified around 10,000 individual looping events in the human genome, almost all linking loci over distances of less than 2 Mb, and around 30% connecting predicted enhancer and promoter chromatin states. Rao *et al.*^[13] also found a 6-fold overall increase in expression when comparing those promoters participating in a looping event with those not. Furthermore, 86% of these loops involved CTCF bound regions, with roughly the same proportion involving cohesion subunits RAD21 and SMC3. The authors thus proposes that a CTCF-binding motif formed the "anchor" for this transitive complex of architectural proteins.^[13] A majority of these loops (65%) also demarcated a topological domain, and at much higher resolution than previously observed (Section 1.1.4). Another striking finding of this research was that CTCF loops almost always occur in between bound motifs with a convergent orientation,^[13] though questions remain over why this should be the case, especially when considering the interactions of a flexible polymer in 3-D solution.^[60]

While the evidence linking CTCF and genome architecture is substantial, it should be noted that from a global perspective as few as 15% of all CTCF ChIP-seq peaks were found to occur at TAD boundaries in human and mouse cells^[10] and similarly around 25% if TAD borders had no observable CTCF binding.^[40] These facts indicate that CTCF alone is neither necessary nor sufficient for the formation of higher order chromatin structures such as TADs. Indeed, the degree of insulation at a given genomic site was recently reported to correlate with the degree of co-binding of a range of architectural proteins including not only CTCF but cohesin, condensin and the transcription complex TFIIIC, among others.^[61]

1.3 CRITICISMS OF C-METHODS

C-methods are a relatively new and developing set of assays, especially compared to long-standing microscopy techniques which have for decades been used to visualise chromosome conformation. In this section, we discuss some of the limitations and issues with applying or interpreting the results of C-methods.

1.3.1 Cell populations

As previously mentioned (Section 1.1.2), the Hi-C assay typically takes place in a cell population (though proof-of-concept single-cell experiments have been reported^[21]). An obvious consideration, then, is that all interaction counts reflect the average over a

large number of cells, often including unsynchronised populations at different stages of the cell cycle.^[2] Given evidence that, while the interphase chromosomes exhibit cell-to-cell variability, the mitotic state is much more static,^[62,63] one might expect even a small proportion of dividing cells to add a detectable bias to averaged genome-wide contact maps.

1.3.2 Ploidy

A more esoteric consideration with C-methods data is that organisms under study are typically diploid, while maps of chromosome organisation are commonly collapsed onto a haploid pseudo-genome. Haplotype conformation can be delineated from C-methods data a variety of ways, such as using haploid cell lines (e.g. [13](#)) or via detectable sequence differences using either deep sequencing or a targeted area (e.g. [64](#)). An altogether different and inventive solution is to use the inherent proximity-ligation information produced by C-methods to discriminate haplotypes,^[11] an idea since extended to deconvolution problems in metagenomics.^[65,66]

1.3.3 Resolution

The resolution of a Hi-C experiment has a hard-limit imposed by the choice of restriction enzyme. For example, the commonly-used HindIII enzyme is a six-cutter that recognises the motif AAGCTT and cuts approximately every 4 kb, on average.^[3] This results in on the order of 10 million restriction fragments with a total pairwise interaction space of 10^{12} .^[27] The depth of sequencing required to cover this interaction space is cost-prohibitive, so in practice analysis takes place with data aggregated into bins of either fixed length or fixed number of restriction fragments.

More recent studies have switched to a four-cutter restriction enzyme, for example MboI,^[13] which increases this upper-bound on resolution to the order of hundreds of basepairs (e.g. theoretical mean fragment size of 422 bp in mouse^[24]), but again ultra deep-sequencing is required to realise such resolutions during analysis. A downside of using more frequent restriction enzymes is the potential side-effect of promoting more non-specific ligations by increasing the concentration of fragments in solution.^[13]

Realistically and in most instances, an experimental design may either target high-resolution interactions through targeted 4C or 5C, or low-resolution genome-wide interactions — but not both.

1.3.4 Biological interpretation

A key consideration with C-methods is that, when accurately stated, the assays are measuring “the frequency at which sequences are ligated together by formaldehyde

cross-linking”,^[67] which is then assumed to be a proxy for physical distance within the nucleus. This is a marked difference from aforementioned FISH methods, where the physical distance is observed directly, albeit through the addition of non-native probes. So strong is this assumption, that methods have been developed that use a known FISH distance to then calibrate genome-wide Hi-C distances,^[68] however it need not be the case that population-level interaction frequencies capture physical distance.^[27] Consider, for example, a tight enhancer–promoter interaction occurring in 50% of cells, but not at all in the other half. In this scenario, the two loci would have an intermediate interaction frequency overall, which is then converted to a distance measure that reflects the realities of neither cell sub-population. For similar reasons, the transience of an interaction cannot be directly inferred from its interaction frequencies: a weak interaction frequency may be the result of either the same fleeting contact in many cells, or stable contacts in only a subset of cells.^[27]

When interpreting C-methods data it should also be kept in mind that even verifiable contacts are by no-means functional. To elaborate, C-methods may find two regions to be strongly co-localised, but an understanding of the region may explain their co-localisation to be caused by mutual interaction with a nuclear lamina or nucleolus, for example, rather than any specific functional relationship between the two loci.^[17] In addition, a functional enhancer–promoter interaction will necessarily constrain the contacts of other nearby regions, potentially causing highly-reproducible “bystander interactions”^[17] that are nevertheless uninteresting from a functional perspective.

1.3.5 Other considerations

An additional and separate issue identified with C-methods, specifically β C in this instance, emerges from reports that the observed ligation frequency is as low as 1% of expected values in a model system,^[69] potentially magnifying the relative influence of noise and artefacts.

1.4 MACHINE LEARNING IN GENOMICS

Machine learning offers a powerful framework for understanding complex datasets, such as those produced in large-scale genomics studies. Problems in the field such as gene prediction and inferring regulatory networks can be approached by employing a learning algorithm, either in a supervised way based on a known truth set, or through unsupervised methods aimed at pattern detection or clustering (for reviews see [70,71](#)). If a successful predictive model can be built, it can then be dissected to explore statistical rules which may impart novel biological insight. As a toy example,

learning a highly-accurate model of enhancer prediction could itself identify novel epigenetic marks indicative of enhancers, generating testable hypotheses about how enhancers are activated.

In this section, we introduce recent and high-profile machine learning applications in the context of the ENCODE consortium, and give examples of how their vast datasets have empowered research groups worldwide to tackle complex biological questions through a variety of machine learning approaches. We then discuss research broadly aligned with the aims of this thesis, those attempting to advance an understanding higher order chromatin structure through machine learning and related techniques.

1.4.1 ENCODE

The Encyclopaedia of DNA Elements (ENCODE) is a consortium project started over a decade ago with the ambitious aim of comprehensively cataloguing all functional elements in the human genome.^[72-74] This project involves huge amounts of data production from a diverse array of experimental methods, such as: ChIP-seq, DNase-seq, RNA-seq, CAGE, DNase-seq and ChiA-PET.^[75] Importantly these methods were applied to a range of human cell types, including many well-studied immortalised cell lines as well as primary cells and tissues, and according to standardised experimental methods^[76] coupled with statistical quality control^[74,77,78] to ensure data is comparable between different data produces and of consistently-high accuracy. Despite ENCODE's human-focus, there also exists spin-off projects aimed at building similar genomics resources for mouse^[79] and, more recently, *Drosophila* and *C. elegans*.^[80] Together these data sources offer an unparalleled resource for comparative and within-species genomics research, and as such have been used in at least 1200 publications to date.^[81]

Data generated by ENCODE consortium members has a proven utility in genomics research. Notably two ENCODE-associated groups have released models which classify the human genome into discrete "chromatin states", such as actively transcribed regions or gene promoters. The first, named SegWay, trained a dynamic Bayesian network on 31 ENCODE-generated input variables and called an unsupervised 25-state genome segmentation in the ENCODE pilot region.^[82] Independently another chromatin state predictor named ChromHMM was developed.^[83,84] As the name suggests, this approach instead used multivariate Hidden Markov Models (HHMs) and has the capability to learn a single generative model over multiple cell types. Original runs of the model called 51 chromatin states using over 40 input features,^[85] but more recently these two methods were combined to call a consensus set of just 7 chromatin states.^[86] Since their publication, a study was able to experimentally validate many of these state predictions.^[87] This discretisation of the chromatin landscape greatly helps

interpretability, at the cost of simplifying the complex underlying data series, and is used for this reason later in this work (Section 3.6.1).

More broadly, ENCODE data has been used by external researchers to generate input variables for machine learning-based predictive models which describe transcriptional output,^[88] gene regulation,^[89] cell cycle-associated genes^[90] and enhancer identification^[91] to name but a few. One such study in particular, that of Dong *et al.*^[92], is reproduced and further analysed in this work (Section 4.2) and is used as a template for our own machine learning framework applied in the context of higher order chromatin structure (Chapter 4). We also make use of ENCODE data in other chapters (e.g. Chapter 5) due to its comprehensive coverage of model human cell types and stringent data production guidelines referenced above.

1.4.2 Related work

In this thesis we will be applying machine learning and other forms of statistical analysis to gain a greater understanding of the biological underpinnings of higher order chromatin conformation (introduced in Section 1.1). We shall now consider existing and overlapping works, some of which were published after or during the time that the research presented herein was performed.

1.5 AIMS

In the broadest terms, the aims of this work are to investigate the relationship between structure and function of the genome. In particular, we aim to answer the following questions:

1. How does higher order chromatin structure compare across cell types?
2. Can we predict higher order chromatin structure from locus-level features?
3. How do the characteristics of boundaries marking higher order domains vary between cell types and domain classes?

In an attempt to address these questions, we will bring together the huge volumes of data generated by the ENCODE consortium (Section 1.4.1) and employ machine learning techniques and other statistical analysis to explore how these locus-level features relate to higher order chromatin structure.

2 | METHODS

2.1 HI-C DATA

2.1.1 Mapping

Raw Hi-C reads were downloaded from published datasets (Table 1) through the Gene Expression Omnibus (GEO)^[93] or the Short Read Archive (SRA)^[94] with identifiers: GSE35156 (H1 hESC), GSE18199 (K562) and SRX030113 (GM12878). These paired reads were mapped independently to a reference genome: hg19/GRCh37 for human data, and mm10/GRCm38 for mouse.

Mapping was performed using the hiclib software package^[16] and bowtie2^[95] with the --very-sensitive flag. An iterative mapping approach was used to maximise the number of aligning fragments.^[16] Each fragment end was aligned first using short terminal sub-sequences. Those unmapped or with ambiguous mapping were then taken forward into the next iteration and extended until the entire fragment end had been aligned. Those remaining pairs with one or more unmapped ends were discarded.

This approach is designed to maximise uniquely-alignable fragment ends, while avoiding mismappings caused by crossing the fragment junction.^[27]

2.1.2 Filtering

After mapping, interactions are first aggregated into restriction fragments then by regular binning of various resolutions (particularly 40 kb, 100 kb and 1 Mb). Several filters were applied at this stage, with the following cases removed:^[16,27]

- Reads directly adjacent to a restriction enzyme site (within 5 bp)
- Identical read pairs (presumed PCR duplicates)

Table 1: Public Hi-C data used in this work.

Cell line	Total reads	Accession	Citation
Gm12878	31×10^6	SRX030113	20
H1 hESC	331×10^6	GSE35156	10
K562	36×10^6	GSE18199	9
Cortex	373×10^6	GSE35156	10
mESC	476×10^6	GSE35156	10
IMR90	355×10^6	GSE35156	10

- Very large restriction fragments (> 100 kb) which are likely from a repetitive or poorly-assembled region
- Extremely over-represented fragments (top .05%) which may throw-off eigenvector derivation

2.1.3 Correction

Iterative correction and eigenvector expansion (ICE) is an approach to normalisation and processing Hi-C data, implemented as software library written in python.^[16] The iterative correction algorithm performs matrix balancing with the aim of generating a doubly stochastic matrix from raw interaction counts.^[27] That is, such that symmetric matrix \mathbf{A} has both row and columns of equal sum. In practice, this effectively enforces “equal visibility” of each fragment, correcting for previously-described biases in interaction recovery such as GC-content and fragment length^[14] but without explicitly modelling these latent variables. This procedure is thus converting actual interaction counts into normalised interaction frequencies (IF), and to relative rather than absolute quantities. Scaling of IFs permits comparison of Hi-C experiments with very different sequencing depths (as is the case in this work, see Table 1). Despite differences in the levels of sequencing, otherwise the experiment methods underlying the produced Hi-C data were similar: the HindIII restriction enzyme was used in each case and the Hi-C protocol was largely unchanged (that is, we did not consider data from Hi-C variants such as TCC^[20] and *in-situ* Hi-C^[13]).

2.1.4 Eigenvector calculation

Additional functionality provided by ICE is the eigenvector expansion of normalised contact maps. Eigenvectors from observed/expected matrices were chosen for consistency with Lieberman Aiden *et al.*,^[9] as opposed to the related eigenvectors calculated in Imakaev *et al.*^[16] from the corrected maps alone. The details of this procedure are described in section 2.5.2. Briefly, observed contacts (O) are divided by an expected matrix (E) which is generated by averaging the super- and sub-diagonals of the O matrix. That is, the E matrix gives the expected value of interactions at a given distance.

Importantly, the first two principle components (PCs) were calculated, and that with the highest absolute Spearman correlation with GC content is taken to reflect A/B compartmentalisation. PC eigenvectors were then orientated to positively correlate with GC, ensuring positive values reflected A compartments and negative values B compartments. Another subtlety is the calculation of eigenvectors per chromosome arm as opposed to per chromosome, this prevents issues with some meta- and submetacentric chromosomes where the first principle component indicated chro-

mosome arms.^[9,16] Eigenvector expansion was performed on both 1 Mb and 100 kb matrices, below these resolutions results became less stable, and besides it has been shown that eigenvectors at higher resolution — when they do indeed capture A/B compartmentalisation — add little, if any, additional information.^[96]

2.1.5 TAD calling

TADs were called using the software provided in Dixon *et al.*^[10] and their recommended parameters. This method is introduced in Section 1.1.4 (see also Fig. 3) but will be described here in greater detail.

The TAD calling algorithm is a multi-stage process. Firstly, a statistic called the "directionality index" (DI) is calculated for each bin.^[10] The equation for calculating the DI of a given bin is shown (Eqn. 1), where U represents the sum of reads mapped up to 2 Mb upstream of a given 40 kb bin, and D likewise for downstream contacts. Here E is the expected number of downstream or upstream contacts (equal under the null hypothesis), hence is $E = \frac{U+D}{2}$.

$$\text{DI} = \left(\frac{U - D}{|U - D|} \right) \left(\frac{(D - E)^2}{E} + \frac{(U - E)^2}{E} \right) \quad (1)$$

Equation 1 can be intuitively understood as first determining the direction of the bias (the sign is given by $\frac{U-D}{|U-D|}$) and then calculating the extent of the bias (with $\frac{(D-E)^2}{E} + \frac{(U-E)^2}{E}$ being akin to a χ^2 -type statistic).^[10]

This DI metric could be used as-is to call domains. Peaks of downstream contacts culminating in a peak of upstream contacts would delineate self-interacting domains. However, Dixon *et al.*^[10] instead use a hidden Markov model (HMM; Methods 2.3.3) in a manner similar of that we later employed to call compartments (Section 2.5.2).

Here, the DI metric is considered a noisy observation emitted by an unobserved underlying three-state sequence of upstream, downstream or no- directional contact bias.^[10] The HMM was fit to each chromosome with between 1 and 20 Gaussian mixtures allowed per state, however in some cases the expectation-maximisation (EM) algorithm used to parameterise these hidden states failed to converge; such cases were ignored. The Akaike information criterion (AIC) was used to selection the optimal number of mixtures (in practice, we found 5–10 were selected).

Finally, given a fully-specified HMM we can calculate the posterior probability of a given state in a specific bin, using the forward-backward algorithm and given its observed data and preceding state sequence. Dixon *et al.*^[10] enforce the heuristic that regions are only classified as downstream- or upstream-biased if the state is called for two consecutive bins, or if a single bin has an especially high posterior probability ($\geq .99$). Domains are called from this state sequence and run from an

initial downstream-biased bin through to the last in a run of ≥ 2 of upstream biased states. This procedure was implemented by Dixon *et al.*^[10] in Matlab.

2.2 ENCODE FEATURES

Genome-wide ChIP-seq datasets for: 22 DNA binding proteins and 10 histone marks were made available by the ENCODE consortium^[74,77] along with DNase I hypersensitivity and H2A.Z occupancy, for each of the Tier 1 ENCODE cell lines used in this work: H1 hESC, K562 and GM12878. These data were pre-processed using MACSv2^[97] to produce signal fold-change relative to input chromatin. In most cases a paired input control was generated per cell type and by the same laboratory as that which performed a set of ChIP-seq experiments.^[77] GC content was also calculated and used in the featureset to give 35 total inputs (Table 2).

Table 2: ChIP-seq and other public datasets used in this work.

Histone modifications	DNA binding proteins	Other
H3K27ac, H3K27me3, H3K36me3, H3K4me1, H3K4me2, H3K4me3, H3K79me2, H3K9ac, H3K9me3, H4K20me1	ATF3, CEBPB, CHD1, CHD2, CMYC, CTCF, EGR1, EZH2, GABP, JUND, MAX, MXI1, NRSF, POL2, P300, RAD21, SIX5, SP1, TAF1, TBP, YY1, ZNF143	DNase, GC content, H2A.Z

2.2.1 Clustering input features

To quantify collinearity of input features, correlation matrices built from genome-wide vectors of input feature measures were build and hierarchically clustered. The “significance” of observed clustering was assessed using sub- and super-sampled bootstrapping, with stable clusters deemed significant, as implemented in the *pvclust* R package.^[98]

2.3 MODELLING COMPARTMENT EIGENVECTORS

2.3.1 Random Forest

Random Forest (RF) regression,^[99] was used as implemented in the R package *randomForest*.^[100] The RF algorithm (Fig. 6) makes use of a collective of regres-

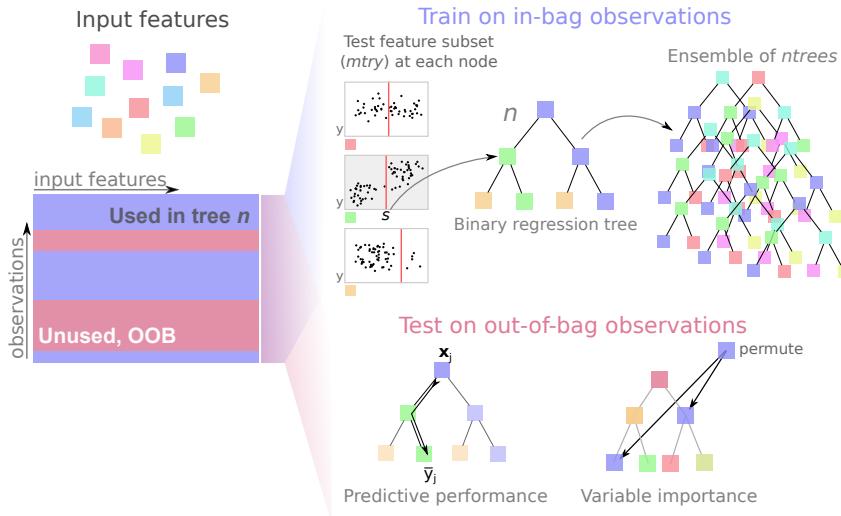


Figure 6: Random Forests overview. Random Forests are an ensemble of bagged, de-correlated classification or regression trees first described by Breiman.^[99]

sion trees (size $ntrees$), each built from a bootstrapped sample of the training set. In growing each tree, a small number of variables ($mtry$) is tested at each bifurcation node, and that which minimises the variance in child node subsets is selected at a specific threshold. Having trained a group of trees, these can then be used as predictive tools by inputting a vector of features to each tree and averaging the output leaf node value across the forest. RF regression was used as it is known to be one of the most powerful regression methods developed to date,^[101,102] typically providing low bias and low variance predictions without the need for variable selection.^[103,104]

Additionally the RF method represents an example of “algorithmic modelling”^[105] in that it makes no assumptions about the underlying data model. Parameters of $mtry = \frac{n}{3}$ (where n is the number of input features) and $ntrees = 200$ were assumed as they are known to be largely insensitive;^[104,106] this was verified with the dataset used in this work (Fig. 7).

Variable importance within Random Forest regression models was measured using mean decrease in accuracy in the out-of-bag (OOB) sample. This represents the average difference (over the forest) between the accuracy of a tree with permuted and unpermuted versions of a given variable (Fig. 6), in units of mean squared error (MSE).^[102,104]

2.3.2 Model performance

The effectiveness of the modelling approach was measured by four different metrics. Prediction accuracy was assessed by the Pearson correlation coefficient between the OOB predictions and observed eigenvectors, and the root mean-squared error

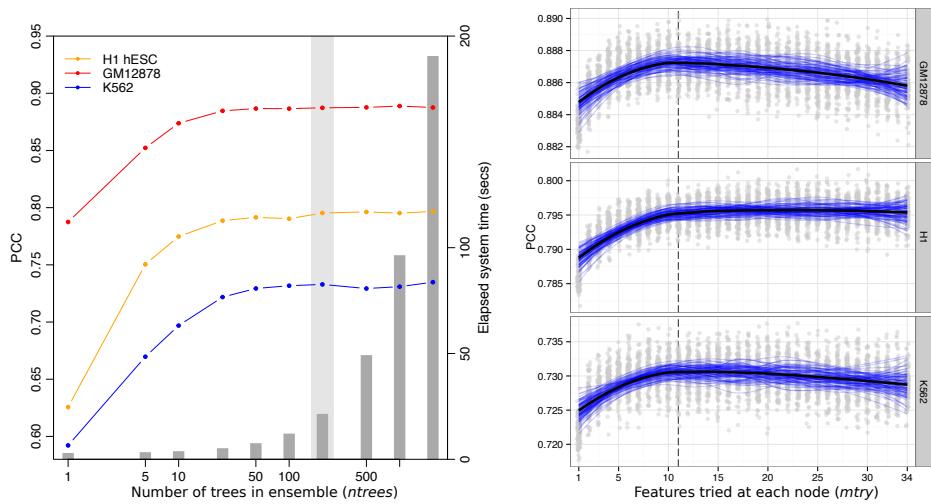


Figure 7: Random Forest parameters are largely insensitive. Two user-facing Random Forest parameters are known to be insensitive over a broad range.^[106] Optimisations for *ntrees* (the number of trees in the forests) and *mtry* (the number of features tested at each node) are shown for three different models, with typical values of 200 trees and $\frac{1}{3}$ of input variables highlighted.

(RMSE) of the same data. Classification error, when predictions were thresholded into $A \geq 0; B < 0$, was also calculated using accuracy (% correct classifications or True Positives) and area under the receiver operating characteristic (AUROC) curve. Together these give a comprehensive overview of the model performance, both in terms of regression accuracy of the continuous eigenvector, and in how that same model could be used to label discrete chromatin compartments.

For cross-application of cell type specific models, a single Random Forest regression model was learned from all 1 Mb bins for a given cell type. This was then used to predict all bins from each of the other two cell types.

To test the sensitivity of the models to resolution, we also applied cell-type specific models learnt at 1 Mb resolution to input features binned at 100 kb. This was done by training a Random Forest regression model on all available 1 Mb bins in a given cell type, then applying that model to the prediction of all compartment eigenvectors derived at 100 kb. Model performance was then assessed as above, with the caveat that here the test set represents a higher-resolution window onto the original training set, therefore we might expect this to inflate the measures of generalisation error.

2.3.3 Hidden Markov models

Hidden Markov models (HMMs) are used both for calling TADs (Methods 2.1.5) and for identifying chromosome compartments (Methods 2.5.2, discussed in Section 3.4.1). Here we briefly introduce the HMM framework in general terms.

HMMs are widely used in computational biology, and have been called "the Legos of computational sequence analysis"^[107] due to their wide applicability. HMMs provide a probabilistic modelling framework to explore any system that can be reduced to a 1D state sequence.^[108,109] In the discrete case, each state in this sequence is capable of "emitting" one of a number of symbols, each with its own probability. In the continuous case, used in this work, instead a state has an associated emission distribution which can be a simple univariate Gaussian or a more complex mixture model. After an emission, each state has a number of "transition" probabilities, where the sequence can either change to another state or remain in the same state.

A typical representation of an HMM is shown in Equation 2, where hidden states (θ) emit a sequence of observed states (y).^[110]

$$\begin{array}{ccccccc} \dots & \longrightarrow & y_{i-1} & \longrightarrow & y_i & \longrightarrow & y_{i+1} \longrightarrow \dots \\ & & \uparrow & & \uparrow & & \uparrow \\ \dots & \longrightarrow & \theta_{i-1} & \longrightarrow & \theta_i & \longrightarrow & \theta_{i+1} \longrightarrow \dots \end{array} \quad (2)$$

HMM state emission and transition parameters can be learned from an observation sequence via the Baum-Welch algorithm,^[111] a special case of the Expectation-Maximisation algorithm applied to HMMs. Following initialisation of transition and emission matrices (this can be random), the Baum-Welch algorithm first performs the *E*-step, calculating the expected number of transitions and emissions via a Forward-Backward procedure, then the *M*-step re-estimates transition and emission parameters based on these expected values. These two steps repeat until the HMM parameters converge to a local maximum.

Given a fully-specified HMM, the Viterbi algorithm can be applied to find the most probable state sequence given a sequence of observations.^[112] Using the notation of Equation 2, the Viterbi algorithm finds $\hat{\theta} = \operatorname{argmax}_{\theta} \Pr(y, \theta)$ using dynamic programming.^[110]

2.3.4 Stepwise regression

Stepwise regression is a form of model selection used with multiple regression. This simple approach starts with a complete model and serially remove and/or add variables, then calculate a metric (here we use the Bayesian information criterion, BIC) which weighs the the model likelihood against model complexity. This process is iterated until the metric reaches a (local) minimum, thus creating a more parsimonious model which retains predictive accuracy and should be less prone to overfitting. Stepwise regression also aids interpretation by selecting representative features from collinear clusters.^[113]

It should be noted that despite its continued widespread usage, several statistical issues have been identified with the stepwise procedure for model selection.^[114,115]

2.3.5 LASSO

The least absolute shrinkage and selection operator (LASSO) is a form of ℓ_1 regularisation that penalises the sum of absolute values of standardised regression coefficients. By penalising absolute values and sums, rather than squared values as in ℓ_2 regularisation (Ridge regression, for example), coefficients can be shrunk to 0 thereby removing terms from the model. Thus the LASSO combines coefficient shrinkage of techniques like Ridge regression with a type of feature selection by promoting model sparsity.^[106,116]

Simply put, the LASSO minimises the sum of squared errors subject to a tuneable constraint on the sum total of absolute model coefficients. In equation form, we are fitting a simple linear model:

$$\hat{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n \quad (3)$$

or $\hat{y} = \mathbf{X}\boldsymbol{\beta}$

We then wish to find that $\boldsymbol{\beta}$ which minimises $\sum_{j=1}^n (\hat{y}_j - y_j)^2$ while at the same time satisfying the inequality:

$$\sum_{i=1}^p |\beta_i| \leq c \quad (4)$$

Where here c represents a tuneable parameter inversely proportional to the level of regularisation imposed on the model. It can be seen, for example, that if c is set to the sum of the coefficients fit by ordinary least squares, the LASSO solution will be equivalent. Eqn. 4 can be contrasted with Ridge regression, where the same inequality instead constrains $\sum_{i=1}^p \beta_i^2$.

Formally, the LASSO problem has been expressed as:^[106]

$$\hat{\boldsymbol{\beta}}^{\text{lasso}} = \arg \min_{\boldsymbol{\beta}} \left\{ \frac{1}{2} \sum_{i=1}^N (y_i - \beta_0 - \sum_{j=i}^p x_{ij} \beta_j)^2 + \lambda \sum_{j=1}^p |\beta_j| \right\} \quad (5)$$

This formulation introduces the λ parameter as used in Section 4.6.2. This parameter translates β coefficients, such that larger values of λ place stronger constraints on the coefficient total, thus encourage greater shrinkage and model sparsity (Eqn. 5).

In this thesis, we used the `glmnet` R package to fit LASSO models.^[117,118] In order to select λ , we use a 10-fold cross-validation approach on a separate held-out training set. We chose that λ which produced a mean cross-validated error within 1 standard error of the minimum, thus favouring a sparser model than the global minimima.

2.3.6 Other modelling approaches

Linear regression was used as a baseline for comparison with more complicated approaches such as Random Forest. If the same modelling accuracy could be achieved with simple multiple linear regression, this would be a faster and more interpretable modelling framework.

Partial least squares (PLS) regression was also used to model compartment profiles. PLS regression is well-suited to highly correlated inputs, employing a dimensionality reduction step to help address this redundancy, yet lacks the interpretability of a multiple linear regression. Similar to RF, PLS regression is aimed at building highly-predictive models rather than understanding singular relationships between a predictor and independent variable.^[119] The `plsdepot` R implementation of PLS regression was used in this work.

2.4 VARIABLE REGIONS

2.4.1 Stratification by variability

Median absolute deviation (MAD) was chosen as a robust measure of the variability in a given 1 Mb block between the three primary cell types used in this work: H₁, K₅₆₂ and GM₁₂₈₇₈. Blocks were ranked by this measure and split into thirds that represented “low” variability (the third of blocks with the lowest MAD), “mid” and “high” variability. Each subgroup was then independently modelled using the previously-described Random Forest approach.

“Flipped” regions are those whose compartment state differs in one cell type relative to the other two. For example, if a 1 Mb bin was classified as “open” in H₁ hESC and “closed” in both K₅₆₂ and GM₁₂₈₇₈, this is said to be a “flipped” compartment (to open).

2.4.2 Chromatin state enrichment

Chromatin state annotations used in this work were retrieved from the ChromHMM^[83] and SegWay^[82] combined annotations.^[86] These represent the consensus from two independent chromatin state prediction algorithms, and ignore regions of apparent disagreement; hence in theory making more robust and conservative predictions than either algorithm independently. Nevertheless, Hoffman *et al.* caution that in areas of disagreement, each algorithm may highlight differing biological phenomena so should also be considered separately.^[86]

The set of state predictions from the combined algorithms are:

1. Predicted transcription start sites (TSS)
2. Promoter flanking regions
3. Transcribed regions
4. Repressed regions
5. Predicted enhancers
6. Predicted weak enhancer or *cis* regulatory element
7. CTCF-enriched elements

Short, discrete state predictions such as enhancers were considered “shared” if there was an overlapping enhancer annotation in either of the two other cell types, and labelled as “tissue-specific” otherwise. This was repeated for each of the called chromatin states.

2.4.3 Gene ontology analysis

Variable regions (section 2.4.1) were tested for functional enrichments using Gene Ontology (GO) annotations.^[120] The DAVID tool^[121] was used to compare GO terms for genes located in variable compartments with a background set of genes within all annotated compartments.

2.5 BOUNDARIES

2.5.1 TAD boundaries

Having called TADs (Section 2.1.5), we then have a set of boundaries at the start and end of each domain. We generated average boundary enrichment or depletion profiles by averaging input features into 50 kb bins spanning ± 450 kb from the boundary bin.

To test for the enrichment or depletion of a chromatin feature over a given boundary, a two tailed Mann-Whitney test was used to compare the boundary bin with the ten outermost bins of the window (5 from either side). The significance level at $\alpha = 0.01$ was then Bonferroni-adjusted for multiple testing correction, and results with p -values exceeding this threshold were deemed significantly enriched or depleted at a given boundary.

To compare boundaries between cells, each TAD boundary called in K562 and GM12878 were compared with those called in H1 hESC. For each boundary, the minimum absolute difference to the nearest matching boundary in H1 hESC was recorded, and this was then compared with a null model of an equal number of

boundaries randomly-placed along available bins. A Kolmogorov-Smirnov test was then used to compare the empirical cumulative distributions of these distances.

2.5.2 Compartments

Eigenvectors were calculated as described in section 2.1.4. A/B compartmentalisation has previously been called simply from the properly-orientated principle component eigenvector, with positive values representing a bin in an A compartment state, and negative values representing a bin in a B, more repressive state.^[9]

Compartment boundaries were called by first training a two-state hidden Markov model (HMM) on the compartment eigenvector and then using the Viterbi algorithm to predict the most likely state sequence that produced the observed values (Methods 2.3.3). Justification for this approach is discussed in Section 3.4.1 and we also note the similar use of an HMM in TAD calling (Section 2.1.5).

The point at which transitions occurred between states was taken as a boundary which was then extended ± 1.5 Mb to give a 3 Mb window in which a boundary was thought to occur. Boundary enrichments and alignments were tested in the same manner as TADs (Section 2.5.1).

2.6 PREDICTING TAD BOUNDARIES

2.6.1 AUC-RF

To predict TAD boundaries we used a classification Random Forest model, built with the AUC-RF algorithm,^[122] as implemented in the AUCRF R package. This is a form of stepwise model selection which optimises feature subset selection relative to the area under the receiver operating characteristic (AUROC), a metric which captures both the speciality and sensitivity of a classifier hence is better-suited to unbalanced datasets than previously-described RF variable selection methods that used simple classification accuracy.^[103,123] The AUC-RF procedure has been successfully applied in other bioinformatics applications, such as identifying a subset of most relevant variants in a genome-wide association study.^[124]

More specifically, the AUC-RF algorithm is a backwards elimination procedure, commencing with variable ranking by importance. In these classification RF models, mean decrease in Gini impurity (Methods 2.6.2) was chosen as the measure of variable importance, as it proved to be more stable than mean decrease in accuracy on permuted data.^[122] Regardless, impurity and permutation-based importance measures are thought to be largely consistent in many cases.^[100,106]

Steps in the algorithm can be summarised as:^[122]

1. Train an RF classifier using all available variables and calculate variable importance
2. Remove the least important 10% of variables and fit a new RF model
3. Calculate the AUROC on predictions made with out-of-bag data
4. Iterate steps 2–3 until a single variable model is built
5. Select that model with the highest AUROC

Importantly, AUC-RF avoids some of the problems of stepwise regression. Both over-optimistic model performance (due to repeated training and testing on the same pool of data) and errors due to the instability of variable rankings are mediated through an additional cross-validation step.^[122]

The input feature set for this model was made up of the same 35 ENCODE features used in models of compartment eigenvector (Methods 2.2), with the addition of counts of Alu repeat elements (as used in Section 5.2.2). TAD boundary bins were called as previously described (Methods 2.1.5) and were resolved to 40 kb. Bins containing a TAD boundary were our true positives (TP), and to generate true negatives (TN) we took matched bins 450 kb upstream of each boundary bin. Of these, a randomly-selected 80% of TP/TN pairs were used as our training and validation set in each cell type, while the remaining 20% of cases were held-out as independent test sets.

2.6.2 Gini importance

The Gini impurity, G , of a single node containing some proportions of n classes of variable is calculated as shown (Eqn. 6), and is observably related to the concept of entropy or information gain.

$$G = \sum_{i=1}^n p_i(1 - p_i) \quad (6)$$

In our simple two-class setting (i.e. boundary, b , or non-boundary), this simplifies to Equation 7. Here it can be seen that a G of 0.5 means the node contains a 50 : 50 split of class labels, whereas a node of 95% boundaries has a much lower impurity ($G = 0.095$).

$$G = 2p_b(1 - p_b) \quad (7)$$

To convert the impurity into a measure of importance, we compare G of a parent node with that of its two daughter nodes (G_{d_1} and G_{d_2}), following a partition on a given variable of interest.

This decrease in Gini impurity can then be summed over all splits in which a specific variable has been selected per tree (N_{used}), and the averaged over all trees in the forest ($ntrees$). This approach is described in Equation 8.

$$I = \frac{1}{ntrees} \sum_{ntrees} \sum_{j=1}^{N_{used}} G_j - (G_{d_1} + G_{d_2}) \quad (8)$$

2.7 METATAD ANALYSIS

MetaTADs are a conceptual level of genome organisation discovered by collaborators in the Pombo lab. Their method for calling metaTADs involve the constrained hierarchical clustering of those neighbouring TADs with the greatest inter-TAD contacts. This pairing was recursed up to the level of whole chromosomes, thus resulting in a tree of increasing metaTAD aggregation.

2.7.1 Size selection

For boundary analysis of metaTADs, again a similar approach was used to that of TADs (Section 2.5.1) but thresholded to within a given range of sizes. MetaTADs below 10 Mb were excluded, as to have no lower bound results in $\frac{2}{3}$ of all TAD boundaries likewise considered MetaTAD boundaries, reducing the power to analyse any differences. 10 Mb was chosen in an attempt to compromise minimising the overlap between TAD and metaTAD boundaries, while also retaining a large enough sample size. An upper bound of 40 Mb was also chosen, as beyond this threshold inter-TAD contacts were found to be no higher than expected by chance. In practice, the tree-like structure means any upper-bound has little impact as a filter: in almost all cases, any boundary in a metaTAD of size > 40 Mb will also fortaliam metaTADs below this value. Additionally, the hierarchical nature of metaTADs means that some boundaries are present at multiple levels of the tree. Only one case of each boundary position was tested for feature enrichments, and this was performed as with TAD boundaries (Section 2.5.1).

2.7.2 Collaborator datasets

Our collaborators in the metaTAD project performed ChIP-seq experiments for PolIII (three variants), H3K27me3, CTCF and DNase-I hypersensitivity. Mapped reads from these experiments were processed using MACSv2^[97] to give relative signal over background (from an estimated local model), which was then averaged over all boundaries genome wide.

Cap analysis of gene expression (CAGE) data was produced by the FANTOM consortium.^[125,126] This method produces sequencing data from the 5' end of cDNAs, and can be used to quantify expression activity at precise promoter locations.^[127] Here, CAGE was performed at multiple points along a neural-differentiation timecourse and tags were clustered to form CAGE TSS (CTSS) in a manner developed for the FANTOM5 project.^[125] To count these CTSS over boundary bins, we simply intersect the annotations and count CTSS per bin using bedtools.^[128]

Gene density over metaTAD boundaries was calculated using UCSC mm9 gene models.^[129] Again simple intersections were taken to count genes over boundaries using bedtools^[128] and requiring a minimal overlap fraction of 0.5% of a bin (250 bp).

2.7.3 LAD coincidence

To compare metaTAD boundaries with those of LADs, we made use of previously-published Lamin-B1 DamID microarray probe intensities. Peric-Hupkes *et al.*^[130] For analysis over boundaries, these values were averaged into the same boundary windows as used previously (50 kb bins \pm 450 kb around boundary, as in Section 2.5.1).

Transitions between high and low lamina association were detected by fitting a linear regression model across each series of consecutive boundary bins (i.e. Lamina assoc. = $\beta \cdot \text{bin} + c$). Linear models which had an absolute coefficient $|\beta| > .05$ were taken as crossing a LAD transition. This threshold is a heuristic which appears to perform well at conservatively selecting clear transitions. As a method of seriation for the *y*-axis of heatmap figures (e.g. Fig. 57), boundaries were divided into those that coincided with a lamin transition and those that did not, and members within each group were then sorted by average intensity.

To test the significance of the association between boundaries and lamin transitions, we circularly permuted both TAD and metaTAD boundaries on each chromosome 1000 times, and calculated the proportion of boundaries that crossed LAD boundaries using the same linear regression procedure described above. Empirical *p*-values were then calculated as the number of permuted results greater than or equal to the observed value.

2.8 GIEMSA BAND COMPARISON

Cytogenic band data and Giemsa stain results were downloaded from the UCSC genome browser (table cytoBandIdeo). The genomic co-ordinates are an approximation of cytogenic band data inferred from a large number of FISH experiments.^[131]

To compare G-band boundaries with our compartment data, we allowed for a ± 500 kb inaccuracy in G-band boundary. For each G-band boundary, the minimum absolute distance to any compartment or TAD boundary was calculated for each cell type. To generate a null model, ...

2.9 NUCLEAR POSITIONING

Previously published data on chromosome positioning preference within the nucleus was used to label each chromosome as “inner”, “middle” or “outer”.^[132] Chromosomes whose DAPI hybridisation signals were significantly enriched ($p \leq 2 \times 10^{-2}$) in the inner nuclear shell, as defined by Boyle *et al.*^[132], made up the “inner” group and included chromosomes 1 and 16. Similarly the “outer” group had enriched signals ($p \leq 5 \times 10^{-3}$) in the outer shell relative to the inner nuclear shell and included chromosomes 2, 3, 11-13 and 18. The remaining chromosomes in our filtered dataset, 6, 14 and 15, were assigned to the “middle” group and showed no significant to either inner or outer nuclear shells ($p \geq 0.1$).^[132] The significance of the difference in distribution of eigenvectors in the inner versus outer shell was determined by a two-sided Kolmogorov-Smirnov (K-S) test, with the alternative hypothesis that the empirical cumulative density function of the inner chromosome eigenvectors F_{inner} was not equal to F_{outer} . This chromosomal positioning data was measured in lymphoblastoid cells though nuclear architecture is thought to be largely conserved between cell types^[133,134] and even higher primates,^[135] so should be comparable in this instance.

2.10 MODELLING TRANSCRIPTIONAL OUTPUT

2.10.1 Reproducing a published study

In Section 4.2 we reproduce and extend a previously published study by Dong *et al.*^[92]. In doing so, we reuse much of the code and materials made available by the authors and more widely the ENCODE consortium^[74], of which this paper was a part. Some scripts were extracted from the ENCODE virtual machine, designed to provide an environment in which to reproduce their main findings.^[75]

Input features for models of transcription were derived from the January 2011 ENCODE data freeze.^[74] Normalised ChIP-seq signals were generated by ENCODE using `wiggler` and retrieved for this study as `bigWig` files. These were averaged into 40×100 bp bins across each GENCODE v7 TSS, to give ± 2 kb windows around each start site. These bins were then used to find the ‘bestbin’, that which correlates best with transcriptional output on a training subset of TSS. A bin representing the average intensity over the whole gene (TSS to TES) was also considered. That which best

correlated on a training set was then used as the representative region for that feature in subsequent modelling steps.^[92] The justification for this approach is discussed in Section 4.2.1.

2.10.2 Predicting FANTOM5 data

We transferred this transcriptional modelling approach to what was at the time novel, unpublished CAGE data produced by the FANTOM consortium. This data has since been released in the FANTOM5 series of publications.^[125]

We used H1 hESC t_0 CAGE data from a differentiation timecourse study, as generated by FANTOM5 members. The consortium pre-processed raw CAGE tags into clusters using decomposition-based peak identification.^[125] To filter for gene-associated CAGE clusters, we discarded those tag clusters centered on a point > 50 bp from an Ensembl (v69) annotated TSS, thereby removing enhancers and other non-genic transcribed regions. When multiple clusters were linked to the same TSS, that with the highest peak was kept. Expression was matched with ENCODE ChIP-seq data for the H1 hESC cell type (processed as described in Section 2.10.1) and an additional measure of replication timing.

Input data for models of FANTOM5 CAGE are shown in Table 3.

Table 3: ENCODE datasets generated in the H1 hESC cell line and used in models of transcriptional output.

Histone modifications	Other
H3K27ac, H3K27me3, H3K36me3, H3K4me1, H3K4me2, H3K4me3, H3K79me2, H3K9ac, H3K9me3, H4K20me1	HDAC6, DNase I, H2A.Z, Input

2.11 4C ANALYSIS

For computational analysis of 3C-seq data (also known as 4C), the experimental protocol used by our collaborators recommends the r3Cseq R package,^[136,137] part of the BioConductor repository^[138,139] for the R programming environment.^[140]

This package produces normalised interaction frequencies which are comparable between experiments and then assigns statistical significance to any identified contacts, thereby reporting regions that co-localise to a greater degree than expected by their genomic proximity alone.

2.11.1 Normalisation

The normalisation procedure for 4C data is adapted from a previous method for normalising deepCAGE data between samples.^[141] In short, the reverse-cumulative distribution of read counts per restriction fragment is fit to a power-law model; this effectively encodes the *a priori* expectation of exponential decay of the number of contacts as distance increases from the viewpoint. Transformed read counts per million (RPM) can then be retrieved from a standardised reverse cumulative distribution, parametrised with the empirical coefficient, $\alpha = -1.35$.^[137]

This normalisation procedure has the effect of making the output RPM value independent of the original experiment's sequencing depth and, more importantly, acts to reduces the impact of artefacts and errors by enforcing the expected power-law relationship of restriction fragment read counts.

2.11.2 Significance estimation

The r3Cseq package^[137] also attempts to assign a measure of significance to observed contact frequencies. This is done through a simple method of background estimation based on observed values. The justification for this non-independent estimate of background signal is that a relatively small proportion of observed contacts are expected to be significantly enriched, thus won't unduly perturb an average signal.^[137] An improved method that avoids this assumption has since been developed where a background model was iteratively fitted, with outlier removal at each revision.^[142]

Here a non-parametric cubic smooth spline is fit to normalised read count data using a heuristic smoothing parameter. This model then provides an expected level of interaction at a given distance from the viewpoint in *cis*. From this, it is simple to calculate a Z-score as:

$$Z = \frac{(O - E)}{\sigma} \quad (9)$$

Where σ is the standard deviation of residuals from the observed (O), expected (E) difference. This Z-score can then be converted to a p -value which in turn is corrected for multiple testing using bootstrapped estimates of false-discovery rate (FDR) q -values^[143] (as implemented in the qvalue R package^[144]). This Z-test approach assumes a normally-distributed test statistic, an assumption that typically does not hold on 4C data where interactions distal to the viewpoint are increasingly sparse, however this approach and variants thereof have been applied in a variety 4C and 5C analyses (e.g. 7,33,53,145–147). Some publications (e.g. 29) use a more appropriate distribution to assign p -values to the Z statistic, such as the Weibull (extreme value) distribution.

While we are mostly concerned with these *cis* interactions, r3Cseq also offers significance testing for *trans* interactions between the viewpoint and restriction fragments on different chromosomes. Here instead of distance scaling, the expected (E) terms in Equation 9 are genome-wide averages excluding regions ± 100 kb around the viewpoint.^[137] This means the absolute values of normalised RPMs reported for *trans* interactions are in practice upscaled, being equivalent to experimental RPMs less the most deeply-sequenced regions, i.e. the viewpoint and immediately adjacent regions.

2.12 SCRIPTS AND OTHER ANALYSES

Much of this work has been performed by writing custom scripts in the R programming language.^[140] Code for the majority of analyses described in this thesis are available through a public git repository hosted on github at github.com/blmoore/3dgenome (instructions on how to reproduce analyses and figures are included therein). A special mention goes to the packages of Hadley Wickham which are used throughout, especially `ggplot2`^[148] and `dplyr`^[149].

The programming language python^[150] was also employed to a lesser-extent, as were command-line tools such as `bedtools`^[128] and `SAMtools`^[151]. Additionally command-line BigWig* tools^[152] were used, as well as the UCSC genome browser associated data tracks.^[153–155]

3

REANALYSIS OF HI-C DATASETS

3.1 INTRODUCTION

Since the initial publication of the Hi-C technique in 2009,^[9] there has been rapid advancement of both the technique itself and the resolution at which interaction frequencies have been analysed. From the proof-of-concept analysis at 1 megabase (Mb) and 100 kilobase (kb) resolution,^[9] subsequent experiments achieved resolutions first of 40 kb^[10], then 10 kb^[12] and most recently 1 kb,^[13] enabling bona fide genome-wide fragment-level analysis for the first time.

Such rapid progression in the field has resulted in a wide variety of public Hi-C datasets being available, albeit with differing qualities. With proper correction and at a suitable resolution, these interaction frequencies can be compared and contrasted both within and between species.

In this chapter we uniformly reprocessed publicly-available human Hi-C datasets in order to address fundamental questions about the stability of higher order genome organisation between cell populations from the same species. Previously Hi-C studies have compared across two samples, such as K562 against GM06990^[9] or IMR90 against GM12878.^[10] Here we make use of three Hi-C datasets corresponding to extensively-studied human cell lines: K562, GM12878 and H1 hESC. Together these make up the “Tier 1” cell lines studied by the ENCODE consortium,^[74] hence have huge amounts of matched ChIP-seq and histone modification data available.

By combinatorial reanalysis of these cell-matched datasets, we can comprehensively investigate the quantitative relationships between higher order chromatin structure and locus-level chromatin features.

3.2 HI-C REPROCESSING

Each Hi-C dataset used in this work was reprocessed from raw sequencing reads using the same pipeline (Methods 2.1). Briefly, raw sequencing reads were sourced from three different publications: Lieberman-Aiden *et al.*^[9], Dixon *et al.*^[10] and Kalhor *et al.*^[20]. These reads were mapped to human genome build hg19 using an iterative mapping procedure that maximised the number of uniquely mappable reads from each sample (Methods 2.1.1).

Next a filtering step was applied, which removed those fragment pairs that were likely artifactual or erroneous (Methods 2.1.2). A correction step was then applied,

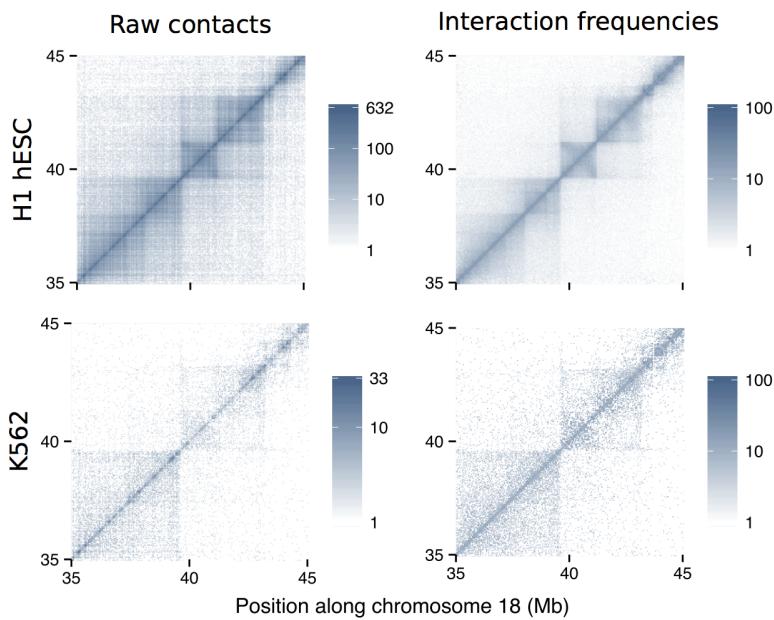


Figure 8: Iterative correction converts raw counts to normalised interaction frequencies. The sample with highest sequencing depth (H1 hESC) is shown alongside that with much lower sequencing (K562) both before and after iterative correction and normalisation procedures were applied (Methods 2.1) at 40 kb resolution for a 10 Mb section of human chromosome 18. Fill gradients are on a \log_{10} scale.

whereby biases such as mappability and GC content were removed to give each fragment equal visibility (Methods 2.1.3). Overall these steps produced comparable maps of interaction frequency in different cell types, despite their differing origins (Fig. 8).

Figure 8 shows a 10 Mb region of chromosome 18 before and after filtering and normalisation in two different cell types. Self-interacting domains visible in the deeply-sequenced H1 hESC cell type also become more visible in the K562 cell type after normalisation. In addition many of the long-range and intra-domain contacts visible in each raw contact map are down-weighted during the normalisation procedure, indicating their prominence was enhanced by biases or other sources of noise in the experimental procedure (Fig. 8).

The relative sparsity of the K562 Hi-C contact map compared to that of the H1 hESC cell line should also be noted (Fig. 8). At the time much of this study was performed, deeply-sequenced Hi-C datasets for cell lines K562 and GM12878 were not available, thus the majority of analyses were performed at a lower resolution of 1 Mb to further reduce the impact of variable sequencing depth between cell lines (Methods 2.1).

3.3 COMPARTMENT PROFILES

After uniformly reprocessing each Hi-C dataset and calling compartment eigenvector profiles (Methods 2.1.4), we can compare these between three human cell lines. We find compartment profiles have a striking concordance (Fig. 9), despite the variable sources of both sample material and experimental data. This strong correlation of higher order chromatin structure (at the level of compartments) between three very different human cell types shows that genomic regions appear to be constitutively present in either the A or B compartments regardless of cell lineage.

This close correspondence also validates our approach of combining these different datasets, and suggests our uniform pipeline is successfully accounting for differences in sequencing depth and other batch effects. The pairwise Pearson correlation coefficients between these independent measures are all in the interval [.75,.8] (Fig. 10). Also of note is that each cell type independently shows a similar bimodal distribution of compartment eigenvector, indicative of the two distinct underlying A/B compartment states (Fig. 10).

3.4 DOMAIN CALLS

3.4.1 Compartments

The continuous compartment eigenvector is most commonly used as-is to classify A/B compartments by thresholding based on sign: typically the eigenvector is orientated such that positive values reflect A compartments and negative values B compartments.^[9,20] However, given compartments are understood to be generally broad and alternating domains along a chromosome, often aligning with other large domains such as LADs, an improved classification method might penalise the calls of very short compartment calls, which may be the result of noise. For this reason, instead of using raw eigenvector values we consider observed values as emissions from unobserved underlying states (Fig. 11). We built a hidden Markov model (HMM; Methods 2.3.3) to represent these states through a well-described probabilistic framework.^[107]

Firstly we designed the HMM to have two unobserved states with univariate Gaussian distributed emissions (representing our A and B compartments; Fig. 12). To parameterise these states we used the iterative Baum-Welch algorithm, an Expectation-Maximisation procedure designed for HMMs. Having parameterised the HMM for each cell type, we then use the Viterbi algorithm to infer the most likely state sequence to have generated our observed data. This two-state sequence is then used to assign compartment identities to genomic bins. A schematic of this procedure is shown in Figure 11.

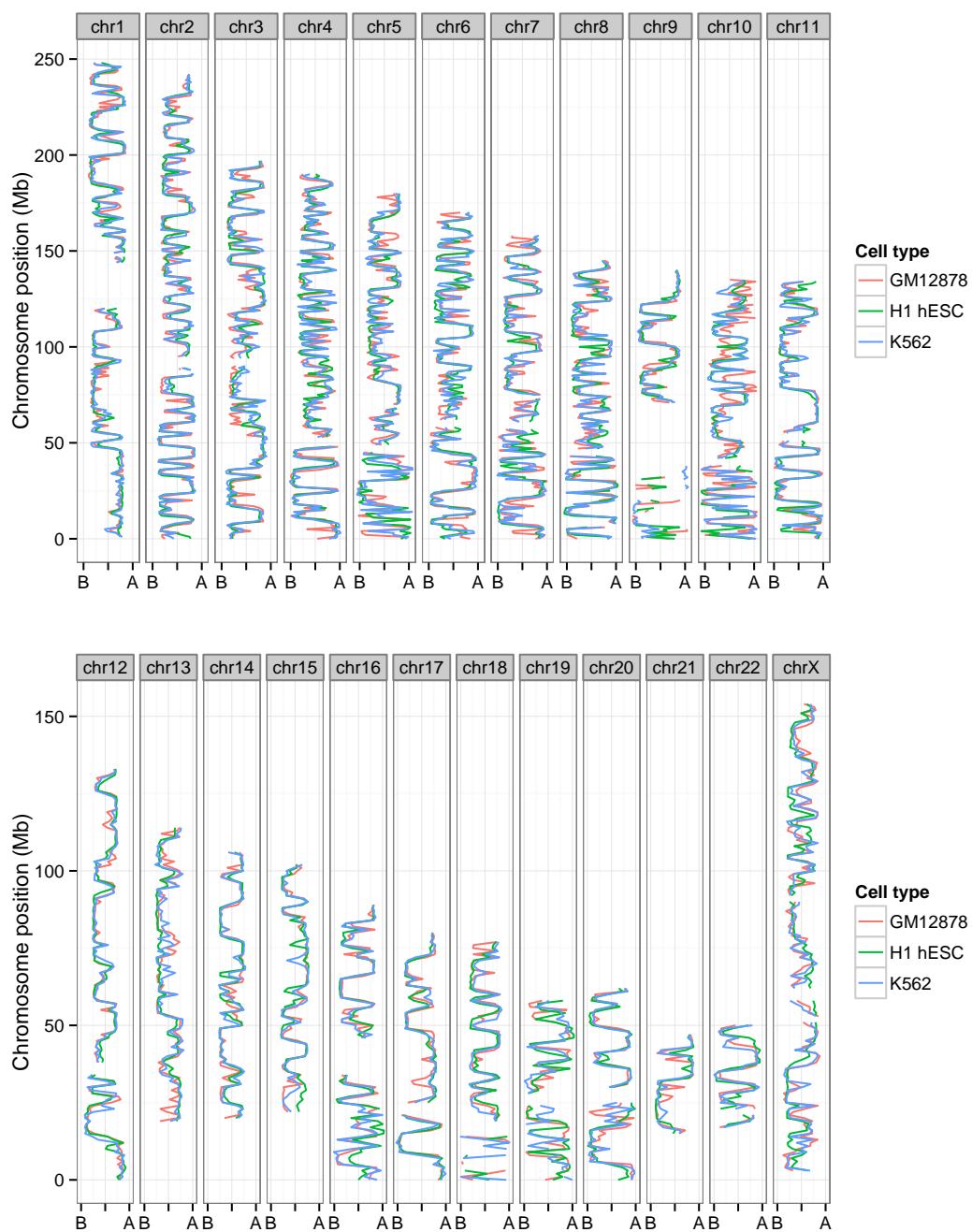


Figure 9: Compartment profiles are observably well-correlated between human cell types and across all chromosomes. Compartment eigenvectors are plotted along the lengths of each human chromosome (chrY and chrM are omitted) displaying strong concordance between three different human cell types.

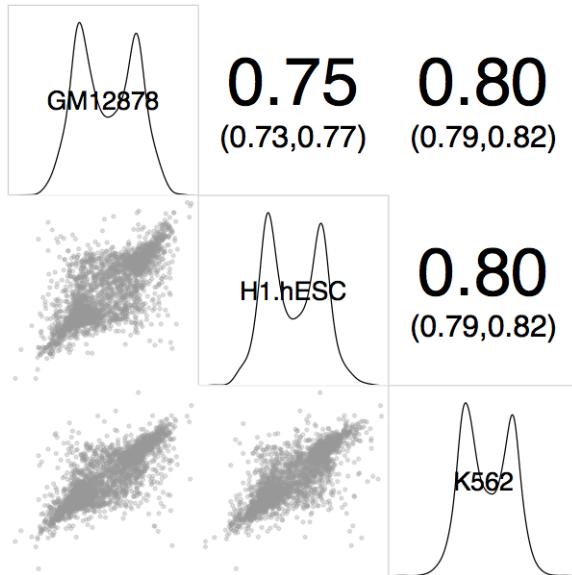


Figure 10: Compartment eigenvectors are highly correlated between human cell types. Megabase resolution compartment eigenvector values are shown in a plot matrix. *Upper triangle*: Pearson correlation coefficients between pairs, with 95% confidence intervals; *diagonal*: Kernel density estimates of eigenvector values per cell type; *lower triangle*: x - y scatterplot of values.

In practice, this acts to de-noise our compartment calls. Whereas single sign-changes along the series would (under a thresholding procedure) have resulted in a single-block compartment, these may now be modelled as noisy emissions from a single unobserved state. An exemplar region is shown in Fig. 13. This shows an approximately 50 Mb region from chromosome 8 with eigenvector data from the H1 hESC cell line. A simple thresholding method in this region calls a total of 12 regions, whereas our HMM method finds only 6 larger regions in the same window. The disparity is caused by very short and single-bin compartments being disfavoured by the HMM-based method (e.g. Fig. 13).

Having called compartments we can compare their properties across cell types. In each case, a majority of chromosome compartment sizes are in the range 0–10 Mb, with a handful of compartments reaching up to 40 Mb in size (Fig. 14). Median sizes for compartments called in this work match those reported previously, with a median size of around 5 Mb.^[17] Our slightly larger mean compartment sizes (up to 7.6 Mb in H1 hESC) may be due to our altered domain calling procedure (Fig. 13) and is clearly influenced by some large outliers (Fig. 14).

Next we compare compartments between the three cell types under study. To do this, we calculate the minimum absolute distance from each boundary in one cell type against those in a designated comparison cell type (we used H1 hESC). The cumulative distribution of this boundary differences is shown (Fig. 15) and compared to a null distribution of random compartment boundaries. We find boundaries are

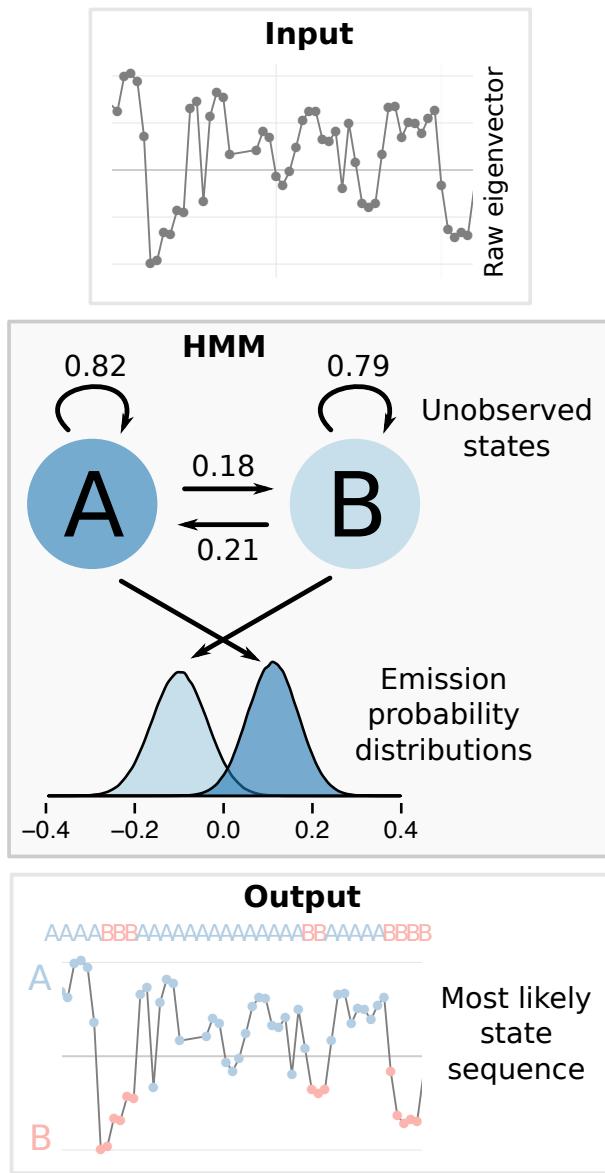


Figure 11: Overview of HMM method for compartment calls. Schematic of HMM method for compartment calls, showing transition and emissions distributions learned in the GM12878 cell type. A description of HMMs is given in Methods 2.3.3. Emission distributions for each cell type are shown in Figure 12.

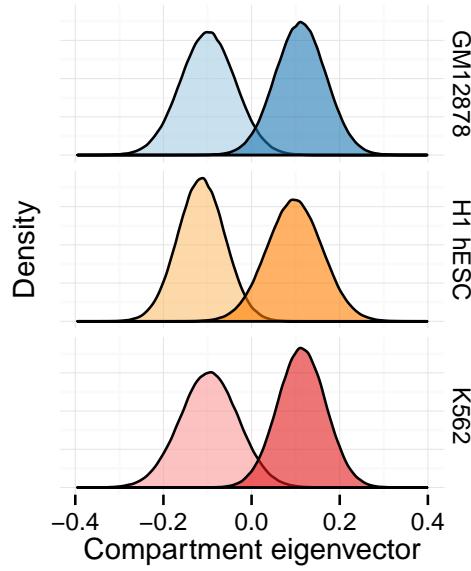


Figure 12: Univariate Gaussian emission distributions for A and B unobserved HMM states. Probability distributions for compartment eigenvector values per HMM state are shown for each cell type. Distributions centred below zero (lighter colours) show the distribution for the B compartment state, distributions centred above zero (darker) represent the A compartment state.

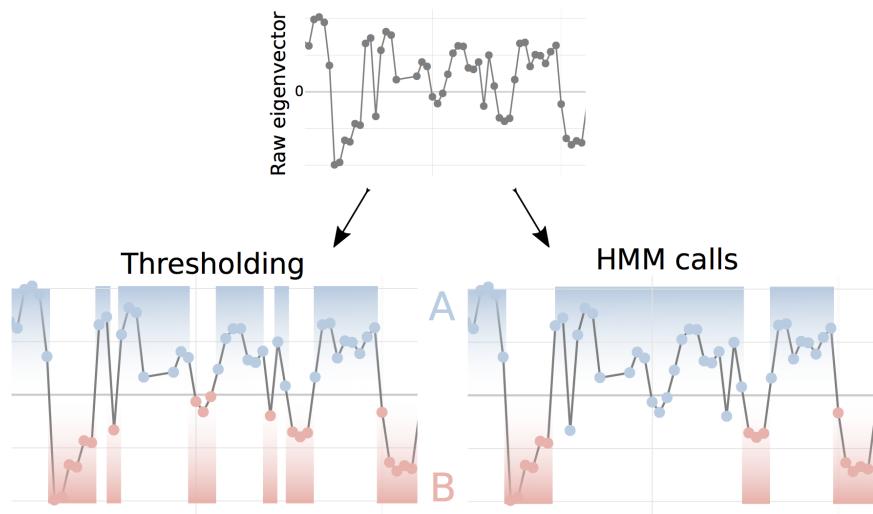


Figure 13: Compartment calls by simple thresholding method or context-aware HMMs. Chromosome compartments have previously been called through simple thresholding at 0,^[9] in this work we also use an HMM-based method to call unobserved states that have emitted our noisy observed values (*right*).

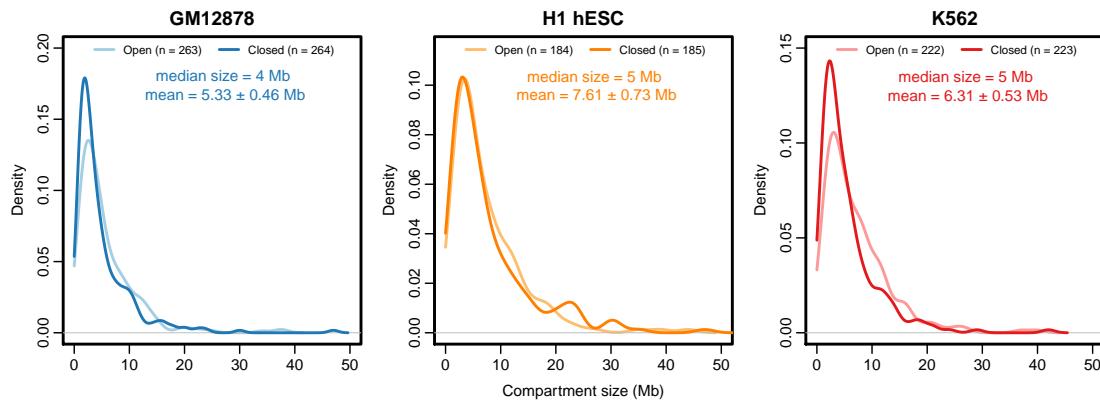


Figure 14: Size distributions of compartment calls in three human cell types. Kernel density estimates of compartment sizes (Open: A; Closed: B) are shown per cell type with summary statistics (*inset*), including mean compartment size with 95% confidence intervals.

significantly more closely aligned across cell types than is expected by chance. For example, genome-wide approximately 37% of compartment boundaries in H1 hESC have a corresponding boundary within 100 kb in GM12878 (and 35% in K562, but only 5% in random boundaries). Comparisons of the cumulative boundary distance distributions yield statistically significant differences relative to the null model (K-S test, K562: $D = 0.47$; $p \approx 0$; GM12878: $D = 0.49$; $p \approx 0$; Fig. 15).

3.4.2 TADs

Topological associating domains (TADs) are self-interacting blocks of the genome first described by Dixon *et al.*^[10]. We applied the original TAD calling method without modification, which uses a measure of the directional contact bias of a fragment (Section 1.1.4 and Fig. 3).

The Dixon *et al.*^[10] method of calling TADs relies on the detection of boundaries,^[13] thus is affected by sequencing depth: experiments with sparser contact matrices may not contain enough for a sufficiently high degree of bias to allow a boundary call. This is evident in our datasets even after normalisation, with the deeply-sequenced H1 hESC cell type having approximately 50% more TADs called than in the GM12878 cell type (Fig. 16). This effect could have been mitigated by down-sampling reads in the H1 cell type, but at a cost of reducing the quality of the best dataset under study. Instead this disparity should just be noted as a potential cofounder in downstream TAD analysis; at lower-resolution such as that used to calculate compartment eigenvectors (1 Mb) this sensitivity to sequencing depth is not evident (Figs. 9, 10).

Despite differing numbers, there is still detectable levels of conservation of TADs between cell types (Fig. 17). Genome-wide, 33% of all H1 TAD boundaries have a matching boundary in GM12878 in the same or an adjacent 40 kb bin (K562: 31%,

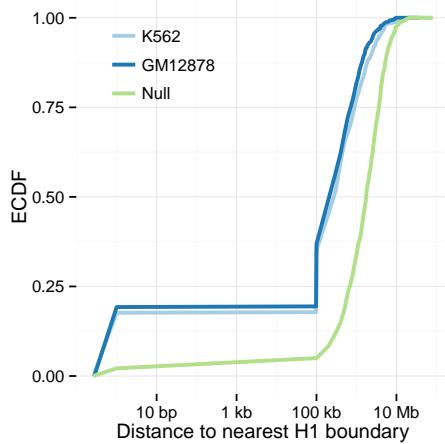


Figure 15: Compartment boundaries are shared between cell types. The empirical cumulative density functions (ECDF) of distances between H1 compartments and those called in GM12878 and K562 are shown. These distances were compared with a null distribution calculated from shuffled boundaries at a matched resolution.

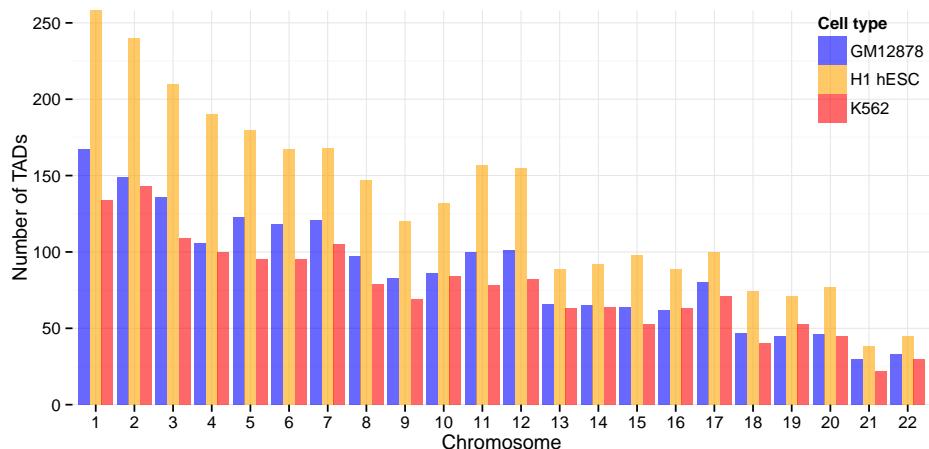


Figure 16: The number of called TADs per cell type under study. A greater number of TADs were called in H1 hESC (2,897 total) than in GM12878 (1,925) or K562 (1,677), due to the difference in sequencing depths in each experiment when matrices were binned at 40 kb resolution.

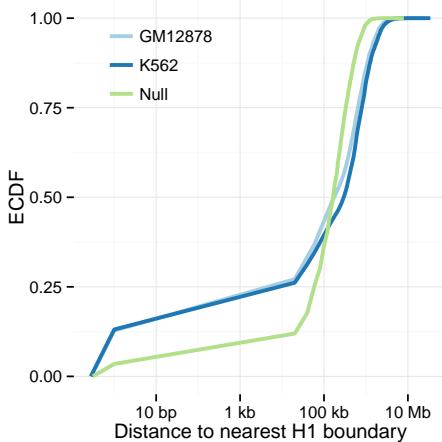


Figure 17: TAD boundaries are shared between cell types. The empirical cumulative density functions (ECDF) of distances between H1 TADs and those called in GM12878 and K562 are shown. These distances were compared with a null distribution calculated from randomly placed boundaries allocated at a matched resolution.

null model: 18%; K–S test: $D = 0.26$, $p \approx 0$). To illustrate this conservation with a real example, a 20 Mb region of chromosome 2 is pictured (Fig. 18), highlighting the conservation between both TADs and compartment calls across the three cell types and at multiple scales: from chromosome-wide 1 Mb compartment eigenvectors, to TADs with individual boundaries resolved to 40 kb.

3.5 DOMAIN EPIGENOMICS

The use of well-studied human cell types allows intersection with publicly-available epigenomics datasets, such as those produced by the ENCODE consortium.^[74] In total, 35 cell-matched ChIP-seq datasets were available for all three of the tier 1 ENCODE cell lines: GM12878, H1 hESC and K562 (see Methods 2.2). In this section we integrate reprocessed Hi-C data and derived higher order domains with these various high-resolution datasets.

3.5.1 A/B compartments

The overwhelming majority of intersected chromatin features are significantly enriched in active A compartments relative to B compartments (Fig. 19). This is expected, A compartments represent the actively-transcribed and accessible portions of the genome, and have previously been shown to positively correlate with many of the features shown.^[9,17]

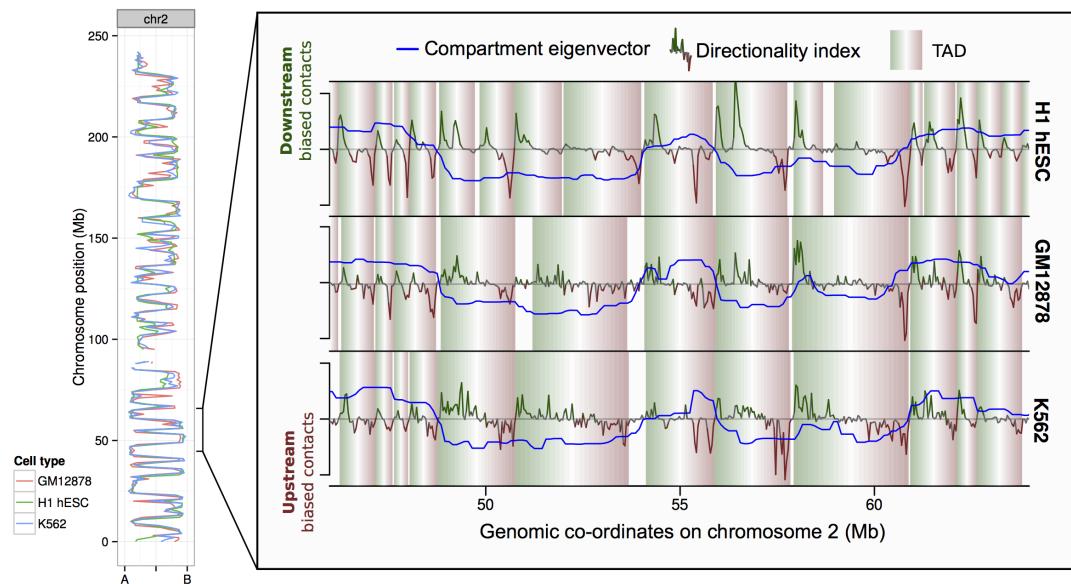


Figure 18: Concordance of chromatin structure at multiple scales over three human cell types. The eigenvector compartment profile is shown for chromosome 2 for three human cell types (left). At higher resolution, the zoomed region illustrates conservation of topological domains (TADs) over 20 Mb of the same chromosome.

Exceptions to this rule are few. However the repressive histone modification H3k9me3 is found more often in B compartments in two cell types, as is the P300 transcription factor (Fig. 19). Also of note is the histone variant H2A.Z which is significantly enriched in A compartments in GM12878 and K562, but this relationship is reversed in the embryonic stem cell line (Fig. 19). Recent evidence suggests specialised roles for H2A.Z in regulating both repression and activation during embryonic stem cell differentiation, acting as a “general facilitator”.^[156] Additionally H2A.Z has been reported to mark histone octamers for depletion, thereby permitting gene activation during differentiation.^[157] Potentially, then, the H2A.Z enrichment in B compartments could be driven by regions soon to be de-repressed as the stem cell differentiates.

3.5.2 TAD classes

Unlike compartments, initially TADs were not observably correlated with blocks of chromatin features.^[10] Later studies have linked TADs with such enrichments, first in *Drosophila*^[31] and later in human cells, where it was argued TADs are merely a low-resolution window to smaller “sub-compartments”, bearing similar active and inactive marks to their much-larger namesakes.^[13] Here we look for evidence that TADs called in our human cell types correspond to the “epigenomic domains” identified in *Drosophila* by Sexton *et al.*^[31] Epigenomic domains were identified through supervised

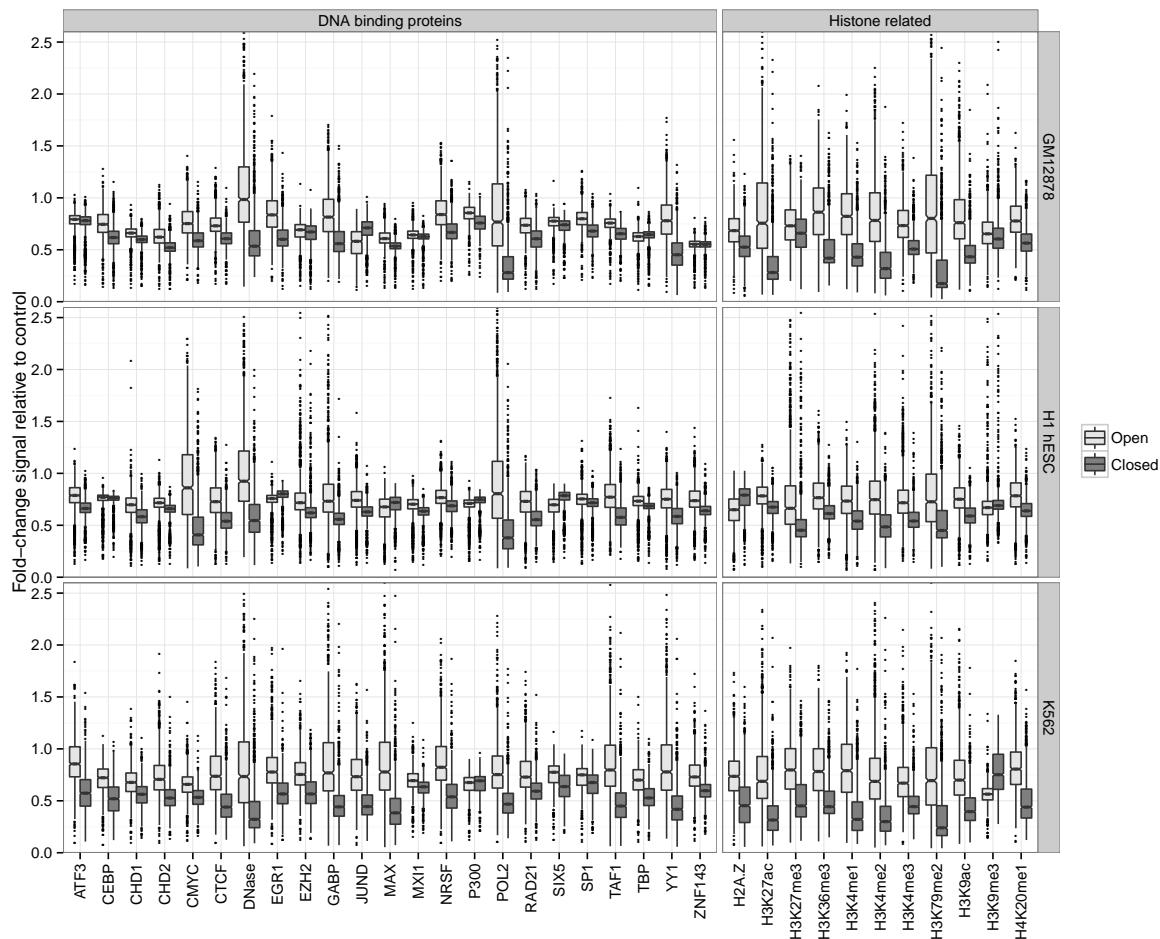


Figure 19: The chromatin signatures of A/B compartments. Notched boxplots summarise the distribution of each feature over 1 Mb bins in open (A) and closed (B) compartments genome-wide.

clustering of physical domains by their average enrichment for selected epigenomic features of known function, for example enrichment of H₃K27me3 mark was used to call Polycomb (PcG) associated domains.

We found that TADs called across the three cell types used in this work could similarly be clustered into transcriptionally active (active), repressed heterochromatin (null) and polycomb-associated (PcG) domains, based on the patterns of DNase hypersensitivity, H₃k9me3 and H₃k27me3, respectively (Fig. 2o). *Drosophila* physical domains were clustered into four categories, with three of those matching our annotations. The fourth *Drosophila* domain type was enriched for the HP1 protein (therefore likely centromeric) for which we did not have ENCODE ChIP-seq data in all human cell types under study.

This analysis reveals that active compartments typically cover both active and PcG-associated TADs, while B compartments appear more homogeneous and are composed mostly of H₃k9me3-enriched heterochromatin even when considering fine-grained TAD structures rather than megabase-sized genomic blocks (Fig. 2o).

These findings also link with recent work that suggested TADs are windows into “sub-compartments”^[13] which more closely reflect the functional enrichments of compartments. However, in our data we did not find statistical support for the suggested 5 classes of sub-compartment; instead, an ensemble of algorithms for optimising the number of cluster centroids voted for two or three clusters of TADs (*data not shown*). This is not wholly surprising as Rao *et al.*^[13] report sub-compartments only on extremely deep-sequenced samples, and at a scale of below that of TADs.

3.6 VARIABLE REGIONS

Despite the vast majority of the genome being in matched chromatin compartments across human cell types (Fig. 9), there are also regions of disagreement. Reasons for observable differences include technical errors and biases, but also more interesting functional explanations, where cell-type specific activation or repression is reflected in changes in higher order structure.

To conservatively call regions of variable structure (RVS), we used HMM-called compartment states and selected those which were either: i) open in one cell type and closed in both others or ii) closed in one cell type and open in both others. This left sets of RVS which could be considered as “flipped open” or “flipped closed” in a given cell type.

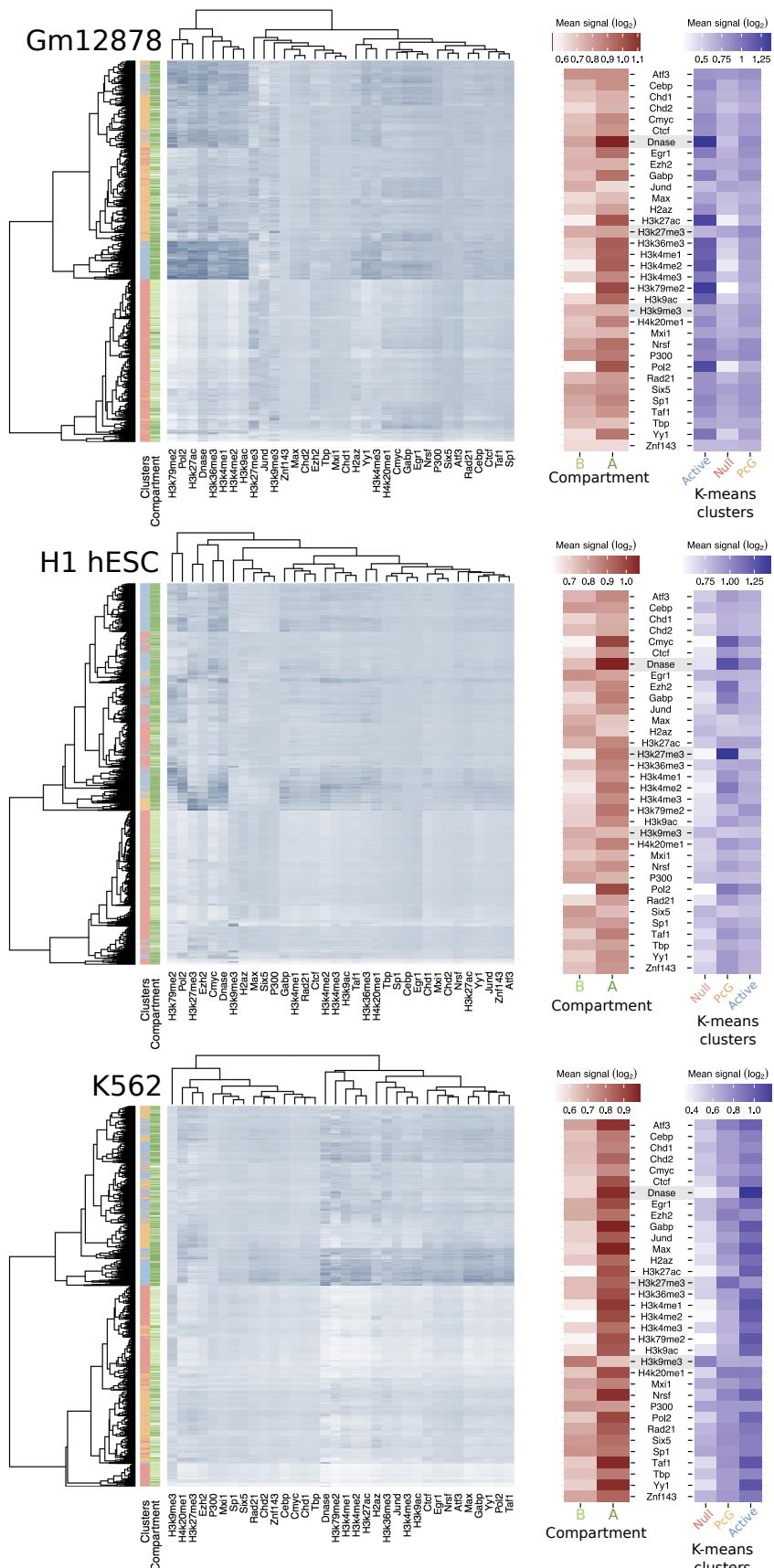


Figure 20: TADs reflect epigenomic domains. Following the Drosophila results of Sexton *et al.* [31], clustering of TAD domains by mean log₂ signal of 34 ENCODE features distinguishes null, active and polycomb-associated (PcG) domains, as well as reflecting the encompassing A/B compartments.

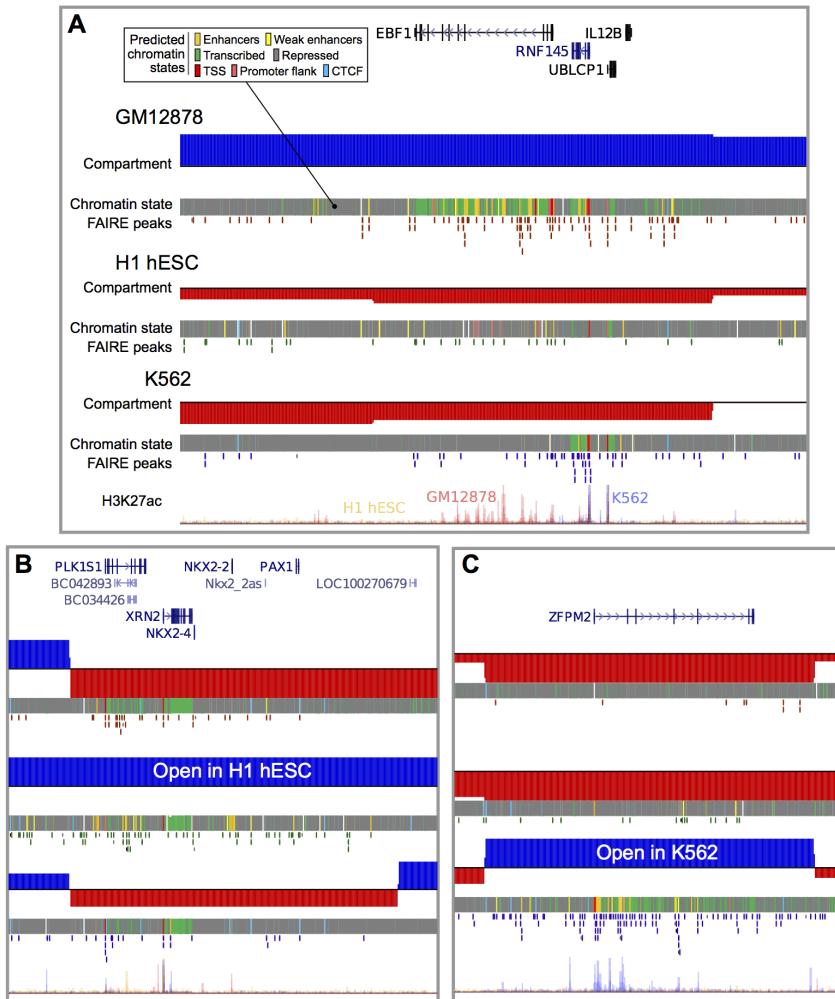


Figure 21: Structurally variable regions indicate cell type specific biology. Regions occupying the active A nuclear compartment in one cell type, but the repressive B compartment in the other two, were selected and ranked by the number of predicted active enhancers. Examples of particular interest from the top 5 regions per cell type are shown: (A) the chr5:158-159 Mb region which occupies the open A compartment in GM12878 cells, (B) the chr20:21-22 Mb region which is open in H1 hESC, (C) the chr8: 106-107 Mb region which is open in K562. Displayed tracks are: known (UCSC) genes, compartment eigenvectors, chromHMM/Segway combined chromatin state predictions, open chromatin FAIRE peaks, and H3K27ac signal.

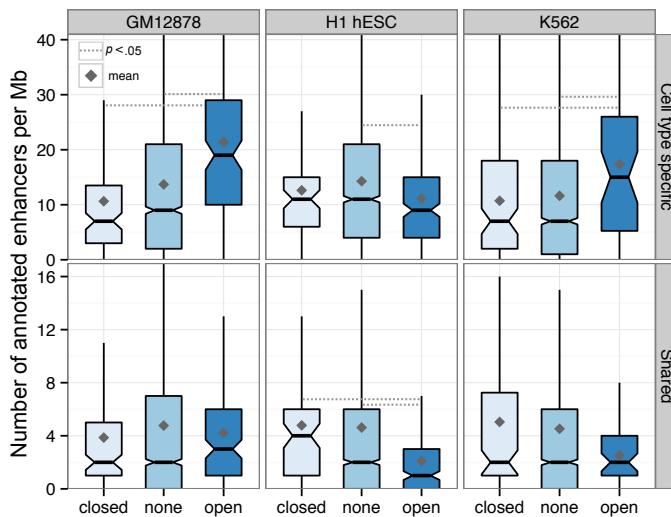


Figure 22: Regions of variable structure are enriched for cell type specific enhancers. Numbers of predicted enhancer states (cell type specific or shared between two or more cell types) are shown for regions with altered (open or closed) and non-altered (none) compartments in each cell type.

3.6.1 Chromatin state enrichment

Given our conservative definition of RVS (Section 3.6), such notable changes between transcriptionally permissive and repressive environments might be expected to be associated with cell-type-specific biology, such as functional chromatin states. To test this, we used consensus predicted chromatin state annotations, built from two machine learning algorithms, ChromHMM^[84] and SegWay^[82,86], and tested for enrichment or depletion in our set of RVS (Methods 2.4.2).

We found that RVS show a striking enrichment for cell-type specific enhancers in both of our derived cell lines, but not in embryonic stem cells (Fig. 22). This observation can be explained as the undifferentiated cell type would not be expected to have lineage-specific enhancer contacts active in its pluripotent state. The same pattern was not seen for enhancers shared between two or more of the cell types under study. We observed a similar enrichment for cell-type-specific transcription but not for several other chromatin states including promoter activity (Fig. 23).

Together these state enrichments suggest the identified RVS reflect regions of cell-type specific biology, with heightened enhancer and transcriptional activity in their active cell type Fig. 23). Combined with the observed large-scale concordance of higher order chromatin organisation between cell types (Figs. 9, 18), these results reinforce a model of organisation whereby chromatin organisation is largely conserved and static across cell types, but also permits local flexibility in order to activate or repress regions of biological importance to a given cell type.

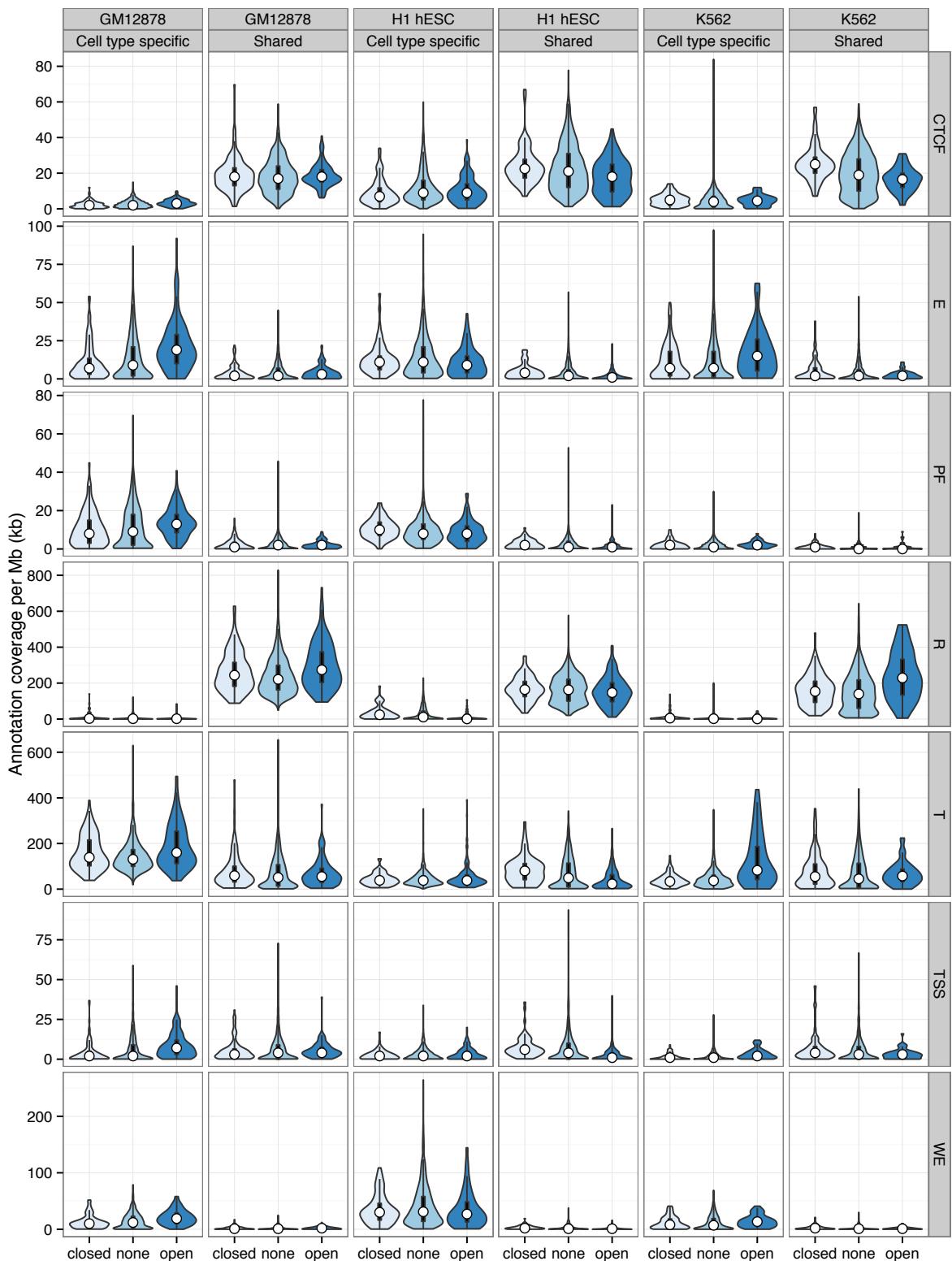


Figure 23: Distributions of features across all predicted chromatin states in regions of variable higher order structure. Distributions of the summed coverage of predicted chromatin states in each Mb per cell type are shown as bean plots. Predicted chromatin states are those from Hoffman *et al.* [86] and are labelled as: TSS: promoter and TSS; PF: promoter flanking region; E: enhancer; WE: weak enhancer or cis-regulatory element; CTCF: CTCF enriched element; T: transcribed region; R: repressed or low-activity.

3.6.2 Gene ontology enrichment

Specific examples of RVS highlight genes of interest (Fig. 21) but should be coupled with statistical evidence prior to suggestions of a general trend. For this reason we used Gene Ontology (GO) terms to test for functional enrichment within open RVS per cell type.

Functional enrichments of genes found in “flipped open” RVS in each cell type were calculated using DAVID^[121,158] and filtered by false discovery rate (FDR < .05). This revealed slight enrichments for keywords “blood”, “oxygen carrier” and “ β Haemoglobin” in the K562 cell type, a multipotent cell type which is known to show properties of an early erythrocyte, among others.^[159] However, in the other two cell types we did not find significant enrichments across regions, except for artefacts caused by violations of the independence assumption used in GO term hypergeometric testing. Our RVS blocks were at least 1 Mb each so could contain more than one gene, thus enrichments were seen for those genes known to form paralogous clusters along a chromosome, such as olfactory receptors. The full results of these tests are given in the appendix (Tables A1, A2, A3).

The size of RVS could also explain we do not capture the relationship hinted at by cherry-picked examples (Fig. 21). Given regions contain multiple (often unrelated) genes, we can imagine a case where a cell type specific locus is activated and moves into a more central position, disturbing adjacent genes which remain in a repressed state. Thus the cell type specific signals contained within the sum of all RVS in a given cell type could be obscured by the noise of adjacent genes captured in these broad compartment transitions.

3.6.3 Contact changes

A defining characteristic of active A compartment regions is a preferential bias in contacting other A compartment regions.^[9] However, it is not clear whether cell-type-specific transitions in higher-order structure are solely compartment-level phenomena, or involve other structural strata. We therefore examined the genome-wide contact profiles of each region of variable cell-type-specific chromatin structure in detail.

If our cell-type-specific RVS are mediated by finer-scale structural levels (such as TADs) we might expect to see predominantly short-range contact changes in their underlying contact profile. Instead, we found that variable regions preferentially interact with other A compartment regions in the cell types in which they are active (Fig. 24), but not in the other cell types in which they are inactive. This supports the idea that these cell-type-specific regions are undergoing compartment-level transitions, disproportionately mediated by the formation of long-range contacts, while also not precluding additional changes at lower levels such as TADs.

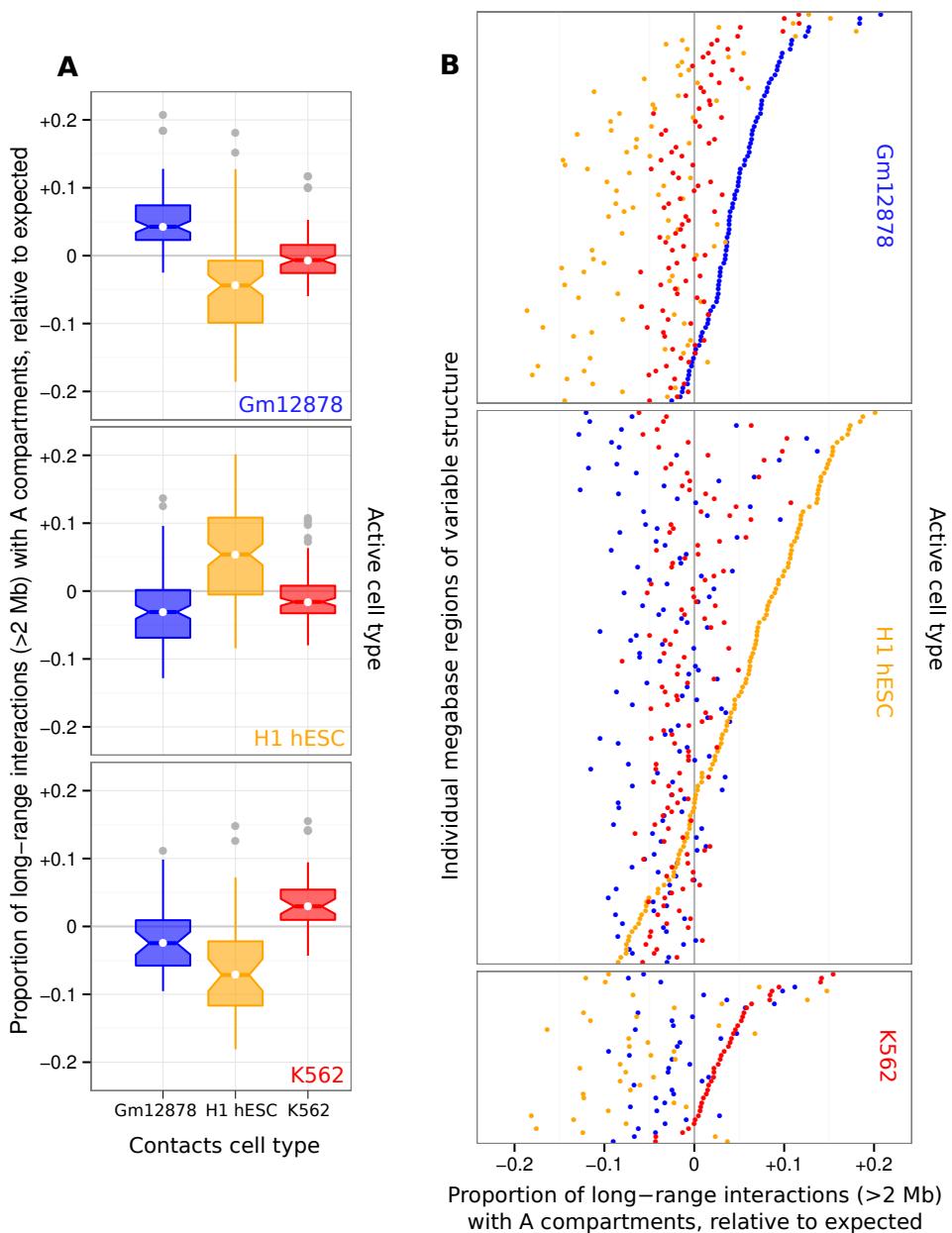


Figure 24: Regions of variable higher order structure change their genome-wide contact profiles to favour active compartments. Genome-wide normalised contacts were summed for each region of variable structure and the relative proportion of those that were with active / A compartments is shown across the three cell types used in this study. Proportions were subtracted from the genome-wide average per cell type, such that positive values indicate a greater than expected interaction bias with active compartments. These data are presented both as a summary boxplot (A) and with each individual region visualised, sorted by relative proportion of A contacts in active cell type (B).

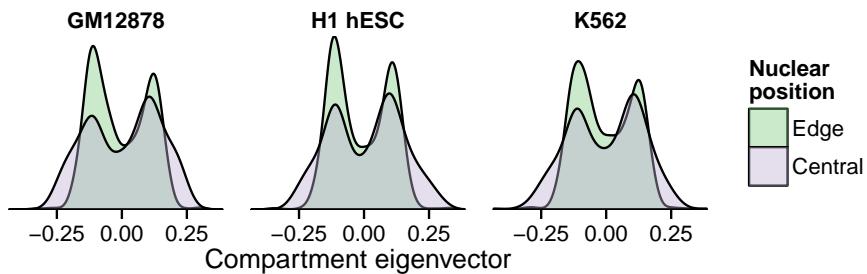


Figure 25: Nuclear positioning of chromosomes relative to compartment eigenvectors. Kernel density estimates showing peripheral chromosomes have a greater proportion of B compartments (negative eigenvectors) relative to centrally-positioned chromosomes. Positioning data from Boyle *et al.* [132] (Methods 2.9).

3.7 NUCLEAR POSITIONING

Chromosome positioning within the nucleus is known to reflect gene density, with the most gene-dense chromosomes occupying the centre of the nucleus in human cells.^[160] Kalhor *et al.*^[20] used a Hi-C variant to recreate probability density maps of chromosome positions which again reflected this feature of higher order chromatin organisation, and also reported active regions were more diffuse than inactive. A testable hypothesis with the eigenvector data used in this work is that active A compartments are enriched in the central nucleus of our human cell types, and B compartments are preferentially located in the nuclear periphery.

To test this, published data on chromosome positioning preference within the nucleus was used to label chromosomes as “central” or “edge”.^[132] Chromosomes whose DAPI hybridisation signals were significantly enriched ($p \leq 2 \times 10^{-2}$) in the inner nuclear shell, as defined by Boyle *et al.*^[132], made up the “central” group and included chromosomes 1, 16, 17, 19 and 22. Similarly the “edge” group had enriched signals ($p \leq 5 \times 10^{-3}$) in the outer shell relative to the inner nuclear shell and included chromosomes 2, 3, 4, 7, 8, 11, 13 and 18. The remaining chromosomes showed no significant preference to either inner or outer nuclear shells at $\alpha = 0.05$.^[132]

We found that positive eigenvectors (reflecting A compartments) did show a modest relative enrichment in centrally-positioned chromosomes relative to those located at the nuclear periphery (Fig. 25). The significance of the difference in distribution of eigenvectors in the central and edge of the nucleus was determined by a two-sided Kolmogorov-Smirnov (K-S) test, with the null hypothesis that there is no difference between the empirical cumulative density functions of the central chromosome eigenvectors ($F_{central}$) and peripheral (F_{edge}). The difference was found to be statistically significant in each cell type ($H_0 : F_{edge} = F_{central}$; GM12878: $D = 0.11$, $p < 6 \times 10^{-4}$; H1 hESC: $D = 0.12$, $p < 8 \times 10^{-8}$; K562: $D = 0.10$, $p < 5 \times 10^{-3}$)

4

INTEGRATIVE MODELLING AS A TOOL TO EXPLORE BIOLOGICAL SYSTEMS

4.1 INTRODUCTION

Large-scale chromatin data has recently been produced by multiple consortia, most notably ENCODE^[74] (Section 1.4.1) but also the NIH Roadmap Epigenomics project.^[161] The breadth and depth of this new data offers unprecedented opportunities to advance our understanding of the complex biology of the chromatin landscape. To this end, studies have already enjoyed success in integrating these data through modelling techniques, with the subsequent dissection of these models revealing novel insights into complex biological phenomena.

Recent studies have shown convincingly that local chromatin state measurements can accurately predict expression levels of genes on a genome-wide basis. Tippmann *et al.*^[162] designed a linear model to predict steady-state mRNA levels in mouse embryonic stem cells based on just four predictors: 3 histone modifications (H3K36me3, H3K4me2 and H3K27me3) and Pol-II occupancy. Remarkably, the linear model was found to explain 84.6% of an estimated 91% maximal variance that could be explained (as calculated through a detailed determination of noise).^[162] An additional finding of this study was that mRNA half-life and microRNA mediated transcript degradation both had relatively minor influence on steady-state mRNA levels, with the authors concluding that “the lion’s share of regulatory contribution is at the level of mRNA synthesis and predictable from chromatin alone.”^[162] An independent study used a similar regression modelling approach to chromatin and transcription factor data and again concluded that models built with histone modifications and chromatin accessibility data were almost as accurate as those which also included binding data for 12 transcription factors.^[163]

A recent key study from the ENCODE consortium used ChIP-seq datasets to predict gene expression in a range of cell types as measured by a variety of experimental techniques.^[92] The authors here developed a two-stage model which first attempts to classify each transcription start site (TSS) into an ‘on’ or ‘off’ state using a powerful ensemble classifier technique called Random Forests (RF). The second stage of the model used the same range of histone modifications as regressors in a simple linear modelling framework to quantify predicted expression. This approach proved very successful, producing a median Pearson correlation coefficient (PCC) between predicted and empirical expression levels using 10-fold cross-validation of 0.83 across

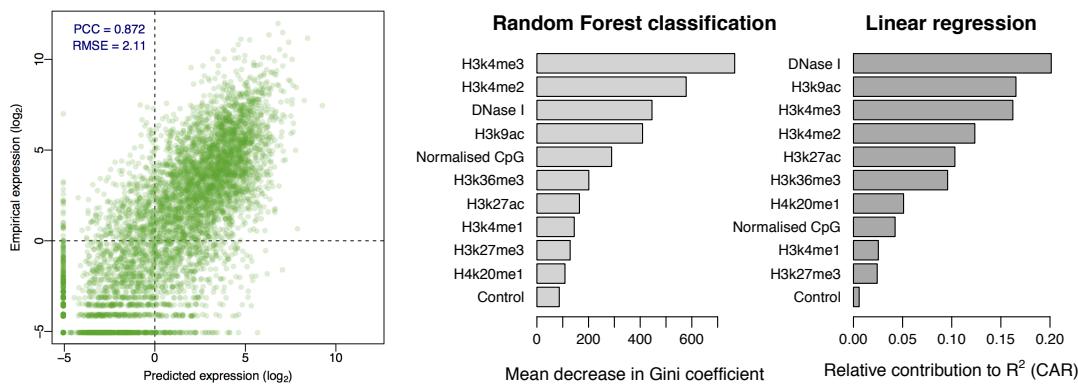


Figure 26: Highly accurate models of expression were built following Dong *et al.* A scatterplot shows the strong correlation between predicted and observed expression levels per transcript (*left*). Variable importance metrics are shown for the on/off RF classification step and continuous linear regression step (*right*).

all cell lines and expression level technologies.^[92] Additionally, this study highlighted cap analysis of gene expression (CAGE) as the technology, relative to RNA-seq and RNA-PET, which produced the most predictable expression response. CAGE uses 5' capped transcripts to generate short, specific tags which precisely identify TSS positions as well as quantifying the abundance of a given transcript.^[127,164]

These recent publications highlight the importance and relevance of advancing our understanding of chromatin biology through a model-based approach. We can extend this idea to the related domain of nuclear architecture, in the hope of understanding the relationships between chromatin and higher order structure in the same way that chromatin features have been related to transcriptional output.

4.2 EXTENDING DONG *et al.*

We reimplemented the published modelling framework of Dong *et al.*^[92] (introduced in Section 4.1) to replicate their results and analyse the strengths and caveats of their approach.

We were able to reproduce the reported results and highly accurate models of transcriptional output. An example is shown for a model of CAGE expression in the H1 hESC cell type (Fig. 26). Note that not all variables used in Dong *et al.*^[92] were made available for this particular modelling scenario, however the Pearson correlation between predicted and observed expression (0.87) is above the study's median value (0.83), and in-line with other models predicting CAGE data (median $PCC \approx 0.87$).^[92]

We also re-calculated measures of variable importance for this model of transcription (Fig. 26). We note some small variations from the example model shown in Dong *et al.*^[92] which was predicting cytosolic CAGE data recorded in K562 cells. This

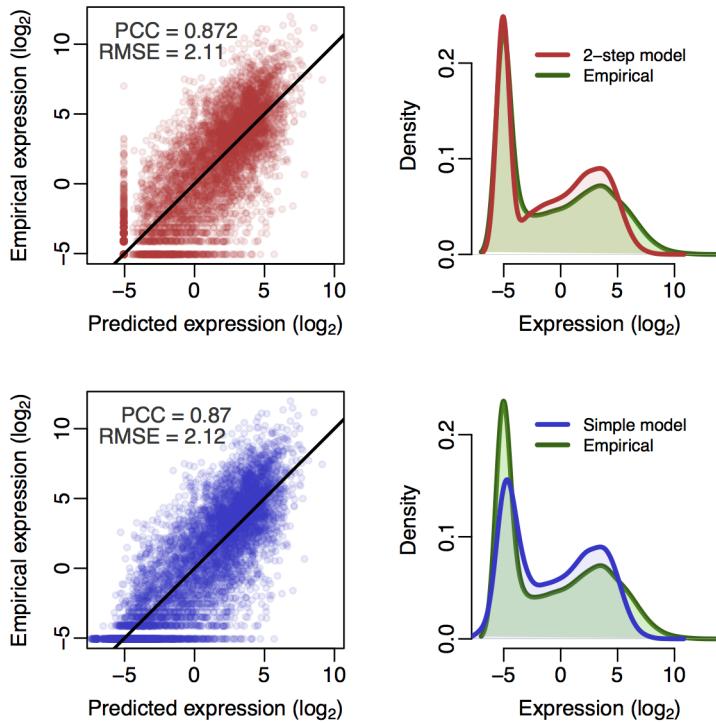


Figure 27: Comparison of a published two-step classification-regression model of transcription with a simple linear regression model. Scatterplots of predicted against empirical \log_2 reads per million (RPM) expression values for the two-step model of Dong *et al.* [92] and simple multiple linear regression are shown (left) along with frequency distributions of predicted and observed expression levels (right). Scatterplots are annotated with Pearson’s correlation coefficient (PCC) and the root mean squared error ($RMSE$); black trendlines describe $y = x$. Overall correlations calculated with 10-fold cross-validation.

hints at some degree of some variability between cell type models, though broad similarities also exist such as both models ranking DNase I hypersensitivity as a relatively informative variable (Fig. 26).

When replicating the modelling approach of Dong *et al.* [92], we were surprised to find that the two-step classification then regression (firstly assessing a gene as ‘on’ or ‘off’ and then predicting its expression level) added little additional accuracy relative to a simple linear regression model (Fig. 27). Indeed, it appears the “best bin” technique (Section 4.2.1) had much greater impact on overall predictive power than the addition of this classification step.

4.2.1 Bestbin method

An innovative element of the modelling approach used in Dong *et al.* [92] is the ‘bestbin’ method of matching chromatin measurements to the expression of a given TSS. This strategy first bins normalised signal intensities into 40×100 bp bins encompassing

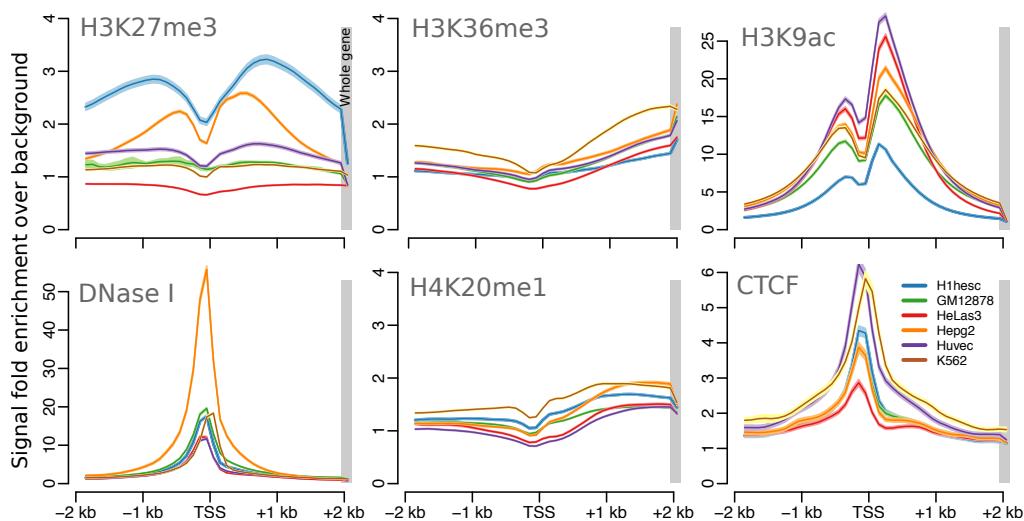


Figure 28: Average input feature profiles over transcription start sites. Mean ChIP-seq signal over input control is shown for 6 factors in 6 human cell types used in Dong *et al.* [92]. Each is averaged genome-wide over GENCODE v7 hg19 defined TSS ± 2 kb, and over whole genes (grey shading). Ribbons shown 99% confidence intervals of the mean.

4 kb around the TSS, and adds an additional bin representing the remaining gene body. Then the correlation between the signal of a given mark and the expression of a TSS across all genes is measured, then the bin producing the highest correlation is designated as the ‘bestbin’ and that bin’s normalised ChIP-seq signal intensity is taken forward for the full model. This was shown to raise the correlation (between predicted and observed expression) by 0.1 in the simple regression model, an increase in accuracy of almost 13%, relative to simply taking the average value across all bins. [92]

The justification for such an approach hinges on the idea that the multitude of input features (mostly histone modifications and DNA binding proteins) have a variety of biological functions, and so the bestbin method is one way of learning these functions in an automated and unsupervised way. For example, the histone modification H3K36me3 is understood to be painted across exons that are being actively-transcribed, [162, 165, 166] thus the genome-wide summary statistic that best captures this function is likely the whole-gene measurement, rather than the level of H3k36me3 at a gene’s TSS or upstream promoter. A re-analysis of ENCODE data used in Dong *et al.* [92] highlights this kind of variability across input features (Fig. 28). Some marks clearly are enriched directly over TSS (CTCF, DNase; Fig. 28) while others show enrichments along the gene body (H3K36me3, H4K20me1; Fig. 28) as well as more-complex, asymmetrical “shoulder” patterns (H3K27me3, H3K9ac; Fig. 28). Bestbin will therefore, to some degree, capture these spatial relationships without *a priori* specification.

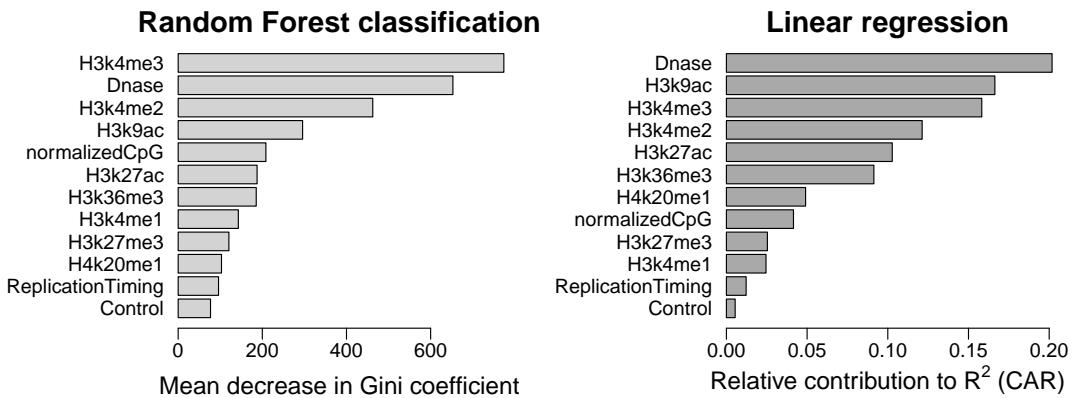


Figure 29: Relative importance metrics for variables in both stages of a reimplementation of a published model for predicting transcriptional output. Variable importance is measured by decrease in Gini coefficient for the RF classification step, and by CAR R^2 decomposition^[167] for the linear regression step.

4.2.2 Model adjustments

We attempted to improve the accuracy of predicted expression values produced by Dong *et al.*^[92] through increasing the number of informative regressors. While Dong *et al.*^[92] included broad coverage of different histone modifications, they did not investigate the impact of higher order chromatin data. For this reason, we matched the TSS positions used in Dong *et al.*^[92] with previously-published genome-wide replication timing ratios measured in BGo2 ESCs.^[168] This data is of a different origin to the transcriptional data in this case (which was recorded in H1 hESC) but replication timing is thought to be largely conserved between cell types.^[133]

We then used these values as an additional regressor in both the two-step classification regression model and the simple linear model but saw no significant improvement in either model's accuracy (*data not shown*). The reasons for this are likely that the data were relatively low-resolution (1 Mb), from an imperfectly matched cell line and also that the existing model is already achieving such accurate results that they must already be accounting for most of the maximal explainable variance in gene expression given experimental and biological noise. With this in mind, additional regressors would be expected to yield diminishing returns. Even so, on closer examination, the replication timing data appeared only slightly more informative than the control ChIP-seq input measurements when evaluated with relative importance metrics (Fig. 29), implying that large-scale chromatin domains do not have significant influence on the expression of the genes resident within them.

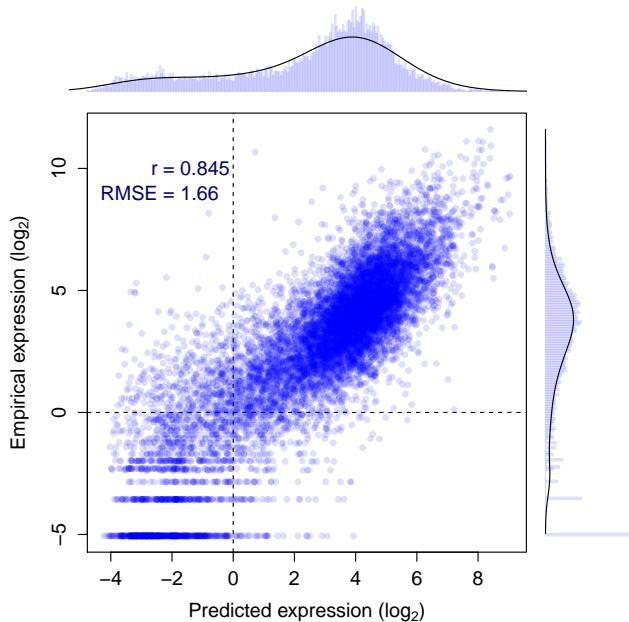


Figure 30: Random Forest predictions of FANTOM5 expression data. RF model predictions are plotted against their empirical values. The marginal distributions of predicted and empirical expression values are shown opposite their respective axes. Pearson’s correlation coefficient (r) and the root mean-squared error (RMSE) are shown (inset).

4.3 MODELLING FANTOM5 EXPRESSION DATA

Using FANTOM5 CAGE data^[125] and the approach established above (Section 4.2), we next attempted to model gene expression at timepoint zero (t_0) of a differentiation timecourse of Human H1 embryonic stem cells (H1 hESC) to CD34+ hematopoietic stem cells. Applying this modelling strategy to a novel dataset will allow us to assess the portability of the model design, as well as permitting more detailed breakdown of model components, such as the bestbin strategy.

We retrieved a number of genome-wide ChIP-seq datasets measured in H1 hESC cells and produced by the ENCODE consortium^[74] (Methods 2.10.2). These were matched to transcript annotations to build an input feature set for use in building a predictive model of transcriptional output.

Due to the finding that a two-step (classification–regression) approach added little additional modelling accuracy (Fig. 27), we employed a single-step design using a Random Forest (RF) regression model.^[103,169] With a total of 14 predictors (10 histone modifications, HDAC6, H2A.Z, DNase I and an input control, listed in Methods 2.10.2), we were able to build a highly accurate predictive model of transcriptional output of around 11,000 TSS (Fig. 30).

Model predictions evaluated with 10-fold cross validation show a highly significant correlation with measured CAGE levels ($PCC = 0.845 \pm 1 \times 10^{-4}$, $p < 2 \times 10^{-15}$), and

the model is able to explain around 71% of the variance in the expression response (for comparison a linear model resulted in $PCC = 0.825 \pm 3.2 \times 10^{-5}$, $p < 2 \times 10^{-15}$). This result is worse than that of Dong *et al.*^[92] who achieved cross-validated correlation coefficients of up to 0.9, but it is roughly equal to their median test set correlation of 0.83.^[92] However the RMSEs of our predictions, when normalised by the range of observed values, compare more favourably (0.11, compared with Dong *et al.*'s: 0.14).

Our slightly lower predictive power could be explained by our streamlined model design. Dong *et al.*^[92] implemented a pseudocount optimisation step whereby an additional count added to each binned signal intensity prior to log transformation to maximise expression correlation. In the model presented above, a fixed pseudocount of 1 was used to avoid introducing an unwarranted positive bias towards higher correlation. We confirmed that a two-step classification-regression design did not improve our model performance metrics; indeed, the PCC and RMSE of a classification-regression framework with this data showed a slight decrease in prediction accuracy ($PCC = 0.834 \pm 0.007$, RMSE = 1.77 when applied to the same test and training data used in Fig. 30).

4.3.1 Bestbin analysis

We again implemented the previously-described ‘bestbin’ strategy^[92] (Section 4.2.1) to objectively select the most-correlated binned signal for each chromatin H1 hESC mark. To explore the implications of this approach, we analysed the stability of chosen bestbins by calculating them on 200 sets of 1000 randomly selected TSS samples, with each sample representing approximately 8% of the complete dataset. Distributions of chosen bestbins across these 200 sub-samples are shown as boxplots (Fig. 31).

We find that bestbin selections are often highly consistent across sub-samples, indicating there are fairly static informative regions relative to a TSS for each chromatin factor. Furthermore, the selected bestbins match known biological mechanisms; for example the H3K36me3 mark’s bestbin is consistently the whole gene measurement (Fig. 31) and this mark is known to be enriched in actively transcribed exons.^[162,165,166] The negative control variable (ChIP-seq input) shows no strong location bias, as expected (Fig. 31). Other distributions are less easily explained, such as those features showing a tight distribution of informative regions slightly downstream of the TSS (H3K9ac, H4Kme2/3 and H3K79me2; Fig. 31).

4.4 MODELLING HIGHER ORDER CHROMATIN

Accurate predictive modelling of transcription in a variety of cell types offered several novel insights into the interrelationships between locus-level chromatin features and

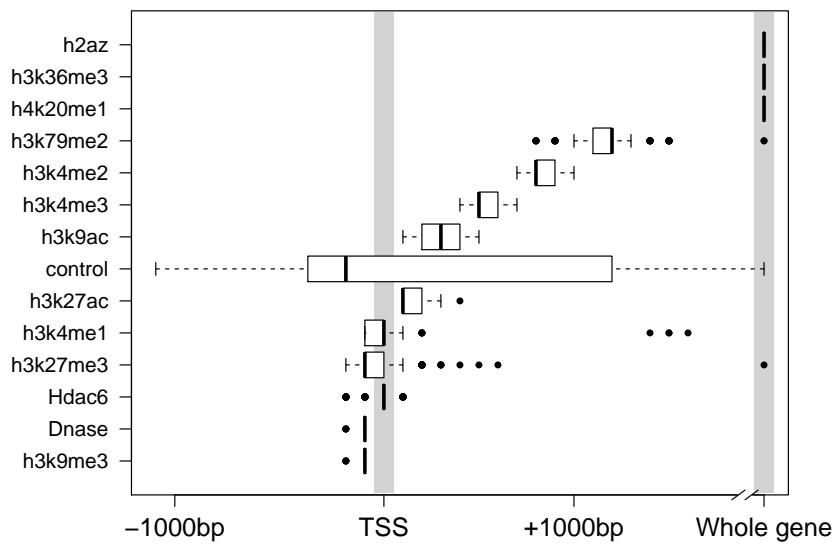


Figure 31: Distributions of bestbin locations relative to the TSS. Bestbins were selected for normalised ChIP-seq signal intensities for 10 histone marks, the H2A.Z histone variant, Hdac6 histone deacetylase, DNase hypersensitivity and a ChIP-seq input chromatin control. Bins analysed extended 2 kb flanking the TSS, but more distal bins were never selected and hence are not shown. ‘Whole gene’ represents the averaged signal intensity from TSS to transcript end site, as defined by Ensembl Genes v69.

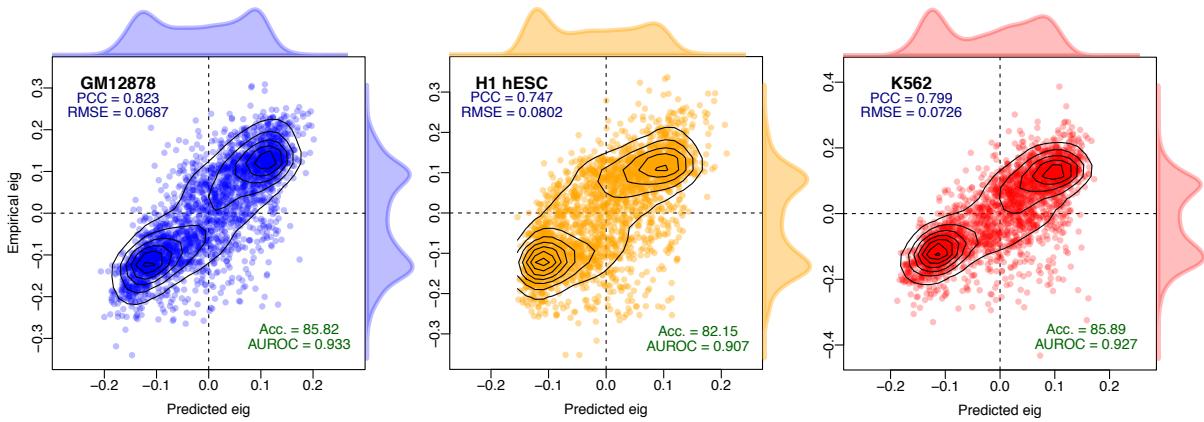


Figure 32: Compartment eigenvector model predictions are highly correlated with observed values. Pearson correlation coefficient (PCC) and root mean-squared error (RMSE) report the degree of success of the regression model, whereas accuracy (Acc.) and area under the receiver operating characteristic (AUROC) give the classification accuracy of binarized outcomes.

transcriptional machinery, as well as advancing a quantitative explanation of the degree to which correlated features are informative. It is of interest then, to test whether this approach can be applied to other data, such as the reprocessed higher order chromatin organisation data assembled in this work (Chapter 3).

Previous publications have identified several correlates which track compartment eigenvector profiles to varying degrees,^[9,16] yet to date these relationships have not been quantitatively investigated. The above-described modelling framework offers a statistical approach towards understanding the drivers of these observed correlations.

4.4.1 Predictive model

We built Random Forest regression models (Methods 2.3.1) to predict compartment eigenvector profiles genome-wide in three human cell types. Models were found to have high predictive accuracy, with Pearson correlation between predicted and observed compartment eigenvectors in the range of 0.82–0.75 (Fig. 32), comparable to that achieved by Dong *et al.*^[92] in the prediction of transcription.

Our predictive models were also assessed in terms of classification performance, i.e. did the model correctly assign each block to an A or B compartment. Instead of retraining a classifier and building parallel models, instead for an estimate of classification accuracy we threshold our regression predictions (Methods 2.3.2). We found our Random Forest models achieved high classification accuracy with $\geq 82\%$ of all 1 Mb genomic bins correctly assigned in each cell type (Fig. 32).

This predictive performance underlines the strong connection between locus-level features and higher order chromatin structure previously noted by Lieberman-Aiden *et al.*^[9] Given such highly-predictive models can be generated, it is then of interest

to dissect said models in an attempt to understand the nature of this captured relationship.

4.4.2 Cross-application

High predictive accuracy on cell type specific models could be the result of “over-fitting”. In machine-learning, over-fitting refers to the point at which parameters are being optimised to capture noise within a feature set, as well as signal, thereby giving an overoptimistic model performance which would not generalise to another featureset with different noise profiles.

To test if over-fitting was causing our high observed accuracy, we cross-applied models learnt in one cell type to unseen input data from each of the other two cell types under study. If predictive accuracy is a lot lower on unseen data, this lends evidence to the idea that our models may be overfit to their respective cell types. Conversely, it could be the case that biologically-distinct mechanisms are in place that differ between cell types, preventing a simple cross-application.

We found cross-application between cell types was possible and resulted in similarly-high levels of accuracy to within cell-type cross-validation (Fig. 33). This gives good evidence not only that models are not overfitting to cell-type specific noise, but also that there exist broad rules linking chromatin conformation and locus-level feature aggregation. The cross-application suggests there exists enough commonalities for compartment profile predictions to transcend the cell-type specific biology inherent to an embryonic stem cell or differentiated lymphoblast.

4.4.3 Between-cell variability

Given much of the higher order chromatin organisation is conserved between the three cell types used in this work (Fig. 10), a testable hypothesis is that these conserved regions are drivers of cross-applicability between cell types. Conversely, genomic regions which vary most across the cell types in our dataset should be more difficult to predict.

Indeed we found the most variable regions across cell types were then most difficult to predict through our Random Forest modelling framework (Fig. 34). In each cell type, the third of the genome with the most consistent compartment eigenvectors across cell types could then most accurately be modelled in each cell type, and conversely the most variable third shown significantly depleted predictability (Fig. 34). This latter result suggests these variable regions could either be those which are noisiest, where the eigenvector is least capturing compartment structure, or where cell-type specific biology is influencing compartment structure in ways not captured by our input feature set and low resolution modelling pipeline.

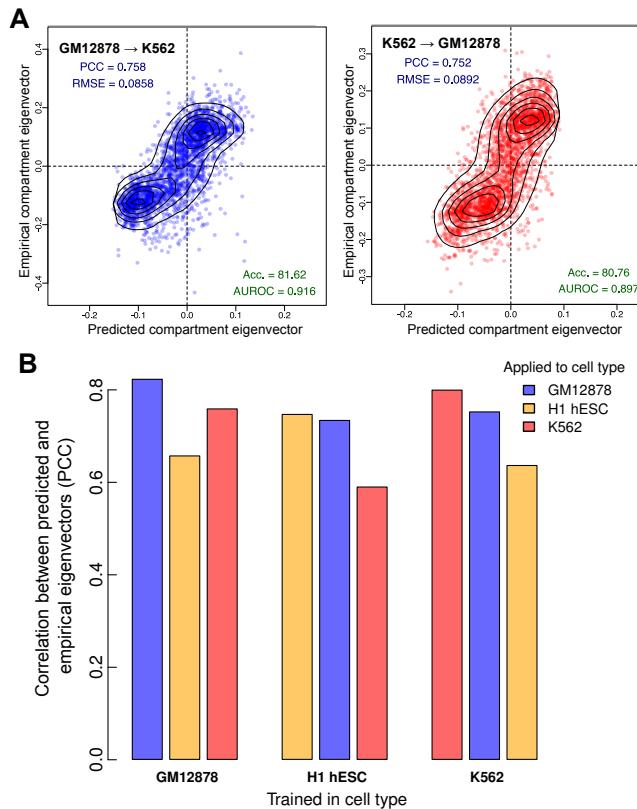


Figure 33: Models of higher order chromatin structure learned in one cell type can be cross-applied to others. Each model, trained in one cell type, was applied to the chromatin feature datasets from the other two cell types. (A) The GM12878 model achieved high accuracy when applied to K562 features ($PCC = 0.76$), as did the reciprocal cross ($PCC = 0.75$). (B) In each case, predictive accuracy decreased on cross-application but there remains significant agreement between predicted and empirical values. Acc., accuracy; AUROC, area under the receiver operating characteristic curve; PCC, Pearson correlation coefficient; RMSE, root mean-squared error.

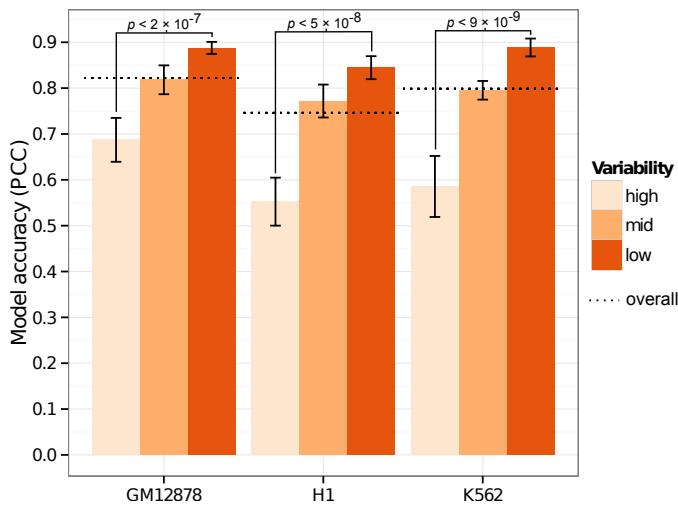


Figure 34: Genomic regions that vary across cell types are modelled less successfully than static regions. Genome-wide compartment eigenvectors were partitioned into thirds according to their median absolute deviation (MAD) across the three cell types under study. Models were fit independently to each third, and the modelling accuracy is compared.

4.4.4 Variable importance

Having built accurate predictive models, we next dissect the relative variable contributions made from our range of input features and compare these across cell types. An overview on the top 10 most highly-ranked features in cell type specific models shows some agreement but also substantial differences between cell types (Fig. 35)

Only one input feature, H3k9me3, is present in the top 10 most important variables of each model (Fig. 36). H3k9me3 is one of the few features to be negatively correlated with compartment eigenvectors (e.g. Fig. 37). Of those shared between two cell type models, H3k27me3 is also a repressive mark and deposited by polycomb repressive complex 2 (PRC2)^[170] while H2A.Z is a histone variant again linked to polycomb-regulated genes and essential for embryonic development.^[171] Furthermore EZH2, the catalytic subunit of PRC2,^[172] is also included in the feature set but only highly ranked in the GM12878 cell type model. As another example, MYC and MAX are found in the top 10 influential variables in H1 hESC, while MXI1 is found to be an informative variable in GM12878. This is in keeping with recent results suggesting MYC binds open chromatin as a transcriptional amplifier in embryonic stem cells,^[173,174] with MAX and MXI1 long being known as antagonistic co-regulators of MYC.^[175] These biological relationships between variables may help explain the observed differences between models: different representatives of correlated clusters of input variables may be being selected in each model (see Section 4.4.5).

To assess the significance of observed intersections (Fig. 36), the variable selection process could be modelled with, for example, a multivariate hypergeometric distribution or via simulation. Simulation was used here for simplicity: each intersection

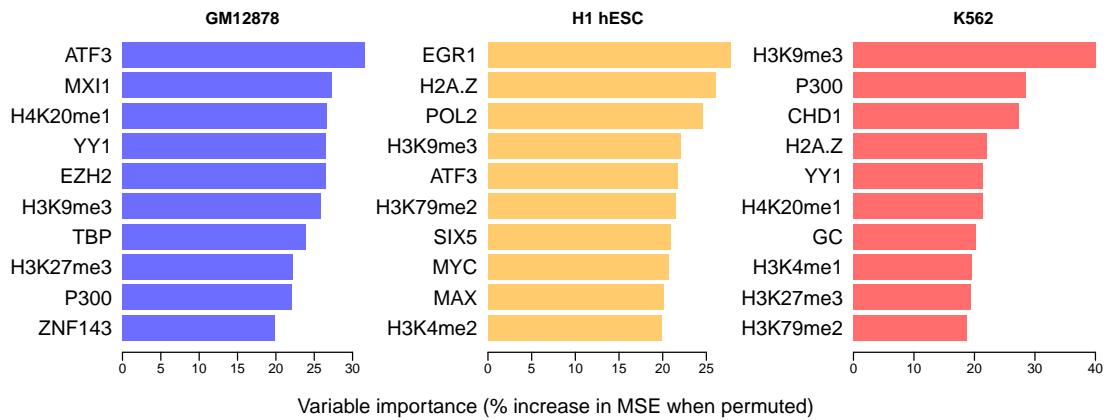


Figure 35: Variable importance per cell type specific model. Variable importance for each Random Forest model was measured in terms of percentage increase in mean squared error when permuted (Methods 2.3.1) and the top 10 ranking variables are shown for each model.

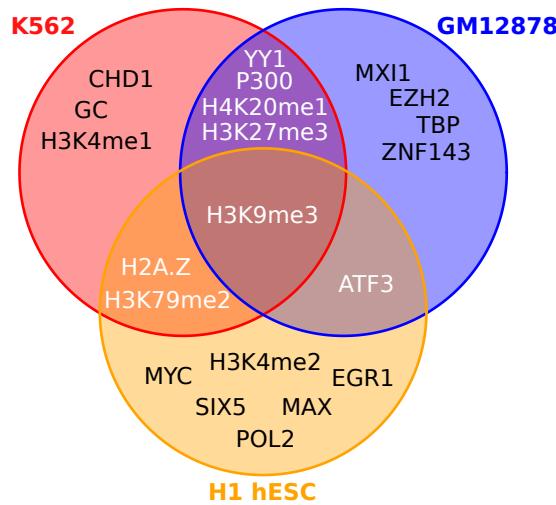


Figure 36: Intersections of the top 10 ranked variables in the cell type specific models. Venn diagram illustrating intersections between sets of ten most influential variables per cell type specific Random Forest regression model of compartment eigenvector (Fig. 35).

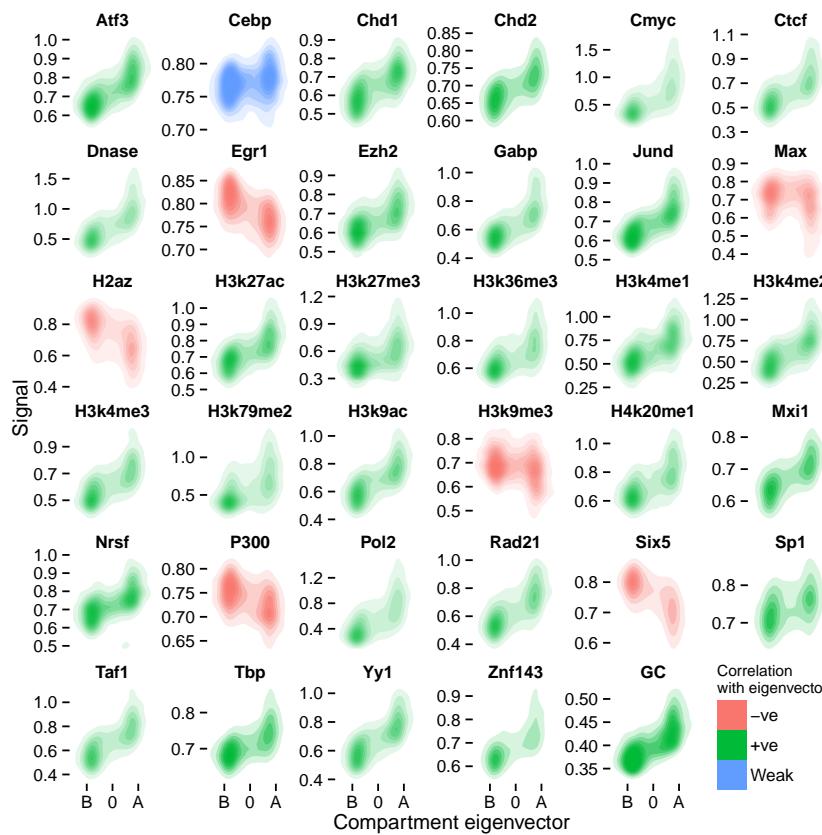


Figure 37: Correlations of individual features with compartment eigenvector in the H1 hESC cell type. Two-dimensional kernel density estimates show the density of points in a scatterplot of compartment eigenvector (*x*-axis) against each input feature individually (*y*-axes). Features with a PCC against eigenvector of above or below 0.1 are coloured as positive or negative, respectively.

was calculated under 10,000 variables draws with uniform distribution and empirical *p*-values were then calculated accordingly. Under the assumption that variables are ranked independently in each cell type, drawing at least one variable in all three cell types would be expected by chance ($p = 0.6$). Similarly, the overlaps between pairs of cell types is within the range of expectation (probability of 7 or more variables appearing in exactly two sets: 0.39). Hence these data suggest the top 10 most influential variables are not significantly more alike across the three cell-type specific models than expected by chance, however ten is an arbitrary cutoff, and many of the rankings are based on small differences in variable importance, thus could be unstable between multiple generations of stochastic Random Forest models.

In addition to rankings, raw variable importance metrics can be compared between cell-type specific models (Fig. 38). This shows that variables such as CTCF have a relatively small but highly consistent variable importance across the three cell type specific models, whereas other features like ATF3 are highly influential in one cell type but not the other two. Absolute differences in these figures should not be

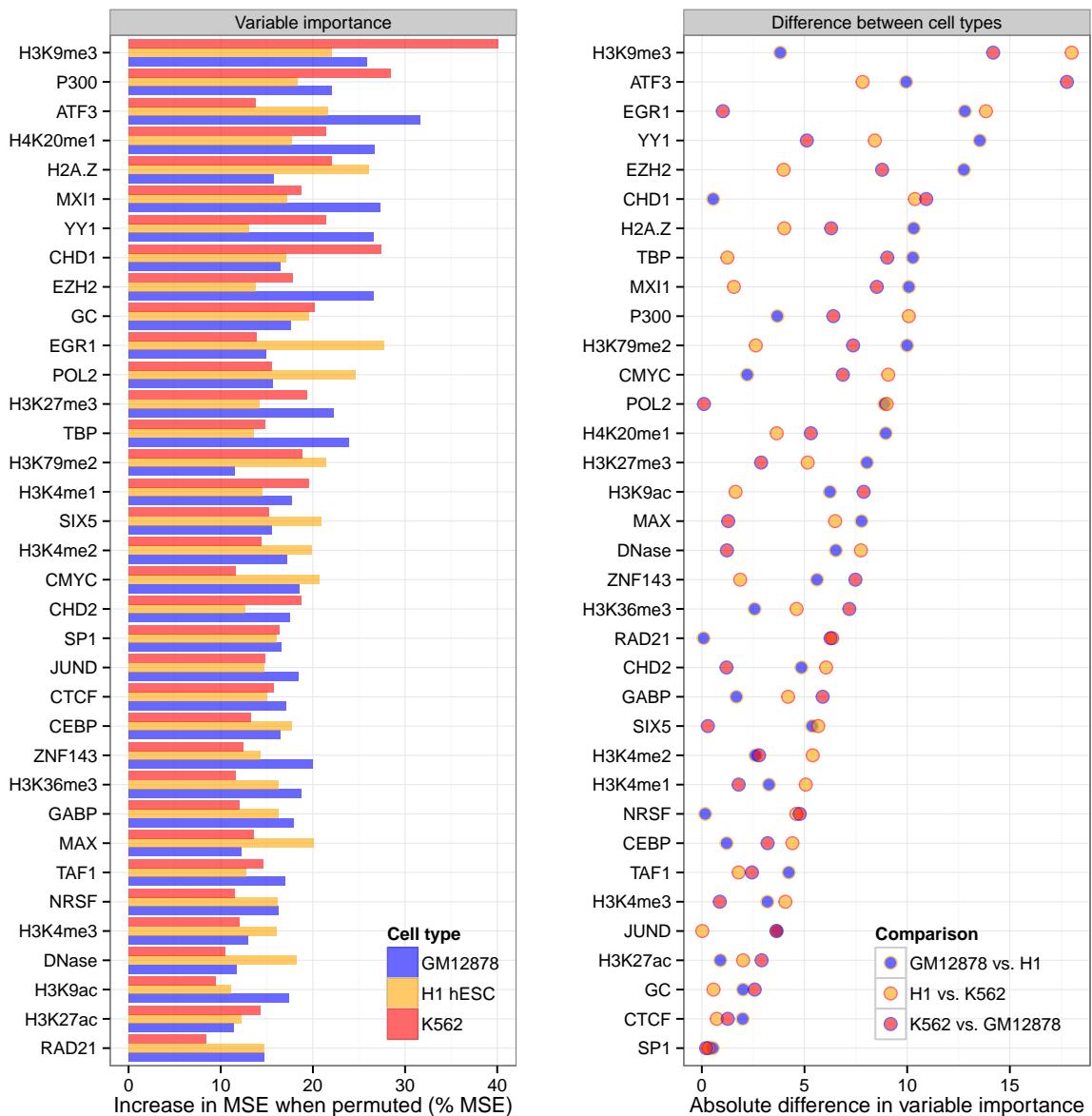


Figure 38: Comparison of variable importance between three cell type specific Random Forest models. Variable importance for each Random Forest model was measured in terms of percentage increase in mean squared error when permuted (Methods 2.3.1). Results are shown sorted by mean variable importance (*left*) and by largest absolute difference in pairwise comparisons (*right*).

over interpreted and will be affected to some degree by data quality, eigenvector calculation and other sources of noise. Nevertheless there are observations which may reflect biological phenomena, such as the higher relative importance of P300 in both hematopoietic cell line models, potentially reflecting its activity as a histone acetyl transferase that regulates hematopoiesis^[176] and a noted involvement with CTCF in chromatin looping.^[177]

4.4.5 Correlating input features

We have an *a priori* expectation of multicollinearity in our feature set, for example between those that each broadly correlate with transcriptional activity (including POL2, H3K36me3, GC content). To explore these relationships, we performed unsupervised clustering of our feature sets in each cell type (Fig. 39).

We found pervasive multicollinearity across our feature sets, with the majority of input variables in each model falling into a persistent “active” cluster containing regions with high DNase hypersensitivity, POL2 binding and histone modifications H3K36me3 as well as GC content (Fig. 39).

Outliers are also present. H3K9me3, noted for high variable importance in each model (Fig. 35) and the only feature ranked within the top 10 in each model (Fig. 36) is a clear outgroup in the H1 hESC and GM12878 correlation heatmaps, and in K562 forms a stable cluster only with the P300 transcription factor (Fig. 39). This suggests H3K9me3 is providing orthogonal information to many of the other input variables, and likely explains its high variable importance.

4.5 TECHNICAL CONSIDERATIONS

4.5.1 Resolution

Thus far models were built at 1 Mb resolution, but if we are capturing true biological relationships we would expect these to hold at higher or lower resolutions. To test this, models leaned at 1 Mb resolution were applied to feature sets binned at 100 kb, an order of magnitude higher resolution.

Model accuracy when applied to higher resolution input features proved to be similarly high, with empirical PCC being 88 to 95% as high as that at 1 Mb native resolution (Fig. 40).

Note however, there is some indirect leakage between test and training set when 100 kb bins have been used in aggregate in learning the 1 Mb models. Nevertheless, sustained accuracy is evidence that our models are not resolution-sensitive, and could likely be applied to higher resolutions than the 1 Mb predominantly used in this work.

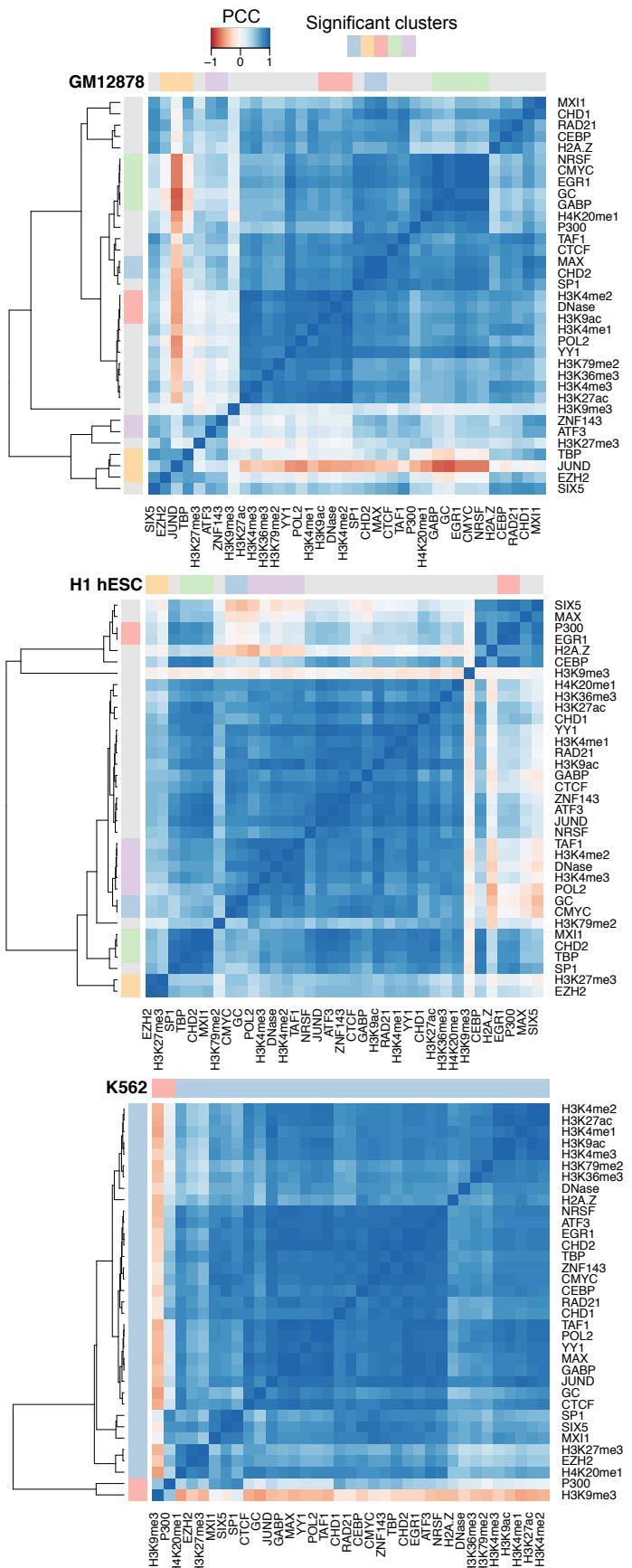


Figure 39: Correlation heatmaps of the 35 features used to model compartment eigenvectors. The Pearson correlation coefficient (PCC) of genome-wide 1 Mb bins of each feature were pairwise correlated with each other. The features were also clustered using hierarchical clustering. The significance of these clusters was determined through multi-scale bootstrap resampling, with those clusters that were stable across different sizes of resampling deemed significant, as implemented in the *pvclust* R package. [98]

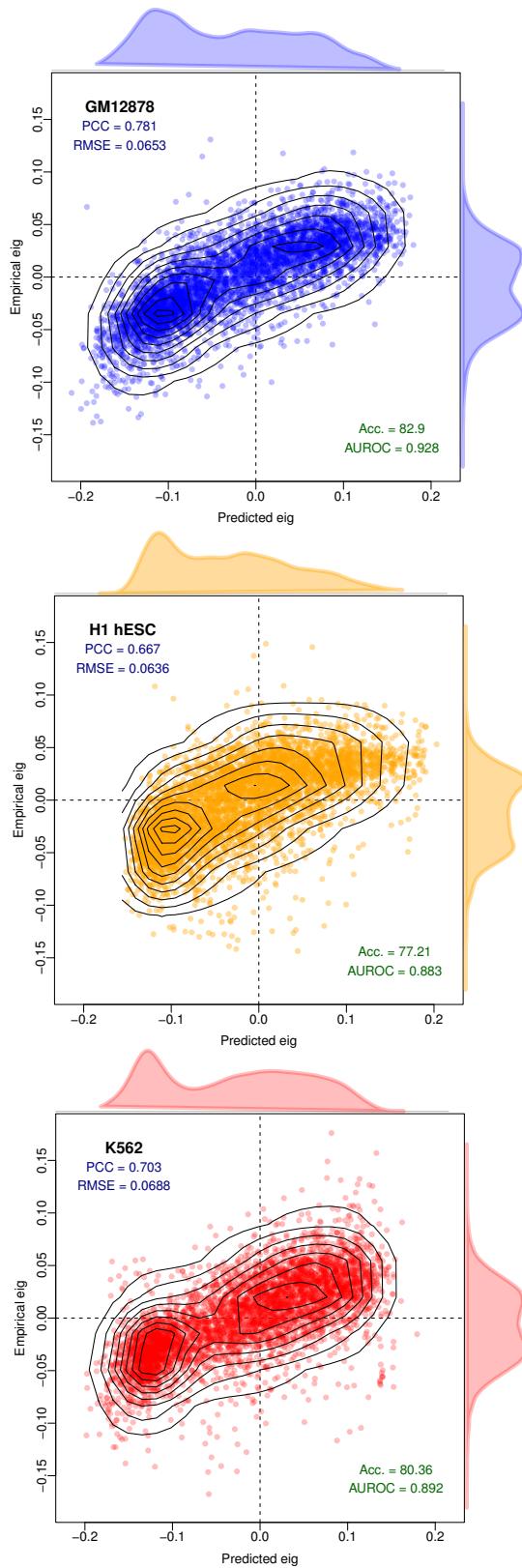


Figure 40: Models learned at 1 Mb resolution can be applied to higher resolution datasets. Despite having been trained on low resolution training sets, the Random Forest models generated can successfully predict compartment eigenvectors at higher resolution (100 kb, a 10 \times zoom). Eigenvectors at a higher resolution than this do not necessarily reflect A/B compartmentalisation.

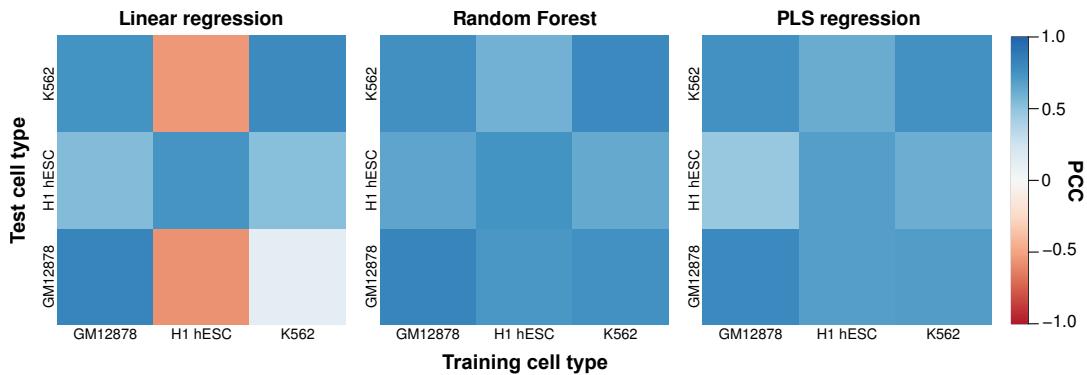


Figure 41: Comparison of Random Forest performance with other modelling approaches. Heatmaps show the Pearson correlation coefficient between predicted and observed compartment eigenvectors genome-wide for three regression techniques: multiple linear regression (LM), Random Forest (RF) and partial least squares (PLS). Results are summarised in Table 4.

Table 4: Performance comparison of different modelling techniques. Comparison of mean Pearson correlation coefficient between predicted and observed compartment eigenvectors for three different modelling approaches: LM: linear regression; RF: Random Forest regression; PLS: partial least squares regression. Correlations were averaged per cell type over three cell types (cell type specific) and in the six possible crosses (cross-application) shown in Fig. 41.

	LM	RF	PLS
Cell type specific	0.787	0.790	0.750
Cross-application	0.139	0.689	0.641

4.5.2 Other modelling approaches

Random Forest (RF) was *a priori* chosen as an appropriate and powerful modelling tool for this work. Other methods could have been used and should be compared. Here we compare our RF approach with two other options: multiple linear regression and partial least squares regression (Methods 2.3.6).

Our results confirm RF as a suitable and powerful approach for modelling our relationships of interest in this work (Fig. 41), with both the highest cell-type specific performance (PCC between predicted and observed = 0.790) and on cross-applications (mean PCC = 0.689).

Multiple linear regression assumes linear relationships between model parameters and input features and allows for simple, normally-distributed errors. Surprisingly, this simple approach is capable of accurate cell-type specific predictions (mean PCC = 0.787; Table 4), likely due to the high raw correlation between the inputs and dependent variable. However this simple approach fails to cross-apply between cell types (mean PCC = 0.139; Table 4) indicating a problems with overfitting. This can be remedied through variable selection procedures, however a strength of the RF approach is that this step is not necessary, and pre-selection of model variables may result in a sub-optimal end result.^[103]

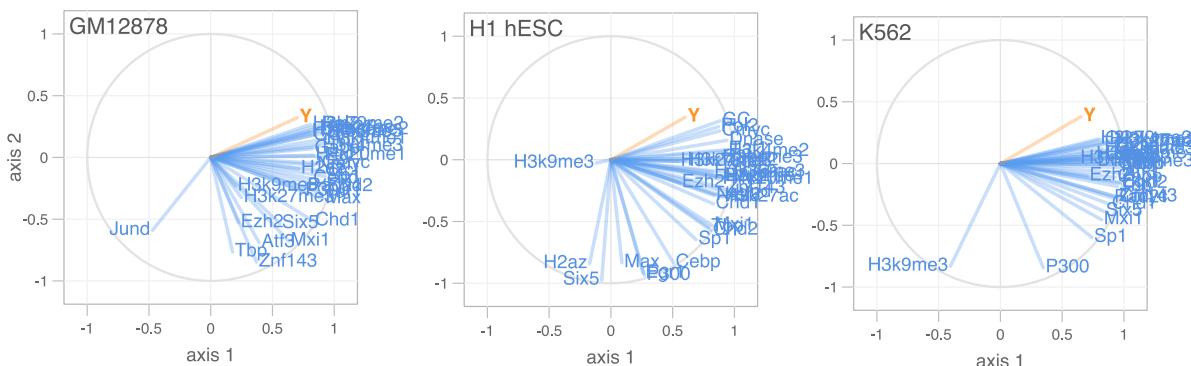


Figure 42: Circle of correlations of variables compared with PLS axes. Model variables are plotted against the first two axes used in PLS regression models per cell type. Y represents our compartment eigenvector.

Partial least squares regression is another technique which used dimensionality reduction to engineer a lower-dimension and orthogonal feature set. Hence this method is well-suited to multi collinear inputs, such as the set of variables used in this work (e.g. Fig. 39). As expected, PLS regression provides highly accurate cell type specific predictions (mean PCC = 0.750; Table 4) and during cross-application (mean PCC = 0.641; Table 4), though in both cases produces slightly inferior results to RF models (Fig. 41).

PLS uses a type of dimensionality reduction, which offers another way to explore the inter-relationships between our feature set. Plotting input features against these lower-dimension components can give a revealing insight beyond simple correlations (e.g. Fig. 39). Figure 42 shows a “circle of correlations”, where features are plotted onto polar co-ordinates against the first two PLS components (Methods 2.3.6). Interpretation of this figure is that nearby variables in the scatterplot are positively correlated, and the vector length from the circle centre is proportional to said variable’s representation in the model. Negatively correlated variables point in opposite directions while uncorrelated variables are orthogonal to each other.^[178] We therefore see the known multicollinearity represented as groupings of overlapping variables in each cell type, with a smaller number of orthogonal and negatively correlated variables in each cell type (Fig. 42).

4.5.3 Non-independence

As recognised through our use of Hidden Markov Models (Methods 2.5.2), consecutive bins along a chromosome are non-independent yet thus far predictive models have not considered this inter-dependence.

This is for two reasons: firstly non independence could be thought of as an artefact of bin-sizing (we have elected to use regular, fixed binning beneath the scale of

compartments themselves whereas another approach could use variable bin sizes, for example per compartment, TAD or restriction fragment); secondly using information of a bin’s surroundings may obscure by proxy the chromatin features which would otherwise prove predictive. As an example, knowing that bin x_{i-1} and bin x_{i+1} are in compartment state A would allow us with high confidence to predict the state of bin x_i , but without learning anything of the region’s relationship with its encompassed histone modifications and bound factors.

4.6 PARSIMONIOUS MODELS FROM EXPANDED FEATURE SETS

Strongly predictive models can be useful tools to reason about a complex system, however from a researcher’s perspective there also exists a trade-off between predictive power and parsimony. Namely simpler models with fewer inputs may be more interpretable and of wider utility, for example in cell types with less ChIP-seq data available than those used in this work. For this reason we explore parsimonious models with reduced feature sets, with an aim to build simpler models of chromatin state while retaining, if possible, similar levels of predictive accuracy.

Conversely, the 35 variables used thus far as model inputs are not the complete set available in each cell type, but only the subset of those assayed in all three cell types under study. The ENCODE consortium has produced a significantly greater number of datasets^[74,77] in each cell type which have thus far gone unused. Here we’ll explore models of higher order chromatin structure, in some cases built from over 100 variables, and then generate parsimonious models using optimal subsets guided by statistical techniques that penalise model complexity.

4.6.1 Stepwise regression

Multiple linear regression is a simple and analytically well-described modelling framework which is amenable to regularisation through a variety of methods. A simple approach is to start with a complete model and serially remove and/or add variables, then calculate a metric (here we use the Bayesian information criterion, BIC) which weighs the the model likelihood against model complexity. This process is iterated until the metric reaches a (local) minimum, thus creating a more parsimonious model which retains predictive accuracy and should be less prone to overfitting. Stepwise regression also aids interpretation by selecting representative features from collinear clusters.^[113] A detailed explanation of this feature selection procedure can be found in Methods 2.3.4. It should be noted that despite its continued widespread usage, several statistical issues have been identified with the stepwise procedure for model selection.^[114,115]

Table 5: Performance comparison of full and optimised RF and ML models. PCC between predicted and empirical compartment eigenvectors is shown for a range of modelling scenarios, including multiple linear regression (LM) and Random Forest (RF) approaches. For model selection, two methods are used: stepwise BIC-regularised linear models and LASSO regression; in each case those same features were then also used in building a separate RF for comparison.

	GM12878			H1 hESC			K562		
	n	LM	RF	n	LM	RF	n	LM	RF
All features	115	.836	.828	71	.744	.755	187	.811	.813
Matched subset	35	.827	.823	35	.740	.747	35	.796	.799
LASSO ℓ_1	23	.823	.836	23	.734	.750	39	.779	.811
Stepwise BIC	21	.840	.831	13	.746	.738	27	.819	.810

In terms of model performance alone, stepwise regression gives the highest predictive accuracy on a held-out validation set in each cell type specific model of compartment eigenvector (Table 5), however it must be said that differences in model performance across all comparisons are modest. These results do show that even expanded feature sets of up to 187 input features add little explanatory power beyond that of much less complex models with 20 or fewer input variables (Table 5).

4.6.2 LASSO regression

A more modern technique for regularisation of linear models is the least absolute shrinkage and selection operator (LASSO). In brief, the LASSO is a form of ℓ_1 regularisation that penalises the sum of absolute values of standardised regression coefficients. By penalising total absolute values, rather than squared values as in ℓ_2 regularisation, coefficients can be shrunk to 0 thereby removing terms from the model.^[106,116] Thus LASSO combines the coefficient shrinkage of techniques like Ridge regression with a type of feature selection as seen in stepwise regression. A detailed explanation of this method can be found in Methods 2.3.5.

Again we can perform a simplistic comparison of model performance using LASSO regression and other techniques (Table 5). LASSO retrieves comparable numbers of informative variables to the stepwise regression technique in each cell type, and again removes the majority of input features from expanded sets as redundant or relatively uninformative.

Of those variables with a non-zero coefficient at the optimally-selected tuning parameter λ (Methods 2.3.5), the ten largest in each cell type are shown (Fig. 43). Similarities can be observed with variable importance from subset models (Fig. 36), including the large (negative) coefficient for EGR1 in the H1 hESC model as well as that of P300 in K562 (Fig. 43).

Of interest is the appearance of group of factors known to interact as part of the activator protein-1 (AP-1), these include c-Fos, c-Jun and ATF1–3; all are spread across

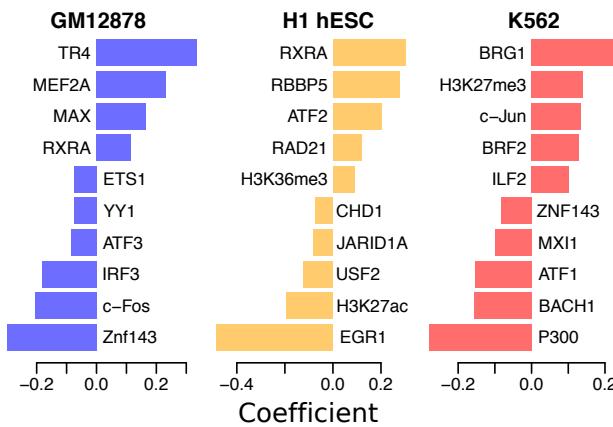


Figure 43: Ten largest LASSO model coefficients from expanded feature sets. Those coefficients with the largest absolute value are plotted for each cell type specific LASSO model.

the most highly-ranked variables in each model of chromatin organisation (Fig. 43). The AP-1 complex has been shown to have DNA bending properties,^[179] and recently FOS and JUN members were associated with long-range chromatin interactions^[180] suggesting an under-explored role for this complex in genome organisation.

4.6.3 Regularised Random Forest

Random Forest (RF) comparisons are included for comparison in Table 5 where RF models were built using model-selection procedures based on linear regression. The result of this is the linear regression-based feature selection acts as a "filter" method for feature selection, fully independent of the RF learning algorithm. A more coherent approach might be an "embedded" method, where a regularisation procedure is integrated with the learning algorithm.^[181,182]

While RF is a much younger technique than linear models, a framework for Regularised Random Forests (RRF) has recently been described^[183] and implemented in the R package RRF.^[184] The RRF algorithm uses the idea that at each node in a tree, unused variable should only be included if they offer a significant information gain over those available variables which have already been used in the tree. This differs from the standard RF algorithm where splitting decisions at each node are entirely independent of each other (Methods 2.3.1).

We found that this algorithm was unable to perform feature selection on our highly collinear feature set, instead leaving full or almost full feature sets in each case (*data not shown*) and so providing equal results to a standard RF model using expanded feature sets (Table 5).

5

CHROMATIN DOMAIN BOUNDARIES

5.1 INTRODUCTION

Multiple studies have defined chromatin domains of different types, for example: chromosome compartments;^[9] topological associating domains (TADs);^[10] contact and loop domains;^[13] physical domains;^[31,32] and others.^[42] The existence of these domains necessitates "boundary regions" either between consecutive domains or bookending more sparsely-positioned domains, however the functional relevance of said boundary regions is still open to debate.

In their study of topological domains, Dixon *et al.* identified average enrichments over TAD boundary regions in both human and mouse for various features including CTCF and PolII.^[10] Boundaries were also enriched for signs of active transcription, such as with the histone modification H3k36me3. These results, coupled with an observable enrichment for promoters at domain boundaries, have lead to the theory that boundaries may act as an additional layer of transcriptional control,^[40] however an alternative theory could be that looping between enhancer elements and promoters results in an observable boundary through C-method experiments.^[13] Another non-exclusive explanation is that if chromatin domains represent co-regulatory regions as is widely thought,^[40,41,185] boundaries themselves could be mere side-effects and as such of limited biological interest.

An obvious experiment to resolve these opposing theories would be to delete a predicted boundary region and test for local changes in both contacts and expression. Such an experiment was performed on a region of the human X-chromosome containing the genes encoding the dosage-compensation long non-coding RNAs Xist and Tsix, which are separated by a TAD boundary.^[29] This study found that while histone modifications within the body of a TAD could be removed without affecting the structure, deletion of a boundary did have an effect and lead to increased intradomain contacts.^[29] Surprisingly however, this effect was not total and some observable barrier remained, lending evidence that TADs may be centrally constrained, rather than by their borders.^[29]

A second experiment used CRISPR genome editing to link TAD boundary changes with limb development disorders,^[186] indicating that boundary changes could provide an underlying explanation for pathogenic non-coding structural variants.^[187] Similarly, domain boundaries on X-chromosomes were found to be weakened following the disruption of condensation binding sites.^[33] Together these studies suggest a complex

scenario whereby TAD boundaries are an important structural feature, yet do not fully explain domain partitioning.

Computational analysis of boundaries has emerged during the time this work was completed. Border “strength”, here defined by the ratio of total intra:inter-domain contacts, was found to correlate with increased occupancy of a combination of bound architectural proteins.^[61]

Many questions remain about chromatin boundaries. For example, are the observed enrichments persistent across cell types and how do they compare across organisation strata, such as compartments and TADs? Through computational analysis of the set of boundaries re-called from published datasets, we can investigate these questions and probe boundary enrichments across a broad array of locus-level chromatin features.

5.2 TAD AND COMPARTMENT BOUNDARIES

The mammalian genome is organized into TADs, predominantly self-interacting chromatin domains, with boundary regions reportedly associated with pronounced peaks and troughs of particular features within 500 kb of the predicted boundary.^[10] Exploration of this phenomenon using a set of 24 mouse ESC chromatin features (and a smaller number of human ESC features) reportedly revealed enrichment peaks of CTCF, H₃K4me3 and H₃K36me3, as well as a pronounced dip in H₃K9me3, suggesting that high levels of transcription may contribute to boundary formation.^[10] However, it was unclear whether other features show unusual patterns in TAD boundary regions, and whether the constellation of features involved changes between cell types. The features associated with boundaries separating A and B compartments calculated from Hi-C eigenvectors have not been studied to our knowledge. The datasets assembled here, consisting of 35 matched chromatin features across three cell types, allow us to conduct the first comparative study of the constituents of human TAD and compartment boundary regions.

We derived TAD boundaries according to established methods (see Methods 2.1.5) for all three cell types under study. We then sought evidence for significantly enriched or depleted features at TAD boundary regions using a conservative approach (a nonparametric statistical test and Bonferroni multiple testing correction, see Methods ??).

Our findings confirmed the previously reported peaks (CTCF and POL2) and dip (H₃K9me3) in ESC data, but also revealed substantial heterogeneity between cell types. CTCF binding was found enriched at TAD boundaries across all cell types, but other features, including H₃K36me3 and H₃K4me3, show dramatic peaks of enrichment in H₁ hESC cells that are not seen consistently in other cell types (Figure 6, Additional file 1: Figure S12). Although the dip in H₃K9me3 at TAD boundaries is seen in all

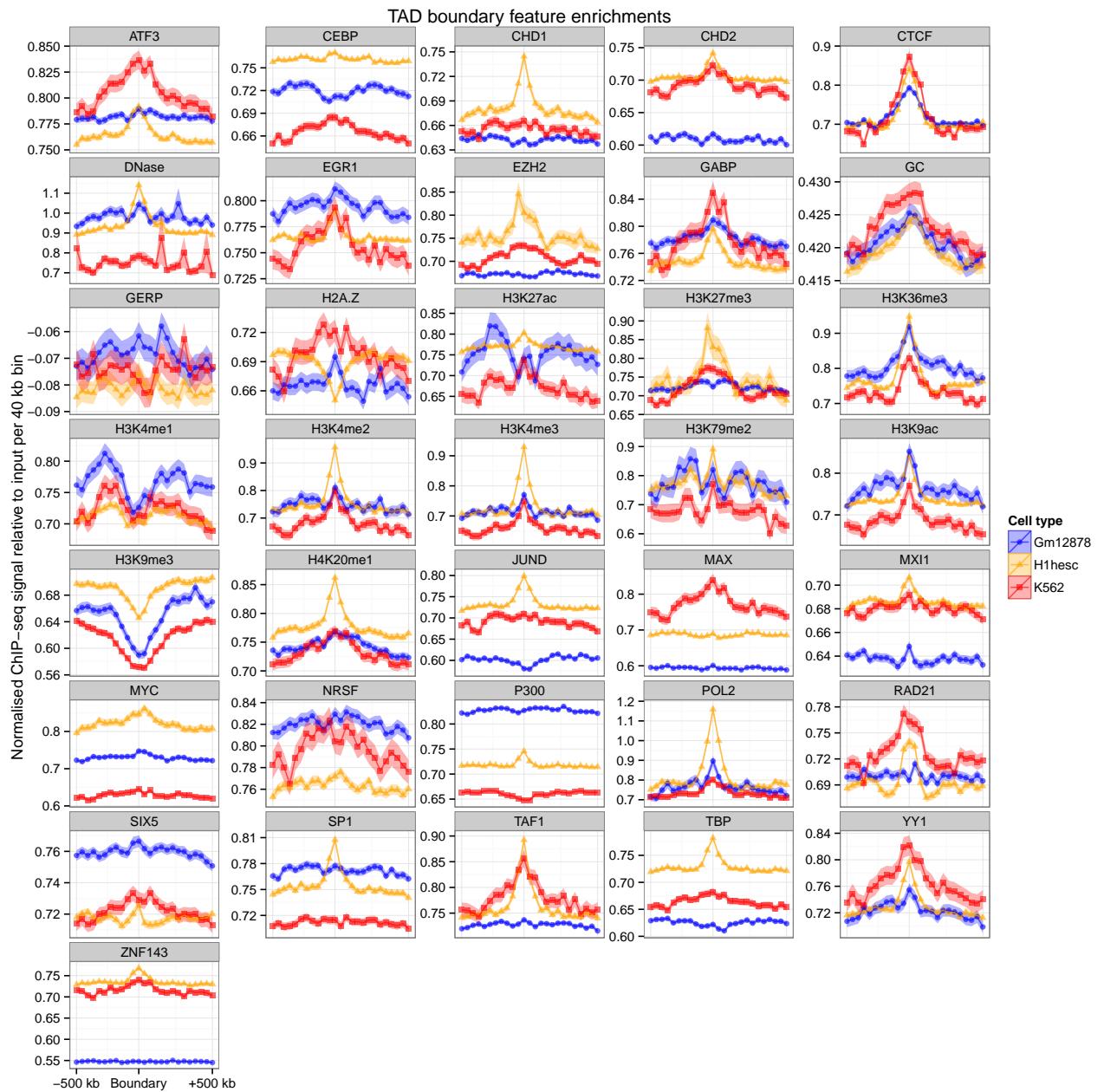


Figure 44: TAD boundary enrichments and depletions. 36 features were averaged over 1 Mb windows centred on TAD boundaries genome-wide (25×40 kb bins). Ribbons represent 95% confidence intervals of the mean at each position.

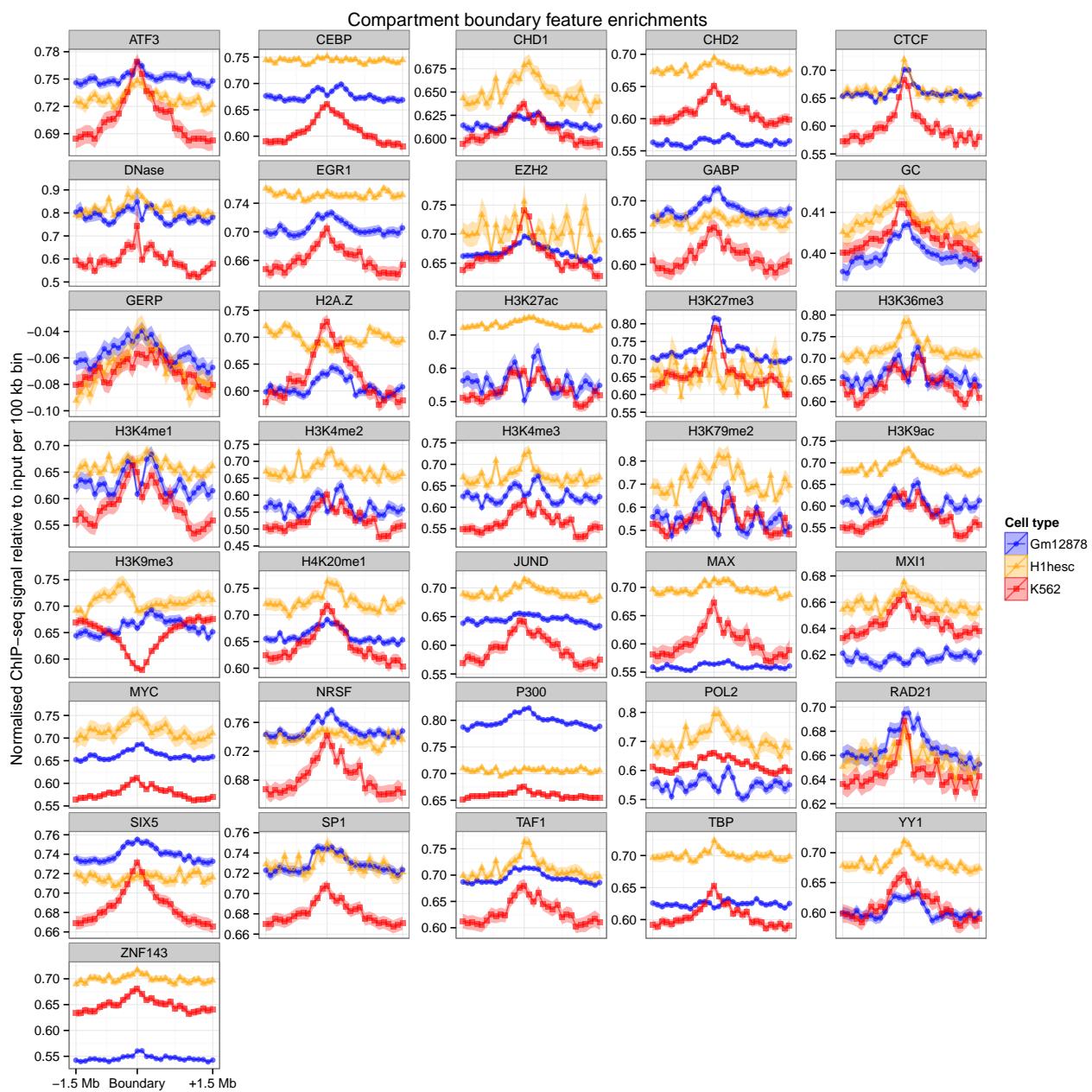


Figure 45: Compartment boundary enrichments and depletions. 36 features were averaged over 3 Mb windows centred on compartment boundaries genome-wide (30×100 kb bins). Ribbons represent 95% confidence intervals of the mean at each position.

cell types, the extent of the depletion varies and is weakest in H1 hESC cells. Many other features show significant, though often modest, enrichments in a particular cell type. However, overall the complexity of TAD boundaries (measured as the number of strongly enriched features) is notably higher in H1 hESC than in the other two, more differentiated, cell types (Figure 6), involving large increases in the binding of sequence specific factors such as SP1 and JUND.

Across all three cell types several features demonstrate consistent and statistically significant patterns at TAD boundaries (Figure 6, Figure S12), including peaks associated with active transcription of genes (POL2, H3K9ac) and dips in H3K9me3, as previously reported.^[10] However other novel feature peaks of interest emerge across cell types, such as peaks of H4K20me1, a modification previously implicated in chromatin compaction.^[188] We also observe consistent increases in GC content at TAD boundaries, at a scale that is difficult to reconcile with the presence of smaller-scale features such as repeat elements or CpG islands (Additional file 1: Figure S12).

Where neighbouring genomic regions occupy contrasting A and B nuclear compartments, the disparity implies the presence of a boundary region. Putative compartment boundaries were identified by using an HMM to infer the state sequence of A/B compartments across the genome based on observed principal component eigenvectors. Analogously to the TAD boundary analysis we then sought significant enrichments or depletions in 36 chromatin features over these compartment boundaries (Figure 6, Figure S13). Compartment boundaries display similar spectra of enrichments to previously studied TAD boundaries^[10] but at lower resolution, reflecting the different scales of these levels of organization (Figure 6B, Figure S13). Peaks associated with active promoters (POL2, TAF1, H3K9ac) are again evident. Parallel enrichments of CTCF, YY1 and H4K20me1 are also seen at compartment boundaries, as they were for TAD boundaries, in each cell type under study. In addition, compartment boundaries show enrichments of H3K79me2, which is known to play critical roles in cellular reprogramming.^[189] Remarkably, H3K79me2 has also recently been shown to mark the borders of small (hundreds of bp) regions of open chromatin.^[190] Thus there may be similarities in chromatin compaction boundaries at very different scales.

Certain features show intriguing contrasts between cell types the histone variant H2A.Z lacks any trace of enrichment at H1 hESC compartment boundaries, but is significantly enriched in the other two cell types (Figure 6A), consistent with reports describing H2A.Z relocation during cellular differentiation.^[191] Compartment boundaries also show enrichment for the cohesin complex subunit RAD21 in the two hematopoietic cell types , and cohesin is another factor implicated in modulating nuclear architecture in partnership with CTCF.^[38] Various other enrichments with very modest effect sizes are also evident at compartment boundaries (Figure 6B, Figure S13). In contrast to TAD boundaries, the composition of compartment boundaries appears least complex in H1 hESC, relative to the other two cell types. Overall compartment and TAD boundaries are associated with overlapping spectra of chromatin features

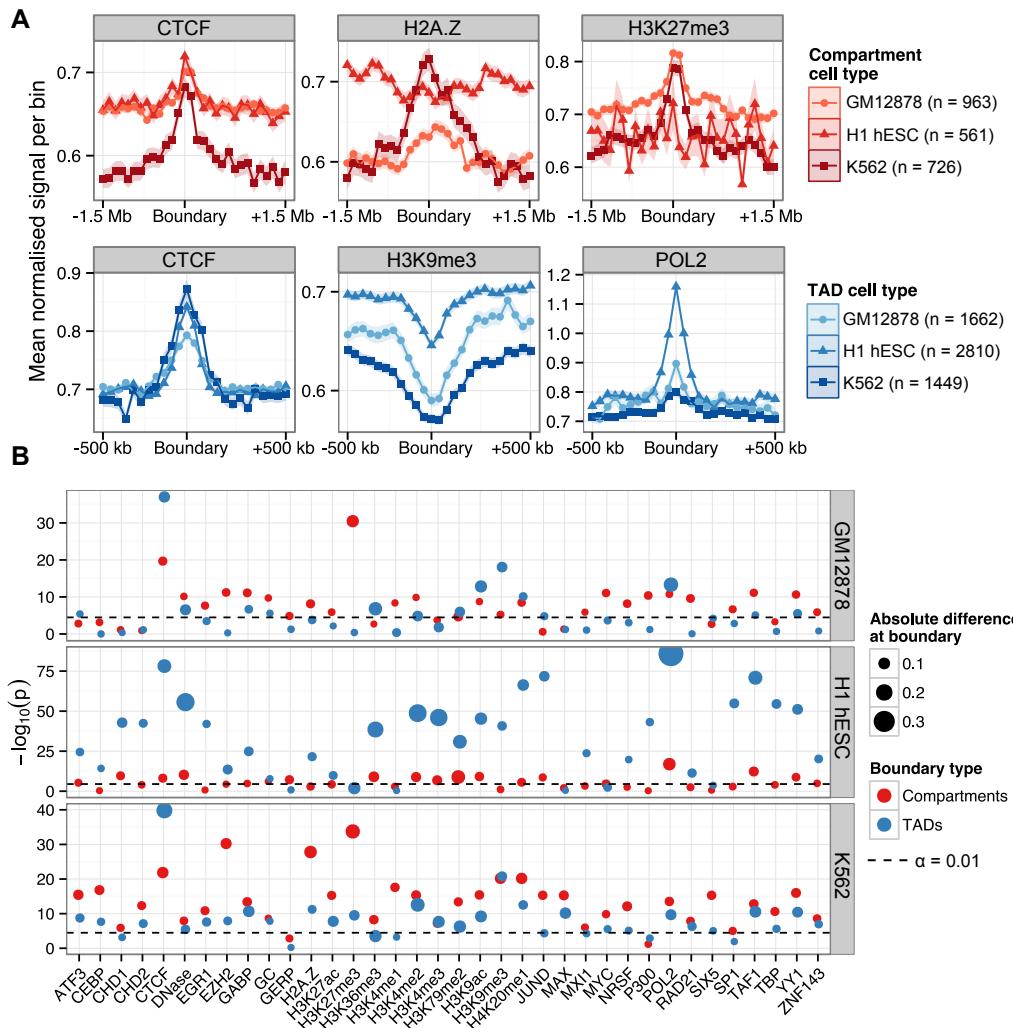


Figure 46: Compartment and TAD boundary enrichment summary in three human cell types. (A) Selected profiles for locus-level features are shown for TAD boundaries (CTCF, H3K9me3 and YY1) and compartment boundaries (H2A.Z, H3K4me2 and YY1), as a mean normalized ChIP-seq signal relative to input chromatin per bin (± 1 standard error). TAD boundaries were examined over 40 kb bins over the 1 Mb flanking each boundary; compartment boundaries were examined over 100-kb bins over 3 Mb. (B) The significance of enrichment or depletion ($-\log_{10}(p)$ two-tailed Mann–Whitney test) of a feature was calculated as the boundary bin relative to the ten most peripheral bins (five either side). Points are scaled by the absolute mean difference in signal over the boundary relative to the mean of peripheral bins. ChIP-seq, chromatin immunoprecipitation sequencing; TAD, topological domain.

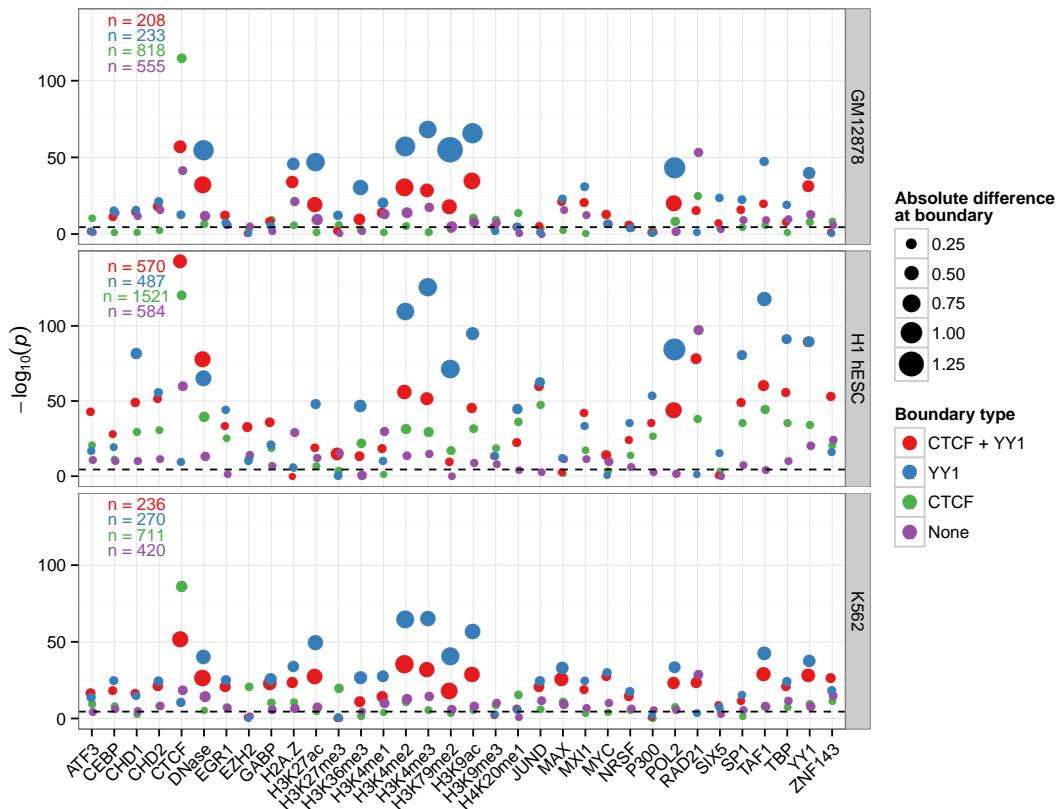


Figure 47: Distinct enrichments of CTCF and YY1 boundaries. TAD boundary feature enrichments are shown (as in Fig. 46) for boundaries split into classes based on specific enrichments: CTCF and YY1 groups are those boundaries with at least one ENCODE region peak^[74] for their respective features, while CTCF + YY1 is the group of boundaries which had one or more overlapping peaks for these two factors. Boundaries in the none group has neither a CTCF or YY1 region peak called (but can still be enriched for their respective features in terms of raw signal).

across cell types. These involve DNA binding proteins implicated in chromosome architecture (CTCF, YY1, RAD21), but also implicate the initiation and repression of transcription as critical to boundary formation. However these two boundary classes occur at different scales, with patterns of informative features typically spanning regions up to 500 Kb for TAD boundaries, and patterns associated with compartment boundaries often spanning more than 1 Mb.

5.2.1 CTCF and YY1

Significant peaks in YY1 are evident in all cell types, which is intriguing given the evidence that YY1 and CTCF cooperate to affect long distance interactions.^[192] Co-binding of CTCF with YY1 has also been shown to identify a subset of highly conserved CTCF sites.^[193] Co-binding of CTCF and YY1 may also therefore be a contributing

factor in the establishment of TAD boundaries, which appear to be broadly conserved across mammals.^[10] To test this, we split our sets of TAD boundaries into those possessing ChIP-seq peaks (region peaks called by ENCODE^[74]) for CTCF, YY1, both CTCF and YY1 (overlapping peaks) and neither. We then tested each boundary subset for genome-wide enrichments of the other features in our dataset (Fig. 47). Unexpectedly, we found that boundaries marked by YY1 (without overlapping CTCF peaks) were generally most strongly-enriched for other features in our dataset. We also found that boundaries lacking both CTCF and YY1 peaks showed instead the strongest enrichments for RAD21 in each cell type (Fig. 47), reinforcing previous findings that describe the distinct influences of CTCF and cohesin in organising chromatin structure.^[38,58,194]

5.2.2 Repeats

Dixon *et al.*'s study of TAD boundaries identified short interspersed element (SINE) repeats as being enriched over domain boundaries and suggested roles for these repeats in altering genome organisation, in line with prior evidence.^[10,195] Interestingly, SINE elements are thought to be responsible for spreading CTCF binding sites through mammalian genomes^[196] (thought not in primates^[193]). Analysis of recent high-resolution Hi-C data again reported a SINE B2 link with CTCF loops in mice.^[13] Together these results suggest repeats could be a key component in the makeup of domain boundaries.

To investigate this, we used the RepeatMasker^[197] software package to call repeat classes and families in the hg19 and mm10 genome assemblies. Counts for each annotated feature were then average over boundaries as described previously (Methods 2.5).

At the level of repeat class, we corroborate the findings of Dixon *et al.*^[10] that the majority of repeat classes show no enrichment or depletion at TAD boundaries, and we find that this also holds for compartment boundaries (Fig. 48). A notable exception is the short interspersed element (SINE) repeat class which appears to be enriched at TAD boundaries in each cell type. Testing the significance of this observed peak confirms this to be the case, with SINEs significantly enriched at TAD boundaries in each cell type, and borderline significant enrichments can also be observed at compartment boundaries (Fig. 49).

Repeat class profiles also suggest LINEs may be depleted over TAD boundaries and DNA repeats may be enriched at both boundary types (Fig. 48), however statistically these observations do not surpass our pre-defined significance threshold ($\alpha = 0.05$) after multiple testing correction (Fig. 49).

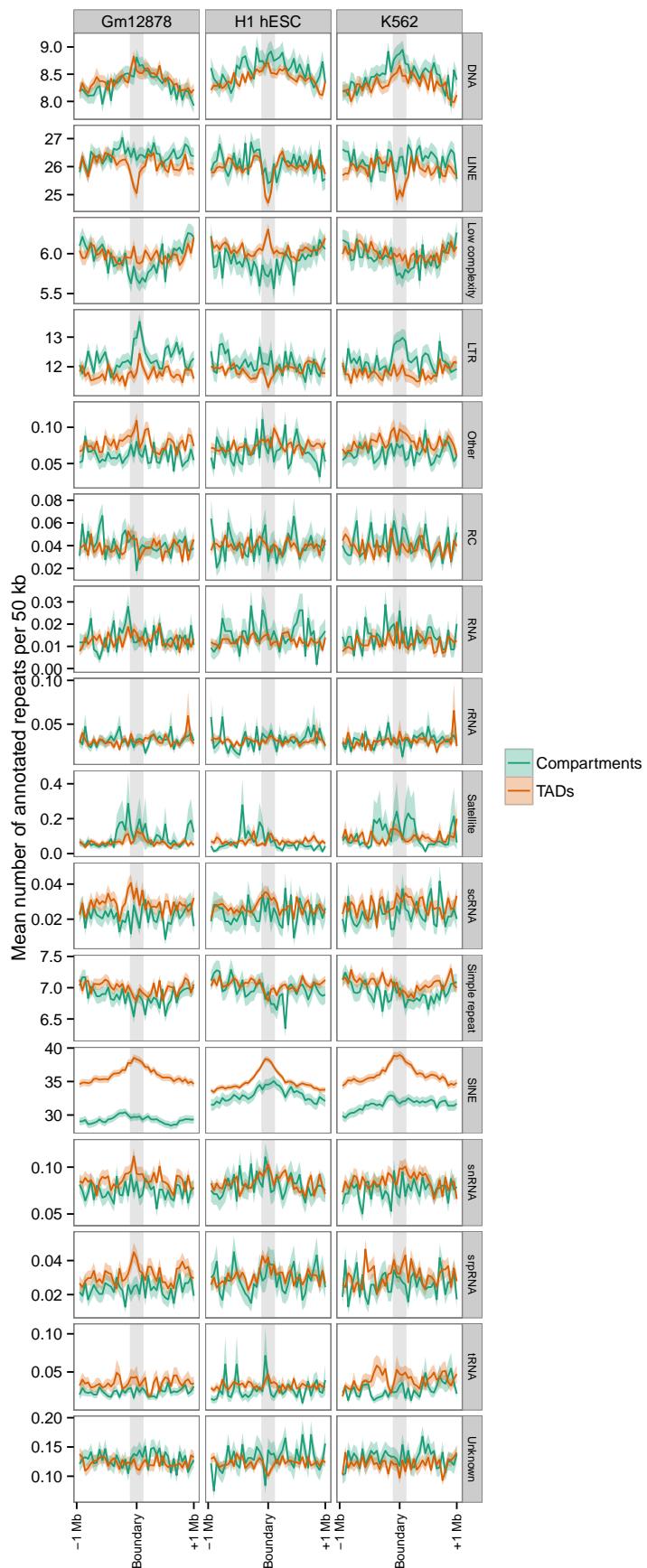


Figure 48: Repeat class average-o-grams over all TAD and compartment boundaries. RepeatMasker repeat annotations are counted per 50 kb for 1 Mb either side of each TAD and compartment boundaries. The mean count genome-wide is plotted with $\pm 95\%$ confidence intervals.

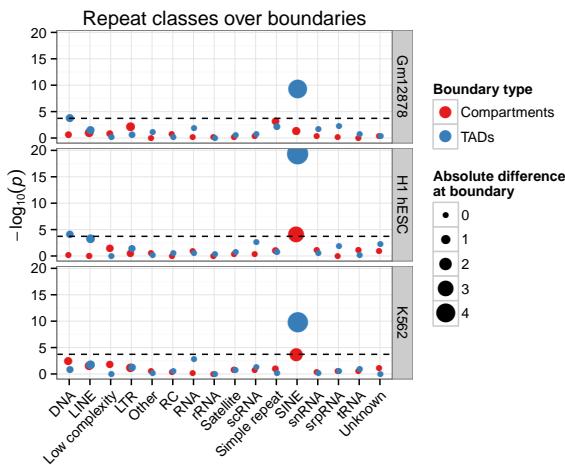


Figure 49: Significance and effect sizes of repeat class enrichments/depletions over boundaries. Boundary profiles (Fig. 48) were tested for enrichment or depletion of each factor at the boundary bin relative to peripheral non-boundary bins (see Methods 2.5). Bubble area is proportional to the raw effect size of an enrichment or depletion. The Bonferroni-corrected significance threshold is highlighted with a dashed line.

Repeat classes can be broken into smaller repeat families. Dixon *et al.*[¹⁰] reported that the Alu (or B1 in mouse) repeat families are enriched over TAD boundaries. Again we can reproduce this finding and extend it to compartment boundaries (Fig. 50).

5.3 DE NOVO BOUNDARY PREDICTION

We have shown TAD and compartment domain boundaries to be well-marked by a variety of features. Compartment boundaries are successfully predicted as a side-effect of modelling the continuous compartment profile eigenvector (Section 4.4) however a related measure of activity and repression does not exist for TADs. Instead then, we attempt to predict TAD boundaries within a class-balanced classification framework.

5.3.1 Learning boundary classification

Results presented in this thesis describe the spectra of chromatin marks over TAD boundaries (Figs. 44, 46), it is thus of interest to test if we can build a predictive model (in the manner of Chapter 4) that can call boundary regions from these marks alone. Such a model, if successful, could have broad utility in domain prediction in metazoan organisms where Hi-C data is not available.

A straightforward approach to this modelling task is to build a supervised classifier that learns the associations between two classes of genomic region: those labelled TAD

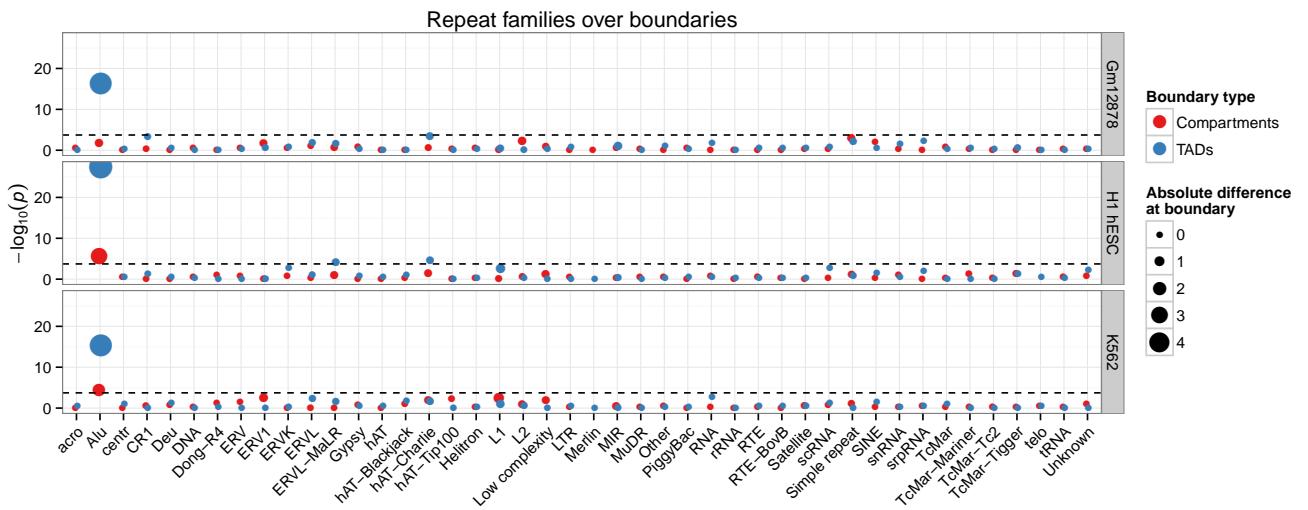


Figure 50: Significance and effect sizes of repeat family enrichments/depletions over boundaries. As per Fig. 49 but for a higher resolution repeat classification.

boundaries and those which are not. To this end, we again turn to a Random Forest (RF) model, due to its many attractive properties discussed previously (Methods 2.3.1). Our input feature set is made up of the same 35 matched features used in models of compartment eigenvector (Section 4.4), with the addition of Alu repeat elements (Section 5.2.2). Classifications are those produced by the Dixon *et al.*^[10] TAD calling algorithm (Methods 2.1.5), therefore TAD boundaries were resolved to 40 kb bins. We class such bins as boundary true positives (TP), and select matched bins 500 kb upstream as boundary true negatives (TN) for our training set.

To build parsimonious and accurate models (as discussed in Section 4.6), we used the AUC–RF algorithm.^[122] This is a form of stepwise model selection which optimises feature subset selection relative to the area under the receiver operating characteristic (AUROC), a metric which captures both the speciality and sensitivity of a classifier. This method was used a training set of 80% of boundaries per cell type, with predictions assessed on out-of-bag (OOB) data as each forest was constructed. Selected models were then applied to the remaining held-out test set of 20% of TAD boundaries, with their matched non-boundary bins (full details are in Methods 2.6).

Predictive performance of these models is shown as ROC plots (Fig. 52) and in each case an AUROC of around 0.67–0.71 was achieved. In practice, this means that each classifier has around a 70% probability of ranking a random boundary region more highly than a random non-boundary region.^[198] According to a commonly-used AUROC “rule of thumb”, this performance falls between the ranges of “poor” to “moderate” classification accuracy.^[199]

Despite this sub-optimal classification accuracy, it is still of interest to analyse the variable importances in each cell type model. Strikingly we find that CTCF stands

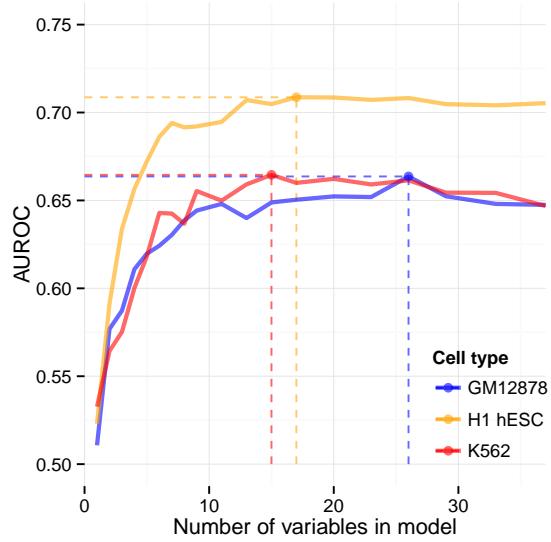


Figure 51: The AUC-RF stepwise algorithm finds that variable subset which maximises the AUROC on out-of-bag data. The AUROC is calculated at each stage of a stepwise method for selecting the best subset model from a full featureset. Here AUC-RF selected the following combinations: GM12878: 26 vars, 0.66 AUC; H1 hESC: 17 vars, 0.71 AUC; K562: 15 vars, 0.66 AUC. The AUC-RF algorithm is described in Methods 2.6.

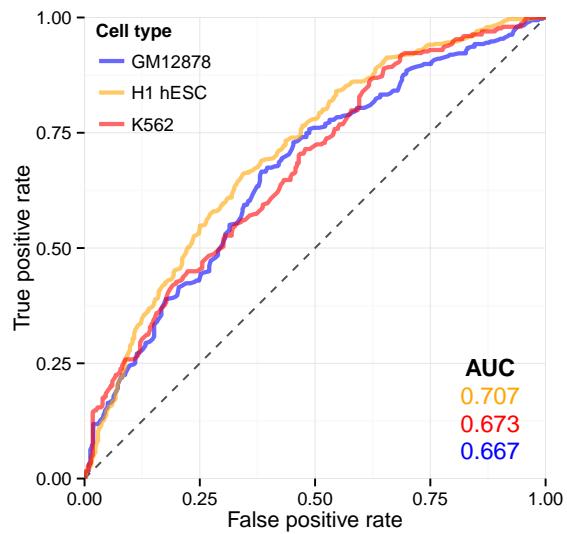


Figure 52: Receiver operating characteristics for TAD boundary classifications. ROCs are shown for three cell-type specific classifiers of TAD boundary bins. The area under each curve is also shown (*inset*).

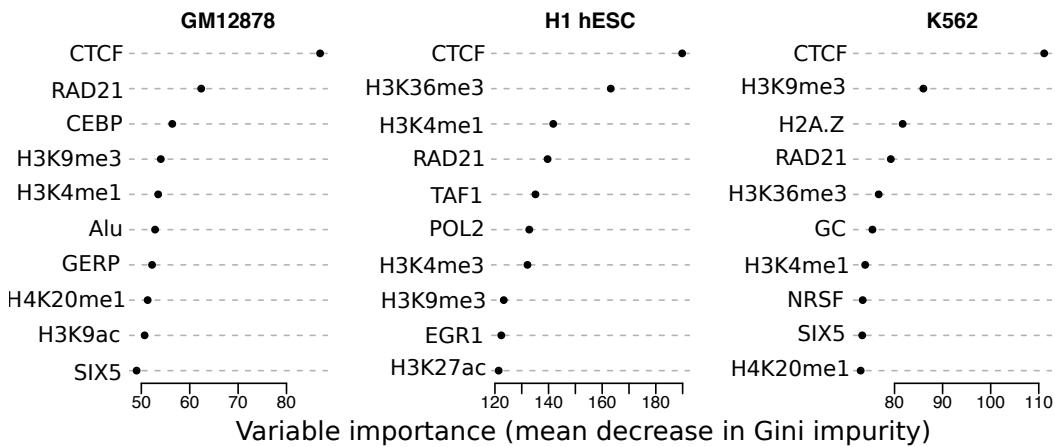


Figure 53: Variable importance for boundary classification Random Forest models. The highest ten most important variables in each boundary classification model are shown and ranked by their variable importance as defined by mean decrease in Gini impurity (Methods 2.6.2).

out as the most informative variable in each classifier by some margin (Fig. 53). This is in agreement with our results that CTCF showed among the highest and most consistent enrichments at TAD boundaries (Fig. 46). RAD21 is also highly ranked in each case and this ties in with our previous results suggesting orthogonal boundary enrichments for either CTCF or RAD21 (Section 5.2.1). Surprisingly YY1 does not feature as highly ranked in any model despite our observed consistent enrichments at TAD boundaries (Fig. 46). In fact YY1 was preened from the optimal H1 hESC and GM12878 models by the AUC-RF algorithm due to its low variable importance (*data not shown*). This could be due to a redundancy between information provided by YY1 and the CTCF variable as, for example, co-binding of YY1 and CTCF is thought to occur at sites of long-range chromatin interactions.^[192]

5.4 METATAD BOUNDARIES

Our collaborators uncovered the concept of “metaTADs”: sequential aggregations of adjacent and strongly-interacting TADs to form a hierarchy of domain organisation covering each chromosome.

MetaTADs are constructed simply by performing constrained heretical clustering based on inter-TAD contacts. That is, those two neighbour TADs that have the largest number of interTAD contacts are linked to form a metaTAD and this process is recursed until all TADs on a chromosome are joined into a tree-like network which fully describes the hierarchical nature of domain organisation.

My contribution to this work was to explore these newly-described metaTAD structures and perform boundary analysis as was done with TADs and compartments

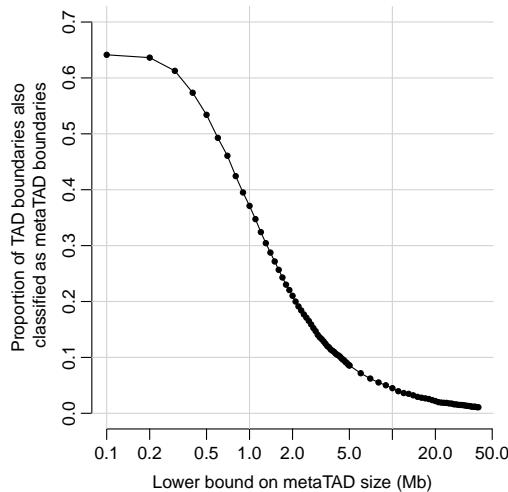


Figure 54: Calibration of metaTAD size selection bounds. As the lower bound on metaTAD size is increased, the proportion of all TAD boundaries which are also metaTAD boundaries decreases.

(Section 5.2). A testable hypothesis, for example, is that boundaries of larger metaTAD structures could display greater enrichments for boundary-defining features.

5.4.1 MetaTAD / TAD boundary comparison

Due to the way metaTADs were constructed by our collaborators, by sequential aggregation of TADs (Methods 2.7), boundary comparisons between TADs and metaTADs are not completely straightforward. For one, every metaTAD boundary is, at a lower level, also a TAD boundary hence for a meaningful comparison we compared only a subset of metaTAD boundaries. Selection of this threshold involved a trade-off between maintaining a sufficient sample size of metaTADs and minimising the overlap between metaTAD and TAD boundaries, as a proportion of all TAD boundaries (Fig. 54).

From this calibration plot, a lower bound metaTAD size cut-off of 10 Mb was selected for comparison with TAD boundaries. This left a reasonable sample size of 263 metaTAD boundaries, while reducing the overlap with the set of all TAD boundaries to approximately 5% (Fig. 54). We also used an upper bound for size selection, based on observations by our collaborators that interactions between metaTADs larger than around 40 Mb were no higher than expected background signal (*data not shown*). In practice, almost all boundaries making up metaTADs larger than 10 Mb are also present in those larger than 40 Mb, but as hierarchical clustering continued up until a whole chromosome level, this upper bound may exclude a small number of edge-case peripheral TADs which aggregated into chromosome-wide metaTADs without evidence of heightened intra-TAD interactions.

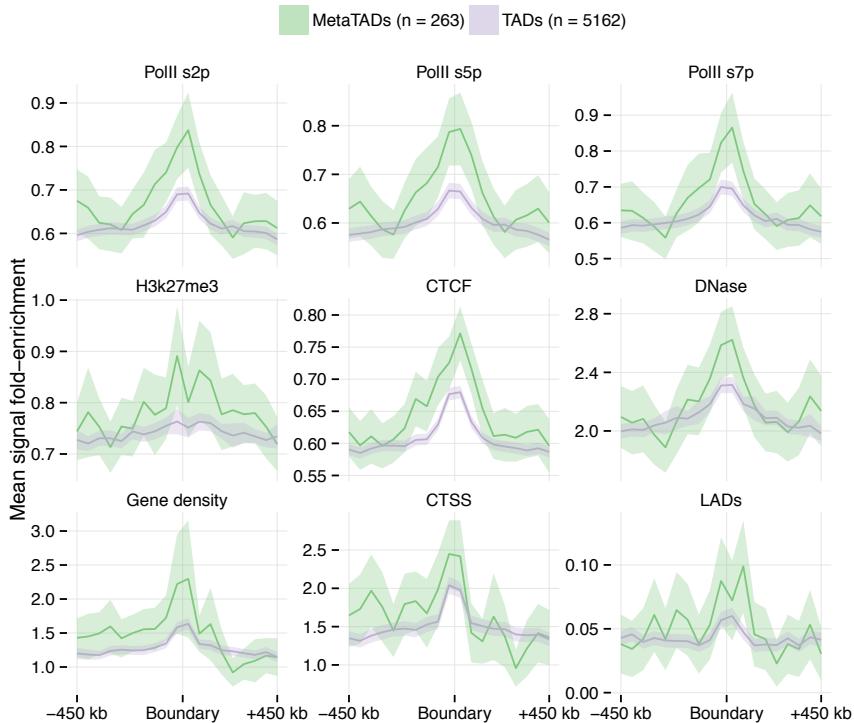


Figure 55: Large metaTADs show greater enrichments for an array of boundary features. Genome-wide profiles of epigenomic features and gene densities averaged over all TAD and metaTAD (10 – 40 Mb) boundaries (ribbons show 95% confidence intervals of the mean).

Next a comparison between metaTAD boundaries for metaTAD size (s) in the range $10 \text{ Mb} < s < 40 \text{ Mb}$ was performed. Our collaborators generated several ChIP-seq datasets, including for CTCF and three PolII variants, as well as expression data in the form of CAGE (Methods 2.7.2). We averaged these features over the set of all metaTAD and TAD boundaries and compared the average profiles of each (Fig. 55). These average profiles show heightened enrichment for PolII variants, CTCF and DNase, with non-overlapping 95% confidence intervals of the mean over the boundary bin. Increased enrichments of gene density and histone modification H3K27me3 are also suggestive of a heightened prevalence at metaTAD boundaries relative to TAD boundaries (Fig. 55). The observable co-incidence of metaTAD boundaries and lamina associated domains (LADs) is explored further in Section 5.4.2.

Increased enrichment at metaTAD boundaries relative to TAD boundaries lends evidence to the functional importance of metaTADs, and suggests boundaries become increasingly well-demarcated at higher levels of organisation. However, if this is a genuine biological phenomenon, we'd expect the trend not just to be observable in a comparison between two selected sets, but to increase monotonically as we ascended the metaTAD hierarchy from TADs to chromosomes.

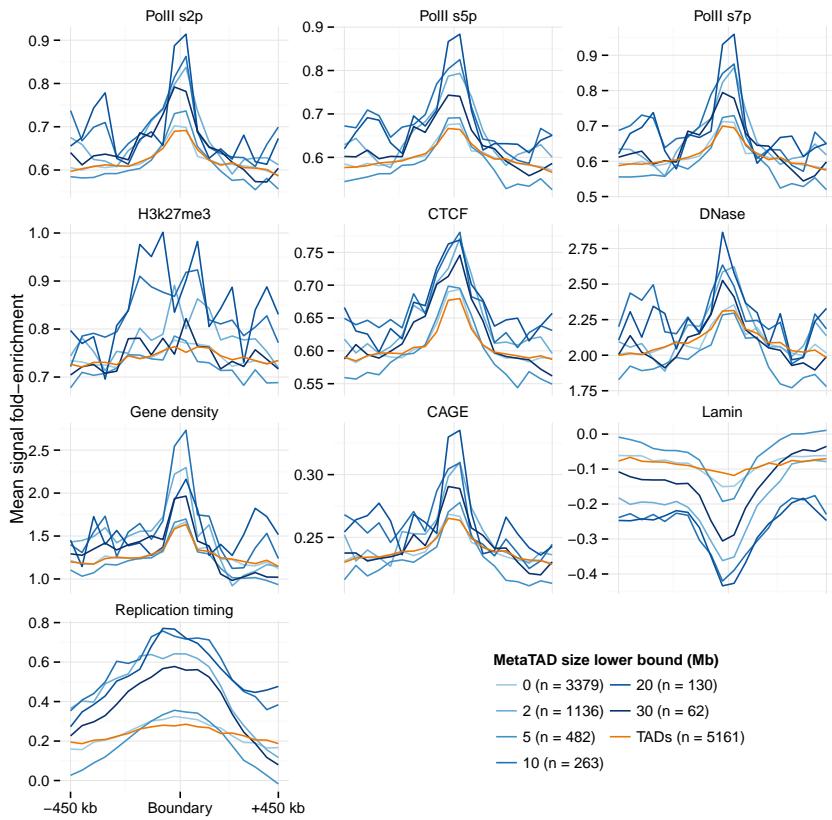


Figure 56: MetaTAD boundary enrichments and sample sizes with varying size selection. Boundary average-o-grams are shown for TAD and metaTAD boundaries with variable lower bound cut-offs. Sample sizes for each threshold are shown in the legend (*inset*).

To test this, we reran that above boundary analysis (Fig. 55) but at a range of metaTAD size cut-offs (Fig. 56). Generally we find increasing enrichments in metaTAD boundaries relative to TAD bounds through the range of lower bound cutoffs from 0 to 20 Mb, possibly with a slight decreased effect size at the highest cutoff of 30 Mb, where the sample size of boundaries decreases to just 62 (Fig. 56). This analysis strengthens the evidence for heightened functional enrichment of metaTAD boundaries (Figs. 55, 56) and suggests the metaTAD aggregation procedure is capturing boundaries of increasing strength, in terms of enrichment of boundary associated features (e.g. Fig. 44), through the metaTAD hierarchy.

5.4.2 Lamina associated domains

We report a coincidence of metaTAD boundaries and lamina associated domains (LADs), and at a greater level than that observed with smaller TADs (Fig. 55). This hints at an association between metaTADs and LADs which can be further investigated.

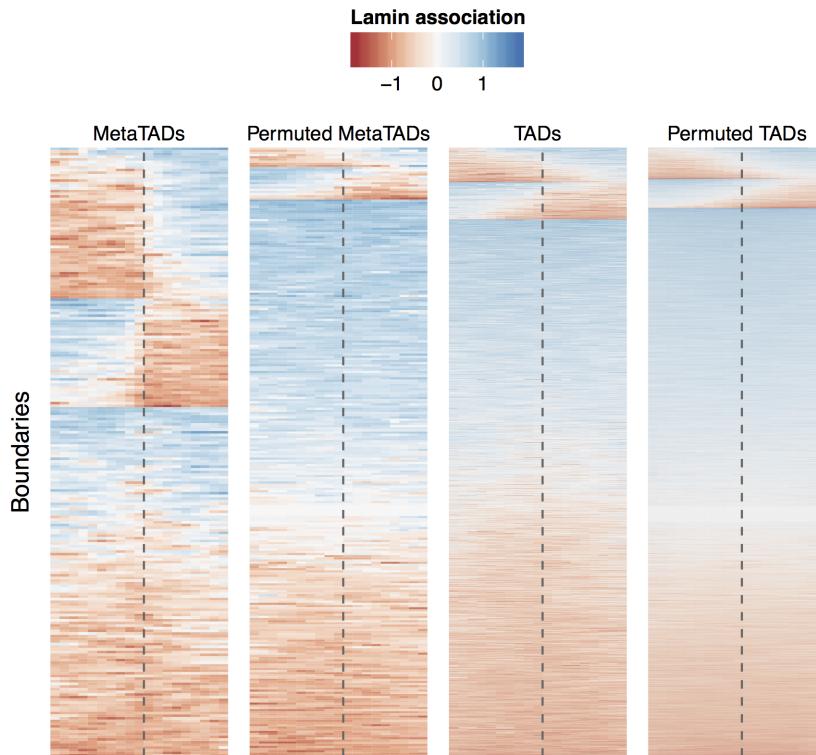


Figure 57: MetaTADs align with lamin associated domains. Heatmaps of LaminB1 association microarray probe intensity values over MetaTAD boundaries (from domains of size 10 – 40 Mb) and TAD boundaries, are displayed alongside examples of circularly-permuted boundaries. Profiles are shown ± 450 kb from each boundary.

High resolution LAD data in mouse embryonic stem cells were retrieved from Peric-Hupkes *et al.*^[130] in the form of continuous measures of lamin-B1 association produced by the DamID technique, known to reflect proximity to the nuclear lamin.^[200] This measure of lamina association was then processed in windows around each metaTAD and TAD boundary, and profiles were combined to form a heatmap (Fig. 57).

Boundaries were seriated in order to separate out those that coincide with a LAD boundary (Methods 2.7.3) and we found a large number of metaTAD boundaries (43%) in our 10–40 Mb subset appeared to correspond to LAD boundaries (Fig. 57). The same comparison using TAD boundaries found a coincidence of just 12%. However LADs are large domains and there were over 5,000 TADs called in this Hi-C data by our collaborators, thus in absolute numbers of boundaries this is still represents a large overlap.

To test the significance of these observations, we apply a permutation-based statistical test where our observed coincidences are compared with those produced by 1,000 circular (per-chromosome) permutations (Methods 2.7.3). We found that the metaTAD boundary coincidence is around 2.7-fold increase above null expectation (observed:

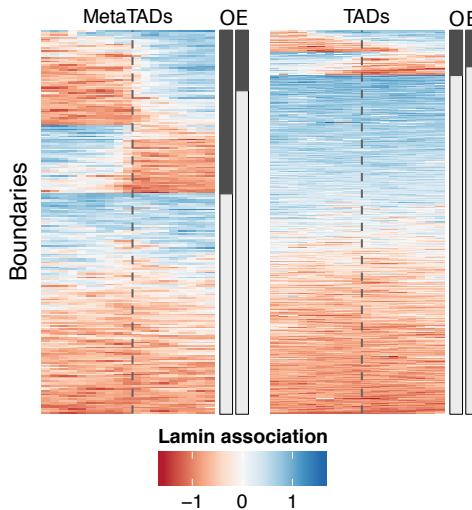


Figure 58: MetaTAD boundaries much LAD boundaries much more often than expected by chance. Heatmaps of lamina association over MetaTAD boundaries are shown as in Fig. 57. Sidebars labelled O and E reflect observed and expected proportions of metaTAD / LAD boundary overlaps.

42.6%; expected: 15.8%; empirical p -value: $p < 1 \times 10^{-4}$; Fig. 58). Meanwhile TAD boundaries were found to have a smaller, yet still significant, 1.2-fold increase in coincidence with LAD boundaries relative to a null model (observed: 11.8%; expected: 9.5%; empirical p -value: $p < 1 \times 10^{-4}$; Fig. 58).

As with other enrichments (Fig. 56), we went on to verify that this result was not specific to the choice of boundary size cutoff. Recall that as metaTADs are derived from TADs, selecting metaTADs within a size range is a trade-off between minimising overlap between TADs and metaTADs to enable more powerful comparison, while retaining a sufficiently large sample size of metaTAD boundaries (Section 5.4.1). In the case of LAD–metaTAD coincidence, we again find this result is insensitive to the selection of domain size cutoff, and indeed that there's evidence for an increasing proportion of co-occurrence as we ascend the metaTAD hierarchy (Fig. 59).

This result highlights again that metaTADs offer useful perspectives onto higher order genome organisation. In this case, it appears TADs will often neatly aggregate within LADs and together these constitute what we observe as a metaTAD.

5.4.3 Boundaries over a time series

For the first time, our collaborator's applied the Hi-C technique over a differentiation time course from mouse embryonic stem cells, to neural pre-cursors and finally fully-differentiated neuron cells. Successive expression measures were also taken alongside this Hi-C data in the form of CAGE data, produced by the FANTOM5 consortium.^[125]

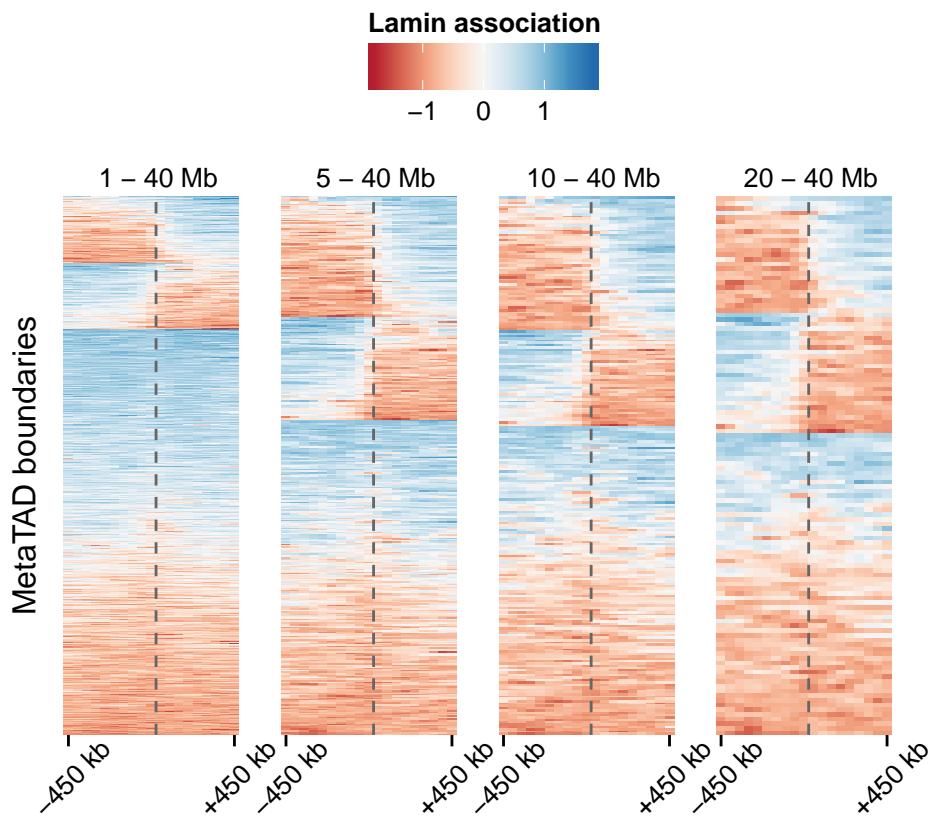


Figure 59: MetaTAD–LAD coincidence increases at higher levels of the metaTAD hierarchy. Heatmaps of lamina association over MetaTAD boundaries are shown as in Fig. 57. Panels show the size selection cutoffs for metaTAD domains considered in each case.

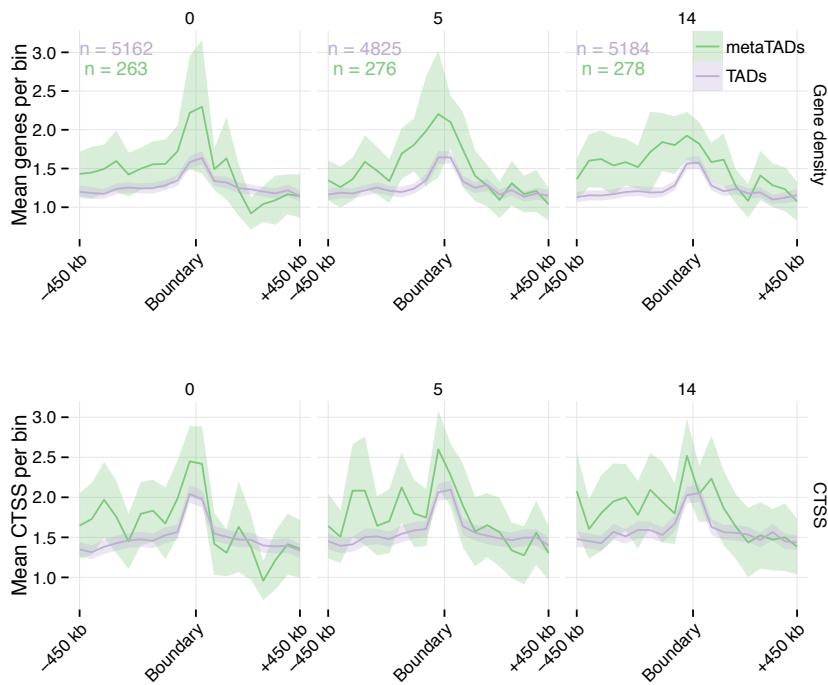


Figure 60: Observed enrichments persist over a time series. CAGE-defined active TSS (CTSS) were counted per 50 kb bin across each TAD and MetaTAD (10–40 Mb) boundary and averaged (ribbons show 95% confidence intervals of the mean). Gene densities refer to mean counts of annotated genes per bin, with an overlap of at least 250 bp.

Together these datasets offer a unique perspective onto how higher order genome organisation varies with expression during differentiation.

Collaborators explored changes in both the overall tree structure between timepoints, and aggregate expression changes between TADs and metaTADs at successive timepoints. They identified rewiring events in the metaTAD tree over the timecourse, and found corresponding changes in expression (*data not shown*). Given metaTAD structures appear to differ and matched CAGE data exists for each timepoint, it was of interest to test how observed boundary enrichments for gene expression (Figs. 55, 56) might vary over this timecourse.

We find actively-transcribed CAGE-defined TSS (CTSS) to be consistently enriched over the shifting boundaries through the differentiation timecourse (Fig. 60). We coupled this with a static measure of gene density in order to distinguish expression changes from genic overlap, however both series show similar patterns so it does not seem that boundary expression changes occur at a global scale over this timecourse. Peak heights over boundary bins suggest modestly stronger enrichments at metaTAD boundaries relative to TAD boundaries, as seen with other features (Fig. 55).

5.5 OTHER BOUNDARIES

5.5.1 Giemsa bands

A recent analysis of Hi-C datasets examined the hierarchy of nuclear compartment and TAD organisation in human HeLa cells across the cell cycle. They found that interphase and metaphase chromatin structure are highly distinct, such that the TADs and compartments observed here are effectively abolished in metaphase.^[62] This raises the question of how the structural organization seen in (and often shared between) interphase cells is inherited through the cell cycle.

Human Giemsa metaphase banding (G-band) pattern data have been integrated with the human genome assembly, and although such data are widely used, they are also necessarily of low resolution.^[131] These G-band patterns are constant over human cell types at metaphase, but all traces of interphase higher order structure were reported to be absent at metaphase.^[62] We would therefore expect no agreement between metaphase G-bands and the patterns of interphase TADs and A/B nuclear compartments defined here, over all three cell types.

We examined the genome wide similarity of all interphase domain structure boundaries to metaphase G-band boundaries, relative to an expected distribution derived by permutation (Methods 2.8). There is a significant, though modest, excess of compartment boundaries within close proximity of G-band boundaries, such that 13.90% of compartment boundaries are within 500 kb of a G-band boundary (expectation = 10.50%, K-S test: $D = 0.076$, $p < 3 \times 10^{-12}$). This is seen for compartment boundaries calculated for all three cell types independently (a full comparison for GM12878 is shown in Fig. 61).

The genome wide overlap of compartment A and B regions with particular G-band classes is nonrandom, and suggests much greater correspondence. Regions assigned to compartment A are significantly over-represented within lighter staining (especially G-negative) bands, while compartment B regions are over-represented in the most darkly staining (G-positive) bands (Fig. 62). Approximately 40% of the genome jointly occupies interphase compartment A as well as gneg/gpos25 metaphase G-bands, or occupies the interphase B compartment as well as gpos75/gpos100 at metaphase. Again, the same trends are seen significantly across all three cell types. This agreement is not unexpected given the broad differences in G-negative and G-positive bands, with contrasting gene density, GC content and replication timing^[131] that is strongly reminiscent of the contrasts between interphase A and B compartments,^[9] but to our knowledge has not been directly studied before. These data suggest that across the genome most fine structure, reflected in domain boundaries, is not well preserved between interphase and metaphase. However there is evidence for conservation of broader structural categories across a substantial fraction of the genome, which may

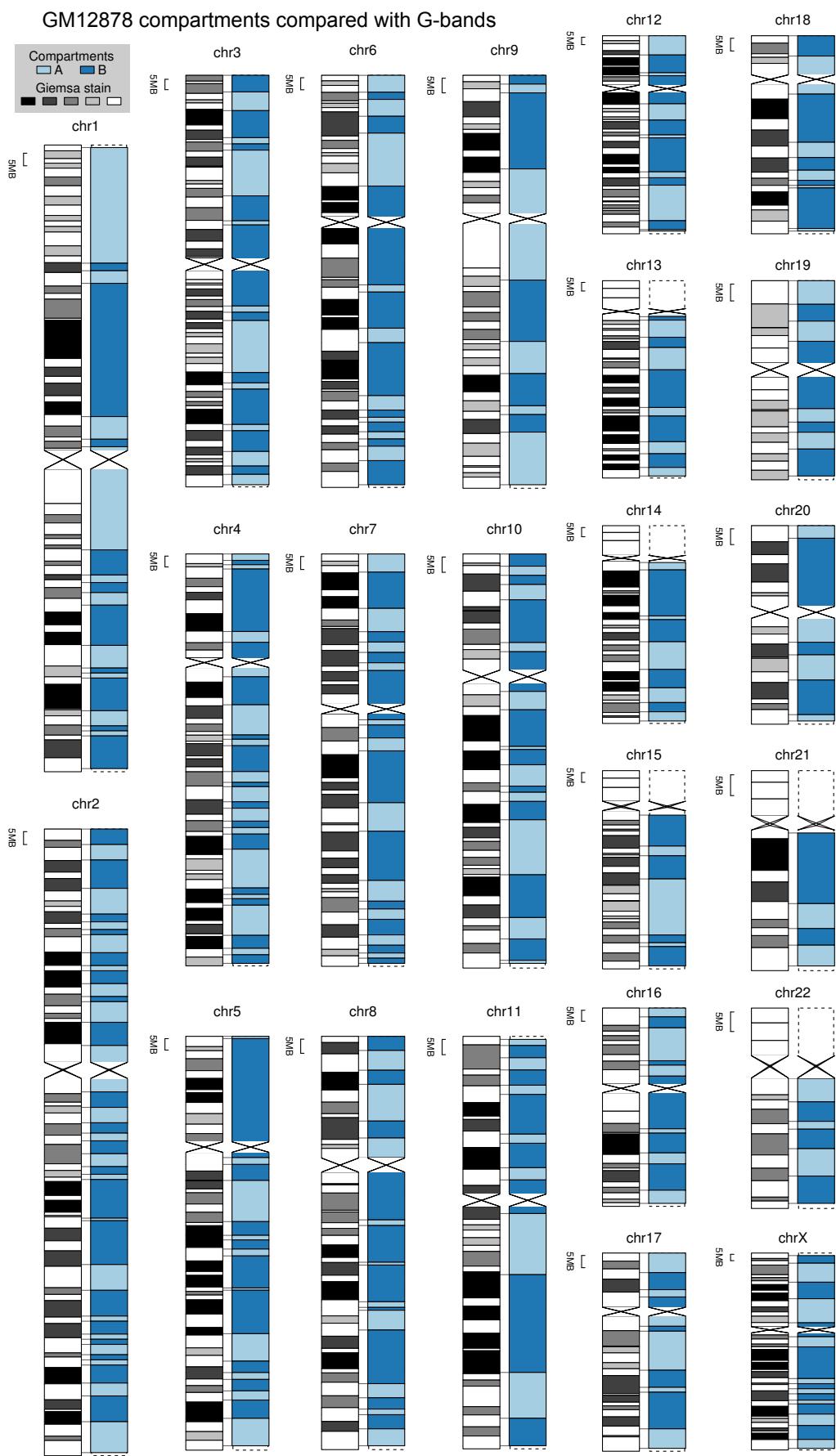


Figure 61: Genome-wide agreement between Giemsa bands and A/B compartments. G-bands, assayed at metaphase, often correspond with interphase A/B compartments across all chromosomes. Data for cell type GM12878 is shown.

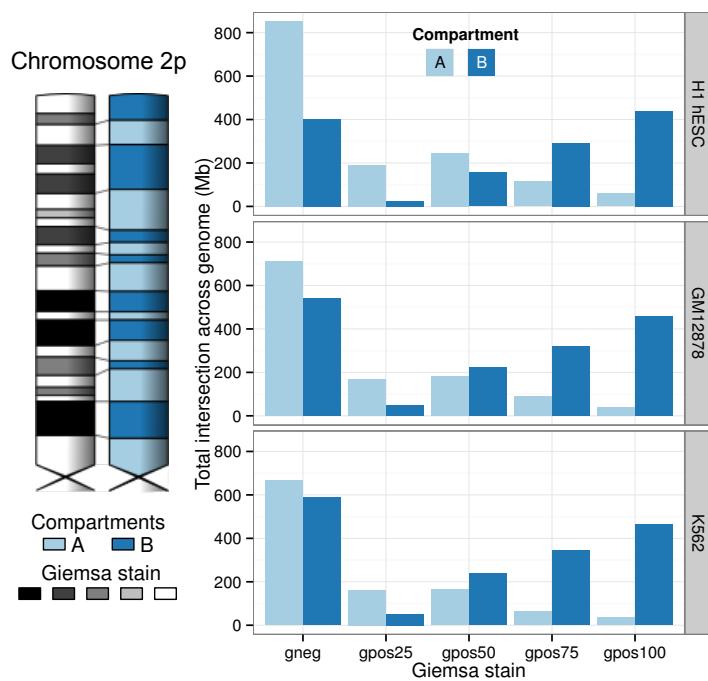


Figure 62: Giemsa-stain bands correspond to A/B compartments. The correspondence between G-bands and A/B compartments is broken down into the five levels of Giemsa stain. A compartments largely match *gneg* staining, while *gpos75* and *gpos100* are enriched in B compartments.

reflect broad similarities in the degree of compaction seen at many regions across the cell cycle.

6

LOCAL CHROMATIN CONFORMATION

6.1 INTRODUCTION

The Hi-C assay provides a genome-wide overview of chromatin conformation, however this broad scope imposes resolution limits inherent to an all-vs-all assay. For a closer look at chromatin conformation within a region of interest, alternative C-based assays such as 3C, 4C and 5C can be employed alongside classical microscopy techniques like FISH.

Here I discuss two collaborative projects involving the use of 4C and 5C data to "zoom in" on two well-studied regions related to limb development: the ZRS enhancer and HoxD gene cluster.

6.2 4C AT THE SHH LOCUS

Anterior-posterior patterning in the developing limb is regulated in mammals by *Sonic hedgehog* (SHH).^[202] Specifically, the SHH gene is expressed within a confined region named the "zone of polarising activity". Its expression within this region is known to be regulated by a well-studied enhancer, the "zone of polarising activity regulatory sequence" or ZRS.^[203] ZRS is located almost 1 Mb downstream of its target SHH promoter in humans, and is located in intronic regions of another gene, LMBR1 (Fig. 63).^[203,204] Single point mutations and short insertions within this enhancer have been linked to various limb deformities, including pre- and post-axial polydactyly.^[202,204,205] For example, a heritable point mutation in the ZRS enhancer is the cause of polydactyly in "Hemingway cats", a large group of domestic cats with extra toes that reside at the former home of Ernest Hemingway.^[205]

Collaborators have developed a model system which allows inducible SHH expression in a non-expressing 14fp cell line derived from the developing limb bud. Application of trichostatin A (TSA) then leads to detectable SHH expression, and increased levels of the histone activation mark H3K27ac at the ZRS (*unpublished data*). However, the question remains whether this TSA treatment is fundamentally altering local chromatin structure, that is, bringing together the ZRS enhancer with its target SHH promoter, or whether ZRS and SHH are in contact in both the active and non-expressing cell lines and SHH expression is blocked through other means. Analysis of the region through FISH implies similar levels of compaction in SHH expressing

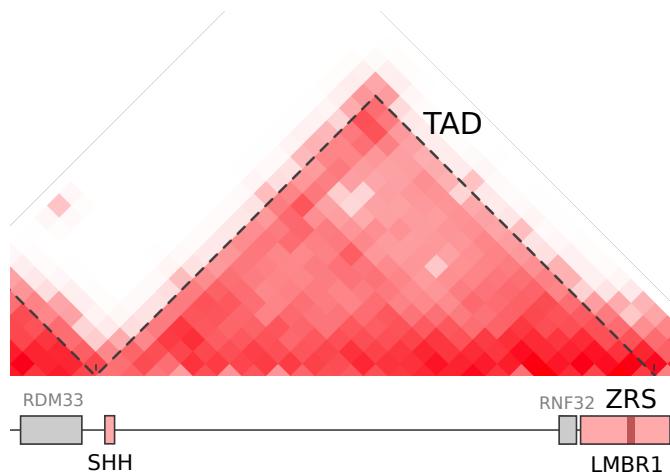


Figure 63: SHH–ZRS contacts occur within a stable TAD. An approximately 1 Mb region of the mouse genome is shown below a Hi-C contact map (derived from previously published data^[10]). A clear TAD can be identified spanning from SHH to ZRS, dashed lines show TAD boundaries called by Dixon *et al.*^[10]. This figure was generated for Anderson *et al.*^[201].

and non-expressing cells (*data not shown*), suggesting the latter explanation. Additionally, studies have previously reported the SHH–ZRS interaction is an example of a “pre-formed loop”, and as such is maintained regardless of transcriptional activity.^[206]

My part in this collaboration was to analyse 3C-seq (also known as 4C) data generated by our collaborators for the SHH–ZRS region in mouse. Additionally, the 4C procedure^[136] was adapted for specific in-house sequencing instruments (an Ion Torrent Ion Proton™ sequencer as opposed to Illumina™ technology) and as such required diagnostics to confirm the experimental data was accurate.

6.2.1 4C pipeline

The 4C analysis pipeline, starting from de-multiplexed fastq files as produced by our in-house sequencing facilities, can be summarised as:

1. Trim known bait sequence using cutadapt,^[207] select only those reads where known sequence was present
2. Map reads to reference genome mm9 using bowtie2^[95] with the very-sensitive flag
3. Filter alignments with a MAPQ score < 30 to select for high-confidence alignments using samtools^[151]
4. Normalise and analyse contacts using the r3cseq R package (Methods 2.11)

6.2.2 Analysis of ZRS interactions

4C experiments were performed by collaborators using the ZRS region as a bait sequence, or “viewpoint”, such that it contacts were measured with all other HindIII restriction fragments genome-wide. 4C was performed in both untreated and non-SHH expressing cells (*TSA-*) and in cells treated with TSA, thereby causing SHH expression (*TSA+*).

The first stage in analysing these contacts is to convert observed raw sequencing reads to normalised frequencies (Methods 2.11.1), these normalised values are then assigned significance scores in the form of *q*-values, with the aim of finding those significantly over-represented relative to expectation (Methods 2.11.2).

The results of a comparison between TSA treated and untreated samples is shown in Figure 64. In it we see a striking and highly significant ZRS–SHH contact in the treated sample (*q*-value $< 5 \times 10^{-10}$), with a weaker but still significant contact in the adjacent restriction fragment in the untreated sample (*q*-value $< 5 \times 10^{-5}$).

We also see more broadly a much higher total number of significant contacts in the untreated sample around the viewpoint (Fig. 65). In the treated samples, only a few contacts cross the stringent *q*-value threshold, with the SHH–ZRS contact among the most significant in terms of both *q*-value and supporting number of reads (indicated by the thickness of the arc, Figs. 64, 65).

Existing multi-probe FISH data produced by our collaborators shows approximately equal levels of compaction in this region in both TSA treated and untreated cells (*data not shown*). This information in combination with the 4C results reported here (Fig. 64) support a hypothesis that while both samples are held together in a TAD (Fig. 63) — unavoidably inducing many contacts — it is only in the treated sample where a highly-specific ZRS–SHH contact occurs and potentially is then bring about expression of the *SHH* gene.

6.2.3 Assay diagnostics

The 4C protocol used by our collaborators in this work was that of Stadhouders *et al.*^[136]. In it, the authors advise some statistical tests to ensure the quality of the experiment results. Among these were:^[136]

1. Sequencing reads should be found to have high duplication rates of 95% or greater.
2. 50% or more of all reads should map to the chromosome on which the bait region is located.

Sequence duplication levels were measured with FastQC^[208] and are shown in Table 6. We find slightly lower than expected levels of duplication, ranging from 62.8%

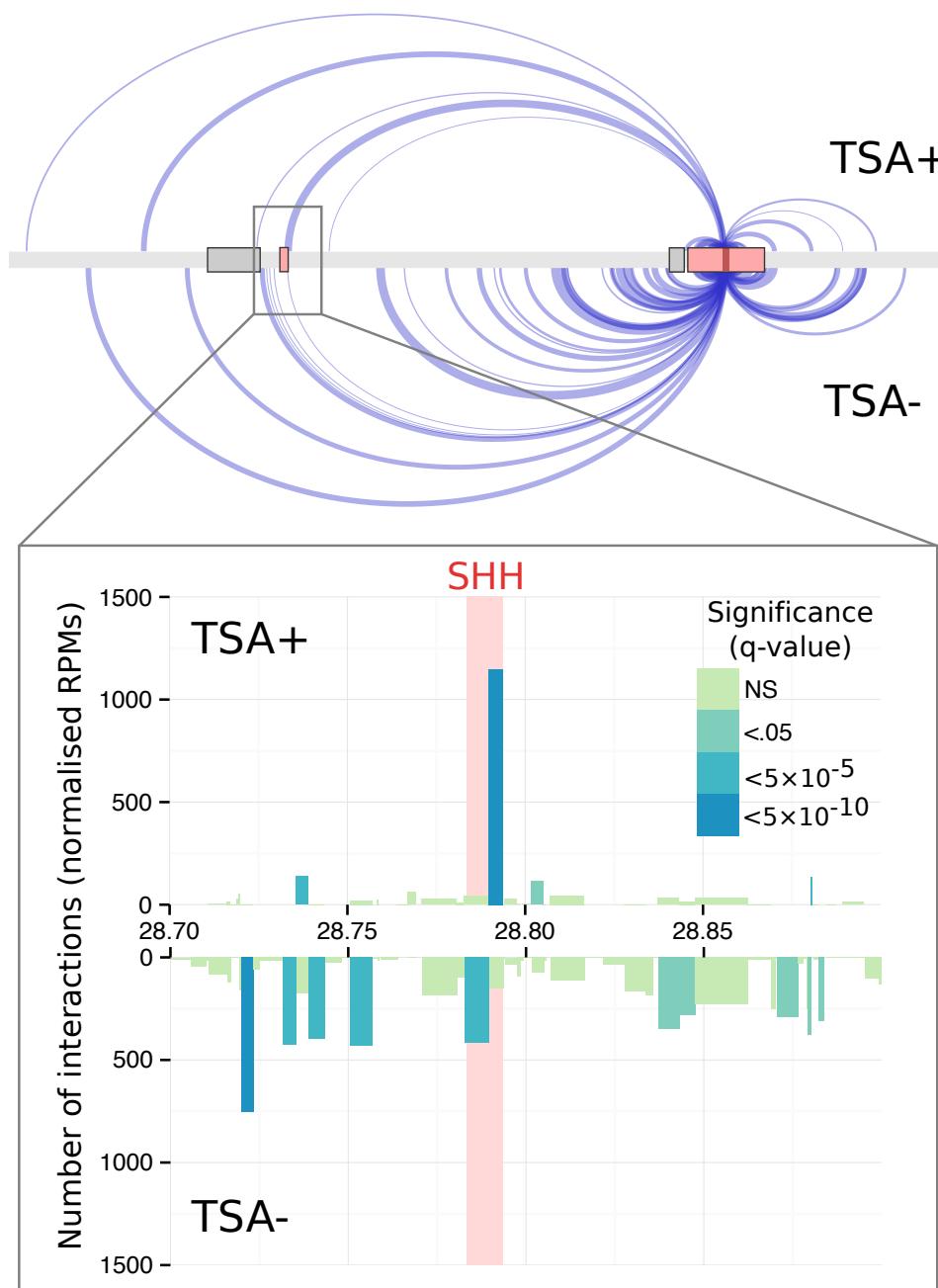


Figure 64: TSA treatment induces a strong ZRS–SHH interaction. 4C interactions are shown as edges from source node (ZRS enhancer bait fragment) to targets along an approximately 2 Mb region of chromosome 5. Edge width is proportional to the number of interactions, only highly significant interactions are shown (FDR q -value $< 5 \times 10^{-5}$). Zoomed region shows the number of interactions of the bait region with SHH in both untreated and TSA treated (after 18h) samples. Each rectangle is a restriction fragment, coloured by FDR q -value indicating the interaction above expected levels.

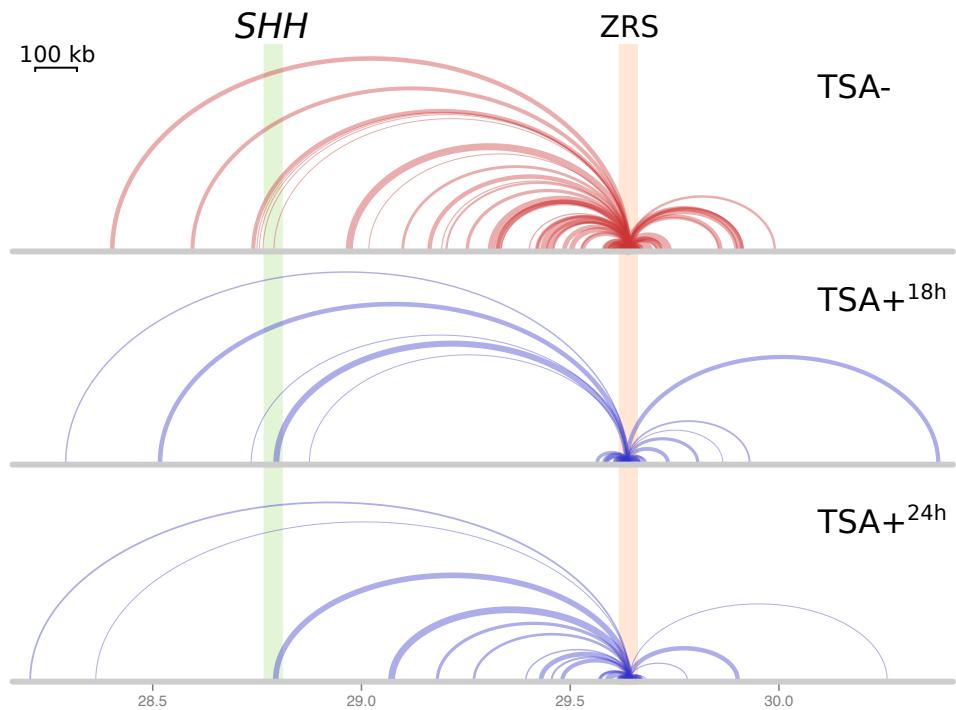


Figure 65: A stable ZRS-SHH interaction is coupled with reduced extraneous contacts. Arc plots are shown for an untreated, non-expressing 14fp cell population (*untreated*) and following TSA treatment after 18 and 24 hours. Arcs link highly significant interactions (q -value $< 5 \times 10^{-5}$) and arc widths are proportional to the normalised number of reads recorded for the interaction (Methods 2.11).

Table 6: 4C sequencing library statistics. 4C experiments are summarised as total number of reads in each experiment and the percentage of those reads labelled “duplicates”. Note in 4C these duplicates are not artifactual and instead result from large numbers of contacts nearby to the viewpoint.

	TSA-		TSA+	
	MluI	HaeIII	18h	24h
	Reads (Million)		10	10.4
Duplicated (%)		62.8	74.0	71.2 84.4

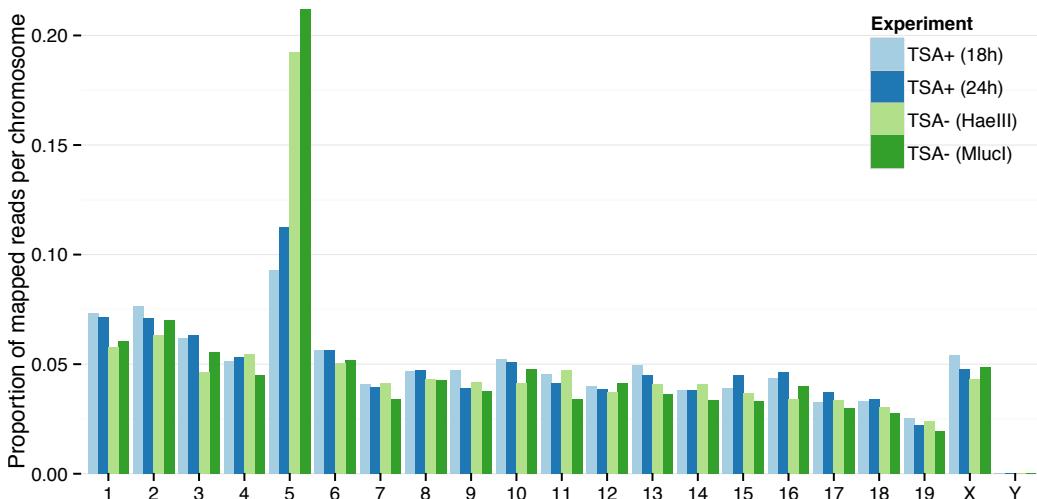


Figure 66: The bait chromosome is enriched for 4C sequencing reads. Chromosome 5 is visibly enriched for 4C reads as it contains the ZRS bait region (or viewpoint). Untreated control samples (TSA-) were assayed with two different secondary restriction enzymes (4-cutters HaeIII and MluI).

to 84.4%. This suggests that while the assay does appear to be working, there may be extraneous noise and non-bait interactions in the sequencing library.

We found the proportion of reads mapped to the fair region chromosome, chromosome 5 in this case, fell below the prescribed level of 50%. Looking at three experiments (two from the untreated control), we find instead that between approximately 10–20% of all reads mapped to the bait chromosome (Fig. 66). While this is still a clear enrichment over non-bait chromosomes, it suggests the assay results suffer from either increased *trans*-contact noise or decreased *cis*-contact enrichment around the bait region.

Lower than expected levels of both sequence duplication and bait chromosome enrichment suggest loss of signal around the bait region itself. This is the area where we’d expect both very high levels of duplication (identical restriction fragment pairings between nearby genomic locations) and a majority of all sequencing reads, driving the overall chromosome enrichment. The precise reason for the discrepancy is unclear but suggests the results may have a lower signal-to-noise ratio than has previously been achievable in 4C experiments.^[136] Potentially the signal-to-noise ratio could

be improved by utilising a double cross-linking procedure such as that used in Lin *et al.*^[209]

6.3 3D MODELLING OF CHROMATIN FIBRE

Chromosome conformation capture allow investigation of genome organisation, but such data are commonly analysed using one or two-dimensional representations. A growing set of algorithms looks instead to rebuild the three-dimensional polymer trajectory of a chromatin fibre, using Hi-C or 5C data as input (e.g. 210–217). Intuitively, in each method the interaction frequency between two regions is idealised as inversely proportional to their physical distance (where possible and according to various other constraints). Where these methods differ is in their approaches to solving this optimisation problem. We chose the AutoChrom3D method^[215] for use in this work (described in Section 6.3.1) as the algorithm can accept 5C input and model polymers at high resolution of 8 kb or greater.

6.3.1 AutoChrom3D method

The procedure implemented in AutoChrom3D can be summarised as:^[215]

1. The chromatin fibre is represented as beads-on-a-string, with $N_{beads} = \lceil \frac{L}{R} \rceil$ (where L is the length of the region and R the resolution)
2. A local compaction parameter is calculated using a sliding window of each 50 adjacent beads (intra-window contacts are averaged and compared to those over the whole region under study)
3. Interaction frequency between beads of a given genomic distance is modelled as a Poisson-distributed random variable and noisy or unstable contacts, considered in the context of neighbouring beads, are filtered
4. This filtered set of interaction frequencies are then normalised using the previously-calculated compaction parameter to give an $N_{beads} \times N_{beads}$ matrix of interaction strengths
5. Interaction strength is converted to spatial distance through two linear transformations based on experimental observations of nuclear occupancy and regional flexibility^[20]
6. Cartesian co-ordinates are then calculated via non-linear constrained optimisation of pairwise spatial distances using LINGO^[218]

Table 7: Measurement distances between ZRS and SHH in each inferred 3D structure. Distances are given in arbitrary units. *Shh* spans two beads of the polymer model, hence two distances are calculated in each case (d_1 , d_2). RMSD is the minimised root mean squared deviation between the two structures and is given as a relative unitless quantity. The radius of gyration (gyradius) is also shown.

		Distance		RMSD	Gyradius (μm)	
		TSA-	TSA+		TSA-	TSA+
88fp	d_1	5.4	5.1	1.701	0.244	0.244
	d_2	4.1	3.9			
MD	d_1	6.2	3.3	2.377	0.217	0.205
	d_2	4.8	2.0			

6.3.2 Modelling the *Shh* region with 5C

5C data was generated by our collaborators over the same *Shh*-ZRS region as was assayed with 4C (Fig. 63; Section 6.2) with the aim of developing a multi-point perspective on local chromatin conformation beyond that available from 4C data.

We used this 5C experimental data in combination with a particular three-dimensional inference program (AutoChrom3D^[215]) in an attempt to compare polymer trajectories in TSA treated and untreated 88fp mouse cells, a similar and complimentary cell line to that used in earlier 4C experiments (14fp). As a control, 5C was also performed on embryonic MD cells, with and without TSA treatment, which do not express *Shh*. Prior to structural modelling, the my5C program was used to generate normalised 5C interaction frequencies.^[219]

We find that TSA treatment of 88fp cells does appear to slightly reduce the distance between *Shh* and ZRS in inferred 3D structures (Fig. 67), however this difference is overshadowed—to our surprise—by that observed in the non-expressing MD cell line. This latter embryonic cell line undergoes a large structural transition which brings together the *Shh* gene and the ZRS enhancer. Measurements between these elements for each structure are shown in Table 7.

We also report a greater overall structural shift following TSA treatment in the MD cell line, with an RMSD between the two structures of 2.377 arbitrary units, relative to 1.701 between TSA+ and TSA- 88fp cells. The radius of gyration, unchanged in 88fp, is also decreased in the MD cell line following TSA treatment, indicating the region becomes more compact following TSA treatment (Table 7).

6.3.3 Repeat simulations

We have shown what appears to be a structural shift in the *Shh*-ZRS locus per 3D modelling predictions (Section 6.3.2). It is of interest to assess the stability and reproducibility of these results through repeat simulations of the polymer trajectory. At this point it is unclear whether the *Shh*-ZRS bound state represents a firm consensus

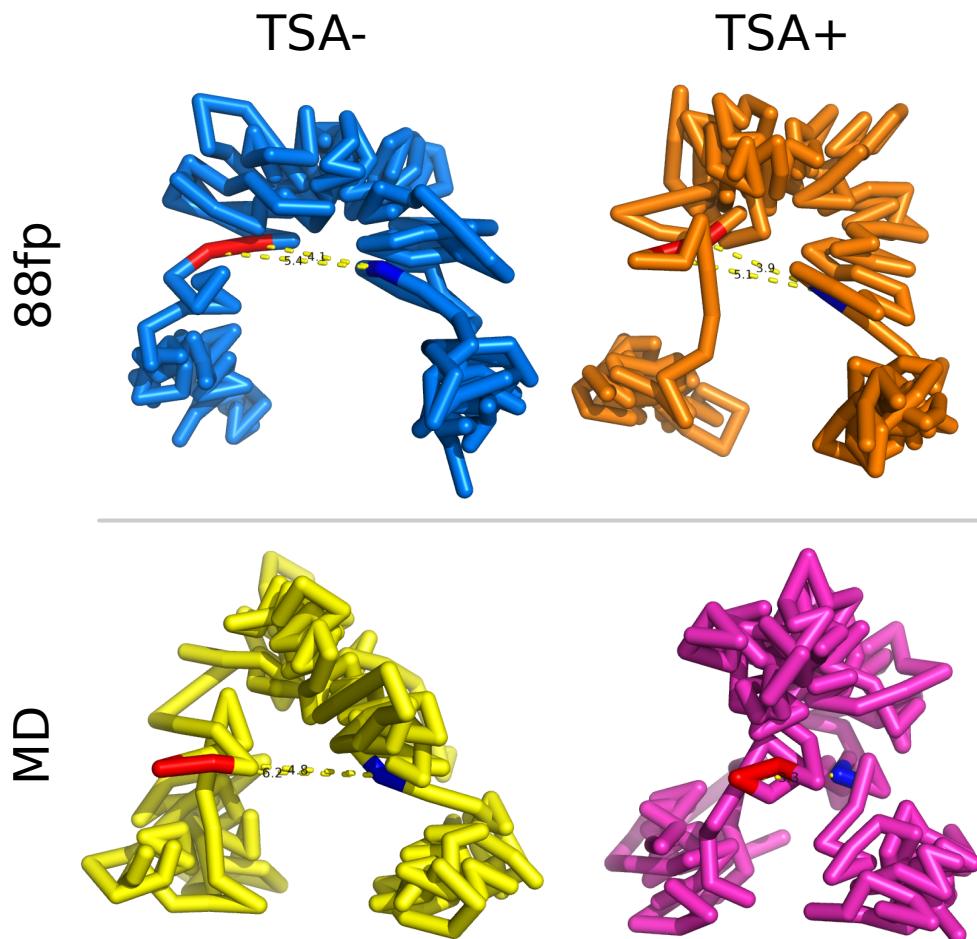


Figure 67: Inferred polymer trajectories of the ZRS-SHH region following TSA treatment in two cell lines. 3D structures are shown for 5C experiments assaying the region around *Shh* (red) and ZRS (blue) in an *Shh*-expressing limb bud cell line (88fp) and a non-expressing embryonic cell line (MD). Labelled measurements are given in Table 7. Structures were predicted by AutoChrom3D^[215] using 210 × 8 kb beads per polymer.

over the cell population, or an alternative structure with similar optimisation energy to that of the more non-bound state.

We re-ran simulations of the 3D chromatin fibre in the *Shh*-ZRS region a total of five times (Fig. 68). In every case, the algorithm generates the known *Shh*-ZRS TAD as a compacted domain bookended by the two loci under study. This sanity check ensures the results are broadly compatible with our *a prior* expectation of the region's structure given the 2D heatmap representation of 5C data (Fig. 63).

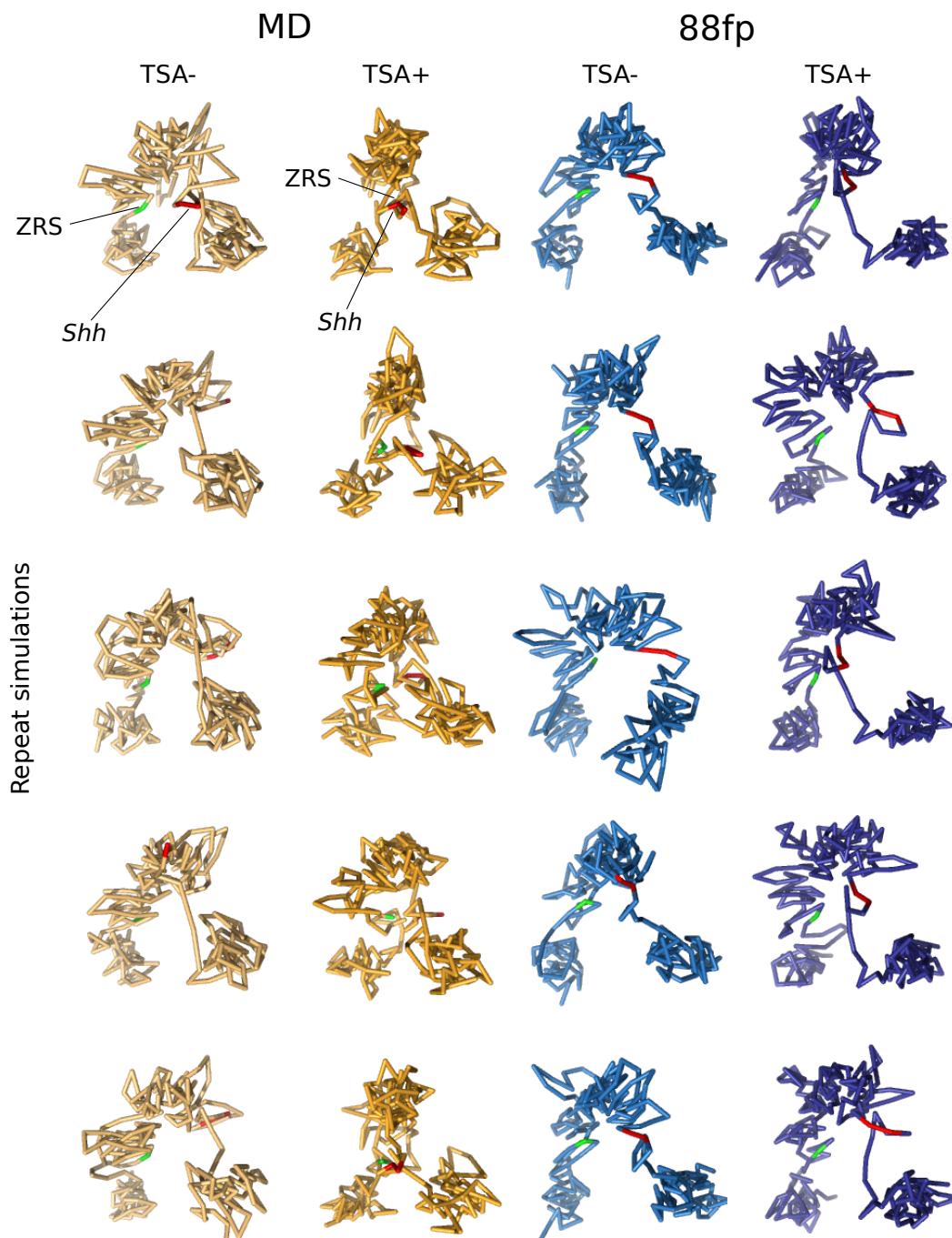


Figure 68: Repeat simulations of 3D polymer trajectories in the *Shh*-ZRS region. 3D structures are shown for 5C experiments assaying the region around *Shh* (red) and ZRS (blue) in an *Shh*-expressing limb bud cell line (88fp) and a non-expressing embryonic cell line (MD). Structures were aligned as whole molecules with the uppermost replicate in each column.

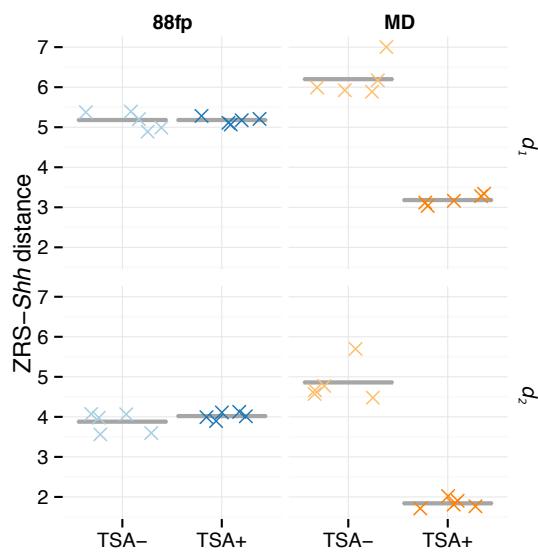


Figure 69: *Shh*-ZRS distance measurements from repeated 3D polymer simulations. Measurements were taken from 5 replicate 3D simulations (shown in Fig. 68). Distances are given in arbitrary units. *Shh* spans two beads of the polymer model, hence two distances are calculated in each case (d_1, d_2).

7

DISCUSSION

7.1 MODELLING HIGHER ORDER CHROMATIN ORGANISATION

Integrative analyses of locus level chromatin data have allowed the prediction of functional chromatin states^[74,84,86,220] but these states typically encompass small regions, on the order of hundreds of basepairs, rather than the larger-scale structures we are concerned with in this work.

Our data show that accurate predictions of Hi-C derived eigenvector values, and therefore chromosome compartments, are entirely achievable. Generalisation across cell types further suggests that chromosome compartments could be inferred for those cell types without any available Hi-C data but with available ChIP-seq for a handful of chromatin features. For example, the NIH Roadmap Epigenomics project has generated histone modification data in hundreds of cell lines, tissues and developmental stages.^[161,221] If models in this work were adapted to use matched inputs, this would allow comprehensive comparisons of inferred chromosome compartments across a diverse range of conditions and cell types. In the same vein, chromosome compartments are known to be related to and recapitulate other aspects of higher order chromatin organisation, including replication timing domains, Lamina associated domains and nucleolus association domains. We therefore suggest a similar modelling approach could prove successful for each of these domains of interest. An exciting idea is that an integrative model capable of identifying these LADs and NADs could forward this information to a subsequent three-dimensional reconstruction algorithm, giving a truly *in situ* perspective onto nuclear architecture.

We had less success with the prediction of TAD boundaries (Section 5.3.1). One reason for this is that the TAD calling algorithm used in this work^[10] (Methods ??), though a published and well-used method, produces observably-flawed domain calls in some contexts. In addition the sensitivity of this method is proportional to the sample sequencing depth, which varied across our three human Hi-C datasets. We resolved TAD domains to 40 kb bins, far below the resolution of individual CTCF motifs which can generate physical domains. Indeed, given the newly-available very highly-sequenced Hi-C datasets,^[13] an improved method of predicting domains might start from individual ChIP-seq peaks and consider pairs of correctly-orientated CTCF motifs. In addition, any predictive model of such domains would do well to consider the hierarchical nature of chromatin organisation (exemplified by metaTADs, Section 5.4) rather than seeking simple linear discretisation of chromatin fibre into adjacent domains. Finally, we note that an accurate predictive model of lower-levels of domain

organisation, be they TADs or smaller physical domains, could likely recapitulate, on aggregate, broader domains such as compartments and metaTADs, culminating in a multi-scale model of nuclear architecture from the levels of kilobases up to entire chromosomes.

7.2 DOMAIN BOUNDARIES

Chromatin domains have been described at multiple scales, from 5 Mb chromosome compartments^[9] down to 185 kb contact domains^[13] in human cells. Across all domains, questions remain about how they are constructed and maintained. Two competing ideas are that boundary elements, akin to the classic chromatin insulators, block intra-domain contacts and the spread of heterochromatin and hence create chromatin domains; however, another suggestion is that boundary regions are rather less important and in fact the unavoidable consequence of adjacent self-interacting domains, which are perhaps instead held together through internal enhancer–promoter interactions and other contacts. The importance of boundary elements has implications for the re-establishment process of domains during the cell cycle, where it has been shown that domains are entirely absent during mitosis and re-established in early G1 phase.^[62]

In favour of functional boundary elements, both knockdown of CTCF^[38] and deletion of a specific boundary element^[29] have been shown to increase inter-TAD contacts, suggesting boundaries indeed contribute to domain delineation. In this thesis we report an array of boundary enrichments and depletions (Section 5.2), which at minimum suggests some biological process is in effect. Conversely not all observed enrichments and depletions are expected to have a function; it has been shown for example that removal of the H3K27me3 mark had no effect on domain boundaries.^[29] One suggestion is that, due to boundary enrichments for gene promoters,^[10] genes positioned adjacent or over a domain boundary might be most amenable to dynamic regulation, for example by associating or disassociating from the nuclear lamina. Alternatively, this boundary enrichment could be due to promoter–promoter looping inducing domain boundaries.^[40,53,222]

The incidental boundary hypothesis is supported by data showing that deletion of specific boundary elements is insufficient to cause adjacent domains to completely merge.^[29] In addition, the majority of CTCF sites fall within TADs rather than at their boundaries (approximately 85% of human CTCF sites are non-boundary^[10]). Further it has been shown that the majority of enhancer–promoter contacts are tissue invariant,^[206] hence these constitutive contacts could account for the high levels of domain conservation reported previously^[9,10,13,133] and in this work (Chapter 3).

As is the case with many biological phenomena, the question of whether boundary regions or internal contacts are responsible for chromatin domains is reductive, and it

seems likely that both boundary insulation and intra-TAD contacts work together to maintain chromatin domains.

7.3 DOMAIN EVOLUTION

In this work we find an array of chromatin features that, on average, are statistically associated or excluded from TAD or compartment boundaries (Section 5.2). Among these are features with a long history of implications in chromatin organisation, including CTCF and cohesin subunit RAD21. We also report enrichments for Alu repeat elements (Section 5.2.2) but no other repeat classes. Alu repeats and CTCF are linked by evidence that CTCF binding sites have in the past been dispersed through waves of retroposon expansion.^[196,223] Thus this suggests a model for the evolution of topological domains, whereby purifying selection removes those inserted CTCF sites which disrupt desirable regulatory environments, while those which bring-about efficient "regulon" structures are favoured. Newly-released comparative Hi-C and CTCF datasets^[30] provide an opportunity to investigate this proposed evolutionary model.

7.4 A NOTE ON CAUSALITY

Throughout this thesis we have probed correlative relationships: those between chromatin features and expression, or higher order chromatin structure, or domain boundaries. However even the most predictive correlations make no comment on the underlying chain of causality. Whether genome organisation is a cause of consequence of the functions of underlying genetic elements remains an open question.^[40]

Two different approaches could be used to address the causality question. A standard rejoinder is to design wet-lab experiments, for example extending Hi-C studies to perturbation or differentiation time courses, such as that performed by collaborators in Chapter 5. However, another approach is first develop theoretical models which, under simulation, recapitulate observed data, and then to use these models to generate falsifiable hypotheses about the effects of specific perturbations. This latter approach is exemplified in a study by Giorgetti *et al.*^[224] where the authors applied physical polymer modelling to deconvolute population-level 5C data into single-cell conformations. The model suggests that population-level averages are explained by transient contacts in each cell, rather than persistent loops. Furthermore, these models were able to predict the effects of a genetic deletion of a CTCF site and found that contacts within a TAD contribute to maintenance of the domain, dispelling

an insulation-only explanation.^[224] This is also in agreement with experimental results showing that TADs can remain intact with the depletion of CTCF over a timecourse.^[38]

The models built in this thesis could also be applied to predicting the effects of experimental perturbations. For example, an experiment decreasing the tri-methylation of H₃K9, through down-regulation of SETDB1 or SV39H1 for example, might be expected to lead to heterochromatic regions to become more permissive or allow the transcription of marked tandem repeat sequences.^[225] Our models further suggest the effect would be most pronounced in K562 cells (Section 4.4.4). A previous experiment analysed the effects of losing H₃K9me3 in SETDB1 knockout mice and found increased expression of a number of endogenous retroviruses,^[226] but whether these expression changes were also coupled with alterations in chromosome compartment was not tested. Performing such an experiment over a number of timepoints could help to establish whether expression drives genomic regions to an active compartment or *vice versa*.

7.5 INSIGHTS INTO GENOME ORGANISATION

Overall our results agree with a functional model of genome architecture whereby a majority of the genome is arranged into large static compartments (Section 3.3), be they Lamina associated, nucleolus associated or central and accessible chromatin. Indeed, it seems plausible that such large, constitutive anchor points may be enough to generate a significant amount of concordance in nuclear architecture between cell types.^[206] These broad similarities are coupled with local structural changes in different cell lines (Section 3.6), allowing cell type specific regulation of gene environments through "looping out", detachment from the nuclear lamina and other conceivable mechanisms of structural variation. Whether these local changes are driven by DNA-binding proteins and chromatin remodelers or functional contacts such as enhancer–promoter interactions remains unclear.

7.6 CONCLUSION

It has become commonplace to discuss the multi-layered, hierarchical organization of interphase chromosomes across strata ranging from nuclear compartments, down to the spectra of histone modifications and bound proteins at individual sub-genic regions. However we lack a detailed understanding of how these strata interact. We have shown that our perspectives of features occurring at different strata can be bridged by modelling approaches, and the models produced can be used to explore the interrelationships between these different features quantitatively.

We constructed cell type specific models of nuclear organization, as reflected in Hi-C derived eigenvector profiles, to discover the most influential features underlying higher order structures. We found open and closed compartments to be well-correlated with combinatorial patterns of histone modifications and DNA binding proteins, enabling accurate predictive models. These models could be cross-applied successfully between cell types highlighting constellations of common structural features associated with different nuclear compartments as expected. Dissection of the most influential variables also revealed important differences between models, consistent with the known biological contrasts among these cell types, such as the prominence of EGR1 in embryonic stem cells and H₃K9me3 in the leukaemia cell line. Investigation of regions showing variable nuclear organization across the three cell types under study, revealed enrichments for cell type specific enhancer activity, often nucleated at genes with known roles in cell type specific functions. Finally we used model predictions to examine boundary composition between higher order domains across cell types. Among enrichments of a large number of factors observed at different boundaries in different cell types, CTCF and YY1 were found consistently and may cooperate to establish domain boundaries. In summary, we show that integrative modelling of large chromatin dataset collections using random forests can generate useful insights into chromosome structure and seed testable hypotheses for further experimental studies.

APPENDICES

Table A1: Gm12878 functional enrichments in regions of variable structure. FE: fold enrichment; FDR: false discovery rate.

Category	Term	Count	%	FE	p-value	FDR
GOTERM.CC.FAT	GO:0005882 intermediate filament	36	4.20	4.90	6.42E-15	8.95E-12
GOTERM.CC.FAT	GO:0045111 intermediate filament cytoskeleton	36	4.20	4.79	1.35E-14	1.87E-11
SP_PIR_KEYWORDS	keratin	31	3.62	5.64	1.72E-14	2.47E-11
INTERPRO	IPR007951:PMG	11	1.28	25.11	9.80E-14	1.56E-10

Table A2: H1 hESC functional enrichments in regions of variable structure. FE: fold enrichment; FDR: false discovery rate.

Category	Term	Count	%	FE	p-value	FDR
PIR_SUPERFAMILY	PIRSF003152:G protein-coupled olfactory receptor, class II	116	10.55	6.64	3.25E-68	4.41E-65
INTERPRO	IPR000725:Olfactory receptor	116	10.55	6.53	7.58E-63	1.21E-59
SP_PIR_KEYWORDS	olfaction	116	10.55	6.40	2.07E-61	2.97E-58
GOTERM_MF_FAT	GO:0004984 olfactory receptor activity	116	10.55	6.13	1.30E-60	1.97E-57
GOTERM_BP_FAT	GO:0007608 sensory perception of smell	117	10.64	5.96	1.91E-59	3.35E-56
GOTERM_BP_FAT	GO:0007606 sensory perception of chemical stimulus	118	10.73	5.37	1.71E-54	3.01E-51
KEGG_PATHWAY	hsa04740:Olfactory transduction	108	9.82	4.94	8.72E-51	1.03E-47
SP_PIR_KEYWORDS	sensory transduction	125	11.36	4.58	2.61E-48	3.74E-45
INTERPRO	IPR017452:GPCR, rhodopsin-like superfamily	131	11.91	4.03	1.40E-44	2.24E-41
INTERPRO	IPR000276:7TM GPCR, rhodopsin-like	131	11.91	4.02	1.68E-44	2.68E-41
PIR_SUPERFAMILY	PIRSF00006:rhodopsin-like G protein-coupled receptors	131	11.91	3.63	5.04E-43	6.85E-40
GOTERM_BP_FAT	GO:0007600 sensory perception	138	12.55	3.54	4.78E-41	8.40E-38
SP_PIR_KEYWORDS	g-protein coupled receptor	136	12.36	3.62	1.69E-40	2.42E-37
GOTERM_BP_FAT	GO:0050890 cognition	143	13.00	3.23	5.34E-38	9.38E-35
SP_PIR_KEYWORDS	transducer	137	12.45	3.39	1.48E-37	2.12E-34
GOTERM_BP_FAT	GO:0050877 neurological system process	163	14.82	2.72	3.85E-34	6.76E-31
GOTERM_BP_FAT	GO:0007186 G-protein coupled receptor protein signaling pathway	148	13.45	2.77	1.36E-31	2.40E-28
SP_PIR_KEYWORDS	receptor	172	15.64	2.31	3.72E-26	5.33E-23
GOTERM_BP_FAT	GO:0007166 cell surface receptor linked signal transduction	188	17.09	2.06	8.02E-24	1.41E-20
SP_PIR_KEYWORDS	cell membrane	198	18.00	1.86	5.96E-19	8.52E-16
UP_SEQ_FEATURE	topological domain:Extracellular	227	20.64	1.72	1.26E-17	2.20E-14
UP_SEQ_FEATURE	topological domain:Cytoplasmic	250	22.73	1.52	1.13E-12	1.98E-09
UP_SEQ_FEATURE	disulfide bond	211	19.18	1.56	9.11E-12	1.60E-08
SP_PIR_KEYWORDS	disulfide bond	214	19.45	1.52	6.20E-11	8.88E-08
UP_SEQ_FEATURE	glycosylation site:N-linked (GlcNAc...)	285	25.91	1.41	7.31E-11	1.28E-07
GOTERM_CC_FAT	GO:0005886 plasma membrane	255	23.18	1.37	1.26E-09	1.77E-06
SP_PIR_KEYWORDS	glycoprotein	289	26.27	1.37	1.83E-09	2.61E-06
GOTERM_CC_FAT	GO:0016021 integral to membrane	328	29.82	1.27	9.34E-09	1.31E-05
SP_PIR_KEYWORDS	transmembrane	317	28.82	1.31	1.37E-08	1.96E-05
UP_SEQ_FEATURE	transmembrane region	314	28.55	1.31	2.03E-08	3.56E-05
GOTERM_CC_FAT	GO:0031224 intrinsic to membrane	333	30.27	1.24	7.49E-08	1.05E-04
SMART	SM00355:ZnF_C2H2	69	6.27	1.86	4.23E-07	5.43E-04
UP_SEQ_FEATURE	zinc finger region:C2H2-type 5	55	5.00	2.08	5.12E-07	8.99E-04
UP_SEQ_FEATURE	zinc finger region:C2H2-type 4	57	5.18	2.01	8.49E-07	0.0015
INTERPRO	IPR013087:Zinc finger, C2H2-type/integrase, DNA-binding	59	5.36	1.94	1.73E-06	0.0028
UP_SEQ_FEATURE	zinc finger region:C2H2-type 2	58	5.27	1.95	1.73E-06	0.0030
SP_PIR_KEYWORDS	membrane	372	33.82	1.21	2.69E-06	0.0038
INTERPRO	IPR015880:Zinc finger, C2H2-like	69	6.27	1.78	4.09E-06	0.0065
UP_SEQ_FEATURE	zinc finger region:C2H2-type 8	44	4.00	2.14	4.13E-06	0.0073
UP_SEQ_FEATURE	zinc finger region:C2H2-type 3	58	5.27	1.90	4.43E-06	0.0078
UP_SEQ_FEATURE	zinc finger region:C2H2-type 7	46	4.18	2.06	5.87E-06	0.0103
INTERPRO	IPR007087:Zinc finger, C2H2-type	67	6.09	1.75	9.19E-06	0.0147
UP_SEQ_FEATURE	zinc finger region:C2H2-type 6	48	4.36	1.99	9.83E-06	0.0173

Table A3: K562 functional enrichments in regions of variable structure. FE: fold enrichment; FDR: false discovery rate.

Category	Term	Count	%	FE	p-value	FDR
PIR_SUPERFAMILY	PIRSF038651:G protein-coupled olfactory receptor, class I	26	7.08	24.94	7.86E-30	8.99E-27
GOTERM_MF_FAT	GO:0004984 olfactory receptor activity	40	10.90	6.12	7.39E-20	1.01E-16
INTERPRO	IPR000725:Olfactory receptor	39	10.63	6.18	3.00E-19	4.29E-16
SP_PIR_KEYWORDS	olfaction	39	10.63	6.15	4.55E-19	6.09E-16
GOTERM_BP_FAT	GO:0007608 sensory perception of smell	39	10.63	5.48	1.19E-17	1.94E-14
SP_PIR_KEYWORDS	sensory transduction	44	11.99	4.60	8.72E-17	1.44E-13
GOTERM_BP_FAT	GO:0007606 sensory perception of chemical stimulus	39	10.63	4.89	6.32E-16	1.09E-12
KEGG_PATHWAY	hsa04740:Olfactory transduction	38	10.35	4.58	6.87E-16	7.22E-13
INTERPRO	IPR017452:GPCR, rhodopsin-like superfamily	43	11.72	3.72	2.96E-13	4.23E-10
INTERPRO	IPR000276:7TM GPCR, rhodopsin-like	43	11.72	3.72	3.10E-13	4.43E-10
SP_PIR_KEYWORDS	transducer	46	12.53	3.26	4.97E-12	6.65E-09
SP_PIR_KEYWORDS	g-protein coupled receptor	44	11.99	3.35	6.34E-12	8.48E-09
PIR_SUPERFAMILY	PIRSF800006:rhodopsin-like G protein-coupled receptors	42	11.44	3.26	6.34E-12	7.26E-09
GOTERM_BP_FAT	GO:0007600 sensory perception	45	12.26	3.18	1.10E-11	1.80E-08
GOTERM_BP_FAT	GO:0050890 cognition	46	12.53	2.87	1.87E-10	3.07E-07
UP_SEQ_FEATURE	zinc finger region:C2H2-type 10	27	7.36	4.64	1.94E-10	3.10E-07
UP_SEQ_FEATURE	zinc finger region:C2H2-type 1; degenerate	17	4.63	8.23	2.35E-10	3.77E-07
GOTERM_BP_FAT	GO:0007186 G-protein coupled receptor protein signaling pathway	51	13.90	2.63	2.87E-10	4.70E-07
UP_SEQ_FEATURE	zinc finger region:C2H2-type 11	25	6.81	4.91	3.32E-10	5.31E-07
UP_SEQ_FEATURE	zinc finger region:C2H2-type 9	28	7.63	4.30	4.58E-10	7.33E-07
UP_SEQ_FEATURE	zinc finger region:C2H2-type 12	23	6.27	5.27	5.15E-10	8.24E-07
SMART	SM00349:KRAB	26	7.08	4.36	7.67E-10	8.65E-07
UP_SEQ_FEATURE	zinc finger region:C2H2-type 15	17	4.63	7.40	1.17E-09	1.88E-06
UP_SEQ_FEATURE	zinc finger region:C2H2-type 7	30	8.17	3.84	1.33E-09	2.13E-06
INTERPRO	IPR001909:Krueppel-associated box	26	7.08	4.20	3.15E-09	4.49E-06
UP_SEQ_FEATURE	domain:KRAB	25	6.81	4.37	3.38E-09	5.41E-06
UP_SEQ_FEATURE	zinc finger region:C2H2-type 14	17	4.63	6.32	1.19E-08	1.90E-05
UP_SEQ_FEATURE	zinc finger region:C2H2-type 13	19	5.18	5.50	1.19E-08	1.91E-05
UP_SEQ_FEATURE	zinc finger region:C2H2-type 8	27	7.36	3.73	1.86E-08	2.98E-05
UP_SEQ_FEATURE	zinc finger region:C2H2-type 6	29	7.90	3.42	3.22E-08	5.15E-05
INTERPRO	IPR01089:Small chemokine, C-X-C	7	1.91	29.85	4.94E-08	7.06E-05
INTERPRO	IPR002473:Small chemokine, C-X-C/Interleukin 8	7	1.91	27.72	8.52E-08	1.22E-04
GOTERM_BP_FAT	GO:0050877 neurological system process	48	13.08	2.21	2.61E-07	4.27E-04
INTERPRO	IPR018048:Small chemokine, C-X-C, conserved site	7	1.91	22.83	3.35E-07	4.79E-04
INTERPRO	IPR002337:Haemoglobin, beta	5	1.36	55.44	5.04E-07	7.20E-04
INTERPRO	IPR013087:Zinc finger, C2H2-type/integrase, DNA-binding	30	8.17	2.77	1.34E-06	0.002
SMART	SM00355:ZnF_C2H2	33	8.99	2.48	1.77E-06	0.002
SP_PIR_KEYWORDS	receptor	52	14.17	2.00	2.39E-06	0.003
UP_SEQ_FEATURE	zinc finger region:C2H2-type 5	27	7.36	2.90	2.39E-06	0.004
UP_SEQ_FEATURE	zinc finger region:C2H2-type 3	29	7.90	2.70	3.79E-06	0.006
GOTERM_MF_FAT	GO:0047760 butyrate-CoA ligase activity	5	1.36	38.47	3.81E-06	0.005
INTERPRO	IPR007087:Zinc finger, C2H2-type	33	8.99	2.43	5.58E-06	0.008
PIR_SUPERFAMILY	PIRSF002522:CXC chemokine	6	1.63	20.55	6.13E-06	0.007
SP_PIR_KEYWORDS	oxygen carrier	5	1.36	35.19	6.39E-06	0.009
INTERPRO	IPR015880:Zinc finger, C2H2-like	33	8.99	2.39	7.71E-06	0.011
GOTERM_BP_FAT	GO:0007166 cell surface receptor linked signal transduction	59	16.08	1.78	9.41E-06	0.015
UP_SEQ_FEATURE	zinc finger region:C2H2-type 16	11	3.00	6.18	1.14E-05	0.018

PIR_SUPERFAMILY	PIRSF500045:hemoglobin, vertebrate type	5	1.36	29.97	1.16E-05	0.013
UP_SEQ_FEATURE	zinc finger region:C2H2-type 17	10	2.72	7.02	1.20E-05	0.019
UP_SEQ_FEATURE	disulfide bond	77	20.98	1.62	1.27E-05	0.020
UP_SEQ_FEATURE	topological domain:Extracellular	75	20.44	1.62	1.99E-05	0.032
PIR_SUPERFAMILY	PIRSF005559:zinc finger protein ZFP-36	13	3.54	4.58	2.22E-05	0.025
SP_PIR_KEYWORDS	disulfide bond	78	21.25	1.59	2.44E-05	0.033
UP_SEQ_FEATURE	zinc finger region:C2H2-type 20	7	1.91	11.56	2.64E-05	0.042
SP_PIR_KEYWORDS	blood	5	1.36	25.59	2.89E-05	0.039
SP_PIR_KEYWORDS	cell membrane	63	17.17	1.70	3.07E-05	0.041

RESEARCH**Open Access**

Integrative modeling reveals the principles of multi-scale chromatin boundary formation in human nuclear organization

Benjamin L Moore, Stuart Aitken and Colin A Semple^{*}

Abstract

Background: Interphase chromosomes adopt a hierarchical structure, and recent data have characterized their chromatin organization at very different scales, from sub-genic regions associated with DNA-binding proteins at the order of tens or hundreds of bases, through larger regions with active or repressed chromatin states, up to multi-megabase-scale domains associated with nuclear positioning, replication timing and other qualities. However, we have lacked detailed, quantitative models to understand the interactions between these different strata.

Results: Here we collate large collections of matched locus-level chromatin features and Hi-C interaction data, representing higher-order organization, across three human cell types. We use quantitative modeling approaches to assess whether locus-level features are sufficient to explain higher-order structure, and identify the most influential underlying features. We identify structurally variable domains between cell types and examine the underlying features to discover a general association with cell-type-specific enhancer activity. We also identify the most prominent features marking the boundaries of two types of higher-order domains at different scales: topologically associating domains and nuclear compartments. We find parallel enrichments of particular chromatin features for both types, including features associated with active promoters and the architectural proteins CTCF and YY1.

Conclusions: We show that integrative modeling of large chromatin dataset collections using random forests can generate useful insights into chromosome structure. The models produced recapitulate known biological features of the cell types involved, allow exploration of the antecedents of higher-order structures and generate testable hypotheses for further experimental studies.

Background

The chromatin structure of human interphase chromosomes plays critical roles in a wide range of cellular functions and consists of many hierarchically arranged but interconnected layers of structure. These range from the three-dimensional arrangement of multi-megabase-scale domains within the nucleus down to the chemical modifications carried by individual nucleosomes and nucleotides at particular loci. A recurring question has been how these many different levels of chromatin structure are related to one another [1]. In the wake of recent efforts to comprehensively map the epigenomic landscape in human cells, integrative approaches have suggested classifications of

chromatin into distinct, functional states. The number of chromatin states identified in these pioneering studies has varied widely, from as few as 6 to as many as 51, using a variety of locus-level features such as DNA methylation, histone modifications and transcription factor binding patterns [2-5]. These states usually encompass small, sub-genic regions and have provided intriguing insights into chromatin-mediated variation in promoter and enhancer activity. At the same time technological developments such as the Hi-C method have provided datasets describing the overall spatial organization of the human genome [6], but the relationships between such datasets and the wide spectrum of locus-level features are not well understood. A recent study examining seven such features and their relationships to the spatial organization of the mouse genome in embryonic stem cells (ESCs) concluded that chromosome architecture is largely determined by the

*Correspondence: colin.semple@igmm.ed.ac.uk

MRC Human Genetics Unit, MRC Institute of Genetics and Molecular Medicine, University of Edinburgh, Crewe Road, Edinburgh, EH4 2XU, UK

binding patterns of particular transcription factors, and that these cells have a unique higher-order chromatin structure as a result [7]. Thus it is unclear whether such results are relevant to other cell types and species, or whether the inclusion of a broader range of features would provide additional insights.

Many aspects of higher-order chromatin remain broadly invariant between cell types, and genome-wide datasets as diverse as replication timing domains, lamin association domains and Hi-C interaction matrix eigenvectors show strong correlations across many different human cell lines [8]. Indeed, most measurable aspects of higher-order structure have been conserved during evolution across the majority of the mammalian genome [8–10]. However, a minority (perhaps 20% to 30%) of the genome is within more labile structures, such that the behaviors of many replication timing domains and lamin association domains change significantly upon cellular differentiation from ESCs, altering the transcriptional output of many resident genes [10,11]. A large literature surrounds the dynamics of locus-level chromatin during differentiation and reprogramming, emphasizing the critical importance of genomic patterns of DNA binding proteins, particular histone modifications and DNA methylation (for example, [12]). Yet we still lack an integrated view of chromatin dynamics that details the dependencies between these locus-level phenomena, the remodeling of large domains and changes in nuclear organization. The extent to which higher-order chromatin dynamics depends upon the spectra of features occurring at these lower levels has not been studied quantitatively.

Given the existence of neighboring chromatin domains with distinct structures and activities, the boundaries defining such domains have been a focus of particular interest. The topological domains (TADs) described by Dixon et al. [9] were reported to be separated by boundary regions showing pronounced peaks of the insulator binding protein CTCF, although depletion of CTCF appears to have little effect on TAD boundaries [13]. Similarly, deletion of a TAD boundary on the mouse X chromosome resulted in many altered interactions, but did not cause the two TADs separated by this boundary to completely merge [14]. Thus there is much left to learn about the basis of TAD boundaries. The scale of TAD organization (median length 880 kb) is below that of the multi-megabase chromatin domains delineating occupancy of A and B nuclear compartments [15]. These compartments constitute domains of transcriptionally active, relatively centrally positioned chromatin, and relatively inactive, peripheral chromatin respectively; consequently compartment boundaries often mark a profound divergence in functional state. It is not known whether TAD boundaries coincide with compartment boundaries, and the similarities or differences in the features

underlying these two boundary classes also remain unstudied.

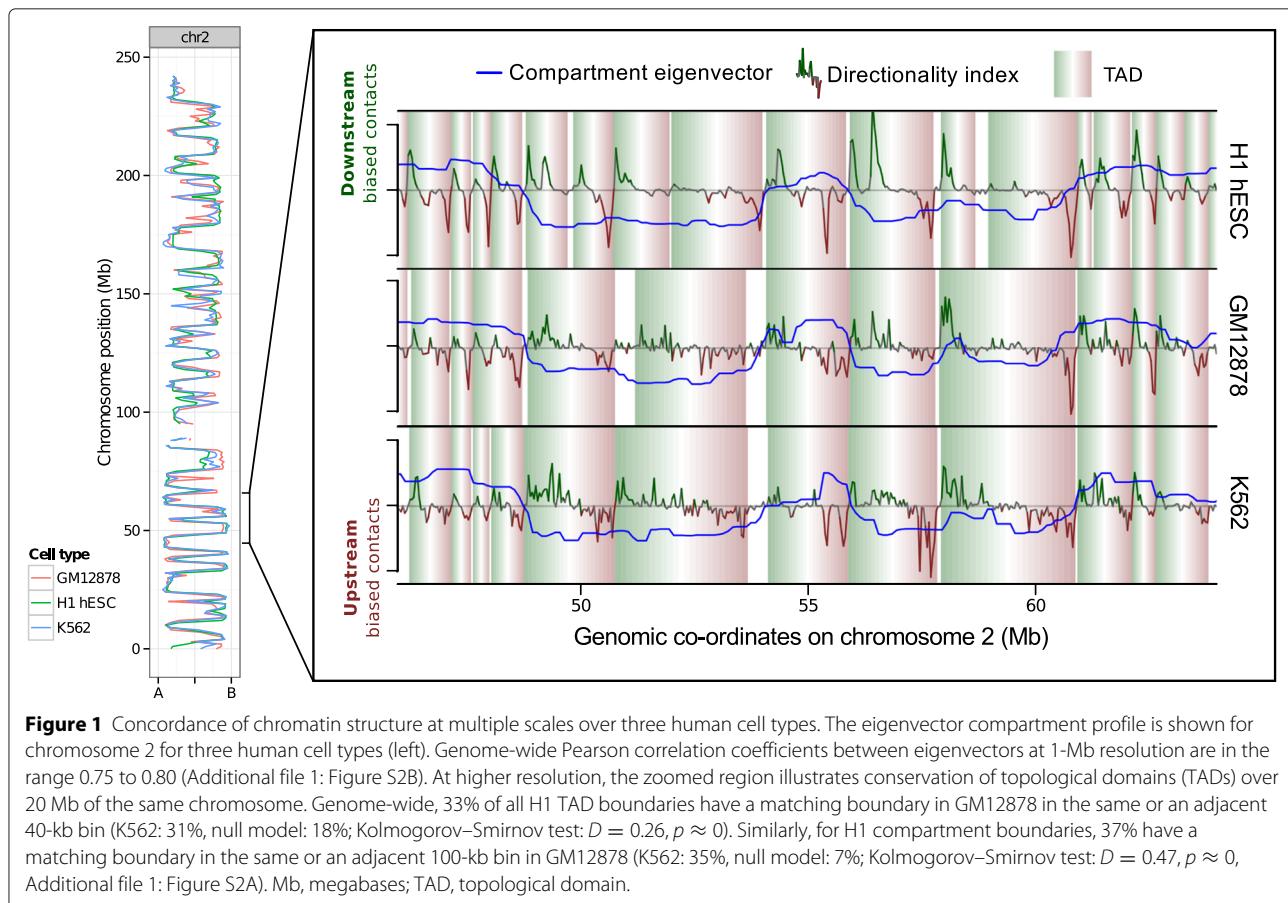
Here we exploit the unprecedented volumes of data produced recently [4] to provide an integrated and rigorously quantitative view of locus-level chromatin features, higher-order chromatin structure and nuclear organization across three cell types. We use integrative modeling approaches to directly study the contribution of 35 locus-level chromatin features to chromosome architecture across three human cell types as measured by Hi-C. These data are relevant to the quantitative, molecular basis of higher-order chromatin, the dominant determinants of chromatin dynamics, and prominent features conferring the structure of domain boundaries.

Results

Higher-order chromatin organization is largely concordant and predictable across cell types

In common with previous studies of higher-order chromatin structure [8–11], there was evidence for good concordance of Hi-C data between different cell types. Hi-C eigenvectors were calculated for three human cell types (GM12878, H1 hESC and K562 cell lines) using the same analysis protocols, and were found to be strongly and significantly correlated (Figure 1; Additional file 1: Figure S1). Most 1-Mb regions appear to be constitutively present (that is, across cell types) in either the A or B compartments, corresponding to relatively centrally positioned, transcriptionally active or more peripheral repressive chromatin, respectively [15]. Strong correspondence across cell types was also observed for TAD boundaries, and for the positioning of compartment boundaries, separating A and B compartments (Additional file 1: Figure S2).

Although it is often assumed that higher-order chromatin domain organization (at the megabase scale) across the genome is to some degree dependent upon lower-level features (at the scale of tens or hundreds of base pairs), the identity and independent contributions of these features are unknown. Beyond this it has also been unclear whether there are strong enough dependencies to allow accurate prediction of higher-order structure. For each of the three Hi-C eigenvector datasets corresponding to the Tier 1 ENCODE cell lines (GM12878, H1 hESC and K562) we assembled datasets of 35 matched locus-level chromatin features, including sites bound by 21 DNA binding proteins, and 11 histone modifications/variants and DNase hypersensitive sites (see Materials and methods). The GC content of each 1-Mb region, which is known to be correlated with higher-order structure (for example, [8]), was also included as an additional feature in each model for comparison with chromatin features. Importantly, each Hi-C dataset was re-analyzed to provide comparable identically processed data, which



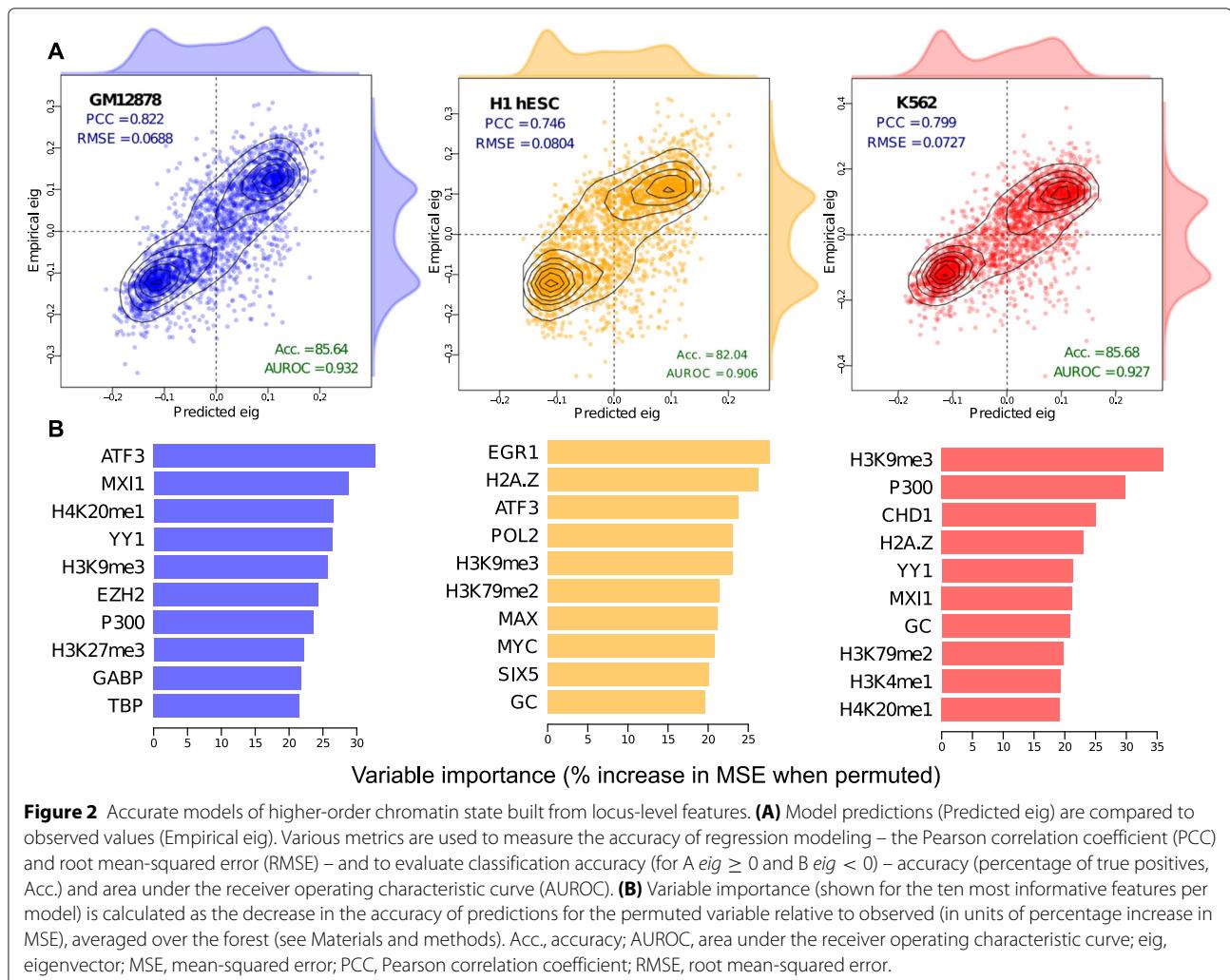
was complementary to the identically processed, locus-level ENCODE data. It was possible to construct random forest models with good predictive accuracy, and strong and significant correlations were seen between predicted and empirically measured eigenvector values for each cell type (Figure 2). The models show high predictive power, particularly for GM12878 where the model achieved a Pearson correlation coefficient (PCC) of 0.805 between predicted and measured values. These levels of accuracy are similar to those reported (median PCC = 0.83 over seven cell types) for strikingly successful models of the transcriptional output of promoters using locus-level chromatin features [16]. Other evaluation metrics also suggested successful models, such as the ability to correctly assign 1-Mb regions to compartments A and B (see area under the receiver operating characteristic data in Figure 2). It would be feasible to construct similar, but more comprehensive models using all ENCODE chromatin features for a given cell type, although the resulting models would not be comparable between cell types. However, the high accuracy of the current models suggests there is limited potential for improvement by adding further features. Also, even the most comprehensive models that could be constructed, using all currently

available data, inevitably represent a minority of the features actually present in chromatin [1].

While 1-Mb compartment eigenvectors are low resolution relative to that typically employed for chromatin immunoprecipitation sequencing (ChIP-seq) data, megabase bins are a suitable choice for analyzing large chromosomal compartments [15,17]. To confirm our modeling accuracy is not sensitive to resolution, we applied models trained with 1 Mb to 100 kb resolution datasets and saw similarly high levels of accuracy (88% to 95%, as accurate as 1-Mb models in terms of predicted and empirical PCC, Additional file 1: Figure S3).

Influential features underlying higher-order structure differ between cell types

Given the correlations seen between Hi-C eigenvectors from different cell types (Figure 1) and the similar predictive power of cell-type-specific models (Figure 2A), one might assume that a similar combination of informative variables appears in each of the models. The broad trends in relative variable importance (see Materials and methods) do indeed suggest that many features have a similar influence in each of the three models (Additional file 1: Figure S4A). For example the genomic distributions



of CTCF binding patterns, H3K36me3, H3K27ac and GC content maintain very similar influence across all three models, while certain variables depart from this trend and show a notably higher variable importance in a particular model. Thus substantial levels of variation between cell types are seen for the top ten most influential variables across models (Figure 2B), such that the repressive histone modification H3K9me3 is the only feature, among the ten most influential, shared between all three cell-type models. This is expected since H3k9me3 is anticorrelated or uncorrelated with most other input features (Additional file 1: Figure S5), and is therefore a relatively information-rich variable. Overall, more highly ranked features are shared between the two relatively differentiated, hematopoietic cell lines (GM12878 and K562), with the pluripotent ESC line (H1 hESC) showing more distinct characteristics. The EGR1 transcription factor plays critical roles in cellular differentiation and shows markedly higher variable importance in the H1 hESC model. While the P300 transcriptional co-activator

protein, which controls the proliferation and differentiation of hematopoietic progenitor cells, ranks more highly in the two hematopoietic cell line models (Figure 2B, Additional file 1: Figure S4).

Many of the variables examined here are heavily interdependent, and for example co-occur in clusters denoting functional chromatin states [4]. Care must be taken not to over-interpret the differences in variable importance between models, given the pervasive multi-collinearity and clustering between variables in the input locus-level feature set (Additional file 1: Figure S5). For instance, MXI1 is an influential feature in both the hematopoietic models, while MYC and MAX are among the highest ranked features in the H1 hESC model. This is in keeping with recent results suggesting MYC binds open chromatin as a transcriptional amplifier in ESCs [18,19], with MAX and MXI1 long being known as antagonistic co-regulators of MYC [20]. Thus, in identifying nominally different informative variables for each model we will, to some extent, select different representatives of

the same cluster (Additional file 1: Figure S5). It follows that we would expect a large number of different feature combinations to have similar predictive power in broadly equivalent random forest models. With a broader perspective, there are general similarities across all three models, in that all derive much of their predictive power from indicators of transcriptional activity, markers of heterochromatin and the binding levels of combinations of broadly expressed transcription factors (Additional file 1: Figure S6).

Consistent with the presence of broad commonalities among the three models, cross-application of models showed that models trained in one cell type often performed well in another (Figure 3). In each instance of cross-application, predictive accuracy declined by no more than 21% relative to the model's native cell type. In reciprocal crosses between the two hematopoietic cell lines (K562 and GM12878), this loss of accuracy was between 5.9% and 7.8% (Figure 3A), but was 20.2% to 20.4% when these models were applied to H1 hESC data.

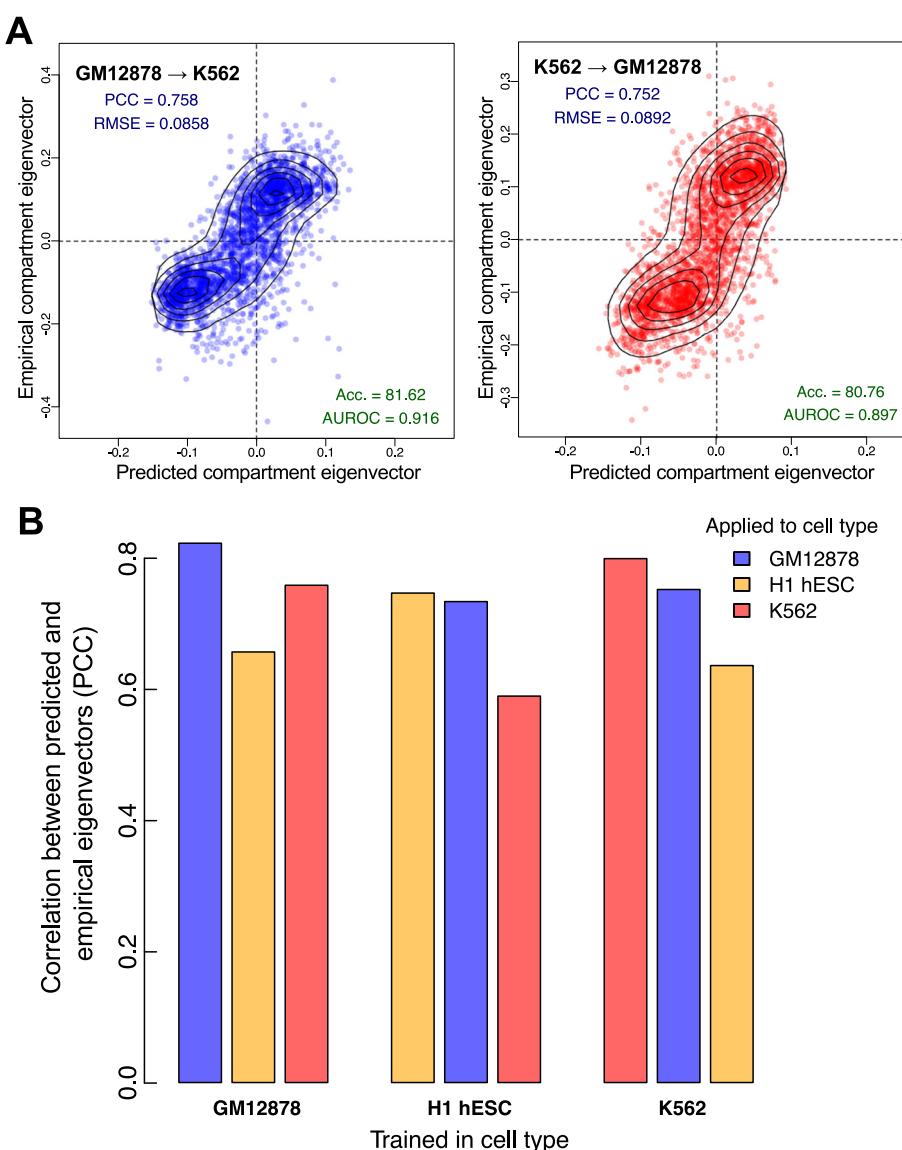


Figure 3 Models trained in one cell type can generalize to others. Each model, trained in one cell type, was applied to the chromatin feature datasets from the other two cell types. **(A)** The GM12878 model achieved high accuracy when applied to K562 features ($PCC = 0.76$), as did the reciprocal cross ($PCC = 0.75$). **(B)** In each case, predictive accuracy decreased on cross-application but there remains significant agreement between predicted and empirical values. Acc., accuracy; AUROC, area under the receiver operating characteristic curve; PCC, Pearson correlation coefficient; RMSE, root mean-squared error.

This again highlights the relatively unusual structural features of the pluripotent state.

We compared the performance of our random forest approach with two other regression methods: simple multiple linear regression and partial least squares regression, a method particularly well suited to highly correlated inputs [21]. While cell-type-specific prediction accuracy remained high for each method, cross-application between cell types confirmed our random forest approach as that most capable of learning generalizable rules of compartment prediction (Additional file 1: Figure S7).

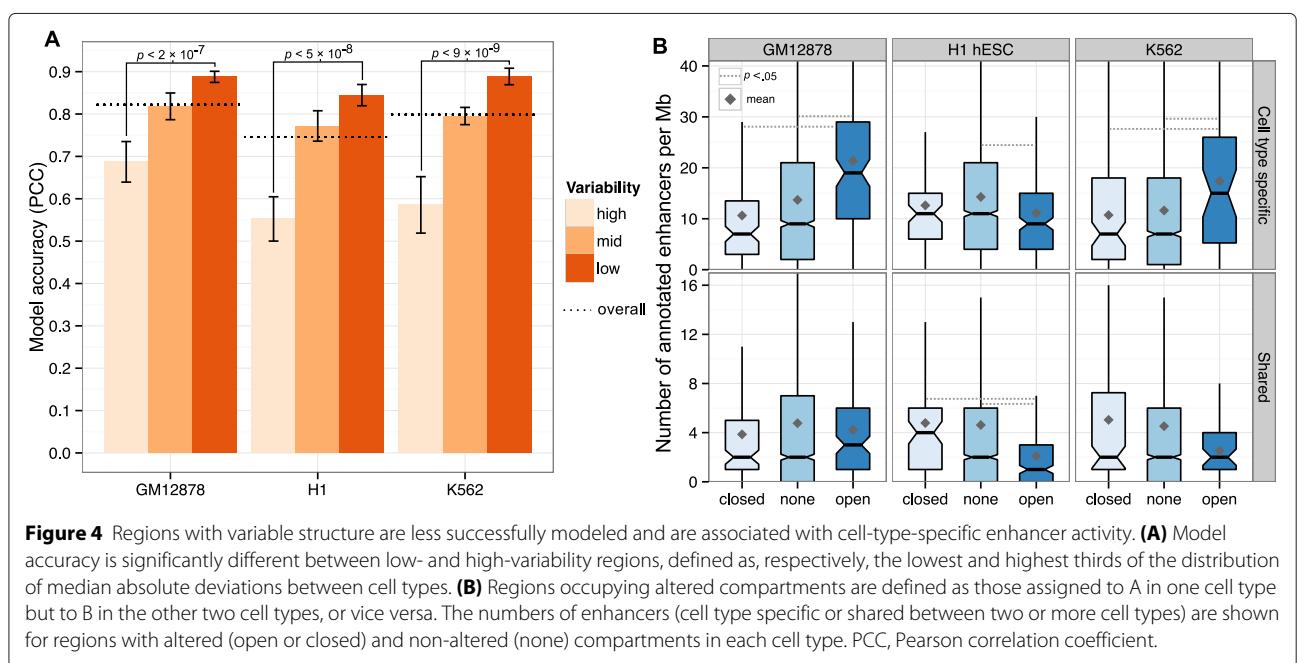
Regions of variable structure are enriched for cell-type-specific enhancers

Although the chromatin organization of much of the genome appears to be invariant between cell types (Figure 1), some regions are more dynamic. There is a clear relationship between modeling accuracy and structural stability between cell types such that the structures of more variable regions are more challenging to predict. This is evident even with the most liberal definitions of variability; for instance, if we calculate the median absolute deviation between eigenvectors across all three cell types and simply trisect the distribution, we found that the most structurally variable regions between cell types were significantly less accurately modeled in each case (Figure 4A). This could indicate the cell-type-specific features responsible for organizing these regions are largely missing from our training set, which undoubtedly represents a tiny minority of all the actual components of

chromatin in real human cells. However, it is unclear whether structural variability defined so broadly reflects altered biological function or is dominated by stochastic variations in structure among cells [22].

A more conservative definition of structurally variable regions is that they are regions altering their compartment state (between A and B compartments) in one cell type relative to the other two. Such regions will often undergo dramatic changes between transcriptionally permissive and repressive environments and might be expected to be associated with cell-type-specific biology, such as functional chromatin states [4]. This indeed seems to be the case, with regions occupying altered compartments showing corresponding changes in enhancer activity. Regions undergoing a B to A compartment transition, to a relatively transcriptionally permissive structure, were enriched for cell-type-specific enhancers in the two derived cell types used in this study but not in the ESC line, which would not be expected to have lineage-specific enhancer contacts active in its pluripotent state (Figure 4B). The same pattern was not seen for enhancers shared between two or more of the cell types under study. We observed a similar enrichment for cell-type-specific transcription (Additional file 1: Figure S8) but not for several other chromatin states including promoter activity (Additional file 1: Figure S9).

For each cell line, we identified all regions showing cell-type-specific occupancy of the active A compartment and ranked these regions according to the density of predicted active enhancers. Close examination of these regions reveals many examples of enhancer



activity nucleated upon genes associated with cell-type-specific biology (Figure 5A, Additional file 1: Figure S10). For the GM12878 (B-cell derived) cell line, an active region of variable structure rich in active enhancers was found to contain the EBF1 (early B-cell factor 1) gene (Figure 5A). The transcription factor encoded by this gene has been identified as essential in maintaining B-cell identity and establishing early lineage commitment [23,24]. Similarly a variable region active in H1 hESC (Additional file 1: Figure S10B.1) harbors the PAX1 regulator of patterning during embryogenesis [25], while a K562-specific active region (Additional file 1: Figure S10C.3) contains a gene encoding a regulator of hematopoiesis (ZFPN2/FOG2 [26]). Each example is concordant with the known biology of the cell type concerned, and each is illustrative of the genome-wide relationship between

higher-order structural variability and cell-type-specific enhancer activity (Figure 4B). We explored the functional annotations of genes in regions of cell-type-specific structure (Additional file 2: Tables S1, S2 and S3), and although we observed some artificial enrichments (generated by duplicated gene clusters within some of these 1-Mb regions), no significant enrichments were seen across regions.

A defining characteristic of active A compartment regions is a preferential bias in contacting other A compartment regions [15]. However, it is not clear whether cell-type-specific transitions in higher-order structure are solely compartment-level phenomena, or involve other structural strata. We therefore examined the genome-wide contact profiles of each region of variable cell-type-specific chromatin structure in detail. If these

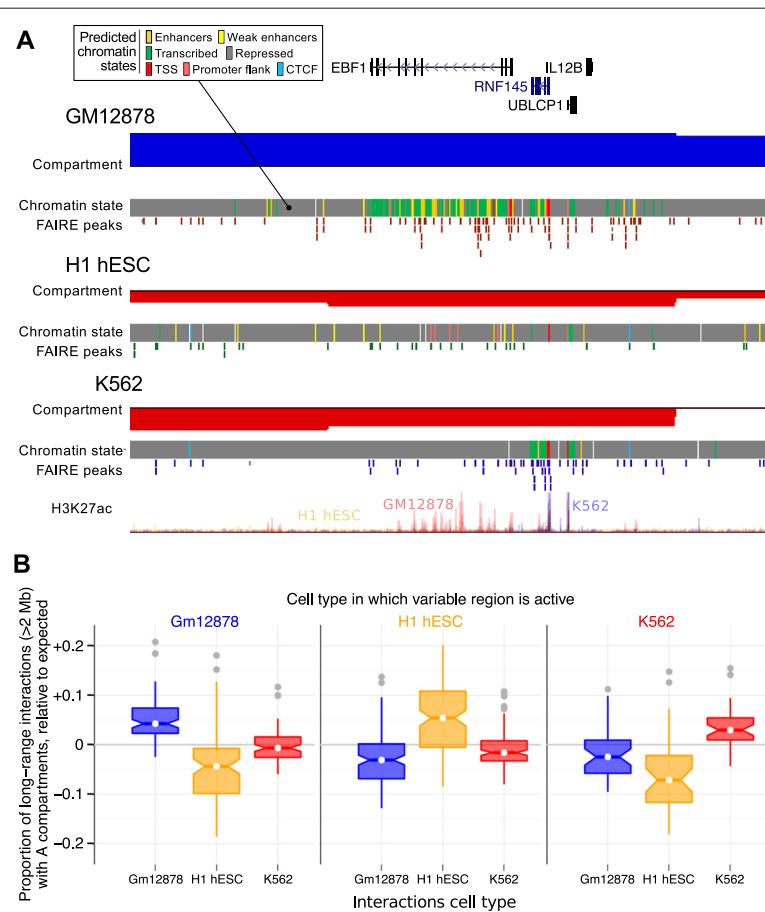


Figure 5 Structurally variable regions indicate cell-type-specific biology. Regions occupying the active A nuclear compartment in one cell type, but the repressed B compartment in the other two, were selected and ranked by the number of predicted active enhancers (Figure 4). **(A)** The region chr5:158–159 Mb, which occupies the open A compartment in GM12878 cells, is shown as an example (top five regions for each cell type are shown in Additional file 1: Figure S10). Displayed tracks are: known genes (UCSC), compartment eigenvectors, chromHMM/Segway combined chromatin state predictions, open chromatin FAIRE peaks, and H3K27ac signal. **(B)** Structurally variable regions show a greater than expected proportion of contacts with other active A compartments, in the cell type in which they are active relative to those same regions in the other two cell types. Box plot notches represent 95% confidence intervals of the median. Each variable region is also shown individually in Additional file 1: Figure S11. TSS, transcription start site.

cell-type-specific structures are mediated by finer-scale structural levels (such as TADs) we might expect to see predominantly short-range contacts in their underlying contact profile. Instead, we found that variable regions preferentially interact with other A compartment regions in the cell types in which they are active (Figure 5B, Additional file 1: Figure S11), but not in the other cell types in which they are inactive. This supports the idea that these cell-type-specific regions are undergoing compartment-level transitions, disproportionately mediated by the formation of long-range contacts, while also not precluding additional changes at lower levels such as TADs.

TAD boundaries and compartment boundaries possess similar features

The mammalian genome is organized into TADs, predominantly self-interacting chromatin domains, with boundary regions reportedly associated with pronounced peaks and troughs of particular features within 500 kb of the predicted boundary [9]. Exploration of this phenomenon using a set of 24 mouse ESC chromatin features (and a smaller number of human ESC features) reportedly revealed enrichment peaks of CTCF, H3K4me3 and H3K36me3, as well as a pronounced dip in H3K9me3, suggesting that high levels of transcription may contribute to boundary formation [9]. However, it was unclear whether other features show unusual patterns in TAD boundary regions, and whether the constellation of features involved changes between cell types. The features associated with boundaries separating A and B compartments calculated from Hi-C eigenvectors have not been studied to our knowledge. The datasets assembled here, consisting of 35 matched chromatin features across three cell types, allow us to conduct the first comparative study of the constituents of human TAD and compartment boundary regions.

We derived TAD boundaries according to established methods [9] for all three cell types under study. We then sought evidence for significantly enriched or depleted features at TAD boundary regions using a conservative approach (a nonparametric statistical test and Bonferroni multiple testing correction, see Materials and methods), and confirmed the previously reported peaks (CTCF and POL2) and dip (H3K9me3) in ESC data, but also revealed substantial heterogeneity between cell types. CTCF binding was found enriched at TAD boundaries across all cell types, but other features, including H3K36me3 and H3K4me3, show dramatic peaks of enrichment in H1 hESC cells that are not seen consistently in other cell types (Figure 6, Additional file 1: Figure S12). Although the dip in H3K9me3 at TAD boundaries is seen in all cell types, the extent of the depletion varies and is weakest in H1 hESC cells. Many other features show significant, though

often modest, enrichments in a particular cell type. However, overall the complexity of TAD boundaries (measured as the number of strongly enriched features) is notably higher in H1 hESC than in the other two, more differentiated, cell types (Figure 6), involving large increases in the binding of sequence specific factors such as SP1 and JUND.

Across all three cell types, several features demonstrate consistent and statistically significant patterns at TAD boundaries (Figure 6, Additional file 1: Figure S12), including peaks associated with active transcription of genes (POL2 and H3K9ac) and dips in H3K9me3, as previously reported [9]. However, other novel feature peaks of interest emerge across cell types, such as peaks of H4K20me1, a modification previously implicated in chromatin compaction [27]. Significant peaks in YY1 are evident in all cell types, which is intriguing given the evidence that YY1 and CTCF cooperate to affect long-distance interactions [28]. Co-binding of CTCF with YY1 has also been shown to identify a subset of highly conserved CTCF sites [29]. Co-binding of CTCF and YY1 may also therefore be a contributing factor in the establishment of TAD boundaries, which appear to be broadly conserved across mammals [9]. To test this, we split our sets of TAD boundaries into those possessing ChIP-seq peaks (region peaks called by ENCODE [4]) for CTCF, YY1, both CTCF and YY1 (overlapping peaks) and neither. We then tested each boundary subset for genome-wide enrichments of the other features in our dataset (Additional file 1: Figure S14). Unexpectedly, we found that boundaries marked by YY1 (without overlapping CTCF peaks) were generally most strongly enriched for other features in our dataset. We also found that boundaries lacking both CTCF and YY1 peaks showed instead the strongest enrichments for RAD21 in each cell type (Additional file 1: Figure S14), reinforcing previous findings that describe the distinct influences of CTCF and cohesin in organizing chromatin structure [13,30,31]. We also observe consistent increases in GC content at TAD boundaries, at a scale that is difficult to reconcile with the presence of smaller-scale features such as repeat elements or CpG islands (Additional file 1: Figure S12).

Where neighboring genomic regions occupy contrasting A and B nuclear compartments, the disparity implies the presence of a boundary region. Putative compartment boundaries were identified by using a hidden Markov model to infer the state sequence of A/B compartments across the genome based on observed principal component eigenvectors. Analogously to the TAD boundary analysis, we then sought significant enrichments or depletions in 36 chromatin features over these compartment boundaries (Figure 6, Additional file 1: Figure S13). Compartment boundaries display similar spectra of enrichments to previously studied TAD boundaries [9] but at

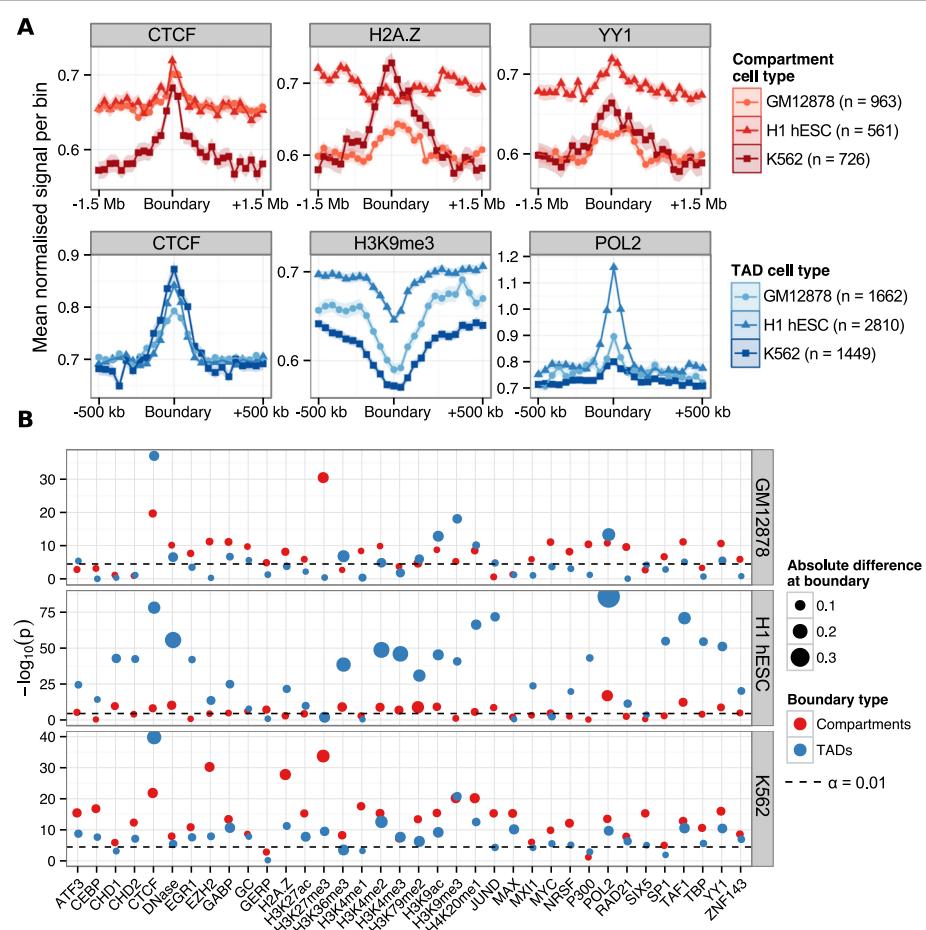


Figure 6 Chromatin features underlying TAD and compartment boundaries. **(A)** Selected profiles for locus-level features are shown for TAD boundaries (CTCF, H3K9me3 and POL2) and compartment boundaries (H2A.Z, H3K4me2 and YY1), as a mean normalized ChIP-seq signal relative to input chromatin per bin (± 1 standard error). TAD boundaries were examined over 40-kb bins over the 1 Mb flanking each boundary; compartment boundaries were examined over 100-kb bins over 3 Mb. **(B)** The significance of enrichment or depletion ($-\log_{10} P$ two-tailed Mann–Whitney test) of a feature was calculated as the boundary bin relative to the ten most peripheral bins (five either side). Points are scaled by the absolute mean difference in signal over the boundary relative to the mean of peripheral bins. ChIP-seq, chromatin immunoprecipitation sequencing; TAD, topological domain.

lower resolution, reflecting the different scales of these levels of organization (Figure 6B, Additional file 1: Figure S13). Peaks associated with active promoters (POL2, TAF1 and H3K9ac) are again evident. Parallel enrichments of CTCF, YY1 and H4K20me1 are also seen at compartment boundaries, as they were for TAD boundaries, in each cell type under study. In addition, compartment boundaries show enrichments of H3K79me2, which is known to play critical roles in cellular reprogramming [32]. Remarkably, H3K79me2 has also recently been shown to mark the borders of small regions of open chromatin (hundreds of base pairs) [33]. Thus, there may be similarities in chromatin compaction boundaries at very different scales.

Certain features show intriguing contrasts between cell types. The histone variant H2A.Z lacks any trace

of enrichment at H1 hESC compartment boundaries, but is significantly enriched in the other two cell types (Figure 6A), consistent with reports describing H2A.Z relocation during cellular differentiation [34]. Compartment boundaries also show enrichment for the cohesin complex subunit RAD21 in the two hematopoietic cell types (Additional file 1: Figure S12), and cohesin is another factor implicated in modulating nuclear architecture in partnership with CTCF [13]. Various other enrichments with very modest effect sizes are also evident at compartment boundaries (Figure 6B, Additional file 1: Figure S13). In contrast to TAD boundaries, the composition of compartment boundaries appears least complex in H1 hESC, relative to the other two cell types. Overall compartment and TAD boundaries are associated with overlapping spectra of chromatin features across cell

types. These involve DNA-binding proteins implicated in chromosome architecture (CTCF, YY1 and RAD21), but also implicate the initiation and repression of transcription as critical to boundary formation. However, these two boundary classes occur at different scales, with patterns of informative features typically spanning regions up to 500 kb for TAD boundaries, and patterns associated with compartment boundaries often spanning more than 1 Mb (Additional file 1: Figure S12, Additional file 1: Figure S13).

Topological domains cluster by epigenetic enrichments

Sexton et al. [35] showed that, in the *Drosophila* genome, topological structures termed physical domains could observably be clustered into distinct functional groups based on their average feature enrichments. It is of interest to repeat this experiment with our human datasets and across multiple cell types to detect finer delineation of chromatin state beyond A and B compartmentalization. We found that TADs called across the three cell types used in this work could be clustered into transcriptionally active (active), repressed heterochromatin (null) and polycomb-associated (PcG) domains, based on the patterns of DNase hypersensitivity, H3k9me3 and H3k27me3, respectively (Additional file 1: Figure S15). This analysis reveals that active compartments typically cover both active and PcG-associated TADs, while B compartments appear more homogeneous and are composed mostly of H3k9me3-enriched heterochromatin even when considering fine-grained TAD structures rather than megabase-sized genomic blocks.

Discussion

The recent abundance of epigenomic data for model cell types has enabled accurate modeling of the transcriptional output of human promoters, and a rigorously quantitative assessment of the most influential chromatin features underlying gene expression [16]. We have shown that it is possible to construct comparable models describing the features underlying higher-order chromatin structure, and that their predictive accuracy can be high. Our analysis exploits Hi-C datasets that have been re-analyzed, from the initial sequence read mapping onwards, identically for three different cell types. These data were collated with 35 locus-level ENCODE chromatin datasets, also processed identically, and matched across the same cell types. In common with previous studies [8,9], we observed good concordance of higher-order chromatin structure, reflected in Hi-C data, between different cell types. Random forest models summarized the important relationships among these many variables, providing insights into the quantitative contributions of locus-level chromatin features to higher-order structures. Although certain features were notably more influential in a particular

cell type, the models shared overlapping constellations of informative features, allowing the cross-application of models between cell types.

Integrative analyses of locus-level chromatin data have allowed the prediction of functional chromatin states [2–5] but these states typically encompass small regions such as the enhancers examined here. The prediction of higher-order chromatin domains has received much less attention, and it was not clear until now that sufficient data existed to allow accurate predictions. Our data show that accurate predictions of Hi-C-derived eigenvector values, and the nuclear compartment domains based upon them, are entirely feasible. Strong and significant correlations are seen between cell types for a variety of human higher-order domains, delineating variation in replication timing, lamin association and nuclear compartments derived from Hi-C eigenvectors [8]. The data presented here therefore suggest that a variety of such domains could be successfully modeled. Given that the binding patterns of most human chromatin components have not yet been mapped, the models presented here are remarkably successful, though will undoubtedly improve with further data and algorithm development. These models also allowed us to probe the features underlying regions with variable higher-order structure between cell types, revealing enrichments of cell-type-specific enhancer activity, and suggesting links between functional chromatin states and higher-order domain dynamics. It is not possible to distinguish cause and effect using the current data, but it seems likely that the alterations in domain organization occur prior to enhancer activity.

The current data suggest that the contributions of certain locus-level chromatin features to higher-order structures vary between cell types. Striking examples include the strong influence of H3K9me3 in K562 leukemia cells, and EGR1 binding in H1 hESC. EGR1 is a pivotal regulator of cell fate and mitogenesis with critical roles in development and cancer [36]. The patterns of repressive H3K9me3 accumulation have been a focus in the cancer literature and have been proposed as a diagnostic marker in leukemia [37]. Similarly, the model for GM12878 (Epstein–Barr virus transformed lymphoblastoid) cells shows a disproportionate influence of ATF3 binding patterns, and ATF3 induction is a known consequence of virus-transformed cells [38]. Thus, the most cell-type-specific features in these models may be important indicators of cell-type-specific functions. These cell-type-specific features present a paradox, in view of the strong correlations in organization genome-wide across different cell types [8,9], and the demonstration that models trained in one cell type often perform well with data from other cell types. These contradictory observations are reconciled by the presence of inter-correlated clusters of features underlying A and B compartments. The

shifting membership of these clusters evidently retains enough similarity between cell types to enable the cross-application of models.

Chromatin boundaries, separating TADs and nuclear compartments at different scales, also showed cell-type-specific enrichments of various locus-level chromatin features. Across cell types, the complexity of boundary composition varies considerably so that only a few features were seen consistently enriched or depleted at boundaries. Peaks associated with active promoters were notable for both TAD and compartment boundaries in all cell types. Among the most influential variables for the random forest models constructed for the two hematopoietic cell lines was the ubiquitous transcription factor YY1, which reappeared in the analysis of chromatin boundary regions. Significant enrichments of YY1 were seen at TAD and nuclear compartment boundaries in all three cell types. Thus, the same protein was implicated at the level of broad genomic binding patterns (over 1-Mb intervals) and at the level of locally enriched peaks at boundary regions (spanning 100 to 500 kb). This is intriguing as YY1 has recently been shown to co-localize with the architectural protein CTCF [39] and suggests that these proteins cooperate in the establishment of domain boundaries. The identification of such features, significantly enriched at boundary regions, provides potential targets for deletion in experimental studies further exploring the structure and function of domains (for example, [14]). Both cell-type-specific and general constituents of boundaries may have utility in the biomedical interpretation of genomic variation in noncoding regions of the genome.

Conclusions

It has become commonplace to discuss the multi-layered, hierarchical organization of interphase chromosomes across strata ranging from nuclear compartments, down to the spectra of histone modifications and bound proteins at individual sub-genic regions. However, we lack a detailed understanding of how these strata interact. We have shown that our perspectives of features occurring at different strata can be bridged by modeling approaches, and the models produced can be used to explore the interrelationships between these different features quantitatively.

We constructed cell-type-specific models of nuclear organization, as reflected in Hi-C-derived eigenvector profiles, to discover the most influential features underlying higher-order structures. We found open and closed compartments to be well correlated with combinatorial patterns of histone modifications and DNA binding proteins, enabling accurate predictive models. These models could be cross-applied successfully between cell types highlighting constellations of common structural features associated with different nuclear compartments

as expected. Dissection of the most influential variables also revealed important differences between models, consistent with the known biological contrasts among these cell types, such as the prominence of EGR1 in ESCs and H3K9me3 in the leukemia cell line. Investigation of regions showing variable nuclear organization across the three cell types under study, revealed enrichments for cell-type-specific enhancer activity, often nucleated at genes with known roles in cell-type-specific functions. Finally we used model predictions to examine boundary composition between higher-order domains across cell types. Among enrichments of a large number of factors observed at different boundaries in different cell types, CTCF and YY1 were found consistently and may cooperate to establish domain boundaries. In summary, we show that integrative modeling of large chromatin dataset collections using random forests can generate useful insights into chromosome structure and seed testable hypotheses for further experimental studies.

Materials and methods

Hi-C data and locus-level chromatin features

Hi-C datasets for human cell types H1 hESC [9], K562 [15] and GM12878 [40] were retrieved (Gene Expression Omnibus accession numbers: [GEO:GSE35156], [GEO:GSE18199] and [GEO:SRX030113]) and mapped to the genome (hg19/GRCh37). Iterative mapping was performed using the hiclib software package [41] and bowtie2 [42] with the very-sensitive flag. Mapped reads were then binned into contact maps and iteratively corrected [41]. The hiclib software was also used for eigenvector expansion of each intrachromosomal contact map, performed independently for each chromosome arm.

Genome-wide ChIP-seq datasets for 22 DNA binding proteins (ATF3, CEBPB, CHD1, CHD2, CMYC, CTCF, EGR1, EZH2, GABP, JUND, MAX, MXI1, NRSF, POL2, P300, RAD21, SIX5, SP1, TAF1, TBP, YY1 and ZNF143) and ten histone modifications (H3K27ac, H3K27me3, H3K36me3, H3K4me1, H3K4me2, H3K4me3, H3K79me2, H3K9ac, H3K9me3 and H4K20me1) were produced by ENCODE (July 2012 data freeze, used in [43,44]), in addition to DNase I hypersensitivity data and H2A.Z occupancy (Additional file 1: Figure S5), for each of the Tier 1 ENCODE cell lines used in this work: H1 hESC, K562 and GM12878 [4]. These data were processed using MACSv2 [45] to produce a fold-change signal relative to input chromatin and the data are available from [43]. Regional GC content was also calculated for each 1-Mb region and used in the feature modeling set (Additional file 3).

Structural modeling and variability

Random forest regression [46] was used as implemented in the R package randomForest [47]. Parameters of

$mtry = n/3 = 12$ and $ntrees = 200$ were assumed as the algorithm is known to be largely insensitive [48]. Variable importance within random forest regression models was measured using the mean decrease in accuracy in the out-of-bag sample. This represents the average difference (over the forest) between the accuracy of a tree with permuted and unpermuted versions of a given variable in units of percentage mean-squared error [49]. The effectiveness of the modeling approach was measured by four different metrics. Prediction accuracy was assessed by the PCC between the predicted and observed eigenvectors (out-of-bag estimate), and the root mean-squared error of the same data. Classification error, when predictions were thresholded into $A \geq 0$ and $B < 0$, was also calculated using accuracy (percentage correct classifications or true positives) and the area under the receiver operating characteristic (AUROC) curve. Together these give a comprehensive overview of model performance, both in terms of regression accuracy of the continuous eigenvector, and in how that same model could be used to label discrete chromatin compartments.

For cross-application of cell-type-specific models, a single random forest regression model was learned from all 1-Mb bins for a given cell type. This was then used to predict all bins from each of the other two cell types. The median absolute deviation was chosen as a robust measure of the variability in a given 1-Mb block between the three cell types. Blocks were ranked by this measure and the distribution was split into thirds that represented low variability (the third of blocks with the lowest median absolute deviation), and mid and high variability. Each subgroup was then independently modeled using the random forest approach described above. For each cell type we identified 1-Mb regions whose compartment state was altered relative to the other two. For example, if a 1-Mb bin was classified as occupying compartment A in H1 hESC and B in both K562 and GM12878, it is said to occupy an altered open compartment in H1 hESC. Chromatin state annotations were calculated from ENCODE ChromHMM/SegWay combined annotations for each cell type [5]. Annotated features were considered shared if there was an overlapping annotation in either of the two other cell types, and labeled as specific to a cell type otherwise.

Chromatin boundaries

TAD boundaries were called using software provided by Dixon et al. [9] with recommended parameters. For the generation of locus-level feature profiles over TAD boundaries, input features were averaged into 40-kb bins spanning ± 500 kb from the boundary center. For compartment boundaries, a two-state hidden Markov model was trained on the compartment eigenvector data and the Viterbi algorithm was used to infer

the most likely underlying state sequence that generated the observed compartment eigenvectors. Compartment boundaries were then defined as the point of transition between different compartment types. To generate boundary profiles, locus-level features were averaged into 100-kb windows extending ± 1.5 Mb either side of the boundary center.

To test for the enrichment or depletion of a chromatin feature over a given boundary, a two-tailed Mann-Whitney test was used to compare the boundary bin with the ten outermost bins of the window (five from either side). The significance level at $\alpha = 0.01$ was then Bonferroni-adjusted for multiple testing correction, and results with P values exceeding this threshold were deemed significantly enriched or depleted at a given boundary.

Scripts to reproduce the analyses and generate manuscripts figures are available at [50].

Additional files

Additional file 1: Figures S1 to S15. Collection of supplementary figures (S1 to S15) with captions.

Additional file 2: Tables S1 to S3. Functional enrichments of genes located within structurally variable regions in each cell type.

Additional file 3: cellTypeFeatureSets. Archive containing comma-separated value (CSV) files of binned input features and compartment eigenvectors used for modeling, for each of the three cell types used in this study.

Abbreviations

AUROC: Area under the receiver operating characteristic curve; ChIP-seq: Chromatin immunoprecipitation sequencing; ESC: Embryonic stem cell; kb: kilobases; Mb: megabases; PCC: Pearson correlation coefficient; Pcg: polycomb-associated; TAD: Topological domain.

Competing interests

The authors declare that they have no competing interests.

Authors' contributions

BLM carried out the analysis and helped draft the manuscript. CAS and SA conceived of the study, participated in its design and coordination and drafted the manuscript. All authors read and approved the final manuscript.

Acknowledgements

We are indebted to the ENCODE Consortium for timely and comprehensive access to its data. We are grateful to Anshul Kundaje, Stanford University, for advice on using these data. We thank the UK Medical Research Council for financial support.

Received: 9 September 2014 Accepted: 24 April 2015

Published online: 27 May 2015

References

1. Bickmore Wa, van Steensel B. Genome architecture: domain organization of interphase chromosomes. *Cell*. 2013;152:1270–84. doi:10.1016/j.cell.2013.02.001.
2. Ernst J, Kellis M. ChromHMM: automating chromatin-state discovery and characterization. *Nat Methods*. 2012;9:215–16. doi:10.1038/nmeth.1906.
3. Ram O, Goren A, Amit I, Shores N, Yosef N, Ernst J, et al. Combinatorial patterning of chromatin regulators uncovered by genome-wide location analysis in human cells. *Cell*. 2011;147:1628–39. doi:10.1016/j.cell.2011.09.057.

4. ENCODE. An integrated encyclopedia of DNA elements in the human genome. *Nature*. 2012;489:57–74. doi:10.1038/nature11247.
5. Hoffman MM, Ernst J, Wilder SP, Kundaje A, Harris RS, Libbrecht M, et al. Integrative annotation of chromatin elements from ENCODE data. *Nucleic Acids Res*. 2013;41:827–41. doi:10.1093/nar/gks1284.
6. Dekker J, Marti-Renom Ma, Mirny La. Exploring the three-dimensional organization of genomes: interpreting chromatin interaction data. *Nat Rev Genet*. 2013;14:390–403. doi:10.1038/nrg3454.
7. de Wit E, Bouwman BA, Zhu Y, Klos P, Splinter E, Versteegen MJ, et al. The pluripotent genome in three dimensions is shaped around pluripotency factors. *Nature*. 2013;501:227–31. doi:10.1038/nature12420.
8. Chambers EV, Bickmore WA, Semple CA. Divergence of mammalian higher order chromatin structure is associated with developmental loci. *PLoS Comput Biol*. 2013;9:1003017. doi:10.1371/journal.pcbi.1003017.
9. Dixon JR, Selvaraj S, Yue F, Kim A, Li Y, Shen Y, et al. Topological domains in mammalian genomes identified by analysis of chromatin interactions. *Nature*. 2012;485:376–80. doi:10.1038/nature11082.
10. Meuleman W, Peric-Hupkes D, Kind J, Beaudry JB, Pagie L, Kellis M, et al. Constitutive nuclear lamina–genome interactions are highly conserved and associated with A/T-rich sequence. *Genome Res*. 2013;23:270–80. doi:10.1101/gr.141028.112.
11. Hiratani I, Ryba T, Itoh M, Rathjen J, Kulik M, Papp B, et al. Genome-wide dynamics of replication timing revealed by *in vitro* models of mouse embryogenesis. *Genome Res*. 2010;20:155–69. doi:10.1101/gr.099796.109.
12. Liang G, Zhang Y. Embryonic stem cell and induced pluripotent stem cell: an epigenetic perspective. *Cell Res*. 2013;23:49–69. doi:10.1038/cr.2012.175.
13. Zuin J, Dixon JR, van der Reijden MI, Ye Z, Kolovos P, Brouwer RWW, et al. Cohesin and CTCF differentially affect chromatin architecture and gene expression in human cells. *Proc Natl Acad Sci USA*. 2014;111:996–1001. doi:10.1073/pnas.1317788111.
14. Nora EP, Lajoie BR, Schulz EG, Giorgetti L, Okamoto I, Servant N, et al. Spatial partitioning of the regulatory landscape of the X-inactivation centre. *Nature*. 2012;485:381–5. doi:10.1038/nature11049.
15. Lieberman-Aiden E, van Berkum NL, Williams L, Imakaev M, Ragoczy T, Telling A, et al. Comprehensive mapping of long-range interactions reveals folding principles of the human genome. *Science*. 2009;326:289–93. doi:10.1126/science.1181369.
16. Dong X, Greven MC, Kundaje A, Djebali S, Brown JB, Cheng C, et al. Modeling gene expression using chromatin features in various cellular contexts. *Genome Biol*. 2012;13:53. doi:10.1186/gb-2012-13-9-r53.
17. Lajoie BR, Dekker J, Kaplan N. The Hitchhiker's Guide to Hi-C analysis: practical guidelines. *Methods*. 2015;72:65–75. doi:10.1016/j.jymeth.2014.10.031.
18. Nie Z, Hu G, Wei G, Cui K, Yamane A, Resch W, et al. c-Myc is a universal amplifier of expressed genes in lymphocytes and embryonic stem cells. *Cell*. 2012;151:68–79. doi:10.1016/j.cell.2012.08.033.
19. Kieffer-Kwon KR, Tang Z, Mathe E, Qian J, Sung MH, Li G, et al. Interactome maps of mouse gene regulatory domains reveal basic principles of transcriptional regulation. *Cell*. 2013;155:1507–20. doi:10.1016/j.cell.2013.11.039.
20. Zervos AS, Gyuris J, Brent R. Mxi1, a protein that specifically interacts with Max to bind Myc-Max recognition sites. *Cell*. 1993;72:223–32. doi:10.1016/0092-8674(93)90662-A.
21. Wold S, Ruhe A, Wold H, Dunn III WJ. The collinearity problem in linear regression. The partial least squares (PLS) approach to generalized inverses. *SIAM J Sci Stat Comput*. 1984;5:735–43. doi:10.1137/0905052.
22. Nagano T, Lubling Y, Stevens TJ, Schoenfelder S, Yaffe E, Dean W, et al. Single-cell Hi-C reveals cell-to-cell variability in chromosome structure. *Nature*. 2013;502:59–64. doi:10.1038/nature12593.
23. Nechanitzky R, Akbas D, Scherer S, Györy I, Hoyler T, Ramamoorthy S, et al. Transcription factor EBF1 is essential for the maintenance of B cell identity and prevention of alternative fates in committed cells. *Nat Immunol*. 2013;14:867–75. doi:10.1038/ni.2641.
24. Mansson R, Welinder E, Åhsberg J, Lin YC, Benner C, Glass CK, et al. Positive intergenic feedback circuitry, involving EBF1 and FOXO1, orchestrates B-cell fate. *Proc Natl Acad Sci USA*. 2012;109:21028–33. doi:10.1073/pnas.1211427109.
25. Pohl E, Aykut A, Beleggia F, Karaca E, Durmaz B, Keupp K, et al. A hypofunctional PAX1 mutation causes autosomal recessively inherited otofaciocervical syndrome. *Hum Genet*. 2013;132:1311–20. doi:10.1007/s00439-013-1337-9.
26. Svensson EC, Tufts RL, Polk CE, Leiden JM. Molecular cloning of FOG-2: a modulator of transcription factor GATA-4 in cardiomyocytes. *Proc Natl Acad Sci USA*. 1999;96:956–61.
27. Evertts AG, Manning AL, Wang X, Dyson NJ, Garcia BA, Coller HA, et al. H4K20 methylation regulates quiescence and chromatin compaction. *Mol Biol Cell*. 2013;24:3025–7. doi:10.1091/mbc.E12-07-0529.
28. Atchison ML. Function of YY1 in long-distance DNA interactions. *Front Immunol*. 2014;5:45. doi:10.3389/fimmu.2014.00045.
29. Schwalie PC, Ward MC, Cain CE, Faure AJ, Gilad Y, Odom DT, et al. Co-binding by YY1 identifies the transcriptionally active, highly conserved set of CTCF-bound regions in primate genomes. *Genome Biol*. 2013;14:148. doi:10.1186/gb-2013-14-12-r148.
30. Seitan VC, Faure AJ, Zhan Y, McCord RP, Lajoie BR, Ing-Simmons E, et al. Cohesin-based chromatin interactions enable regulated gene expression within preexisting architectural compartments. *Genome Res*. 2013;23:2066–77. doi:10.1101/gr.161620.113.
31. Phillips-Cremins JE, Sauria MEG, Sanyal A, Gerasimova TI, Lajoie BR, Bell JSK, et al. Architectural protein subclasses shape 3D organization of genomes during lineage commitment. *Cell*. 2013;153:1281–95. doi:10.1016/j.cell.2013.04.053.
32. Onder TT, Kara N, Cherry A, Sinha AU, Zhu N, Bernt KM, et al. Chromatin-modifying enzymes as modulators of reprogramming. *Nature*. 2012;483:598–602. doi:10.1038/nature10953.
33. Chai X, Nagarajan S, Kim K, Lee K, Choi JK. Regulation of the boundaries of accessible chromatin. *PLoS Genet*. 2013;9:1003778. doi:10.1371/journal.pgen.1003778.
34. Ku M, Jaffe JD, Koche RP, Rheinbay E, Endoh M, Koseki H, et al. H2A.Z landscapes and dual modifications in pluripotent and multipotent stem cells underlie complex genome regulatory functions. *Genome Biol*. 2012;13:85. doi:10.1186/gb-2012-13-10-r85.
35. Sexton T, Yaffe E, Kenigsberg E, Bantignies F, Leblanc B, Hoichman M, et al. Three-dimensional folding and functional organization principles of the *Drosophila* genome. *Cell*. 2012;148:458–72. doi:10.1016/j.cell.2012.01.010.
36. Zwang Y, Oren M, Yarden Y. Consistency test of the cell cycle: roles for p53 and EGR1. *Cancer Res*. 2012;72:1051–4. doi:10.1158/0008-5472.CAN-11-3382.
37. Müller-Tidow C, Klein HU, Hascher A, Isken F, Tickenbrock L, Thoenissen N, et al. Profiling of histone H3 lysine 9 trimethylation levels predicts transcription factor activity and survival in acute myeloid leukemia. *Blood*. 2010;116:3564–71. doi:10.1182/blood-2009-09-240978.
38. Hagmeyer BM, Duynstam MC, Angel P, de Groot RP, Verlaan M, Elfferich P, et al. Altered AP-1/ATF complexes in adenovirus-E1-transformed cells due to E1A-dependent induction of ATF3. *Oncogene*. 1996;12:1025–32.
39. Ong CT, Corces VG. CTCF: an architectural protein bridging genome topology and function. *Nat Rev Genet*. 2014;15:234–46. doi:10.1038/nrg3663.
40. Kalhor R, Tjong H, Jayathilaka N, Alber F, Chen L. Genome architectures revealed by tethered chromosome conformation capture and population-based modeling. *Nat Biotechnol*. 2012;30:90–8. doi:10.1038/nbt.2057.
41. Imakaev M, Fudenberg G, McCord RP, Naumova N, Goloborodko A, Lajoie BR, et al. Iterative correction of Hi-C data reveals hallmarks of chromosome organization. *Nat Methods*. 2012;9:999–1003. doi:10.1038/nmeth.2148.
42. Langmead B, Salzberg SL. Fast gapped-read alignment with Bowtie 2. *Nat Methods*. 2012;9:357–9. doi:10.1038/nmeth.1923.
43. Boyle AP, Araya CL, Brdlik C, Cayting P, Cheng C, Cheng Y, et al. Comparative analysis of regulatory information and circuits across distant species. *Nature*. 2014;512:453–6. doi:10.1038/nature13668. <https://www.encodeproject.org/comparative/regulation/#HumanSet9>.
44. Ho JWK, Jung YL, Liu T, Alver BH, Lee S, Ikegami K, et al. Comparative analysis of metazoan chromatin organization. *Nature*. 2014;512:449–52. doi:10.1038/nature13415.
45. Zhang Y, Liu T, Meyer CA, Eeckhoute J, Johnson DS, Bernstein BE, et al. Model-based analysis of ChIP-Seq (MACS). *Genome Biol*. 2008;9:137. doi:10.1186/gb-2008-9-9-r137.
46. Breiman L. Random forests. *Mach Learn*. 2001;45:5–32.
47. Liaw A, Wiener M. Classification and regression by randomForest. *R News*. 2002;2:18–22.

48. Hastie T. Kernel smoothing methods. In: Elements of Statistical Learning. 2nd. Springer-Verlag; 2009. doi:10.1007/b94608_6.
49. Cutler DR, Edwards TC, Beard KH, Cutler A, Hess KT, Gibson J, et al. Random forests for classification in ecology. *Ecology*. 2007;88:2783–92.
50. Moore BL. 3dgenome (release v0.1.0). Github. <https://github.com/blmoore/3dgenome>.

**Submit your next manuscript to BioMed Central
and take full advantage of:**

- Convenient online submission
- Thorough peer review
- No space constraints or color figure charges
- Immediate publication on acceptance
- Inclusion in PubMed, CAS, Scopus and Google Scholar
- Research which is freely available for redistribution

Submit your manuscript at
www.biomedcentral.com/submit



REFERENCES

- [1] Pombo A, Dillon N (2015) Three-dimensional genome architecture: players and mechanisms. *Nature Reviews Molecular Cell Biology*, **16**(4): 245–257.
- [2] Fraser J, Williamson I, Bickmore Wa, Dostie J (2015) An Overview of Genome Organization and How We Got There: from FISH to Hi-C. *Microbiology and Molecular Biology Reviews*, **79**(3): 347–372.
- [3] de Wit E, de Laat W (2012) A decade of 3C technologies: insights into nuclear organization. *Genes & development*, **26**(1): 11–24.
- [4] van Steensel B, Dekker J (2010) Genomics tools for unraveling chromosome architecture. *Nature biotechnology*, **28**(10): 1089–1095.
- [5] Dekker J, Rippe K, Dekker M, Kleckner N (2002) Capturing chromosome conformation. *Science (New York, N.Y.)*, **295**(February): 1306–1311.
- [6] Zhao Z, Tavoosidana G, Sjölinder M, Göndör A, Mariano P, Wang S, Kanduri C, Lezcano M, Sandhu KS, et al. (2006) Circular chromosome conformation capture (4C) uncovers extensive networks of epigenetically regulated intra- and interchromosomal interactions. *Nature genetics*, **38**(11): 1341–1347.
- [7] Simonis M, Klous P, Splinter E, Moshkin Y, Willemse R, de Wit E, van Steensel B, de Laat W (2006) Nuclear organization of active and inactive chromatin domains uncovered by chromosome conformation capture-on-chip (4C). *Nature genetics*, **38**(11): 1348–1354.
- [8] Dostie J, Richmond Ta, Arnaout Ra, Selzer RR, Lee WL, Honan Ta, Rubio ED, Krumm A, Lamb J, et al. (2006) Chromosome Conformation Capture Carbon Copy (5C): A massively parallel solution for mapping interactions between genomic elements. *Genome Research*, **16**(10): 1299–1309.
- [9] Lieberman-Aiden E, van Berkum NL, Williams L, Imakaev M, Ragoczy T, Telling A, Amit I, Lajoie BR, Sabo PJ, et al. (2009) Comprehensive mapping of long-range interactions reveals folding principles of the human genome. *Science*, **326**(5950): 289–93.
- [10] Dixon JR, Selvaraj S, Yue F, Kim A, Li Y, Shen Y, Hu M, Liu JS, Ren B (2012) Topological domains in mammalian genomes identified by analysis of chromatin interactions. *Nature*, **485**(7398): 376–80.

- [11] Selvaraj S, R Dixon J, Bansal V, Ren B (2013) Whole-genome haplotype reconstruction using proximity-ligation and shotgun sequencing. *Nature biotechnology*, **31**(12): 1111–8.
- [12] Jin F, Li Y, Dixon JR, Selvaraj S, Ye Z, Lee AY, Yen Ca, Schmitt AD, Espinoza CA, Ren B (2013) A high-resolution map of the three-dimensional chromatin interactome in human cells. *Nature*, **503**(7475): 290–4.
- [13] Rao S, Huntley M, Durand N, Stamenova E, Bochkov I, Robinson J, Sanborn A, Machol I, Omer A, et al. (2014) A 3D Map of the Human Genome at Kilobase Resolution Reveals Principles of Chromatin Looping. *Cell*, **159**(7): 1665–1680.
- [14] Yaffe E, Tanay A (2011) Probabilistic modeling of Hi-C contact maps eliminates systematic biases to characterize global chromosomal architecture. *Nature genetics*, **43**(11): 1059–65.
- [15] Hu M, Deng K, Qin Z, Liu JS (2013) Understanding spatial organizations of chromosomes via statistical analysis of Hi-C data. *Quantitative Biology*, **1**(2): 156–174.
- [16] Imakaev M, Fudenberg G, McCord RP, Naumova N, Goloborodko A, Lajoie BR, Dekker J, Mirny LA (2012) Iterative correction of Hi-C data reveals hallmarks of chromosome organization. *Nature methods*, **9**(10): 999–1003.
- [17] Dekker J, Marti-Renom Ma, Mirny La (2013) Exploring the three-dimensional organization of genomes: interpreting chromatin interaction data. *Nature reviews. Genetics*, **14**(6): 390–403.
- [18] Hu M, Deng K, Selvaraj S, Qin Z, Ren B, Liu JS (2012) HiCNorm: removing biases in Hi-C data via Poisson regression. *Bioinformatics (Oxford, England)*, **28**(23): 3131–3.
- [19] Li W, Gong K, Li Q, Alber F, Zhou XJ (2014) Hi-Corrector: a fast, scalable and memory-efficient package for normalizing large-scale Hi-C data. *Bioinformatics (Oxford, England)*, (November): 1–3.
- [20] Kalhor R, Tjong H, Jayathilaka N, Alber F, Chen L (2012) Genome architectures revealed by tethered chromosome conformation capture and population-based modeling. *Nature biotechnology*, **30**(1): 90–8.
- [21] Nagano T, Lubling Y, Stevens TJ, Schoenfelder S, Yaffe E, Dean W, Laue ED, Tanay A, Fraser P (2013) Single-cell Hi-C reveals cell-to-cell variability in chromosome structure. *Nature*, **502**(7469): 59–64.
- [22] Hughes JR, Roberts N, McGowan S, Hay D, Giannoulatou E, Lynch M, De Gobbi M, Taylor S, Gibbons R, Higgs DR (2014) Analysis of hundreds of cis-regulatory

- landscapes at high resolution in a single, high-throughput experiment. *Nature genetics*, **46**(2): 205–12.
- [23] Dryden NH, Broome LR, Dudbridge F, Johnson N, Orr N, Schoenfelder S, Nagano T, Andrews S, Wingett S, *et al.* (2014) Unbiased analysis of potential targets of breast cancer susceptibility loci by Capture Hi-C. *Genome research*, pp. 1854–1868.
- [24] Sahlén P, Abdullayev I, Ramsköld D, Matskova L, Rilakovic N, Lötstedt B, Albert TJ, Lundeberg J, Sandberg R (2015) Genome-wide mapping of promoter-anchored interactions with close to single-enhancer resolution. *Genome Biology*, **16**(1): 156.
- [25] Mifsud B, Tavares-Cadete F, Young AN, Sugar R, Schoenfelder S, Ferreira L, Wingett SW, Andrews S, Grey W, *et al.* (2015) Mapping long-range promoter contacts in human cells with high-resolution capture Hi-C. *Nature Genetics*, (April): 1–12.
- [26] Nagano T, Várnai C, Schoenfelder S, Javierre BM, Wingett SW, Fraser P (2015) Comparison of Hi-C results using in-solution versus in-nucleus ligation. *Genome Biology*, **16**(1): 175.
- [27] Lajoie BR, Dekker J, Kaplan N (2014) The Hitchhikers Guide to Hi-C Analysis: Practical guidelines. *Methods*, (November).
- [28] Tanay A, Cavalli G (2013) Chromosomal domains: epigenetic contexts and functional implications of genomic compartmentalization. *Current opinion in genetics & development*, **23**(2): 197–203.
- [29] Nora EP, Lajoie BR, Schulz EG, Giorgetti L, Okamoto I, Servant N, Piolot T, van Berkum NL, Meisig J, *et al.* (2012) Spatial partitioning of the regulatory landscape of the X-inactivation centre. *Nature*, **485**(7398): 381–5.
- [30] Vietri Rudan M, Barrington C, Henderson S, Ernst C, Odom DT, Tanay A, Hadjur S (2015) Comparative Hi-C Reveals that CTCF Underlies Evolution of Chromosomal Domain Architecture. *Cell Reports*, **10**(8): 1297–1309.
- [31] Sexton T, Yaffe E, Kenigsberg E, Bantignies F, Leblanc B, Hoichman M, Parolinello H, Tanay A, Cavalli G (2012) Three-dimensional folding and functional organization principles of the Drosophila genome. *Cell*, **148**(3): 458–72.
- [32] Hou C, Li L, Qin ZS, Corces VG (2012) Gene Density, Transcription, and Insulators Contribute to the Partition of the Drosophila Genome into Physical Domains. *Molecular Cell*, **48**(3): 471–484.

- [33] Crane E, Bian Q, McCord RP, Lajoie BR, Wheeler BS, Ralston EJ, Uzawa S, Dekker J, Meyer BJ (2015) Condensin-driven remodelling of X chromosome topology during dosage compensation. *Nature*.
- [34] Feng S, Cokus S, Schubert V, Zhai J, Pellegrini M, Jacobsen S (2014) Genome-wide Hi-C Analyses in Wild-Type and Mutants Reveal High-Resolution Chromatin Interactions in Arabidopsis. *Molecular Cell*, **55**(5): 694–707.
- [35] Wang C, Liu C, Roqueiro D, Grimm D, Schwab R, Becker C, Lanz C, Weigel D (2015) Genome-wide analysis of local chromatin packing in Arabidopsis thaliana. *Genome Research*, **25**(2): 246–256.
- [36] Duan Z, Andronescu M, Schutz K, McIlwain S, McIlwain S, Kim YJ, Lee C, Shendure J, Fields S, et al. (2010) A Three-Dimensional Model of the Yeast Genome. *Nature*, **465**(7296): 363–367.
- [37] Gong K, Tjong H, Zhou XJ, Alber F (2015) Comparative 3D Genome Structure Analysis of the Fission and the Budding Yeast. *Plos One*, **10**(3): e0119672.
- [38] Zuin J, Dixon JR, van der Reijden MIJa, Ye Z, Kolovos P, Brouwer RWW, van de Corput MPC, van de Werken HJG, Knoch Ta, et al. (2013) Cohesin and CTCF differentially affect chromatin architecture and gene expression in human cells. *Proceedings of the National Academy of Sciences of the United States of America*, pp. 1–6.
- [39] Narendra V, Rocha PP, An D, Raviram R, Skok JA, Mazzoni EO, Reinberg D (2015) CTCF establishes discrete functional chromatin domains at the Hox clusters during differentiation. *Science*, **347**(6225): 1017–1021.
- [40] Sexton T, Cavalli G (2015) Review The Role of Chromosome Domains in Shaping the Functional Genome. *Cell*, **160**(6): 1049–1059.
- [41] Le Dily F, Bau D, Pohl a, Vicent GP, Serra F, Soronellas D, Castellano G, Wright RHG, Ballare C, et al. (2014) Distinct structural transitions of chromatin topological domains correlate with coordinated hormone-induced gene regulation. *Genes & Development*, **28**(19): 2151–2162.
- [42] Filippova D, Patro R, Duggal G, Kingsford C (2014) Identification of alternative topological domains in chromatin. *Algorithms for molecular biology : AMB*, **9**: 14.
- [43] Barbieri M, Chotalia M, Fraser J, Lavitas LM, Dostie J, Pombo A, Nicodemi M (2012) Complexity of chromatin folding is captured by the strings and binders switch model. *Proceedings of the National Academy of Sciences of the United States of America*, **109**(40): 16173–8.

- [44] Mirny La (2011) The fractal globule as a model of chromatin architecture in the cell. *Chromosome research : an international journal on the molecular, supramolecular and evolutionary aspects of chromosome biology*, **19**(1): 37–51.
- [45] Grosberg AY, Nechaev S, Shakhnovich E (1988) The role of topological constraints in the kinetics of collapse of macromolecules. *Journal de Physique*, **49**(12): 2095–2100.
- [46] Kadavuke S, Blobel Ga (2009) Chromatin loops in gene regulation. *Biochimica et Biophysica Acta - Gene Regulatory Mechanisms*, **1789**(1): 17–25.
- [47] Sexton T, Bantignies F, Cavalli G (2009) Genomic interactions: Chromatin loops and gene meeting points in transcriptional regulation. *Seminars in Cell and Developmental Biology*, **20**(7): 849–855.
- [48] Banerji J, Rusconi S, Schaffner W (1981) Expression of a beta-globin gene is enhanced by remote SV40 DNA sequences. *Cell*, **27**(2 Pt 1): 299–308.
- [49] Engel JD, Tanimoto K (2000) Looping, linking, and chromatin activity: new insights into beta-globin locus regulation. *Cell*, **100**(5): 499–502.
- [50] Blackwood EM, Kadonaga JT (1998) Going the distance: a current view of enhancer action. *Science (New York, N.Y.)*, **281**(5373): 60–63.
- [51] Tolhuis B, Palstra RJ, Splinter E, Grosveld F, De Laat W (2002) Looping and interaction between hypersensitive sites in the active ??-globin locus. *Molecular Cell*, **10**(6): 1453–1465.
- [52] van de Corput MPC, de Boer E, Knoch Ta, van Cappellen Wa, Quintanilla a, Ferrand L, Grosveld FG (2012) Super-resolution imaging reveals 3D folding dynamics of the -globin locus upon gene activation. *Journal of Cell Science*, pp. 4630–4639.
- [53] Sanyal A, Lajoie BR, Jain G, Dekker J (2012) The long-range interaction landscape of gene promoters. *Nature*, **489**(7414): 109–13.
- [54] Ong CT, Corces VG (2014) CTCF: an architectural protein bridging genome topology and function. *Nature reviews. Genetics*, **15**(4): 234–46.
- [55] Phillips JE, Corces VG (2009) CTCF: Master Weaver of the Genome. *Cell*, **137**(7): 1194–1211.
- [56] Filippova GN, Fagerlie S, Klenova EM, Myers C, Dehner Y, Goodwin G, Neiman PE, Collins SJ, Lobanenkov VV (1996) An exceptionally conserved transcriptional repressor, CTCF, employs different combinations of zinc fingers to bind diverged promoter sequences of avian and mammalian c-myc oncogenes. *Molecular and cellular biology*, **16**(6): 2802–2813.

- [57] Splinter E, Heath H, Kooren J, Palstra RJ, Klous P, Grosveld F, Galjart N, De Laat W (2006) CTCF mediates long-range chromatin looping and local histone modification in the ??-globin locus. *Genes and Development*, **20**(17): 2349–2354.
- [58] Phillips-Cremins JE, Sauria MEG, Sanyal A, Gerasimova TI, Lajoie BR, Bell JSK, Ong CT, Hookway Ta, Guo C, et al. (2013) Architectural Protein Subclasses Shape 3D Organization of Genomes during Lineage Commitment. *Cell*, **153**(6): 1281–95.
- [59] Gómez-Díaz E, Corces VG (2014) Architectural proteins: regulators of 3D genome organization in cell fate. *Trends in Cell Biology*, **24**(11): 703–711.
- [60] Nichols M, Corces V (2015) A CTCF Code for 3D Genome Architecture. *Cell*, **162**(4): 703–705.
- [61] Van Bortle K, Nichols MH, Li L, Ong CT, Takenaka N, Qin ZS, Corces VG (2014) Insulator function and topological domain border strength scale with architectural protein occupancy. *Genome biology*, **15**(5): R82.
- [62] Naumova N, Imakaev M, Fudenberg G, Zhan Y, Lajoie BR, Mirny La, Dekker J (2013) Organization of the mitotic chromosome. *Science (New York, N.Y.)*, **342**(6161): 948–53.
- [63] Dekker J (2014) Two ways to fold the genome during the cell cycle : insights obtained with chromosome conformation capture. *7*(1): 1–12.
- [64] Splinter E, de Wit E, Nora EP, Klous P, van de Werken HJG, Zhu Y, Kaaij LJT, van Ijcken W, Gribnau J, et al. (2011) The inactive X chromosome adopts a unique three-dimensional conformation that is dependent on Xist RNA. *Genes & development*, **25**(13): 1371–83.
- [65] Burton JN, Liachko I, Dunham MJ, Shendure J (2014) Species-Level Deconvolution of Metagenome Assemblies with Hi-C-Based Contact Probability Maps. *G3 (Bethesda, Md.)*, **4**(July): 1339–1346.
- [66] Beitel CW, Froenicke L, Lang JM, Korf IF, Michelmore RW, Eisen Ja, Darling AE (2014) Strain- and plasmid-level deconvolution of a synthetic metagenome by sequencing proximity ligation products. *PeerJ*, **2**: e415.
- [67] Williamson I, Berlivet S, Eskeland R, Boyle S, Illingworth RS, Paquette D, Bickmore WA (2014) Spatial genome organization: contrasting views from chromosome conformation capture and fluorescence in situ hybridization. pp. 2778–2791.
- [68] Shavit Y, Hamey FK, Lio' P (2014) FisHiCal: an R package for iterative FISH-based calibration of Hi-C data. *Bioinformatics (Oxford, England)*, pp. btu491–.

- [69] Gavrilov Aa, Golov AK, Razin SV (2013) Actual ligation frequencies in the chromosome conformation capture procedure. *PLoS one*, **8**(3): e60403.
- [70] Jordan MI, Mitchell TM (2015) Machine learning: Trends, perspectives, and prospects. *Science*, **349**(6245): 255–260.
- [71] Libbrecht MW, Noble WS (2015) Machine learning applications in genetics and genomics. *Nature Reviews Genetics*, **16**(6): 321–332.
- [72] Feingold E, Good P, Guyer M, Kamholz S, Liefer L, Wetterstrand K, Collins F, Gingeras T, Kampa D, et al. (2004) The ENCODE (ENCylopedia of DNA elements) Project.
- [73] Qu H, Fang X (2013) A Brief Review on the Human Encyclopedia of DNA Elements (ENCODE) Project. *Genomics, Proteomics and Bioinformatics*, **11**(3): 135–141.
- [74] ENCODE (2012) An integrated encyclopedia of DNA elements in the human genome. *Nature*, **489**(7414): 57–74.
- [75] Myers RM, Stamatoyannopoulos J, Snyder M, Dunham I, Hardison RC, Bernstein BE, Gingeras TR, Kent WJ, Birney E, et al. (2011) A user's guide to the Encyclopedia of DNA elements (ENCODE). *PLoS Biology*, **9**(4).
- [76] Landt S, Marinov G (2012) ChIP-seq guidelines and practices of the ENCODE and modENCODE consortia. *Genome* . . . , (Park 2009): 1813–1831.
- [77] Boyle AP, Araya CL, Brdlik C, Cayting P, Cheng C, Cheng Y, Gardner K, Hillier LW, Janette J, et al. (2014) Comparative analysis of regulatory information and circuits across distant species. *Nature*, **512**(7515): 453–456.
- [78] Marinov GK, Kundaje A, Park PJ, Wold BJ (2013) Large-Scale Quality Analysis of Published ChIP-seq Data. *G3 (Bethesda, Md.)*, **4**(February): 209–223.
- [79] Yue F, Cheng Y, Breschi A, Vierstra J, Wu W, Ryba T, Sandstrom R, Ma Z, Davis C, et al. (2014) A comparative encyclopedia of DNA elements in the mouse genome. *Nature*, **515**(7527): 355–364.
- [80] Ho JWK, Jung YL, Liu T, Alver BH, Lee S, Ikegami K, Sohn KA, Minoda A, Tolstorukov MY, et al. (2014) Comparative analysis of metazoan chromatin organization. *Nature*, **512**(7515): 449–452.
- [81] ENCODE DCC (2015) Encode news, may 13 2015. <https://www.encodeproject.org/news/>. Accessed: 2015-07-29.
- [82] Hoffman MM, Buske OJ, Wang J, Weng Z, Bilmes Ja, Noble WS (2012) Unsupervised pattern discovery in human chromatin structure through genomic segmentation. *Nature Methods*, **9**(5): 473–476.

- [83] Ernst J, Kheradpour P, Mikkelsen TS, Shores N, Ward LD, Epstein CB, Zhang X, Wang L, Issner R, et al. (2011) Mapping and analysis of chromatin state dynamics in nine human cell types. *Nature*, **473**(7345): 43–9.
- [84] Ernst J, Kellis M (2012) ChromHMM: automating chromatin-state discovery and characterization. *Nature methods*, **9**(3): 215–6.
- [85] Ernst J, Kellis M (2010) Discovery and characterization of chromatin states for systematic annotation of the human genome. *Nature biotechnology*, **28**(8): 817–825.
- [86] Hoffman MM, Ernst J, Wilder SP, Kundaje A, Harris RS, Libbrecht M, Giardine B, Ellenbogen PM, Bilmes Ja, et al. (2013) Integrative annotation of chromatin elements from ENCODE data. *Nucleic acids research*, **41**(2): 827–41.
- [87] Kwasnieski JC, Fiore C, Chaudhari HG, Cohen Ba (2014) High-throughput functional testing of ENCODE segmentation predictions. *Genome Research*.
- [88] Cheng C, Yan Kk, Yip KY, Rozowsky J, Alexander R, Shou C, Gerstein M (2011) A statistical framework for modeling gene expression using chromatin features and application to modENCODE datasets. *Genome biology*, **12**(2): R15.
- [89] Althammer S, Pagès A, Eyras E (2012) Predictive models of gene regulation from high-throughput epigenomics data. *Comparative and functional genomics*, **2012**: 1–13.
- [90] Cheng C, Ung M, Grant GD, Whitfield ML (2013) Transcription Factor Binding Profiles Reveal Cyclic Expression of Human Protein-coding Genes and Non-coding RNAs. *PLoS Computational Biology*, **9**(7).
- [91] Rajagopal N, Xie W, Li Y, Wagner U, Wang W, Stamatoyannopoulos J, Ernst J, Kellis M, Ren B (2013) RFECS: a random-forest based algorithm for enhancer identification from chromatin state. *PLoS computational biology*, **9**(3): e1002968.
- [92] Dong X, Greven MC, Kundaje A, Djebali S, Brown JB, Cheng C, Gingeras TR, Gerstein M, Guigó R, et al. (2012) Modeling gene expression using chromatin features in various cellular contexts. *Genome biology*, **13**(9): R53.
- [93] Barrett T, Wilhite SE, Ledoux P, Evangelista C, Kim IF, Tomashevsky M, Marshall Ka, Phillippy KH, Sherman PM, et al. (2013) NCBI GEO: archive for functional genomics data sets—update. *Nucleic acids research*, **41**(Database issue): D991–5.
- [94] Leinonen R, Sugawara H, Shumway M (2011) The sequence read archive. *Nucleic acids research*, **39**(Database issue): D19–21.
- [95] Langmead B, Salzberg SL (2012) Fast gapped-read alignment with Bowtie 2. *Nature methods*, **9**(4): 357–9.

- [96] Fortin JP, Hansen KD (2015) Reconstructing A/B compartments as revealed by Hi-C using long-range correlations in epigenetic data. *bioRxiv*, pp. 1–52.
- [97] Zhang Y, Liu T, Meyer Ca, Eeckhoute J, Johnson DS, Bernstein BE, Nusbaum C, Myers RM, Brown M, et al. (2008) Model-based analysis of ChIP-Seq (MACS). *Genome biology*, **9**(9): R137.
- [98] Suzuki R, Shimodaira H (2006) Pvclust: an R package for assessing the uncertainty in hierarchical clustering. *Bioinformatics (Oxford, England)*, **22**(12): 1540–2.
- [99] Breiman L (2001) Random Forests. *Machine learning*, **45**(1): 5–32.
- [100] Liaw A, Wiener M (2002) Classification and Regression by randomForest. *R News*, **2**(December): 18–22.
- [101] Svetnik V, Liaw A, Tong C, Culberson JC, Sheridan RP, Feuston BP (2003) Random forest: a classification and regression tool for compound classification and QSAR modeling. *Journal of chemical information and computer sciences*, **43**(6): 1947–58.
- [102] Cutler DR, Edwards TC, Beard KH, Cutler A, Hess KT, Gibson J, Lawler JJ (2007) Random forests for classification in ecology. *Ecology*, **88**(11): 2783–92.
- [103] Díaz-Uriarte R, Alvarez de Andrés S (2006) Gene selection and classification of microarray data using random forest. *BMC bioinformatics*, **7**: 3.
- [104] Dasgupta A, Sun YV, König IR, Bailey-Wilson JE, Malley JD (2011) Brief review of regression-based and machine learning methods in genetic epidemiology: the Genetic Analysis Workshop 17 experience. *Genetic epidemiology*, **35 Suppl 1**(Suppl 1): S5–11.
- [105] Breiman L (2001) Statistical Modeling: The Two Cultures. *Statistical Science*, **16**(3): 199–231.
- [106] Hastie T, Tibshirani R, Friedman J (2009) *Elements of Statistical Learning: Data Mining, Inference, and Prediction*. Springer, 2 edition. ISBN 978-0-387-84858-7.
- [107] Eddy SR (2004) What is a hidden Markov model? *Nature biotechnology*, **22**(10): 1315–1316.
- [108] Eddy SR (1996) Hidden Markov models. *Current opinion in structural biology*, **6**(3): 361–365.
- [109] Rabiner L (1989) A tutorial on hidden Markov models and selected applications in speech recognition. *Proceedings of the IEEE*, **77**(2): 257–286.

- [110] Vogl C, Futschik A (2010) Hidden Markov Models in Biology. In: O Carugo, F Eisenhaber, eds., *Energy*, Humana Press, volume oo, chapter 14, pp. 241–253. ISBN 038795399X.
- [111] Baum LE, Petrie T, Soules G, Weiss N (1970) A Maximization Technique Occurring in the Statistical Analysis of Probabilistic Functions of Markov Chains.
- [112] Ryan MS, Nudd GR (1993) The viterbi algorithm.
- [113] Mantel N (1970) Why Stepdown Procedures in Variable Selection. *Technometrics*, **12**(3): 621–625.
- [114] Hurvich CM, Tsai CL (1990) The Impact of Model Selection on Inference in Linear Regression. *The American Statistician*, **44**(3): 214.
- [115] Whittingham MJ, Stephens PA, Bradbury RB, Freckleton RP (2006) Why do we still use stepwise modelling in ecology and behaviour? *Journal of Animal Ecology*, **75**(5): 1182–1189.
- [116] Tibshirani R (1994) Regression Selection and Shrinkage via the Lasso.
- [117] Friedman J, Hastie T, Tibshirani R (2010) Regularization paths for generalized linear models via coordinate descent. *Journal of Statistical Software*, **33**(1): 1–22.
- [118] Simon N, Friedman J, Hastie T, Tibshirani R (2011) Regularization paths for cox's proportional hazards model via coordinate descent. *Journal of Statistical Software*, **39**(5): 1–13.
- [119] Tobias RD (1995) An Introduction to Partial Least Squares Regression. *Proc. Ann. SAS Users Group Int. Conf. 20th*, pp. 1250–1257.
- [120] Ashburner M, Ball CA, Blake JA, Botstein D, Butler H, Cherry JM, Davis AP, Dolinski K, Dwight SS, et al. (2000) Gene ontology: tool for the unification of biology. The Gene Ontology Consortium. *Nature genetics*, **25**(1): 25–29.
- [121] Huang BDW, Lempicki R (2008) Systematic and integrative analysis of large gene lists using DAVID bioinformatics resources. *Nature protocols*, **(301)**: 1–43.
- [122] Calle ML, Urrea V, Boulesteix AL, Malats N (2011) AUC-RF: A new strategy for genomic profiling with random forest. *Human Heredity*, **72**(2): 121–132.
- [123] Chen X, Ishwaran H (2012) Random forests for genomic data analysis. *Genomics*, **99**(6): 323–329.
- [124] De Maturana EL, Ye Y, Calle ML, Rothman N, Urrea V, Kogevinas M, Petrus S, Chanock SJ, Tardón A, et al. (2013) Application of multi-SNP approaches Bayesian LASSO and AUC-RF to detect main effects of inflammatory-gene variants associated with bladder cancer risk. *PLoS ONE*, **8**(12).

- [125] Consortium TF, Pmi R, Dgt C (2014) A promoter-level mammalian expression atlas. *Nature*, **507**(7493): 462–70.
- [126] Itoh M, Kojima M, Nagao-Sato S, Saijo E, Lassmann T, Kanamori-Katayama M, Kaiho A, Lizio M, Kawaji H, et al. (2012) Automated workflow for preparation of cDNA for cap analysis of gene expression on a single molecule sequencer. *PLoS ONE*, **7**(1).
- [127] Kodzius R, Kojima M, Nishiyori H, Nakamura M, Fukuda S, Tagami M, Sasaki D, Imamura K, Kai C, et al. (2006) CAGE: cap analysis of gene expression. *Nature methods*, **3**(3): 211–22.
- [128] Quinlan AR, Hall IM (2010) BEDTools: A flexible suite of utilities for comparing genomic features. *Bioinformatics*, **26**(6): 841–842.
- [129] Karolchik D, Barber GP, Casper J, Clawson H, Cline MS, Diekhans M, Dreszer TR, Fujita Pa, Guruvadoo L, et al. (2014) The UCSC Genome Browser database: 2014 update. *Nucleic Acids Research*, **42**(D1): 764–770.
- [130] Peric-Hupkes D, Meuleman W, Pagie L, Bruggeman SWM, Solovei I, Brugman W, Gräf S, Flück P, Kerkhoven RM, et al. (2010) Molecular Maps of the Reorganization of Genome-Nuclear Lamina Interactions during Differentiation. *Molecular Cell*, **38**(4): 603–613.
- [131] Furey TS (2003) Integration of the cytogenetic map with the draft human genome sequence. *Human Molecular Genetics*, **12**(9): 1037–1044.
- [132] Boyle S, Gilchrist S, Bridger JM, Mahy NL, Ellis Ja, Bickmore Wa (2001) The spatial organization of human chromosomes within the nuclei of normal and emerin-mutant cells. *Human molecular genetics*, **10**(3): 211–9.
- [133] Chambers EV, Bickmore Wa, Semple CA (2013) Divergence of mammalian higher order chromatin structure is associated with developmental loci. *PLoS computational biology*, **9**(4): e1003017.
- [134] de Wit E, Bouwman BaM, Zhu Y, Klous P, Splinter E, Versteegen MJaM, Krüger PHL, Festuccia N, Nora EP, et al. (2013) The pluripotent genome in three dimensions is shaped around pluripotency factors. *Nature*, pp. 1–7.
- [135] Tanabe H, Müller S, Neusser M, von Hase J, Calcagno E, Cremer M, Solovei I, Cremer C, Cremer T (2002) Evolutionary conservation of chromosome territory arrangements in cell nuclei from higher primates. *Proceedings of the National Academy of Sciences of the United States of America*, **99**(7): 4424–9.

- [136] Stadhouders R, Kolovos P, Brouwer R, Zuin J, van den Heuvel A, Kockx C, Palstra RJ, Wendt KS, Grosveld F, *et al.* (2013) Multiplexed chromosome conformation capture sequencing for rapid genome-scale high-resolution detection of long-range chromatin interactions. *Nature protocols*, **8**(3): 509–24.
- [137] Thongjuea S, Stadhouders R, Grosveld FG, Soler E, Lenhard B (2013) R3Cseq: An R/Bioconductor package for the discovery of long-range genomic interactions from chromosome conformation capture and next-generation sequencing data. *Nucleic Acids Research*, **41**(13): 1–12.
- [138] Gentleman RC, Gentleman RC, Carey VJ, Carey VJ, Bates DM, Bates DM, Bolstad B, Bolstad B, Dettling M, *et al.* (2004) Bioconductor: open software development for computational biology and bioinformatics. *Genome biology*, **5**(10): R80.
- [139] Huber W, Carey VJ, Gentleman R, Anders S, Carlson M, Carvalho BS, Bravo HC, Davis S, Gatto L, *et al.* (2015) Orchestrating high-throughput genomic analysis with Bioconductor. *Nature Publishing Group*, **12**(2): 115–121.
- [140] Ihaka R, Gentleman R (1996) R: A Language for Data Analysis and Graphics.
- [141] Balwierz PJ, Carninci P, Daub CO, Kawai J, Hayashizaki Y, Van Belle W, Beisel C, van Nimwegen E (2009) Methods for analyzing deep sequencing expression data: constructing the human and mouse promoterome with deepCAGE data. *Genome biology*, **10**(7): R79.
- [142] Ay F, Bailey TL, Noble WS (2014) Statistical confidence estimation for Hi-C data reveals regulatory chromatin contacts. *Genome Research*.
- [143] Storey JD, Taylor JE, Siegmund D (2004) Strong control, conservative point estimation and simultaneous conservative consistency of false discovery rates: A unified approach. *Journal of the Royal Statistical Society. Series B: Statistical Methodology*, **66**(1): 187–205.
- [144] Storey J (2015) *qvalue: Q-value estimation for false discovery rate control*. R package version 2.0.0.
- [145] Splinter E, de Wit E, van de Werken HJG, Klous P, de Laat W (2012) Determining long-range chromatin interactions for selected genomic sites using 4C-seq technology: From fixation to computation. *Methods*, **58**(3): 221–230.
- [146] Gao F, Wei Z, Lu W, Wang K (2013) Comparative analysis of 4C-Seq data generated from enzyme-based and sonication-based methods. *BMC genomics*, **14**(1): 345.
- [147] Dixon JR, Jung I, Selvaraj S, Shen Y, Antosiewicz-Bourget JE, Lee AY, Ye Z, Kim A, Rajagopal N, *et al.* (2015) Chromatin architecture reorganization during stem cell differentiation. *Nature*, **518**(7539): 331–336.

- [148] Wickham H (2009) *ggplot2: elegant graphics for data analysis*. Springer New York. ISBN 978-0-387-98140-6.
- [149] Wickham H, Francois R (2015) *dplyr: A Grammar of Data Manipulation*. R package version 0.4.2.
- [150] Van Rossum G (1995) *Python reference manual*.
- [151] Li H, Handsaker B, Wysoker A, Fennell T, Ruan J, Homer N, Marth G, Abecasis G, Durbin R (2009) The Sequence Alignment/Map format and SAMtools. *Bioinformatics*, **25**(16): 2078–2079.
- [152] Kent WJ, Zweig aS, Barber G, Hinrichs aS, Karolchik D (2010) BigWig and BigBed: Enabling browsing of large distributed datasets. *Bioinformatics*, **26**(17): 2204–2207.
- [153] Kent WJ, Sugnet CW, Furey TS, Roskin KM, Pringle TH, Zahler AM, Haussler D (2002) The Human Genome Browser at UCSC The Human Genome Browser at UCSC. *Genome Research*, pp. 996–1006.
- [154] Raney BJ, Dreszer TR, Barber GP, Clawson H, Fujita Pa, Wang T, Nguyen N, Paten B, Zweig AS, et al. (2014) Track data hubs enable visualization of user-defined genome-wide annotations on the UCSC Genome Browser. *Bioinformatics*, **30**(7): 1003–1005.
- [155] Kuhn RM, Haussler D, James Kent W (2013) The UCSC genome browser and associated tools. *Briefings in Bioinformatics*, **14**(2): 144–161.
- [156] Hu G, Cui K, Northrup D, Liu C, Wang C, Tang Q, Ge K, Levens D, Crane-Robinson C, Zhao K (2013) H2A.Z facilitates access of active and repressive complexes to chromatin in embryonic stem cell self-renewal and differentiation. *Cell Stem Cell*, **12**(2): 180–192.
- [157] Li Z, Gadue P, Chen K, Jiao Y, Tuteja G, Schug J, Li W, Kaestner KH (2012) Foxa2 and H2A.Z mediate nucleosome depletion during embryonic stem cell differentiation. *Cell*, **151**(7): 1608–1616.
- [158] Huang DW, Sherman BT, Lempicki Ra (2009) Bioinformatics enrichment tools: paths toward the comprehensive functional analysis of large gene lists. *Nucleic acids research*, **37**(1): 1–13.
- [159] Lozzio BB, Lozzio CB, Bamberger EG, Feliu AS (1981) A multipotential leukemia cell line (k-562) of human origin. *Experimental Biology and Medicine*, **166**(4): 546–550.
- [160] Bickmore Wa (2013) The spatial organization of the human genome. *Annual review of genomics and human genetics*, **14**: 67–84.

- [161] Bernstein BE, Stamatoyannopoulos Ja, Costello JF, Ren B, Milosavljevic A, Meissner A, Kellis M, Marra Ma, Beaudet AL, et al. (2010) The NIH Roadmap Epigenomics Mapping Consortium. *Nature biotechnology*, **28**(10): 1045–8.
- [162] Tippmann SC, Ivanek R, Gaidatzis D, Schöler A, Hoerner L, van Nimwegen E, Stadler PF, Stadler MB, Schübeler D (2012) Chromatin measurements reveal contributions of synthesis and decay to steady-state mRNA levels. *Molecular systems biology*, **8**(593): 593.
- [163] McLeay RC, Lesluyes T, Cuellar Partida G, Bailey TL (2012) Genome-wide in silico prediction of gene expression. *Bioinformatics*, **28**(21): 2789–96.
- [164] Shiraki T, Kondo S, Katayama S, Waki K, Kasukawa T, Kawaji H, Kodzius R, Watahiki A, Nakamura M, et al. (2003) Cap analysis gene expression for high-throughput analysis of transcriptional starting point and identification of promoter usage. *Proceedings of the National Academy of Sciences of the United States of America*, **100**(26): 15776–81.
- [165] Kolasinska-Zwierz P, Down T, Latorre I, Liu T, Liu XS, Ahringer J (2009) Differential chromatin marking of introns and expressed exons by H3K36me3. *Nature genetics*, **41**(3): 376–81.
- [166] Schaft D (2003) The histone 3 lysine 36 methyltransferase, SET2, is involved in transcriptional elongation. *Nucleic Acids Research*, **31**(10): 2475–2482.
- [167] Zuber V, Strimmer K (2011) High-Dimensional Regression and Variable Selection Using CAR Scores. *Statistical Applications in Genetics and Molecular Biology*, **10**(1): 1–27.
- [168] Ryba T, Hiratani I, Lu J, Itoh M, Kulik M, Zhang J, Schulz TC, Robins AJ, Dalton S, Gilbert DM (2010) Evolutionarily conserved replication timing profiles predict long-range chromatin interactions and distinguish closely related cell types. *Genome research*, **20**(6): 761–70.
- [169] Breiman L (2001) Random forests. *Machine learning*, **45**: 5–32.
- [170] Beringer M, Ballar C, Croce LD, Viz P (2015) Role of PRC2-associated factors in stem cells and disease. *282*: 1723–1735.
- [171] Creyghton MP, Markoulaki S, Levine SS, Hanna J, Lodato Ma, Sha K, Young Ra, Jaenisch R, Boyer La (2008) H2AZ Is Enriched at Polycomb Complex Target Genes in ES Cells and Is Necessary for Lineage Commitment. *Cell*, **135**(4): 649–661.
- [172] Deb G, Singh AK, Gupta S (2014) EZH2: Not EZHY (Easy) to Deal. *Molecular cancer research : MCR*, **12**(5): 639–53.

- [173] Nie Z, Hu G, Wei G, Cui K, Yamane A, Resch W, Wang R, Green DR, Tessarollo L, *et al.* (2012) c-Myc is a universal amplifier of expressed genes in lymphocytes and embryonic stem cells. *Cell*, **151**(1): 68–79.
- [174] Kieffer-Kwon KR, Tang Z, Mathe E, Qian J, Sung MH, Li G, Resch W, Baek S, Pruett N, *et al.* (2013) Interactome maps of mouse gene regulatory domains reveal basic principles of transcriptional regulation. *Cell*, **155**(7): 1507–20.
- [175] Zervos AS, Gyuris J, Brent R (1993) Mxi1, a protein that specifically interacts with Max to bind Myc-Max recognition sites. *Cell*, **72**(2): 223–232.
- [176] Sun XJ, Man N, Tan Y, Nimer SD, Wang L (2015) The Role of Histone Acetyltransferases in Normal and Malignant Hematopoiesis. *Frontiers in Oncology*, **5**(May): 1–11.
- [177] Handoko L, Xu H, Li G, Ngan CY, Chew E, Schnapp M, Lee CWH, Ye C, Ping JLH, *et al.* (2011) CTCF-mediated functional chromatin interactome in pluripotent cells. *Nature genetics*, **43**(7): 630–8.
- [178] Abdi H, Williams LJ (2010) Principal component analysis. *Wiley Interdisciplinary Reviews: Computational Statistics*, **2**(4): 433–459.
- [179] Kerppola TK, Curran T (1993) Selective DNA bending by a variety of bZIP proteins. *Molecular and cellular biology*, **13**(9): 5479–5489.
- [180] Heidari N, Phanstiel DH, He C, Grubert F, Jahanbanian F, Kasowski M, Zhang MQ, Snyder MP (2014) Genome-wide map of regulatory interactions in the human genome. *Genome Research*.
- [181] Guyon I, Weston J, Barnhill S, Vapnik V (2003) An Introduction to Variable and Feature Selection. *Journal of Machine Learning Research*, **3**: 1157–1182.
- [182] Kohavi R, Kohavi R (1997) Wrappers for feature subset selection. *Artificial Intelligence*, **97**(1-2): 273–324.
- [183] Deng H, Runger G (2012) Feature selection via regularized trees. In: *Neural Networks (IJCNN), The 2012 International Joint Conference on*. IEEE, pp. 1–8.
- [184] Deng H, Runger G (2013) Gene selection with guided regularized random forest. *Pattern Recognition*, **46**(12): 3483–3489.
- [185] Nora EP, Dekker J, Heard E (2013) Segmental folding of chromosomes: A basis for structural and regulatory chromosomal neighborhoods? *BioEssays*, **35**(9): 818–828.
- [186] Lupiáñez D, Kraft K, Heinrich V, Krawitz P, Brancati F, Klopocki E, Horn D, Kayserili H, Opitz J, *et al.* (2015) Disruptions of Topological Chromatin Domains Cause Pathogenic Rewiring of Gene-Enhancer Interactions. *Cell*, pp. 1012–1025.

- [187] Ren B, Dixon J (2015) A CRISPR Connection between Chromatin Topology and Genetic Disorders. *Cell*, **161**(5): 955–957.
- [188] Evertts AG, Manning AL, Wang X, Dyson NJ, Garcia Ba, Coller Ha (2013) H4K20 methylation regulates quiescence and chromatin compaction. *Molecular biology of the cell*, **24**(19): 3025–37.
- [189] Onder TT, Kara N, Cherry A, Sinha AU, Zhu N, Bernt KM, Cahan P, Marcarci BO, Unternaehrer J, et al. (2012) Chromatin-modifying enzymes as modulators of reprogramming. *Nature*, **483**(7391): 598–602.
- [190] Chai X, Nagarajan S, Kim K, Lee K, Choi JK (2013) Regulation of the boundaries of accessible chromatin. *PLoS genetics*, **9**(9): e1003778.
- [191] Ku M, Jaffe JD, Koche RP, Rheinbay E, Endoh M, Koseki H, Carr SA, Bernstein BE (2012) H2A.Z landscapes and dual modifications in pluripotent and multipotent stem cells underlie complex genome regulatory functions. *Genome biology*, **13**(10): R85.
- [192] Atchison ML (2014) Function of YY1 in Long-Distance DNA Interactions. *Frontiers in immunology*, **5**(February): 45.
- [193] Schwalie PC, Ward MC, Cain CE, Faure AJ, Gilad Y, Odom DT, Fliceck P (2013) Co-binding by YY1 identifies the transcriptionally active, highly conserved set of CTCF-bound regions in primate genomes. *Genome biology*, **14**(12): R148.
- [194] Seitan VC, Faure AJ, Zhan Y, McCord RP, Lajoie BR, Ing-Simmons E, Lenhard B, Giorgetti L, Heard E, et al. (2013) Cohesin-based chromatin interactions enable regulated gene expression within preexisting architectural compartments. *Genome research*, **23**(12): 2066–77.
- [195] Lunyak VV, Prefontaine GG, Núñez E, Cramer T, Ju BG, Ohgi KA, Hutt K, Roy R, García-Díaz A, et al. (2007) Developmentally regulated activation of a SINE B2 repeat as a domain boundary in organogenesis. *Science (New York, N.Y.)*, **317**(5835): 248–251.
- [196] Schmidt D, Schwalie PC, Wilson MD, Ballester B, Gonçalves A, Kutter C, Brown GD, Marshall A, Fliceck P, Odom DT (2012) Waves of retrotransposon expansion remodel genome organization and CTCF binding in multiple mammalian lineages. *Cell*, **148**(1-2): 335–348.
- [197] Tarailo-Graovac M, Chen N (2009) Using RepeatMasker to identify repetitive elements in genomic sequences. *Current Protocols in Bioinformatics*, (SUPPL. 25).
- [198] Fawcett T (2006) An introduction to ROC analysis. *Pattern Recognition Letters*, **27**(8): 861–874.

- [199] Streiner DL, Cairney J (2007) What's under the ROC? An introduction to receiver operating characteristics curves. *Canadian Journal of Psychiatry*, **52**(2): 121–128.
- [200] Pickersgill H, Kalverda B, de Wit E, Talhout W, Fornerod M, van Steensel B (2006) Characterization of the *Drosophila melanogaster* genome at the nuclear lamina. *Nature genetics*, **38**(9): 1005–1014.
- [201] Anderson E, Devenney PS, Hill RE, Lettice La (2014) Mapping the Shh long-range regulatory domain. *Development (Cambridge, England)*, (September): 1–10.
- [202] Anderson E, Peluso S, Lettice La, Hill RE (2012) Human limb abnormalities caused by disruption of hedgehog signaling. *Trends in Genetics*, **28**(8): 364–373.
- [203] Hill RE, Lettice La, B PTRS (2013) Alterations to the remote control of Shh gene expression cause congenital abnormalities Alterations to the remote control of Shh gene expression cause congenital abnormalities Author for correspondence .. (May).
- [204] Laurell T, Vandermeer JE, Wenger AM, Grigelioniene G, Nordenskjöld A, Arner M, Ekblom AG, Bejerano G, Ahituv N, Nordgren A (2012) A novel 13 base pair insertion in the sonic hedgehog ZRS limb enhancer (ZRS/LMBR1) causes preaxial polydactyly with triphalangeal thumb. *Human Mutation*, **33**(7): 1063–1066.
- [205] Lettice La, Hill AE, Devenney PS, Hill RE (2008) Point mutations in a distant sonic hedgehog cis-regulator generate a variable regulatory output responsible for preaxial polydactyly. *Human Molecular Genetics*, **17**(7): 978–985.
- [206] Bouwman BA, de Laat W (2015) Getting the genome in shape: the formation of loops, domains and compartments. *Genome Biology*, **16**(1): 154.
- [207] Martin M (2011) Cutadapt removes adapter sequences from high-throughput sequencing reads. *EMBnet.journal*, **17**(1): 10–12.
- [208] Andrews S (2015) FastQC (vo.10.1): A quality control tool for high throughput sequence data.
- [209] Lin YC, Benner C, Mansson R, Heinz S, Miyazaki K, Miyazaki M, Chandra V, Bossen C, Glass CK, Murre C (2012) Global changes in the nuclear positioning of genes and intra- and interdomain genomic interactions that orchestrate B cell fate. *Nature immunology*, **13**(12): 1196–204.
- [210] Baù D, Sanyal A, Lajoie BR, Capriotti E, Byron M, Lawrence JB, Dekker J, Marti-Renom Ma (2011) The three-dimensional folding of the α -globin gene domain reveals formation of chromatin globules. *Nature structural & molecular biology*, **18**(1): 107–114.

- [211] Hu M, Deng K, Qin Z, Dixon J, Selvaraj S, Fang J, Ren B, Liu JS (2013) Bayesian inference of spatial organizations of chromosomes. *PLoS computational biology*, **9**(1): e1002893.
- [212] Varoquaux N, Ay F, Noble WS, Vert Jp (2014) A statistical approach for inferring the 3D structure of the genome. *Bioinformatics (Oxford, England)*, **30**(12): i26–i33.
- [213] Lesne A, Riposo J, Roger P, Cournac A, Mozziconacci J (2014) 3D genome reconstruction from chromosomal contacts. *Nature methods*, (september).
- [214] Trieu T, Cheng J (2014) Large-scale reconstruction of 3D structures of human chromosomes from chromosomal contact data. *Nucleic Acids Research*, **42**(7): 1–11.
- [215] Peng C, Fu LY, Dong PF, Deng ZL, Li JX, Wang XT, Zhang HY (2013) The sequencing bias relaxed characteristics of Hi-C derived data and implications for chromatin 3D modeling. *Nucleic Acids Research*, **41**(19).
- [216] Ay F, Bunnik EM, Varoquaux N, Bol SM, Prudhomme J, Vert JP, Noble WS, Le Roch KG (2014) Three-dimensional modeling of the *P. falciparum* genome during the erythrocytic cycle reveals a strong connection between genome architecture and gene expression. *Genome research*.
- [217] Caudai C, Salerno E, Zoppè M, Tonazzini A (2015) Inferring 3D chromatin structure using a multiscale approach based on quaternions. *BMC Bioinformatics*, **16**(1): 234.
- [218] LINDO (2015) LINGO (v15.0): Optimization modeling software for linear, non-linear, and integer programming.
- [219] Lajoie BR, van Berkum NL, Sanyal A, Dekker J (2009) My5C: web tools for chromosome conformation capture studies. *Nature methods*, **6**(10): 690–691.
- [220] Ram O, Goren A, Amit I, Shores N, Yosef N, Ernst J, Kellis M, Gymrek M, Issner R, et al. (2011) Combinatorial patterning of chromatin regulators uncovered by genome-wide location analysis in human cells. *Cell*, **147**(7): 1628–39.
- [221] Kundaje A, Meuleman W, Ernst J, Bilenky M, Yen A, Heravi-Moussavi A, Kheradpour P, Zhang Z, Wang J, et al. (2015) Integrative analysis of 111 reference human epigenomes. *Nature*, **518**(7539): 317–330.
- [222] Li G, Ruan X, Auerbach RK, Sandhu KS, Zheng M, Wang P, Poh HM, Goh Y, Lim J, et al. (2012) Extensive promoter-centered chromatin interactions provide a topological basis for transcription regulation. *Cell*, **148**(1-2): 84–98.

- [223] Nikolaev LG, Akopov SB, Didych Da, Sverdlov ED (2009) Vertebrate Protein CTCF and its Multiple Roles in a Large-Scale Regulation of Genome Activity. *Current genomics*, **10**(5): 294–302.
- [224] Giorgetti L, Galupa R, Nora EP, Piolot T, Lam F, Dekker J, Tiana G, Heard E (2014) Predictive polymer modeling reveals coupled fluctuations in chromosome conformation and transcription. *Cell*, **157**(4): 950–963.
- [225] Kim J, Kim H (2012) Recruitment and biological consequences of histone modification of H₃K₂₇me₃ and H₃K₉me₃. *ILAR journal / National Research Council, Institute of Laboratory Animal Resources*, **53**(3-4): 232–9.
- [226] Karimi MM, Goyal P, Maksakova Ia, Bilenky M, Leung D, Tang JX, Shinkai Y, Mager DL, Jones S, et al. (2011) DNA methylation and SETDB1/H₃K₉me₃ regulate predominantly distinct sets of genes, retroelements, and chimeric transcripts in mescs. *Cell Stem Cell*, **8**(6): 676–687.