# 1 | LOCAL CHROMATIN CONFORMATION

#### 1.1 INTRODUCTION

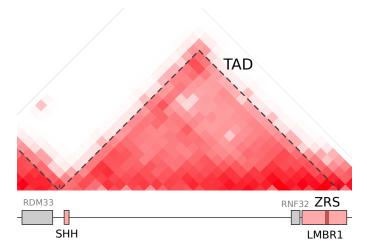
The Hi-C assay provides a genome-wide overview of chromatin conformation, however this broad scope imposes resolution limits inherent to an all-vs-all assay. For a closer look at chromatin conformation within a region of interest, alternative C-based assays such as 3C, 4C and 5C can be employed alongside classical microscopy techniques like FISH.

Here I discuss a collaborative project involving the use of 4C and 5C data to "zoom in" on a well-studied locus involved in limb development: the Sonic Hedgehog (*Shh*) gene and its distal *cis*-regulatory element named ZRS.

#### 1.2 THE SHH LOCUS

Anterior-posterior patterning in the developing limb is regulated in mammals by Sonic Hedgehog (*Shh*). [3] Specifically, the *Shh* gene is expressed within a confined region named the "zone of polarising activity". Its expression within this region is known to be regulated by a well-studied enhancer, the "zone of polarising activity regulatory sequence" or ZRS. [4] ZRS is located almost 1 Mb downstream of its target SHH promoter in humans, and is located in intronic regions of another gene, LMBR1 (Fig. 1). [4,5] Expression of *Shh* within the ZPA is tightly controlled, initiating in mice at developmental stage E9.5 and terminating at E12.5. [6] As such, single point mutations and short insertions within the ZRS enhancer have been linked to various limb deformities, including pre- and post-axial polydactyly. [3,5,7] For example, a heritable point mutation in the ZRS enhancer is the cause of polydactyly in "Hemingway cats", a large group of domestic cats with extra toes that reside at the former home of Ernest Hemingway. [7,8]

To further investigate the dynamics of the *Shh* locus, our collaborators in the Hill lab (University of Edinburgh) have developed a model system which allows inducible *Shh* expression in a non-expressing 14fp cell line derived from the developing limb bud. Treatment of this cell line with the histone deacetylase inhibitor trichostatin A (TSA) then leads to detectable *Shh* expression, and increased levels of the histone activation mark H<sub>3</sub>K<sub>2</sub>7ac at the ZRS (*unpublished data*). However, the question remains whether this TSA treatment is fundamentally altering local chromatin structure—that is, bringing together the ZRS enhancer with its target *Shh* promoter—or whether ZRS



**Figure 1: SHH–ZRS contacts occur within a stable TAD.** An approximately 1 Mb region of the mouse genome is shown below a Hi-C contact map (derived from previously published data  $^{[1]}$ ). A clear TAD can be identified spanning from SHH to ZRS, dashed lines show TAD boundaries called by Dixon *et al.*  $^{[1]}$ . This figure was generated for Anderson *et al.*  $^{[2]}$ .

and *Shh* are in contact in both the active and non-expressing cell lines in a poised state. Previous 3D-FISH experiments have shown *Shh*–ZRS contact to be associated with *Shh* expression in the developing limb bud, though it is not detected in every cell. <sup>[4,6]</sup> Instead only a proportion of cells in the ZPA are *Shh*-expressing at a given time, and it is within these expressing cells where *Shh*–ZRS colocalisation is most likely. <sup>[6]</sup>

My part in this collaboration was to analyse 3C-seq (also known as 4C), then 5C data generated by our collaborators over the *Shh*–ZRS region in mouse. Experimental design and wet-lab procedures were performed by members of the Hill lab.

# 1.3 4C AT THE shh LOCUS

# 1.3.1 4C pipeline

The 4C analysis pipeline, starting from de-multiplexed fastq files as produced by our in-house sequencing facilities, can be summarised as:

- 1. Trim known bait sequence using cutadapt, [9] select only those reads where known sequence was present
- 2. Map reads to reference genome mm9 using bowtie2<sup>[10]</sup> with the very-sensitive flag
- Filter alignments with a MAPQ score > 30 to select for high-confidence alignments using samtools<sup>[11]</sup>
- 4. Normalise and analyse contacts using the r3cseq R package (Methods ??)

# 1.3.2 ZRS-Shh interaction following TSA treatment

4C experiments were performed by collaborators using the ZRS region as a bait sequence, or "viewpoint", such that it contacts were measured with all other HindIII restriction fragments genome-wide. The experimental design, again generated entirely by collaborators, involved two control experiments. The first used cells derived from whole limb bud at developmental stage E11.5, thereby containing some *Shh* expressing cells as a positive control. The negative control was a mouse mandibular cell line (MD) which does not express *Shh*. 4C was then also performed in the *Shh*-inducible 14fp cell line, both with and without trichostatin A (TSA) treatment.

The first stage in analysing these contacts is to convert observed raw sequencing reads to normalised frequencies (Methods ??), these normalised values are then assigned significance scores in the form of *q*-values, with the aim of finding those significantly over-represented relative to expectation (Methods ??).

The results of a comparison between TSA treated and untreated samples is shown in Figure 2. In it we see a striking and highly significant ZRS–SHH contact in the treated sample (q-value  $< 5 \times 10^{-10}$ ), with a weaker but still significant contact in the adjacent restriction fragment in the untreated sample (q-value  $< 5 \times 10^{-5}$ ).

# 1.3.3 Comparison with controls

Comparing these results with controls shows a constitutive *Shh*–ZRS contact in each case, regardless of *Shh* expression status (Fig. 3). This is in agreement with previous evidence suggesting ZRS contacts *Shh* constitutively. [12] REF XX However the TSA–14fp cell line shows a large number of off-target contacts, potentially indicating many spurious contacts across the cell population.

Existing multi-probe FISH data produced by our collaborators shows approximately equal levels of compaction in this region in both TSA treated and untreated cells (*data not shown*). This information in combination with the 4C results reported here (Fig. 2) support a hypothesis that while both samples are held together in a TAD (Fig. 1) — unavoidably inducing many contacts — it is only in the treated sample where a highly-specific ZRS–SHH contact occurs and potentially is then bring about expression of the *Shh* gene.

# 1.3.4 4C time series

We also see more broadly a much higher total number of significant contacts in the untreated sample around the viewpoint (Fig. 4). In the treated samples, only a few contacts cross the stringent *q*-value threshold, with the SHH–ZRS contact among the

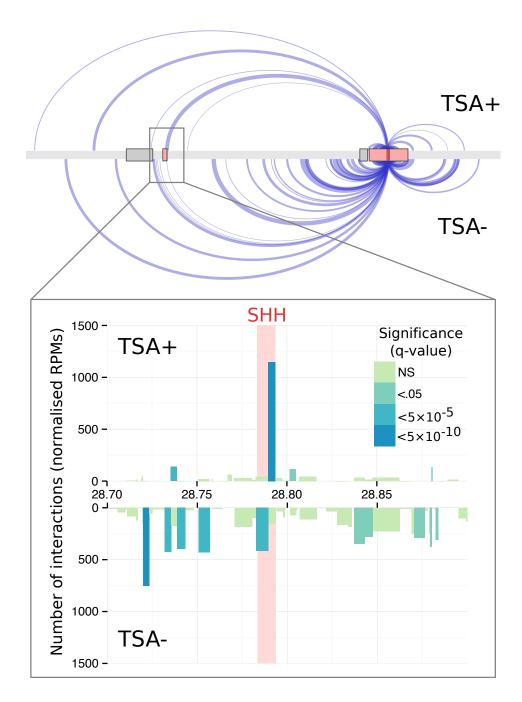


Figure 2: TSA treatment induces a strong ZRS–SHH interaction.  $_4$ C interactions are shown as edges from source node (ZRS enhancer bait fragment) to targets along an approximately 2 Mb region of chromosome 5. Edge width is proportional to the number of interactions, only highly significant interactions are shown (FDR  $_4$ -value  $< 5 \times 10^{-5}$ ). Zoomed region shows the number of interactions of the bait region with SHH in both untreated and TSA treated (after 18h) samples. Each rectangle is a restriction fragment, coloured by FDR  $_4$ -value indicating the significance of the interaction above expected levels.

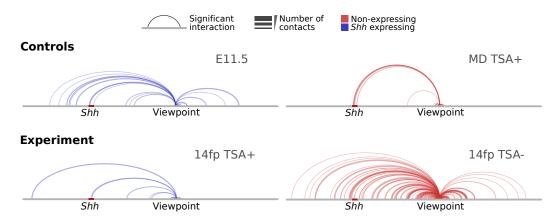


Figure 3: TSA treatment in 14fp cells results in a more specific ZRS–Shh contact. Are plots are shown for two control experiments: the Shh expressing E11.5 whole limb bud and non-expressing mandibular cell line (MD). Also shown is the 14fp inducible cell line, with and without treatment with trichostatin A (TSA) after 18 hours. Arcs link significant interactions (q-value < 0.05) and arc widths are proportional to the normalised number of reads recorded for the interaction (Methods ??).

most significant in terms of both q-value and supporting number of reads (indicated by the thickness of the arc, Figs. 2, 4).

ChIP-seq experiments performed by our collaborators show an increase in the H<sub>3</sub>K<sub>2</sub>7ac histone mark over ZRS following TSA treatment which peaks after 24 hours, but starts to increase after around 16 (*data not shown*).

### 1.3.5 Assay diagnostics

The 4C protocol used by our collaborators in this work was that of Stadhouders *et al.*<sup>[13]</sup>. In it, the authors advise some statistical tests to ensure the quality of the experiment results. Among these were:<sup>[13]</sup>

- 1. Sequencing reads should be found to have high duplication rates of 95% or greater.
- 2. 50% or more of all reads should map to the chromosome on which the bait region is located.

Additionally, the 4C procedure<sup>[13]</sup> was adapted for specific in-house sequencing instruments (an Ion Torrent Ion Proton<sup>TM</sup> sequencer as opposed to Illumina<sup>TM</sup> technology) and as such required diagnostics to confirm the experimental data was accurate.

Sequence duplication levels were measured with FastQC<sup>[14]</sup> and are shown in Table 1. We find slightly lower than expected levels of duplication, ranging from 62.8% to 84.4%. This suggests that while the assay does appear to be working, there may be extraneous noise and non-bait interactions in the sequencing library.

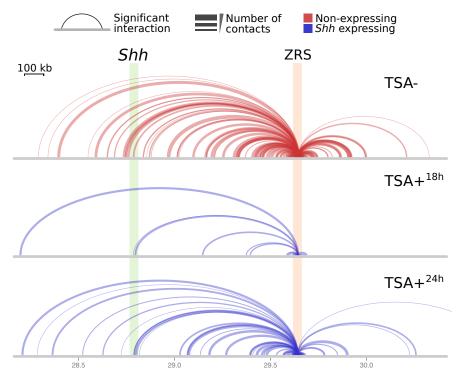
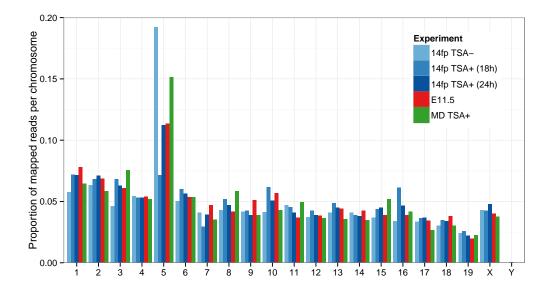


Figure 4: A stable ZRS–SHH interaction is coupled with reduced extraneous contacts. Are plots are shown for an untreated, non-expressing 14fp cell population (TSA-) and following TSA treatment after 18 and 24 hours. Arcs link significant interactions (q-value < 0.05) and arc widths are proportional to the normalised number of reads recorded for the interaction (Methods ??).

**Table 1: 4C sequencing library statistics. 4C** experiments are summarised as total number of reads in each experiment and the percentage of those reads labelled "duplicates". Note in 4C these duplicates are not artifactual and instead result from large numbers of contacts nearby to the viewpoint.

|                 | 14fp TSA- | <b>14fp TSA+</b><br>18h 24h |      | E11.5 | MD TSA+ |
|-----------------|-----------|-----------------------------|------|-------|---------|
| Reads (million) | 10.0      | 8.8                         | 24.2 | 10.7  | 12.2    |
| Duplicated (%)  | 62.8      | 74.2                        | 84.4 | 80.2  | 72.8    |



**Figure 5: The bait chromosome is enriched for 4C sequencing reads.** Chromosome 5 is visibly enriched for 4C reads as it contains the ZRS bait region (or viewpoint). Untreated control samples (*TSA*-) were assayed with two different secondary restriction enzymes (4-cutters HaeIII and MlucI).

We found the proportion of reads mapped to the fair region chromosome, chromosome 5 in this case, fell below the prescribed level of 50%. Across 4C experiments, we find instead that between approximately 10–20% of all reads mapped to the bait chromosome (Fig. 5), except for the 18 hour TSA+ treatment experiment which shows only around 7%. While this is still a clear enrichment over non-bait chromosomes, it suggests the assay results suffer from either increased *trans*-contact noise or decreased *cis*-contact enrichment around the bait region.

Lower than expected levels of both sequence duplication and bait chromosome enrichment suggest loss of signal around the bait region itself. This is the area where we'd expect both very high levels of duplication (identical restriction fragment pairings between nearby genomic locations) and a majority of all sequencing reads, driving the overall chromosome enrichment. The precise reason for the discrepancy is unclear but suggests the results may have a lower signal-to-noise ratio than has previously been achievable in 4C experiments.<sup>[13]</sup> Potentially the signal-to-noise ratio could be improved by utilising a double cross-linking procedure such as that used in Lin *et al.*<sup>[15]</sup>

# 1.4 POLYMER MODELLING OF CHROMATIN

Chromosome conformation capture allow investigation of genome organisation, but such data are commonly analysed using one or two-dimensional representations. A

growing set of algorithms looks instead to rebuild the three-dimensional polymer trajectory of a chromatin fibre, using Hi-C or 5C data as input (e.g. 16–23). Intuitively, in each method the interaction frequency between two regions is idealised as inversely proportional to their physical distance (where possible and according to various other constraints). Where these methods differ is in their approaches to solving this optimisation problem. We chose the AutoChrom3D method<sup>[21]</sup> for use in this work (described in Section 1.4.1) as the algorithm can accept 5C input and model polymers at high resolution of 8 kb or greater.

#### 1.4.1 AutoChrom3D method

The procedure implemented in AutoChrom3D can be summarised as: [21]

- 1. The chromatin fibre is represented as beads-on-a-string, with  $N_{beads} = \lceil \frac{L}{R} \rceil$  (where L is the length of the region and R the resolution)
- 2. A local compaction parameter is calculated using a sliding window of each 50 adjacent beads (intra-window contacts are averaged and compared to those over the whole region under study)
- 3. Interaction frequency between beads of a given genomic distance is modelled as a Poisson-distributed random variable and noisy or unstable contacts, considered in the context of neighbouring beads, are filtered
- 4. This filtered set of interaction frequencies are then normalised using the previously-calculated compaction parameter to give an  $N_{beads} \times N_{beads}$  matrix of interaction strengths
- 5. Interaction strength is converted to spatial distance through two linear transformations based on experimental observations of nuclear occupancy and regional flexibility<sup>[24]</sup>
- 6. Cartesian co-ordinates are then calculated via non-linear constrained optimisation of pairwise spatial distances using LINGO<sup>[25]</sup>

#### 1.4.2 Modelling the *Shh* region with 5C

5C data was generated by our collaborators over the same *Shh*–ZRS region as was assayed with 4C (Fig. 1; Section 1.3) with the aim of developing a multi-point perspective on local chromatin conformation beyond that available from 4C data.

We used this 5C experimental data in combination with a particular three-dimensional inference program (AutoChrom3D<sup>[21]</sup>) in an attempt to compare polymer trajectories in TSA treated and untreated 88fp mouse cells, a similar and complimentary cell line to

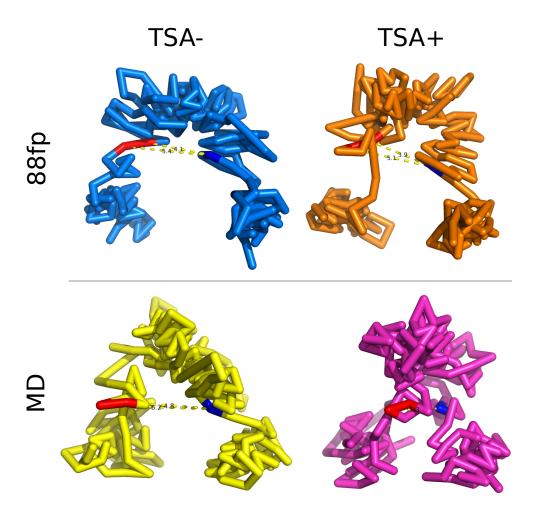


Figure 6: Inferred polymer trajectories of the ZRS–SHH region following TSA treatment in two cell lines. 3D structures are shown for 5C experiments assaying the region around Shh (red) and ZRS (blue) in an Shh-expressing limb bud cell line (88fp) and a non-expressing mandibular cell line (MD). Labelled measurements are given in Table 2. Structures were predicted by AutoChrom3D<sup>[21]</sup> using  $210 \times 8$  kb beads per polymer.

that used in earlier 4C experiments (14fp). As a control, 5C was also performed on mandibular (MD) cells, with and without TSA treatment, which do not express *Shh*. Prior to structural modelling, the my5C program was used to generate normalised 5C interaction frequencies. [26]

We find that TSA treatment of 88fp cells does appear to slightly reduce the distance between *Shh* and ZRS in inferred 3D structures (Fig. 6), however this difference is overshadowed—to our surprise—by that observed in the non-expressing MD cell line. This latter mandibular cell line undergoes a large structural transition which brings together the *Shh* gene and the ZRS enhancer. Measurements between these elements for each structure are shown in Table 2.

Table 2: Measurement distances between ZRS and SHH in each inferred 3D structure. Distances are given in arbitrary units. Shh spans two beads of the polymer model, hence two distances are calculated in each case  $(d_1, d_2)$ . RMSD is the minimised root mean squared deviation between the two structures and is given as a relative unitless quantity. The radius of gyration (gyradius) is also shown.

|      |       | Distance |      | RMSD  | <b>Gyradius</b> (μm)<br>TSA- TSA+ |       |
|------|-------|----------|------|-------|-----------------------------------|-------|
|      |       | TSA-     | TSA+ | KWISD | TSA-                              | TSA+  |
| 88fp | $d_1$ | 5.4      | 5.1  | 1.701 | 0.244                             | 0.244 |
|      | $d_2$ | 4.1      | 3.9  |       |                                   |       |
| MD   | $d_1$ | 6.2      | 3.3  | 2.377 | 0.217                             | 0.205 |
|      | $d_2$ | 4.8      | 2.0  |       | 0.217                             |       |

We also report a greater overall structural shift following TSA treatment in the MD cell line, with an RMSD between the two structures of 2.377 arbitrary units, relative to 1.701 between TSA+ and TSA- 88fp cells. The radius of gyration, unchanged in 88fp, is also decreased in the MD cell line following TSA treatment, indicating the region becomes more compact following TSA treatment (Table 2).

# 1.4.3 Repeat simulations

We have shown what appears to be a structural shift in the *Shh*-ZRS locus per 3D modelling predictions (Section 1.4.2). It is of interest to assess the stability and reproducibility of these results through repeat simulations of the polymer trajectory. At this point it is unclear whether the *Shh*-ZRS bound state represents a firm consensus over the cell population, or an alternative structure with similar optimisation energy to that of the non-contacting state.

We re-ran simulations of the 3D chromatin fibre in the *Shh-ZRS* region a total of five times (Fig. 7). In every case, the algorithm generates the known *Shh-ZRS* TAD as a compacted domain bookended by the two loci under study. This sanity check ensures the results are broadly compatible with our *a prior* expectation of the region's structure given the 2D heatmap representation of 5C data (Fig. 1).

Repeat simulations indeed appear to recreate the induced ZRS–*Shh* contact in the mandibular cell line (MD) following TSA treatment (Fig. 7). This is again surprising, as the MD cell lines do not express *Shh* and so were included as a negative control, with no expected changes in local chromatin structure following TSA treatment. In repeat simulations of the 88fp cell line, a close analogue of the 14fp cell line used in 4C, we see relatively little change in distance between *Shh* and ZRS (Fig. 7).

We quantified these distances by measuring form the single bead containing ZRS to the two beads which overlap the *Shh* gene (Fig. 8). While these are not biological replicates, just repeat simulations, we find the distance shift in MD cells is statistically significant at the level of  $\alpha = 0.05$  for both bead distances (Mann-Whitney:

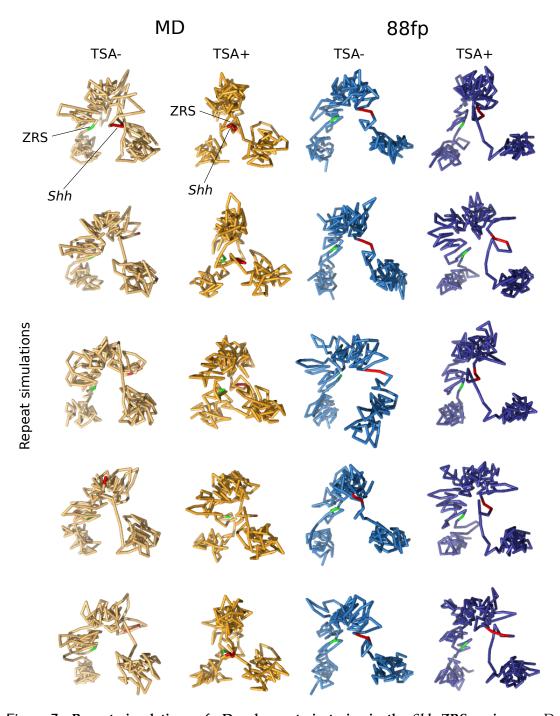


Figure 7: Repeat simulations of 3D polymer trajectories in the *Shh*–ZRS region. 3D structures are shown for 5C experiments assaying the region around *Shh* (*red*) and ZRS (*green*) in an *Shh*-expressing limb bud cell line (88fp) and a non-expressing mandibular cell line (MD). Structures were aligned as whole molecules with the uppermost replicate in each column.

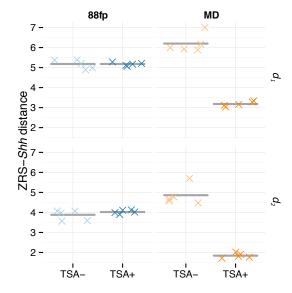


Figure 8: *Shh*–**ZRS** distance measurements from repeated 3D polymer simulations. Measurements were taken from 5 replicate 3D simulations (shown in Fig. 7). Distances are given in arbitrary units. *Shh* spans two beads of the polymer model, hence two distances are calculated in each case  $(d_1, d_2)$ .

 $d_1$ : p < 0.012,  $d_2$ : p < 0.012). Distances in the 88fp cell line were not significantly different following TSA treatment (Fig. 8).

Qualitatively, there could be some observable structural dynamics caused by TSA treatment in 88fp cells. It appears potentially that part of the *Shh*–ZRS TAD becomes more loosely-packed at the ZRS side. This can be seen most clearly in simulations 2 and 4 of the TSA treated 88fp polymer models (Fig. 7). Given the function of TSA as a histone dactyls inhibitor, and unpublished results showing it causes an increase in H<sub>3</sub>K<sub>2</sub>7 acetylation over the ZRS, we speculate that this additional acetyl groups could be causing greater repulsion between histones leading to a less-compacted structure. Potentially then, the ZRS is transitioning to a more accessible state despite no change in its physical distance relative to *Shh*.

The main result, that TSA treatment induces a *Shh*–ZRS contact in mandibular cell lines but not in limb bud, is difficult to explain and runs contrary to our expectations. 4C experiments performed over the same region reported ZRS–*Shh* contacts (Fig. 4) but polymer models using 5C found instead that these two loci remain relatively separated with or without TSA treatment (though still much closer than expected relative to their genomic distance; Fig. 6). One explanation for this could be the filtering method used by AutoChrom3D (Section 1.4.1). Highly improbably contacts are filtered before structural prediction to prevent errors or artefacts leading to aberrant structures. In this case, a genuine instance of long-range *cis*-regulation may end up being down-weighted or removed before polymer modelling. Alternatively this may be an example of where, as has been noted at high-resolution, the results of 5C as formaldehyde cross-linking efficiencies cannot be interpreted as spatial distances. [27]

Additional follow-up experiments are underway to further explore the dynamics in this region.

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