P1 -Write a program for insertion and deletion in a Binary Search Tree ?Any pattern you can see while in the inorder traversal of BST?

BST.java file:

```
class BSTNode {
  int val;
  BSTNode left;
  BSTNode right;
  BSTNode(int val) {
     this.val = val;
     this.left = null;
     this.right = null;
  }
}
public class BST {
  public BSTNode root;
  public void insert(int val) {
     this.root = this.insert(val, this.root);
  }
  public BSTNode insert(int val, BSTNode node) {
     if (node == null)
       return new BSTNode(val);
     int cmp = val - node.val;
     if (cmp > 0)
        node.right = insert(val, node.right);
     else
        node.left = insert(val, node.left);
     return node;
  }
  public void delete(int key) {
     this.root = deleteNode(this.root, key);
  }
  public BSTNode deleteNode(BSTNode root, int key) {
     if (root == null)
       return root;
```

```
int cmp = key - root.val;
  if (cmp > 0)
     root.right = deleteNode(root.right, key);
  else if (cmp < 0)
     root.left = deleteNode(root.left, key);
  else {
     if (root.left == null)
        return root.right;
     if (root.right == null)
        return root.left;
     BSTNode temp = root;
     root = min(temp.right);
     root.right = deleteMin(temp.right);
     root.left = temp.left;
  }
  return root;
}
public BSTNode deleteMin(BSTNode root) {
  if (root.left == null)
     return root.right;
  root.left = deleteMin(root.left);
  return root;
}
public BSTNode min(BSTNode root) {
  if (root.left == null)
     return root;
  return min(root.left);
}
public void inorder(BSTNode node) {
  if (node == null)
     return;
  inorder(node.left);
  System.out.println(node.val);
  inorder(node.right);
```

```
}
  public void inorder() {
     inorder(this.root);
  }
  public static void main(String[] args) {
     BST bst = new BST();
     bst.insert(3);
     bst.insert(33);
     bst.insert(7);
     bst.insert(9);
     bst.insert(4);
     bst.inorder();
     bst.delete(33);
     bst.inorder();
  }
}
```

Output:

The inorder traversal always yields an ascending order of elements. Also, the traversal this depth-first traversal and left-to-right traversal.

P4- Write a program for level Order traversal in a Binary Tree and also explain your code complexities(Time/Space)?

```
import java.util.ArrayList;
import java.util.LinkedList;
import java.util.Queue;
class BSTNode {
  int val;
  BSTNode left;
  BSTNode right;
  BSTNode(int val) {
     this.val = val;
     this.left = null;
     this.right = null;
  }
}
public class BST {
  public BSTNode root;
  public void insert(int val) {
     this.root = this.insert(val, this.root);
  }
  public BSTNode insert(int val, BSTNode node) {
     if (node == null)
       return new BSTNode(val);
     int cmp = val - node.val;
     if (cmp > 0)
       node.right = insert(val, node.right);
     else
        node.left = insert(val, node.left);
     return node;
  }
  public ArrayList<ArrayList<Integer>> levelOrder(BSTNode root) {
     if(root==null)
        ArrayList<ArrayList<Integer>> res=new ArrayList<>();
        return res;
```

```
ArrayList<ArrayList<Integer>> res=new ArrayList<>();
  Queue<BSTNode> ob =new LinkedList<>();
  ob.add(root);
  ob.add(null);
  ArrayList<Integer> subRes=new ArrayList<>();
  while(!ob.isEmpty())
     BSTNode front=ob.poll();
     if(front==null)
     {
       if(!ob.isEmpty())
          res.add(subRes);
          subRes=new ArrayList<>();
          ob.add(front);
       }
       else
          res.add(subRes);
          return res;
       }
     }
     else{
       subRes.add(front.val);
       if(front.left!=null) ob.add(front.left);
       if(front.right!=null) ob.add(front.right);
     }
  }
  return res;
public ArrayList<ArrayList<Integer>> levelOrder() {
  return levelOrder(this.root);
public static void main(String[] args) {
  BST bst = new BST();
  bst.insert(3);
```

}

}

```
bst.insert(33);
bst.insert(7);
bst.insert(9);
bst.insert(4);

ArrayList<ArrayList<Integer>> result = bst.levelOrder();

for (int i = 0; i < result.size(); i++) {
    for (int j = 0; j < result.get(i).size(); j++) {
        System.out.print(result.get(i).get(j) + " ");
    }
    System.out.println();
}</pre>
```

Time Complexity:

We can see that we are traversing the whole tree by visiting each node exactly once. Hence, the time complexity will be O(n) where n = number of nodes in tree

Space Complexity:

Since, we are storing the nodes at every level, the space complexity will be equal to the number of nodes in the tree and hence it will also be O(n) where n = number of nodes in tree