



you own a magic pair of shoes. You have run the 10 meters with it a lot and you have a long log of the time you have run with it.

one day, you come home and it seems like someone has moved your shoes. You get concerned that someone might have taken your (beloved) shoes and instead replaced it with identical looking shoes.

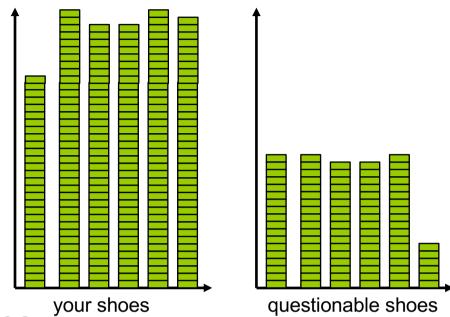
you inspect the shoes long and hard and they *look* the same. But still worried. How do you verify that they are the same?

### <30 sec brainstorming>

ok, so you run the 10 meters with the "questionable" shoes a bunch of times.

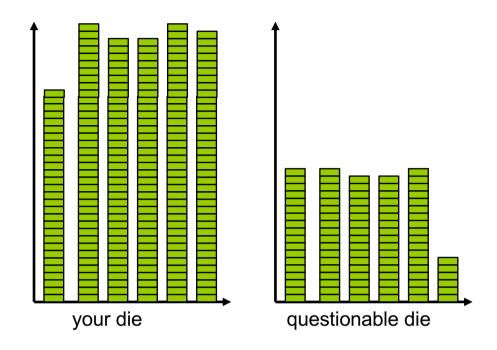
here is what you see...





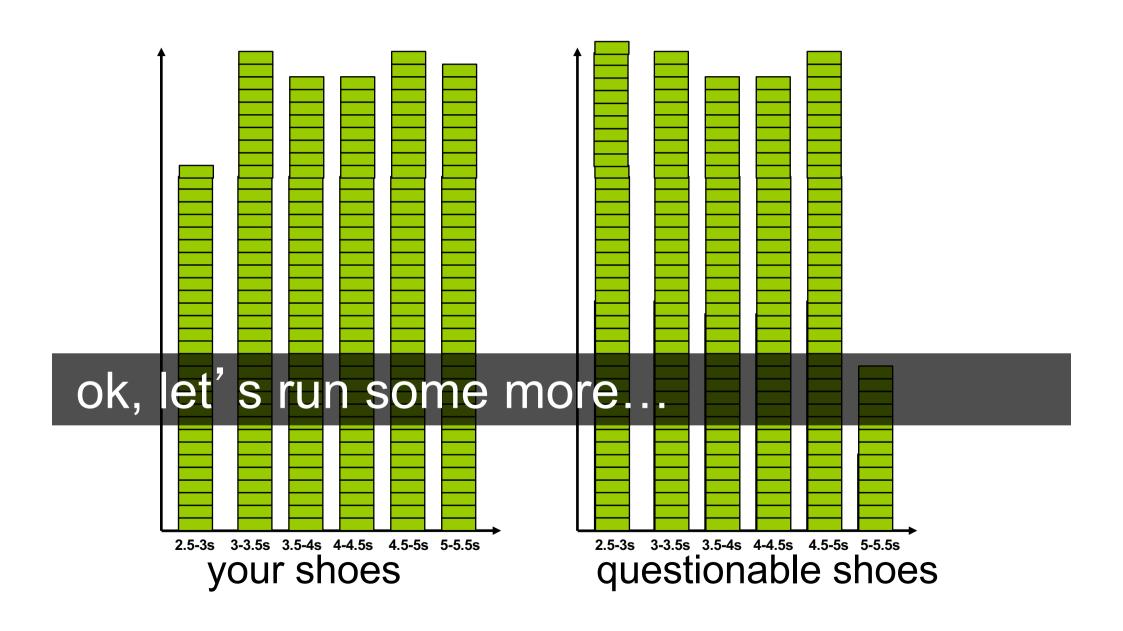
- [] this is still the original shoes
- [] someone has replaced my shoes
- [x] could be the original or replacement shoes

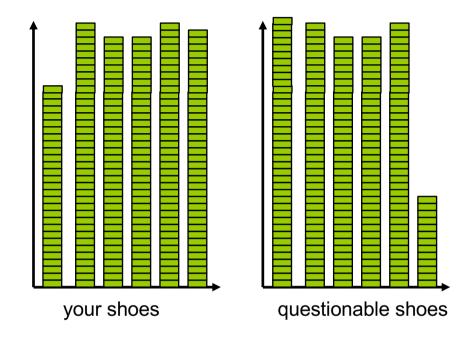
#### <let's vote>



the distribution looks different from the shoes you know

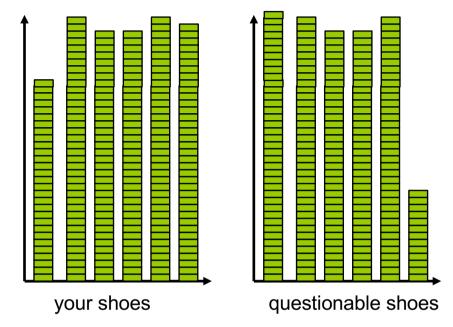
while it is possible that it is the same shoes, it seems somewhat unlikely



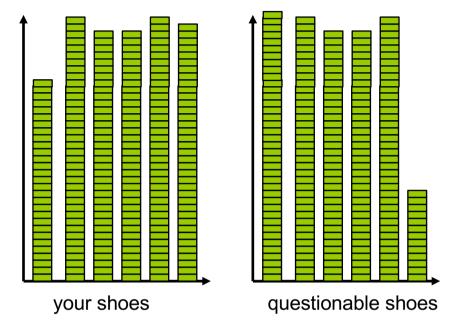


- [] this is probably still the original shoes
- [x] someone probably has replaced my shoes
- [x] could be the original or replacement shoes

#### <let's vote>



again, the distribution could have happened by chance, but it seems even more unlikely. This is probably not your shoes



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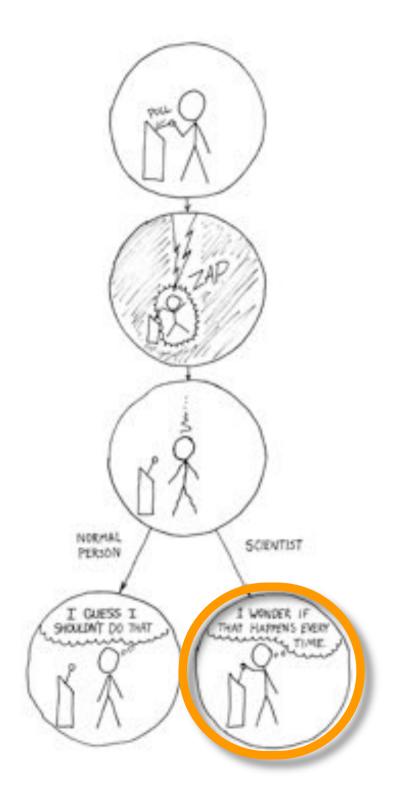
are you sure this it is not your shoes?

you are not sure.

what can you do to be sure?

there is **nothing** you can do, you can **never be sure** 

it is a limitation of science: no matter how often you pull the lever, it could always be chance



# the good news:

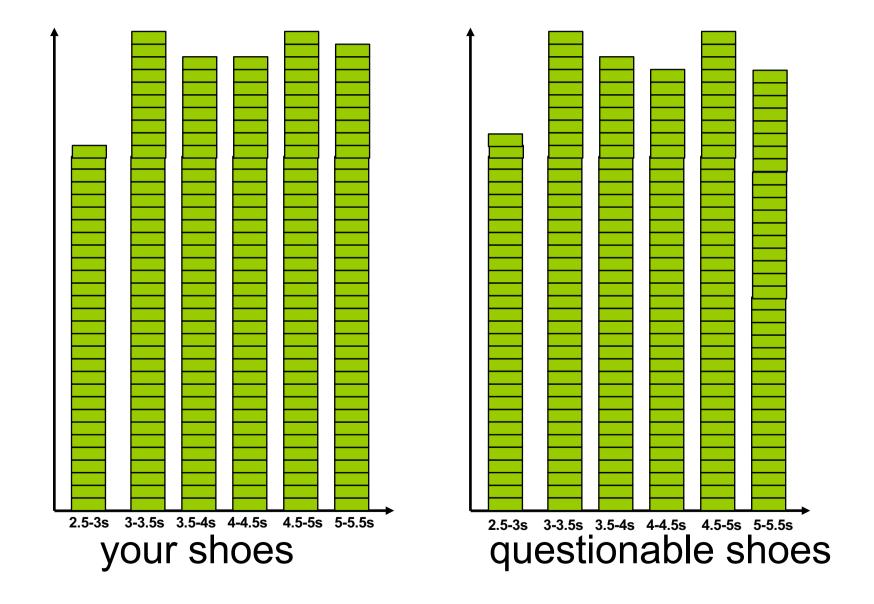
the more sample (# of runs), the more your confidence increases

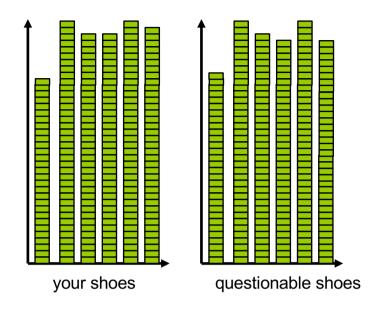
you can be arbitrarily sure

# another round

ok, you get your original shoes back

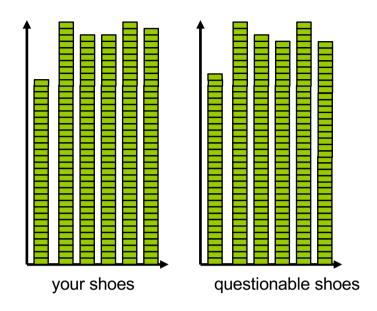
a week later the same thing happens again. again, you run 10 meters a few times with the questionable shoes ...



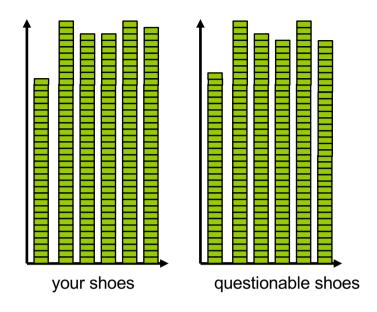


- [] this is still the original shoes
- [] someone has replaced my shoes
- [] could be the original or replacement shoes

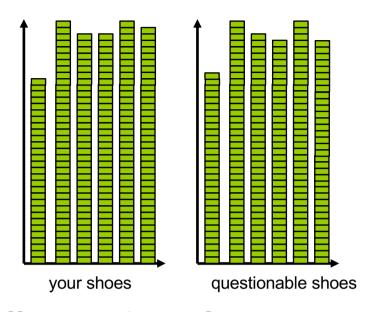
#### <let's vote>



- [] this is still the original shoes
- [] someone has replaced my shoes
- [x] could be the original or replacement shoes



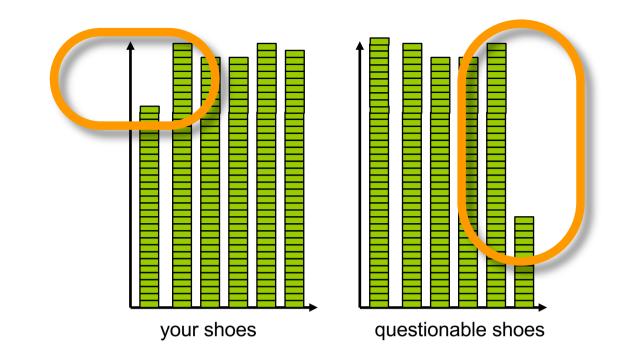
it could be your original shoes, or one that just happens to behave the same. a very, very, good copy maybe.



what are the odds of this being a different shoes?

you cannot compute the odds.

that's strange! why not?



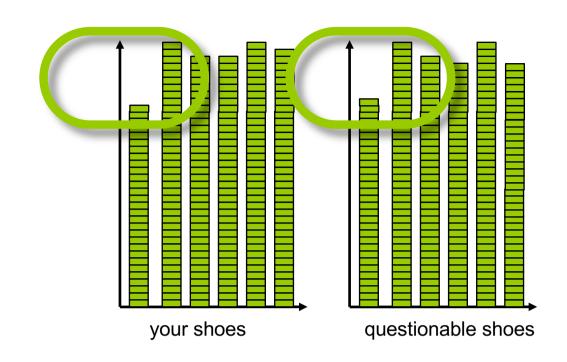
this seems unlikely...

in both cases, there are two explanations

- 1.same shoes •
- 2.different shoes

...thus this must be true

...now, in the other case



this does seem not unlikely...

in both cases, there are two explanations

- 1.same shoes
- 2.different shoes

we still have two possible explanations
→ we cannot conclude anything

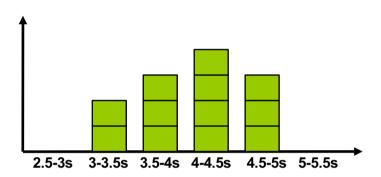
# let's use stats

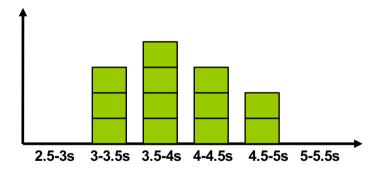
## statistical significance ::

a result is called statistically significant if it is unlikely to have occurred by chance

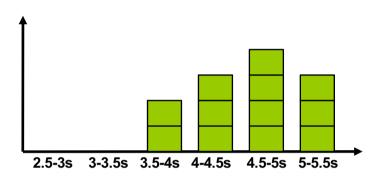
before I show you how to compute, let's test our intuition

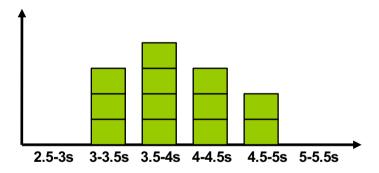
I show you pairs of distributions, you tell me if the differences are "statistically different"



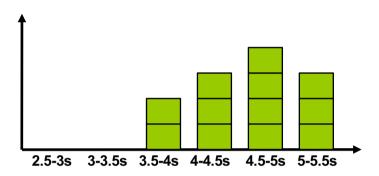


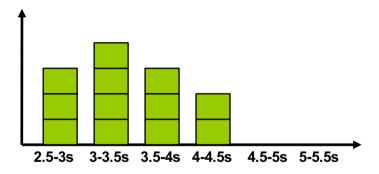
could have happened by chance (45% dissimilar)





still could have happened by chance (14% dissimilar)





unlikely to have happened by chance (0.1% dissimilar) rainstorming

### (student's) t-test return a <u>p-value</u>

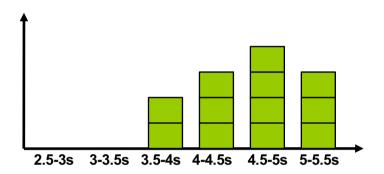
want to verify this: run a t-test

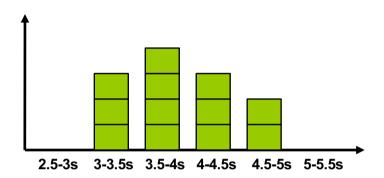
### significance level ::

If a test of significance gives a p-value lower than the significance level, such results are informally referred to as 'statistically significant'.

Popular levels of significance are 10% (0.1), 5% (0.05), 1% (0.01), 0.5% (0.005), and 0.1% (0.001).

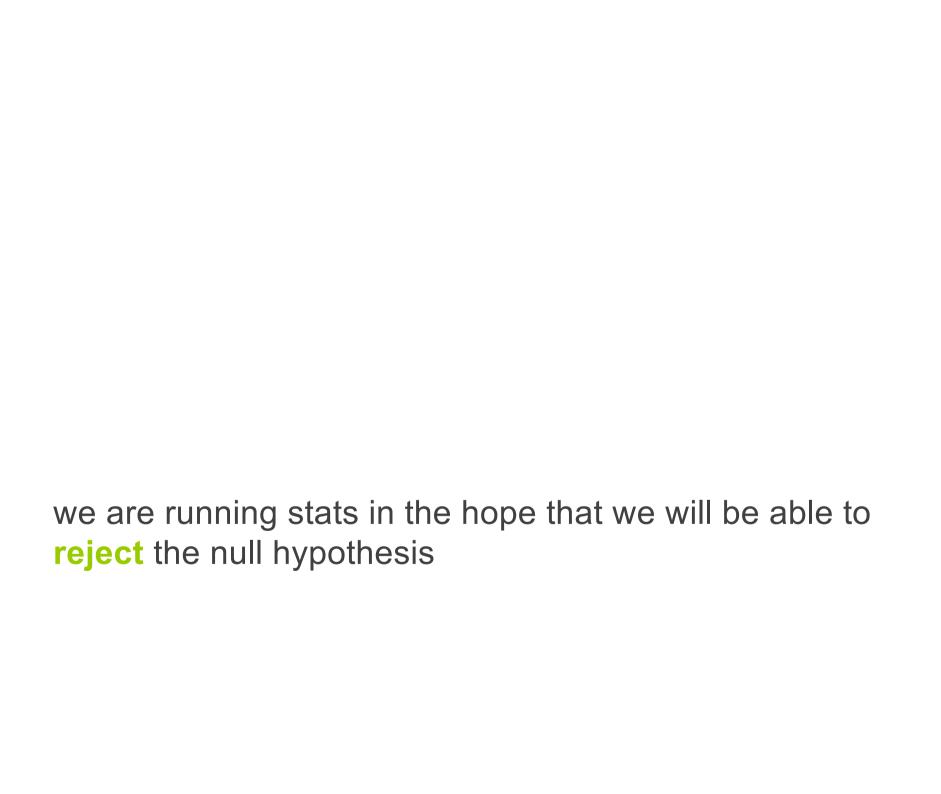
i.e., oddly, when we want to prove that they are different, we ask whether they are the same...





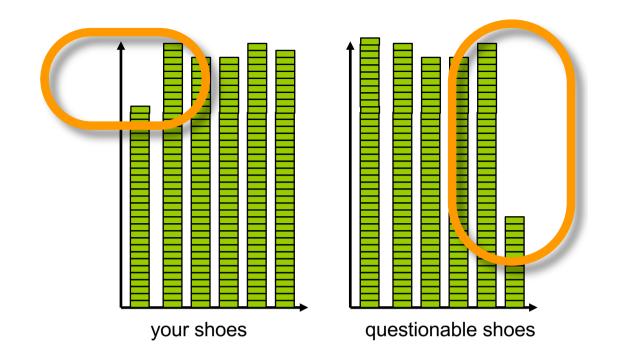
## **VS**

null hypothesis: both data sets are from same mechanism



→ if comparison of two groups reveals no statistically significant difference between the two, it does not mean that there is no difference in reality.

It only means that there is not enough evidence to reject the null hypothesis (it fails to reject the null hypothesis).



this seems unlikely...

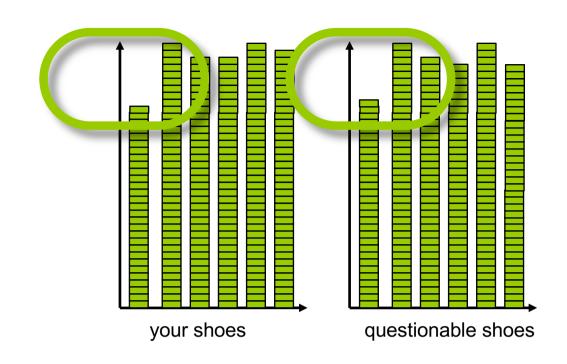
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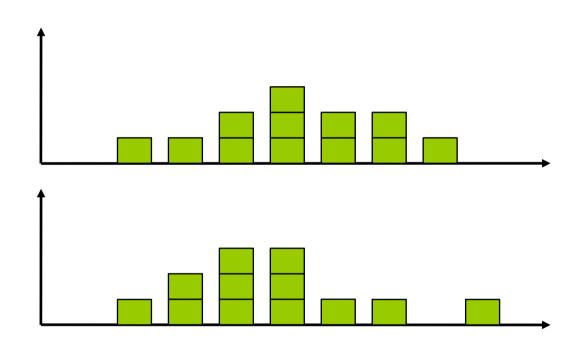
## a classic screw-ups

you are making a new input device. You know that it cannot be better than a mouse, but you want to show that it is as good as the mouse.

how do you proceed?

<30sec brainstorming

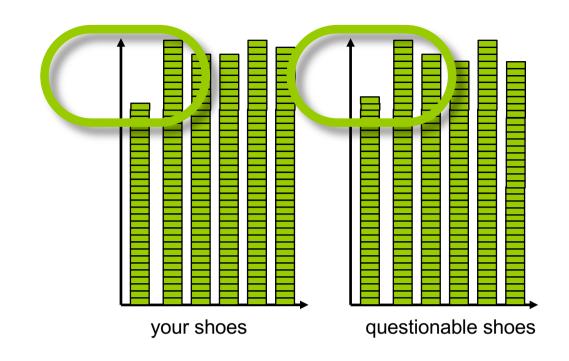
how about you run a test and if stats come out non-significant you write "our tests showed that there was no difference"?



#### nope!

significant difference → mechanisms different no significant difference → nothing

so how do you prove that two mechanisms are the same?



in both cases, there are two explanations

1.same shoes

2.different shoes

this does seem not unlikely...



you cannot

how to report non-significant results:

"our test did not find a significant difference"

## practically

you want to test the effect of two soporific drugs (independent variable) on amount of sleep(dependent variable). You take 10 participants and make then sleep to get their basic (control) sleep time. Then you give them drug 1 and note the difference of sleep time. You do the same for drug 2.

sleep extra drug 1	sleep extra drug 2
1 0.7	1 1.9
2 -1.6	2 0.8
3 -0.2	3 1.1
4 -1.2	4 0.1
5 -0.1	5 -0.1
6 3.4	6 4.4
7 3.7	7 5.5
8 0.8	8 1.6
9 0.0	9 4.6
10 2.0	10 3.4



#### in your terminal

head(sleep) # sleep is the table that already comes with R and contain 20 observations on 10 patients to show the effect of two soporific drugs on the increase in hours of sleep

```
plot(extra ~ group, data = sleep)
```

#### you then have two options for t-test: paired or unpaired

with(sleep, t.test(extra[group == 1], extra[group == 2]))#
unpaired

```
with(sleep, t.test(extra[group == 1], extra[group == 2],
paired = TRUE))# paired
```



you want to test the effect of two soporific drugs (independent variable) on amount of sleep(dependent variable). You take 10 participants and make then sleep to get their basic (control) sleep time. Then you give them drug 1 and note the difference of sleep time. You do the same for drug 2.

all participants did both conditions, i.e. had both drugs

= within subject experiment so the data is paired

otherwise (e.g. take 10 new participants for drug 2)

= between subject experiment so the data is unpaired

#### between subject experiment

with(sleep, t.test(extra[group == 1], extra[group == 2]))#
unpaired

```
data: extra[group == 1] and extra[group == 2]
t = -1.8608, df = 17.776, p-value = 0.07939
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval: -3.3654832  0.2054832
sample estimates: mean of x mean of y 0.75  2.33
```

#### what you would write

"An unpaired student t-test showed no significant difference between the two drugs."

#### within subject experiment



```
with(sleep, t.test(extra[group == 1], extra[group == 2],
paired = TRUE))# paired
```

```
data: extra[group == 1] and extra[group == 2]
t = -4.0621, df = 9 p-value = 0.002833
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval: -2.4598858 -0.7001142
sample estimates: mean of the differences -1.58
```

#### what you would write

"A paired student t-test showed significant difference between the two drugs (two-tailed t(9)=-4.0621, p < 0.05)"

(note: try to design your studies within-subject as it will increase the chance to reach a smaller p-value ... otherwise need twice more participants!)

#### one vs. two tail?



```
with(sleep, t.test(extra[group == 1], extra[group == 2],
paired = TRUE, alternative="less")) # or "greater"

Paired t-test

data: extra[group == 1] and extra[group == 2]
t = -4.0621 df = 9, p-value = 0.001416
alternative hypothesis: true difference in means is less than 0
95 percent confidence interval: -Inf -0.8669947
sample estimates: mean of the differences -1.58
```

#### what you would write

"A paired student t-test showed significant difference between the two drugs (one-tailed t(9)=-4.0621, p < 0.001)."

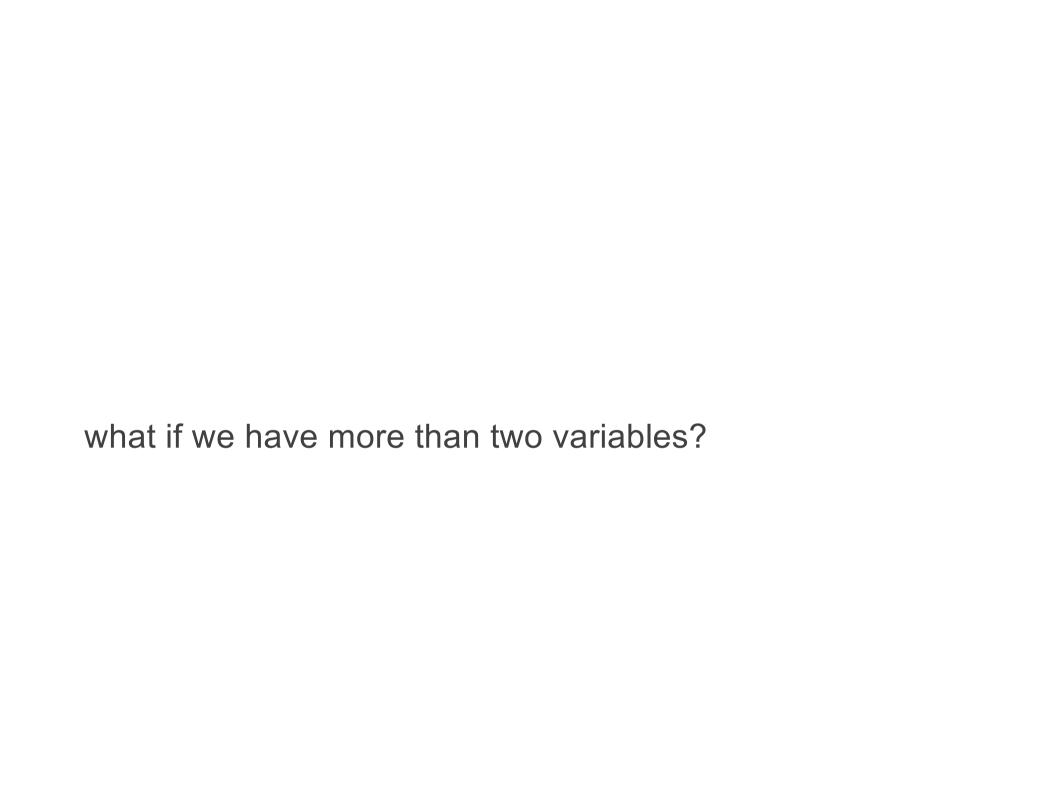
two-tails: effect of drug 1 is > and/or < Drug 2

```
one-tail: only one side of the effect, i.e.
effect of Drug 1 > Drug 2 (less)
or
effect of Drug 1 < Drug 2 (greater)
```

e.g. created a shampoo for hair loss and want to know if better than concurrent one

(note: you will mostly use two-tails but if you can use a one-tail do it, it will increase the chance to reach a smaller p-value!)

## multiple variables

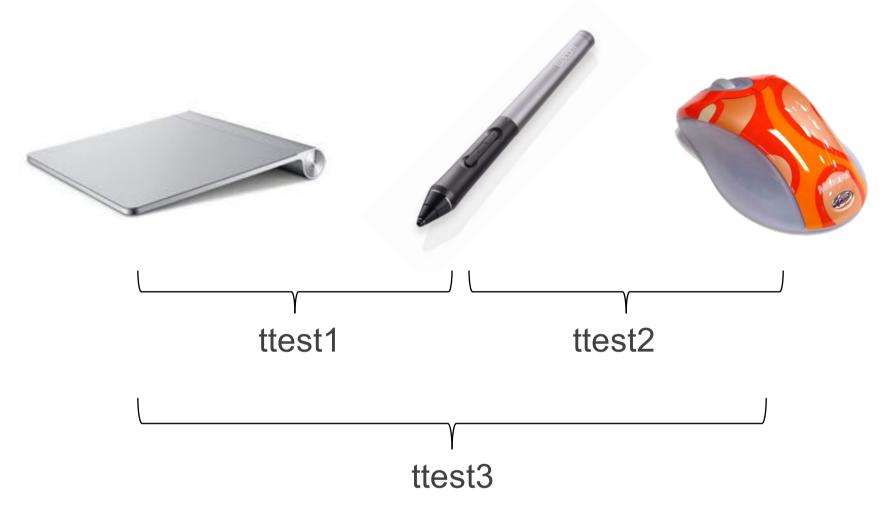




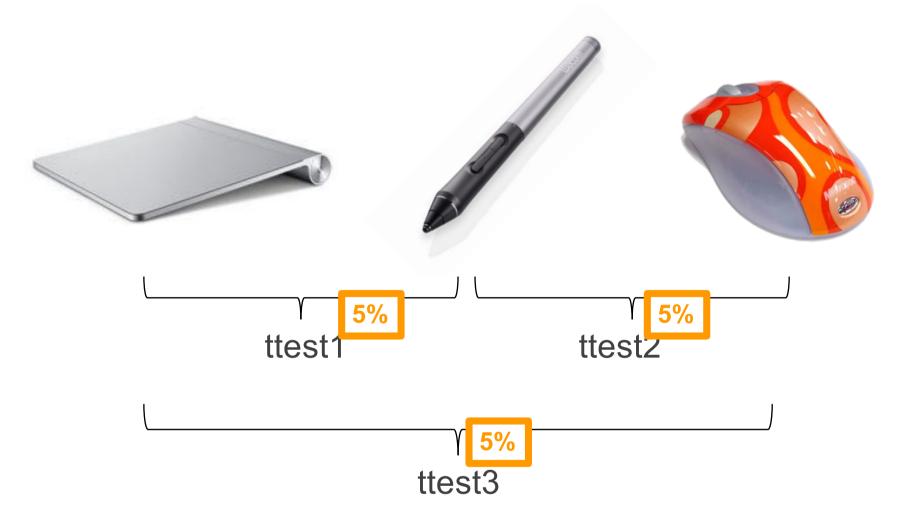
you are making two new input devices, a track pad and a stylus. You want to know which one is better and if they are also better than a mouse.

how do we proceed?

## <30sec brainstorming>

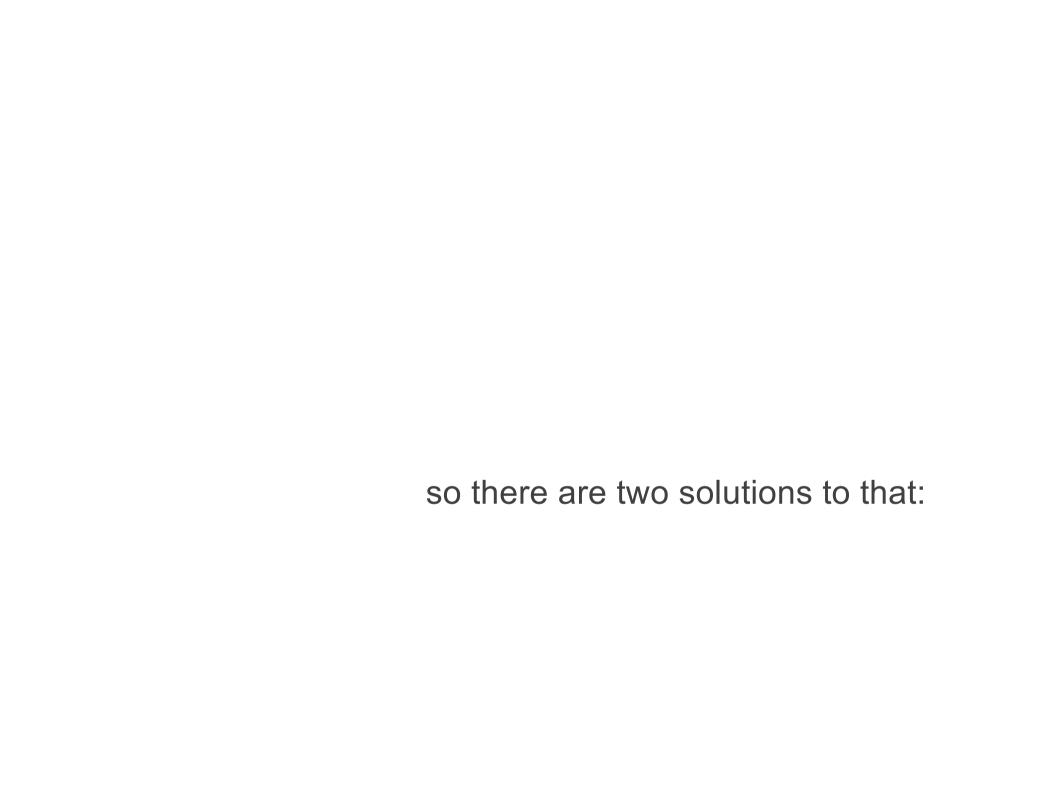


a simple solution would be to do this ...



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problem: any given test has a 5% chance of lying to you so when you use them multiple time you increase your risk of having errors (statisticians call this a "type I error")



### bonferroni correction ::

when testing *n* hypotheses, test each one against 0.05/n

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in our example we would need to use 0.05/3 as a significant threshold instead of 0.05

or you could also use an

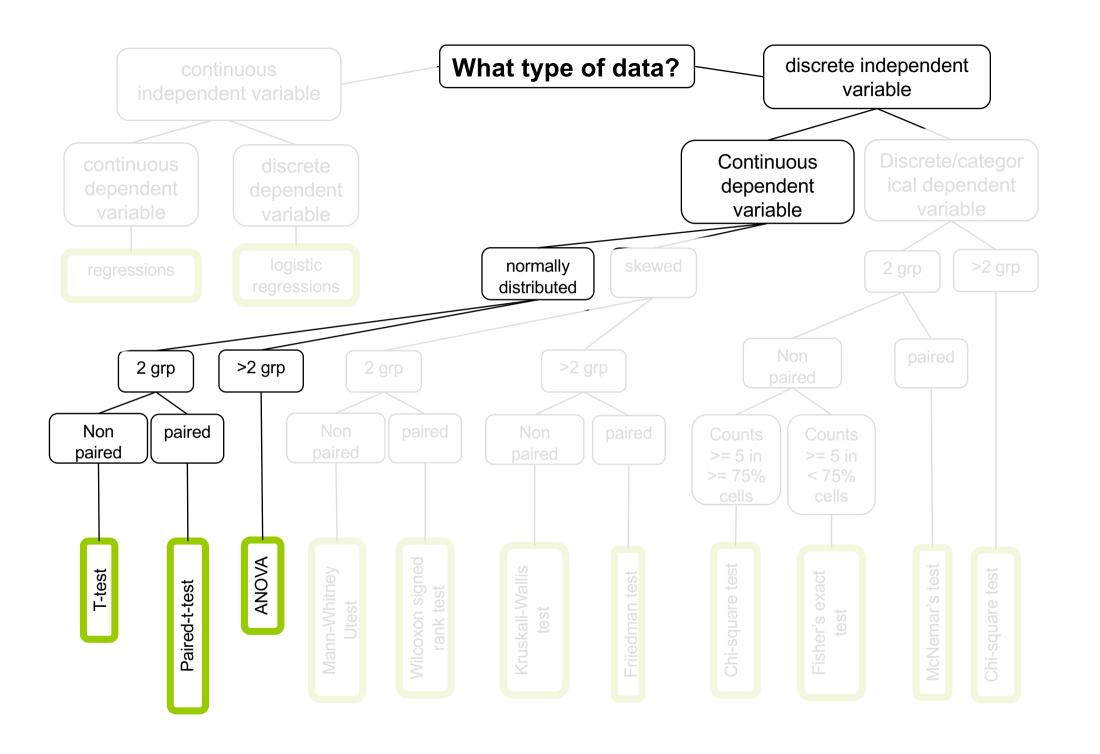
#### anova::

analyze of variance to compare multiple variables

one-way anova = one variable with multiple levels

two-way anova = two variables with multiple levels

we will look at ANOVA in the next few weeks



- 1. Explain what is hypothesis testing
- 2. Identify the limit of hypothesis testing (we cannot prove that things are similar)
- 3. Explain what is a p value and a significance value
- 4. Explain what is a t-test and when to use it
- 5. Explain the difference between within and between subject studies
- 6. Explain what is a Bonferroni correction and find the new significance level given an experimental design

## take away

#