

P1 - Draw comparisons Between the sorting Algorithm Bubble Sort, Selection Sort , Insertion Sort ,Merge Sort and Heap Sort ?

	Stable	Time Complexity (Best Case)	Time Complexity (Average Case)	Time Complexity (Worst Case)	Inplace
Bubble sort	Yes	$O(n^2)$	$O(n^2)$	$O(n^2)$	Yes
Selection sort	No	$O(n^2)$	$O(n^2)$	$O(n^2)$	Yes
Insertion sort	Yes	$O(n)$ - (sorted)	$O(n^2)$	$O(n^2)$	Yes
Merge sort	Yes	$O(n \cdot \log n)$	$O(n \cdot \log n)$	$O(n \cdot \log n)$	No
Heap sort	No	$O(n \cdot \log n)$	$O(n \cdot \log n)$	$O(n \cdot \log n)$	Yes

References:

1. <https://en.wikipedia.org/wiki/Heapsort>

P2- Write a program to find out factorial for larger value like (100,150 etc.)?Note: No use of library

```
#include <iostream>
```

```
#include <vector>
```

```
using namespace std;
```

```
void multiply(vector<int>& fact, int n) {  
    int carry = 0;  
    for (int i = 0; i < fact.size(); i++) {  
        int mulResult = (fact[i] * n) + carry;  
        fact[i] = mulResult % 10;  
        carry = mulResult / 10;  
    }
```

```
    while (carry != 0) {  
        fact.push_back(carry % 10);  
        carry /= 10;  
    }  
}
```

```
string factorial(int n) {  
    vector<int> fact(1, 1);  
  
    for (int i = 2; i <= n; i++)  
        multiply(fact, i);  
  
    string result = "";  
    for (int i = fact.size() - 1; i >= 0; i--) {  
        result += to_string(fact[i]);  
    }
```

```
    return result;  
}
```

```
int main() {  
    int n;  
    cin >> n;  
    if (n < 1) {  
        cout << "Invalid input" << "\n";  
        return 0;  
    }
```

```
    cout << factorial(n) << "\n";  
    return 0;  
}
```

P3-Justify the Time Complexity of give pseudo Code with proper reasoning;

a-)

```
int j = 0;
for(int i = 0; i < n; ++i) {
    while(j < n && arr[i] < arr[j]) {
        j++;
    }
}
```

b-)

```
int a = 0, i = N;
while (i > 0) a += i;
i /= 2;
}
```

a) $O(n)$

- If predicate condition of while loop is false then i will increment, otherwise j will increment. In either case, the outer for loop will terminate after at most $2n$ steps.

b) $O(\log n)$

- After every iteration of the while loop, i become half of its previous value.

P4-What is the additional benefit of a circular queue? Illustrate with at least 2 practical examples (programming/application) where a circular queue is used. Write the enqueue and dequeue functions/pseudocode

(not the program) for array and linked list based implementation of a circular queue.

Benefits of Circular queue :

1. Good utilization of memory :

Example :

- Consider a simple Queue and a Circular Queue of size 5.
- Simple Queue = {1, 2, 3, 4, 5}. front is at index = 0 and rear is at index = 4
- Circular Queue = {1, 2, 3, 4, 5} front is at index = 0 and rear is at index = 4

- Now If we remove the first element in the queue which is 1 (pointed by the front of both queues) then the state of both of the queues will be as follows.

- Simple Queue = {-, 2, 3, 4, 5}. front is at index = 1 and rear is at index = 4
- Circular Queue = {-, 2, 3, 4, 5} front is at index = 1 and rear is at index = 4

- Now if we want to insert 6 in both the queues then their state will be as follows.

- Not possible to insert in the simple queue as the rear has reached at the end.
- Circular Queue = {6, 2, 3, 4, 5} front is at index = 1 and rear is at index = 0. This is because the rear will move circularly from index 4 to index 0. Thus vacant positions can be utilized which was not possible in linear queue.

2. Elements can be inserted again :

Example :

- Consider a simple Queue and a Circular Queue of size 5.
- Simple Queue = {1, 2, 3, 4, 5}. front is at index = 0 and rear is at index = 4
- Circular Queue = {1, 2, 3, 4, 5} front is at index = 0 and rear is at index = 4

- Now If we remove the first 3 elements in the both queues then the state of both of the queues will be as follows.

- Simple Queue = {-, -, -, 4, 5}. front is at index = 3 and rear is at index = 4
- Circular Queue = {-, -, -, 4, 5} front is at index = 3 and rear is at index = 4

- Now if we want to insert 6, 7 in both the queues then their state will be as follows.
- Not possible to insert in the simple queue as the rear has reached at the end. So, in a linear queue, once an element is removed then it is not possible to insert new elements at those indices.
- Circular Queue = {6, 7, -, 4, 5} front is at index = 3 and rear is at index = 1. This is because the rear will move in a circular manner from index 4 to index 1 and thus the vacant positions can be filled again unlike in a linear queue.

Pseudocode :

1. Array Based Implementation :

Enqueue :

Enqueue(arr, front, rear, capacity, num):

If (rear + 1) % capacity == front :

 return

If rear == -1:

 front = 0

 rear = 0

 arr[rear] = num

 return

rear = (rear + 1) % capacity

arr[rear] = num

Dequeue :

Dequeue(arr, front, rear, capacity):

If rear == -1:

 return

If front == rear :

 num = arr[front]

 front = -1

 rear = -1

num = arr[front]

front = (front + 1) % capacity

return num

2. Linked List Based Implementation :

Enqueue :

Enqueue(front, rear, num, size, capacity):

If size == 0:

 front = rear

 rear.data = num

 size++

If capacity == size:

 return

rear = rear.next

rear.data = num

size++

Dequeue :

Dequeue(front, rear, size, capacity):

If size == 0:

 return

If size == 1:

 num = front.data

 front = rear

 size = 0

 return num

num = front.data

front = front.next

size--

return num

References:

1. <https://www.mvorganizing.org/what-is-the-reason-for-using-a-circular-queue-instead-of-a-regular-one>