SUNDIALSTB v2.2.0, a MATLAB Interface to SUNDIALS

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1 Introduction

SUNDIALS [2], SUite of Nonlinear and DIfferential/ALgebraic equation Solvers, is a family of software tools for integration of ODE and DAE initial value problems and for the solution of nonlinear systems of equations. It consists of CVODE, IDA, and KINSOL, and variants of these with sensitivity analysis capabilities.

SUNDIALSTB is a collection of MATLAB functions which provide interfaces to the SUNDIALS solvers. The core of each MATLAB interface in SUNDIALSTB is a single MEX file which interfaces to the various user-callable functions for that solver. However, this MEX file should not be called directly, but rather through the user-callable functions provided for each MATLAB interface.

A major design principle for SUNDIALSTB was to provide an interface that is, as much as possible, equally familiar to both SUNDIALS users and MATLAB users. Moreover, we tried to keep the number of user-callable functions to a minimum. For example, the CVODES MATLAB interface contains only 12 such functions, 2 of which relate to forward sensitivity analysis and 4 more interface solely to the adjoint sensitivity module in CVODES. A user who is only interested in integration of ODEs and not in sensitivity analysis therefore needs to call at most 6 functions. In tune with the MATLAB ODESET function, optional solver inputs in SUNDIALSTB are specified through a single function; e.g. CvodeSetOptions for CVODES (a similar function is used to specify optional inputs for forward sensitivity analysis). However, unlike the ODE solvers in MATLAB, we have kept the more flexible SUNDIALS model in which a separate "solve" function (CVodeSolve for CVODES) must be called to return the solution at a desired output time. Solver statistics, as well as optional outputs (such as solution and solution derivatives at additional times) can be obtained at any time with calls to separate functions (CVodeGetStats and CVodeGet for CVODES).

This document provides a complete documentation for the SUNDIALSTB functions. For additional details on the methods and underlying SUNDIALS software consult also the coresponding SUNDIALS user guides [3, 1].

1.1 Notes

The version numbers for the MATLAB interfaces correspond to those of the corresponding SUNDIALS solver with wich the interface is compatible.

1.2 Requirements

Each interface module in SUNDIALSTB requires the appropriate version of the corresponding SUNDIALS solver. For parallel support, SUNDIALSTB depends on MPITB with LAM v > 7.1.1 (for MPI-2 spawning feature).

1.3 Installation/Setup

The following steps are required to install and setup SUNDIALSTB:

1.3.1 Compilation and installation of sundialsTB

As of version 2.3.0, SUNDIALSTB is distributed only with the complete SUNDIALS package and, on *nix systems (or under cygwin in Windows), the MATLAB toolbox can be configured, built, and installed using the main SUNDIALS configure script. For details see the SUNDIALS file INSTALL_NOTES.

For systems that do not support configure scripts (or if the configure script fails to configure SUNDIALSTB), we provide a MATLAB script (install_STB.m) which can be used to build and install SUNDIALSTB from within MATLAB. In the sequel, we assume that the SUNDIALS package was unpacked under the directory *srcdir*. The SUNDIALSTB files are therefore in *srcdir*/sundialsTB.

To facilitate the compilation of SUNDIALSTB on platforms that do not have a make system, we rely on MATLAB's mex command. Compilation of SUNDIALSTB is done by running from under MATLAB the install_STB.m script which is present in the SUNDIALSTB top directory.

1. Launch matlab in sundialsTB

```
% cd srcdir/sundialsTB
% matlab
```

2. Run the install_STB matlab script

Note that parallel support will be compiled into the MEX files only if \$LAMHOME is defined and \$MPITB_ROOT is defined and \$srcdir/src/nvec_par exists.

After the MEX files are generated, you will be asked if you wish to install the SUNDIALSTB toolbox. If you answer yes, you will be then asked for the installation directory (called in the sequel *instdir*). To install SUNDIALSTB for all MATLAB users (not usual), assuming MATLAB is installed under /usr/local/matlab7, specify *instdir* = /usr/local/matlab7/toolbox. To install SUNDIALSTB for just one user (usual configuration), install SUNDIALSTB under a directory of your choice (typically under your matlab working directory). In other words, specify *instdir* = /home/user/matlab.

1.3.2 Configuring Matlab's startup

After a successful installation, a SUNDIALSTB.m startup script is generated in *instdir*/sundialsTB. This file must be called by MATLAB at initialization.

If SUNDIALSTB was installed for all MATLAB users (not usual), add the SUNDIALSTB startup to the system-wide startup file (by linking or copying):

```
% cd /usr/local/matlab7/toolbox/local
% ln -s ../sundialsTB/startup_STB.m .
and add these lines to your original local startup.m
% SUNDIALS Toolbox startup M-file, if it exists.
if exist('startup_STB','file')
    startup_STB
end
```

If SUNDIALSTB was installed for just one user (usual configuration) and assuming you do not need to keep any previously existing startup.m, link or copy the startup_STB.m script to your working 'matlab' directory:

```
% cd ~/matlab
% ln -s sundialsTB/startup_STB.m startup.m
```

If you already have a startup.m, use the method described above, first linking (or copying) startup_STB.m to the destination subdirectory and then editing the file /matlab/startup.m to run startup_STB.m.

1.3.3 Testing the installation

If everything went fine, you should now be able to try one of the CVODES, IDAS, or KINSOL examples (in matlab, type 'help cvodes', 'help idas', or 'help kinsol' to see a list of all examples available). For example, cd to the CVODES serial example directory:

```
% cd instdir/sundialsTB/cvode/examples_ser and then launch matlab and execute cvdx.
```

1.4 Links

The required software packages can be obtained from the following addresses.

```
SUNDIALS http://www.llnl.gov/CASC/sundials
MPITB http://atc.ugr.es/javier-bin/mpitb_eng
LAM http://www.lam-mpi.org/
```

2 MATLAB Interface to CVODES

The MATLAB interface to CVODES provides access to all functionality of the CVODES solver, including IVP simulation and sensitivity analysis (both forward and adjoint).

The interface consists of 9 user-callable functions. The user must provide several required and optional user-supplied functions which define the problem to be solved. The user-callable functions and the types of user-supplied functions are listed in Table 1 and fully documented later in this section. For more in depth details, consult also the CVODES user guide [3].

To illustrate the use of the CVODES MATLAB interface, several example problems are provided with SUNDIALSTB, both for serial and parallel computations. Most of them are MATLAB translations of example problems provided with CVODES.

Table 1: CVODES MATLAB interface functions

	1	
	${\it CVodeSetOptions}$	creates an options structure for CVODES.
	CVodeSetFSAOptions	creates an options structure for FSA with CVODES.
SU	${ m CVodeMalloc}$	allocates and initializes memory for CVODES.
tioi	${ m CVodeSensMalloc}$	allocates and initializes memory for FSA with CVODES.
Functions	CVadjMalloc	allocates and initializes memory for ASA with CVODES.
Fu	${ m CVodeMallocB}$	allocates and initializes backward memory for CVODES.
	CVode	integrates the ODE.
	${ m CVodeB}$	integrates the backward ODE.
	${ m CVodeGetStats}$	returns statistics for the CVODES solver.
	${ m CVodeGetStatsB}$	returns statistics for the backward CVODES solver.
	${ m CVodeGet}$	extracts data from CVODES memory.
	${ m CVodeFree}$	deallocates memory for the CVODES solver.
	${ m CVodeMonitor}$	sample monitoring function.
	CVRhsFn	RHS function
	$\operatorname{CVRootFn}$	root-finding function
	${ m CVQuadRhsFn}$	quadrature RHS function
es	${ m CVDenseJacFn}$	dense Jacobian function
yp	${ m CVBandJacFn}$	banded Jacobian function
n t	${ m CVJacTimesVecFn}$	Jacobian times vector function
tio	${ m CVPrecSetupFn}$	preconditioner setup function
Function types	${ m CVPrecSolveFn}$	preconditioner solve function
F	${ m CVGlocalFn}$	RHS approximation function (BBDPre)
	${ m CVGcommFn}$	communication function (BBDPre)
	${ m CVSensRhsFn}$	sensitivity RHS function
	${\operatorname{CVMonitorFn}}$	monitoring function

2.1 Interface functions

CVodeSetOptions

PURPOSE CVodeSetOptions creates an options structure for CVODES. Synopsis function options = CVodeSetOptions(varargin) DESCRIPTION CVodeSetOptions creates an options structure for CVODES. Usage: OPTIONS = CVodeSetOptions('NAME1', VALUE1, 'NAME2', VALUE2,...) OPTIONS = CVodeSetOptions(OLDOPTIONS,'NAME1',VALUE1,...) OPTIONS = CVodeSetOptions(OLDOPTIONS, NEWOPTIONS) OPTIONS = CVodeSetOptions('NAME1', VALUE1, 'NAME2', VALUE2,...) creates a CVODES options structure OPTIONS in which the named properties have the specified values. Any unspecified properties have default values. It is sufficient to type only the leading characters that uniquely identify the property. Case is ignored for property names. OPTIONS = CVodeSetOptions(OLDOPTIONS,'NAME1', VALUE1,...) alters an existing options structure OLDOPTIONS. OPTIONS = CVodeSetOptions(OLDOPTIONS, NEWOPTIONS) combines an existing options structure OLDOPTIONS with a new options structure NEWOPTIONS. Any new properties overwrite corresponding old properties. CVodeSetOptions with no input arguments displays all property names and their possible values. CVodeSetOptions properties (See also the CVODES User Guide) LMM - Linear Multistep Method ['Adams' | 'BDF'] This property specifies whether the Adams method is to be used instead of the default Backward Differentiation Formulas (BDF) method. The Adams method is recommended for non-stiff problems, while BDF is recommended for stiff problems. NonlinearSolver - Type of nonlinear solver used [Functional | Newton] The 'Functional' nonlinear solver is best suited for non-stiff problems, in conjunction with the 'Adams' linear multistep method, while 'Newton' is better suited for stiff problems, using the 'BDF' RelTol - Relative tolerance [positive scalar | 1e-4] RelTol defaults to 1e-4 and is applied to all components of the solution vector. See AbsTol. AbsTol - Absolute tolerance [positive scalar or vector | 1e-6]

```
with components
     ewt(i) = 1/(RelTol*|y(i)| + AbsTol)
                                           if AbsTol is a scalar
     ewt(i) = 1/(RelTol*|y(i)| + AbsTol(i)) if AbsTol is a vector
   This vector is used in all error and convergence tests, which
  use a weighted RMS norm on all error-like vectors v:
     WRMSnorm(v) = sqrt((1/N) sum(i=1..N) (v(i)*ewt(i))^2),
  where N is the problem dimension.
MaxNumSteps - Maximum number of steps [positive integer | 500]
   CVode will return with an error after taking MaxNumSteps internal steps
   in its attempt to reach the next output time.
InitialStep - Suggested initial stepsize [ positive scalar ]
   By default, CVode estimates an initial stepsize hO at the initial time
   t0 as the solution of
    WRMSnorm(h0^2 ydd / 2) = 1
   where ydd is an estimated second derivative of y(t0).
MaxStep - Maximum stepsize [ positive scalar | inf ]
  Defines an upper bound on the integration step size.
MinStep - Minimum stepsize [ positive scalar | 0.0 ]
  Defines a lower bound on the integration step size.
MaxOrder - Maximum method order [ 1-12 for Adams, 1-5 for BDF | 5 ]
   Defines an upper bound on the linear multistep method order.
StopTime - Stopping time [ scalar ]
  Defines a value for the independent variable past which the solution
   is not to proceed.
RootsFn - Rootfinding function [ function ]
   To detect events (roots of functions), set this property to the event
   function. See CVRootFn.
NumRoots - Number of root functions [ integer | 0 ]
   Set NumRoots to the number of functions for which roots are monitored.
   If NumRoots is 0, rootfinding is disabled.
StabilityLimDet - Stability limit detection algorithm [ on | off ]
  Flag used to turn on or off the stability limit detection algorithm
  within CVODES. This property can be used only with the BDF method.
   In this case, if the order is 3 or greater and if the stability limit
   is detected, the method order is reduced.
LinearSolver - Linear solver type [Dense|Diag|Band|GMRES|BiCGStab|TFQMR]
   Specifies the type of linear solver to be used for the Newton nonlinear
   solver (see NonlinearSolver). Valid choices are: Dense (direct, dense
   Jacobian), Band (direct, banded Jacobian), Diag (direct, diagonal Jacobian),
  GMRES (iterative, scaled preconditioned GMRES), BiCGStab (iterative, scaled
  preconditioned stabilized BiCG), TFQMR (iterative, scaled transpose-free QMR).
  The GMRES, BiCGStab, and TFQMR are matrix-free linear solvers.
JacobianFn - Jacobian function [ function ]
   This propeerty is overloaded. Set this value to a function that returns
   Jacobian information consistent with the linear solver used (see Linsolver).
   If not specified, CVODES uses difference quotient approximations.
  For the Dense linear solver, JacobianFn must be of type CVDenseJacFn and
  must return a dense Jacobian matrix. For the Band linear solver, JacobianFn
  must be of type CVBandJacFn and must return a banded Jacobian matrix.
  For the iterative linear solvers, GMRES, BiCGStab, and TFQMR, JacobianFn must
  be of type CVJacTimesVecFn and must return a Jacobian-vector product. This
  property is not used for the Diag linear solver.
```

The relative and absolute tolerances define a vector of error weights

- KrylovMaxDim Maximum number of Krylov subspace vectors [integer | 5] Specifies the maximum number of vectors in the Krylov subspace. This property is used only if an iterative linear solver, GMRES, BiCGStab, or TFQMR is used (see LinSolver).
- GramSchmidtType Gram-Schmidt orthogonalization [Classical | Modified]
 Specifies the type of Gram-Schmidt orthogonalization (classical or modified).
 This property is used only if the GMRES linear solver is used (see LinSolver).
- PrecType Preconditioner type [Left | Right | Both | None]

 Specifies the type of user preconditioning to be done if an iterative linear solver, GMRES, BiCGStab, or TFQMR is used (see LinSolver). PrecType must be one of the following: 'None', 'Left', 'Right', or 'Both', corresponding to no preconditioning, left preconditioning only, right preconditioning only, and both left and right preconditioning, respectively.
- PrecModule Preconditioner module [BandPre | BBDPre | UserDefined]

 If PrecModule = 'UserDefined', then the user must provide at least a preconditioner solve function (see PrecSolveFn)

 CVODES provides the following two general-purpose preconditioner modules:

 BandPre provide a band matrix preconditioner based on difference quotients of the ODE right-hand side function. The user must specify the lower and upper half-bandwidths through the properties LowerBwidth and UpperBwidth, respectively.

BBDPre can be only used with parallel vectors. It provide a preconditioner matrix that is block-diagonal with banded blocks. The blocking corresponds to the distribution of the dependent variable vector y among the processors. Each preconditioner block is generated from the Jacobian of the local part (on the current processor) of a given function g(t,y) approximating f(t,y) (see GlocalFn). The blocks are generated by a difference quotient scheme on each processor independently. This scheme utilizes an assumed banded structure with given half-bandwidths, mldq and mudq (specified through LowerBwidthDQ and UpperBwidthDQ, respectively). However, the banded Jacobian block kept by the scheme has half-bandwiths ml and mu (specified through LowerBwidth and UpperBwidth), which may be smaller.

- PrecSetupFn Preconditioner setup function [function]

 If PrecType is not 'None', PrecSetupFn specifies an optional function which,
 together with PrecSolve, defines left and right preconditioner matrices
 (either of which can be trivial), such that the product P1*P2 is an
 aproximation to the Newton matrix. PrecSetupFn must be of type CVPrecSetupFn.
 PrecSolveFn Preconditioner solve function [function]
 - If PrecType is not 'None', PrecSolveFn specifies a required function which must solve a linear system Pz = r, for given r. PrecSolveFn must be of type CVPrecSolveFn.
- GlocalFn Local right-hand side approximation funciton for BBDPre [function] If PrecModule is BBDPre, GlocalFn specifies a required function that evaluates a local approximation to the ODE right-hand side. GlocalFn must be of type CVGlocFn.
- GcommFn Inter-process communication function for BBDPre [function]

 If PrecModule is BBDPre, GcommFn specifies an optional function
 to perform any inter-process communication required for the evaluation of
 GlocalFn. GcommFn must be of type CVGcommFn.
- LowerBwidth Jacobian/preconditioner lower bandwidth [integer | 0]
 This property is overloaded. If the Band linear solver is used (see LinSolver),
 it specifies the lower half-bandwidth of the band Jacobian approximation.
 If one of the three iterative linear solvers, GMRES, BiCGStab, or TFQMR is used
 (see LinSolver) and if the BBDPre preconditioner module in CVODES is used

```
(see PrecModule), it specifies the lower half-bandwidth of the retained banded approximation of the local Jacobian block. If the BandPre preconditioner module (see PrecModule) is used, it specifies the lower half-bandwidth of the band preconditioner matrix. LowerBwidth defaults to 0 (no sub-diagonals).
```

UpperBwidth - Jacobian/preconditioner upper bandwidth [integer | 0]

This property is overloaded. If the Band linear solver is used (see LinSolver), it specifies the upper half-bandwidth of the band Jacobian approximation. If one of the three iterative linear solvers, GMRES, BiCGStab, or TFQMR is used (see LinSolver) and if the BBDPre preconditioner module in CVODES is used (see PrecModule), it specifies the upper half-bandwidth of the retained banded approximation of the local Jacobian block. If the BandPre preconditioner module (see PrecModule) is used, it specifies the upper half-bandwidth of the band preconditioner matrix. UpperBwidth defaults to 0 (no super-diagonals).

LowerBwidthDQ - BBDPre preconditioner DQ lower bandwidth [integer | 0] Specifies the lower half-bandwidth used in the difference-quotient Jacobian approximation for the BBDPre preconditioner (see PrecModule).

UpperBwidthDQ - BBDPre preconditioner DQ upper bandwidth [integer | 0]

Specifies the upper half-bandwidth used in the difference-quotient Jacobian approximation for the BBDPre preconditioner (see PrecModule).

Quadratures - Quadrature integration [on | off] Enables or disables quadrature integration.

QuadRhsFn - Quadrature right-hand side function [function]

Specifies the user-supplied function to evaluate the integrand for quadrature computations. See CVQuadRhsfn.

QuadInitCond - Initial conditions for quadrature variables [vector] Specifies the initial conditions for quadrature variables.

QuadErrControl - Error control strategy for quadrature variables [on | off] Specifies whether quadrature variables are included in the error test.

QuadRelTol - Relative tolerance for quadrature variables [scalar 1e-4] Specifies the relative tolerance for quadrature variables. This parameter is used only if QuadErrCon=on.

QuadAbsTol - Absolute tolerance for quadrature variables [scalar or vector 1e-6] Specifies the absolute tolerance for quadrature variables. This parameter is used only if QuadErrCon=on.

ASANumDataPoints - Number of data points for ASA [integer | 100] Specifies the (maximum) number of integration steps between two consecutive check points.

ASAInterpType - Type of interpolation [Polynomial | Hermite]
Specifies the type of interpolation used for estimating the forward solution during the backward integration phase. At this time, the only option is 'Hermite', specifying cubic Hermite interpolation.

MonitorFn - User-provied monitoring function [function]

Specifies a function that is called after each successful integration step.

This function must have type CVMonitorFn. A simple monitoring function,

CVodeMonitor is provided with CVODES.

MonitorData - User-provied data for the monitoring function [struct] Specifies a data structure that is passed to the Monitor function every time it is called.

ErrMessages - Turn on/off display of error/warning messages [on | off]

CVodeSetFSAOptions

Purpose

CVodeSetFSAOptions creates an options structure for FSA with CVODES.

Synopsis

function options = CVodeSetFSAOptions(varargin)

Description

CVodeSetFSAOptions creates an options structure for FSA with CVODES.

OPTIONS = CVodeSetFSAOptions('NAME1', VALUE1, 'NAME2', VALUE2,...) creates a CVODES options structure OPTIONS in which the named properties have the specified values. Any unspecified properties have default values. It is sufficient to type only the leading characters that uniquely identify the property. Case is ignored for property names.

OPTIONS = CVodeSetFSAOptions(OLDOPTIONS,'NAME1',VALUE1,...) alters an existing options structure OLDOPTIONS.

OPTIONS = CVodeSetFSAOptions(OLDOPTIONS, NEWOPTIONS) combines an existing options structure OLDOPTIONS with a new options structure NEWOPTIONS. Any new properties overwrite corresponding old properties.

 ${\tt CVodeSetFSAOptions\ with\ no\ input\ arguments\ displays\ all\ property\ names\ and\ their\ possible\ values.}$

CVodeSetFSAOptions properties (See also the CVODES User Guide)

ParamField - Problem parameters [string]

Specifies the name of the field in the user data structure (passed as an argument to CVodeMalloc) in which the nominal values of the problem parameters are stored. This property is used only if CVODES will use difference quotient approximations to the sensitivity right-hand sides (see SensRhsFn).

ParamList - Parameters with respect to which FSA is performed [integer vector] Specifies a list of Ns parameters with respect to which sensitivities are to be computed. This property is used only if CVODES will use difference-quotient approximations to the sensitivity right-hand sides (see SensRhsFn below).

Its length must be Ns, consistent with the number of columns of ySO (see CVodeSensMalloc).

- ParamScales Order of magnitude for problem parameters [vector]

 Provides order of magnitude information for the parameters with respect to
 which sensitivities are computed. This information is used if CVODES
 approximates the sensitivity right-hand sides (see SensRhsFn below) or if CVODES
 estimates integration tolerances for the sensitivity variables (see SensReltol
 and SensAbsTol).
- SensRelTol Relative tolerance for sensitivity variables [positive scalar] Specifies the scalar relative tolerance for the sensitivity variables. See also SensAbsTol.
- SensAbsTol Absolute tolerance for sensitivity variables [row-vector or matrix] Specifies the absolute tolerance for sensitivity variables. SensAbsTol must be either a row vector of dimension Ns, in which case each of its components is used as a scalar absolute tolerance for the coresponding sensitivity vector, or a N x Ns matrix, in which case each of its columns is used as a vector of absolute tolerances for the corresponding sensitivity vector.

 By default, CVODES estimates the integration tolerances for sensitivity variables, based on those for the states and on the order of magnitude information for the problem parameters specified through ParamScales.
- SensErrControl Error control strategy for sensitivity variables [on | off] Specifies whether sensitivity variables are included in the error control test. Note that sensitivity variables are always included in the nonlinear system convergence test.
- SensRhsFn Sensitivity right-hand side function [function]

 Specifies a user-supplied function to evaluate the sensitivity right-hand sides. If not specified, CVODES uses a default internal difference-quotient function to approximate the sensitivity right-hand sides.
- SensDQtype Type of DQ approx. of the sensi. RHS [Centered | Forward]
 Specifies whether to use centered (second-order) or forward (first-order)
 difference quotient approximations of the sensitivity eqation right-hand
 sides. This property is used only if a user-defined sensitivity right-hand
 side function was not provided.
- SensDQparam Cut-off parameter for the DQ approx. of the sensi. RHS [scalar | 0.0] Specifies the value which controls the selection of the difference-quotient scheme used in evaluating the sensitivity right-hand sides (switch between simultaneous or separate evaluations of the two components in the sensitivity right-hand side). The default value 0.0 indicates the use of simultaneous approximation exclusively (centered or forward, depending on the value of SensDQtype. For SensDQparam >= 1, CVODES uses a simultaneous approximation if the estimated DQ perturbations for states and parameters are within a factor of SensDQparam, and separate approximations otherwise. Note that a value SensDQparam < 1 will inhibit switching! This property is used only if a user-defined sensitivity right-hand side function was not provided.

See also CVodeSensMalloc, CVSensRhsFn

CVodeMalloc

Purpose

CVodeMalloc allocates and initializes memory for CVODES.

Synopsis

function [] = CVodeMalloc(fct,t0,y0,varargin)

DESCRIPTION

CVodeMalloc allocates and initializes memory for CVODES.

Usage: CVodeMalloc (ODEFUN, TO, YO [, OPTIONS [, DATA]])

ODEFUN is a function defining the ODE right-hand side: y' = f(t,y). This function must return a vector containing the current

value of the righ-hand side.

TO is the initial value of t.

YO is the initial condition vector y(t0).

OPTIONS is an (optional) set of integration options, created with

the CVodeSetOptions function.

DATA is (optional) problem data passed unmodified to all

user-provided functions when they are called. For example,

YD = ODEFUN(T, Y, DATA).

See also: CVRhsFn

CVodeSensMalloc

$\mathbf{Purpose}$

CVodeSensMalloc allocates and initializes memory for FSA with CVODES.

Synopsis

function [] = CVodeSensMalloc(Ns,meth,yS0,varargin)

DESCRIPTION

CVodeSensMalloc allocates and initializes memory for FSA with CVODES.

Usage: CVodeSensMalloc (NS, METH, YSO [, OPTIONS])

 ${\tt NS}$ is the number of parameters with respect to which sensitivities

are desired

METHOD FSA solution method ['Simultaneous' | 'Staggered']

Specifies the FSA method for treating the nonlinear system solution for sensitivity variables. In the simultaneous case, the nonlinear systems for states and all sensitivities are solved simultaneously. In the Staggered case, the nonlinear system for states is solved first and then the nonlinear systems for all sensitivities are solved at the same time.

YSO Initial conditions for sensitivity variables.

YSO must be a matrix with N rows and Ns columns, where N is the problem dimension and Ns the number of sensitivity systems.

 ${\tt OPTIONS} \quad \hbox{is an (optional) set of FSA options, created with} \\$

the CVodeSetFSAOptions function.

CVadjMalloc

Purpose

CVadjMalloc allocates and initializes memory for ASA with CVODES.

Synopsis

function [] = CVadjMalloc(steps, interp)

DESCRIPTION

CVadjMalloc allocates and initializes memory for ASA with CVODES.

Usage: CVadjMalloc(STEPS, INTEPR)

STEPS specifies the (maximum) number of integration steps between two

consecutive check points.

INTERP Specifies the type of interpolation used for estimating the forward

solution during the backward integration phase. INTERP should be 'Hermite', indicating cubic Hermite interpolation, or 'Polynomial',

indicating variable order polynomial interpolation.

CVodeMallocB

Purpose

CVodeMallocB allocates and initializes backward memory for CVODES.

Synopsis

function [] = CVodeMallocB(fctB,tB0,yB0,varargin)

DESCRIPTION

CVodeMallocB allocates and initializes backward memory for CVODES.

Usage: CVodeMallocB (FCTB, TBO, YBO [, OPTIONSB])

FCTB is a function defining the adjoint ODE right-hand side.

This function must return a vector containing the current

value of the adjoint ODE righ-hand side.

TBO is the final value of t.

YBO is the final condition vector yB(tB0).

 ${\tt OPTIONSB} \ \, {\tt is \ \, an \ \, (optional) \ \, set \ \, of \ \, integration \ \, options, \ \, created \ \, with }$

the ${\tt CVodeSetOptions}$ function.

See also: CVRhsFn

CVode

PURPOSE

CVode integrates the ODE.

Synopsis

function [status,t,y,varargout] = CVode(tout,itask)

DESCRIPTION

CVode integrates the ODE.

```
Usage: [STATUS, T, Y] = CVode ( TOUT, ITASK )

[STATUS, T, Y, YS] = CVode ( TOUT, ITASK )

[STATUS, T, Y, YQ] = CVode ( TOUT, ITASK )

[STATUS, T, Y, YQ, YS] = CVode ( TOUT, ITASK )
```

If ITASK is 'Normal', then the solver integrates from its current internal T value to a point at or beyond TOUT, then interpolates to T = TOUT and returns Y(TOUT). If ITASK is 'OneStep', then the solver takes one internal time step and returns in Y the solution at the new internal time. In this case, TOUT is used only during the first call to CVode to determine the direction of integration and the rough scale of the problem. In either case, the time reached by the solver is returned in T. The 'NormalTstop' and 'OneStepTstop' modes are similar to 'Normal' and 'OneStep', respectively, except that the integration never proceeds past the value tstop.

If quadratures were computed (see CVodeSetOptions), CVode will return their values at T in the vector YQ.

If sensitivity calculations were enabled (see CVodeSetOptions), CVode will return their values at T in the matrix YS.

On return, STATUS is one of the following:

- 0: CVode succeeded and no roots were found.
- 1: CVode succeded and returned at tstop.
- 2: CVode succeeded, and found one or more roots.
- -1: Illegal attempt to call before CVodeMalloc
- -2: One of the inputs to CVode is illegal. This includes the situation when a component of the error weight vectors becomes < 0 during internal time-stepping.
- -4: The solver took mxstep internal steps but could not reach TOUT. The default value for mxstep is 500.
- -5: The solver could not satisfy the accuracy demanded by the user for some internal step.
- -6: Error test failures occurred too many times (MXNEF = 7) during one internal time step or occurred with |h| = hmin.
- -7: Convergence test failures occurred too many times (MXNCF = 10) during one internal time step or occurred with |h| = hmin.
- -9: The linear solver's setup routine failed in an unrecoverable manner.
- -10: The linear solver's solve routine failed in an unrecoverable manner.

See also ${\tt CVodeSetOptions}$, ${\tt CVodeGetStats}$

CVodeB

Purpose

CVodeB integrates the backward ODE.

Synopsis

function [status,t,yB,varargout] = CVodeB(tout,itask)

Description

CVodeB integrates the backward ODE.

```
Usage: [STATUS, T, YB] = CVodeB ( TOUT, ITASK )

[STATUS, T, YB, YQB] = CVodeB ( TOUT, ITASK )
```

If ITASK is 'Normal', then the solver integrates from its current internal T value to a point at or beyond TOUT, then interpolates to T = TOUT and returns YB(TOUT). If ITASK is 'OneStep', then the solver takes one internal time step and returns in YB the solution at the new internal time. In this case, TOUT is used only during the first call to CVodeB to determine the direction of integration and the rough scale of the problem. In either case, the time reached by the solver is returned in T.

If quadratures were computed (see CVodeSetOptions), CVodeB will return their values at T in the vector YQB.

On return, STATUS is one of the following:

- 0: CVodeB succeeded and no roots were found.
- -2: One of the inputs to CVodeB is illegal.
- -4: The solver took mxstep internal steps but could not reach TOUT. The default value for mxstep is 500.
- -5: The solver could not satisfy the accuracy demanded by the user for some internal step.
- -6: Error test failures occurred too many times (MXNEF = 7) during one internal time step or occurred with |h| = hmin.
- -7: Convergence test failures occurred too many times (MXNCF = 10) during one internal time step or occurred with |h| = hmin.
- -9: The linear solver's setup routine failed in an unrecoverable manner.
- -10: The linear solver's solve routine failed in an unrecoverable manner.
- -101: Illegal attempt to call before initializing adjoint sensitivity (see CVodeMalloc).
- -104: Illegal attempt to call before CVodeMallocB.
- -108: Wrong value for TOUT.

See also CVodeSetOptions, CVodeGetStatsB

CVodeGetStats

PURPOSE

CVodeGetStats returns run statistics for the CVODES solver.

Synopsis

function si = CVodeGetStats()

DESCRIPTION

CVodeGetStats returns run statistics for the CVODES solver.

Usage: STATS = CVodeGetStats

Fields in the structure STATS

- o nst number of integration steps
- o nfe number of right-hand side function evaluations
- o nsetups number of linear solver setup calls
- o netf number of error test failures
- o nni number of nonlinear solver iterations o ncfn - number of convergence test failures
- o qlast last method order used o qcur - current method order
- o hOused actual initial step size used
- o hlast last step size used o hcur current step size
- o tcur current time reached by the integrator
 o RootInfo strucutre with rootfinding information
- o QuadInfo structure with quadrature integration statistics
- o LSInfo structure with linear solver statistics
- o FSAInfo structure with forward sensitivity solver statistics

If rootfinding was requested, the structure RootInfo has the following fields

- o nge number of calls to the rootfinding function
- o roots array of integers (a value of 1 in the i-th component means that the i-th rootfinding function has a root (upon a return with status=2 from CVode).

If quadratures were present, the structure QuadInfo has the following fields

- o nfQe number of quadrature integrand function evaluations
- o netfQ number of error test failures for quadrature variables

The structure LSinfo has different fields, depending on the linear solver used.

Fields in LSinfo for the 'Dense' linear solver

- o name 'Dense'
- o njeD number of Jacobian evaluations
- o nfeD number of right-hand side function evaluations for difference-quotient Jacobian approximation

Fields in LSinfo for the 'Diag' linear solver

- o name 'Diag'
- o nfeDI number of right-hand side function evaluations for difference-quotient Jacobian approximation

Fields in LSinfo for the 'Band' linear solver

- o name 'Band'
- o njeB number of Jacobian evaluations

o nfeB - number of right-hand side function evaluations for difference-quotient Jacobian approximation

Fields in LSinfo for the 'GMRES' and 'BiCGStab' linear solvers

- o name 'GMRES' or 'BiCGStab'
- o nli number of linear solver iterations
- o npe number of preconditioner setups
- o nps number of preconditioner solve function calls
- o ncfl number of linear system convergence test failures
- o njeSG number of Jacobian-vector product evaluations
- o nfeSG number of right-hand side function evaluations for difference-quotient Jacobian-vector product approximation

If forward sensitivities were computed, the structure FSAInfo has the following fields

- o nfSe number of sensitivity right-hand side evaluations
- o nfeS number of right-hand side evaluations for difference-quotient
 - sensitivity right-hand side approximation
- o nsetupsS number of linear solver setups triggered by sensitivity variables
- o netfS number of error test failures for sensitivity variables
- o ${\tt nniS}$ number of nonlinear solver iterations for sensitivity variables
- o ncfnS number of convergence test failures due to sensitivity variables

CVodeGetStatsB

PURPOSE

CVodeGetStatsB returns run statistics for the backward CVODES solver.

Synopsis

function si = CVodeGetStatsB()

DESCRIPTION

CVodeGetStatsB returns run statistics for the backward CVODES solver.

Usage: STATS = CVodeGetStatsB

Fields in the structure STATS

- o nst number of integration steps
- o nfe number of right-hand side function evaluations
- o nsetups number of linear solver setup calls
- o netf number of error test failures
- o nni number of nonlinear solver iterations
- o ncfn number of convergence test failures
- o qlast last method order used
- o qcur current method order
- o hOused actual initial step size used
- o hlast last step size used
- o hcur current step size

```
o tcur - current time reached by the integrator
```

- o QuadInfo structure with quadrature integration statistics
- o LSInfo structure with linear solver statistics

The structure LSinfo has different fields, depending on the linear solver used.

If quadratures were present, the structure QuadInfo has the following fields

- o nfQe number of quadrature integrand function evaluations
- o netfQ number of error test failures for quadrature variables

Fields in LSinfo for the 'Dense' linear solver

- o name 'Dense'
- o njeD number of Jacobian evaluations
- o nfeD number of right-hand side function evaluations for difference-quotient Jacobian approximation

Fields in LSinfo for the 'Diag' linear solver

- o name 'Diag'
- o nfeDI number of right-hand side function evaluations for difference-quotient Jacobian approximation

Fields in LSinfo for the 'Band' linear solver

- o name 'Band'
- o njeB number of Jacobian evaluations
- o nfeB number of right-hand side function evaluations for difference-quotient Jacobian approximation

Fields in LSinfo for the 'GMRES' and 'BiCGStab' linear solvers

- o name 'GMRES' or 'BiCGStab'
- o nli number of linear solver iterations
- o npe number of preconditioner setups
- o nps number of preconditioner solve function calls
- o ncfl number of linear system convergence test failures
- o njeSG number of Jacobian-vector product evaluations
- o nfeSG number of right-hand side function evaluations for difference-quotient Jacobian-vector product approximation

CVodeGet

PURPOSE

CVodeGet extracts data from the CVODES solver memory.

Synopsis

function varargout = CVodeGet(key, varargin)

DESCRIPTION

CVodeGet extracts data from the CVODES solver memory.

```
Usage: RET = CVodeGet ( KEY [, P1 [, P2] ... ])
```

CVodeGet returns internal CVODES information based on KEY. For some values of KEY, additional arguments may be required and/or more than one output is returned.

KEY is a string and should be one of:

- o DerivSolution Returns a vector containing the K-th order derivative of the solution at time T. The time T and order K must be passed through the input arguments P1 and P2, respectively:

 DKY = CVodeGet('DerivSolution', T, K)
- o ErrorWeights Returns a vector containing the current error weights. EWT = CVodeGet('ErrorWeights')
- o CheckPointsInfo Returns an array of structures with check point information. CK = CVodeGet('CheckPointInfo)
- o CurrentCheckPoint Returns the address of the active check point ADDR = CVodeGet('CurrentCheckPoint');
- o DataPointInfo Returns information stored for interpolation at the I-th data point in between the current check points. The index I must be passed through the agument P1.

If the interpolation type was Hermite (see CVodeSetOptions), it returns two vectors, Y and YD:

[Y, YD] = CVodeGet('DataPointInfo', I)

CVodeFree

PURPOSE

CVodeFree deallocates memory for the CVODES solver.

Synopsis

function [] = CVodeFree()

Description

CVodeFree deallocates memory for the CVODES solver.

Usage: CVodeFree

CVodeMonitor

PURPOSE

CVodeMonitor is the default CVODES monitoring function.

Synopsis

function [new_data] = CVodeMonitor(call, T, Y, YQ, YS, data)

Description

```
{\tt CVodeMonitor}\ \ {\tt is}\ \ {\tt the}\ \ {\tt default}\ \ {\tt CVODES}\ \ {\tt monitoring}\ \ {\tt function}.
```

To use it, set the Monitor property in CVodeSetOptions to 'CVodeMonitor' or to @CVodeMonitor and 'MonitorData' to mondata (defined as a structure).

With default settings, this function plots the evolution of the step size, method order, and various counters.

Various properties can be changed from their default values by passing to CVodeSetOptions, through the property 'MonitorData', a structure MONDATA with any of the following fields. If a field is not defined, the corresponding default value is used.

```
Fields in MONDATA structure:
```

- o stats [true | false]
 - If true, report the evolution of the step size and method order.
- o cntr [true | false]
 - If true, report the evolution of the following counters:
 - nst, nfe, nni, netf, ncfn (see CVodeGetStats)
- o mode ['graphical' | 'text' | 'both']
 - In graphical mode, plot the evolutions of the above quantities.
 - In text mode, print a table.
- o sol [true | false]
 - If true, plot solution components.
- o sensi [true | false]
 - If true and if FSA is enabled, plot sensitivity components.
- o select [array of integers]
 - To plot only particular solution components, specify their indeces in
 - the field select. If not defined, but sol=true, all components are plotted.
- o updt [integer | 50]
 - Update frequency. Data is posted in blocks of dimension n.
- o skip [integer | 0]
 - Number of integrations steps to skip in collecting data to post.
- o dir [1 | -1]
 - Specifies forward or backward integration.
- o post [true | false]
 - If false, disable all posting. This option is necessary to disable monitoring on some processors when running in parallel.

See also CVodeSetOptions, CVMonitorFn

NOTES:

- 1. The argument mondata is REQUIRED. Even if only the default options are desired, set mondata=struct; and pass it to CVodeSetOptions.
- 2. The yQ argument is currently ignored.

SOURCE CODE

```
function [new_data] = CVodeMonitor(call, T, Y, YQ, YS, data)

Radu Serban <radu@llnl.gov>
Copyright (c) 2005, The Regents of the University of California.
Revision: 1.4 $Date: 2006/10/05 22:12:20 $
```

```
new_data = [];
53
   if call == 0
55
56
   % Initialize unspecified fields to default values.
57
      data = initialize_data(data);
58
59
   % Open figure windows
60
      if data.post
61
62
        if data.grph
63
          if data.stats | data.cntr
64
             data.hfg = figure;
65
          end
66
          Number of subplots in figure hfg
   %
67
          if data.stats
68
            data.npg = data.npg + 2;
69
          end
70
          if data.cntr
71
            data.npg = data.npg + 1;
72
          end
73
        end
74
75
        if data.text
76
          if data.cntr | data.stats
77
            data.hft = figure;
78
          end
79
        end
80
81
        if data.sol | data.sensi
82
          data.hfs = figure;
83
        end
84
85
      end
86
87
   % Initialize other private data
88
      data.i = 0;
89
      data.n = 1;
      data.t = zeros(1, data.updt);
91
      if data.stats
        data.h = zeros(1, data.updt);
93
        data.q = zeros(1, data.updt);
94
95
      if data.cntr
96
        data.nst = zeros(1, data.updt);
97
        data.nfe = zeros(1, data.updt);
98
        data.nni = zeros(1, data.updt);
99
        data.netf = zeros(1, data.updt);
100
        data.ncfn = zeros(1, data.updt);
101
      end
102
103
      data.first = true;
                                   % the next one will be the first call = 1
104
      data.initialized = false; % the graphical windows were not initalized
105
106
```

```
new_data = data;
107
      return;
109
    else
111
   % If this is the first call \tilde{}=0,
113
   % use Y and YS for additional initializations
114
115
      if data.first
116
117
         if isempty (YS)
118
           data.sensi = false;
        end
120
121
         if data.sol | data.sensi
122
123
           if isempty(data.select)
124
125
             data.N = length(Y);
126
             data.select = [1:data.N];
128
           else
129
130
             data.N = length (data.select);
131
132
           end
133
134
           if data.sol
135
             data.y = zeros (data.N, data.updt);
136
             data.nps = data.nps + 1;
137
           end
138
139
           if data.sensi
140
             data.Ns = size(YS, 2);
141
             data.ys = zeros(data.N, data.Ns, data.updt);
             data.nps = data.nps + data.Ns;
143
           end
145
         end
146
147
        data.first = false;
148
149
      end
150
151
   % Extract variables from data
152
153
      hfg
          = data.hfg;
154
      hft
           = data.hft;
155
      hfs
           = data.hfs;
156
           = data.npg;
      npg
157
      nps
           = data.nps;
158
      i
            = data.i;
      \mathbf{n}
            = data.n;
160
```

```
= data.t;
161
      Ν
            = data.N;
162
      Ns
            = data.Ns;
163
            = data.y;
      у
            = data.ys;
      уs
165
            = data.h;
      h
166
            = data.q;
167
            = data.nst;
      nst
168
      nfe = data.nfe;
169
      nni = data.nni;
170
      netf = data.netf;
171
      ncfn = data.ncfn;
172
    end
174
175
176
   % Load current statistics?
177
178
    if call == 1
179
180
      if i \tilde{}=0
         i = i - 1;
182
         data.i = i;
183
         new_data = data;
184
         return;
185
      end
186
187
      if data.dir == 1
188
         si = CVodeGetStats;
189
      else
190
         si = CVodeGetStatsB;
191
      end
192
193
      t(n) = si.tcur;
194
195
      if data.stats
         h(n) = si.hlast;
197
        q(n) = si.qlast;
      end
199
200
      if data.cntr
201
         nst(n) = si.nst;
202
         nfe(n) = si.nfe;
203
         nni(n) = si.nni;
204
         netf(n) = si.netf;
205
         ncfn(n) = si.ncfn;
206
      end
207
208
      if data.sol
209
         for j = 1:N
210
           y(j,n) = Y(data.select(j));
211
         end
212
      end
213
214
```

```
if data.sensi
215
         for k = 1:Ns
216
           for j = 1:N
217
             ys(j,k,n) = YS(data.select(j),k);
219
         end
220
      end
221
222
    end
223
224
   % Is it time to post?
225
226
    if data.post & (n == data.updt | call == 2)
227
228
      if call == 2
229
        n = n-1;
230
      end
231
232
      if "data.initialized
233
234
         if (data.stats | data.cntr) & data.grph
           graphical_init (n, hfg, npg, data.stats, data.cntr, data.dir, ...
236
                            t, h, q, nst, nfe, nni, netf, ncfn);
237
         end
238
239
         if (data.stats | data.cntr) & data.text
240
           text_init(n, hft, data.stats, data.cntr, ...
241
                      t\;,\;\;h\;,\;\;q\;,\;\;nst\;,\;\;nfe\;,\;\;nni\;,\;\;netf\;,\;\;ncfn\;)\;;
242
         end
243
244
         if data.sol | data.sensi
245
           sol_init(n, hfs, nps, data.sol, data.sensi, data.dir, ...
246
                     N, Ns, t, y, ys;
247
         end
248
249
         data.initialized = true;
250
251
      else
252
253
         if (data.stats | data.cntr) & data.grph
254
           graphical_update(n, hfg, npg, data.stats, data.cntr, ...
255
                               t, h, q, nst, nfe, nni, netf, ncfn);
256
         end
257
258
         if (data.stats | data.cntr) & data.text
259
           text_update(n, hft, data.stats, data.cntr, ...
260
                         t, h, q, nst, nfe, nni, netf, ncfn);
261
         end
262
263
         if data.sol
264
           sol_update(n, hfs, nps, data.sol, data.sensi, N, Ns, t, y, ys);
265
        end
266
267
      end
268
```

```
269
      if call == 2
270
271
         if (data.stats | data.cntr) & data.grph
272
           graphical_final(hfg, npg, data.cntr, data.stats);
273
         end
274
275
         if data.sol | data.sensi
276
           sol_final(hfs, nps, data.sol, data.sensi, N, Ns);
277
         end
278
279
         return;
280
281
      end
282
283
      n = 1;
284
285
    else
286
287
      n = n + 1;
288
290
291
292
   % Save updated values in data
293
294
    data.i
               = data.skip;
295
    data.n
               = n;
296
    data.npg
               = npg;
297
    data.t
               = t;
298
    data.y
               = y;
299
    data.ys
               = ys;
300
    data.h
               = h;
301
    data.q
               = q;
302
    data.nst = nst;
303
    data.nfe
               = nfe;
    data.nni
               = nni;
305
    data.netf = netf;
    data.ncfn = ncfn;
307
308
    new_data = data;
309
310
    return;
311
312
313
314
    function data = initialize_data(data)
315
316
    if ~isfield (data, 'mode')
317
      data.mode = 'graphical';
318
319
    if ~isfield(data, 'updt')
320
      data.updt = 50;
322
   end
```

```
if ~isfield (data, 'skip')
323
      data.skip = 0;
324
325
   if ~isfield(data, 'stats')
     data.stats = true;
327
328
   if ~isfield(data,'cntr')
329
      data.cntr = true;
330
   end
331
   if ~isfield(data, 'sol')
332
      data.sol = false;
333
334
   if ~ isfield (data, 'sensi')
335
      data.sensi = false;
336
337
    if ~isfield(data, 'select')
338
      data.select = [];
339
340
   if ~isfield(data,'dir')
      data.dir = 1;
342
    end
    if ~isfield(data, 'post')
344
      data.post = true;
345
346
347
   data.grph = true;
348
    data.text = true;
349
    if strcmp (data.mode, 'graphical')
350
      data.text = false;
351
   end
352
    if strcmp(data.mode, 'text')
353
      data.grph = false;
354
   end
355
356
    if data.sol & data.sensi
357
      data.select = [];
   end
359
   % Other initializations
361
   data.npg = 0;
362
   data.nps = 0;
363
   data.hfg = 0;
364
   data.hft = 0;
365
   data.hfs = 0;
   data.h = 0:
367
   data.q = 0;
368
   data.nst = 0;
369
   data.nfe = 0;
370
   data.nni = 0;
371
   data.netf = 0;
372
   data.ncfn = 0;
373
   data.N = 0;
374
   data.Ns = 0;
   data.y = 0;
376
```

```
data.ys = 0;
377
379
380
    function [] = graphical_init(n, hfg, npg, stats, cntr, dir, ...
381
                                      t, h, q, nst, nfe, nni, netf, ncfn)
382
383
    fig_name = 'CVODES_run_statistics';
384
385
   % If this is a parallel job, look for the MPI rank in the global
386
   % workspace and append it to the figure name
387
388
    global sundials_MPI_rank
389
390
    if ~isempty (sundials_MPI_rank)
391
      fig_name = sprintf('%s_(PE_%d)', fig_name, sundials_MPI_rank);
392
   end
393
394
    figure (hfg);
395
    set(hfg,'Name',fig_name);
396
    set(hfg, 'color', [1 1 1]);
397
    pl = 0;
398
399
   % Time label and figure title
400
401
   if dir == 1
402
      tlab = '\rightarrow___t_\rightarrow';
403
404
      tlab = '\leftarrow___t_\leftarrow';
405
   end
406
407
   % Step size and order
408
   if stats
409
      pl = pl + 1;
410
      subplot (npg, 1, pl)
411
      semilogy(t(1:n), abs(h(1:n)), '-');
412
      hold on;
413
      box on;
414
      grid on;
415
      xlabel(tlab);
416
      ylabel('|Step_size|');
417
418
      pl = pl + 1;
419
      subplot(npg,1,pl)
420
      plot (t (1:n), q (1:n), '-');
421
      hold on;
422
      box on;
423
      grid on;
424
      xlabel(tlab);
425
      vlabel('Order');
426
   end
427
428
   % Counters
429
   if cntr
430
```

```
pl = pl + 1;
431
      subplot(npg,1,pl)
432
      plot(t(1:n), nst(1:n), 'k-');
433
      hold on;
      plot(t(1:n), nfe(1:n), 'b-');
435
      plot (t (1:n), nni (1:n), 'r-');
436
      plot(t(1:n), netf(1:n), 'g-');
437
      plot(t(1:n), ncfn(1:n), 'c-');
438
      box on:
439
440
      grid on;
      xlabel(tlab);
441
      ylabel('Counters');
442
    end
443
444
    drawnow;
445
446
447
448
    function [] = graphical\_update(n, hfg, npg, stats, cntr, ...
                                          t, h, q, nst, nfe, nni, netf, ncfn)
450
451
    figure (hfg);
452
    pl = 0;
453
454
   % Step size and order
455
    if stats
456
      pl = pl + 1;
457
      subplot (npg, 1, pl)
458
      hc = get(gca, 'Children');
459
      xd = [get(hc, 'XData') t(1:n)];
460
      yd = [get(hc, 'YData') abs(h(1:n))];
461
      set (hc, 'XData', xd, 'YData', yd);
462
463
      pl = pl + 1;
464
      subplot(npg,1,pl)
465
      \begin{array}{ll} hc \ = \ get(gca, 'Children'); \\ xd \ = \ [get(hc, 'XData') \ t(1:n)]; \end{array}
467
      yd = [get(hc, 'YData') q(1:n)];
      set (hc, 'XData', xd, 'YData', yd);
469
    end
470
471
   % Counters
472
    if cntr
473
      pl = pl + 1;
474
      subplot (npg, 1, pl)
475
      hc = get(gca, 'Children');
476
      Attention: Children are loaded in reverse order!
477
      xd = [get(hc(1), 'XData') t(1:n)];
478
      yd = [get(hc(1), 'YData') ncfn(1:n)];
479
      set (hc(1), 'XData', xd, 'YData', yd);
480
      yd = [get(hc(2), 'YData') netf(1:n)];
481
      set (hc(2), 'XData', xd, 'YData', yd);
482
      yd = [get(hc(3), 'YData') nni(1:n)];
483
      set (hc(3), 'XData', xd, 'YData', yd);
484
```

```
yd = [get(hc(4), 'YData') nfe(1:n)];
485
      set(hc(4), 'XData', xd, 'YData', yd);
      yd = [get(hc(5), YData), nst(1:n)];
487
      set(hc(5), 'XData', xd, 'YData', yd);
489
490
    drawnow;
491
492
493
494
    function [] = graphical_final(hfg,npg,stats,cntr)
495
496
    figure (hfg);
497
    pl = 0;
498
499
500
    if stats
      pl = pl + 1;
501
      subplot(npg,1,pl)
502
      hc = get(gca, 'Children');
503
      xd = get(hc, 'XData');
504
      set (gca, 'XLim', sort ([xd(1) xd(end)]));
505
506
      pl = pl + 1;
507
      subplot(npg,1,pl)
508
      ylim = get(gca, 'YLim');
509
      ylim(1) = ylim(1) - 1;
510
      y \lim (2) = y \lim (2) + 1;
511
      set (gca , 'YLim', ylim);
512
      set (gca, 'XLim', sort ([xd(1) xd(end)]));
513
    end
514
515
    if cntr
516
      pl = pl + 1;
517
      subplot(npg,1,pl)
518
      hc = get(gca, 'Children');
519
      xd = get(hc(1), 'XData');
      set (gca, 'XLim', sort ([xd(1) xd(end)]));
521
      legend('nst', 'nfe', 'nni', 'netf', 'ncfn', 2);
523
524
525
526
    function [] = text_init(n, hft, stats, cntr, t, h, q, nst, nfe, nni, netf, ncfn)
527
528
    fig_name = 'CVODES_run_statistics';
529
530
   % If this is a parallel job, look for the MPI rank in the global
   % workspace and append it to the figure name
532
533
    global sundials_MPI_rank
534
    if ~isempty (sundials_MPI_rank)
536
      fig_name = sprintf('%s_(PE_%d)', fig_name, sundials_MPI_rank);
   end
538
```

```
539
         figure (hft);
         set(hft, 'Name', fig_name);
541
         set(hft, 'color',[1 1 1]);
542
         set(hft, 'MenuBar', 'none');
543
         set(hft, 'Resize', 'off');
544
545
        % Create text box
546
547
         margins=[10 10 50 50]; % left, right, top, bottom
548
         pos=get(hft, 'position');
549
         tbpos = [margins(1) \ margins(4) \ pos(3) - margins(1) - margins(2) \dots
550
                          pos(4) - margins(3) - margins(4);
         tbpos(tbpos<1)=1;
552
        htb=uicontrol(hft, 'style', 'listbox', 'position', tbpos, 'tag', 'textbox');
554
         set (htb, 'BackgroundColor',[1 1 1]);
555
         set(htb,'SelectionHighlight','off');
556
         set(htb, 'FontName', 'courier');
557
558
        % Create table head
559
560
        tpos = [tbpos(1) tbpos(2) + tbpos(4) + 10 tbpos(3) 20];
561
        ht=uicontrol(hft, 'style', 'text', 'position', tpos, 'tag', 'text');
562
         set(ht, 'BackgroundColor',[1 1 1]);
563
         set(ht, 'HorizontalAlignment', 'left');
564
         set (ht, 'FontName', 'courier');
565
         newline = 'untimendation step near order o
566
         set(ht, 'String', newline);
567
568
        % Create OK button
569
570
         bsize = [60, 28];
571
         badjustpos = [0, 25];
572
         bpos = [pos(3)/2 - bsize(1)/2 + badjustpos(1) - bsize(2)/2 + badjustpos(2)...
573
                        bsize(1) bsize(2)];
         bpos=round(bpos);
575
         bpos(bpos<1)=1;
576
        hb=uicontrol(hft, 'style', 'pushbutton', 'position', bpos,...
577
                                           'string', 'Close', 'tag', 'okaybutton');
578
         set (hb, 'callback', 'close');
579
580
        % Save handles
581
582
         handles=guihandles(hft);
583
         guidata(hft, handles);
584
585
         for i = 1:n
586
              newline = '';
587
              if stats
588
                   newline = sprintf('\%10.3e_{--}\%10.3e_{---}\%1d_{---}|',t(i),h(i),q(i));
589
              end
590
              if cntr
591
                   newline = sprintf('\%s - \%5d - \%5d - \%5d - \%5d - \%5d'),...
592
```

```
newline, nst(i), nfe(i), nni(i), netf(i), ncfn(i));
593
      end
594
      string = get(handles.textbox, 'String');
595
      string { end+1}=newline;
596
      set (handles.textbox, 'String', string);
597
    end
598
599
    drawnow
600
601
602
603
    function [] = text_update(n, hft, stats, cntr, t, h, q, nst, nfe, nni, netf, ncfn)
604
    figure (hft);
606
607
    handles=guidata(hft);
608
609
    for i = 1:n
610
        if stats
611
         newline = sprintf('\%10.3e_{---}\%10.3e_{----}\%1d_{----})', t(i), h(i), q(i));
612
      end
613
      if cntr
614
         newline = sprintf('\%s \ \%5d \ \%5d \ \%5d \ \%5d \ \%5d \ \%...
615
                              newline, nst(i), nfe(i), nni(i), netf(i), ncfn(i));
616
      end
617
      string = get(handles.textbox, 'String');
618
      string \{end+1\} = newline;
619
      set (handles.textbox, 'String', string);
620
    end
621
622
    drawnow
623
624
625
626
    function [] = sol_init(n, hfs, nps, sol, sensi, dir, N, Ns, t, y, ys)
627
    fig_name = 'CVODES_solution';
629
630
   % If this is a parallel job, look for the MPI rank in the global
631
   % workspace and append it to the figure name
632
633
    global sundials_MPI_rank
634
635
    if "isempty (sundials_MPI_rank)
636
      fig_name = sprintf('%s_(PE_%d)', fig_name, sundials_MPI_rank);
637
    end
638
639
640
    figure (hfs);
641
    set (hfs, 'Name', fig_name);
642
    set(hfs, 'color', [1 1 1]);
643
644
   % Time label
645
646
```

```
if dir==1
647
      tlab = '\rightarrow \__\rightarrow ';
649
      tlab = '\leftarrow___t_\leftarrow';
650
651
652
   % Get number of colors in colormap
653
    map = colormap;
654
    n cols = size (map, 1);
655
656
   % Initialize current subplot counter
657
    pl = 0;
658
    if sol
660
661
662
      pl = pl + 1;
      subplot (nps , 1 , pl );
663
      hold on;
664
665
      for i = 1:N
666
        hp = plot(t(1:n), y(i, 1:n), '-');
667
         ic = 1+(i-1)*floor(ncols/N);
668
         set (hp, 'Color', map(ic,:));
669
      end
670
      box on;
671
      grid on;
672
      xlabel(tlab);
673
      ylabel('y');
674
      title ('Solution');
675
676
    end
677
678
    if sensi
679
680
      for is = 1:Ns
681
682
         pl = pl + 1;
683
         subplot (nps,1,pl);
684
         hold on;
685
686
         ys\_crt = ys(:, is, 1:n);
687
         for i = 1:N
688
           hp = plot(t(1:n), ys_crt(i, 1:n), '-');
689
           ic = 1+(i-1)*floor(ncols/N);
690
           set (hp, 'Color', map(ic,:));
691
         end
692
         box on;
693
         grid on;
694
         xlabel(tlab);
695
         str = sprintf('s_{{}^{-}}{%d}', is); ylabel(str);
696
         str = sprintf('Sensitivity_%d', is); title(str);
697
698
699
      end
700
```

```
701
    end
703
    drawnow;
704
705
706
707
    function [] = sol_update(n, hfs, nps, sol, sensi, N, Ns, t, y, ys)
708
709
    figure (hfs);
710
711
    pl = 0;
712
    if sol
714
715
      pl = pl + 1;
716
      subplot (nps , 1 , pl );
717
718
      hc = get(gca, 'Children');
      xd = [get(hc(1), 'XData') t(1:n)];
720
    % Attention: Children are loaded in reverse order!
      for i = 1:N
722
         yd = [get(hc(i), 'YData') y(N-i+1,1:n)];
723
         set(hc(i), 'XData', xd, 'YData', yd);
724
      end
725
726
    end
727
    if sensi
729
730
      for is = 1:Ns
731
732
         pl = pl + 1;
733
         subplot(nps,1,pl);
734
735
         ys\_crt = ys(:, is,:);
736
737
         hc = get(gca, 'Children');
738
         xd = [get(hc(1), 'XData') t(1:n)];
739
         Attention: Children are loaded in reverse order!
740
         \quad \quad \text{for} \quad i \ = \ 1\!:\!N
741
           yd = [get(hc(i), 'YData') ys\_crt(N-i+1,1:n)];
742
           set(hc(i), 'XData', xd, 'YData', yd);
743
         end
744
745
      end
746
    end
748
749
750
    drawnow;
751
752
753
754
```

```
755
    function [] = sol_final(hfs, nps, sol, sensi, N, Ns)
756
757
    figure (hfs);
758
759
    pl = 0;
760
761
    if sol
762
763
       pl = pl +1;
764
       subplot (nps,1,pl);
765
766
      hc = get(gca, 'Children');
      xd = get(hc(1), 'XData');
768
       set (gca, 'XLim', sort ([xd(1) xd(end)]));
769
770
       ylim = get (gca, 'YLim');
771
       addon = 0.1 * abs(ylim(2) - ylim(1));
772
       y \lim (1) = y \lim (1) + sign(y \lim (1)) *addon;
773
       y \lim (2) = y \lim (2) + sign(y \lim (2)) * addon;
774
       set (gca , 'YLim', ylim);
775
776
       for i = 1:N
777
         cstring\{i\} = sprintf('y_{-}\{\%d\}', i);
778
       end
779
       legend(cstring);
780
781
    end
782
783
    if sensi
784
785
       for is = 1:Ns
786
787
         pl = pl + 1;
788
         subplot (nps , 1 , pl );
789
790
         hc = get (gca, 'Children');
791
         xd = get(hc(1), 'XData');
792
         set (gca, 'XLim', sort ([xd(1) xd(end)]));
793
794
         ylim = get(gca, 'YLim');
795
         addon = 0.1 * abs(ylim(2) - ylim(1));
796
         ylim(1) = ylim(1) + sign(ylim(1))*addon;
797
         ylim(2) = ylim(2) + sign(ylim(2))*addon;
798
         set(gca, 'YLim', ylim);
799
800
         for i = 1:N
801
           cstring\{i\} = sprintf('s\%d_{\{Md\}}', is, i);
802
803
         legend(cstring);
804
805
       end
806
   end
808
```

810 drawnow

2.2 Function types

CVBandJacFn

PURPOSE

CVBandJacFn - type for user provided banded Jacobian function.

Synopsis

This is a script file.

DESCRIPTION

CVBandJacFn - type for user provided banded Jacobian function.

IVP Problem

The function BJACFUN must be defined as FUNCTION [J, FLAG] = BJACFUN(T, Y, FY)

and must return a matrix J corresponding to the banded Jacobian of f(t,y). The input argument FY contains the current value of f(t,y). If a user data structure DATA was specified in CVodeMalloc, then BJACFUN must be defined as

FUNCTION [J, FLAG, NEW_DATA] = BJACFUN(T, Y, FY, DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the matrix J, the BJACFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function BJACFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function BJACFUNB must be defined either as FUNCTION [JB, FLAG] = BJACFUNB(T, Y, YB, FYB) or as

FUNCTION [JB, FLAG, NEW_DATA] = BJACFUNB(T, Y, YB, FYB, DATA) depending on whether a user data structure DATA was specified in CVodeMalloc. In either case, it must return the matrix JB, the Jacobian of fB(t,y,yB), with respect to yB. The input argument FYB contains the current value of f(t,y,yB).

The function BJACFUNB must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also CVodeSetOptions

See the CVODES user guide for more information on the structure of

a banded Jacobian.

NOTE: BJACFUN and BJACFUNB are specified through the property JacobianFn to CVodeSetOptions and are used only if the property LinearSolver was set to 'Band'.

CVDenseJacFn

Purpose

CVDenseJacFn - type for user provided dense Jacobian function.

Synopsis

This is a script file.

DESCRIPTION

CVDenseJacFn - type for user provided dense Jacobian function.

IVP Problem

The function DJACFUN must be defined as FUNCTION [J, FLAG] = DJACFUN(T, Y, FY)

and must return a matrix J corresponding to the Jacobian of f(t,y). The input argument FY contains the current value of f(t,y). If a user data structure DATA was specified in CVodeMalloc, then DJACFUN must be defined as

FUNCTION [J, FLAG, NEW_DATA] = DJACFUN(T, Y, FY, DATA) If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the matrix J, the DJACFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function DJACFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function DJACFUNB must be defined either as FUNCTION [JB, FLAG] = DJACFUNB(T, Y, YB, FYB) or as

FUNCTION [JB, FLAG, NEW_DATA] = DJACFUNB(T, Y, YB, FYB, DATA) depending on whether a user data structure DATA was specified in CVodeMalloc. In either case, it must return the matrix JB, the Jacobian of fB(t,y,yB), with respect to yB. The input argument FYB contains the current value of f(t,y,yB).

The function DJACFUNB must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also CVodeSetOptions

NOTE: DJACFUN and DJACFUNB are specified through the property JacobianFn to CVodeSetOptions and are used only if the property LinearSolver was set to 'Dense'.

CVGcommFn

PURPOSE

CVGcommFn - type for user provided communication function (BBDPre).

Synopsis

This is a script file.

DESCRIPTION

CVGcommFn - type for user provided communication function (BBDPre).

IVP Problem

The function GCOMFUN must be defined as FUNCTION FLAG = GCOMFUN(T, Y)

and can be used to perform all interprocess communication necessary to evaluate the approximate right-hand side function for the BBDPre preconditioner module.

If a user data structure DATA was specified in CVodeMalloc, then ${\tt GCOMFUN}$ must be defined as

FUNCTION [FLAG, NEW_DATA] = GCOMFUN(T, Y, DATA)

If the local modifications to the user data structure are needed in other user-provided functions then the GCOMFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function GCOMFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function GCOMFUNB must be defined either as FUNCTION FLAG = GCOMFUNB(T, Y, YB)

or as

FUNCTION [FLAG, NEW_DATA] = GCOMFUNB(T, Y, YB, DATA)
depending on whether a user data structure DATA was specified in
CVodeMalloc.

The function GCOMFUNB must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also CVGlocalFn, CVodeSetOptions

NOTES:

GCOMFUN and GCOMFUNB are specified through the GcommFn property in CVodeSetOptions and are used only if the property PrecModule is set to 'BBDPre'.

Each call to GCOMFUN is preceded by a call to the RHS function ODEFUN with the same arguments T and Y (and YB in the case of GCOMFUNB). Thus GCOMFUN can omit any communication done by ODEFUN if relevant to the evaluation of G by GLOCFUN. If all necessary communication was done by ODEFUN, GCOMFUN need not be provided.

CVGlocalFn

Purpose

CVGlocalFn - type for user provided RHS approximation function (BBDPre).

Synopsis

This is a script file.

DESCRIPTION

CVGlocalFn - type for user provided RHS approximation function (BBDPre).

IVP Problem

The function GLOCFUN must be defined as FUNCTION [GLOC, FLAG] = GLOCFUN(T,Y)

and must return a vector GLOC corresponding to an approximation to f(t,y) which will be used in the BBDPRE preconditioner module. The case where G is mathematically identical to F is allowed.

If a user data structure DATA was specified in CVodeMalloc, then GLOCFUN must be defined as

FUNCTION [GLOC, FLAG, NEW_DATA] = GLOCFUN(T,Y,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector G, the GLOCFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function GLOCFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function GLOCFUNB must be defined either as FUNCTION [GLOCB, FLAG] = GLOCFUNB(T,Y,YB) or as

FUNCTION [GLOCB, FLAG, NEW_DATA] = GLOCFUNB(T,Y,YB,DATA) depending on whether a user data structure DATA was specified in CVodeMalloc. In either case, it must return the vector GLOCB corresponding to an approximation to fB(t,y,yB).

The function GLOCFUNB must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also CVGcommFn, CVodeSetOptions

NOTE: GLOCFUN and GLOCFUNB are specified through the GlocalFn property in CVodeSetOptions and are used only if the property PrecModule is set to 'BBDPre'.

CVMonitorFn

Purpose

CVMonitorFn - type for user provided monitoring function.

Synopsis

This is a script file.

DESCRIPTION

CVMonitorFn - type for user provided monitoring function.

The function MONFUN must be defined as FUNCTION [] = MONFUN(CALL, T, Y, YQ, YS)

It is called after every internal CVode step and can be used to monitor the progress of the solver. MONFUN is called with CALL=0 from CVodeMalloc at which time it should initialize itself and it is called with CALL=2 from CVodeFree. Otherwise, CALL=1.

It receives as arguments the current time T, solution vector Y, and, if they were computed, quadrature vector YQ, and forward sensitivity matrix YS. If YQ and/or YS were not computed they are empty here.

If additional data is needed inside MONFUN, it must be defined as

FUNCTION NEW_MONDATA = MONFUN(CALL, T, Y, YQ, YS, MONDATA)

If the local modifications to the user data structure need to be saved (e.g. for future calls to MONFUN), then MONFUN must set
NEW_MONDATA. Otherwise, it should set NEW_MONDATA=[]

(do not set NEW_MONDATA = DATA as it would lead to unnecessary copying).

A sample monitoring function, CVodeMonitor, is provided with CVODES.

See also CVodeSetOptions, CVodeMonitor

NOTES:

MONFUN is specified through the MonitorFn property in CVodeSetOptions. If this property is not set, or if it is empty, MONFUN is not used. MONDATA is specified through the MonitorData property in CVodeSetOptions.

If MONFUN is used on the backward integration phase, YS will always be empty.

See CVodeMonitor for an example of using MONDATA to write a single monitoring function that works both for the forward and backward integration phases.

CVQuadRhsFn

Purpose

CVQuadRhsFn - type for user provided quadrature RHS function.

Synopsis

This is a script file.

DESCRIPTION

CVQuadRhsFn - type for user provided quadrature RHS function.

IVP Problem

The function ODEQFUN must be defined as FUNCTION [YQD, FLAG] = ODEQFUN(T,Y)

and must return a vector YQD corresponding to fQ(t,y), the integrand for the integral to be evaluated.

If a user data structure DATA was specified in ${\tt CVodeMalloc}$, then ${\tt ODEQFUN}$ must be defined as

FUNCTION [YQD, FLAG, NEW_DATA] = ODEQFUN(T,Y,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector YQD, the ODEQFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function ODEQFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function ODEQFUNB must be defined either as FUNCTION [YQBD, FLAG] = ODEQFUNB(T,Y,YB) or as

FUNCTION [YQBD, FLAG, NEW_DATA] = ODEQFUNB(T,Y,YB,DATA) depending on whether a user data structure DATA was specified in CVodeMalloc. In either case, it must return the vector YQBD corresponding to fQB(t,y,yB), the integrand for the integral to be evaluated on the backward phase.

The function ODEQFUNB must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error

occurred.

See also CVodeSetOptions

NOTE: ODEQFUN and ODEQFUNB are specified through the property QuadRhsFn to CVodeSetOptions and are used only if the property Quadratures was set to 'on'.

CVRhsFn

PURPOSE

CVRhsFn - type for user provided RHS type

Synopsis

This is a script file.

DESCRIPTION

CVRhsFn - type for user provided RHS type

IVP Problem

The function ODEFUN must be defined as FUNCTION [YD, FLAG] = ODEFUN(T,Y)

ODEFUN must be defined as

and must return a vector YD corresponding to f(t,y). If a user data structure DATA was specified in CVodeMalloc, then

FUNCTION [YD, FLAG, NEW_DATA] = ODEFUN(T,Y,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector YD, the ODEFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function ODEFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function ODEFUNB must be defined either as FUNCTION [YBD, FLAG] = ODEFUNB(T,Y,YB)

or as

FUNCTION [YBD, FLAG, NEW_DATA] = ODEFUNB(T,Y,YB,DATA) depending on whether a user data structure DATA was specified in CVodeMalloc. In either case, it must return the vector YBD corresponding to fB(t,y,yB).

The function ODEFUNB must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also CVodeMalloc, CVodeMallocB

NOTE: ODEFUN and ODEFUNB are specified through the CVodeMalloc and CVodeMallocB functions, respectively.

CVRootFn

PURPOSE

CVRootFn - type for user provided root-finding function.

Synopsis

This is a script file.

Description

CVRootFn - type for user provided root-finding function.

The function ROOTFUN must be defined as FUNCTION [G, FLAG] = ROOTFUN(T,Y)

and must return a vector G corresponding to g(t,y).

If a user data structure DATA was specified in CVodeMalloc, then ROOTFUN must be defined as

FUNCTION [G, FLAG, NEW_DATA] = ROOTFUN(T,Y,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector G, the ROOTFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function ROOTFUN must set FLAG=0 if successful, or FLAG~=0 if a failure occurred.

See also CVodeSetOptions

NOTE: ROOTFUN is specified through the RootsFn property in CVodeSetOptions and is used only if the property NumRoots is a positive integer.

CVSensRhsFn

PURPOSE

CVSensRhsFn - type for user provided sensitivity RHS function.

Synopsis

This is a script file.

Description

CVSensRhsFn - type for user provided sensitivity RHS function.

The function ODESFUN must be defined as

FUNCTION [YSD, FLAG] = ODESFUN(T,Y,YD,YS)

and must return a matrix YSD corresponding to fS(t,y,yS).

If a user data structure DATA was specified in CVodeMalloc, then

ODESFUN must be defined as

FUNCTION [YSD, FLAG, NEW_DATA] = ODESFUN(T,Y,YD,YS,DATA) If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the matrix YSD, the ODESFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function ODESFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also CVodeSetFSAOptions

NOTE: ODESFUN is specified through the property FSARhsFn to CVodeSetFSAOptions.

CVJacTimesVecFn

Purpose

CVJacTimesVecFn - type for user provided Jacobian times vector function.

Synopsis

This is a script file.

DESCRIPTION

CVJacTimesVecFn - type for user provided Jacobian times vector function.

IVP Problem

The function JTVFUN must be defined as

FUNCTION [JV, FLAG] = JTVFUN(T,Y,FY,V)

and must return a vector JV corresponding to the product of the Jacobian of f(t,y) with the vector v.

The input argument FY contains the current value of f(t,y). If a user data structure DATA was specified in CVodeMalloc, then JTVFUN must be defined as

FUNCTION [JV, FLAG, NEW_DATA] = JTVFUN(T,Y,FY,V,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector JV, the JTVFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function JTVFUN must set FLAG=0 if successful, or FLAG~=0 if

a failure occurred.

Adjoint Problem

The function JTVFUNB must be defined either as FUNCTION [JVB, FLAG] = JTVFUNB(T,Y,YB,FYB,VB) or as

FUNCTION [JVB, FLAG, NEW_DATA] = JTVFUNB(T,Y,YB,FYB,VB,DATA) depending on whether a user data structure DATA was specified in CVodeMalloc. In either case, it must return the vector JVB, the product of the Jacobian of fB(t,y,yB) with respect to yB and a vector vB. The input argument FYB contains the current value of f(t,y,yB).

The function JTVFUNB must set FLAG=0 if successful, or FLAG~=0 if a failure occurred.

See also CVodeSetOptions

NOTE: JTVFUN and JTVFUNB are specified through the property JacobianFn to CVodeSetOptions and are used only if the property LinearSolver was set to 'GMRES', 'BiCGStab', or 'TFQMR'.

CVPrecSetupFn

PURPOSE

CVPrecSetupFn - type for user provided preconditioner setup function.

Synopsis

This is a script file.

DESCRIPTION

CVPrecSetupFn - type for user provided preconditioner setup function.

The user-supplied preconditioner setup function PSETFUN and the user-supplied preconditioner solve function PSOLFUN together must define left and right preconditoner matrices P1 and P2 (either of which may be trivial), such that the product P1*P2 is an approximation to the Newton matrix M = I - gamma*J. Here J is the system Jacobian J = df/dy, and gamma is a scalar proportional to the integration step size h. The solution of systems P z = r, with P = P1 or P2, is to be carried out by the PrecSolve function, and PSETFUN is to do any necessary setup operations.

The user-supplied preconditioner setup function PSETFUN is to evaluate and preprocess any Jacobian-related data needed by the preconditioner solve function PSOLFUN. This might include forming a crude approximate Jacobian, and performing an LU factorization on the resulting approximation to M. This function will not be called in advance of every call to PSOLFUN, but instead will be called

only as often as necessary to achieve convergence within the Newton iteration. If the PSOLFUN function needs no preparation, the PSETFUN function need not be provided.

For greater efficiency, the PSETFUN function may save Jacobian-related data and reuse it, rather than generating it from scratch. In this case, it should use the input flag JOK to decide whether to recompute the data, and set the output flag JCUR accordingly.

Each call to the PSETFUN function is preceded by a call to ODEFUN with the same (t,y) arguments. Thus the PSETFUN function can use any auxiliary data that is computed and saved by the ODEFUN function and made accessible to PSETFUN.

IVP Problem

The function PSETFUN must be defined as

FUNCTION [JCUR, FLAG] = PSETFUN(T,Y,FY,JOK,GAMMA)

and must return a logical flag JCUR (true if Jacobian information
was recomputed and false if saved data was reused). If PSETFUN
was successful, it must return FLAG=0. For a recoverable error (in
which case the setup will be retried) it must set FLAG to a positive
integer value. If an unrecoverable error occurs, it must set FLAG
to a negative value, in which case the integration will be halted.
The input argument FY contains the current value of f(t,y).
If the input logical flag JOK is false, it means that
Jacobian-related data must be recomputed from scratch. If it is true,
it means that Jacobian data, if saved from the previous PSETFUN call
can be reused (with the current value of GAMMA).

If a user data structure DATA was specified in CVodeMalloc, then PSETFUN must be defined as

FUNCTION [JCUR, FLAG, NEW_DATA] = PSETFUN(T,Y,FY,JOK,GAMMA,DATA) If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the flags JCUR and FLAG, the PSETFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

Adjoint Problem

The function PSETFUNB must be defined either as
FUNCTION [JCURB, FLAG] = PSETFUNB(T,Y,YB,FYB,JOK,GAMMAB)
or as

FUNCTION [JCURB, FLAG, NEW_DATA] = PSETFUNB(T,Y,YB,FYB,JOK,GAMMAB,DATA) depending on whether a user data structure DATA was specified in CVodeMalloc. In either case, it must return the flags JCURB and FLAG.

See also CVPrecSolveFn, CVodeSetOptions

NOTE: PSETFUN and PSETFUNB are specified through the property PrecSetupFn to CVodeSetOptions and are used only if the property LinearSolver was set to 'GMRES', 'BiCGStab', or 'TFQMR' and if the

CVPrecSolveFn

PURPOSE

CVPrecSolveFn - type for user provided preconditioner solve function.

Synopsis

This is a script file.

DESCRIPTION

CVPrecSolveFn - type for user provided preconditioner solve function.

The user-supplied preconditioner solve function PSOLFN is to solve a linear system P z=r in which the matrix P is one of the preconditioner matrices P1 or P2, depending on the type of preconditioning chosen.

IVP Problem

The function PSOLFUN must be defined as FUNCTION [Z, FLAG] = PSOLFUN(T,Y,FY,R)

and must return a vector Z containing the solution of Pz=r. If PSOLFUN was successful, it must return FLAG=0. For a recoverable error (in which case the step will be retried) it must set FLAG to a positive value. If an unrecoverable error occurs, it must set FLAG to a negative value, in which case the integration will be halted. The input argument FY contains the current value of f(t,y).

If a user data structure DATA was specified in ${\tt CVodeMalloc}$, then ${\tt PSOLFUN}$ must be defined as

FUNCTION [Z, FLAG, NEW_DATA] = PSOLFUN(T,Y,FY,R,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector Z and the flag FLAG, the PSOLFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

Adjoint Problem

The function PSOLFUNB must be defined either as FUNCTION [ZB, FLAG] = PSOLFUNB(T,Y,YB,FYB,RB)

or as

FUNCTION [ZB, FLAG, NEW_DATA] = PSOLFUNB(T,Y,YB,FYB,RB,DATA) depending on whether a user data structure DATA was specified in CVodeMalloc. In either case, it must return the vector ZB and the flag FLAG.

See also CVPrecSetupFn, CVodeSetOptions

NOTE: PSOLFUN and PSOLFUNB are specified through the property

PrecSolveFn to CVodeSetOptions and are used only if the property LinearSolver was set to 'GMRES', 'BiCGStab', or 'TFQMR' and if the property PrecType is not 'None'.

3 MATLAB Interface to IDAS

The MATLAB interface to IDAS provides access to all functionality of the IDAS solver, including DAE simulation and sensitivity analysis (both forward and adjoint).

The interface consists of 9 user-callable functions. The user must provide several required and optional user-supplied functions which define the problem to be solved. The user-callable functions and the types of user-supplied functions are listed in Table 2 and fully documented later in this section. For more in depth details, consult also the IDAS user guide [4].

To illustrate the use of the IDAS MATLAB interface, several example problems are provided with SUNDIALSTB, both for serial and parallel computations. Most of them are MATLAB translations of example problems provided with IDAS.

Table 2: IDAS MATLAB interface functions

Functions	IDASetOptions IDAMalloc IDASolve IDAGetStats IDAFree IDAMonitor	creates an options structure for IDAS. allocates and initializes memory for IDAS. integrates the ODE. returns statistics for the IDAS solver. deallocates memory for the IDAS solver. sample monitoring function.
Function types	IDAResFn IDARootFn IDADenseJacFn IDABandJacFn IDAJacTimesVecFn IDAPrecSetupFn IDAPrecSolveFn IDAGlocalFn IDAGcommFn IDAMonitorFn	residual function root-finding function dense Jacobian function banded Jacobian function Jacobian times vector function preconditioner setup function preconditioner solve function residual approximation function (BBDPre) communication function (BBDPre) monitoring function

3.1 Interface functions

IDASetOptions

```
PURPOSE
IDASetOptions creates an options structure for IDAS.
Synopsis
function options = IDASetOptions(varargin)
DESCRIPTION
IDASetOptions creates an options structure for IDAS.
   Usage: OPTIONS = IDASetOptions('NAME1', VALUE1, 'NAME2', VALUE2,...)
          OPTIONS = IDASetOptions(OLDOPTIONS,'NAME1', VALUE1,...)
          OPTIONS = IDASetOptions(OLDOPTIONS, NEWOPTIONS)
   OPTIONS = IDASetOptions('NAME1', VALUE1, 'NAME2', VALUE2,...) creates
   a IDAS options structure OPTIONS in which the named properties have
  the specified values. Any unspecified properties have default values.
   It is sufficient to type only the leading characters that uniquely
   identify the property. Case is ignored for property names.
  OPTIONS = IDASetOptions(OLDOPTIONS,'NAME1',VALUE1,...) alters an
   existing options structure OLDOPTIONS.
   OPTIONS = IDASetOptions(OLDOPTIONS, NEWOPTIONS) combines an existing
   options structure OLDOPTIONS with a new options structure NEWOPTIONS.
   Any new properties overwrite corresponding old properties.
   IDASetOptions with no input arguments displays all property names
   and their possible values.
IDASetOptions properties
(See also the IDAS User Guide)
RelTol - Relative tolerance [ positive scalar | 1e-4 ]
  RelTol defaults to 1e-4 and is applied to all components of the solution
   vector. See AbsTol.
AbsTol - Absolute tolerance [ positive scalar or vector | 1e-6 ]
  The relative and absolute tolerances define a vector of error weights
  with components
     ewt(i) = 1/(RelTol*|y(i)| + AbsTol)
                                             if AbsTol is a scalar
     ewt(i) = 1/(RelTol*|y(i)| + AbsTol(i)) if AbsTol is a vector
  This vector is used in all error and convergence tests, which
  use a weighted RMS norm on all error-like vectors v:
      \label{eq:wrmsnorm} \mbox{WRMSnorm(v) = sqrt( (1/N) sum(i=1..N) (v(i)*ewt(i))^2),} 
   where N is the problem dimension.
MaxNumSteps - Maximum number of steps [positive integer | 500]
   IDASolve will return with an error after taking MaxNumSteps internal steps
```

```
in its attempt to reach the next output time.
InitialStep - Suggested initial stepsize [ positive scalar ]
  By default, IDASolve estimates an initial stepsize hO at the initial time
  t0 as the solution of
    WRMSnorm(h0^2 ydd / 2) = 1
   where ydd is an estimated second derivative of y(t0).
MaxStep - Maximum stepsize [ positive scalar | inf ]
  Defines an upper bound on the integration step size.
MaxOrder - Maximum method order [ 1-5 for BDF | 5 ]
   Defines an upper bound on the linear multistep method order.
StopTime - Stopping time [ scalar ]
  Defines a value for the independent variable past which the solution
   is not to proceed.
RootsFn - Rootfinding function [ function ]
   To detect events (roots of functions), set this property to the event
   function. See IDARootFn.
NumRoots - Number of root functions [ integer | 0 ]
   Set NumRoots to the number of functions for which roots are monitored.
   If NumRoots is 0, rootfinding is disabled.
SuppressAlgVars - Suppres algebraic vars. from error test [ on | off ]
VariableTypes - Alg./diff. variables [ vector ]
ConstraintTypes - Simple bound constraints [ vector ]
LinearSolver - Linear solver type [Dense|Band|GMRES|BiCGStab|TFQMR]
   Specifies the type of linear solver to be used for the Newton nonlinear
   solver. Valid choices are: Dense (direct, dense Jacobian), Band (direct,
   banded Jacobian), GMRES (iterative, scaled preconditioned GMRES),
  BiCGStab (iterative, scaled preconditioned stabilized BiCG), TFQMR
   (iterative, scaled transpose-free QMR).
   The GMRES, BiCGStab, and TFQMR are matrix-free linear solvers.
JacobianFn - Jacobian function [ function ]
   This propeerty is overloaded. Set this value to a function that returns
   Jacobian information consistent with the linear solver used (see Linsolver).
   If not specified, IDAS uses difference quotient approximations.
  For the Dense linear solver, JacobianFn must be of type IDADenseJacFn and
  must return a dense Jacobian matrix. For the Band linear solver, JacobianFn
  must be of type IDABandJacFn and must return a banded Jacobian matrix.
  For the iterative linear solvers, GMRES, BiCGStab, and TFQMR, JacobianFn must
   be of type IDAJacTimesVecFn and must return a Jacobian-vector product.
KrylovMaxDim - Maximum number of Krylov subspace vectors [ integer | 5 ]
   Specifies the maximum number of vectors in the Krylov subspace. This property
   is used only if an iterative linear solver, GMRES, BiCGStab, or TFQMR is used
   (see LinSolver).
GramSchmidtType - Gram-Schmidt orthogonalization [ Classical | Modified ]
   Specifies the type of Gram-Schmidt orthogonalization (classical or modified).
   This property is used only if the GMRES linear solver is used (see LinSolver).
PrecModule - Preconditioner module [ BBDPre | UserDefined ]
   If PrecModule = 'UserDefined', then the user must provide at least a
  preconditioner solve function (see PrecSolveFn)
   IDAS provides one general-purpose preconditioner module, BBDPre, which can
  be only used with parallel vectors. It provide a preconditioner matrix that
   is block-diagonal with banded blocks. The blocking corresponds to the
   distribution of the dependent variable vector y among the processors.
```

Each preconditioner block is generated from the Jacobian of the local part (on the current processor) of a given function g(t,y,yp) approximating f(t,y,yp) (see GlocalFn). The blocks are generated by a difference quotient scheme on each processor independently. This scheme utilizes an assumed banded structure with given half-bandwidths, mldq and mudq (specified through LowerBwidthDQ and UpperBwidthDQ, respectively). However, the banded Jacobian block kept by the scheme has half-bandwiths ml and mu (specified through LowerBwidth and UpperBwidth), which may be smaller.

PrecSetupFn - Preconditioner setup function [function]

If PrecType is not 'None', PrecSetupFn specifies an optional function which, together with PrecSolve, defines the preconditioner matrix, which must be an approximation to the Newton matrix. PrecSetupFn must be of type IDAPrecSetupFn.

PrecSolveFn - Preconditioner solve function [function]

If PrecType is not 'None', PrecSolveFn specifies a required function which must solve a linear system Pz = r, for given r. PrecSolveFn must be of type IDAPrecSolveFn.

GlocalFn - Local residual approximation function for BBDPre [function] If PrecModule is BBDPre, GlocalFn specifies a required function that evaluates a local approximation to the DAE residual. GlocalFn must be of type IDAGlocFn.

GcommFn - Inter-process communication function for BBDPre [function]

If PrecModule is BBDPre, GcommFn specifies an optional function
to perform any inter-process communication required for the evaluation of
GlocalFn. GcommFn must be of type IDAGcommFn.

LowerBwidth - Jacobian/preconditioner lower bandwidth [integer | 0]

This property is overloaded. If the Band linear solver is used (see LinSolver), it specifies the lower half-bandwidth of the band Jacobian approximation.

If one of the three iterative linear solvers, GMRES, BiCGStab, or TFQMR is used (see LinSolver) and if the BBDPre preconditioner module in IDAS is used (see PrecModule), it specifies the lower half-bandwidth of the retained banded approximation of the local Jacobian block.

LowerBwidth defaults to 0 (no sub-diagonals).

UpperBwidth - Jacobian/preconditioner upper bandwidth [integer | 0]

This property is overloaded. If the Band linear solver is used (see LinSolver), it specifies the upper half-bandwidth of the band Jacobian approximation. If one of the three iterative linear solvers, GMRES, BiCGStab, or TFQMR is used (see LinSolver) and if the BBDPre preconditioner module in IDAS is used (see PrecModule), it specifies the upper half-bandwidth of the retained banded approximation of the local Jacobian block.

UpperBwidth defaults to 0 (no super-diagonals).

LowerBwidthDQ - BBDPre preconditioner DQ lower bandwidth [integer | 0] Specifies the lower half-bandwidth used in the difference-quotient Jacobian approximation for the BBDPre preconditioner (see PrecModule).

UpperBwidthDQ - BBDPre preconditioner DQ upper bandwidth [integer | 0] Specifies the upper half-bandwidth used in the difference-quotient Jacobian approximation for the BBDPre preconditioner (see PrecModule).

Quadratures - Quadrature integration [on | off]
 Enables or disables quadrature integration.

QuadRhsFn - Quadrature residual function [function]
 Specifies the user-supplied function to evaluate the integrand for quadrature computations. See IDAQuadRhsfn.

QuadInitCond - Initial conditions for quadrature variables [vector]
 Specifies the initial conditions for quadrature variables.

```
QuadErrControl - Error control strategy for quadrature variables [ on | off ] Specifies whether quadrature variables are included in the error test.
```

QuadRelTol - Relative tolerance for quadrature variables [scalar 1e-4]

Specifies the relative tolerance for quadrature variables. This parameter is used only if QuadErrCon=on.

QuadAbsTol - Absolute tolerance for quadrature variables [scalar or vector 1e-6] Specifies the absolute tolerance for quadrature variables. This parameter is used only if QuadErrCon=on.

ASANumDataPoints - Number of data points for ASA [integer | 100] Specifies the (maximum) number of integration steps between two consecutive check points.

ASAInterpType - Type of interpolation [Polynomial | Hermite]
Specifies the type of interpolation used for estimating the forward solution during the backward integration phase. At this time, the only option is 'Hermite', specifying cubic Hermite interpolation.

MonitorFn - User-provied monitoring function [function]
Specifies a function that is called after each successful integration step.
This function must have type IDAMonitorFn. A simple monitoring function,
IDAMonitor is provided with IDAS.

MonitorData - User-provied data for the monitoring function [struct] Specifies a data structure that is passed to the Monitor function every time it is called.

See also

IDARootFn, IDAQuadRhsFn
IDADenseJacFn, IDABandJacFn, IDAJacTimesVecFn
IDAPrecSetupFn, IDAPrecSolveFn
IDAGlocalFn, IDAGcommFn
IDAMonitorFn

IDAMalloc

Purpose

IDAMalloc allocates and initializes memory for IDAS.

Synopsis

function [] = IDAMalloc(fct,t0,yy0,yp0,varargin)

DESCRIPTION

IDAMalloc allocates and initializes memory for IDAS.

```
Usage: IDAMalloc ( DAEFUN, TO, YYO, YPO [, OPTIONS [, DATA] ] )
```

DAEFUN is a function defining the DAE residual: f(t,yy,yp).

This function must return a vector containing the current

value of the residual.

TO is the initial value of t.

YYO is the initial condition vector y(t0).

YPO is the initial condition vector y'(t0).

OPTIONS is an (optional) set of integration options, created with the IDASetOptions function.

DATA is (optional) problem data passed unmodified to all

user-provided functions when they are called. For example,

YD = DAEFUN(T, YY, YP, DATA).

See also: IDARhsFn

IDASolve

Purpose

IDASolve integrates the DAE.

Synopsis

function [status, t, yy, yp, varargout] = IDASolve(tout,itask)

DESCRIPTION

IDASolve integrates the DAE.

```
Usage: [STATUS, T, YY, YP] = IDASolve (TOUT, ITASK)

[STATUS, T, YY, YP, YQ] = IDASolve (TOUT, ITASK)

[STATUS, T, YY, YP, YYS, YPS] = IDASolve (TOUT, ITASK)

[STATUS, T, YY, YP, YQ, YYS, YPS] = IDASolve (TOUT, ITASK)
```

If ITASK is 'Normal', then the solver integrates from its current internal T value to a point at or beyond TOUT, then interpolates to T = TOUT and returns YY(TOUT) and YP(TOUT). If ITASK is 'OneStep', then the solver takes one internal time step and returns in YY and YP the solution at the new internal time. In this case, TOUT is used only during the first call to IDASolve to determine the direction of integration and the rough scale of the problem. In either case, the time reached by the solver is returned in T. The 'NormalTstop' and 'OneStepTstop' modes are similar to 'Normal' and 'OneStep', respectively, except that the integration never proceeds past the value tstop.

If quadratures were computed (see IDASetOptions), IDASolve will return their values at T in the vector YQ.

If sensitivity calculations were enabled (see IDASetOptions), IDASolve will return their values at T in the matrix YS.

On return, STATUS is one of the following:

- 0: IDASolve succeeded and no roots were found.
- 1: IDASolve succeded and returned at tstop.
- 2: IDASolve succeeded, and found one or more roots.
- -1: Illegal attempt to call before IDAMalloc
- -2: One of the inputs to IDASolve is illegal. This includes the situation when a component of the error weight vectors becomes < 0 during internal time-stepping.
- -4: The solver took mxstep internal steps but could not reach TOUT. The default value for mxstep is 500.

- -5: The solver could not satisfy the accuracy demanded by the user for some internal step.
- -6: Error test failures occurred too many times (MXNEF = 7) during one internal time step
 - or occurred with |h| = hmin.
- -7: Convergence test failures occurred too many times (MXNCF = 10) during one internal time step or occurred with |h| = hmin.
- -9: The linear solver's setup routine failed in an unrecoverable manner.
- -10: The linear solver's solve routine failed in an unrecoverable manner.

See also IDASetOptions, IDAGetStats

IDAGetStats

Purpose

IDAGetStats returns run statistics for the IDAS solver.

Synopsis

function si = IDAGetStats()

DESCRIPTION

IDAGetStats returns run statistics for the IDAS solver.

Usage: STATS = IDAGetStats

Fields in the structure STATS

```
o nst - number of integration steps
```

o nre $\,\,$ - number of residual function evaluations

o nsetups - number of linear solver setup calls

o netf - number of error test failures

o nni - number of nonlinear solver iterations o ncfn - number of convergence test failures

o qlast - last method order used o qcur - current method order

o hOused - actual initial step size used

o hlast - last step size used o hcur - current step size

o tcur - current time reached by the integrator

o RootInfo - strucutre with rootfinding information

o QuadInfo - structure with quadrature integration statistics

o LSInfo - structure with linear solver statistics

o FSAInfo - structure with forward sensitivity solver statistics

If rootfinding was requested, the structure RootInfo has the following fields

```
o nge - number of calls to the rootfinding function
```

o roots - array of integers (a value of 1 in the i-th component means that the i-th rootfinding function has a root (upon a return with status=2 from IDASolve).

```
If quadratures were present, the structure QuadInfo has the following fields
o nfQe - number of quadrature integrand function evaluations
o netfQ - number of error test failures for quadrature variables
The structure LSinfo has different fields, depending on the linear solver used.
 Fields in LSinfo for the 'Dense' linear solver
o name - 'Dense'
o njeD - number of Jacobian evaluations
o nreD - number of residual function evaluations for difference-quotient
         Jacobian approximation
 Fields in LSinfo for the 'Band' linear solver
o name - 'Band'
o njeB - number of Jacobian evaluations
o nreB - number of residual function evaluations for difference-quotient
         Jacobian approximation
 Fields in LSinfo for the 'GMRES' and 'BiCGStab' linear solvers
o name - 'GMRES' or 'BiCGStab'
      - number of linear solver iterations
o npe - number of preconditioner setups
o nps - number of preconditioner solve function calls
o ncfl - number of linear system convergence test failures
o njeSG - number of Jacobian-vector product evaluations
o nreSG - number of residual function evaluations for difference-quotient
          Jacobian-vector product approximation
If forward sensitivities were computed, the structure FSAInfo has the
following fields
o nrSe
           - number of sensitivity residual evaluations
           - number of residual evaluations for difference-quotient
o nreS
            sensitivity residual approximation
```

IDAFree

- number of nonlinear solver iterations for sensitivity variables

- number of convergence test failures due to sensitivity variables

o nsetupsS - number of linear solver setups triggered by sensitivity variables - number of error test failures for sensitivity variables

PURPOSE

o netfS

o nniS

o ncfnS

IDAFree deallocates memory for the IDAS solver.

Synopsis

function [] = IDAFree()

Description

IDAFree deallocates memory for the IDAS solver.

Usage: IDAFree

IDAMonitor

Purpose

IDAMonitor is the default IDAS monitoring function.

Synopsis

function [new_data] = IDAMonitor(call, T, YY, YP, YQ, YYS, YPS, data)

DESCRIPTION

IDAMonitor is the default IDAS monitoring function.

To use it, set the Monitor property in IDASetOptions to 'IDAMonitor' or to @IDAMonitor and 'MonitorData' to mondata (defined as a structure).

With default settings, this function plots the evolution of the step size, method order, and various counters.

Various properties can be changed from their default values by passing to IDASetOptions, through the property 'MonitorData', a structure MONDATA with any of the following fields. If a field is not defined, the corresponding default value is used.

Fields in MONDATA structure:

- o stats [true | false]
 - If true, report the evolution of the step size and method order.
- o cntr [true | false]
 - If true, report the evolution of the following counters:
 - nst, nre, nni, netf, ncfn (see IDAGetStats)
- o mode ['graphical' | 'text' | 'both']
 - In graphical mode, plot the evolutions of the above quantities.
 - In text mode, print a table.
- o xaxis ['linear' | 'log']
 - Type of the time axis for the stepsize, order, and counter plots (graphical mode only).
- o sol [true | false]
 - If true, plot solution components.
- o sensi [true | false]
 - If true and if FSA is enabled, plot sensitivity components.
- o select [array of integers]
 - To plot only particular solution components, specify their indeces in the field select. If not defined, but sol=true, all components are plotted.
- o updt [integer | 50]
 - Update frequency. Data is posted in blocks of dimension n.
- o skip [integer | 0]
 - Number of integrations steps to skip in collecting data to post.
- o dir [1 | -1]

Specifies forward or backward integration.

```
o post [ true | false ]

If false, disable all posting. This option is necessary to disable monitoring on some processors when running in parallel.
```

See also IDASetOptions, IDAMonitorFn

NOTES:

- 1. The argument mondata is REQUIRED. Even if only the default options are desired, set mondata=struct; and pass it to IDASetOptions.
- 2. The arguments YP, YQ, and YPS are currently ignored.

SOURCE CODE

```
function [new_data] = IDAMonitor(call, T, YY, YP, YQ, YYS, YPS, data)
50
  % Radu Serban < radu@llnl.gov>
51
  % Copyright (c) 2005, The Regents of the University of California.
52
  % $Revision: 1.1 $Date: 2006/07/17 16:49:50 $
53
5.5
   new_data = [];
56
57
   if call == 0
58
59
  % Initialize unspecified fields to default values.
60
     data = initialize_data(data);
61
62
  % Open figure windows
63
     if data.post
64
65
        if data.grph
66
          if data.stats | data.cntr
67
            data.hfg = figure;
68
          end
         Number of subplots in figure hfg
70
          if data.stats
71
            data.npg = data.npg + 2;
72
          end
73
          if data.cntr
74
            data.npg = data.npg + 1;
75
         end
76
       end
77
78
        if data.text
79
          if data.cntr | data.stats
80
            data.hft = figure;
81
         end
82
       end
83
        if data.sol | data.sensi
85
          data.hfs = figure;
86
       end
87
     end
89
90
```

```
% Initialize other private data
91
      data.i = 0;
92
      data.n = 1;
93
      data.t = zeros(1, data.updt);
      if data.stats
95
        data.h = zeros(1, data.updt);
        data.q = zeros(1, data.updt);
97
      end
98
      if data.cntr
99
        data.nst = zeros(1, data.updt);
100
        data.nre = zeros(1, data.updt);
101
        data.nni = zeros(1, data.updt);
102
        data.netf = zeros(1, data.updt);
        data.ncfn = zeros(1, data.updt);
104
      end
105
106
      data.first = true;
                                   % the next one will be the first call = 1
107
      data.initialized = false; % the graphical windows were not initalized
108
109
      new_data = data;
110
      return;
112
113
    else
114
115
   % If this is the first call = 0,
116
   % use YY and YYS for additional initializations
117
118
      if data.first
119
120
        if isempty (YYS)
121
          data.sensi = false;
122
        end
123
124
        if data.sol | data.sensi
125
           if isempty (data.select)
127
             data.N = length(YY);
129
             data.select = [1:data.N];
130
131
          else
132
133
             data.N = length (data.select);
134
135
          end
136
137
          if data.sol
138
             data.y = zeros (data.N, data.updt);
139
             data.nps = data.nps + 1;
140
          end
141
142
          if data.sensi
143
             data.Ns = size(YYS, 2);
144
```

```
data.ys = zeros(data.N, data.Ns, data.updt);
145
             data.nps = data.nps + data.Ns;
           end
147
        end
149
150
        data.first = false;
151
152
      end
153
154
   % Extract variables from data
155
156
      hfg = data.hfg;
157
            = data.hft;
      hft
158
      hfs
           = data.hfs;
           = data.npg;
160
      nps
           = data.nps;
            = data.i;
162
            = data.n;
163
            = data.t;
164
      Ν
            = data.N;
            = data.Ns;
      Ns
166
            = data.y;
167
            = data.ys;
      уs
168
            = data.h;
169
            = data.q;
170
           = data.nst;
171
      nre
           = data.nre;
172
      nni = data.nni;
173
      netf = data.netf;
174
      ncfn = data.ncfn;
175
176
    end
177
178
179
   % Load current statistics?
180
181
    if call == 1
182
183
      if i = 0
184
        i = i - 1;
185
        data.i = i;
186
        new_data = data;
187
        return;
188
      end
189
190
      if data.dir == 1
191
         si = IDAGetStats;
192
      else
193
         si = IDAGetStatsB;
194
      end
195
196
      t(n) = si.tcur;
197
198
```

```
if data.stats
199
        h(n) = si.hlast;
        q(n) = si.qlast;
201
203
      if data.cntr
204
         n st(n) = si.nst;
205
         nre(n) = si.nre;
206
        n \operatorname{ni}(n) = \operatorname{si.nni};
207
         netf(n) = si.netf;
208
         ncfn(n) = si.ncfn;
209
      end
210
211
      if data.sol
212
         for j = 1:N
213
           y(j,n) = YY(data.select(j));
214
        end
215
      end
216
217
      if data.sensi
218
         for k = 1:Ns
           for j = 1:N
220
             ys(j,k,n) = YYS(data.select(j),k);
221
           end
222
        end
223
      end
224
225
    end
226
227
   % Is it time to post?
228
229
    if data.post & (n == data.updt \mid call == 2)
230
231
      if call == 2
232
        n = n-1;
233
      end
235
      if "data.initialized
237
         if (data.stats | data.cntr) & data.grph
238
           graphical_init (n, hfg, npg, data.stats, data.cntr, data.dir, ...
239
                             t, h, q, nst, nre, nni, netf, ncfn, data.xaxis);
240
        end
241
242
         if (data.stats | data.cntr) & data.text
243
           text_init(n, hft, data.stats, data.cntr, ...
244
                       t, h, q, nst, nre, nni, netf, ncfn);
245
         end
246
247
         if data.sol | data.sensi
248
           sol_init(n, hfs, nps, data.sol, data.sensi, data.dir, data.xaxis, ...
249
                     N, Ns, t, y, ys);
250
251
         end
252
```

```
data.initialized = true;
253
254
      else
255
256
         if (data.stats | data.cntr) & data.grph
257
           graphical_update(n, hfg, npg, data.stats, data.cntr, ...
258
                              t, h, q, nst, nre, nni, netf, ncfn);
259
        end
260
261
        if (data.stats | data.cntr) & data.text
262
           text_update(n, hft, data.stats, data.cntr, ...
263
                        t, h, q, nst, nre, nni, netf, ncfn);
264
        end
265
266
        if data.sol
267
           sol_update(n, hfs, nps, data.sol, data.sensi, N, Ns, t, y, ys);
268
        end
269
270
      end
271
272
      if call == 2
274
         if (data.stats | data.cntr) & data.grph
275
           graphical_final(hfg, npg, data.cntr, data.stats);
276
        end
277
278
        if data.sol | data.sensi
279
           sol_final(hfs, nps, data.sol, data.sensi, N, Ns);
280
        end
281
282
        return;
283
284
      end
285
286
      n = 1;
287
    else
289
290
      n = n + 1;
291
292
    end
293
294
295
   % Save updated values in data
296
297
               = data.skip;
    data.i
298
    data.n
               = n;
299
    data.npg
              = npg;
300
    data.t
               = t;
301
    data.v
               = y;
302
    data.ys
               = ys;
303
    data.h
               = h;
304
    data.q
               = q;
   data.nst = nst;
306
```

```
data.nre = nre;
    data.nni = nni;
    data.netf = netf;
309
   data.ncfn = ncfn;
311
    new_data = data;
312
313
    return;
314
315
316
317
    function data = initialize_data(data)
318
    if ~ isfield (data, 'mode')
320
      data.mode = 'graphical';
321
322
   end
   if ~ isfield (data, 'updt')
323
      data.updt = 50;
324
    end
    if ~isfield(data, 'skip')
326
      data.skip = 0;
328
   if ~ isfield (data, 'stats')
329
      data.stats = true;
330
   end
331
   if ~ isfield (data, 'cntr')
332
      data.cntr = true;
333
   end
334
   if ~isfield(data,'sol')
335
      data.sol = false;
336
337
   if ~isfield (data, 'sensi')
338
      data.sensi = false;
339
340
    if ~isfield (data, 'select')
341
      data.select = [];
    end
343
   if ~ isfield (data, 'xaxis')
      data.xaxis = 'log';
345
346
   if ~ isfield (data, 'dir')
347
      data.dir = 1;
348
349
    if ~isfield(data, 'post')
350
      data.post = true;
351
   end
352
353
    data.grph = true;
354
    data.text = true;
355
   if strcmp (data.mode, 'graphical')
356
      data.text = false;
357
358
   if strcmp(data.mode, 'text')
      data.grph = false;
360
```

```
end
361
362
    if ~data.sol & ~data.sensi
363
      data.select = [];
364
365
366
   % Other initializations
367
    data.npg = 0;
368
    data.nps = 0;
369
    data.hfg = 0;
370
    data.hft = 0;
371
    data.hfs = 0;
372
    data.h = 0;
373
    data.q = 0;
374
    data.nst = 0;
375
    data.nre = 0;
376
    data.nni = 0;
377
    data.netf = 0;
378
    data.ncfn = 0;
    data.N = 0;
380
    data.Ns = 0;
381
    data.y = 0;
382
    data.ys = 0;
383
384
385
386
    function [] = graphical_init(n, hfg, npg, stats, cntr, dir, ...
387
                                      t\;,\;h\;,\;q\;,\;nst\;,\;nre\;,\;nni\;,\;netf\;,\;ncfn\;,\;xaxis\;)
388
389
    fig_name = 'IDAS_run_statistics';
390
391
   % If this is a parallel job, look for the MPI rank in the global
392
   % workspace and append it to the figure name
393
394
    global sundials_MPI_rank
395
396
    if ~isempty (sundials_MPI_rank)
397
      fig_name = sprintf('%s_(PE_%d)', fig_name, sundials_MPI_rank);
398
    end
399
400
    figure (hfg);
401
    set (hfg , 'Name' , fig_name );
402
    set(hfg, 'color',[1 1 1]);
403
    pl = 0;
404
405
   % Time label and figure title
406
407
    if dir==1
408
      tlab = '\rightarrow___t__\rightarrow';
409
410
      tlab = '\leftarrow___t_\leftarrow';
411
    end
412
413
   % Step size and order
```

```
415
    if stats
      pl = pl + 1;
      subplot (npg, 1, pl)
417
      semilogy(t(1:n),abs(h(1:n)),'-');
      if strcmp(xaxis, 'log')
419
         set(gca, 'XScale', 'log');
420
      end
421
      hold on;
422
      box on;
423
      grid on;
424
      xlabel(tlab);
425
      ylabel('|Step_size|');
426
427
      pl = pl + 1;
428
      subplot(npg,1,pl)
429
      plot(t(1:n), q(1:n), '-');
430
      if strcmp(xaxis, 'log')
431
         set (gca , 'XScale', 'log');
432
      end
433
      hold on;
434
      box on;
      grid on;
436
      xlabel(tlab);
437
      ylabel('Order');
438
    end
439
440
   % Counters
441
    if cntr
442
      pl = pl + 1;
443
      subplot(npg,1,pl)
444
      plot(t(1:n), nst(1:n), 'k-');
445
      hold on;
446
      plot(t(1:n), nre(1:n), 'b-');
447
      plot (t (1:n), nni (1:n), 'r-');
448
      plot(t(1:n), netf(1:n), 'g-');
449
      plot (t (1:n), ncfn (1:n), 'c-');
      if strcmp(xaxis, 'log')
451
         set(gca, 'XScale', 'log');
452
      end
453
      box on;
454
      grid on;
455
      xlabel(tlab);
456
      ylabel('Counters');
457
    end
458
459
    drawnow;
460
461
462
463
    function [] = graphical_update(n, hfg, npg, stats, cntr, ...
464
                                         t, h, q, nst, nre, nni, netf, ncfn)
465
466
    figure (hfg);
467
   pl = 0;
468
```

```
469
   % Step size and order
    if stats
471
      pl = pl + 1;
      subplot (npg, 1, pl)
473
      hc = get(gca, 'Children');
474
      xd = [get(hc, 'XData') t(1:n)];
475
      yd = [get(hc, 'YData') abs(h(1:n))];
476
      set (hc, 'XData', xd, 'YData', yd);
477
478
      pl = pl + 1;
479
      subplot (npg, 1, pl)
480
      hc = get(gca, 'Children');
xd = [get(hc, 'XData') t(1:n)];
482
      yd = [get(hc, 'YData') q(1:n)];
      set (hc, 'XData', xd, 'YData', yd);
484
    end
485
486
   % Counters
487
    if cntr
488
      pl = pl + 1;
      subplot (npg, 1, pl)
490
      hc = get(gca, 'Children');
491
      Attention: Children are loaded in reverse order!
492
      xd = [get(hc(1), 'XData') t(1:n)];
493
      yd = [get(hc(1), 'YData') ncfn(1:n)];
494
      set (hc(1), 'XData', xd, 'YData', yd);
495
      yd = [get(hc(2), 'YData') netf(1:n)];
496
      set(hc(2), 'XData', xd, 'YData', yd);
497
      yd = [get(hc(3), 'YData') nni(1:n)];
498
      set(hc(3), 'XData', xd, 'YData', yd);
499
      yd = [get(hc(4), 'YData') nre(1:n)];
500
      set(hc(4), 'XData', xd, 'YData', yd);
501
      yd = [get(hc(5), 'YData') nst(1:n)];
502
      set (hc(5), 'XData', xd, 'YData', yd);
503
    end
504
505
    drawnow;
506
507
508
509
    function [] = graphical_final(hfg,npg,stats,cntr)
510
511
    figure (hfg);
512
    pl = 0;
513
514
    if stats
515
      pl = pl + 1;
516
      subplot (npg, 1, pl)
517
      hc = get (gca, 'Children');
518
      xd = get(hc, 'XData');
519
      set (gca, 'XLim', sort ([xd(1) xd(end)]));
520
521
      pl = pl + 1;
522
```

```
subplot (npg, 1, pl)
523
      ylim = get(gca, 'YLim');
524
      ylim(1) = ylim(1) - 1;
525
      ylim(2) = ylim(2) + 1;
526
      set(gca, 'YLim', ylim);
527
      set (gca, 'XLim', sort ([xd(1) xd(end)]));
528
    end
529
530
   if cntr
531
      pl = pl + 1;
532
      subplot (npg, 1, pl)
533
      hc = get(gca, 'Children');
534
      xd = get(hc(1), 'XData');
535
      set (gca, 'XLim', sort ([xd(1) xd(end)]));
536
      legend('nst', 'nre', 'nni', 'netf', 'ncfn', 2);
538
539
540
541
    function [] = text_init(n, hft, stats, cntr, t, h, q, nst, nre, nni, netf, ncfn)
542
543
    fig_name = 'IDAS_run_statistics';
544
545
   % If this is a parallel job, look for the MPI rank in the global
546
   % workspace and append it to the figure name
547
548
    global sundials_MPI_rank
549
550
    if ~isempty (sundials_MPI_rank)
551
      fig_name = sprintf('%s_(PE_%d)', fig_name, sundials_MPI_rank);
552
   end
553
554
    figure (hft);
555
    set(hft, 'Name', fig_name);
    set(hft, 'color',[1 1 1]);
557
    set(hft, 'MenuBar', 'none');
558
    set(hft, 'Resize', 'off');
559
560
   % Create text box
561
562
    margins = [10 10 50 50]; % left, right, top, bottom
563
    pos=get(hft, 'position');
564
    tbpos = [margins(1) \ margins(4) \ pos(3) - margins(1) - margins(2) \dots
565
            pos(4) - margins(3) - margins(4);
566
    tbpos(tbpos<1)=1;
567
568
   htb=uicontrol(hft, 'style', 'listbox', 'position',tbpos, 'tag', 'textbox');
569
    set(htb, 'BackgroundColor',[1 1 1]);
570
    set(htb, 'SelectionHighlight', 'off');
571
    set (htb, 'FontName', 'courier');
572
   % Create table head
574
575
   [tpos = [tbpos(1) tbpos(2) + tbpos(4) + 10 tbpos(3) 20];
```

```
ht=uicontrol(hft, 'style', 'text', 'position', tpos, 'tag', 'text');
    set(ht, 'BackgroundColor',[1 1 1]);
    set(ht, 'HorizontalAlignment', 'left');
579
    set (ht, 'FontName', 'courier');
580
    newline = '___time____step____order__|__nst___nre___nni__netf__ncfn';
581
    set(ht, 'String', newline);
582
583
   % Create OK button
584
585
    bsize = [60, 28]:
586
    badjustpos = [0, 25];
587
    bpos = [pos(3)/2 - bsize(1)/2 + badjustpos(1) - bsize(2)/2 + badjustpos(2)...
588
           bsize(1) bsize(2)];
    bpos=round(bpos);
590
    bpos (bpos <1)=1;
591
    hb=uicontrol(hft, 'style', 'pushbutton', 'position', bpos,...
592
                    'string', 'Close', 'tag', 'okaybutton');
    set(hb, 'callback', 'close');
594
    % Save handles
596
597
    handles=guihandles(hft):
598
    guidata (hft, handles);
599
600
    for i = 1:n
601
      newline = '';
602
      if stats
603
         newline = sprintf('\%10.3e_{--}\%10.3e_{--}\%1d_{---})', t(i), h(i), q(i));
604
      end
605
      if cntr
606
         newline = sprintf('\%s \ \%5d \ \%5d \ \%5d \ \%5d \ \%5d \ \%...
607
                              newline, nst(i), nre(i), nni(i), netf(i), ncfn(i));
608
609
      string = get (handles.textbox, 'String');
610
      string \{end+1\} = newline;
611
      set (handles.textbox, 'String', string);
    end
613
614
    drawnow
615
616
617
618
    function [] = text_update(n, hft, stats, cntr, t, h, q, nst, nre, nni, netf, ncfn)
619
620
    figure (hft);
621
622
    handles=guidata(hft);
623
624
    for i = 1:n
625
       if stats
626
         newline = sprintf('\%10.3e_{--}\%10.3e_{---}\%1d_{---}|',t(i),h(i),q(i));
627
      end
628
      if cntr
629
         newline = sprintf('\%s - \%5d - \%5d - \%5d - \%5d - \%5d'),...
630
```

```
newline, nst(i), nre(i), nni(i), netf(i), ncfn(i));
631
      end
632
      string = get(handles.textbox, 'String');
633
      string { end+1}=newline;
634
      set (handles.textbox, 'String', string);
635
    end
636
637
    drawnow
638
639
640
641
    function [] = sol_init(n, hfs, nps, sol, sensi, dir, xaxis, N, Ns, t, y, ys)
642
    fig_name = 'IDAS_solution';
644
   % If this is a parallel job, look for the MPI rank in the global
646
   % workspace and append it to the figure name
647
648
    global sundials_MPI_rank
650
    if ~isempty (sundials_MPI_rank)
651
      fig_name = sprintf('%s_(PE_%d)', fig_name, sundials_MPI_rank);
652
    end
653
654
655
    figure (hfs);
656
    set(hfs, 'Name', fig_name);
657
    set(hfs, 'color', [1 1 1]);
658
659
   % Time label
660
661
    if dir==1
662
      tlab = '\rightarrow \_ \rightarrow ';
663
664
      tlab = '\leftarrow___t_\leftarrow';
665
    end
667
   % Get number of colors in colormap
    map = colormap:
669
    n \operatorname{cols} = \operatorname{size} (\operatorname{map}, 1);
670
671
   % Initialize current subplot counter
672
    pl = 0;
673
    if sol
675
676
      pl = pl + 1;
677
      subplot(nps,1,pl);
678
      hold on;
679
680
      for i = 1:N
681
        hp = plot(t(1:n), y(i, 1:n), '-');
682
         ic = 1+(i-1)*floor(ncols/N);
683
         set (hp, 'Color', map(ic,:));
684
```

```
685
       if strcmp(xaxis, 'log')
686
         set(gca, 'XScale', 'log');
687
688
       box on;
689
       grid on;
690
       xlabel(tlab);
691
       ylabel('y');
692
       title ('Solution');
693
694
    end
695
696
    if sensi
697
698
       for is = 1:Ns
699
700
         pl = pl + 1;
701
         subplot (nps , 1 , pl );
702
         hold on;
703
704
         ys\_crt = ys(:, is, 1:n);
705
         for i = 1:N
706
           hp = plot(t(1:n), ys_crt(i, 1:n), '-');
707
           ic = 1+(i-1)*floor(ncols/N);
708
           set(hp, 'Color', map(ic,:));
709
         end
710
         if strcmp(xaxis, 'log')
711
            set(gca, 'XScale', 'log');
7\,1\,2
         end
713
         box on;
714
         grid on;
715
         xlabel(tlab);
716
         str = sprintf('s_{\{0\}}', is); ylabel(str);
717
         str = sprintf('Sensitivity_%d', is); title(str);
718
719
      end
720
721
    end
722
723
724
    drawnow;
725
726
727
728
    function [] = sol_update(n, hfs, nps, sol, sensi, N, Ns, t, y, ys)
729
730
    figure (hfs);
731
732
    pl = 0;
733
734
    if sol
735
736
       pl = pl + 1;
737
       subplot (nps,1,pl);
738
```

```
739
      hc = get(gca, 'Children');
      xd = [get(hc(1), 'XData') t(1:n)];
741
    % Attention: Children are loaded in reverse order!
742
      for i = 1:N
743
        yd = [get(hc(i), 'YData') y(N-i+1,1:n)];
744
        set(hc(i), 'XData', xd, 'YData', yd);
745
      end
746
747
    end
748
749
    if sensi
750
      for is = 1:Ns
752
753
         pl = pl + 1;
754
         subplot (nps , 1 , pl );
755
756
         ys crt = ys(:, is,:);
757
758
        hc = get(gca, 'Children');
759
        xd = [get(hc(1), 'XData') t(1:n)];
760
        Attention: Children are loaded in reverse order!
761
         for i = 1:N
762
           yd = [get(hc(i), 'YData') ys\_crt(N-i+1,1:n)];
763
           set(hc(i), 'XData', xd, 'YData', yd);
764
        end
765
766
      end
767
    end
769
770
771
    drawnow;
772
773
774
775
776
    function [] = sol_final(hfs, nps, sol, sensi, N, Ns)
777
778
    figure (hfs);
779
780
    pl = 0;
7\,8\,1
782
    if sol
783
784
      pl = pl +1;
      subplot (nps,1,pl);
786
787
      hc = get(gca, 'Children');
788
      xd = get(hc(1), 'XData');
789
      set (gca, 'XLim', sort ([xd(1) xd(end)]));
790
791
      ylim = get (gca, 'YLim');
792
```

```
addon = 0.1 * abs(ylim(2) - ylim(1));
793
      y \lim (1) = y \lim (1) + sign(y \lim (1))*addon;
      y \lim (2) = y \lim (2) + sign(y \lim (2)) * addon;
795
      set (gca , 'YLim', ylim);
796
797
      for i = 1:N
798
         cstring\{i\} = sprintf('y_{-}\{\%d\}', i);
799
800
      legend(cstring);
801
802
    end
803
804
    if sensi
805
806
      for is = 1:Ns
807
808
         pl = pl + 1;
809
         subplot(nps,1,pl);
810
811
         hc = get (gca, 'Children');
812
         xd = get(hc(1), 'XData');
813
         set (gca, 'XLim', sort ([xd(1) xd(end)]));
814
815
         ylim = get(gca, 'YLim');
816
         addon = 0.1 * abs(ylim(2) - ylim(1));
817
         ylim(1) = ylim(1) + sign(ylim(1))*addon;
818
         ylim(2) = ylim(2) + sign(ylim(2))*addon;
819
         set (gca, 'YLim', ylim);
820
821
         for i = 1:N
822
           cstring\{i\} = sprintf('s\%d_{\{Md\}}', is, i);
823
824
         legend(cstring);
825
826
      end
827
    end
829
   drawnow
831
```

3.2 Function types

IDABandJacFn

PURPOSE

IDABandJacFn - type for user provided banded Jacobian function.

Synopsis

This is a script file.

DESCRIPTION

IDABandJacFn - type for user provided banded Jacobian function.

IVP Problem

The function BJACFUN must be defined as FUNCTION [J, FLAG] = BJACFUN(T, YY, YP, RR, CJ) and must return a matrix J corresponding to the banded Jacobian (df/dyy + cj*df/dyp).

The input argument RR contains the current value of f(t,yy,yp). If a user data structure DATA was specified in IDAMalloc, then BJACFUN must be defined as

FUNCTION [J, FLAG, NEW_DATA] = BJACFUN(T, YY, YP, RR, CJ, DATA) If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the matrix J, the BJACFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function BJACFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function BJACFUNB must be defined either as

FUNCTION [JB, FLAG] = BJACFUNB(T, YY, YP, YYB, YPB, RRB, CJB)
or as

FUNCTION [JB,FLAG,NEW_DATA] = BJACFUNB(T,YY,YP,YYB,YPB,RRB,CJB) depending on whether a user data structure DATA was specified in IDAMalloc. In either case, it must return the matrix JB, the Jacobian (dfB/dyyB + cjB*dfB/dypB)of fB(t,y,yB). The input argument RRB contains the current value of f(t,yy,yp,yyB,ypB).

The function BJACFUNB must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also IDASetOptions

See the IDAS user guide for more information on the structure of a banded Jacobian.

NOTE: BJACFUN and BJACFUNB are specified through the property JacobianFn to IDASetOptions and are used only if the property LinearSolver was set to 'Band'.

IDADenseJacFn

PURPOSE

IDADenseJacFn - type for user provided dense Jacobian function.

Synopsis

This is a script file.

DESCRIPTION

IDADenseJacFn - type for user provided dense Jacobian function.

IVP Problem

The function DJACFUN must be defined as FUNCTION [J, FLAG] = DJACFUN(T, YY, YP, RR, CJ) and must return a matrix J corresponding to the Jacobian (df/dyy + cj*df/dyp).

The input argument RR contains the current value of f(t,yy,yp). If a user data structure DATA was specified in IDAMalloc, then DJACFUN must be defined as

FUNCTION [J, FLAG, NEW_DATA] = DJACFUN(T, YY, YP, RR, CJ, DATA) If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the matrix J, the DJACFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function DJACFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function DJACFUNB must be defined either as
FUNCTION [JB, FLAG] = DJACFUNB(T, YY, YP, YYB, YPB, RRB, CJB)
or as

 $\label{eq:function} Function [JB,FLAG,NEW_DATA] = DJACFUNB(T,YY,YP,YYB,YPB,RRB,CJB,DATA) \\ depending on whether a user data structure DATA was specified in IDAMalloc. In either case, it must return the matrix JB, the Jacobian (dfB/dyyB + cjb*dfB/dypB). The input argument RRB contains the current value of f(t,yy,yp,yyB,ypB).$

The function DJACFUNB must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error

occurred.

See also IDASetOptions

NOTE: DJACFUN and DJACFUNB are specified through the property JacobianFn to IDASetOptions and are used only if the property LinearSolver was set to 'Dense'.

IDAGcommFn

Purpose

IDAGcommFn - type for user provided communication function (BBDPre).

SYNOPSIS

This is a script file.

DESCRIPTION

IDAGcommFn - type for user provided communication function (BBDPre).

IVP Problem

The function GCOMFUN must be defined as FUNCTION FLAG = GCOMFUN(T, YY, YP)

and can be used to perform all interprocess communication necessary to evaluate the approximate residual function for the BBDPre preconditioner module.

If a user data structure DATA was specified in IDAMalloc, then ${\tt GCOMFUN}$ must be defined as

FUNCTION [FLAG, NEW_DATA] = GCOMFUN(T, YY, YP, DATA) If the local modifications to the user data structure are needed in other user-provided functions then the GCOMFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function GCOMFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function GCOMFUNB must be defined either as FUNCTION FLAG = GCOMFUNB(T, YY, YP, YYB, YPB) or as

FUNCTION [FLAG, NEW_DATA] = GCOMFUNB(T, YY, YP, YYB, YPB, DATA) depending on whether a user data structure DATA was specified in IDAMalloc.

The function GCOMFUNB must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also IDAGlocalFn, IDASetOptions

NOTES .

GCOMFUN and GCOMFUNB are specified through the GcommFn property in IDASetOptions and are used only if the property PrecModule is set to 'BBDPre'.

Each call to GCOMFUN is preceded by a call to the residual function DAEFUN with the same arguments T, YY, and YP (and YYB and YPB in the case of GCOMFUNB). Thus GCOMFUN can omit any communication done by DAEFUN if relevant to the evaluation of G by GLOCFUN.

If all necessary communication was done by DAEFUN, GCOMFUN need

IDAGlocalFn

PURPOSE

IDAGlocalFn - type for user provided RES approximation function (BBDPre).

Synopsis

This is a script file.

not be provided.

DESCRIPTION

IDAGlocalFn - type for user provided RES approximation function (BBDPre).

IVP Problem

The function GLOCFUN must be defined as FUNCTION [GLOC, FLAG] = GLOCFUN(T,YY,YP)

and must return a vector GLOC corresponding to an approximation to f(t,yy,yp) which will be used in the BBDPRE preconditioner module. The case where G is mathematically identical to F is allowed.

If a user data structure DATA was specified in IDAMalloc, then ${\tt GLOCFUN}$ must be defined as

FUNCTION [GLOC, FLAG, NEW_DATA] = GLOCFUN(T,YY,YP,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector G, the GLOCFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function GLOCFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function GLOCFUNB must be defined either as FUNCTION [GLOCB, FLAG] = GLOCFUNB(T,YY,YP,YYB,YPB)

or as

FUNCTION [GLOCB, FLAG, NEW_DATA] = GLOCFUNB(T, YY, YP, YYB, YPB, DATA)

depending on whether a user data structure DATA was specified in IDAMalloc. In either case, it must return the vector GLOCB corresponding to an approximation to fB(t,yy,yp,yyB,ypB).

The function GLOCFUNB must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also IDAGcommFn, IDASetOptions

NOTE: GLOCFUN and GLOCFUNB are specified through the GlocalFn property in IDASetOptions and are used only if the property PrecModule is set to 'BBDPre'.

IDAMonitorFn

Purpose

IDAMonitorFn - type for user provided monitoring function.

Synopsis

This is a script file.

DESCRIPTION

IDAMonitorFn - type for user provided monitoring function.

The function MONFUN must be defined as FUNCTION [] = MONFUN(CALL, T, YY, YP, YQ, YYS, YPS)

It is called after every internal IDASolve step and can be used to monitor the progress of the solver. MONFUN is called with CALL=0 from IDAMalloc at which time it should initialize itself and it is called with CALL=2 from IDAFree. Otherwise, CALL=1.

It receives as arguments the current time T, solution vectors YY and YP, and, if they were computed, quadrature vector YQ, and forward sensitivity matrices YYS and YPS If YQ and/or YYS, YPS were not computed they are empty here.

If additional data is needed inside ${\tt MONFUN}$, it must be defined as

FUNCTION NEW_MONDATA = MONFUN(CALL, T, YY, YP, YQ, YYS, YPS, MONDATA)

If the local modifications to the user data structure need to be saved (e.g. for future calls to MONFUN), then MONFUN must set

NEW_MONDATA. Otherwise, it should set NEW_MONDATA=[]

(do not set NEW_MONDATA = DATA as it would lead to unnecessary copying).

A sample monitoring function, IDAMonitor, is provided with IDAS.

See also IDASetOptions, IDAMonitor

NOTES:

MONFUN is specified through the MonitorFn property in IDASetOptions. If this property is not set, or if it is empty, MONFUN is not used. MONDATA is specified through the MonitorData property in IDASetOptions.

If MONFUN is used on the backward integration phase, YYS and YPS will always be empty.

See IDAMonitor for an example of using MONDATA to write a single monitoring function that works both for the forward and backward integration phases.

IDAResFn

Purpose

IDAResFn - type for user provided RHS type

Synopsis

This is a script file.

DESCRIPTION

IDAResFn - type for user provided RHS type

IVP Problem

The function DAEFUN must be defined as

FUNCTION [R, FLAG] = DAEFUN(T, YY, YP)

and must return a vector R corresponding to f(t,yy,yp).

If a user data structure DATA was specified in IDAMalloc, then

DAEFUN must be defined as

FUNCTION [R, FLAG, NEW_DATA] = DAEFUN(T, YY, YP, DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector YD, the DAEFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function DAEFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

Adjoint Problem

The function DAEFUNB must be defined either as
FUNCTION [RB, FLAG] = DAEFUNB(T, YY, YP, YYB, YPB)
or as

FUNCTION [RB, FLAG, NEW_DATA] = DAEFUNB(T, YY, YP, YYB, YPB, DATA) depending on whether a user data structure DATA was specified in IDAMalloc. In either case, it must return the vector RB corresponding to fB(t,yy,yp,yyB,ypB).

The function DAEFUNB must set FLAG=0 if successful, FLAG<0 if an

unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also IDAMalloc, IDAMallocB

NOTE: DAEFUN and DAEFUNB are specified through the IDAMalloc and IDAMallocB functions, respectively.

IDARootFn

PURPOSE

IDARootFn - type for user provided root-finding function.

Synopsis

This is a script file.

DESCRIPTION

IDARootFn - type for user provided root-finding function.

The function ROOTFUN must be defined as
FUNCTION [G, FLAG] = ROOTFUN(T,YY,YP)
and must return a vector G corresponding to g(t,yy,yp).

If a user data structure DATA was specified in IDAMalloc, then
ROOTFUN must be defined as

FUNCTION [G, FLAG, NEW_DATA] = ROOTFUN(T,YY,YP,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector G, the ROOTFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function ROOTFUN must set FLAG=0 if successful, or FLAG~=0 if a failure occurred.

See also IDASetOptions

NOTE: ROOTFUN is specified through the RootsFn property in IDASetOptions and is used only if the property NumRoots is a positive integer.

IDAJacTimesVecFn

PURPOSE

IDAJacTimesVecFn - type for user provided Jacobian times vector function.

Synopsis

This is a script file.

DESCRIPTION

IDAJacTimesVecFn - type for user provided Jacobian times vector function.

IVP Problem

The function JTVFUN must be defined as

FUNCTION [JV, FLAG] = JTVFUN(T,YY,YP,RR,V,CJ)

and must return a vector JV corresponding to the product of the

Jacobian (df/dyy + cj * df/dyp) with the vector v.

The input argument RR contains the current value of f(t,yy,yp).

If a user data structure DATA was specified in IDAMalloc, then

JTVFUN must be defined as

FUNCTION [JV, FLAG, NEW_DATA] = JTVFUN(T,YY,YP,RR,V,CJ,DATA) If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector JV, the JTVFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function JTVFUN must set FLAG=0 if successful, or $FLAG^*=0$ if a failure occurred.

Adjoint Problem

The function JTVFUNB must be defined either as

FUNCTION [JVB,FLAG] = JTVFUNB(T,YY,YP,YYB,YPB,RRB,VB,CJB)

or as

FUNCTION [JVB,FLAG,NEW_DATA] = JTVFUNB(T,YY,YP,YYB,YPB,RRB,VB,CJB,DATA) depending on whether a user data structure DATA was specified in IDAMalloc. In either case, it must return the vector JVB, the product of the Jacobian (dfB/dyyB + cj * dfB/dypB) and a vector vB. The input argument RRB contains the current value of f(t,yy,yp,yyB,ypB).

The function JTVFUNB must set FLAG=0 if successful, or FLAG~=0 if a failure occurred.

See also IDASetOptions

NOTE: JTVFUN and JTVFUNB are specified through the property JacobianFn to IDASetOptions and are used only if the property LinearSolver was set to 'GMRES', 'BiCGStab', or 'TFQMR'.

IDAPrecSetupFn

Purpose

IDAPrecSetupFn - type for user provided preconditioner setup function.

Synopsis

This is a script file.

DESCRIPTION

IDAPrecSetupFn - type for user provided preconditioner setup function.

The user-supplied preconditioner setup function PSETFUN and the user-supplied preconditioner solve function PSOLFUN together must define a preconditoner matrix P which is an approximation to the Newton matrix M = $J_yy - cj*J_yp$. Here $J_yy = df/dyy$, $J_yp = df/dyp$, and cj is a scalar proportional to the integration step size h. The solution of systems P z = r, is to be carried out by the PrecSolve function, and PSETFUN is to do any necessary setup operations.

The user-supplied preconditioner setup function PSETFUN is to evaluate and preprocess any Jacobian-related data needed by the preconditioner solve function PSOLFUN. This might include forming a crude approximate Jacobian, and performing an LU factorization on the resulting approximation to M. This function will not be called in advance of every call to PSOLFUN, but instead will be called only as often as necessary to achieve convergence within the Newton iteration. If the PSOLFUN function needs no preparation, the PSETFUN function need not be provided.

For greater efficiency, the PSETFUN function may save Jacobian-related data and reuse it, rather than generating it from scratch. In this case, it should use the input flag JOK to decide whether to recompute the data, and set the output flag JCUR accordingly.

Each call to the PSETFUN function is preceded by a call to DAEFUN with the same (t,yy,yp) arguments. Thus the PSETFUN function can use any auxiliary data that is computed and saved by the DAEFUN function and made accessible to PSETFUN.

IVP Problem

The function PSETFUN must be defined as FUNCTION FLAG = PSETFUN(T,YY,YP,RR,CJ)

If successful, it must return FLAG=0. For a recoverable error (in which case the setup will be retried) it must set FLAG to a positive integer value. If an unrecoverable error occurs, it must set FLAG to a negative value, in which case the integration will be halted. The input argument RR contains the current value of f(t,yy,yp).

If a user data structure DATA was specified in IDAMalloc, then ${\tt PSETFUN}$ must be defined as

FUNCTION [FLAG,NEW_DATA] = PSETFUN(T,YY,YP,RR,CJ,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the flags JCUR and FLAG, the PSETFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

Adjoint Problem

The function PSETFUNB must be defined either as FUNCTION FLAG = PSETFUNB(T, YY, YP, YYB, YPB, RRB, CJB) or as

FUNCTION [FLAG, NEW_DATA] = PSETFUNB(T, YY, YP, YYB, YPB, RRB, CJB, DATA) depending on whether a user data structure DATA was specified in IDAMalloc.

See also IDAPrecSolveFn, IDASetOptions

NOTE: PSETFUN and PSETFUNB are specified through the property PrecSetupFn to IDASetOptions and are used only if the property LinearSolver was set to 'GMRES', 'BiCGStab', or 'TFQMR'.

IDAPrecSolveFn

Purpose

IDAPrecSolveFn - type for user provided preconditioner solve function.

Synopsis

This is a script file.

DESCRIPTION

IDAPrecSolveFn - type for user provided preconditioner solve function.

The user-supplied preconditioner solve function PSOLFUN is to solve a linear system P z = r, where P is the preconditioner matrix.

IVP Problem

The function PSOLFUN must be defined as
FUNCTION [Z, FLAG] = PSOLFUN(T,YY,YP,RR,R)
and must return a vector Z containing the solution of Pz=r.

If PSOLFUN was successful, it must return FLAG=0. For a recoverable error (in which case the step will be retried) it must set FLAG to a positive value. If an unrecoverable error occurs, it must set FLAG to a negative value, in which case the integration will be halted.

The input argument RR contains the current value of f(t,yy,yp).

If a user data structure DATA was specified in IDAMalloc, then ${\tt PSOLFUN}$ must be defined as

FUNCTION [Z, FLAG, NEW_DATA] = PSOLFUN(T,YY,YP,RR,R,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector Z and the flag FLAG, the PSOLFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

Adjoint Problem

The function PSOLFUNB must be defined either as FUNCTION [ZB,FLAG] = PSOLFUNB(T,YY,YP,YYB,YPB,RRB,RB)

or as

FUNCTION [ZB,FLAG,NEW_DATA] = PSOLFUNB(T,YY,YP,YYB,YPB,RRB,RB,DATA) depending on whether a user data structure DATA was specified in IDAMalloc. In either case, it must return the vector ZB and the flag FLAG.

See also ${\tt IDAPrecSetupFn}$, ${\tt IDASetOptions}$

NOTE: PSOLFUN and PSOLFUNB are specified through the property PrecSolveFn to IDASetOptions and are used only if the property LinearSolver was set to 'GMRES', 'BiCGStab', or 'TFQMR'.

4 MATLAB Interface to KINSOL

The MATLAB interface to KINSOL provides access to all functionality of the KINSOL solver.

The interface consists of 5 user-callable functions. The user must provide several required and optional user-supplied functions which define the problem to be solved. The user-callable functions and the types of user-supplied functions are listed in Table 3 and fully documented later in this section. For more in depth details, consult also the KINSOL user guide [1].

To illustrate the use of the KINSOL MATLAB interface, several example problems are provided with SUNDIALSTB, both for serial and parallel computations. Most of them are MATLAB translations of example problems provided with KINSOL.

Table 3: KINSOL MATLAB interface functions

Functions	KINSetOptions KINMalloc KINSol KINGetStats KINFree	creates an options structure for KINSOL. allocates and initializes memory for KINSOL. solves the nonlinear problem. returns statistics for the KINSOL solver. deallocates memory for the KINSOL solver.
Function types	KINSysFn KINDenseJacFn KINBandJacFn KINJacTimesVecFn KINPrecSetupFn KINPrecSolveFn KINGlocalFn KINGcommFn	system function dense Jacobian function banded Jacobian function Jacobian times vector function preconditioner setup function preconditioner solve function system approximation function (BBDPre) communication function (BBDPre)

Interface functions 4.1

KINSetOptions

PURPOSE KINSetOptions creates an options structure for KINSOL. Synopsis function options = KINSetOptions(varargin) DESCRIPTION KINSetOptions creates an options structure for KINSOL. Usage: options = KINSetOptions('NAME1', VALUE1, 'NAME2', VALUE2,...) creates a KINSOL options structure options in which the named properties have the specified values. Any unspecified properties have default values. It is sufficient to type only the leading characters that uniquely identify the property. Case is ignored for property names. options = KINSetOptions(oldoptions,'NAME1', VALUE1,...) alters an existing options structure oldoptions. options = KINSetOptions(oldoptions, newoptions) combines an existing options structure oldoptions with a new options structure newoptions. Any new properties overwrite corresponding old properties. KINSetOptions with no input arguments displays all property names and their possible values. KINSetOptions properties (See also the KINSOL User Guide) Verbose - verbose output [false | true] Specifies whether or not KINSOL should output additional information MaxNumIter - maximum number of nonlinear iterations [scalar | 200] Specifies the maximum number of iterations that the nonlinar solver is allowed to take. FuncRelErr - relative residual error [scalar | eps] Specifies the realative error in computing f(y) when used in difference quotient approximation of matrix-vector product J(y)*v. FuncNormTol - residual stopping criteria [scalar | eps^(1/3)] Specifies the stopping tolerance on ||fscale*ABS(f(y))||_L-infinity ScaledStepTol - step size stopping criteria [scalar | eps^(2/3)] Specifies the stopping tolerance on the maximum scaled step length: || y_(k+1) - y_k || || ------ ||_L-infinity

 $|| |y_{k+1}| + y_{k+1}|$

MaxNewtonStep - maximum Newton step size [scalar | 0.0]

```
Specifies the maximum allowable value of the scaled length of the Newton step.
InitialSetup - initial call to linear solver setup [ false | true ]
  Specifies whether or not KINSol makes an initial call to the linear solver
   setup function.
MaxNumSetups - [ scalar | 10 ]
  Specifies the maximum number of nonlinear iterations between calls to the
  linear solver setup function (i.e. Jacobian/preconditioner evaluation)
MaxNumSubSetups - [ scalar | 5 ]
  Specifies the maximum number of nonlinear iterations between checks by the
  nonlinear residual monitoring algorithm (specifies length of subintervals).
  NOTE: MaxNumSetups should be a multiple of MaxNumSubSetups.
MaxNumBetaFails - maximum number of beta-condition failures [ scalar | 10 ]
  Specifies the maximum number of beta-condiiton failures in the line search
  algorithm.
EtaForm - Inexact Newton method [ Constant | Type2 | Type1 ]
  Specifies the method for computing the eta coefficient used in the calculation
  of the linear solver convergence tolerance (used only if strategy='InexactNEwton'
   in the call to KINSol):
     lintol = (eta + eps)*||fscale*f(y)||_L2
  which is the used to check if the following inequality is satisfied:
      ||fscale*(f(y)+J(y)*p)||_L2 <= lintol
  Valid choices are:
                         | ||f(y_{k+1})||_{L2} - ||f(y_k)+J(y_k)*p_k||_{L2} |
  EtaForm='Type1' eta = ------
                                       ||f(y_k)||_{L2}
                                 [ ||f(y_{k+1})||_{L2} ]^{alpha}
  EtaForm='Type2' eta = gamma * [ ----- ]
                                 [ ||f(y_k)||_{L2} ]
  EtaForm='Constant'
Eta - constant value for eta [ scalar | 0.1 ]
  Specifies the constant value for eta in the case EtaForm='Constant'.
EtaAlpha - alpha parameter for eta [ scalar | 2.0 ]
  Specifies the parameter alpha in the case EtaForm='Type2'
EtaGamma - gamma parameter for eta [ scalar | 0.9 ]
  Specifies the parameter gamma in the case EtaForm='Type2'
MinBoundEps - lower bound on eps [ false | true ]
  Specifies whether or not the value of eps is bounded below by 0.01*FuncNormtol.
Constraints - solution constraints [ vector ]
  Specifies additional constraints on the solution components.
    Constraints(i) = 0 : no constrain on y(i)
    Constraints(i) = 1 : y(i) \>= 0
    Constraints(i) = -1 : y(i) <= 0
    Constraints(i) = 2 : y(i) > 0
    Constraints(i) = -2 : y(i) < 0
  If Constraints is not specified, no constraints are applied to y.
LinearSolver - Type of linear solver [ Dense | Band | GMRES | BiCGStab | TFQMR ]
  Specifies the type of linear solver to be used for the Newton nonlinear solver.
  Valid choices are: Dense (direct, dense Jacobian), GMRES (iterative, scaled
  preconditioned GMRES), BiCGStab (iterative, scaled preconditioned stabilized
  BiCG), TFQMR (iterative, scaled preconditioned transpose-free QMR).
  The GMRES, BiCGStab, and TFQMR are matrix-free linear solvers.
JacobianFn - Jacobian function [ function ]
```

This propeerty is overloaded. Set this value to a function that returns Jacobian information consistent with the linear solver used (see Linsolver). If not specified, KINSOL uses difference quotient approximations. For the Dense linear solver, JacobianFn must be of type KINDenseJacFn and must return a dense Jacobian matrix. For the iterative linear solvers, GMRES, BiCGStab, or TFQMR, JacobianFn must be of type KINJactimesVecFn and must return a Jacobian-vector product.

- KrylovMaxDim Maximum number of Krylov subspace vectors [scalar | 10] Specifies the maximum number of vectors in the Krylov subspace. This property is used only if an iterative linear solver, GMRES, BiCGStab, or TFQMR is used (see LinSolver).
- MaxNumRestarts Maximum number of GMRES restarts [scalar | 0]

 Specifies the maximum number of times the GMRES (see LinearSolver) solver
 can be restarted.
- PrecModule Built-in preconditioner module [BBDPre | UserDefined]

 If the PrecModule = 'UserDefined', then the user must provide at least a preconditioner solve function (see PrecSolveFn)

 KINSOL provides a built-in preconditioner module, BBDPre which can only be used with parallel vectors. It provide a preconditioner matrix that is block-diagonal with banded blocks. The blocking corresponds to the distribution of the variable vector among the processors. Each preconditioner block is generated from the Jacobian of the local part (on the current processor) of a given function g(t,y) approximating f(y) (see GlocalFn). The blocks are generated by a difference quotient scheme on each processor independently. This scheme utilizes an assumed banded structure with given half-bandwidths, mldq and mudq (specified through LowerBwidthDQ and UpperBwidthDQ, respectively). However, the banded Jacobian block kept by the scheme has half-bandwiths ml and mu (specified through LowerBwidth and UpperBwidth), which may be smaller.
- PrecSetupFn Preconditioner setup function [function]
 PrecSetupFn specifies an optional function which, together with PrecSolve,
 defines a right preconditioner matrix which is an aproximation
 to the Newton matrix. PrecSetupFn must be of type KINPrecSetupFn.
- PrecSolveFn Preconditioner solve function [function]

 PrecSolveFn specifies an optional function which must solve a linear system

 Pz = r, for given r. If PrecSolveFn is not defined, the no preconditioning will
 be used. PrecSolveFn must be of type KINPrecSolveFn.
- GlocalFn Local right-hand side approximation function for BBDPre [function] If PrecModule is BBDPre, GlocalFn specifies a required function that evaluates a local approximation to the system function. GlocalFn must be of type KINGlocalFn.
- GcommFn Inter-process communication function for BBDPre [function] If PrecModule is BBDPre, GcommFn specifies an optional function to perform any inter-process communication required for the evaluation of GlocalFn. GcommFn must be of type KINGcommFn.
- LowerBwidth Jacobian/preconditioner lower bandwidth [scalar | 0]
 This property is overloaded. If the Band linear solver is used (see LinSolver),
 it specifies the lower half-bandwidth of the band Jacobian approximation.
 If one of the three iterative linear solvers, GMRES, BiCGStab, or TFQMR is used
 (see LinSolver) and if the BBDPre preconditioner module in KINSOL is used
 (see PrecModule), it specifies the lower half-bandwidth of the retained
 banded approximation of the local Jacobian block.
 LowerBwidth defaults to 0 (no sub-diagonals).
- UpperBwidth Jacobian/preconditioner upper bandwidth [scalar | 0]
 This property is overloaded. If the Band linear solver is used (see LinSolver),

it specifies the upper half-bandwidth of the band Jacobian approximation. If one of the three iterative linear solvers, GMRES, BiCGStab, or TFQMR is used (see LinSolver) and if the BBDPre preconditioner module in KINSOL is used (see PrecModule), it specifies the upper half-bandwidth of the retained banded approximation of the local Jacobian block. UpperBwidth defaults to 0 (no super-diagonals).

LowerBwidthDQ - BBDPre preconditioner DQ lower bandwidth [scalar | 0] Specifies the lower half-bandwidth used in the difference-quotient Jacobian approximation for the BBDPre preconditioner (see PrecModule).

UpperBwidthDQ - BBDPre preconditioner DQ upper bandwidth [scalar | 0] Specifies the upper half-bandwidth used in the difference-quotient Jacobian approximation for the BBDPre preconditioner (see PrecModule).

See also

KINDenseJacFn, KINJacTimesVecFn KINPrecSetupFn, KINPrecSolveFn KINGlocalFn, KINGcommFn

KINMalloc

PURPOSE

KINMalloc allocates and initializes memory for KINSOL.

 $\mathbf{Synopsis}$

function [] = KINMalloc(fct,n,varargin)

DESCRIPTION

KINMalloc allocates and initializes memory for KINSOL.

Usage: KINMalloc (SYSFUN, N [, OPTIONS [, DATA]]);

SYSFUN is a function defining the nonlinear problem f(y) = 0. This function must return a column vector FY containing the

current value of the residual

N is the (local) problem dimension.

OPTIONS is an (optional) set of integration options, created with

the KINSetOptions function.

DATA is the (optional) problem data passed unmodified to all

user-provided functions when they are called. For example,

RES = SYSFUN(Y,DATA).

See also: KINSysFn

KINSol

PURPOSE

KINSol solves the nonlinear problem.

Synopsis

function [status,y] = KINSol(y0, strategy, yscale, fscale)

DESCRIPTION

KINSol solves the nonlinear problem.

Usage: [STATUS, Y] = KINSol(YO, STRATEGY, YSCALE, FSCALE)

KINSol manages the computational process of computing an approximate solution of the nonlinear system. If the initial guess (initial value assigned to vector Y0) doesn't violate any user-defined constraints, then KINSol attempts to solve the system f(y)=0. If an iterative linear solver was specified (see KINSetOptions), KINSol uses a nonlinear Krylov subspace projection method. The Newton-Krylov iterations are stopped if either of the following conditions is satisfied:

```
||f(y)||_L-infinity <= 0.01*fnormtol
||y[i+1] - y[i]||_L-infinity <= scsteptol
```

However, if the current iterate satisfies the second stopping criterion, it doesn't necessarily mean an approximate solution has been found since the algorithm may have stalled, or the user-specified step tolerance may be too large.

STRATEGY specifies the global strategy applied to the Newton step if it is unsatisfactory. Valid choices are 'None' or 'LineSearch'. YSCALE is a vector containing diagonal elements of scaling matrix for vector Y chosen so that the components of YSCALE*Y (as a matrix multiplication) all have about the same magnitude when Y is close to a root of f(y) FSCALE is a vector containing diagonal elements of scaling matrix for f(y) chosen so that the components of FSCALE*f(y) (as a matrix multiplication) all have roughly the same magnitude when u is not too near a root of f(y)

On return, status is one of the following:

- 0: KINSol succeeded
- 1: The initial yO already satisfies the stopping criterion given above
- 2: Stopping tolerance on scaled step length satisfied
- -1: Illegal attempt to call before KINMalloc
- -2: One of the inputs to KINSol is illegal.
- -5: The line search algorithm was unable to find an iterate sufficiently distinct from the current iterate
- -6: The maximum number of nonlinear iterations has been reached
- -7: Five consecutive steps have been taken that satisfy the following inequality:

||yscale*p||_L2 > 0.99*mxnewtstep

- -8: The line search algorithm failed to satisfy the beta-condition for too many times.
- -9: The linear solver's solve routine failed in a recoverable manner, but the linear solver is up to date.
- -10: The linear solver's intialization routine failed.
- -11: The linear solver's setup routine failed in an unrecoverable manner.
- -12: The linear solver's solve routine failed in an unrecoverable manner.

See also KINSetOptions, KINGetstats

KINGetStats

```
Purpose
KINGetStats returns statistics for the main KINSOL solver and the linear
Synopsis
function si = KINGetStats()
DESCRIPTION
KINGetStats returns statistics for the main KINSOL solver and the linear
solver used.
   Usage: solver_stats = KINGetStats;
Fields in the structure solver_stats
o nfe
        - total number evaluations of the nonlinear system function SYSFUN
o nni
        - total number of nonlinear iterations
o nbcf - total number of beta-condition failures
o nbops - total number of backtrack operations (step length adjustments)
          performed by the line search algorithm
o fnorm - scaled norm of the nonlinear system function f(y) evaluated at the
          current iterate: ||fscale*f(y)||_L2
       - scaled norm (or length) of the step used during the previous
o step
          iteration: ||uscale*p||_L2
o LSInfo - structure with linear solver statistics
The structure LSinfo has different fields, depending on the linear solver used.
 Fields in LSinfo for the 'Dense' linear solver
o name - 'Dense'
o njeD - number of Jacobian evaluations
o nfeD - number of right-hand side function evaluations for difference-quotient
         Jacobian approximation
```

Fields in LSinfo for the 'GMRES' or 'BiCGStab' linear solver

```
o name - 'GMRES' or 'BiCGStab'
o nli - number of linear solver iterations
```

o npe - number of preconditioner setups

o nps - number of preconditioner solve function calls

o ncfl - number of linear system convergence test failures

KINFree

PURPOSE

KINFree deallocates memory for the KINSOL solver.

Synopsis

function [] = KINFree()

DESCRIPTION

 ${\tt KINFree\ deallocates\ memory\ for\ the\ KINSOL\ solver}.$

Usage: KINFree

4.2 Function types

KINDenseJacFn

PURPOSE

KINDenseJacFn - type for user provided dense Jacobian function.

SYNOPSIS

This is a script file.

DESCRIPTION

KINDenseJacFn - type for user provided dense Jacobian function.

The function DJACFUN must be defined as FUNCTION [J, FLAG] = DJACFUN(Y,FY)

and must return a matrix J corresponding to the Jacobian of f(y). The input argument FY contains the current value of f(y). If a user data structure DATA was specified in KINMalloc, then DJACFUN must be defined as

FUNCTION [J, FLAG, NEW_DATA] = DJACFUN(Y,FY,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the matrix J and the flag FLAG, the DJACFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function DJACFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also KINSetOptions

NOTE: DJACFUN is specified through the property JacobianFn to KINSetOptions and is used only if the property LinearSolver was set to 'Dense'.

KINBandJacFn

Purpose

 ${\tt KINBandJacFn\ -\ type\ for\ user\ provided\ banded\ Jacobian\ function.}$

Synopsis

This is a script file.

DESCRIPTION

KINBandJacFn - type for user provided banded Jacobian function.

The function BJACFUN must be defined as FUNCTION [J, FLAG] = BJACFUN(Y, FY)

and must return a matrix J corresponding to the banded Jacobian of f(y). The input argument FY contains the current value of f(y).

If a user data structure DATA was specified in KINMalloc, then ${\tt BJACFUN}$ must be defined as

FUNCTION [J, FLAG, NEW_DATA] = BJACFUN(Y, FY, DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the matrix J and the flag FLAG, the BJACFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function BJACFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also KINSetOptions

NOTE: BJACFUN is specified through the property JacobianFn to KINSetOptions and is used only if the property LinearSolver was set to 'Band'.

KINGcommFn

Purpose

KINGcommFn - type for user provided communication function (BBDPre).

Synopsis

This is a script file.

DESCRIPTION

KINGcommFn - type for user provided communication function (BBDPre).

The function GCOMFUN must be defined as FUNCTION FLAG = GCOMFUN(Y)

and can be used to perform all interprocess communication necessary to evaluate the approximate right-hand side function for the BBDPre preconditioner module.

If a user data structure DATA was specified in KINMalloc, then ${\tt GCOMFUN}$ must be defined as

FUNCTION [FLAG, NEW_DATA] = GCOMFUN(Y, DATA)

If the local modifications to the user data structure are needed in other user-provided functions then the GCOMFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function GCOMFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also KINGlocalFn, KINSetOptions

NOTES:

 ${\tt GCOMFUN}$ is specified through the ${\tt GcommFn}$ property in KINSetOptions and is used only if the property PrecModule is set to 'BBDPre'.

Each call to GCOMFUN is preceded by a call to the system function SYSFUN with the same argument Y. Thus GCOMFUN can omit any communication done by SYSFUN if relevant to the evaluation of G by GLOCFUN. If all necessary communication was done by SYSFUN, GCOMFUN need not be provided.

KINGlocalFn

Purpose

KINGlocalFn - type for user provided RHS approximation function (BBDPre).

Synopsis

This is a script file.

DESCRIPTION

KINGlocalFn - type for user provided RHS approximation function (BBDPre).

The function GLOCFUN must be defined as FUNCTION [G, FLAG] = GLOCFUN(Y)

and must return a vector G corresponding to an approximation to f(y) which will be used in the BBDPRE preconditioner module. The case where G is mathematically identical to F is allowed.

If a user data structure DATA was specified in KINMalloc, then ${\tt GLOCFUN}$ must be defined as

FUNCTION [G, FLAG, NEW_DATA] = GLOCFUN(Y, DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector G, the GLOCFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function GLOCFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also KINGcommFn, KINSetOptions

NOTE: GLOCFUN is specified through the GlocalFn property in KINSetOptions and is used only if the property PrecModule is set to 'BBDPre'.

KINJacTimesVecFn

Purpose

KINJacTimesVecFn - type for user provided Jacobian times vector function.

Synopsis

This is a script file.

DESCRIPTION

KINJacTimesVecFn - type for user provided Jacobian times vector function.

The function JTVFUN must be defined as

FUNCTION [JV, NEW_Y, FLAG] = JTVFUN(Y, V, NEW_Y) and must return a vector JV corresponding to the product of the Jacobian of f(y) with the vector v. On input, NEW_Y indicates if the iterate has been updated in the interim. JV must be update or reevaluated, if appropriate, unless NEW_Y=false. This flag must be reset by the user.

If a user data structure DATA was specified in KINMalloc, then ${\tt JTVFUN}$ must be defined as

FUNCTION [JV, NEW_Y, FLAG, NEW_DATA] = JTVFUN(Y, V, NEW_Y, DATA)

If the local modifications to the user data structure are needed in

other user-provided functions then, besides setting the vector JV, and

flags NEW_Y and FLAG, the JTVFUN function must also set NEW_DATA. Otherwise,

it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to

unnecessary copying).

If successful, FLAG should be set to 0. If an error occurs, FLAG should be set to a nonzero value.

See also KINSetOptions

NOTE: JTVFUN is specified through the property JacobianFn to KINSetOptions and is used only if the property LinearSolver was set to 'GMRES' or 'BiCGStab'.

KINPrecSetupFn

PURPOSE

KINPrecSetupFn - type for user provided preconditioner setup function.

Synopsis

This is a script file.

DESCRIPTION

KINPrecSetupFn - type for user provided preconditioner setup function.

The user-supplied preconditioner setup subroutine should compute the right-preconditioner matrix P used to form the scaled preconditioned linear system:

$$(Df*J(y)*(P^-1)*(Dy^-1)) * (Dy*P*x) = Df*(-F(y))$$

where Dy and Df denote the diagonal scaling matrices whose diagonal elements are stored in the vectors YSCALE and FSCALE, respectively.

The preconditioner setup routine (referenced by iterative linear solver modules via pset (type KINSpilsPrecSetupFn)) will not be called prior to every call made to the psolve function, but will instead be called only as often as necessary to achieve convergence of the Newton iteration.

NOTE: If the PRECSOLVE function requires no preparation, then a preconditioner setup function need not be given.

The function PSETFUN must be defined as
FUNCTION FLAG = PSETFUN(Y, YSCALE, FY, FSCALE)
The input argument FY contains the current value of f(y), while YSCALE and FSCALE are the scaling vectors for solution and system function, respectively (as passed to KINSol)

If a user data structure DATA was specified in KINMalloc, then PSETFUN must be defined as

FUNCTION [FLAG, NEW_DATA] = PSETFUN(Y, YSCALE, FY, FSCALE, DATA) If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the flag FLAG, the PSETFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

If successful, PSETFUN must return FLAG=0. For a recoverable error (in which case the setup will be retried) it must set FLAG to a positive integer value. If an unrecoverable error occurs, it must set FLAG to a negative value, in which case the solver will halt.

See also KINPrecSolveFn, KINSetOptions, KINSol

NOTE: PSETFUN is specified through the property PrecSetupFn to KINSetOptions and is used only if the property LinearSolver was set to 'GMRES' or 'BiCGStab'.

KINPrecSolveFn

Purpose

KINPrecSolveFn - type for user provided preconditioner solve function.

Synopsis

This is a script file.

DESCRIPTION

KINPrecSolveFn - type for user provided preconditioner solve function.

The user-supplied preconditioner solve function PSOLFN is to solve a linear system $P\ z=r$ in which the matrix P is

the preconditioner matrix (possibly set implicitely by PSETFUN)

The function PSOLFUN must be defined as
FUNCTION [Z, FLAG] = PSOLFUN(Y, YSCALE, FY, FSCALE, R)
and must return a vector Z containing the solution of Pz=r.
The input argument FY contains the current value of f(y), while YSCALE
and FSCALE are the scaling vectors for solution and system function,
respectively (as passed to KINSol)

If a user data structure DATA was specified in KINMalloc, then PSOLFUN must be defined as

FUNCTION [Z, FLAG, NEW_DATA] = PSOLFUN(Y,YSCALE,FY,FSCALE,R,DATA) If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector Z and the flag FLAG, the PSOLFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

If successful, PSOLFUN must return FLAG=0. For a recoverable error it must set FLAG to a positive value (in which case the solver will attempt to correct). If an unrecoverable error occurs, it must set FLAG to a negative value, in which case the solver will halt.

See also KINPrecSetupFn, KINSetOptions

NOTE: PSOLFUN is specified through the property PrecSolveFn to KINSetOptions and is used only if the property LinearSolver was set to 'GMRES' or 'BiCGStab'.

KINSysFn

Purpose

KINSysFn - type for user provided system function

Synopsis

This is a script file.

Description

KINSysFn - type for user provided system function

The function SYSFUN must be defined as
FUNCTION [FY, FLAG] = SYSFUN(Y)
and must return a vector FY corresponding to f(y).

If a user data structure DATA was specified in KINMalloc, then
SYSFUN must be defined as

FUNCTION [FY, FLAG, NEW_DATA] = SYSFUN(Y,DATA)

If the local modifications to the user data structure are needed in other user-provided functions then, besides setting the vector FY, the SYSFUN function must also set NEW_DATA. Otherwise, it should set NEW_DATA=[] (do not set NEW_DATA = DATA as it would lead to unnecessary copying).

The function SYSFUN must set FLAG=0 if successful, FLAG<0 if an unrecoverable failure occurred, or FLAG>0 if a recoverable error occurred.

See also KINMalloc

 ${\tt NOTE:}$ SYSFUN is specified through the KINMalloc function.

5 Supporting modules

This section describes two additional modules in SUNDIALSTB, NVECTOR and PUTILS. The functions in NVECTOR perform various operations on vectors. For serial vectors, all of these operations default to the corresponding MATLAB functions. For parallel vectors, they can be used either on the local portion of the distributed vector or on the global vector (in which case they will trigger an MPI Allreduce operation). The functions in PUTILS are used to run parallel SUNDIALSTB applications. The user should only call the function mpirun to launch a parallel MATLAB application. See one of the parallel SUNDIALSTB examples for usage.

The functions in these two additional modules are listed in Table 4 and described in detail in the remainder of this section.

Table 4: The NVECTOR and PUTILS functions

NVECTOR	N_VMax N_VMaxNorm N_VMin N_VDotProd N_VWrmsNorm N_VWL2Norm N_VL1Norm	returns the largest element of x returns the maximum norm of x returns the smallest element of x returns the dot product of two vectors returns the weighted root mean square norm of x returns the weighted Euclidean L2 norm of x returns the L1 norm of x
PUTILS	mpirun mpiruns mpistart	runs parallel examples runs the parallel example on a child MATLAB process lamboot and MPI_Init master (if required)

5.1 NVECTOR functions

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N_VDotProd

```
PURPOSE
N_VDotProd returns the dot product of two vectors
Synopsis
function ret = N_VDotProd(x,y,comm)
Description
N_VDotProd returns the dot product of two vectors
   Usage: RET = N_VDotProd ( X, Y [, COMM] )
If COMM is not present, N_VDotProd returns the dot product of the
local portions of X and Y. Otherwise, it returns the global dot
product.
Source Code
function ret = N_VDotProd(x, y, comm)
% Radu Serban <radu@llnl.gov>
% Copyright (c) 2005, The Regents of the University of California.
% $Revision: 1.1 $Date: 2006/01/06 19:00:10 $
if nargin == 2
  ret = dot(x,y);
else
  ldot = dot(x, y);
  gdot = 0.0;
  MPI_Allreduce(ldot, gdot, 'SUM', comm);
  ret = gdot;
end
```

N_VL1Norm

```
PURPOSE

N_VL1Norm returns the L1 norm of x

SYNOPSIS

function ret = N_VL1Norm(x,comm)

DESCRIPTION
```

```
N_VL1Norm returns the L1 norm of x
      Usage: RET = N_VL1Norm ( X [, COMM] )
   If COMM is not present, N_VL1Norm returns the L1 norm of
   the local portion of X. Otherwise, it returns the global
   L1 norm..
   Source Code
  | function ret = N_VL1Norm(x, comm) |
  % Radu Serban <radu@llnl.gov>
  % Copyright (c) 2005, The Regents of the University of California.
  % $Revision: 1.1 $Date: 2006/01/06 19:00:10 $
12
13
   if nargin == 1
14
15
     ret = norm(x, 1);
16
17
   else
18
19
     lnrm = norm(x, 1);
20
     gnrm = 0.0;
21
     MPI_Allreduce(lnrm, gnrm, 'MAX', comm);
22
23
     ret = gnrm;
   end
```

N_VMax

```
PURPOSE

N_VMax returns the largest element of x

SYNOPSIS

function ret = N_VMax(x,comm)

DESCRIPTION

N_VMax returns the largest element of x

Usage: RET = N_VMax ( X [, COMM] )

If COMM is not present, N_VMax returns the maximum value of the local portion of X. Otherwise, it returns the global maximum value.

SOURCE CODE

function ret = N_VMax(x,comm)

% Radu Serban <radu@llnl.gov>
% Copyright (c) 2005, The Regents of the University of California.
% $Revision: 1.1 $Date: 2006/01/06 19:00:10 $
```

```
if nargin == 1
15
      ret = \max(x);
17
   else
18
19
     lmax = max(x);
20
     gmax = 0.0;
^{21}
      MPI_Allreduce(lmax,gmax, 'MAX',comm);
22
      ret = gmax;
23
24
   end
25
```

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N_VMaxNorm

```
Purpose
 N_VMaxNorm returns the L-infinity norm of x
 Synopsis
 function ret = N_VMaxNorm(x, comm)
 DESCRIPTION
 N_VMaxNorm returns the L-infinity norm of x
   Usage: RET = N_VMaxNorm ( X [, COMM] )
 If COMM is not present, N_VMaxNorm returns the L-infinity norm
 of the local portion of X. Otherwise, it returns the global
 L-infinity norm..
 Source Code
| function ret = N_VMaxNorm(x, comm) |
% Radu Serban <radu@llnl.gov>
% Copyright (c) 2005, The Regents of the University of California.
% $Revision: 1.1 $Date: 2006/01/06 19:00:10 $
 if nargin == 1
   ret = norm(x, 'inf');
 else
   lnrm = norm(x, 'inf');
   gnrm = 0.0;
   MPI_Allreduce(lnrm, gnrm, 'MAX', comm);
   ret = gnrm;
end
```

N_VMin

```
Purpose
N_VMin returns the smallest element of x
Synopsis
function ret = N_VMin(x,comm)
DESCRIPTION
N_VMin returns the smallest element of x
   Usage: RET = N_VMin ( X [, COMM] )
If COMM is not present, N_{-}VMin returns the minimum value of
the local portion of X. Otherwise, it returns the global
minimum value.
Source Code
function ret = N_VMin(x,comm)
% Radu Serban <radu@llnl.gov>
% Copyright (c) 2005, The Regents of the University of California.
% $Revision: 1.1 $Date: 2006/01/06 19:00:10 $
if nargin == 1
   ret = min(x);
else
   lmin = min(x);
   gmin = 0.0;
   MPI_Allreduce(lmin,gmin,'MIN',comm);
   ret = gmin;
end
```

N_VWL2Norm

```
PURPOSE

N_VWL2Norm returns the weighted Euclidean L2 norm of x

SYNOPSIS

function ret = N_VWL2Norm(x,w,comm)

DESCRIPTION
```

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22 23

```
N_VWL2Norm returns the weighted Euclidean L2 norm of x
      with weight vector w:
      sqrt [(sum (i = 0 to N-1) (x[i]*w[i])^2)]
      Usage: RET = N_VWL2Norm ( X, W [, COMM] )
   If COMM is not present, N_VWL2Norm returns the weighted L2
   norm of the local portion of X. Otherwise, it returns the
   global weighted L2 norm..
   Source Code
  function ret = N_VWL2Norm(x, w, comm)
11
  % Radu Serban < radu@llnl.gov>
12
  % Copyright (c) 2005, The Regents of the University of California.
13
  % $Revision: 1.1 $Date: 2006/01/06 19:00:10 $
14
15
   if nargin == 2
16
17
     ret = dot(x.^2, w.^2);
18
     ret = sqrt(ret);
19
20
   else
21
22
     lnrm = dot(x.^2, w.^2);
23
     gnrm = 0.0;
24
     MPI_Allreduce(lnrm, gnrm, 'SUM', comm);
26
     ret = sqrt(gnrm);
27
28
  end
```

N_VWrmsNorm

```
PURPOSE

N_VWrmsNorm returns the weighted root mean square norm of x

SYNOPSIS

function ret = N_VWrmsNorm(x,w,comm)

DESCRIPTION

N_VWrmsNorm returns the weighted root mean square norm of x

with weight vector w:
    sqrt [(sum (i = 0 to N-1) (x[i]*w[i])^2)/N]

Usage: RET = N_VWrmsNorm ( X, W [, COMM] )

If COMM is not present, N_VWrmsNorm returns the WRMS norm of the local portion of X. Otherwise, it returns the global WRMS norm..
```

Source Code

```
function ret = N_VWrmsNorm(x, w, comm)
11
  % Radu Serban <radu@llnl.gov>
  % Copyright (c) 2005, The Regents of the University of California.
  % $Revision: 1.1 $Date: 2006/01/06 19:00:11 $
14
   if nargin == 2
16
17
     ret = dot(x.^2, w.^2);
18
     ret = sqrt(ret/length(x));
19
20
   else
21
22
     lnrm = dot(x.^2,w.^2);
23
     gnrm = 0.0;
24
     MPI_Allreduce(lnrm, gnrm, 'SUM', comm);
25
26
     ln = length(x);
27
     gn = 0;
28
     MPI_Allreduce(ln,gn,'SUM',comm);
29
     ret = sqrt(gnrm/gn);
31
32
33 end
```

5.2 Parallel utilities

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mpirun

```
PURPOSE
MPIRUN runs parallel examples.
Synopsis
function [] = mpirun(fct,npe,dbg)
DESCRIPTION
MPIRUN runs parallel examples.
  Usage: MPIRUN ( FCT , NPE [, DBG] )
  FCT - function to be executed on all MATLAB processes.
  NPE - number of processes to be used (including the master).
  DBG - flag for debugging [ true | false ]
        If true, spawn MATLAB child processes with a visible xterm.
Source Code
function [] = mpirun(fct, npe, dbg)
% Radu Serban <radu@llnl.gov>
% Copyright (c) 2005, The Regents of the University of California.
% $Revision: 1.2 $Date: 2006/03/07 01:20:01 $
ih = isa(fct, 'function_handle');
is = isa(fct, 'char');
if ih
  sh = functions(fct);
  fct_str = sh.function;
elseif is
  fct_str = fct;
  error('mpirun:: LUnrecognized_function');
end
if exist(fct_str) = 2
  err_msg = sprintf('mpirun::_Function_%s_not_in_search_path.',fct_str);
  error(err_msg);
end
nslaves = npe-1;
mpistart (nslaves);
debug = false;
if (nargin > 2) \& dbg
  debug = true;
end
```

```
38
   cmd_slaves = sprintf('mpiruns(''%s'')', fct_str);
39
40
   if debug
41
     cmd = 'xterm';
42
     args = { '-sb', '-sl', '5000', '-e', 'matlab', '-nosplash', '-nojvm', '-r', cmd_slaves};
43
   else
44
     cmd = 'matlab';
45
     args = { '-nosplash ', '-nojvm ', '-r ', cmd\_slaves };
46
47
48
   [info children errs] = MPI_Comm_spawn(cmd, args, nslaves, 'NULL', 0, 'SELF');
49
   [info NEWORLD] = MPI_Intercomm_merge(children, 0);
51
52
  % Put the MPI communicator in the global workspace
53
   global sundials_MPI_comm;
   sundials\_MPI\_comm = NEWORLD;
55
  % Get rank of current process and put it in the global workspace
57
   [status mype] = MPI_Comm_rank(NEWORLD);
   global sundials_MPI_rank;
   sundials_MPI_rank = mype;
61
  % Call the user main program
   feval(fct ,NEWORLD);
63
64
  % Clear the global MPI communicator variable
65
  clear sundials_MPI_comm
```

mpiruns

```
PURPOSE

MPIRUNS runs the parallel example on a child MATLAB process.

SYNOPSIS

function [] = mpiruns(fct)

DESCRIPTION

MPIRUNS runs the parallel example on a child MATLAB process.

Usage: MPIRUNS ( FCT )

This function should not be called directly. It is called by mpirun on the spawned child processes.

SOURCE CODE

function [] = mpiruns(fct)

Radu Serban < radu@llnl.gov>
Copyright (c) 2005, The Regents of the University of California.
```

```
% $Revision: 1.2 $Date: 2006/03/07 01:20:01 $
12
   clc;
13
   [dummy hostname] = system ('hostname');
1.5
   fprintf('mpiruns_::_child_MATLAB_process_on_%s\n',hostname);
16
17
   MPI_Init;
18
19
   MPI_Errhandler_set('WORLD', 'RETURN');
20
21
   [info parent] = MPI_Comm_get_parent;
22
   fprintf('mpiruns_::_waiting_to_merge_MPI_intercommunicators_..._');
24
   [info NEWORLD] = MPI_Intercomm_merge(parent,1);
25
   fprintf('OK!\n\n');
26
27
   MPI_Errhandler_set (NEWORLD, 'RETURN');
28
29
  % Put the MPI communicator in the global workspace
30
   global sundials_MPI_comm;
   sundials\_MPI\_comm = NEWORLD;
32
33
  % Get rank of current process and put it in the global workspace
34
   [status mype] = MPI_Comm_rank(NEWORLD);
   global sundials_MPI_rank;
   sundials_MPI_rank = mype;
37
   fprintf('mpiruns_::_MPI_rank:_%d\n\n',mype);
39
40
   fprintf('-----
                                                                                --\n\n');
41
42
  % Call the user main program
43
   feval(fct ,NEWORLD);
44
45
  % Clear the global MPI communicator variable
   clear sundials_MPI_comm
47
  % Finalize MPI on this slave
49
  MPI_Finalize;
```

mpistart

```
Purpose

MPISTART invokes lamboot (if required) and MPI_Init (if required).

Synopsis

function mpistart(nslaves, rpi, hosts)

Description
```

```
MPISTART invokes lamboot (if required) and MPI_Init (if required).
   Usage: MPISTART [ ( NSLAVES [, RPI [, HOSTS] ] ) ]
   MPISTART boots LAM and initializes MPI to match a given number of slave
   hosts (and rpi) from a given list of hosts. All three args optional.
   If they are not defined, HOSTS are taken from a builtin HOSTS list
   (edit HOSTS at the beginning of this file to match your cluster)
   or from the bhost file if defined through LAMBHOST (in this order).
   If not defined, RPI is taken from the builtin variable RPI (edit it
   to suit your needs) or from the LAM_MPI_SSI_rpi environment variable
   (in this order).
Source Code
function mpistart (nslaves, rpi, hosts)
% Heavily based on the LAM_Init function in MPITB.
% ARGCHECK
% List of hosts
if nargin>2
% Hosts passed as an argument...
  if ~iscell(hosts)
     error('MPISTART: _3rd_arg_is_not_a_cell');
  end
  for i = 1: length (hosts)
     if ~ischar(hosts{i})
       error ('MPISTART: _3rd_arg_is_not_cell-of-strings');
    end
  end
else
% Get hosts from file specified in env. var. LAMBHOST
  bfile = getenv('LAMBHOST');
  if isempty(bfile)
     error('MPISTART: _cannot _find _list _of _hosts');
  hosts = readHosts(bfile);
end
% RPI
```

17 18 19

21

23

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5.1

if nargin>1

```
53
   % RPI passed as an argument
54
55
      if ~ischar(rpi)
56
        error ('MPISTART: _2nd_arg_is_not_a_string')
57
58
   % Get full rpi name, if single letter used
59
      rpi = rpi_str(rpi);
60
      if isempty (rpi)
61
        error ('MPISTART: _2nd_arg_is_not_a_known_RPI')
62
63
64
   else
65
66
   % Get RPI from env. var. LAM_MPI_SSI_rpi
67
68
     RPI = getenv('LAM_MPI_SSI_rpi');
69
      if isempty (RPI)
70
        If LAM_MPI_SSI_rpi not defined, use RPI='tcp'
71
        RPI = 'tcp';
72
      end
73
      rpi = rpi_str(RPI);
74
75
   end
76
77
   % Number of slaves
78
79
   if nargin>0
80
      if ~isreal (nslaves) || fix (nslaves)~=nslaves || nslaves>=length (hosts)
81
        error ('MPISTART: _1st _arg _is _not _a_valid _#slaves')
82
      end
83
   else
84
      nslaves = length(hosts) - 1;
85
87
   % LAMHALT %
89
   % reasons to lambalt:
91
   \% - not enough nodes (nslv+1) \% NHL < NSLAVES+1
   % - localhost not
                          in list % weird - just lamboot (NHL=0)
93
   % - localhost not last in list % weird - just lamboot (NHL=0)
94
95
96
   % Lam Nodes Output
97
   [stat, LNO] = system('lamnodes');
98
   if "stat
                                                      % already lambooted
99
100
      emptyflag = false;
101
      if isempty (LNO)
102
        % this shouldn't happen
103
        emptyflag=true;
104
        % it's MATLAB's fault I think
105
        fprintf('pushing_stubborn_MATLAB_"system"_call_(lamnodes):_');
106
```

```
end
107
      while isempty (LNO) || stat
109
        fprintf('.');
        [stat, LNO] = system('lamnodes');
111
      end
112
      if emptyflag
113
        fprintf('\n');
114
      end
115
116
     LF = char(10);
117
     LNO = split(LNO, LF);
                                                       % split lines in rows at \n
118
      [stat, NHL] = system('lamnodes|wc_-l');
                                                       % Number of Hosts in Lamnodes
120
121
      emptvflag = false;
122
                                                       % again,
      if isempty (NHL)
                                                       % this shouldn't happen
123
        emptyflag=true;
                                                       % it's MATLAB's fault I think
124
        fprintf('pushing_stubborn_MATLAB_"system"_call_(lamnodes|wc):_');
125
126
      while isempty (NHL) || stat
        fprintf('.');
128
        [stat, NHL] = system('lamnodes|wc_-l');
129
      end
130
      if emptyflag
131
        fprintf('\n');
132
133
134
     NHL = str2num(NHL);
135
      if NHL ~= size (LNO,1) || ~ NHL>0
                                                       % Oh my, logic error
136
                                                       % pretend there are no nodes
        NHL = 0;
137
        disp ('MPISTART: _internal _logic_error: _lamboot')
138
                                                       % to force lamboot w/o lambalt
139
      if isempty (findstr (LNO(end,:), 'this_node')) % master computer last in list
140
        disp ('MPISTART: _local_host_is_not_last_in_nodelist, _hope_that'', s_right')
141
        beforeflag = 0;
        for i = 1: size (LNO, 1)
143
          if ~isempty(findstr(LNO(i,:), 'this_node'))
             beforeflag = 1;
145
                                                       % well, not 1st but it's there
             break;
146
          end
147
                                                       % we already warned the user
        end
148
        if beforeflag
                                                       % Oh my, incredible, not there
149
          NHL = 0:
                                                       % pretend there are no nodes
150
          disp ('MPISTART: _local _host _not _in _LAM? _lamboot')
151
        end
152
      end
                                                       % to force lamboot w/o lambalt
153
154
      if NHL > 0
                                                       % accurately account multiprocessors
155
                                                       % number of CPUs in lamnodes
        NCL = 0;
156
        for i = 1: size (LNO, 1)
                                                       % add the 2nd ":"-separated
157
          fields = split(LNO(i,:), ':');
                                                       % field, ie, #CPUs
158
          NCL = NCL + str2num (fields (2,:));
        end
160
```

```
if NCL<NHL
                                                        % Oh my, logic error
161
          NHL = 0;
                                                        % pretend there are no nodes
162
           disp ('MPISTART: _internal_logic_error: _lamboot')
163
          % update count
165
          NHL=NCL;
166
        end
                                                        % can't get count from MPI,
167
                                                        % since might be not _Init 'ed
      end
168
169
      if NHL < nslaves+1
                                                        % we have to lamboot
170
171
        % but avoid getting caught
172
        [infI flgI] = MPI_Initialized;
                                                        % Init?
        [infF flgF]=MPI_Finalized;
                                                        % Finalize?
174
        if infI || infF
175
           error ('MPISTART: Lerror L calling L Initialized / Finalized?')
176
        end
177
        if flgI && ~flgF
                                                        % avoid hangup due to
178
           MPI_Finalize;
                                                        % inminent lambalt
           clear MPI_*
                                                        % force MPI_Init in Mast/Ping
180
           disp ('MPISTART: _MPI_already _used -_ clearing _before _lamboot')
        end
                                                        % by pretending "not _Init"
182
        if NHL > 0
                                                        % avoid lambalt in weird cases
183
           disp ('MPISTART: _halting _LAM')
184
           system ('lamhalt');
                                                        % won't get caught on this
185
        end
186
      end
187
    end
188
189
190
   % LAMBOOT
191
192
   % reasons to lamboot:
193
   % - not lambooted yet
                                       \% \operatorname{stat} = 0
   \% - lambalted above (or weird) \% NHL < NSLAVES+1 (0 _is_ <)
195
197
    if stat | NHL<nslaves+1
199
      HNAMS=hosts\{end\};
200
      for i=nslaves:-1:1
201
        HNAMS=strvcat(hosts{i},HNAMS);
202
203
      HNAMS = HNAMS';
                                                        % transpose for "for"
204
205
      fid=fopen('bhost','wt');
206
      for h = HNAMS
207
        fprintf(fid, '%s\n',h');
                                                        % write slaves' hostnames
208
      end
209
      fclose (fid);
210
      disp ('MPISTART: booting LAM')
211
212
      stat = system('lamboot\_-s\_-v\_bhost');
213
214
```

```
% again, this shouldn't happen
215
        fprintf('pushing_stubborn_MATLAB_"system"_call_(lamboot):_');
217
          fprintf('.'); stat = system('lamboot_-s_-v_bhost');
218
219
        fprintf('\n');
220
      end
221
222
      system ('rm_-f_bhost');
                                                       % don't need bhost anymore
223
                                                       % won't wipe on exit/could lambalt
224
225
226
   % RPI CHECK
227
228
229
    [infI flgI] = MPI_Initialized;
                                                       % Init?
230
    [infF flgF] = MPI_Finalized;
                                                       % Finalize?
231
232
    if infI || infF
233
      error ('MPISTART: _error_calling __Initialized / _Finalized?')
234
    end
236
    if flgI && ~flgF
                                                       % Perfect, ready to start
                                                       % something we could fix?
    else
238
      % MPI used, will break
239
        clear MPI_*
                                                       % unless we clear MPITB
240
        disp ('MPISTART: _MPI_already _used - _ clearing') % must start over
241
      end
242
243
      MPI_Init;
244
   end
245
246
247
   % NSLAVES CHECK
248
249
    [info attr flag] = MPI_Attr_get(MPLCOMM_WORLD, MPI_UNIVERSE_SIZE);
251
   if info | ~flag
252
      error('MPISTART:_attribute_MPI_UNIVERSE_SIZE_does_not_exist?')
253
   end
   if attr < 2
255
      error('MPISTART: _required _2 _computers _in _LAM')
256
   end
257
258
259
260
    function hosts = readHosts(bfile)
261
262
    hosts = [];
263
264
    fid = fopen(bfile);
265
    if fid == -1
266
      fprintf('Cannot_open_bhost_file_%s\n', bfile);
267
      return;
268
```

```
269
    end
    i = 0;
271
    while ~feof(fid)
272
   % get a line
273
      l = fgetl(fid);
   % Discard comments
275
      ic = \min(strfind(l, '\#'));
276
      if isempty(ic), l = l(1:ic-1); end
277
   % Test if there is anything left :-)
278
      if isempty(1), continue; end
279
   % Got a new host
280
      i = i + 1;
   % Stop at first blank or tab=char(9)
282
      indx = find((l==', ', ') | (l==char(9)));
283
      if isempty (indx)
284
        hosts{i} = 1;
285
      else
286
        hosts{i} = l(1:min(indx));
287
288
    end
290
    fclose (fid);
291
292
293
294
295
    function rpi = rpi str(c)
296
   %RPLSTR Full LAM SSI RPI string given initial letter(s)
297
298
       rpi = rpi_str(c)
299
   %
300
   %
             initial char(s) of rpi name: t,l,u,s
301
   %
       rpi full rpi name, one of: tcp, lamd, usysv, sysv
302
   %
             Use '' if c doesn't match to any supported rpi
303
304
305
    flag = nargin^{\sim} = 1 \mid | isempty(c) | | ~ischar(c);
306
    if flag
307
      return
308
    end
309
310
    c = lower(c(1));
311
    rpis={'tcp', 'lamd', 'usysv', 'sysv', 'none'};  % 'none' is sentinel
312
313
    for i=1:length(rpis)
314
      if rpis \{i\}(1) = c
315
        break
316
      end
317
    end
318
319
    if i < length (rpis)
320
      rpi=rpis\{i\};
                                                         % normal cases
   else
322
```

```
\begin{array}{c|c} {}_{323} & r\,p\,i=\ \\ {}^{323} & end \end{array} % no way, unknown rpi
```

References

- [1] A. M. Collier, A. C. Hindmarsh, R. Serban, and C.S. Woodward. User Documentation for KINSOL v2.2.0. Technical Report UCRL-SM-208116, LLNL, 2004.
- [2] A. C. Hindmarsh, P. N. Brown, K. E. Grant, S. L. Lee, R. Serban, D. E. Shumaker, and C. S. Woodward. SUNDIALS, suite of nonlinear and differential/algebraic equation solvers. *ACM Trans. Math. Softw.*, (in press), 2004.
- [3] A. C. Hindmarsh and R. Serban. User Documentation for CVODES v2.1.0. Technical report, LLNL, 2004. UCRL-SM-208111.
- [4] A. C. Hindmarsh and R. Serban. User Documentation for IDA v2.2.0. Technical Report UCRL-SM-208112, LLNL, 2004.