Chapter 1

Simulation Solution

- 1.1 Smoothed Particle Hydrodynamics
- 1.1.1 PySPH
- 1.2 Code
- 1.3 Deformation of the Surface?
- 1.4 Calculating the Energy Transferred?

```
1 from pysph.sph.equation import Equation
3 class BlackHole2D (Equation):
       \operatorname{def} = \operatorname{init}_{-}(\operatorname{self}, \operatorname{dest}, \operatorname{sources}, \operatorname{soft} = 0.05, \operatorname{t_hit} = 5.0, \operatorname{M} = 1.0)
            self.soft = soft # softening length to not divide by zero
 5
 6
            self.t_hit = t_hit # time when the black hole crosses the
      origin
 7
            self.M = M # mass of black hole
8
            super(BlackHole2D, self).__init__(dest, sources)
9
10
       def initialize (self, d_idx, d_au, d_av):
11
            d_au[d_idx] = 0.0
12
            d_av[d_idx] = 0.0
13
14
       # calculate the force due to the black hole
       def loop(self, d_x, d_y, d_idx, d_au, d_av, t):
15
            d_{au}[d_{idx}] += -self.M * d_{ax}[d_{idx}] / pow((d_{ax}[d_{idx}] **2 +
16
       self.soft**2 + (d_y[d_idx] + t - self.t_hit)**2),3.0/2.0)
17
            d_av[d_idx] += -self.M * (d_y[d_idx] + t - self.t_hit) /
      pow((d_x[d_idx]**2 + self.soft**2 + (d_y[d_idx] + t - self.
      t_hit)**2),3.0/2.0
```

Figure 1.1: Class for adding the acceleration due to the primordial black hole.

```
19 # Import the equations
 20 from pysph.sph.equation import Group
 21 from pysph.sph.BlackHoleEquation import BlackHole2D
40 # Domain and reference values
 41 \text{ Lx} = 120.0; \text{ H} = 15.0; \text{ Ly} = 1.5*H
42 \text{ gy} = -1.0
 43 \text{ Vmax} = \text{np.sqrt}(abs(gy) * H)
44 \text{ c0} = 10 * \text{Vmax}; \text{ rho0} = 1.0
45 \text{ p0} = c0*c0*rho0
 46 \text{ gamma} = 1.0
 47
48 \text{ soft} = 0.01
 49 \text{ t_hit} = 100.0
 50 \text{ Mass} = 1.0
 51 \text{ tf} = 150.0 \# \text{Simulation} ends when the black hole reaches the
       bottom of the tank
 52
 53 # Reynolds number and kinematic viscosity
 54 \text{ Re} = 0; \text{nu} = 0.01 \text{ #Vmax*Ly/Re} \text{ # Ideal fluid}
 55
 56 # Numerical setup
 57 \text{ nx} = 100; \text{ dx} = \text{Lx/nx}
 58 \text{ ghost\_extent} = 5.5 * dx
 59 \text{ hdx} = 1.2
82 class BlackHole (Application):
         def create_equations(self):
171
              # Formulation for REF1
172
              equations1 = [
173
194
                   # Main acceleration block
                   Group (equations=[
195
212
                        # Add the black hole
213
                         BlackHole2D (dest='fluid', sources=None, soft=soft,
         t_hit=t_hit, M=Mass)
214
215
                   ]),
216
```

Figure 1.2: Modifications of the hydrostatic tank.