

# Empirical Methods (17-803)

Introduction to Social Networks  
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# Benefits of Network Diversity

## **Egonetwork level**

One's diverse egonetwork can be more beneficial

## **Subgroup level**

Team with diverse members perform better

## **Network level**

Network with diverse connections are more robust

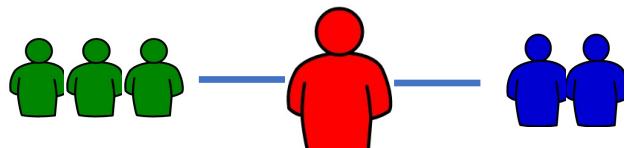
Today is about the local level (egonetwork and tie level)

# Two Related Concepts



## Network Bridging

- A shortcut that connects otherwise separated social contexts.
- Bridging ties are the conduits through which non-redundant information can flow through.



## Network Brokerage

- The separation among one's alters
- Alters likely come from different social groups

# Two Related Concepts



Bridging and brokering are closely related ideas.

From a community's perspective, a **bridging** tie that connects to a far away community can bring diversity to the community (ideas, information, etc.)

Silk road was a socio-cultural, geographical bridge

# Two Related Concepts



An individual bridges/brokers different communities

An individual **brokers** different communities and groups.

Information and other resources flow through the individual from one group to another

# Network Bridging

Dissertation: *Getting a Job*



Mark Granovetter

- Strength of weak ties:  
explaining the puzzling finding  
of job information acquisition  
through acquaintances, not  
close friends
- Benefits bridging to individual  
and group

**One of the most cited papers  
in the social sciences**

# Network Brokerage

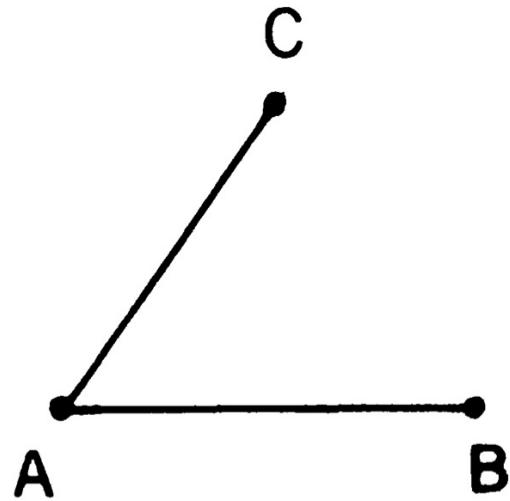


Extended the idea of bridging ties

- From ties to nodes
- Emphasis on individual's agency
- Benefits that accrue to individual

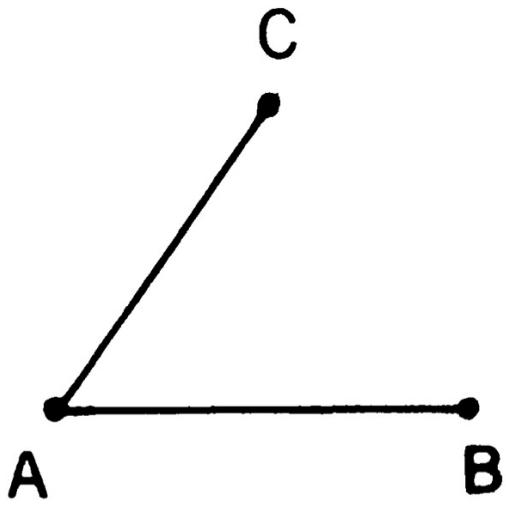
Ron Burt

# Bridging Ties



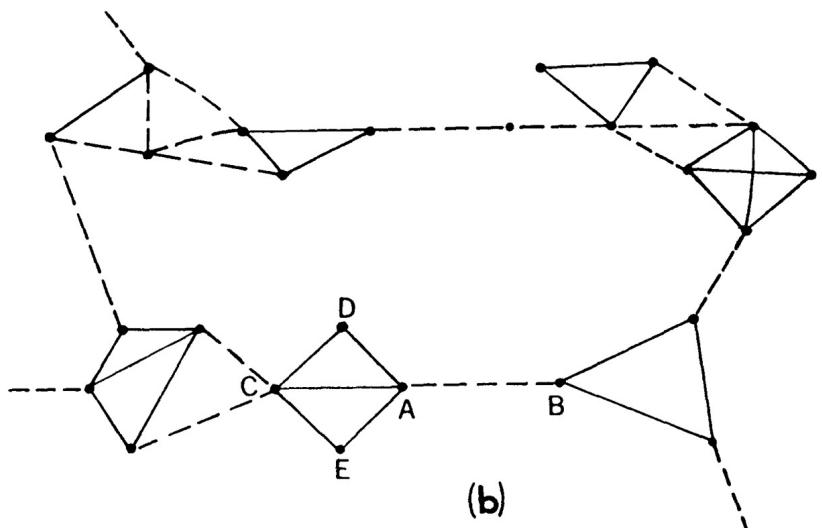
- Tie strength: interaction frequency, reciprocity, emotional intensity
- Forbidden triad: Due to people's desire for cognitive balance, one is likely to form a strong relationship with a close friend's close friend.
- Hence, a triad with only two "strong" ties are not likely. Because strong ties have the tendency to close the triad, they are not likely to be bridging ties.

# Bridging Ties



- On the other hand, acquaintances, or weak ties do not have embedding tendency
- There is much less psychological need for cognitive balance
- Weak ties interact infrequently, so less chance to form common neighbors.
- Hence, Weak ties are more likely to be bridges.
- Key assumption:  
Strong ties are embedded, weak ties are bridging

# Local Bridges



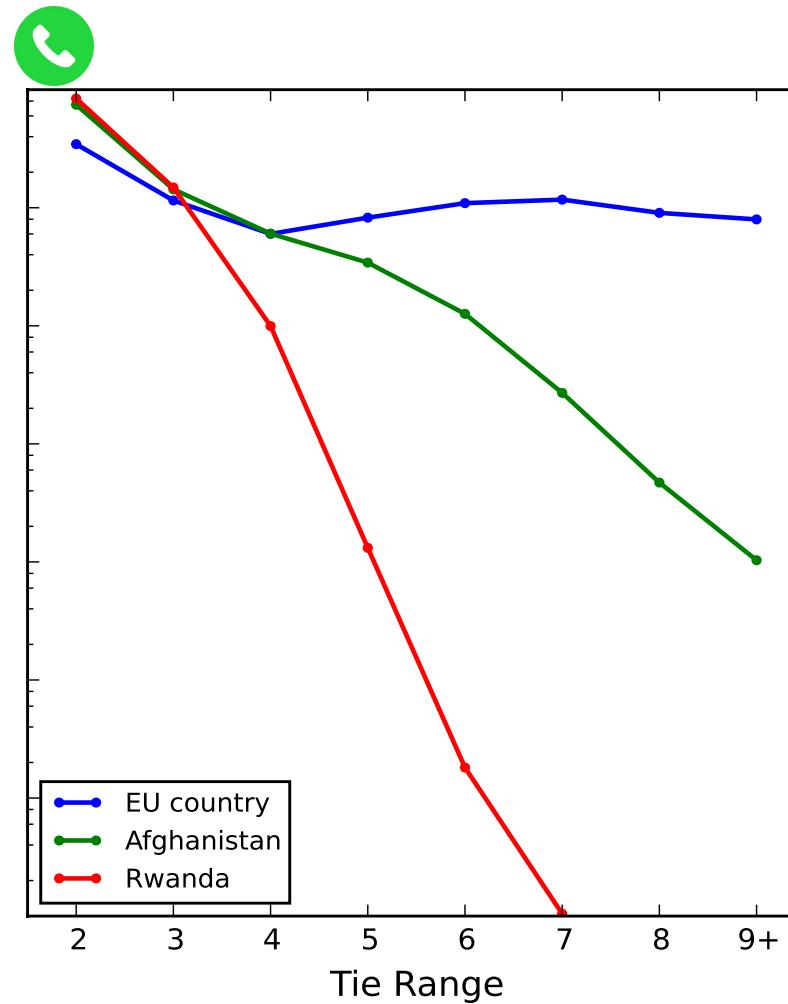
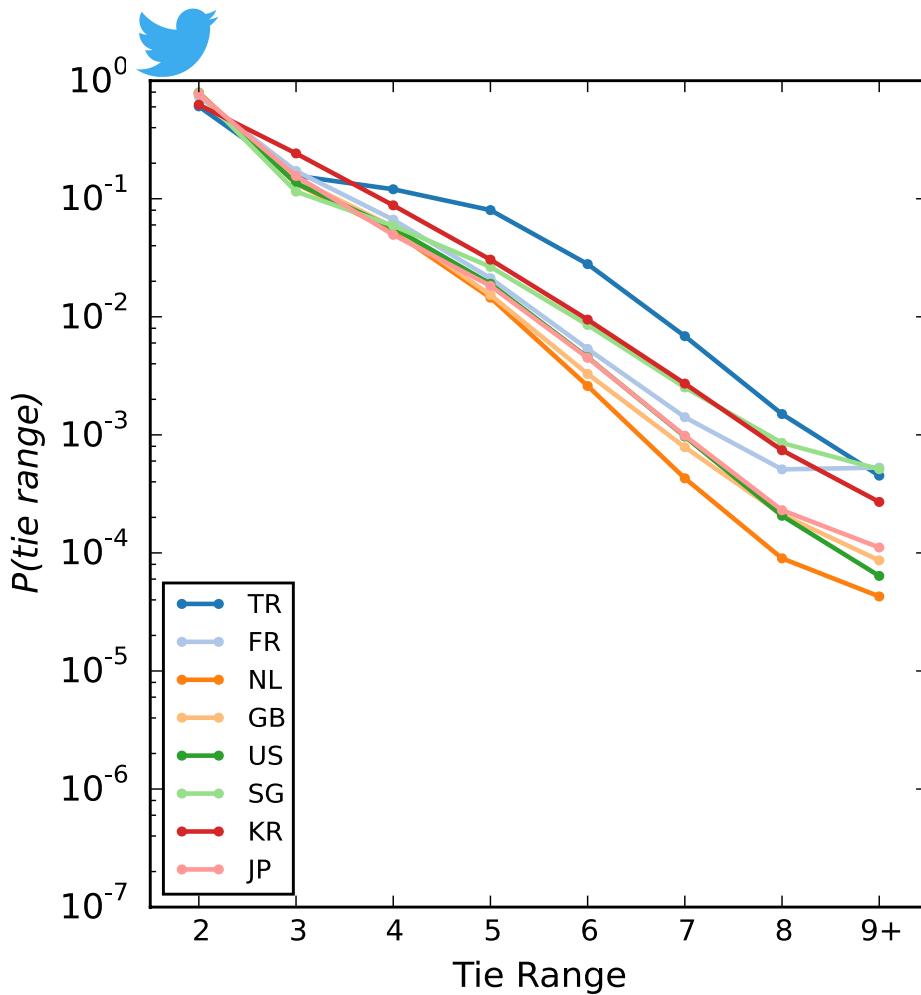
Granovetter created a measure of bridge length → “Local bridge of degree  $n$ ”

Bridge length of the A-B tie:  
- second shortest path length

This measure requires global network information, unmeasurable before internet

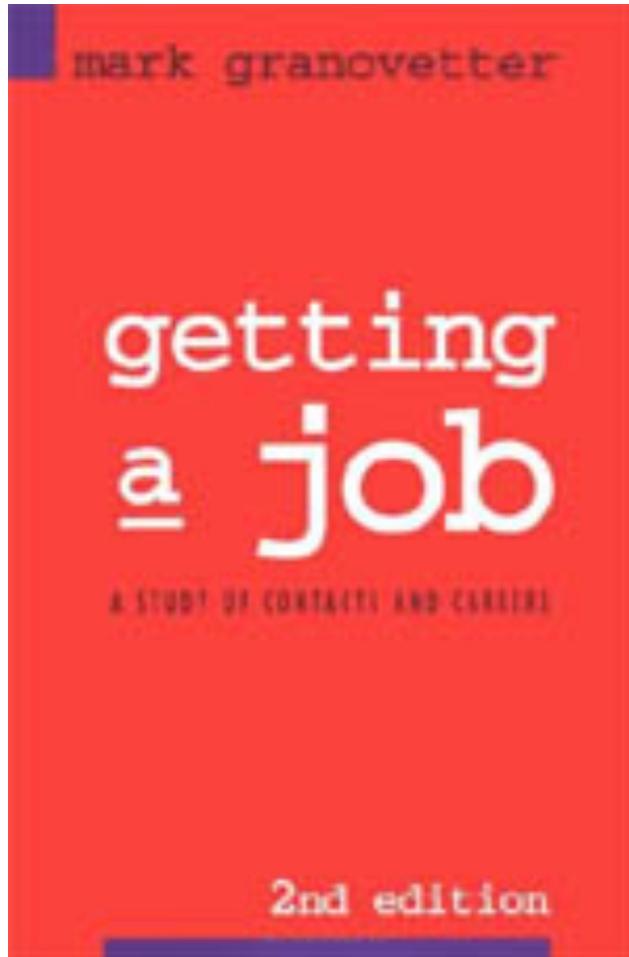
Weakness of ties was a good proxy for bridging ties

# Long-Range Ties Are Rare



Granovetter would  
not have discovered  
globally long bridging  
ties

# Weak Ties and Getting a Job

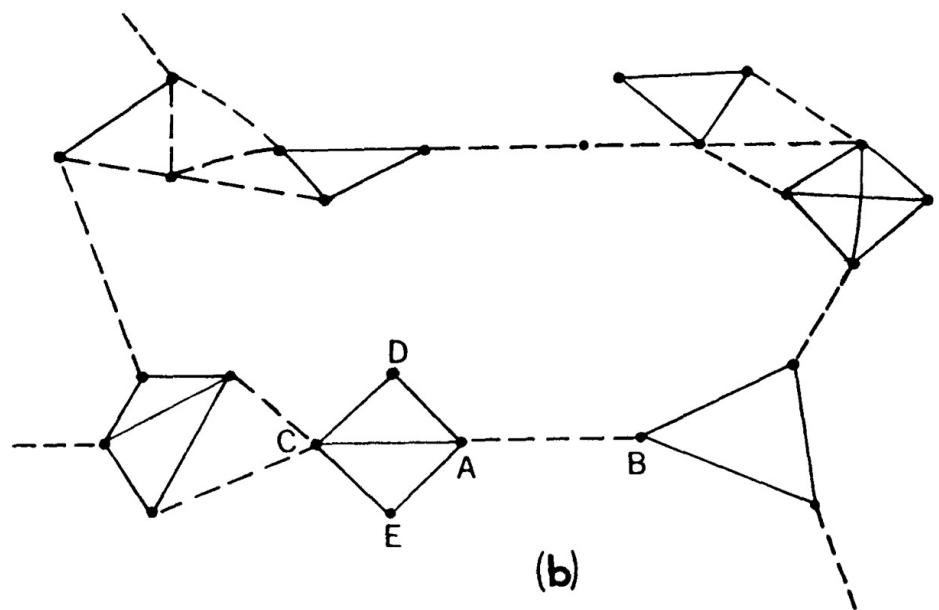


- From his dissertation work at Harvard, Granovetter discovers that people tend to find new job opportunities through acquaintances rather than close friends.

# Continuing Debates

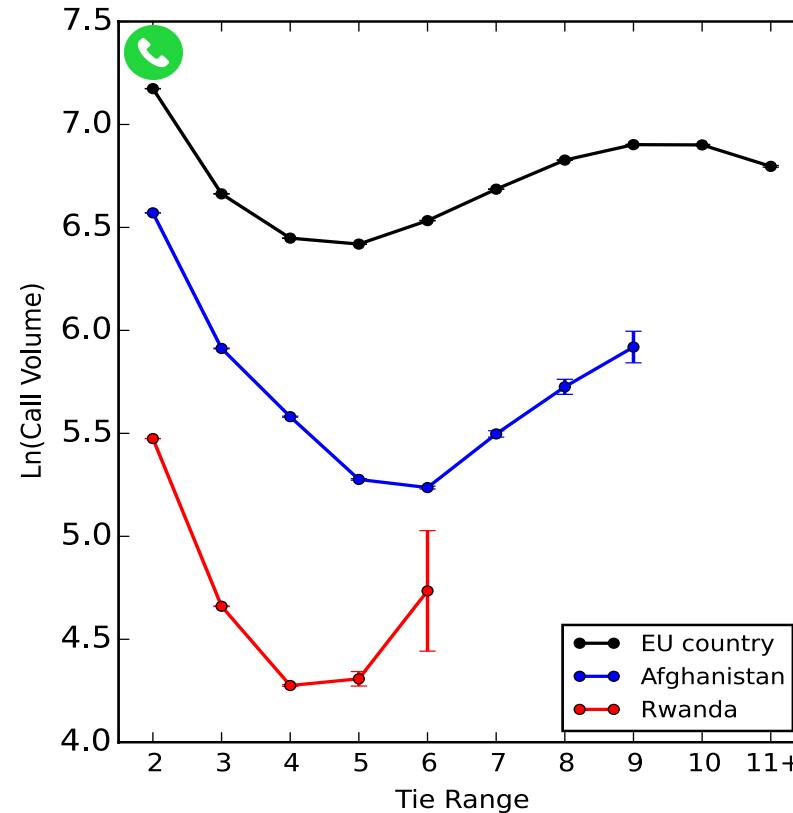
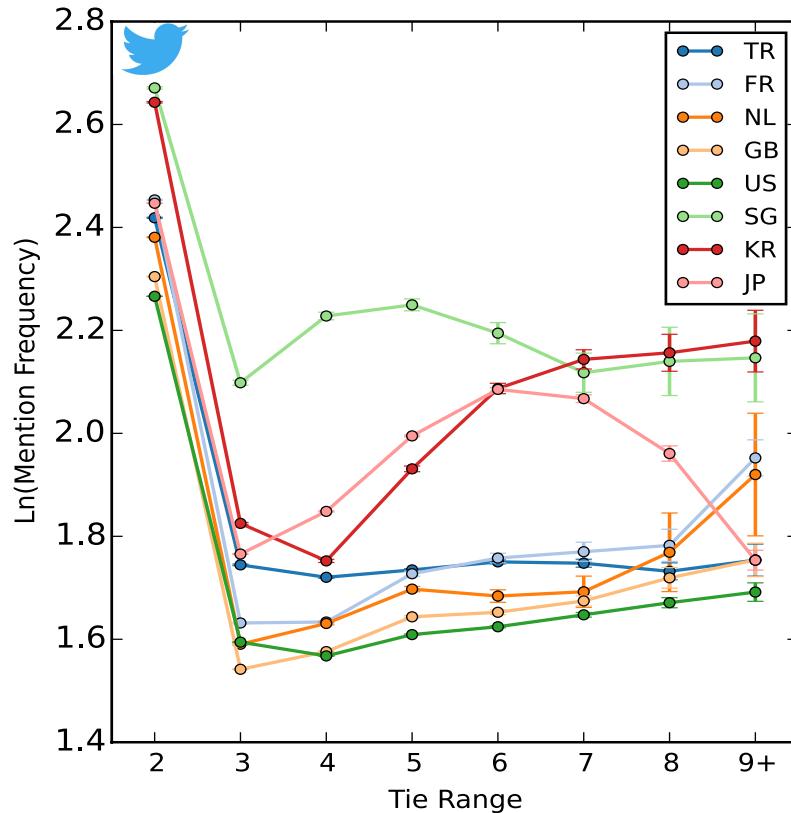
## Getting a job with weak ties

A Facebook study finds that a person is most likely to eventually work with a weak tie because weak ties collectively make up most of a person's social network. However, **strengthening an existing tie increases the probability that one will work with that specific friend.**  
(Gee et al. 2017)



A LinkedIn study finds that **weak ties are effective** for job transmissions, but diminishing returns to tie weakness.  
(Rajkumar et al. 2022)

# Continuing Debates



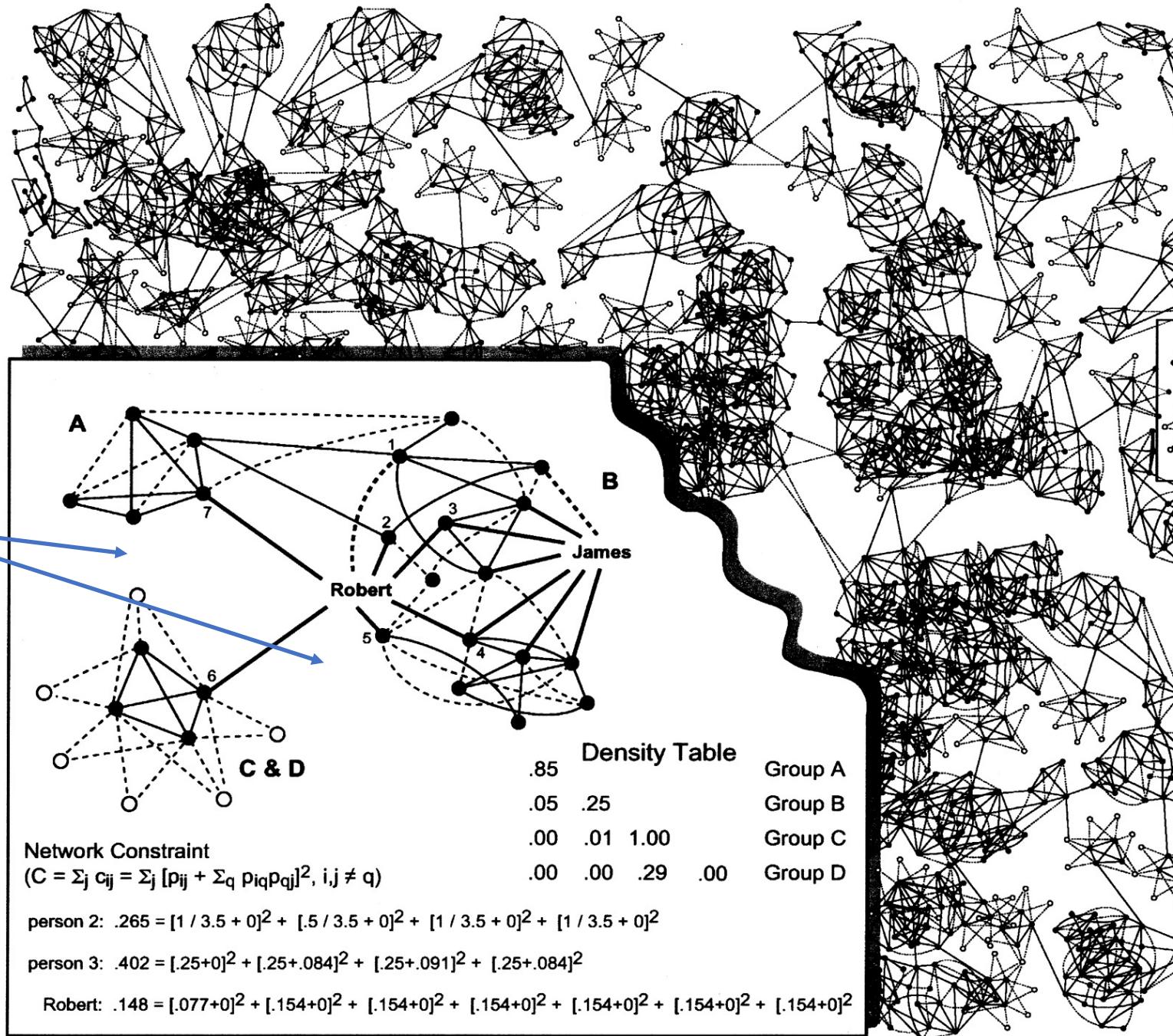
Bridging ties are not necessarily weak

# Brokerage

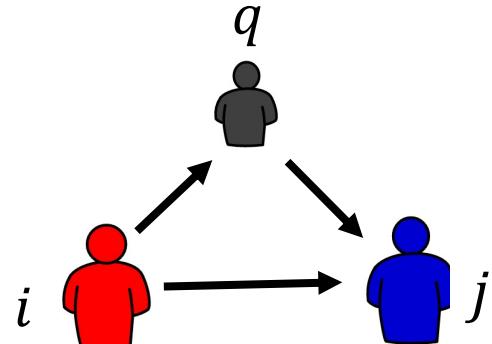
James vs. Robert

How are their positions different?  
Who spans more structural holes?

Structural hole



# Network Constraint



$$c_{ij} = \left( p_{ij} + \sum_q p_{iq} p_{qj} \right)^2$$

$i$ 's dependence on  $j$ : Proportion of direct communication with  $j$  and the sum of the indirect communications with  $j$  through common neighbors,  $q$

$$p_{ij} = \frac{z_{ij}}{\sum_q z_{iq}}$$
 communication with  $j$  relative to the sum of  $i$ 's total communications

$$C_i = \sum_j c_{ij}$$
  $i$ 's total constraint is the sum of  $i$ 's pairwise constraints

# Network Constraint

Network constraint can be interpreted as a composite measure consisting of **size, density, and hierarchy**.

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$$c_{ij} = {p_{ij}}^2 + 2(p_{ij} p_{iq_1} p_{q_1 j} + p_{ij} p_{iq_2} p_{q_2 j} + \dots) + (p_{iq_1} p_{q_1 j} + p_{iq_2} p_{q_2 j} \dots)$$

# Network Constraint

Network constraint can be interpreted as a composite measure consisting of **size (i's degree)**, **density**, and **hierarchy**.

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**size**

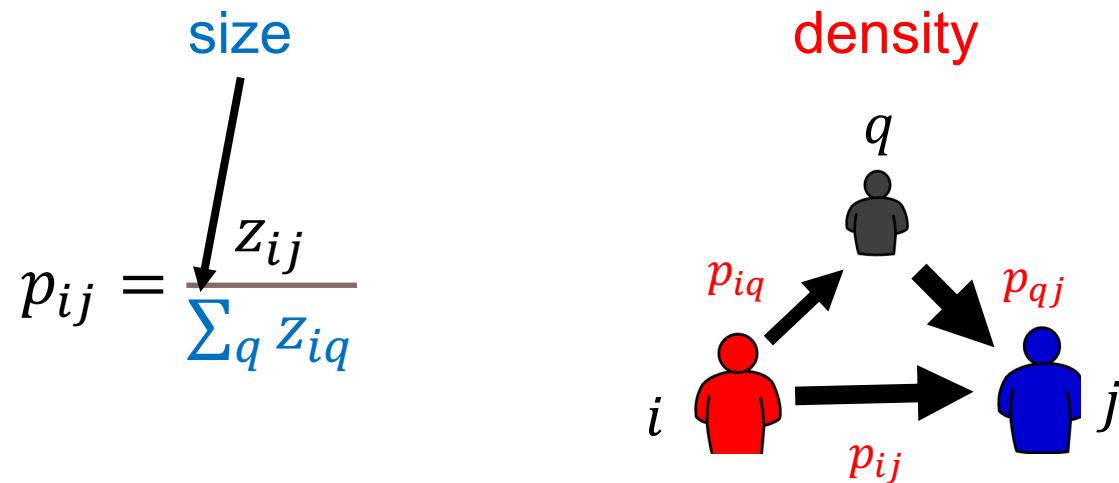
$$p_{ij} = \frac{z_{ij}}{\sum_q z_{iq}}$$

Larger size, less constrained

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Larger size, less constrained

High density, more constrained

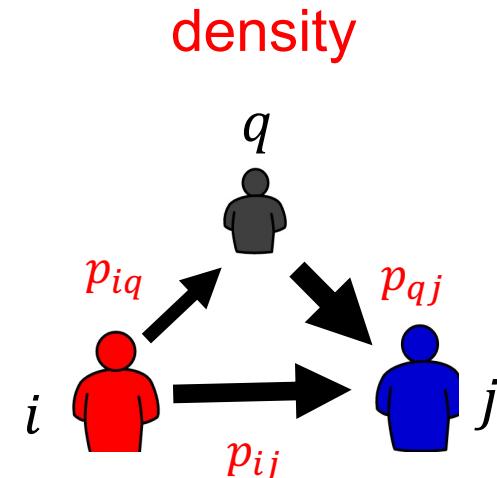
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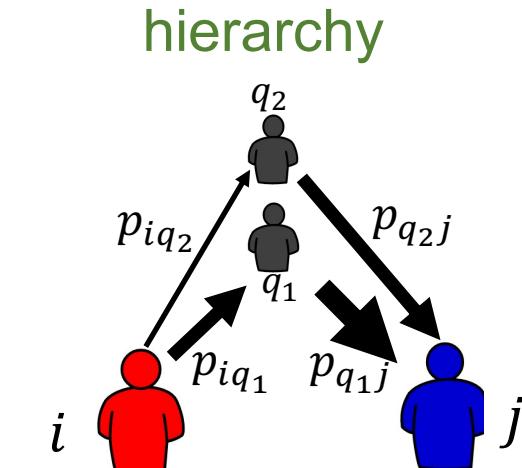
$$c_{ij} = p_{ij}^2 + 2(p_{ij}p_{iq_1}p_{q_1j} + p_{ij}p_{iq_2}p_{q_2j} + \dots) + (p_{iq_1}p_{q_1j} + p_{iq_2}p_{q_2j} \dots)$$

size

$$p_{ij} = \frac{z_{ij}}{\sum_q z_{iq}}$$



Larger size, less constrained



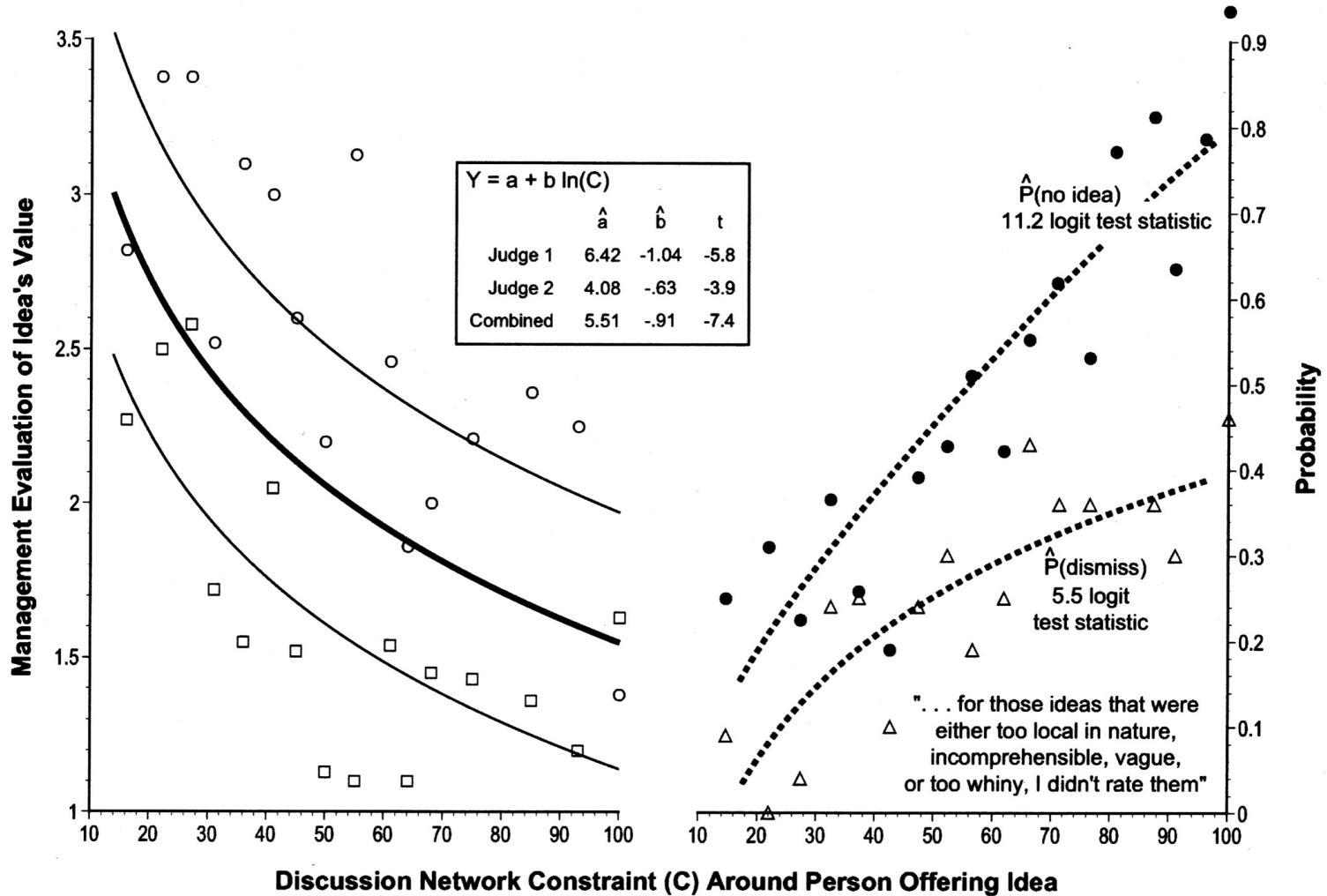
Strong hierarchy, more constrained

# Structural Holes and Good Ideas

## **Vision Advantage Hypothesis**

People whose networks span structural holes have early access to diverse, often contradictory, information and interpretations, which give them a competitive advantage in seeing good ideas. Hence, brokerage should be associated with good ideas.

# Structural Holes and Good Ideas

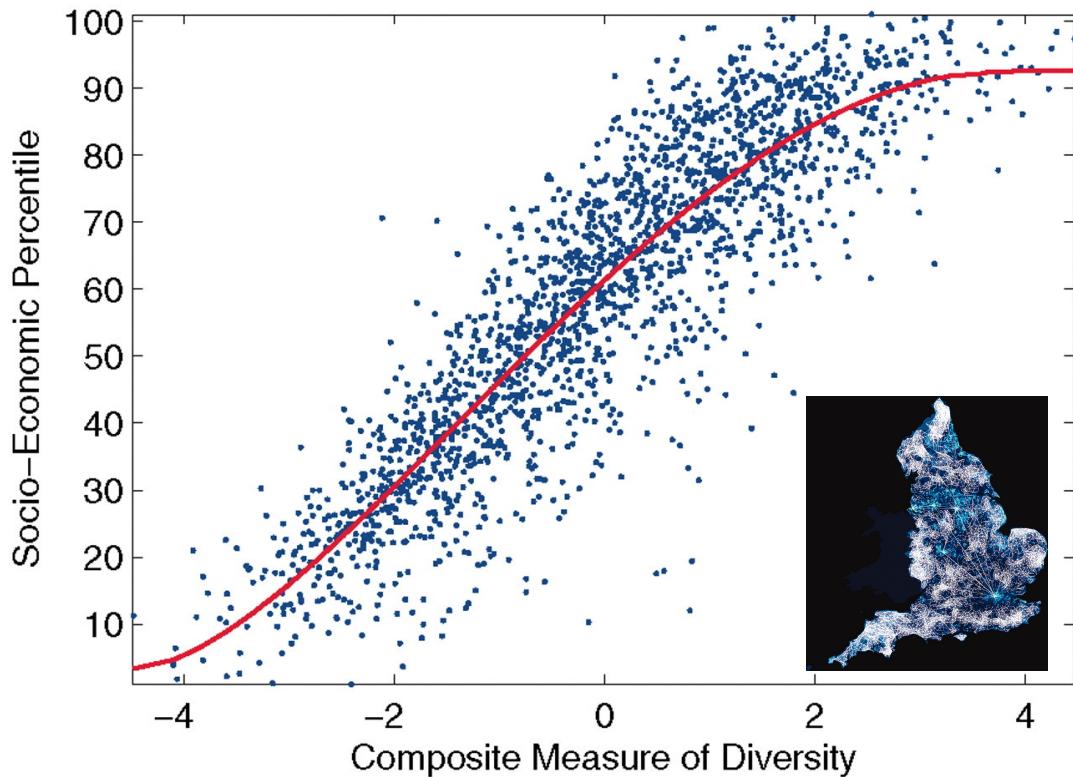


# Structural Holes and Good Ideas

	1 Salary	2 Salary	3 Evaluation	4 Promotion
Manager 1 .....	-31,099** (2,882)	-35,707** (3,498)	-.973 (.678)	.689 (.670)
Manager 2 .....	-16,652** (2,745)	-19,892** (3,479)	-.863 (.631)	1.165 (.648)
Manager 3 (reference) .....	...	...	...	...
Sr. manager .....	19,638** (3,782)	15,484** (4,143)	.116 (.843)	-.635 (.885)
Executive .....	65,394** (4,522)	61,930** (4,835)	.423 (1.01)	.221 (1.08)
Purchasing .....	754 (1,351)	1,811 (1,884)	.410 (.313)	.478 (.345)
Age .....	338** (52)	300** (71)	-.085** (.013)	-.084** (.013)
Bachelor .....	1,610 (1,003)	200 (1,401)	-.211 (.237)	.118 (.240)
Graduate .....	734 (864)	-451 (1,155)	-.208 (.203)	.182 (.204)
Hightech .....	3,516** (880)	3,150* (1,189)	.087 (.209)	.162 (.210)
Lowtech .....	-6,927** (1,481)	-6,607* (2,375)	-.351 (.342)	-.409 (.378)
Urban 1 .....	3,613** (1,046)	3,947** (1,456)	.423 (.247)	-.152 (.252)
Urban 2 .....	5,049** (1,010)	5,585* (1,427)	-.564 (.238)	-.052 (.243)
Network constraint ....	-7 (25)	-1 (38)	-.014** (.004)	-.022** (.006)
Mgr2 × constraint ....	-19 (35)	-47 (58)	.004 (.008)	-.008 (.009)
Mgr3 × constraint ....	-47 (38)	-159* (59)	-.007 (.009)	.003 (.009)
SrMgr × constraint .....	-214* (75)	-216* (84)	-.005 (.017)	.010 (.019)
Executive × constraint .....	-681** (124)	-697** (132)	-.011 (.028)	.024 (.030)
N .....	673	398	673	638

Constraint is bad  
especially for  
leadership  
positions

# Brokerage

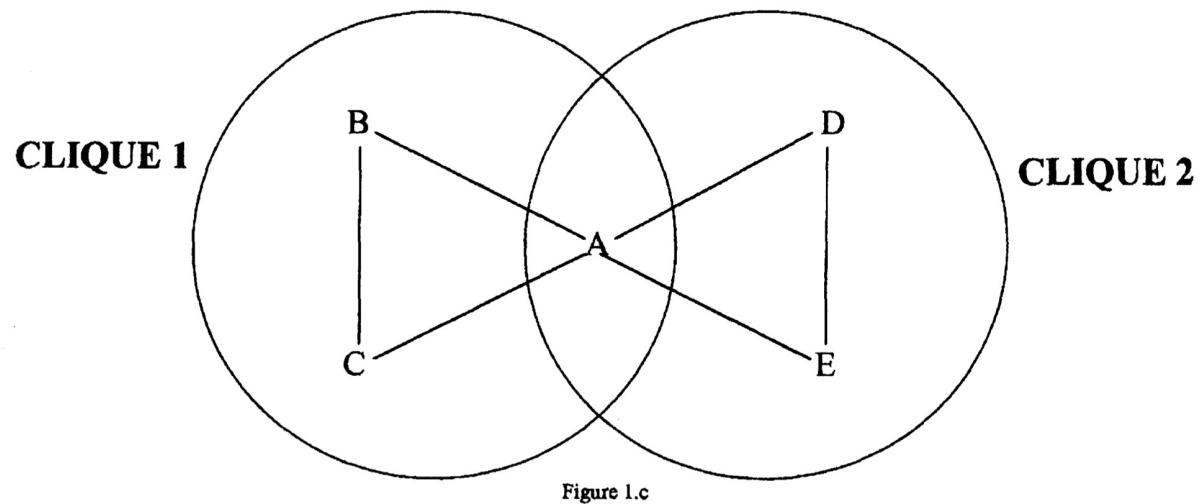


Brokerage positions are beneficial beyond organizations

- United Kingdom phone data
- Average constraint score at phone area code level correlates with the area's economic development

# Brokerage

**Critique to structural hole theory:  
Simmelian Ties**



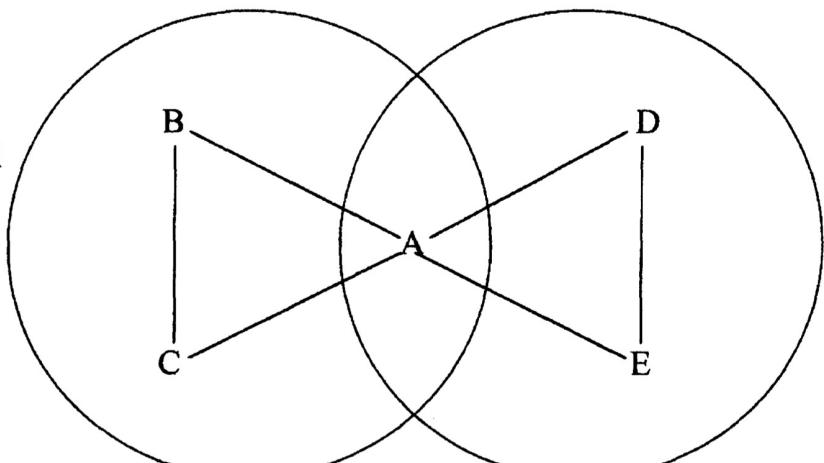
Constraints on A in Figure 1.c: must satisfy two cliques' sets of norms:  $S_1 \cap S_2$

(Krackhardt, 1999)

# Brokerage

**Critique to structural hole theory:  
Simmelian Ties**

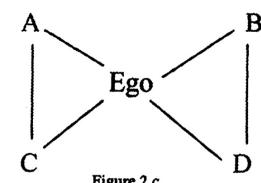
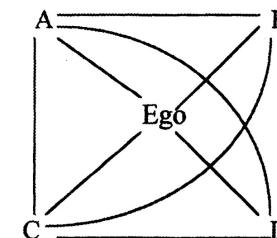
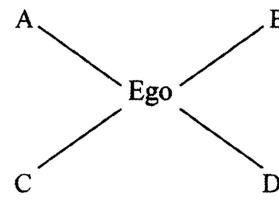
**CLIQUE 1**



**CLIQUE 2**

Constraints on A in Figure 1.c: must satisfy two cliques' sets of norms:  $S_1 \cap S_2$

(Krackhardt, 1999)



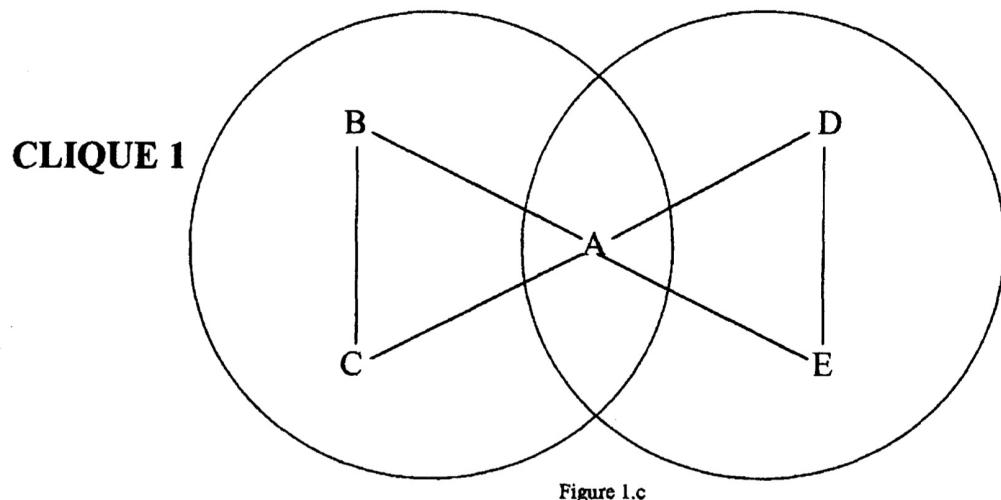
Which is least constraining?

Which is most constraining?

**Figure 2.** Constraint on Ego According to Structural Holes vs. Simmelian Tie Theories

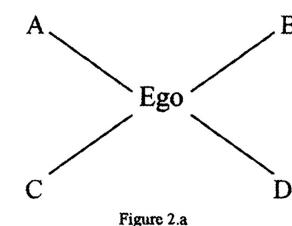
# Brokerage

## Critique to structural hole theory: Simmelian Ties

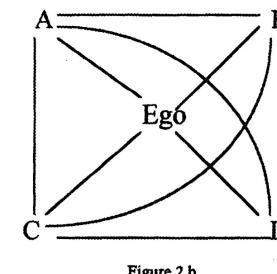


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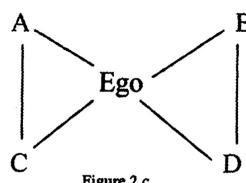
(Krackhardt, 1999)



**Burt's Structural Hole Theory**  
Least Constrained



**Simmelian Tie Theory**  
Least Constrained  
Somewhat Constrained, but only by 1 Clique



**Burt's Structural Hole Theory**  
Most Constrained, must satisfy 2 Cliques  
Somewhat Constrained, but also empowered as bridge between 2 Cliques

**Figure 2.** Constraint on Ego According to Structural Holes vs. Simmelian Tie Theories

# Predicting Romantic Relationships

Backstrom and Kleinberg (2014)

Textbook case of combining:

- deep consideration about the nature of the tie (romantic) and
- corresponding metrics construction

# Nature of the Romantic Tie

Recall from Wellman and Wortley

Intimate ties (psychology):

- a sense of intimacy, voluntary investment in the tie and companionship
- an interest in **being together** as much as possible through interactions **in multiple social contexts** over a long period
- a sense of **mutuality** and support for partner's needs

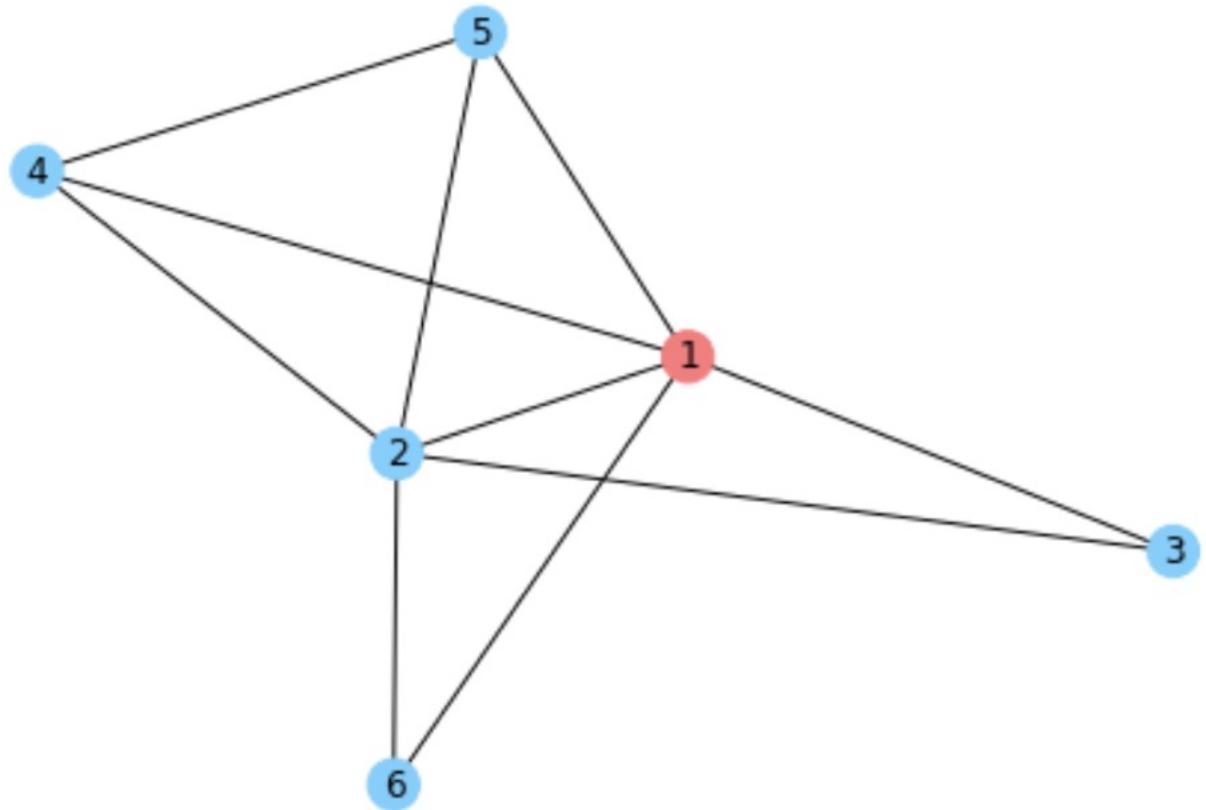
# Metric Construction

## **Network dispersion:**

A new measure that extends the observations and intuition that relationship psychologists made about intimate relationships.

“... the links to a person’s relationship partner or other closest friends may have lower embeddedness, but they will often involve mutual neighbors from several different foci, reflecting the fact that the social orbits of these close friends are not bounded within any one focus.”

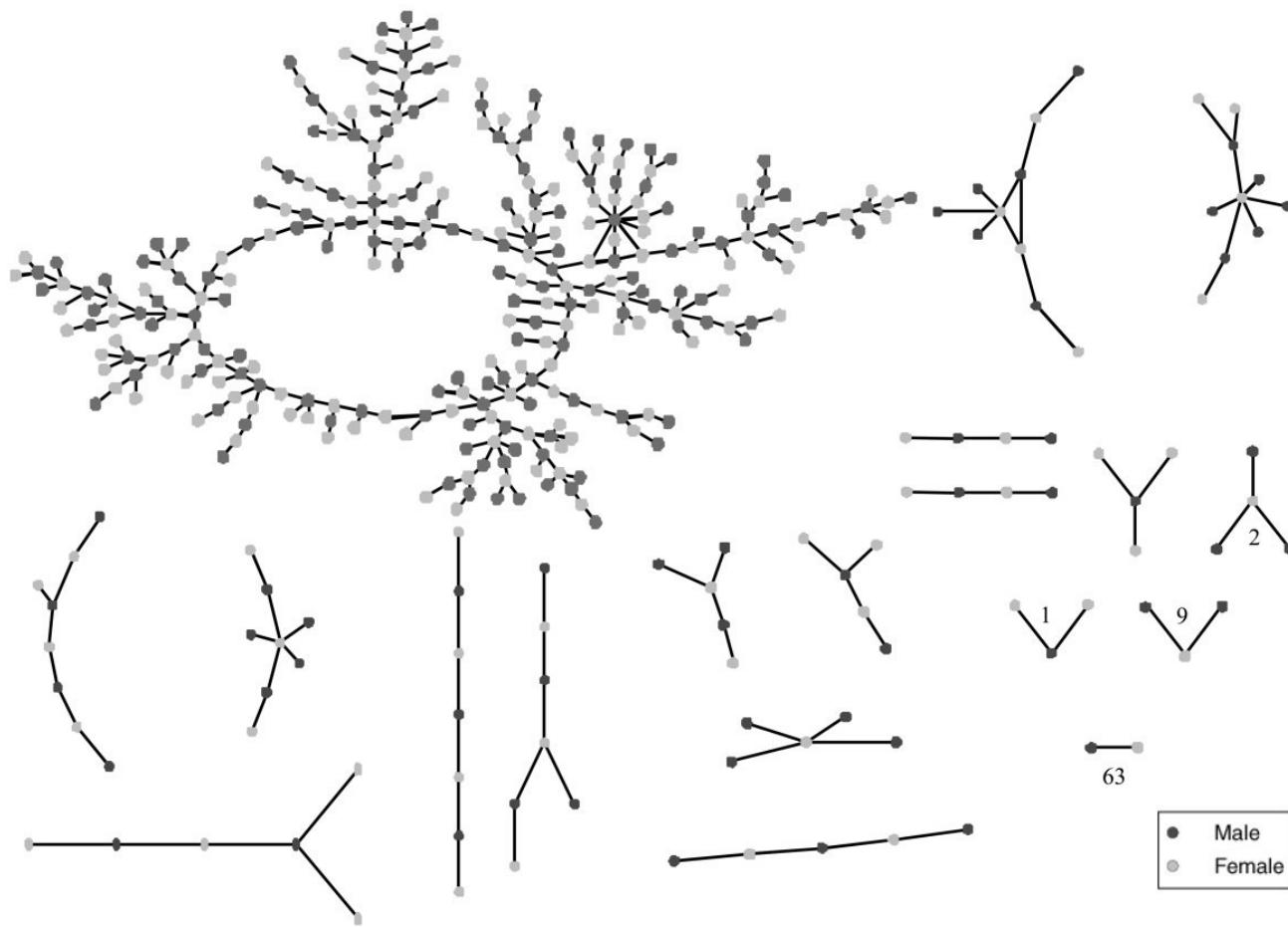
# Operationalizing the Intuition



$$disp(u, v) = \sum_{s, t \in C_{uv}} d_v(s, t)$$

$$d_v(s, t) = \begin{cases} 1, & \text{if } s \text{ and } t \text{ are not linked and have 0 common neighbors} \\ 0, & \text{otherwise} \end{cases}$$

# Explaining Network Structures

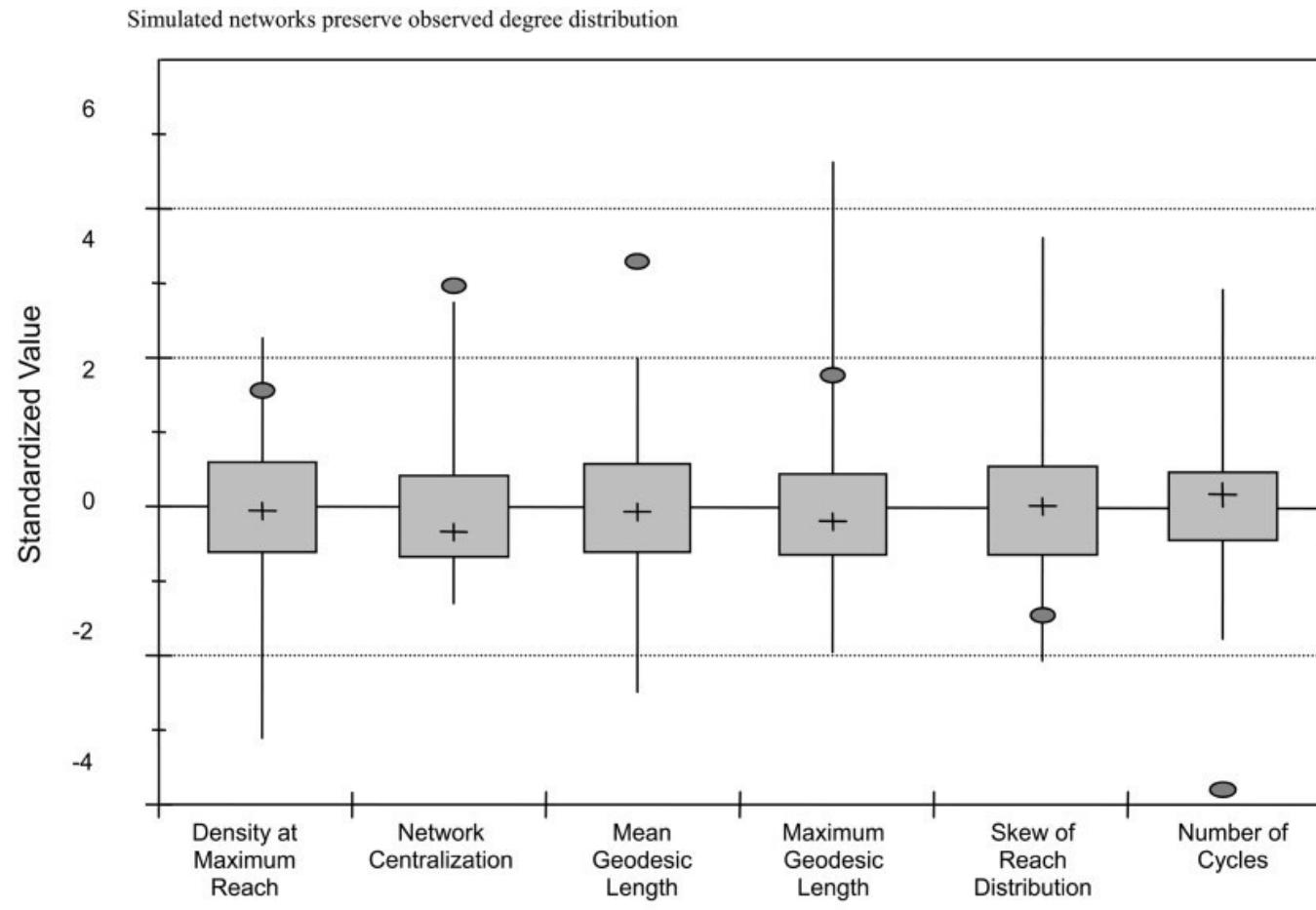


Network scientists employ random graphs as baseline

Divergence of observed network from baseline offers clues to its structure

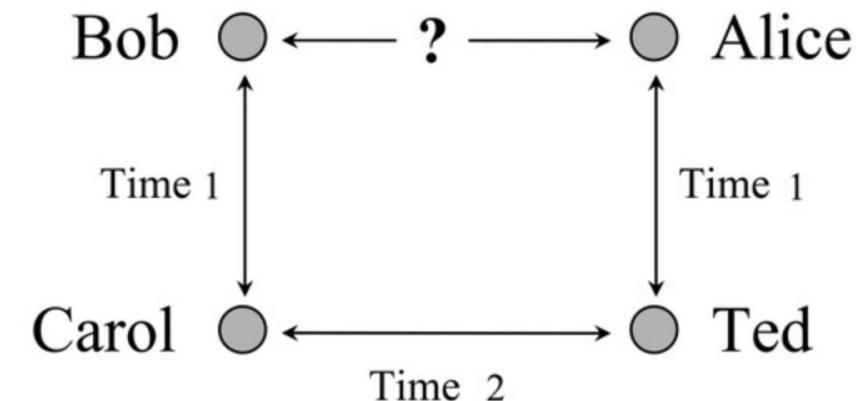
# Explaining Network Structures

Simulated networks preserve observed degree distribution



The clue: Absence of four cycles in the high school network, relative to random baseline

Authors “theorize” behavioral reasons why the cycles are absent



# Questions?