Practical Data Analysis for Political Scientists

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Chapter 1

About This Book

This book contains the course notes for Brenton Kenkel's course Statistics for Political Research II (PSCI 8357 at Vanderbilt University). It covers the basics of statistical modeling and programming with linear models, along with applications in R.

This book is written in R Markdown and published via Bookdown on GitHub Pages. You can find the R Markdown source files at https://github.com/brentonk/pdaps.

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Chapter 2

Principles of Programming

It may seem strange to begin a statistics class with two weeks on programming. It is strange. Here is why I have made this strange choice.

First, as a working social scientist, most of the time you spend on data analysis won't be on the *analysis* part. It'll be on obtaining and cleaning the data, to get it in a form that makes sense to analyze. Good programming skills will let you spend less time cleaning data and more time publishing papers.

Second, even if you don't want to develop good programming habits, journals are going to force you to. Every reputable political science journal requires that you provide replication scripts, and some of the best (e.g., *American Journal of Political Science*) have begun auditing the replication materials as a condition of publication. Better to learn The Right Way now when you have lots of time than to be forced to when you're writing a dissertation or on the market or teaching your own courses.

Third, while I feel embarrassed to invoke the cliché that is Big Data, that doesn't mean it's not a real thing. Political scientists have access to more data and more computing power than ever before. You can't collect, manage, clean, and analyze large quantities of data without understanding the basic principles of programming.

As Bowers (2011) puts it, "Data analysis is computer programming." By getting a PhD in political science, by necessity you're going to become a computer programmer. The choice before you is whether to be a good one or a bad one.

Wilson et al. (2014) list eight "best practices for scientific computing." The first two encapsulate most of what you need to know:

- 1. Write programs for people, not computers.
- 2. Let the computer do the work.

¹Or whatever other social science field.

2.1 Write Programs for People, Not Computers

The first two words here—write programs—are crucial. When you are doing analysis for a research project, you should be writing and running scripts, not typing commands into the R (or Stata) console. The console is ephemeral, but scripts are forever, at least if you save them.

Like the manuscripts you will write to describe your findings, your analysis scripts are a form of scientific communication. You wouldn't write a paper that is disorganized, riddled with grammatical errors, or incomprehensible to anyone besides yourself. Don't write your analysis scripts that way either.

Each script should be self-contained, ideally accomplishing one major task. Using an omnibus script that runs every bit of analysis is like writing a paper without paragraph breaks. A typical breakdown of scripts for a project of mine looks like:

```
• 0-download.r: downloads the data
```

• 1-clean.r: cleans the data

• 2-run.r: runs the main analysis

• 3-figs.r: generates figures

The exact structure varies depending on the nature of the project. Notice that the scripts are numbered in the order they should be run.

Within each script, write the code to make it as easy as possible for your reader to follow what you're doing. You should indent your code according to style conventions such as http://adv-r.had.co.nz/Style.html. Even better, use the Code -> Reindent Lines menu option in R Studio to automatically indent according to a sane style.

Another way to make your code readable—one that, unfortunately, cannot be accomplished quite so algorithmically—is to add explanatory comments. The point of comments is not to document how the language works. The following comment is an extreme example of a useless comment.

```
# Take the square root of the errors and assign them to
# the output variable
output <- sqrt(errors)</pre>
```

A better use for the comment would be to explain why you're taking the square root of the errors, at least if your purpose in doing so would be unclear to a hypothetical reader of the code.

My basic heuristic for code readability is If I got hit by a bus tomorrow, could one of my coauthors figure out what the hell I was doing and finish the paper?

2.2 Let the Computer Do the Work

Computers are really good at structured, repetitive tasks. If you ever find yourself entering the same thing into the computer over and over again, you are Doing It Wrong. Your job as the human directing the computer is to figure out the structure that underlies the repeated task and to program the computer to do the repetition.

For example, imagine you have just run a large experiment and you want to estimate effects by subgroups.² Your respondents differ across four variables—party ID (R or D), gender (male or female), race (white or nonwhite), and education (college degree or not)—giving you 16 subgroups. You *could* copy and paste your code to estimate the treatment effect 16 times. But this is a bad idea for a few reasons.

- Copy-paste doesn't scale. Copy-paste is managable (albeit misguided) for 16 iterations, but probably not for 50 and definitely not for more than 100.
- Making changes becomes painful. Suppose you decide to change how you calculate the estimate. Now you have to go back and individually edit 16 chunks of code.
- Copy-paste is error-prone, and insidiously so. If you do the calculation wrong all 16 times, you'll probably notice. But what if you screwed up for just one or two cases? Are you *really* going to go through and check that you did everything right in each individual case?

We're going to look at the most basic ways to get the computer to repeat structured tasks—functions and control flow statements. To illustrate these, we will use a result you discussed in Stat I: the central limit theorem.

The central limit theorem concerns the sampling distribution of the sample mean,

²There could be statistical problems with this kind of analysis, at least if the subgroups were specified post hoc. See https://xkcd.com/882/ ("Significant"). We're going to leave this issue aside for now, but we'll return to it later when we discuss the statistical crisis in science.

$$\bar{X} = \frac{1}{N} \sum_{n=1}^{N} X_n,$$

where each X_n is independent and identically distributed with mean μ and variance σ^2 . Loosely speaking, the CLT says that as N grows large, the sampling distribution of \bar{X} becomes approximately normal with mean μ and variance σ^2/N .

Here's what we would need to do to see the CLT in practice. We'd want to take a bunch of samples, each of size N, and calculate the sample mean of each. Then we'd have a sample of sample means, and we could check to verify that they are approximately normally distributed with mean μ and variance σ^2/N . This is a structured, repetitive task—exactly the kind of thing that should be programmed. We'll try it out with a random variable from a Poisson distribution with $\lambda = 3$, which has mean $\mu = 3$ and variance $\sigma^2 = 3$.

First things first. We can use the rpois function to draw a random sample of N numbers from the Poisson distribution.

```
samp <- rpois(10, lambda = 3)
samp</pre>
```

```
## [1] 2 3 8 3 5 4 3 4 2 2
```

To calculate the sample mean, we simply use the mean function.

```
mean(samp)
```

```
## [1] 3.6
```

We are interested in the distribution of the sample mean across many samples like this one. To begin, we will write a **function** that automates our core task—drawing a sample of N observations from Poisson(3) and calculating the sample mean. A function consists of a set of *arguments* (the inputs) and a *body* of code specifying which calculations to perform on the inputs to produce the output.

```
pois_mean <- function(n_obs) {
  samp <- rpois(n_obs, lambda = 3)
  ans <- mean(samp)
  return(ans)
}</pre>
```

This code creates a function called pois_mean. It has a single argument, called n_obs. It generates a random sample of n_obs draws from Poisson(3) and calculates its sample mean. It then returns the sample mean as the output.

Let's try calling this function a few times, each with a sample size of N=30. Your output will differ slightly from what's printed here, since the function is generating random numbers.

```
pois_mean(n_obs = 30)

## [1] 3.0333

pois_mean(n_obs = 30)

## [1] 2.4667

pois_mean(n_obs = 30)

## [1] 2.9667
```

Remember that what we're interested in is the *sampling distribution* of the sample mean—the distribution of the sample mean across every possible sample of N observations. We can approximate this distribution by running **pois_mean** many times (e.g., 1000 or more). This would be infeasible via copy-paste. Instead, we will use a **for loop**.

```
# Set up a vector to store the output
n_replicates <- 1000
sampling_dist <- rep(NA, n_replicates)

for (i in 1:n_replicates) {
   sampling_dist[i] <- pois_mean(n_obs = 30)
}</pre>
```

Here's how the for loop works. We specified i as the name of the index variable, with values 1:n_replicates. The for loop takes each value in the sequence, assigns it to the variable i, runs the given expression (in this case, assigning the output of pois_mean to the i'th element of sampling_dist), and then moves on to the next value in sequence, until it reaches the end.

Let's take a look at the results and compare them to our expectations.

[1] 0.096944

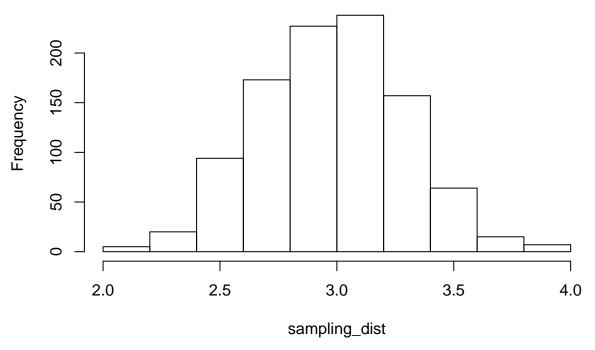
```
mean(sampling_dist) # Expect 3

## [1] 2.9952

var(sampling_dist) # Expect 1/10
```

hist(sampling_dist) # Expect roughly normal

Histogram of sampling_dist



For loops are fun, but don't overuse them. Many simple operations are **vectorized** and don't require a loop. For example, suppose you want to take the square of a sequence of numbers. You could use a for loop ...

```
input <- c(1, 3, 7, 29)
output <- rep(NA, length(input))

for (i in 1:length(input)) {
   output[i] <- input[i]^2
}

output</pre>
```

[1] 1 9 49 841

... but it's faster (in terms of computational speed) and easier to just take advantage of vectorization:

```
input^2
```

[1] 1 9 49 841

Another useful piece of control flow is **if/else statements**. These check a logical condition—an expression whose value is TRUE or FALSE—and run different code depending on the value of the expression. (You may want to catch up on the comparison operators: ==, >, >=, <, <=, etc.)

Let's edit the pois_mean function to allow us to calculate the median instead of the mean. We'll add a second argument to the function, and implement the option using an if/else statement.

```
pois_mean <- function(n_obs, use_median = FALSE) {
  samp <- rpois(n_obs, lambda = 3)
  if (use_median) {
    ans <- median(samp)
  } else {
    ans <- mean(samp)
  }
  return(ans)
}</pre>
```

A couple of things to notice about the structure of the function. We use a comma to separate multiple function arguments. Also, we've specified FALSE as the *default* for the use_median argument. If we call the function without explicitly specifying a value for use_median, the function sets it to FALSE.

```
pois_mean(n_obs = 9)

## [1] 3.7778

pois_mean(n_obs = 9, use_median = TRUE)

## [1] 2

pois_mean(n_obs = 9, use_median = FALSE)

## [1] 2.6667
```

There is a vectorized version of if/else statements called, naturally, the ifelse function. This function takes three arguments, each a vector of the same length: (1) a logical condition, (2) an output value if the condition is TRUE, (3) an output value if the condition is FALSE.

```
x <- 1:10
big_x <- x * 100
small_x <- x * -100

ifelse(x > 5, big_x, small_x)
```

```
## [1] -100 -200 -300 -400 -500 600 700 800 900 1000
```

Functions, for loops, and if/else statements are just a few of the useful tools for programming in ${\bf R}^3$ But even these simple tools are enough to allow you to do much more at scale than you could with a copy-paste philosophy.

³Others include the replicate function, the apply family of functions (sapply, lapply, tapply, mapply, ...), the **foreach** package, the **purrr** package, just to name a few of the most useful off the top of my head.

Chapter 3

Working with Data

Some material in this chapter is adapted from notes Matt DiLorenzo wrote for the Spring 2016 session of PSCI 8357.

Let me repeat something I said last week. In your careers as social scientists, starting with your dissertation research—if not earlier—you will probably spend more time collecting, merging, and cleaning data than you will on statistical analysis. So it's worth taking some time to learn how to do this well.

Best practices for data management can be summarized in a single sentence: Record and document everything you do to the data.

The first corollary of this principle is that raw data is sacrosanct. You should never edit raw data "in place". Once you download the raw data file, that file should never change.¹

In almost any non-trivial analysis, the "final" data—the format you plug into your analysis—will differ significantly from the raw data. It may consist of information merged from multiple sources. The variables may have been transformed, aggregated, or otherwise altered. The unit of observation may even differ from the original source. You must document every one of these changes, so that another researcher working from the exact same raw data will end up with the exact same final data.

The most sensible way to achieve this level of reproducibility is to do all of your data merging and cleaning in a script. In other words, no going into Excel and mucking around manually. Like any other piece of your analysis, your pipeline from raw data to final data should follow the principles of programming that we discussed last week.

Luckily for you,² the **tidyverse** suite of R packages (including **dplyr**, **tidyr**, and others) makes it easy to script your "data pipeline". We'll begin by loading the package.

library("tidyverse")

¹Even if it's data you collected yourself, that data should still have a "canonical" representation that never gets overwritten. See Leek (2015) for more on distributing your own data.

²But not for me, because these tools didn't exist when I was a PhD student. Also, get off my lawn!

3.1 Loading

The first step in working with data is to acquire some data. Depending on the nature of your research, you will be getting some or all of your data from sources available online. When you download data from online repositories, you should keep track of where you got it from. The best way to do so is—you guessed it—to script your data acquisition.

The R function download.file() is the easiest way to download files from URLs from within R. Just specify where you're getting the file from and where you want it to go. For the examples today, we'll use an "untidied" version of the World Development Indicators data from the World Bank that I've posted to my website.

Once you've got the file stored locally, use the utilities from the **readr** package (part of **tidyverse**) to read it into R as a data frame.³ We have a CSV file, so we will use **read_csv**. See help(package = "readr") for other possibilities.

```
untidy_data <- read_csv(file = "my-untidy-data.csv")</pre>
```

```
## Parsed with column specification:
## cols(
##
     country = col_character(),
##
     gdp.2005 = col double(),
     gdp.2006 = col double(),
##
     gdp.2007 = col double(),
##
##
     gdp.2008 = col double(),
##
     pop.2005 = col_double(),
##
     pop.2006 = col double(),
##
     pop.2007 = col double(),
##
     pop.2008 = col_double(),
##
     unemp.2005 = col double(),
##
     unemp.2006 = col double(),
##
     unemp.2007 = col_double(),
##
     unemp.2008 = col double()
## )
```

Remember that each column of a data frame might be a different type, or more formally *class*, of object. read_csv and its ilk try to guess the type of data each column contains: character, integer, decimal number ("double" in programming-speak), or something else. The readout

³More precisely, the **readr** functions produce output of class "tbl_df" (pronounced "tibble diff," I'm told), which are like data frames but better. See help(package = "tibble") for what can be done with tbl_dfs.

above tells you what guesses it made. If it gets something wrong—say, reading a column as numbers that ought to be characters—you can use the col_types argument to set it straight.

FYI, you could also run read csv() directly on a URL, as in:

```
read_csv("http://bkenkel.com/data/untidy-data.csv")
```

However, in analyses intended for publication, it's usually preferable to download and save the raw data. What's stored at a URL might change or disappear, and you'll need to have a hard copy of the raw data for replication purposes.

Now let's take a look at the data we've just loaded in.

head(untidy_data)

```
## # A tibble: 6 × 13
     country gdp.2005 gdp.2006 gdp.2007 gdp.2008
                                                               pop.2006
##
                                                    pop.2005
##
       <chr>
                                    <dbl>
                                                        <dbl>
                                                                  <dbl>
                 <dbl>
                          <dbl>
                                             <dbl>
## 1
               3.8423
                         4.0184
                                   4.0216
                                            3.6759
                                                    0.081223
                                                               0.083373
          AD
## 2
          AE 253.9655 278.9489 287.8318 297.0189
                                                    4.481976
                                                               5.171255
## 3
          AF
               9.7630
                        10.3052
                                 11.7212
                                           12.1445 24.399948 25.183615
                                            1.3902
## 4
          AG
               1.1190
                         1.2687
                                   1.3892
                                                    0.082565
                                                               0.083467
## 5
          AL
               9.2684
                         9.7718
                                 10.3483
                                           11.1275
                                                    3.011487
                                                               2.992547
## 6
          AM
               7.6678
                                   9.8731
                                           10.5544
                         8.6797
                                                    3.014917
                                                               3.002161
     ... with 6 more variables: pop.2007 <dbl>, pop.2008 <dbl>,
## #
      unemp.2005 <dbl>, unemp.2006 <dbl>, unemp.2007 <dbl>, unemp.2008 <dbl>
```

We have a country variable giving country abbreviations. The other variables are numerical values: the country's GDP in 2005, 2006, 2007, and 2008; then the same for population and unemployment. Let's get this into a format we could use for analysis.

3.2 Tidying

Wickham (2014) outlines three qualities that make data "tidy":

- 1. Each variable forms a column.
- 2. Each observation forms a row.
- 3. Each type of observational unit forms a table.

For one thing, this means that whether a dataset is tidy or not depends—at least in part (some data collections are messy from any angle)—on the purpose it's being analyzed for.

Each row of untidy_data is a country. In observational studies in comparative politics and international relations, more commonly the unit of observation is the country-year.⁴ How can we take untidy_data and easily make it into country-year data?

We'll use the **tidyr** package (again, part of **tidyverse**) to clean up this data. The biggest problem right now is that each column, besides the country identifier, really encodes two pieces of information: the year of observation and the variable being observed. To deal with this, we'll have to first transform the data from one untidy format to another. We're going to use the **gather()** function to make each row a country-year-variable.

What gather() does is make a row for each entry from a set of columns. It's probably easiest to understand it by seeing it in practice:

```
## # A tibble: 6 × 3
##
     country variable
                         number
##
       <chr>
                 <chr>>
                          <dbl>
## 1
          AD gdp.2005
                         3.8423
## 2
          AE gdp.2005 253.9655
## 3
          AF gdp.2005
                         9.7630
## 4
          AG gdp.2005
                         1.1190
## 5
          AL gdp.2005
                         9.2684
## 6
          AM gdp.2005
                         7.6678
```

With the first argument, we told gather() to use the untidy_data data frame. With the last argument, we told it the set of columns to "gather" together into a single column. The key column specifies the name of the variable to store the "key" (original column name) in, and the value column specifies the name of the variable to store the associated value. For example, the second row of long_data encodes what we previously saw as the gdp.2005 column of untidy_data.

Now we have a new problem, which is that variable encodes two pieces of information: the variable and the year of its observation. tidyr provides the separate() function to solve that, splitting a single variable into two.

⁴Insert lame joke about how Americanists haven't heard of other countries. But, seriously, if you're confused because you haven't heard of other countries, just think of "state-years".

```
## # A tibble: 6 × 4
##
     country
                var
                      year
                             number
##
       <chr> <chr> <chr>
                               <dbl>
## 1
           AD
                      2005
                              3.8423
                gdp
## 2
           ΑE
                gdp
                      2005 253.9655
## 3
           ΑF
                gdp
                      2005
                              9.7630
## 4
                              1.1190
           AG
                gdp
                      2005
## 5
           AL
                      2005
                              9.2684
                gdp
## 6
           AM
                gdp
                      2005
                              7.6678
```

So now we have country-year-variable data, with the year and variable conveniently stored in different columns. To turn this into country-year data, we can use the **spread()** function, which is like the inverse of **gather()**. **spread()** takes a key column and a value column, and turns each different key into a column of its own.

```
## # A tibble: 6 × 5
     country
##
              year
                         gdp
                                   pop unemp
       <chr> <chr>
##
                       <dbl>
                                 <dbl> <dbl>
## 1
          AD
              2005
                      3.8423 0.081223
## 2
          AD
              2006
                      4.0184 0.083373
                                          NA
## 3
              2007
          AD
                      4.0216 0.084878
                                          NA
## 4
          AD
              2008
                      3.6759 0.085616
                                          NA
## 5
          ΑE
              2005 253.9655 4.481976
                                         3.1
## 6
          ΑE
              2006 278.9489 5.171255
                                         3.3
```

When using spread() on data that you didn't previously gather(), be sure to set the fill argument to tell it how to fill in empty cells. A simple example:

test_data

```
## # A tibble: 3 × 3
##
           id
                  k
                         V
##
       <chr> <chr> <dbl>
## 1 brenton
                  a
                        10
## 2 brenton
                  b
                        20
## 3 patrick
                  b
                         5
```

```
spread(test data, key = k, value = v)
## # A tibble: 2 × 3
##
          id
                  a
                        b
       <chr> <dbl> <dbl>
## 1 brenton
                 10
                       20
## 2 patrick
                 NA
                        5
spread(test data, key = k, value = v, fill = 100)
## # A tibble: 2 × 3
##
          id
                  а
## *
       <chr> <dbl> <dbl>
## 1 brenton
                 10
                       20
## 2 patrick
                100
                        5
```

One more important note on **tidyverse** semantics. It includes a fabulous feature called the *pipe*, %>%, which makes it easy to string together a truly mind-boggling number of commands.

In pipe syntax, x % f () is equivalent to f(x). That seems like a wasteful and confusing way to write f(x), and it is. But if you want to string together a bunch of commands, it's much easier to comprehend

```
x %>%
f() %>%
g() %>%
h() %>%
i()
```

than i(h(g(f(x)))).

You can pass function arguments using the pipe too. For example, f(x, bear = "moose") is equivalent to x % f(bear = "moose").

The key thing about the **tidyverse** functions is that each of them takes a data frame as its first argument, and returns a data frame as its output. This makes them highly amenable to piping. For example, we can combine all three steps of our tidying above with a single command, thanks to the pipe:⁵

⁵If you are reading the PDF copy of these notes (i.e., the ones I hand out in class), the line breaks are eliminated, making the piped commands rather hard to read. I am working on fixing this. For now, you may find the online notes at http://bkenkel.com/pdaps easier to follow.

```
## # A tibble: 860 × 5
    country year
##
                       gdp
                                pop unemp
      <chr> <chr>
                    <dbl>
                              <dbl> <dbl>
         AD 2005
## 1
                    3.8423 0.081223
                                       NA
## 2
         AD 2006 4.0184 0.083373
                                       NA
## 3
         AD 2007
                    4.0216 0.084878
                                       NA
## 4
         AD 2008
                    3.6759 0.085616
                                       NA
         AE 2005 253.9655 4.481976
## 5
                                      3.1
## # ... with 855 more rows
```

Without the pipe, if we wanted to run all those commands together, we would have to write:

Sad!

3.3 Transforming and Aggregating

Tidying the data usually isn't the end of the process. If you want to perform further calculations on the raw, that's where the tools in **dplyr** (part of, you guessed it, the **tidyverse**) come in.

Perhaps the simplest **dplyr** function (or "verb", as the R hipsters would say) is **rename()**, which lets you rename columns.

```
clean_data %>%
  rename(gross_domestic_product = gdp)
```

```
## # A tibble: 860 × 5
##
     country year gross_domestic_product
                                                pop unemp
## *
       <chr> <chr>
                                     <dbl>
                                              <dbl> <dbl>
## 1
          AD 2005
                                    3.8423 0.081223
                                                       NA
## 2
          AD 2006
                                    4.0184 0.083373
                                                       NA
## 3
          AD 2007
                                    4.0216 0.084878
                                                       NA
## 4
          AD 2008
                                    3.6759 0.085616
                                                       NA
          AE 2005
## 5
                                  253.9655 4.481976
                                                      3.1
## # ... with 855 more rows
```

The **dplyr** functions, like the vast majority of R functions, do not modify their inputs. In other words, running rename() on clean_data will return a renamed copy of clean_data, but won't overwrite the original.

clean_data

```
## # A tibble: 860 × 5
##
     country year
                        gdp
                                 pop unemp
## *
       <chr> <chr>
                      <dbl>
                               <dbl> <dbl>
## 1
          AD 2005
                     3.8423 0.081223
                                        NA
## 2
          AD 2006
                     4.0184 0.083373
                                        NA
## 3
          AD 2007
                     4.0216 0.084878
                                        NA
## 4
          AD 2008
                     3.6759 0.085616
                                        NA
              2005 253.9655 4.481976
## 5
          ΑE
                                       3.1
## # ... with 855 more rows
```

If you wanted to make the change stick, you would have to run:

```
clean_data <- clean_data %>%
  rename(gross_domestic_product = gdp)
```

select() lets you keep a couple of columns and drop all the others. Or vice versa if you use minus signs.

```
clean_data %>%
  select(country, gdp)
```

AD 2008

... with 855 more rows

... with 855 more rows

AE 2005 253.9655

4

5

5

```
## # A tibble: 860 × 2
##
     country
                  gdp
## *
       <chr>
                <dbl>
## 1
          AD
               3.8423
               4.0184
## 2
          AD
## 3
               4.0216
          AD
## 4
               3.6759
          AD
## 5
          AE 253.9655
## # ... with 855 more rows
clean data %>%
  select(-pop)
## # A tibble: 860 × 4
##
     country year
                         gdp unemp
## *
       <chr> <chr>
                       <dbl> <dbl>
## 1
          AD 2005
                     3.8423
                                NA
## 2
          AD 2006
                      4.0184
                                NA
## 3
          AD 2007
                     4.0216
                                NA
```

mutate() lets you create new variables that are transformations of old ones.

NA

3.1

3.6759

AE 2005 253.9655 4.481976

```
clean data %>%
 mutate(gdppc = gdp / pop,
         log gdppc = log(gdppc))
## # A tibble: 860 × 7
##
     country year
                        gdp
                                 pop unemp
                                            gdppc log_gdppc
##
       <chr> <chr>
                                            <dbl>
                      <dbl>
                               <dbl> <dbl>
                                                       <dbl>
## 1
          AD 2005
                     3.8423 0.081223
                                        NA 47.305
                                                      3.8566
## 2
          AD 2006
                     4.0184 0.083373
                                        NA 48.198
                                                      3.8753
          AD 2007
                                        NA 47.381
## 3
                     4.0216 0.084878
                                                      3.8582
## 4
          AD
              2008
                     3.6759 0.085616
                                        NA 42.935
                                                      3.7597
```

3.1 56.664

4.0371

filter() cuts down the data according to the logical condition(s) you specify.

```
clean data %>%
  filter(year == 2006)
## # A tibble: 215 × 5
##
     country year
                         gdp
                                   pop unemp
##
       <chr> <chr>
                       <dbl>
                                 <dbl> <dbl>
                              0.083373
## 1
              2006
                      4.0184
          AD
                                           NA
## 2
                              5.171255
          ΑE
              2006 278.9489
                                          3.3
## 3
          AF
              2006
                    10.3052 25.183615
                                          8.8
## 4
          AG
              2006
                      1.2687
                              0.083467
                                           NA
## 5
          AL
              2006
                     9.7718
                              2.992547
                                         12.4
## # ... with 210 more rows
```

summarise() calculates summaries of the data. For example, let's find the maximum unemployment rate.

```
clean_data %>%
   summarise(max_unemp = max(unemp, na.rm = TRUE))

## # A tibble: 1 × 1

## max_unemp

## <dbl>
## 1 37.6
```

This seems sort of useless, until you combine it with the <code>group_by()</code> function. If you group the data before <code>summarise-ing</code> it, you'll calculate a separate summary for each group. For example, let's calculate the maximum unemployment rate for each year in the data.

```
clean_data %>%
  group_by(year) %>%
  summarise(max_unemp = max(unemp, na.rm = TRUE))
```

```
## # A tibble: 4 × 2
##
      year max unemp
##
     <chr>
               <dbl>
      2005
                37.3
## 1
## 2 2006
                36.0
## 3 2007
                34.9
      2008
                37.6
## 4
```

summarise() produces a "smaller" data frame than the input—one row per group. If you want to do something similar, but preserving the structure of the original data, use mutate in combination with group_by.

```
## Source: local data frame [860 x 5]
## Groups: year [4]
##
##
     country year unemp max_unemp unemp_over_max
##
       <chr> <chr> <dbl>
                               <dbl>
                                               <dbl>
## 1
          AD
             2005
                                37.3
                                                  NA
                       NA
## 2
          AD
              2006
                       NA
                                36.0
                                                  NA
## 3
          AD
              2007
                       NA
                                34.9
                                                  NA
              2008
## 4
          AD
                       NA
                                37.6
                                                  NA
## 5
          ΑE
                                37.3
                                            0.08311
              2005
                      3.1
## # ... with 855 more rows
```

This gives us back the original data, but with a max_unemp variable recording the highest unemployment level that year. We can then calculate each individual country's unemployment as a percentage of the maximum. Whether grouped mutate or summarise is better depends, of course, on the purpose and structure of your analysis.

Notice how I selected all of the unemployment-related columns with contains("unemp"). See ?select_helpers for a full list of helpful functions like this for select-ing variables.

3.4 Merging

Only rarely will you be lucky enough to draw all your data from a single source. More often, you'll be merging together data from multiple sources.

The key to merging data from separate tables is to have consistent identifiers across tables. For example, if you run an experiment, you might have demographic data on each subject in one table, and each subject's response to each treatment in another table. Naturally, you'll want to have a subject identifier that "links" the records across tables, as in the following hypothetical example.

```
subject_data
```

```
## 2 1002 female no yes
## 3 1003 male no no
```

subject response data

```
## # A tibble: 6 × 3
##
        id treatment response
##
     <dbl>
               <chr>>
                        <chr>>
## 1 1001 read book
                          sad
## 2 1001 watch tv
                          sad
## 3 1002 read_book
                        happy
## 4 1002 watch tv
                          sad
## 5 1003 read_book
                          sad
## 6 1003 watch tv
                        happy
```

Let's practice merging data with our cleaned-up country-year data. We'll take two datasets from my website: a country-level dataset with latitudes and longitudes, and a country-year–level dataset with inflation over time.

```
latlong_data <- read_csv("http://bkenkel.com/data/latlong.csv")
latlong_data</pre>
```

```
## # A tibble: 245 × 3
##
     country latitude longitude
##
       <chr>
                <dbl>
                           <dbl>
## 1
          AD
                42.546
                          1.6016
## 2
          ΑE
               23.424
                         53.8478
## 3
          ΑF
               33.939
                         67.7100
## 4
          AG
                17.061
                        -61.7964
## 5
                18.221
          ΑI
                        -63.0686
## # ... with 240 more rows
```

```
inflation_data <- read_csv("http://bkenkel.com/data/inflation.csv")
inflation data</pre>
```

```
## # A tibble: 1,070 \times 3
##
     country year inflation
##
       <chr> <int>
                        <dbl>
## 1
          AD 2004
                           NA
## 2
          AD 2005
                           NA
## 3
          AD 2006
                           NA
## 4
          AD
              2007
                           NA
## 5
          AD
              2008
                           NA
## # ... with 1,065 more rows
```

For your convenience, both of these datasets use the same two-letter country naming scheme as the original data. Unfortunately, out in the real world, data from different sources often use incommensurate naming schemes. Converting from one naming scheme to another is part of the data cleaning process, and it requires careful attention.

dplyr contains various _join() functions for merging. Each of these take as arguments the two data frames to merge, plus the names of the identifier variables to merge them on. The one I use most often is left_join(), which keeps every row from the first ("left") data frame and merges in the columns from the second ("right") data frame.

For example, let's merge the latitude and longitude data for each country into clean_data.

```
## # A tibble: 860 × 7
##
     country year
                                   pop unemp latitude longitude
                         gdp
                                 <dbl> <dbl>
##
       <chr> <chr>
                       <dbl>
                                                <dbl>
                                                           <dbl>
## 1
          ΑD
              2005
                      3.8423 0.081223
                                               42.546
                                                          1.6016
                                          NA
## 2
          AD
              2006
                      4.0184 0.083373
                                          NA
                                               42.546
                                                          1.6016
## 3
          AD
              2007
                      4.0216 0.084878
                                          NA
                                               42.546
                                                          1.6016
## 4
          AD 2008
                      3.6759 0.085616
                                          NA
                                               42.546
                                                          1.6016
## 5
              2005 253.9655 4.481976
                                         3.1
                                               23.424
                                                         53.8478
## # ... with 855 more rows
```

Since latlong_data is country-level, the value is the same for each year. So the merged data contains redundant information. This is one reason to store data observed at different levels in different tables—with redundant observations, it is easier to make errors yet harder to catch them and fix them.

We can also merge data when the identifier is stored across multiple columns, as in the case of our country-year data. But first, a technical note.⁶ You might notice that the year column of clean_data is labeled <chr>>, as in character data. Yet the year column of inflation_data is labeled <int>>, as in integer data. We can check that by running class() on each respective column.

```
class(clean_data$year)
```

[1] "character"

⁶This won't be the case if you got clean_data by loading it in directly from clean-data.csv on my website, since read_csv() will have correctly encoded year as an integer.

```
class(inflation_data$year)
```

```
## [1] "integer"
```

From R's perspective, the character string "1999" is a very different thing than the integer number 1999. Therefore, if we try to merge clean_data and inflation_data on the year variable, it will throw an error.

Error in eval(substitute(expr), envir, enclos): Can't join on 'year' x 'year' because of

To fix this, let's use mutate() to convert the year column of clean_data to an integer. We probably should have done this in the first place—after all, having the year encoded as a character string would have thrown off plotting functions, statistical functions, or anything else where it would be more natural to treat the year like a number.

```
## # A tibble: 860 × 5
##
                       gdp
    country year
                                pop unemp
##
      <chr> <int>
                    <dbl>
                              <dbl> <dbl>
## 1
         AD 2005
                    3.8423 0.081223
                                       NA
## 2
         AD 2006 4.0184 0.083373
                                       NA
## 3
         AD 2007 4.0216 0.084878
                                       NA
## 4
         AD 2008
                    3.6759 0.085616
                                       NA
         AE 2005 253.9655 4.481976
                                      3.1
## # ... with 855 more rows
```

Looks the same as before, except with an important difference: year is now labeled <int>.

Now we can merge the two datasets together without issue. Notice how we use a vector in the by argument to specify multiple columns to merge on.

```
## # A tibble: 860 × 6
##
                         gdp
     country year
                                  pop unemp inflation
##
       <chr> <int>
                       <dbl>
                                <dbl> <dbl>
                                                 <dbl>
## 1
          AD
              2005
                      3.8423 0.081223
                                          NA
                                                    NA
## 2
          AD 2006
                      4.0184 0.083373
                                          NA
                                                    NA
## 3
                                                    NA
          AD
              2007
                      4.0216 0.084878
                                          NA
## 4
              2008
                      3.6759 0.085616
          AD
                                          NA
                                                    NA
## 5
              2005 253.9655 4.481976
          ΑE
                                         3.1
                                                    NA
## # ... with 855 more rows
```

You might remember that inflation_data contained some country-years not included in the original data (namely, observations from 2004). If we want the merged data to use the observations from inflation_data rather than clean_data, we can use the right_join() function.

```
## # A tibble: 1,070 \times 6
##
     country year
                       gdp
                                 pop unemp inflation
##
       <chr> <int>
                     <dbl>
                               <dbl> <dbl>
                                                <dbl>
## 1
          AD
              2004
                        NA
                                  NA
                                        NA
                                                   NA
## 2
          AD 2005 3.8423 0.081223
                                        NA
                                                   NA
          AD 2006 4.0184 0.083373
## 3
                                        NA
                                                   NA
## 4
          AD 2007 4.0216 0.084878
                                        NA
                                                   NA
          AD 2008 3.6759 0.085616
## 5
                                        NA
                                                   NA
## # ... with 1,065 more rows
```

One last common issue in merging is that the identifier variables have different names in the two datasets. If it's inconvenient or infeasible to correct this by renaming the columns in one or the other, you can specify the by argument as in the following example.

```
## # A tibble: 1,070 × 3
## the_country the_year inflation
## <chr> <int> <dbl>
## 1 AD 2004 NA
## 2 AD 2005 NA
```

```
## 3 AD 2006 NA
## 4 AD 2007 NA
## 5 AD 2008 NA
## # ... with 1,065 more rows
```

```
## # A tibble: 860 × 6
##
     country year
                                 pop unemp inflation
                        gdp
##
       <chr> <int>
                      <dbl>
                               <dbl> <dbl>
                                               <dbl>
## 1
          AD 2005
                     3.8423 0.081223
                                                  NA
                                        NA
## 2
          AD 2006 4.0184 0.083373
                                        NΑ
                                                  NΑ
          AD 2007
## 3
                     4.0216 0.084878
                                        NA
                                                  NA
## 4
          AD 2008
                     3.6759 0.085616
                                        NA
                                                  NA
## 5
          AE 2005 253.9655 4.481976
                                       3.1
                                                  NA
## # ... with 855 more rows
```

3.5 Appendix: Creating the Example Data

I used the same tools this chapter introduces to create the untidy data. I may as well include the code to do it, in case it helps further illustrate how to use the **tidyverse** tools (and, as a bonus, the **WDI** package for downloading World Development Indicators data).

First I load the necessary packages.

```
library("tidyverse")
library("WDI")
library("countrycode")
library("stringr")
```

Next, I download the relevant WDI data. I used the WDIsearch() function to locate the appropriate indicator names.

```
country year NY.GDP.MKTP.KD SP.POP.TOTL SL.UEM.TOTL.ZS
##
     iso2c
        1A Arab World 2005
## 1
                                1.6428e+12
                                             313430911
                                                               12.1402
## 2
        1A Arab World 2006
                                1.7629e+12
                                             320906736
                                                               11.3296
## 3
        1A Arab World 2007
                                1.8625e+12
                                             328766559
                                                               10.8961
        1A Arab World 2008
                                1.9799e+12
## 4
                                             336886468
                                                               10.5060
                World 2005
## 5
        1W
                                5.7703e+13 6513959904
                                                                6.1593
## 6
                World 2006
                                6.0229e+13 6594722462
                                                                5.9000
        1W
```

I want to get rid of the aggregates, like the "Arab World" and "World" we see here. As a rough tack at that, I'm going to exclude those so-called countries whose ISO codes don't appear in the **countrycode** package data.⁷

```
dat_countries <- dat_raw %>%
  filter(iso2c %in% countrycode_data$iso2c)
```

Let's check on which countries are left. (I cut it down to max six characters per country name for printing purposes.)

```
dat_countries$country %>%
  unique() %>%
  str_sub(start = 1, end = 6)
```

```
[1] "Andorr" "United" "Afghan" "Antigu" "Albani" "Armeni" "Angola"
##
##
     [8] "Argent" "Americ" "Austri" "Austra" "Aruba"
                                                      "Azerba" "Bosnia"
##
    [15] "Barbad" "Bangla" "Belgiu" "Burkin" "Bulgar" "Bahrai" "Burund"
                  "Bermud" "Brunei" "Bolivi" "Brazil" "Bahama" "Bhutan"
##
    [22] "Benin"
    [29] "Botswa" "Belaru" "Belize" "Canada" "Congo," "Centra" "Congo,"
##
    [36] "Switze" "Cote d" "Chile"
                                    "Camero" "China"
                                                       "Colomb" "Costa "
##
    [43] "Cuba"
                  "Cabo V" "Curaca" "Cyprus" "Czech " "German" "Djibou"
##
    [50] "Denmar" "Domini" "Domini" "Algeri" "Ecuado" "Estoni" "Egypt,"
##
    [57] "Eritre" "Spain" "Ethiop" "Finlan" "Fiji"
                                                       "Micron" "Faroe "
##
    [64] "France" "Gabon" "United" "Grenad" "Georgi" "Ghana"
                                                               "Gibral"
##
    [71] "Greenl" "Gambia" "Guinea" "Equato" "Greece" "Guatem" "Guam"
##
    [78] "Guinea" "Guyana" "Hong K" "Hondur" "Croati" "Haiti"
##
                                                                "Hungar"
    [85] "Indone" "Irelan" "Israel" "Isle o" "India"
                                                       "Iraq"
                                                                "Iran, "
##
    [92] "Icelan" "Italy" "Jamaic" "Jordan" "Japan"
                                                      "Kenva"
                                                                "Kyrgyz"
##
    [99] "Cambod" "Kiriba" "Comoro" "St. Ki" "Korea," "Korea," "Kuwait"
##
## [106] "Cayman" "Kazakh" "Lao PD" "Lebano" "St. Lu" "Liecht" "Sri La"
## [113] "Liberi" "Lesoth" "Lithua" "Luxemb" "Latvia" "Libya"
## [120] "Monaco" "Moldov" "Monten" "St. Ma" "Madaga" "Marsha" "Macedo"
## [127] "Mali"
                  "Myanma" "Mongol" "Macao " "Northe" "Maurit" "Malta"
```

 $^{^{7}}$ **countrycode** is a very useful, albeit imperfect, package for converting between different country naming/coding schemes.

```
## [134] "Maurit" "Maldiv" "Malawi" "Mexico" "Malays" "Mozamb" "Namibi"
## [141] "New Ca" "Niger"
                          "Nigeri" "Nicara" "Nether" "Norway" "Nepal"
## [148] "Nauru" "New Ze" "Oman"
                                    "Panama" "Peru"
                                                      "French" "Papua "
## [155] "Philip" "Pakist" "Poland" "Puerto" "West B" "Portug" "Palau"
## [162] "Paragu" "Qatar" "Romani" "Serbia" "Russia" "Rwanda" "Saudi "
## [169] "Solomo" "Seyche" "Sudan"
                                    "Sweden" "Singap" "Sloven" "Slovak"
## [176] "Sierra" "San Ma" "Senega" "Somali" "Surina" "South " "Sao To"
## [183] "El Sal" "Sint M" "Syrian" "Swazil" "Turks " "Chad"
## [190] "Thaila" "Tajiki" "Timor-" "Turkme" "Tunisi" "Tonga" "Turkey"
## [197] "Trinid" "Tuvalu" "Tanzan" "Ukrain" "Uganda" "United" "Urugua"
## [204] "Uzbeki" "St. Vi" "Venezu" "Britis" "Virgin" "Vietna" "Vanuat"
## [211] "Samoa" "Yemen," "South " "Zambia" "Zimbab"
```

With that out of the way, there's still some cleaning up to do. The magnitudes of GDP and population are too large, and the variable names are impenetrable. Also, the country variable, while helpful, is redundant now that we're satisfied with the list of countries remaining.

```
##
     country year
                       gdp
                                 pop unemp
## 1
          AD 2005
                    3.8423 0.081223
                                        NA
## 2
          AD 2006
                    4.0184 0.083373
                                        NA
## 3
          AD 2007
                    4.0216 0.084878
                                        NΑ
## 4
          AD 2008
                    3.6759 0.085616
                                        NA
## 5
          AE 2005 253.9655 4.481976
                                       3.1
          AE 2006 278.9489 5.171255
## 6
                                       3.3
```

Now I convert the data to "long" format.

```
dat_countries_long <- dat_countries %>%
  gather(key = variable,
      value = value,
      gdp:unemp)
head(dat_countries_long)
```

```
##
     country year variable
                              value
## 1
          AD 2005
                        gdp
                              3.8423
## 2
          AD 2006
                              4.0184
                        gdp
## 3
          AD 2007
                              4.0216
                        gdp
          AD 2008
## 4
                        gdp
                              3.6759
## 5
          AE 2005
                        gdp 253.9655
## 6
          AE 2006
                        gdp 278.9489
```

I then smush variable and year into a single column, and drop the individual components.

```
dat_countries_long <- dat_countries_long %>%
  mutate(var_year = paste(variable, year, sep = ".")) %>%
  select(-variable, -year)
head(dat_countries_long)
```

```
value var_year
##
     country
## 1
               3.8423 gdp.2005
          AD
## 2
          AD
               4.0184 gdp.2006
## 3
          AD
               4.0216 gdp.2007
## 4
          AD
               3.6759 gdp.2008
## 5
          AE 253.9655 gdp.2005
          AE 278.9489 gdp.2006
## 6
```

Finally, I "widen" the data, so that each var_year is a column of its own.

```
dat_countries_wide <- dat_countries_long %>%
    spread(key = var_year, value = value)
head(dat_countries_wide)
```

```
##
     country gdp.2005 gdp.2006 gdp.2007 gdp.2008 pop.2005
                                                             pop.2006
## 1
          AD
               3.8423
                        4.0184
                                 4.0216
                                           3.6759
                                                  0.081223
                                                             0.083373
## 2
          AE 253.9655 278.9489 287.8318 297.0189
                                                  4.481976
                                                             5.171255
## 3
                                         12.1445 24.399948 25.183615
          ΑF
               9.7630
                      10.3052
                                11.7212
## 4
          AG
               1.1190
                        1.2687
                                 1.3892
                                           1.3902
                                                 0.082565
                                                             0.083467
               9.2684
                                        11.1275
## 5
          AL
                        9.7718
                               10.3483
                                                  3.011487
                                                             2.992547
## 6
          MA
               7.6678
                        8.6797
                                 9.8731 10.5544
                                                  3.014917
                                                             3.002161
##
      pop.2007 pop.2008 unemp.2005 unemp.2006 unemp.2007 unemp.2008
## 1
     0.084878 0.085616
                                 NA
                                            NA
                                                        NA
                                                                   NA
## 2 6.010100 6.900142
                                3.1
                                            3.3
                                                       3.4
                                                                  4.0
## 3 25.877544 26.528741
                                8.5
                                                                  8.9
                                            8.8
                                                       8.4
## 4 0.084397
                                 NA
                0.085350
                                            NA
                                                        NA
                                                                   NA
## 5
     2.970017 2.947314
                               12.5
                                           12.4
                                                      13.5
                                                                 13.0
## 6 2.988117 2.975029
                               27.8
                                           28.6
                                                      28.4
                                                                 16.4
```

Now we have some ugly data. I save the output to upload to my website.

```
write_csv(dat_countries_wide, path = "untidy-data.csv")
```

And here's how I made the second country-year dataset used in the merging section. The country dataset with latitudes and longitudes is from https://developers.google.com/public-data/docs/canonical/countries_csv.

Chapter 4

Data Visualization

Visualization is most important at the very beginning and the very end of the data analysis process. In the beginning, when you've just gotten your data together, visualization is perhaps the easiest tool to explore each variable and learn about the relationships among them. And when your analysis is almost complete, you will (usually) use visualizations to communicate your findings to your audience.

We only have time to scratch the surface of data visualization. This chapter will cover the plotting techniques I find most useful for exploratory and descriptive data analysis. We will talk about graphical techniques for presenting the results of regression analyses later in the class—once we've, you know, learned something about regression.

4.1 Basic Plots

We will use the **ggplot2** package, which is part of—I'm as tired of it as you are—the **tidyverse**.

```
library("tidyverse")
```

For the examples today, we'll be using a dataset with statistics about the fifty U.S. states in 1977,¹ which is posted on my website.

```
state_data <- read_csv("http://bkenkel.com/data/state-data.csv")
state_data</pre>
```

```
## # A tibble: 50 × 12
## State Abbrev Region Population Income Illiteracy LifeExp Murder
## <chr> <chr> <chr> <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> </dbl>
```

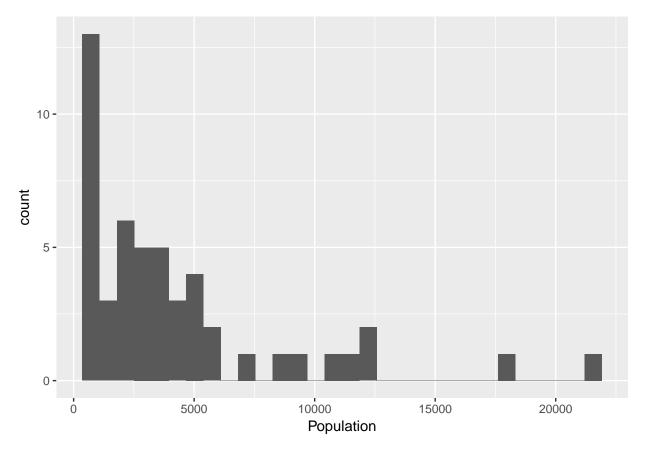
 $^{^{1}\}mathrm{Why}$ 1977? Because it was easily available. See the appendix to this chapter.

```
## 1
        Alabama
                     AL
                          South
                                       3615
                                               3624
                                                            2.1
                                                                  69.05
                                                                           15.1
## 2
         Alaska
                      ΑK
                                        365
                                               6315
                                                            1.5
                                                                  69.31
                                                                           11.3
                           West
## 3
        Arizona
                     AZ
                           West
                                       2212
                                               4530
                                                            1.8
                                                                  70.55
                                                                            7.8
## 4
       Arkansas
                      AR
                          South
                                       2110
                                               3378
                                                            1.9
                                                                  70.66
                                                                           10.1
## 5 California
                                               5114
                                                                  71.71
                      CA
                           West
                                      21198
                                                            1.1
                                                                           10.3
     ... with 45 more rows, and 4 more variables: HSGrad <dbl>, Frost <dbl>,
       Area <dbl>, IncomeGroup <chr>>
## #
```

When I obtain data, I start by looking at the univariate distribution of each variable via a histogram. The following code creates a histogram in ggplot.

```
ggplot(state_data, aes(x = Population)) +
  geom_histogram()
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



Let's walk through the syntax there. In the first line, we call ggplot(), specifying the data frame to draw from, then in the aes() command (which stands for "aesthetic") we specify the variable to plot. If this were a bivariate analysis, here we would have also specified a y variable to put on the y-axis. If we had just stopped there, we would have a sad, empty plot. The + symbol indicates that we'll be adding something to the plot. geom_histogram() is the command to overlay a histogram.

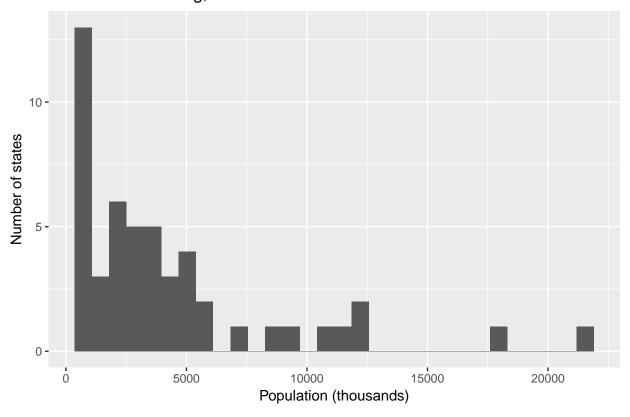
We'll only be looking at a few of the ggplot commands today. I recommend taking a look at the online package documentation at http://docs.ggplot2.org to see all of the many features available.

When you're just making graphs for yourself to explore the data, you don't need to worry about things like axis labels as long as you can comprehend what's going on. But when you prepare graphs for others to read (including those of us grading your problem sets!) you need to include an informative title and axis labels. To that end, use the xlab(), ylab(), and ggtitle() commands.

```
ggplot(state_data, aes(x = Population)) +
  geom_histogram() +
  xlab("Population (thousands)") +
  ylab("Number of states") +
  ggtitle("Some states are big, but most are small")
```

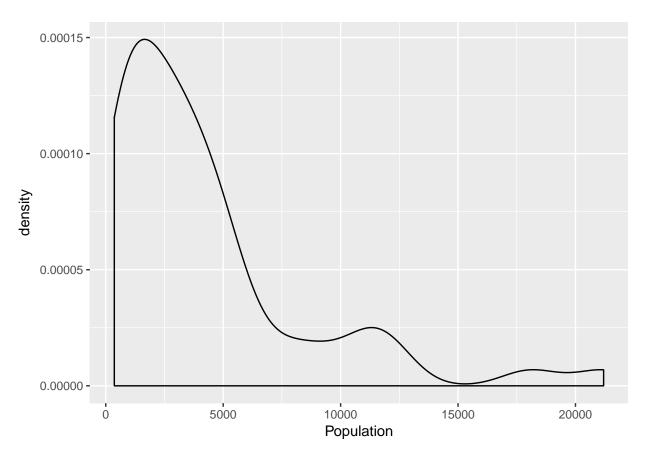
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

Some states are big, but most are small



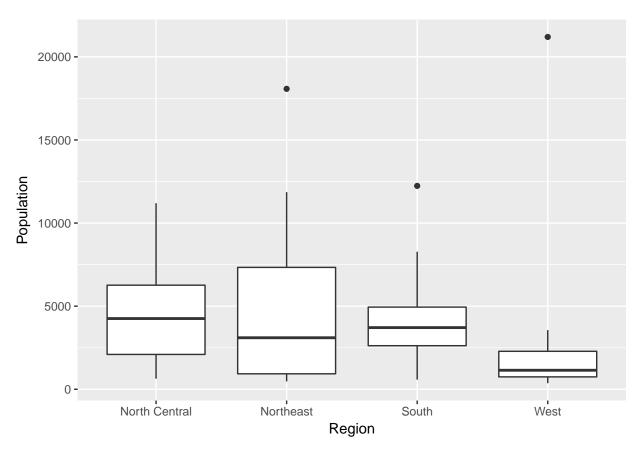
The density plot is a close relative of the histogram. It provides a smooth estimate of the probability density function of the data. Accordingly, the area under the density plot integrates to one. Depending on your purposes, this can make the y-axis of a density plot easier or (usually) harder to interpret than the count given by a histogram.





The box plot is a common way to look at the distribution of a continuous variable across different levels of a categorical variable.

```
ggplot(state_data, aes(x = Region, y = Population)) +
  geom_boxplot()
```

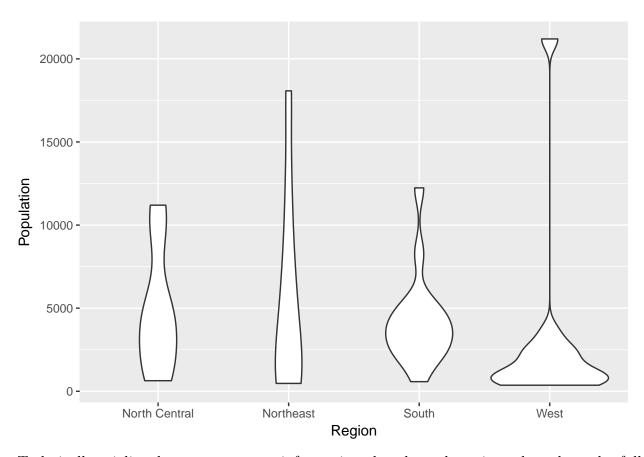


A box plot consists of the following components:

- Center line: median of the data
- Bottom of box: 25th percentile
- Top of box: 75th percentile
- Lower "whisker": range of observations no more than 1.5 IQR (height of box) below the 25th percentile
- Upper "whisker": range of observations no more than 1.5 IQR above the 75th percentile
- Plotted points: any data lying outside the whiskers

If you want to skip the summary and plot the full distribution of a variable across categories, you can use a violin plot.

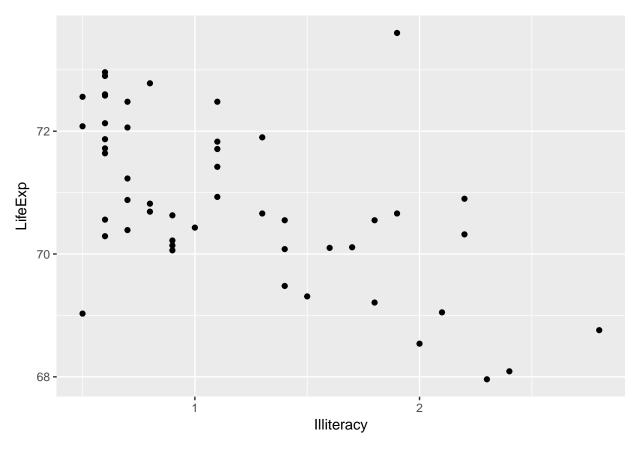
```
ggplot(state_data, aes(x = Region, y = Population)) +
  geom_violin()
```



Technically, violin plots convey more information than box plots since they show the full distribution. However, readers aren't as likely to be familiar with a violin plot. It's harder to spot immediately where the median is (though you could add that to the plot if you wanted). Plus, violin plots look goofy with outliers—see the "West" column above—whereas box plots handle them easily.

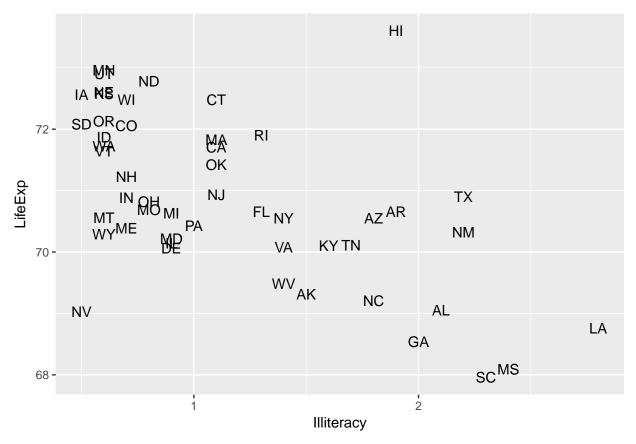
For visualizing relationships between continuous variables, nothing beats the scatterplot.

```
ggplot(state_data, aes(x = Illiteracy, y = LifeExp)) +
  geom_point()
```



When you're plotting states or countries, a hip thing to do is plot abbreviated names instead of points. To do that, you can use <code>geom_text()</code> instead of <code>geom_point()</code>, supplying an additional aesthetic argument telling ggplot where to draw the labels from.

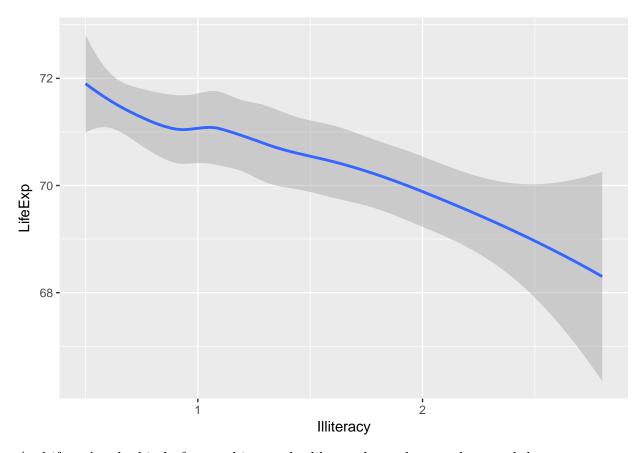
```
ggplot(state_data, aes(x = Illiteracy, y = LifeExp)) +
geom_text(aes(label = Abbrev))
```



Maybe it's overwhelming to look at all that raw data and you just want a summary. For example, maybe you want an estimate of expected LifeExp for each value of Illiteracy. This is called the *conditional expectation* and will be the subject of much of the rest of the course. For now, just now that you can calculate a smoothed conditional expectation via geom_smooth().

```
ggplot(state_data, aes(x = Illiteracy, y = LifeExp)) +
  geom_smooth()
```

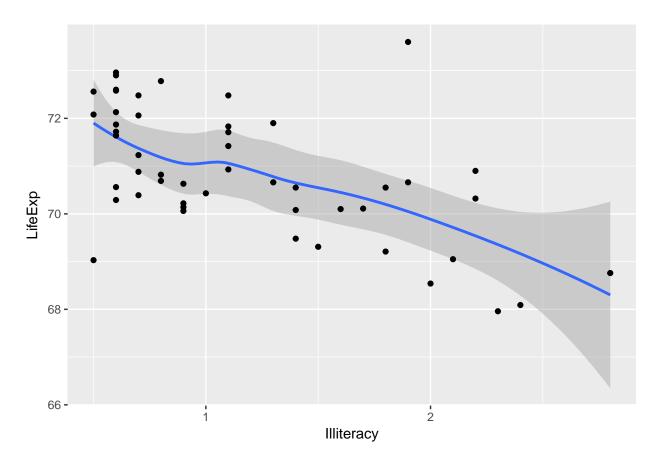
```
## `geom_smooth()` using method = 'loess'
```



And if you're the kind of overachiever who likes to have the raw data and the summary, you can do it. Just add them both to the ggplot() call.

```
ggplot(state_data, aes(x = Illiteracy, y = LifeExp)) +
  geom_smooth() +
  geom_point()
```

```
## `geom_smooth()` using method = 'loess'
```



4.2 Saving Plots

When you're writing in R Markdown, the plots go straight into your document without much fuss. Odds are, your dissertation will contain plots but won't be written in R Markdown, which means you'll need to learn how to save them.

It's pretty simple:

- 1. Assign your ggplot() call to a variable.
- 2. Pass that variable to the ggsave() function.

```
pop_hist <- ggplot(state_data, aes(x = Population)) +
   geom_histogram()

ggsave(filename = "pop-hist.pdf",
        plot = pop_hist,
        width = 6,
        height = 3)</pre>
```

If you want plot types other than PDF, just set a different extension. See ?ggsave for the possibilities.

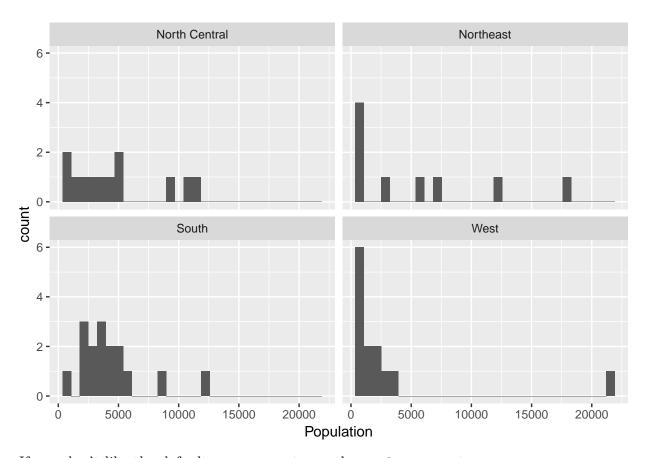
4.3 Faceting

Suppose you want to split the data into subgroups, as defined by some variable in the data (e.g., the region states are in), and make the same plot for each subgroup. ggplot's *faceting* functions, facet_wrap() and facet_grid(), make this easy.

To split up plots according to a single grouping variable, use facet_wrap(). This uses R's formula syntax, defined by the tilde ~, which you'll become well acquainted with once we start running regressions.

```
ggplot(state_data, aes(x = Population)) +
  geom_histogram() +
  facet_wrap(~ Region)
```

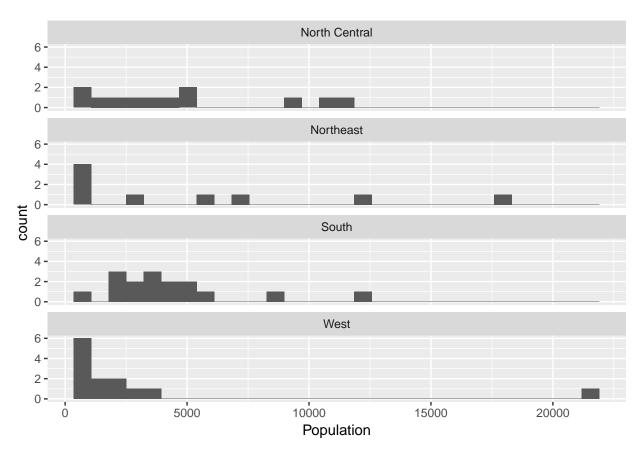
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



If you don't like the default arrangement, use the ncol argument.

```
ggplot(state_data, aes(x = Population)) +
  geom_histogram() +
  facet_wrap(~ Region, ncol = 1)
```

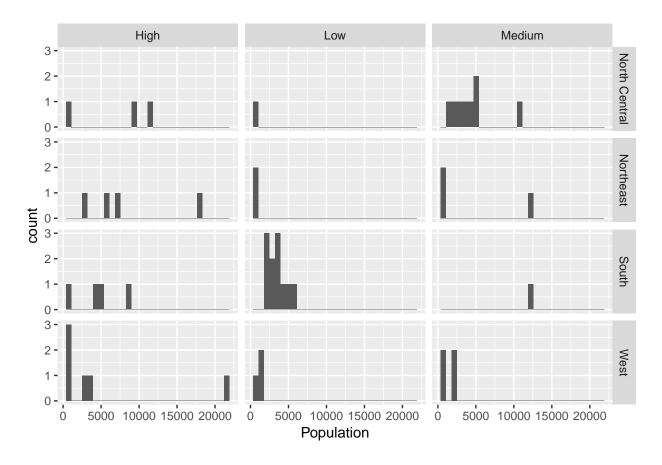
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



For two grouping variables, use facet_grid(), putting variables on both sides of the formula.

```
ggplot(state_data, aes(x = Population)) +
  geom_histogram() +
  facet_grid(Region ~ IncomeGroup)
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

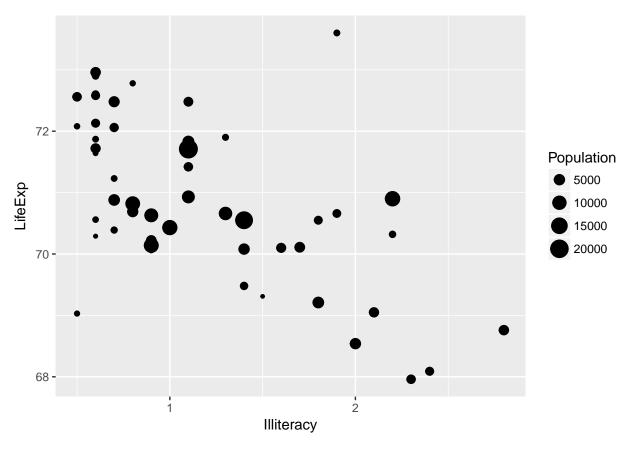


4.4 Aesthetics

Faceting is one way to incorporate information about additional variables into what would otherwise be a plot of just one or two variables. Aesthetics—which alter the appearance of particular plot features depending on the value of a variable—provide another way to do that.

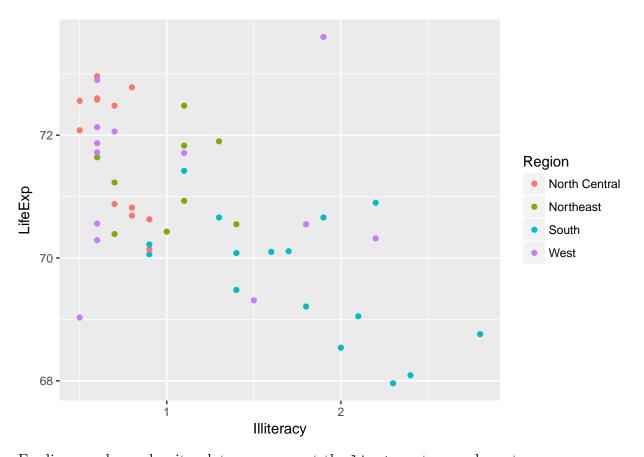
For example, when visualizing the relationship between statewide illiteracy and life expectancy, you might want larger states to get more visual weight. You can set the size aesthetic of the point geometry to vary according to the state's population.

```
ggplot(state_data, aes(x = Illiteracy, y = LifeExp)) +
  geom_point(aes(size = Population))
```



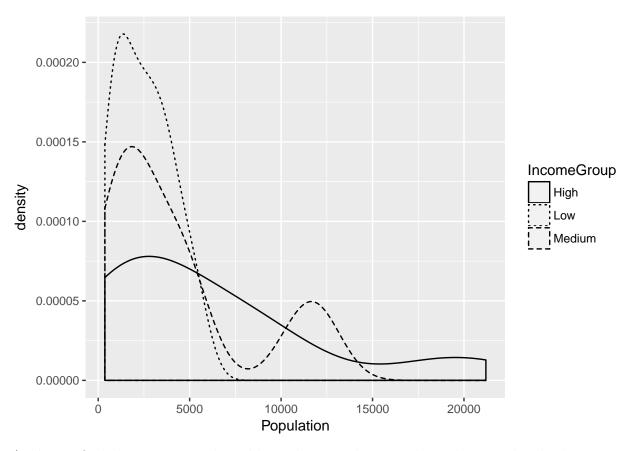
The **ggplot2** documentation lists the available aesthetics for each function. Another popular one is **colour**, which is great for on-screen display but not so much for the printed page. (And terrible for the colorblind!)

```
ggplot(state_data, aes(x = Illiteracy, y = LifeExp)) +
  geom_point(aes(colour = Region))
```



For line graphs or density plots, you can set the linetype to vary by category.

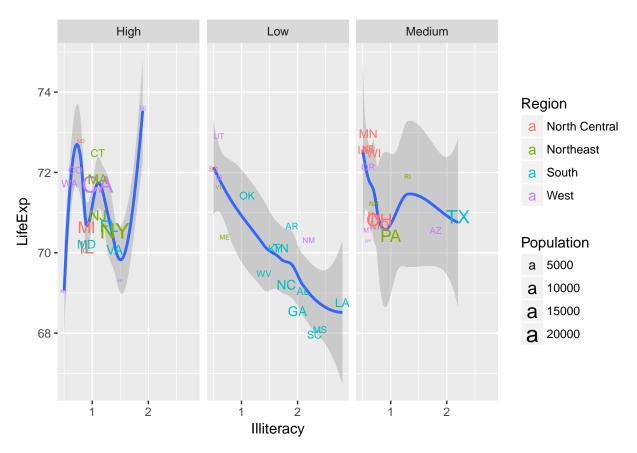
```
ggplot(state_data, aes(x = Population)) +
  geom_density(aes(linetype = IncomeGroup))
```



(I always find these incomprehensible with more than two lines, but maybe that's just me.) You can use multiple aesthetics together, and you can even combine aesthetics with faceting, as in the following example.

```
ggplot(state_data, aes(x = Illiteracy, y = LifeExp)) +
  geom_smooth() +
  geom_text(aes(label = Abbrev, colour = Region, size = Population)) +
  facet_wrap(~ IncomeGroup)
```

`geom_smooth()` using method = 'loess'



But the fact that you can do something doesn't mean you should. That plot is so cluttered that it's hard to extract the relevant information from it. Data visualizations should communicate a clear message to viewers without overwhelming them. To do this well takes practice, patience, and maybe even a bit of taste.

4.5 Appendix: Creating the Example Data

The example data comes from data on U.S. states in 1977 that are included with base R. See ?state.

Chapter 5

Bivariate Regression

The goal of empirical social science is usually to learn about the relationships between variables in the social world. Our goals might be descriptive: were college graduates more likely to vote for Clinton in 2016? Or causal: does receiving more education make a person more liberal on average? Or predictive: what kinds of voters should Democrats target in 2020 to have the best chance of victory?

The linear model is one of the simplest ways to model relationships between variables. Ordinary least squares regression is one of the easiest and (often) best ways to estimate the parameters of the linear model. Consequently, a linear model estimated by OLS is the starting point for many analyses. We will start with the simplest case: regression on a single covariate.

5.1 Probability Refresher

Let Y be a random variable that takes values in the finite set \mathcal{Y} according to the probability mass function $f_Y : \mathcal{Y} \to [0,1]$. The expected value (aka expectation) of Y is the weighted average of each value in \mathcal{Y} , where the weights are the corresponding probabilities:

$$E[Y] = \sum_{y \in \mathcal{Y}} y \, f_Y(y); \tag{5.1}$$

For a continuous random variable Y on \mathbb{R} with probability density function f_Y , the expected value is the analogous integral:

$$E[Y] = \int y \, f_Y(y) \, dy. \tag{5.2}$$

Now suppose (X, Y) is a pair of discrete random variables drawn according to the joint mass function f_{XY} on $\mathcal{X} \times \mathcal{Y}$, with respective marginal mass functions f_X and f_Y .¹ Recall the

¹The marginal mass function, if you don't recall, is $f_X(x) = \sum_{y \in \mathcal{Y}} f_{XY}(x, y)$. In the continuous case, the marginal density function is $f_X(x) = \int f_{XY}(x, y) \, dy$.

formula for conditional probability,

$$\Pr(Y = y \mid X = x) = \frac{\Pr(X = x, Y = y)}{\Pr(X = x)} = \frac{f_{XY}(x, y)}{f_X(x)}.$$
 (5.3)

For each $x \in \mathcal{X}$, we have the conditional mass function

$$f_{Y|X}(y \mid x) = \frac{f_{XY}(x, y)}{f_X(x)}$$
 (5.4)

and corresponding conditional expectation

$$E[Y|X = x] = \sum_{y \in \mathcal{Y}} y \, f_{Y|X}(y|x). \tag{5.5}$$

For continuous random variables, the conditional expectation is

$$E[Y|X = x] = \int y \, f_{Y|X}(y|x) \, dy, \tag{5.6}$$

where $f_{Y|X}$ is the conditional density function.

The variance of a random variable Y is

$$V[Y] = E[(Y - E[Y])^{2}]. (5.7)$$

Given a sample Y_1, \ldots, Y_N of observations of Y, we usually estimate V[Y] with the sample variance

$$S_Y^2 = \frac{1}{N-1} \sum_n (Y_n - \bar{Y})^2, \tag{5.8}$$

where \bar{Y} is the sample mean and \sum_n denotes summation from n=1 to N.

Similarly (in fact a generalization of the above), the covariance between random variables X and Y is

$$Cov[X, Y] = E[(X - E[X])(Y - E[Y])],$$

which we estimate with the sample covariance

$$S_{XY} = \frac{1}{N-1} \sum_{n} (X_n - \bar{X})(Y_n - \bar{Y}). \tag{5.9}$$

A fun fact about the sample covariance is that

$$S_{XY} = \frac{1}{N-1} \sum_{n} (X_n - \bar{X})(Y_n - \bar{Y})$$
 (5.10)

$$= \frac{1}{N-1} \left[\sum_{n} X_n (Y_n - \bar{Y}) + \sum_{n} \bar{X} (Y_n - \bar{Y}) \right]$$
 (5.11)

$$= \frac{1}{N-1} \left[\sum_{n} X_n (Y_n - \bar{Y}) + \bar{X} \sum_{n} (Y_n - \bar{Y}) \right]$$
 (5.12)

$$= \frac{1}{N-1} \sum_{n} X_n (Y_n - \bar{Y}). \tag{5.13}$$

If we had split up the second term instead of the first, we would see that

$$S_{XY} = \frac{1}{N-1} \sum_{n} Y_n (X_n - \bar{X})$$

as well.

Since the (sample) variance is a special case of the (sample) covariance, by the same token we have

$$S_Y^2 = \frac{1}{N-1} \sum_n Y_n (Y_n - \bar{Y}). \tag{5.14}$$

5.2 The Linear Model

Suppose we observe a sequence of N draws from f_{XY} , denoted $(X_1, Y_1), (X_2, Y_2), \ldots, (X_N, Y_N)$, or $\{(X_n, Y_n)\}_{n=1}^N$ for short. What can we learn about the relationship between X and Y from this sample of data?

If we were really ambitious, we could try to estimate the shape of the full joint distribution, f_{XY} . The joint distribution encodes everything there is to know about the relationship between the two variables, so it would be pretty useful to know. But except in the most trivial cases, it would be infeasible to estimate f_{XY} precisely. If X or Y can take on more than a few values, estimating the joint distribution would require an amount of data that we're unlikely to have.²

The first way we simplify our estimation task is to set our sights lower. Let Y be the response or the dependent variable—i.e., the thing we want to explain. We call X the covariate or the independent variable. Instead of estimating the full joint distribution, we're just going to try to learn the conditional expectation, E[Y | X]. In other words, for each potential value of the covariate, what is the expected value of the response? This will allow us to answer questions like whether greater values of X are associated with greater values of Y.

²This problem only gets worse as we move from bivariate into multivariate analysis, a phenomenon called the *curse of dimensionality*.

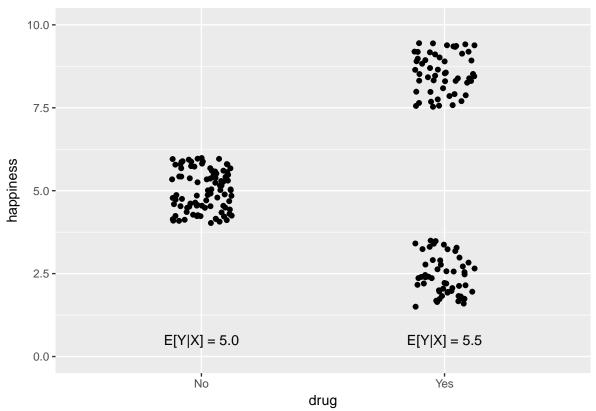
Two important things about the estimation of conditional expectations before we go any further.

1. Statements about conditional expectations are not causal. If Y is rain and X is umbrella sales, we know E[Y|X] increases with X, but that doesn't mean umbrella sales make it rain.

We will spend some time in the latter part of the course on how to move from conditional expectations to causality. Then, in Stat III, you will learn about causal inference in excruciating detail.

2. The conditional expectation doesn't give you everything you'd want to know about the relationship between variables.

As a hypothetical example, suppose I told you that taking a particular drug made people happier on average. In other words, $E[{\rm Happiness} \,|\, {\rm Drug}] > E[{\rm Happiness} \,|\, {\rm No} \,\, {\rm Drug}]$. Sounds great! Then imagine the dose-response graph looked like this:



The fact that expected happiness rises by half a point doesn't quite tell the whole story.

In spite of these caveats, conditional expectation is a really useful tool for summarizing the relationship between variables.

If X takes on sufficiently few values (and we have enough data), we don't need to model the conditional expectation function. We can just directly estimate E[Y|X=x] for each $x \in \mathcal{X}$. The graph above, where there are just two values of X, is one example.

But if X is continuous, or even if it is discrete with many values, estimating E[Y|X] for each distinct value is infeasible. In this case, we need to model the relationship. The very simplest choice—and thus the default for social scientists—is to model the conditional expectation of Y as a linear function of X:

$$E[Y \mid X] = \alpha + \beta X. \tag{5.15}$$

In this formulation, α and β are the parameters to be estimated from sample data. We call α and β "coefficients," with α the "intercept" and β the "slope." Regardless of how many different values X might take on, we only need to estimate two parameters of the linear model.

Exercise your judgment before using a linear model. Ask yourself, is a linear conditional expectation function at least minimally plausible? Not perfect—just a reasonable approximation. If X is years of education and Y is annual income, the answer is probably yes (depending on the population!). But if X is hour of the day (0-24) and Y is the amount of traffic on I-65, probably not.

To obtain the linear conditional expectation, we usually assume the following model of the response variable:

$$Y_n = \alpha + \beta X_n + \epsilon_n, \tag{5.16}$$

where ϵ_n is "white noise" error with the property

$$E[\epsilon_n \mid X_1, \dots X_N] = 0. \tag{5.17}$$

You can think of ϵ_n as the summation of everything besides the covariate X_n that affects the response Y_n . The assumption that $E[\epsilon_n | X_1, \dots, X_N] = 0$ implies that these external factors are uncorrelated with the covariate. This is not a trivial technical condition that you can ignore—it is a substantive statement about the variables in your model. It requires justification, and it is difficult to justify.

For now we will proceed assuming that our data satisfy the above conditions. Later in the course, we will talk about how to proceed when $E[\epsilon_n \mid X_1, \dots, X_N] \neq 0$, and you will learn much more about such strategies in Stat III.

5.3 Least Squares

To estimate the parameters of the linear model, we will rely on a mathematically convenient method called *least squares*. We will see that this method not only is convenient, but also has nice statistical properties.

Given a parameter estimate $(\hat{\alpha}, \hat{\beta})$, define the *residual* of the *n*'th observation as the difference between the true and predicted values:

$$e_n(\hat{\alpha}, \hat{\beta}) = Y_n - \hat{\alpha} - \hat{\beta}X_n. \tag{5.18}$$

The residual is directional. The residual is positive when the regression line falls below the observation, and vice versa when it is negative.

We would like the regression line to lie close to the data—i.e., for the residuals to be small in magnitude. "Close" can mean many things, so we need to be a bit more specific to derive an estimator. The usual one, *ordinary least squares*, is chosen to minimize the sum of squared errors.

$$SSE(\hat{\alpha}, \hat{\beta}) = \sum_{n} e_n(\hat{\alpha}, \hat{\beta})^2.$$

(Throughout the rest of this chapter, I write \sum_n as shorthand for $\sum_{n=1}^N$.) When we focus on squared error, we penalize a positive residual the same as a negative residual of the same size. Moreover, we penalize one big residual proportionally more than a few small ones.

It is important to keep the linear model and ordinary least squares distinct in your mind. The linear model is a model of the data. Ordinary least squares is one estimator—one among many—of the parameters of the linear model. Assuming a linear model does not commit you to estimate it with OLS if you think another estimator is more appropriate. And using OLS does not necessarily commit you to the linear model, as we will discuss when we get to multiple regression.

To derive the OLS estimator, we will derive the conditions for minimization of the sum of squared errors. The SSE is a quadratic and therefore continuously differentiable function of the estimands, $\hat{\alpha}$ and $\hat{\beta}$. You will remember from calculus that, at any extreme point of a continuous function, all its partial derivatives equal zero. To derive necessary conditions for minimization,³ we can take the derivatives of the SSE and set them to equal zero.

The derivative with respect to the intercept is

$$\frac{\partial \operatorname{SSE}(\hat{\alpha}, \hat{\beta})}{\partial \hat{\alpha}} = -2 \sum_{n} (Y_n - \hat{\alpha} - \hat{\beta} X_n).$$

Setting this to equal zero gives

$$\hat{\alpha} = \frac{1}{N} \sum_{n} (Y_n - \hat{\beta} X_n) = \bar{Y} - \hat{\beta} \bar{X}.$$

This gives us one important property of OLS: the regression line estimated by OLS always passes through (\bar{X}, \bar{Y}) .

The derivative with respect to the slope is

$$\frac{\partial \operatorname{SSE}(\hat{\alpha}, \hat{\beta})}{\partial \hat{\beta}} = -2 \sum_{n} X_n (Y_n - \hat{\alpha} - \hat{\beta} X_n).$$

³In fact, since the SSE function is strictly convex, these conditions are sufficient for global minimization.

Setting this equal to zero and substituting in the expression for $\hat{\alpha}$ we derived above gives

$$\sum_{n} X_n(Y_n - \bar{Y}) = \hat{\beta} \sum_{n} X_n(X_n - \bar{X}).$$

As long as the sample variance of X is non-zero (i.e., X is not a constant), we can divide to solve for $\hat{\beta}$:

$$\hat{\beta} = \frac{\sum_{n} X_{n} (Y_{n} - \bar{Y})}{\sum_{n} X_{n} (X_{n} - \bar{X})} = \frac{S_{XY}}{S_{X}^{2}}.$$

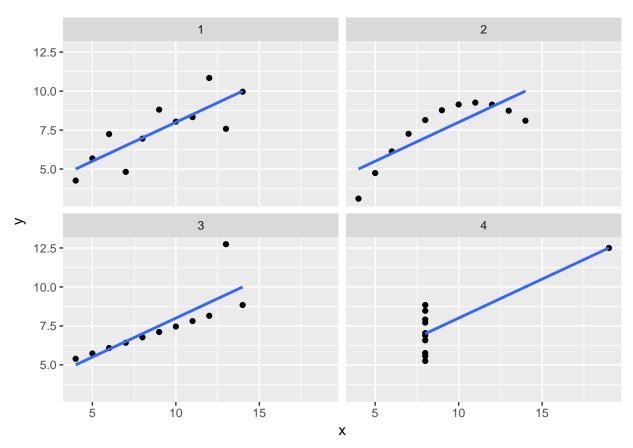
Combining these two results, we have the OLS estimators of the intercept and slope of the bivariate linear model. We write them as functions of $(X_1, \ldots, X_N, Y_1, \ldots, Y_N)$, or (X, Y) for short, to emphasize that an estimator is a statistic, which in turn is a function of sample data. We place the "OLS" subscript on them to emphasize that there are many estimators of these parameters, of which OLS is just one (good!) choice.

$$\hat{\alpha}_{\text{OLS}}(X,Y) = \bar{Y} - \frac{S_{XY}}{S_X^2} \bar{X},$$

$$\hat{\beta}_{\text{OLS}}(X,Y) = \frac{S_{XY}}{S_X^2}.$$

Regression is a convenient way to summarize the relationship between variables, but it is a complement to—not a substitute for—graphical analysis. The statistician Francis Anscombe found that OLS yields nearly identical regression lines for all four of the datasets in the following graph:

⁴This is a bit of an abuse of notation, since previously I used X and Y to refer to the random variables and now I'm using them to refer to vectors of sample data. Sorry.



Unless your data all lie along a line, the regression line estimated by OLS will not predict the data perfectly. Let the *residual sum of squares* be the squared error left over by OLS,

$$RSS = SSE(\hat{\alpha}_{OLS}, \hat{\beta}_{OLS}),$$

and let the *total sum of squares* be the squared error that would result from a horizontal regression line through the mean of Y,

$$TSS = SSE(\bar{Y}, 0).$$

The \mathbb{R}^2 statistic is the proportion of "variance explained" by X, calculated as

$$R^2 = 1 - \frac{\text{RSS}}{\text{TSS}}.$$

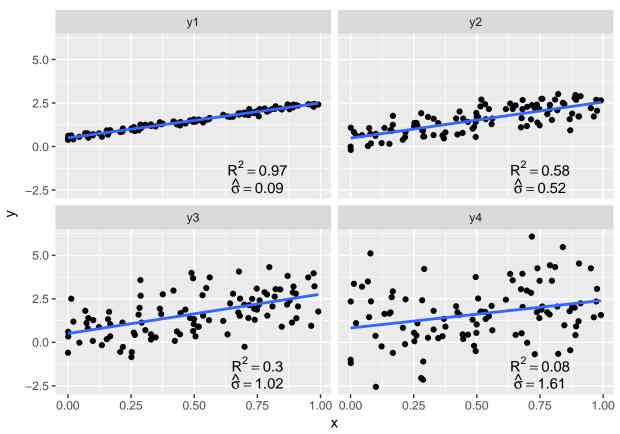
If the regression line is flat, in which case $\hat{\beta}_{OLS} = 0$ and RSS = TSS, we have $R^2 = 0$. Conversely, if the regression line fits perfectly, in which case RSS = 0, we have $R^2 = 1$.

A statistic that is often more useful than R^2 is the *residual variance*. The residual variance is (almost) the sample variance of the regression residuals, calculated as

$$\hat{\sigma}^2 = \frac{1}{N-2} \sum_{n} e_n (\hat{\alpha}_{\text{OLS}}, \hat{\beta}_{\text{OLS}})^2 = \frac{\text{RSS}}{N-2}$$

Since bivariate regression uses two degrees of freedom (one for the intercept, one for the slope), we divide by N-2 instead of the usual N-1. The most useful quantity is $\hat{\sigma}$,

the square root of the residual variance. $\hat{\sigma}$ is measured in the same units as Y, and it is a measure of the spread of points around the regression line. If the residuals are roughly normally distributed, then we would expect roughly 95% of the data to lie within $\pm 2\hat{\sigma}$ of the regression line.



5.4 Properties

We didn't use any fancy statistical theory to derive the OLS estimator. We just found the intercept and slope that minimize the sum of squared residuals. As it turns out, though, OLS indeed has some very nice statistical properties as an estimator of the linear model.

The first desirable property of OLS is that it is *unbiased*. Recall that an estimator $\hat{\theta}$ of the parameter θ is unbiased if $E[\hat{\theta}] = \theta$. This doesn't mean the estimator always gives us the right answer, just that on average it is not systematically biased upward or downward. In other words, if we could take many many samples and apply the estimator to each of them, the average would equal the true parameter.

We will begin by showing that the OLS estimator of the slope is unbiased; i.e., that $E[\hat{\beta}_{\text{OLS}}(X,Y)] = \beta$. At first, we'll take the conditional expectation of the slope estimator,

treating the covariates (X_1, \ldots, X_N) as fixed.

$$E[\hat{\beta}_{OLS}(X,Y) \mid X] = E\left[\frac{S_{XY}}{S_X^2} \mid X\right]$$

$$= E\left[\frac{\sum_n Y_n(X_n - \bar{X})}{\sum_n X_n(X_n - \bar{X})} \mid X\right]$$

$$= \frac{\sum_n E[Y_n \mid X](X_n - \bar{X})}{\sum_n X_n(X_n - \bar{X})}$$

$$= \frac{\sum_n (\alpha + \beta X_n)(X_n - \bar{X})}{\sum_n X_n(X_n - \bar{X})}$$

$$= \frac{\alpha \sum_n (X_n - \bar{X}) + \beta \sum_n X_n(X_n - \bar{X})}{\sum_n X_n(X_n - \bar{X})}$$

$$= \frac{\beta \sum_n X_n(X_n - \bar{X})}{\sum_n X_n(X_n - \bar{X})}$$

$$= \beta.$$

It then follows from the law of iterated expectation⁵ that

$$E[\hat{\beta}_{OLS}(X,Y)] = \beta.$$

Then, for the intercept, we have

$$E[\hat{\alpha}_{OLS}(X,Y) \mid X] = E[\bar{Y} - \hat{\beta}_{OLS}(X,Y)\bar{X} \mid X]$$

$$= E[\bar{Y} \mid X] - E[\hat{\beta}_{OLS}(X,Y) \mid X]\bar{X}$$

$$= E\left[\frac{1}{N}\sum_{n}Y_{n} \mid X\right] - \beta\bar{X}$$

$$= E\left[\frac{1}{N}\sum_{n}(\alpha + \beta X_{n} + \epsilon_{n}) \mid X\right] - \beta\bar{X}$$

$$= \frac{1}{N}\sum_{n}E[\alpha + \beta X_{n} + \epsilon_{n} \mid X] - \beta\bar{X}$$

$$= \frac{1}{N}\sum_{n}\alpha + \frac{\beta}{N}\sum_{n}X_{n} + \frac{1}{N}\sum_{n}E[\epsilon_{n} \mid X] - \beta\bar{X}$$

$$= \alpha + \beta\bar{X} - \beta\bar{X}$$

$$= \alpha.$$

As with the slope, this conditional expectation gives us the unconditional expectation we want:

$$E[\hat{\alpha}_{\text{OLS}}(X,Y)] = \alpha.$$

To sum up: as long as the crucial condition $E[\epsilon_n | X_1, \dots, X_N] = 0$ holds, then OLS is an unbiased estimator of the parameters of the linear model.

⁵For random variables A and B, $E[f(A,B)] = E_A[E_B[f(A,B) \mid A]] = E_B[E_A[f(A,B) \mid B]].$

Another important property of OLS is that it is *consistent*. Informally, this means that in sufficiently large samples, the OLS estimates $(\hat{\alpha}_{OLS}, \hat{\beta}_{OLS})$ are very likely to be close to the true parameter values (α, β) . Another way to think of consistency is that, as $N \to \infty$, the bias and variance of the OLS estimator both go to zero.⁶

Of course the bias "goes to" zero, since OLS is unbiased. The real trick to proving consistency is to show that the variance goes to zero. If you wanted to do that for the slope estimate, you'd derive an expression for

$$V[\hat{\beta}_{\text{OLS}}] = E[(\hat{\beta}_{\text{OLS}} - E[\hat{\beta}_{\text{OLS}}])^2] = E[(\hat{\beta}_{\text{OLS}} - \beta)^2]$$

and show that

$$\lim_{N \to \infty} V[\hat{\beta}_{\text{OLS}}] = 0.$$

This takes more algebra than we have time for, so I leave it as an exercise for the reader.

5.5 Appendix: Regression in R

We will be using the **tidyverse** package as always, the **car** package for the **Prestige** data, and the **broom** package for its convenient post-analysis functions.

```
library("tidyverse")
library("car")
library("broom")
```

Let's take a look at Prestige, which records basic information (including perceived prestige) for a variety of occupations.

```
head(Prestige)
```

```
##
                        education income women prestige census type
## gov.administrators
                            13.11
                                   12351 11.16
                                                    68.8
                                                            1113 prof
## general.managers
                            12.26
                                   25879 4.02
                                                            1130 prof
                                                    69.1
## accountants
                            12.77
                                    9271 15.70
                                                    63.4
                                                            1171 prof
## purchasing.officers
                            11.42
                                    8865
                                          9.11
                                                    56.8
                                                            1175 prof
                                                    73.5
## chemists
                            14.62
                                    8403 11.68
                                                            2111 prof
## physicists
                            15.64
                                   11030 5.13
                                                    77.6
                                                            2113 prof
```

Suppose we want to run a regression of prestige on education. We will use the lm() function, which stands for *linear model*. This will employ the "formula" syntax that you previously saw when faceting in ggplot. The basic syntax of a formula is response ~ covariate,

⁶What I am describing here is *mean square consistency*, which is stronger than the broadest definitions of consistency in statistical theory.

where response and covariate are the names of the variables in question. In this case, with prestige (note that the variable is lowercase, while the dataset is capitalized) as the response and education as the covariate:

```
lm(prestige ~ education, data = Prestige)
```

```
##
## Call:
## lm(formula = prestige ~ education, data = Prestige)
##
## Coefficients:
## (Intercept) education
## -10.73 5.36
```

You'll notice that didn't give us very much. If you've previously used statistical programs like Stata, you might expect a ton of output at this point. It's all there in R too, but R has a different philosophy about models. R sees the fitted model as an object in its own right—like a data frame, a function, or anything else you load or create in R. Therefore, to analyze regression results in R, you will typically save the regression results to a variable.

Like any other variable, you'll want to give your regression results meaningful names. I typically call them fit_ to indicate a fitted model, followed by some memorable description.

```
fit_educ <- lm(prestige ~ education, data = Prestige)</pre>
```

When you do this, the output doesn't get printed. To see the default output, just run the variable name, just like you would to see the content of a data frame:

```
fit_educ
```

```
##
## Call:
## lm(formula = prestige ~ education, data = Prestige)
##
## Coefficients:
## (Intercept) education
## -10.73 5.36
```

For a more detailed readout, use the summary() method:

```
summary(fit_educ)
```

```
##
## Call:
## lm(formula = prestige ~ education, data = Prestige)
## Residuals:
      Min
##
                1Q Median
                                3Q
                                       Max
## -26.040 -6.523
                     0.661
                             6.743
                                   18.164
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                -10.732
                             3.677
                                     -2.92
                                             0.0043
## education
                  5.361
                             0.332
                                     16.15
                                             <2e-16
## Residual standard error: 9.1 on 100 degrees of freedom
## Multiple R-squared: 0.723, Adjusted R-squared:
## F-statistic: 261 on 1 and 100 DF, p-value: <2e-16
```

This prints out a whole boatload of information, including inferential statistics that we're going to wait until later in the course to discuss how to interpret:

- The model you ran
- Basic statistics about the distribution of the residuals
- For each coefficient:
 - Parameter estimate
 - Standard error estimate
 - Test statistic for a hypothesis test of equality with zero
 - p-value associated with the test statistic
- $\hat{\sigma}$ (called the "residual standard error", a term seemingly unique to R)
- R^2 and an "adjusted" variant that accounts for the number of variables in the model
- F statistic, degrees of freedom, and associated p-value for a hypothesis test that every coefficient besides the intercept equals zero

Strangely, summary() doesn't give you the sample size. For that you must use nobs():

```
nobs(fit_educ)
```

```
## [1] 102
```

You can use a fitted model object to make predictions for new data. For example, let's make a basic data frame of education levels.

```
my_data <- data_frame(education = 8:16)
my_data</pre>
```

```
## # A tibble: 9 × 1
##
     education
##
         <int>
## 1
              8
## 2
              9
## 3
             10
## 4
             11
## 5
             12
## 6
             13
## 7
             14
## 8
             15
## 9
             16
```

To calculate the predicted level of prestige for each education level, use predict():

32.155 37.516 42.877 48.238 53.599 58.959 64.320 69.681 75.042

```
predict(fit_educ, newdata = my_data)
## 1 2 3 4 5 6 7 8 9
```

When using predict(), it is crucial that the newdata have the same column names as in the data used to fit the model.

You can also extract a confidence interval for each prediction:

```
## fit lwr upr
## 1 32.155 29.615 34.695
## 2 37.516 35.393 39.639
## 3 42.877 41.024 44.730
## 4 48.238 46.441 50.034
## 5 53.599 51.627 55.571
## 6 58.959 56.632 61.287
## 7 64.320 61.525 67.116
## 8 69.681 66.353 73.010
## 9 75.042 71.142 78.942
```

One of the problems with summary() and predict() is that they return inconveniently shaped output. The output of summary() is particularly hard to deal with. The broom package provides three utilities to help get model output into shape. The first is tidy(), which makes a tidy data frame out of the regression coefficients and the associated inferential statistics:

```
tidy(fit_educ)
```

```
## term estimate std.error statistic p.value
## 1 (Intercept) -10.7320 3.67709 -2.9186 4.3434e-03
## 2 education 5.3609 0.33199 16.1478 1.2863e-29
```

The second is glance(), which provides a one-row data frame containing overall model characteristics (e.g., R^2 and $\hat{\sigma}$):

```
glance(fit_educ)
```

```
## r.squared adj.r.squared sigma statistic p.value df logLik AIC ## 1 0.7228 0.72003 9.1033 260.75 1.2863e-29 2 -369 744.01 ## BIC deviance df.residual ## 1 751.88 8287 100
```

The third is augment(), which "augments" the original data—or new data you supply, as in predict()—with information from the model, such as predicted values.

```
# Lots of output, so only printing first 10 rows
head(augment(fit_educ), 10)
```

```
##
                .rownames prestige education .fitted .se.fit
                                                               .resid
                                                                          .hat
## 1
                              68.8
                                              59.549 1.19689
                                                              9.2509 0.017287
       gov.administrators
                                       13.11
## 2
        general.managers
                              69.1
                                       12.26
                                              54.992 1.03332 14.1076 0.012885
                              63.4
                                              57.726 1.12584
## 3
              accountants
                                       12.77
                                                             5.6736 0.015295
## 4
     purchasing.officers
                              56.8
                                       11.42 50.489 0.92936
                                                              6.3108 0.010422
                                       14.62 67.644 1.57269
                              73.5
## 5
                 chemists
                                                              5.8559 0.029846
                              77.6
## 6
               physicists
                                       15.64 73.112 1.86034 4.4879 0.041763
## 7
               biologists
                              72.6
                                       15.09 70.164 1.70291
                                                              2.4363 0.034993
               architects
                                       15.44 72.040 1.80254 6.0600 0.039208
## 8
                              78.1
## 9
          civil.engineers
                              73.1
                                       14.52 67.108 1.54561 5.9920 0.028827
        mining.engineers
                              68.8
                                       14.64 67.751 1.57814 1.0487 0.030053
## 10
##
                .cooksd .std.resid
      .sigma
      9.1010 0.00924267
## 1
                           1.02511
                           1.55981
## 2
      9.0372 0.01587881
```

```
9.1311 0.00306360
## 3
                           0.62807
## 4 9.1269 0.00255745
                           0.69688
## 5 9.1296 0.00656112
                           0.65310
## 6 9.1375 0.00552702
                           0.50362
     9.1458 0.00134578
                           0.27244
## 7
## 8 9.1280 0.00941104
                           0.67914
## 9 9.1287 0.00662109
                           0.66793
## 10 9.1485 0.00021198
                           0.11697
```

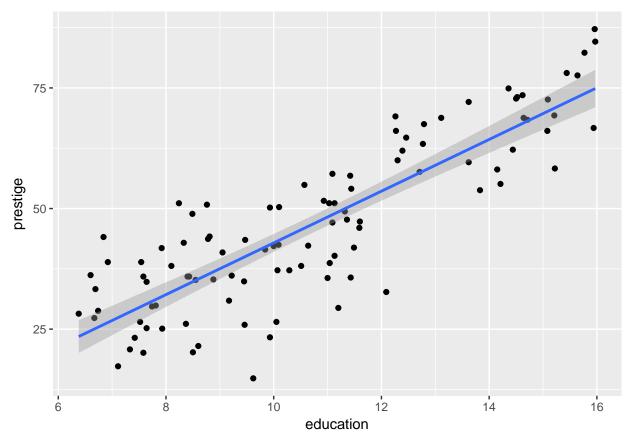
```
augment(fit_educ,
    newdata = my_data)
```

```
##
     education .fitted .se.fit
## 1
               32.155 1.28013
## 2
               37.516 1.07023
## 3
            10
               42.877 0.93407
            11 48.238 0.90555
## 4
## 5
            12 53.599 0.99397
            13
               58.959 1.17319
## 6
            14 64.320 1.40897
## 7
## 8
            15
               69.681 1.67763
## 9
            16
               75.042 1.96574
```

Notice that you get back more information for the data used to fit the model than for newly supplied data. The most important is .fitted, the predicted value. See ?augment.lm for what all the various output represents.

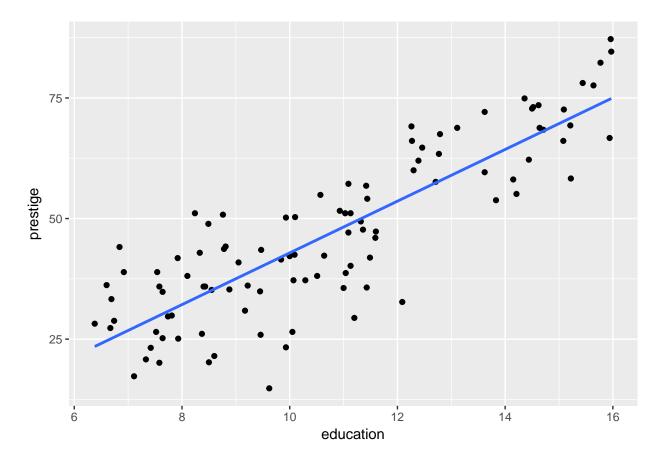
One last note on plotting regression lines with ggplot. Use geom_smooth(method = "lm").

```
ggplot(Prestige, aes(x = education, y = prestige)) +
  geom_point() +
  geom_smooth(method = "lm")
```



To get rid of the confidence interval:

```
ggplot(Prestige, aes(x = education, y = prestige)) +
  geom_point() +
  geom_smooth(method = "lm", se = FALSE)
```



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