



University of Michigan – Shanghai Jiao Tong University Joint Institute  
Center of Optics and Optoelectronics

## VE 320 – Summer 2012 Introduction to Semiconductor Device

### MOS Electrostatics

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**NANO ENERGY LAB**

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## BJT Analogy

Goal: Control output with small input

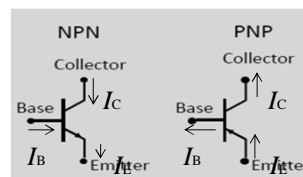
Analogy: Bump controls water flow



“Off”



“On”



Input controls bump height  
Output = water flow

### Electronics analogy

Water flow = electron or hole current

Bump = electronic potential



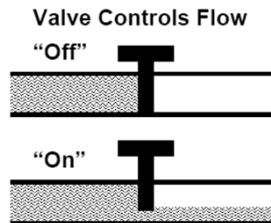
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## FET Analogy

Analogy: Valve controls water flow



- Input controls aperture
- Output = water flow

Electronics analogy

- Water flow = electron or hole current
- Valve = channel conductance controlled by electric field

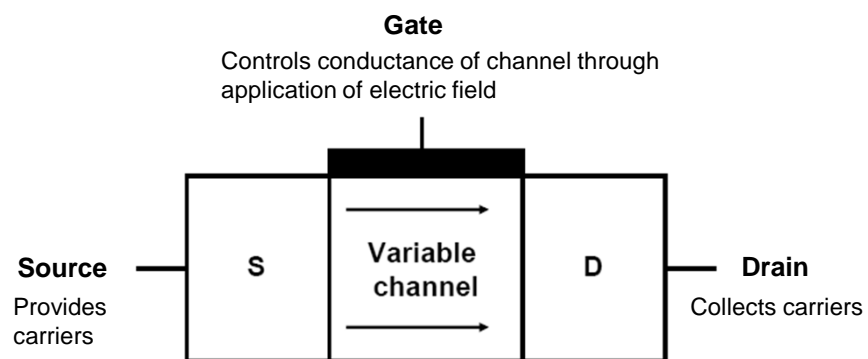


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## Field Effect Transistor



Control source to drain current with gate voltage



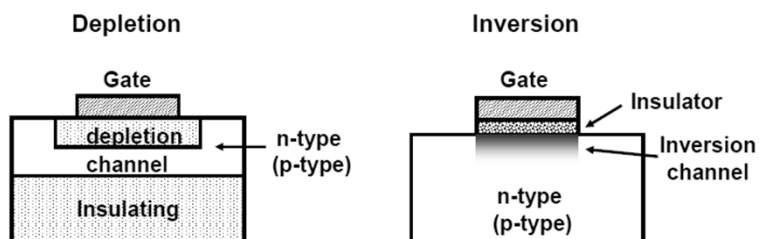
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## Gates For FETs

How do we control conductance of a channel?



- Field controls depletion width, channel depth
- Reverse-bias p-n (JFET)
- Reverse-bias Schottky (MESFET)
- Field inverts surface, controls surface charge density
- Metal-Insulator-Semiconductor (MISFET, MOSFET)

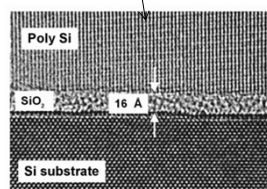
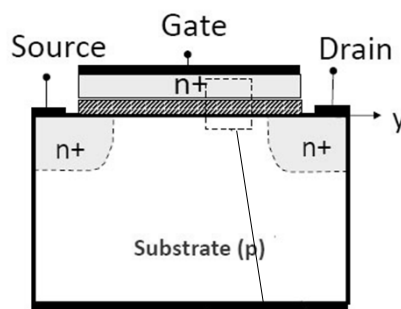
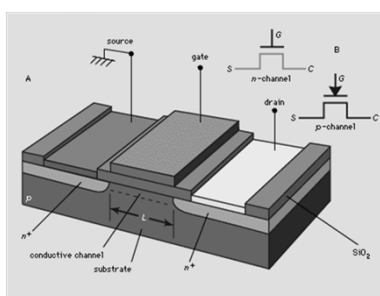


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## Basic Configuration of a MOSFET



Four terminal device.  
Almost like a lateral bipolar transistor!

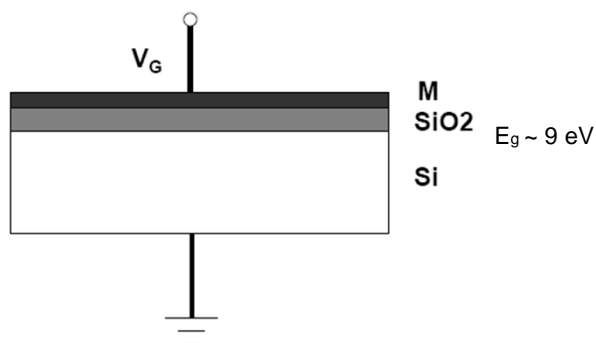


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## MOS Capacitor



In order to understand the operation of MOSFET, we need to understand MOS capacitor first.

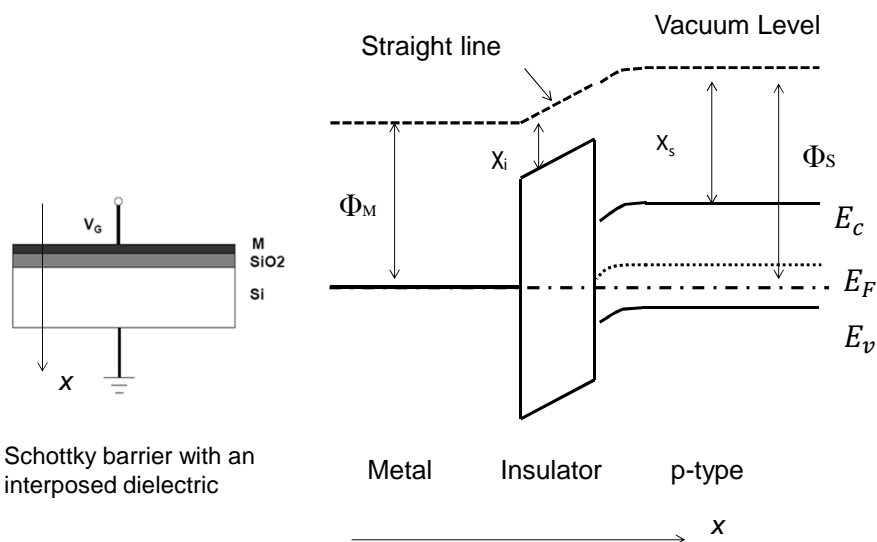


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## Electrostatics (Band Diagram)

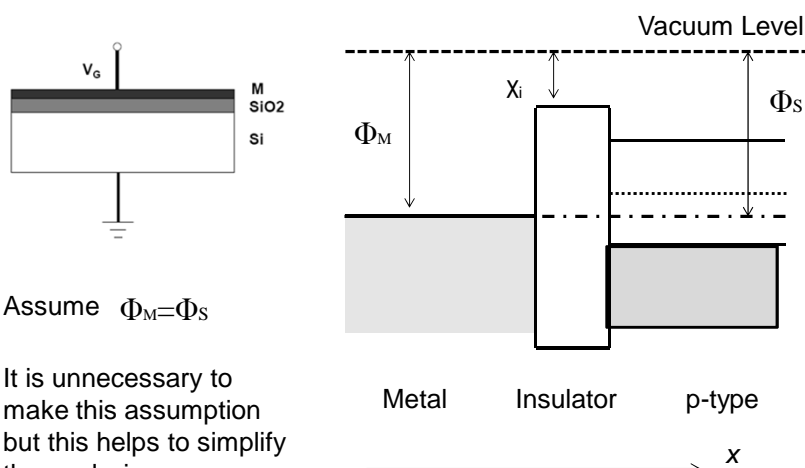


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## Idealized MOS Capacitor



Assume  $\Phi_M = \Phi_S$

It is unnecessary to make this assumption but this helps to simplify the analysis.

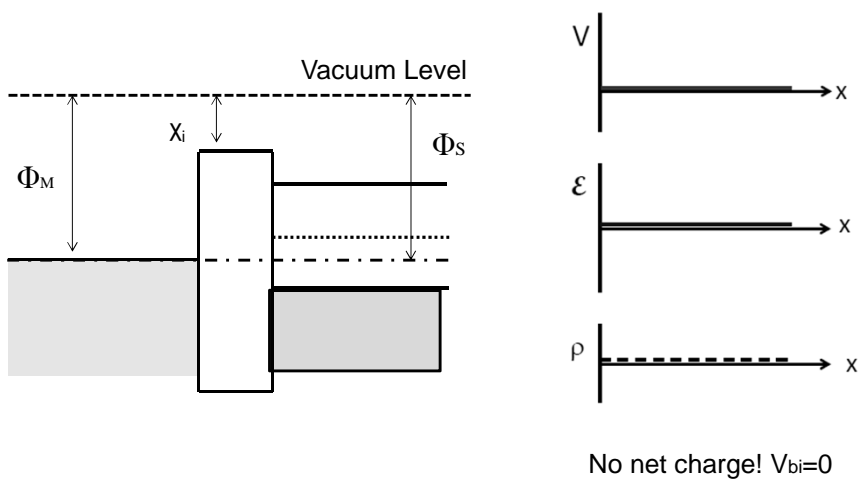


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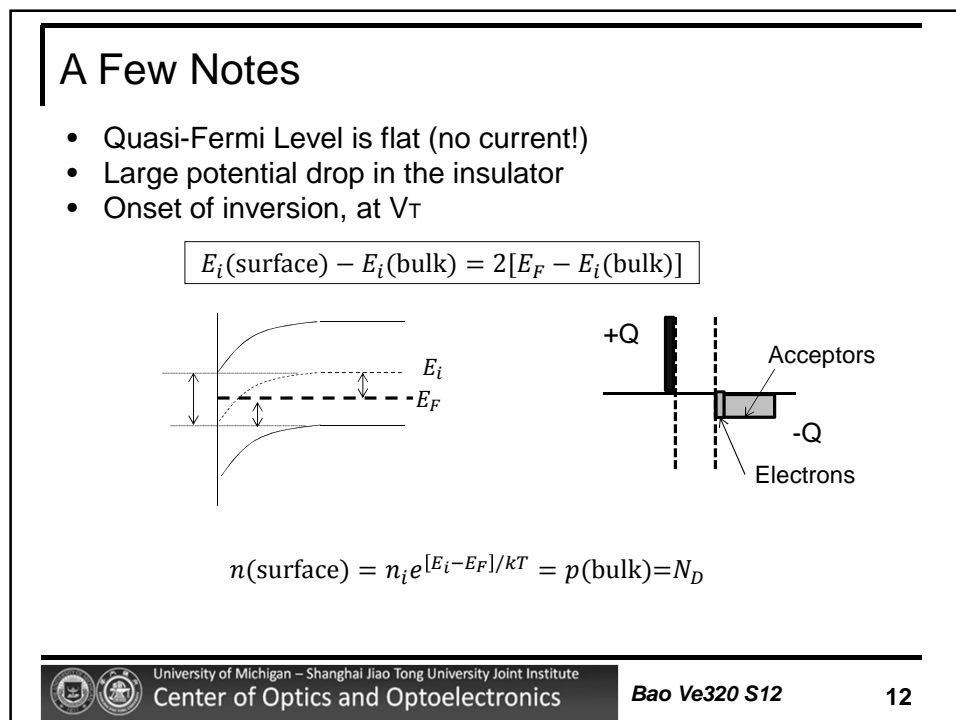
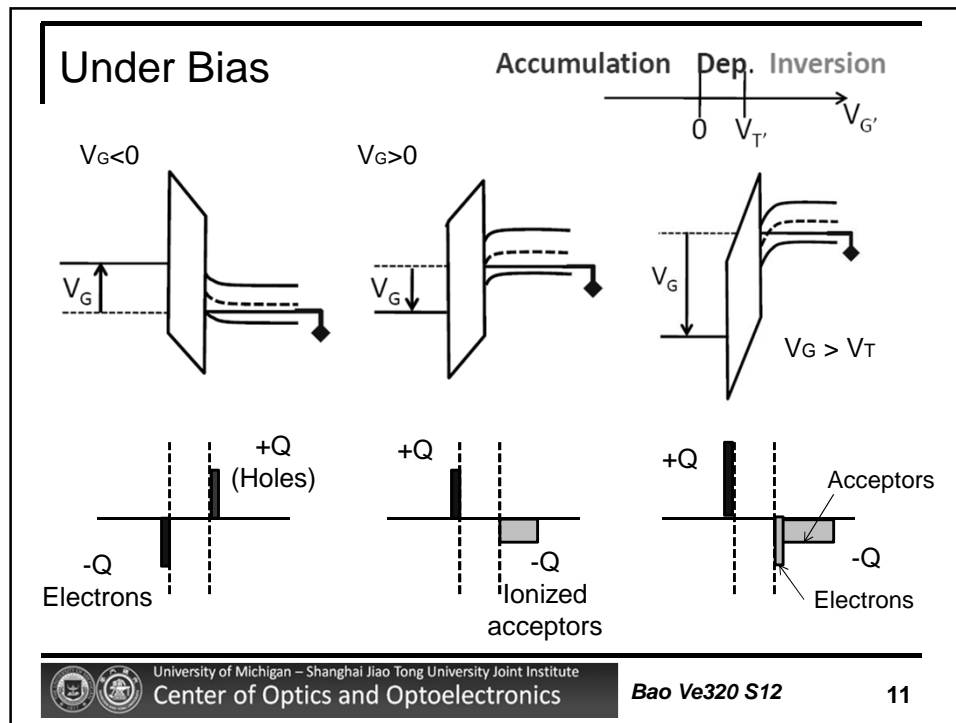
## Potential, Field, Charges



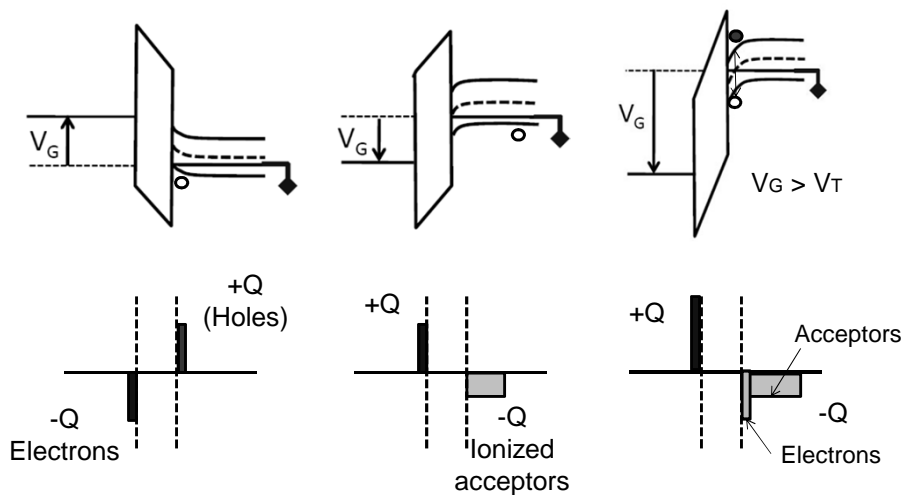
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## Where do charges come from?

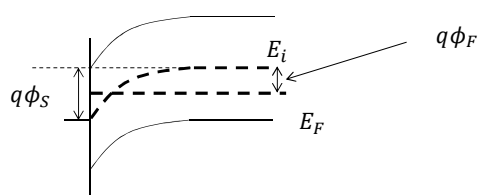


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## Before Quantitative Analysis...



$$\phi_s = \frac{1}{q} [E_i(\text{bulk}) - E_i(\text{surface})]$$

Surface potential  
not semiconductor  
workfunction

$$\phi_F = \frac{1}{q} [E_i(\text{bulk}) - E_F]$$

Potential related to doping



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## Inversion Condition

What is  $\phi_F$  for a given doping level?

**p-type Semiconductor**

$$\phi_F = \frac{kT}{q} \ln\left(\frac{N_A}{n_i}\right)$$

**n-type Semiconductor**

$$\phi_F = -\frac{kT}{q} \ln\left(\frac{N_D}{n_i}\right)$$

Inversion condition

$$\phi_S = 2\phi_F$$

Accumulation:  $\phi_S < 0$

Depletion:  $0 < \phi_S < 2\phi_F$

Inversion:  $\phi_S > 2\phi_F$

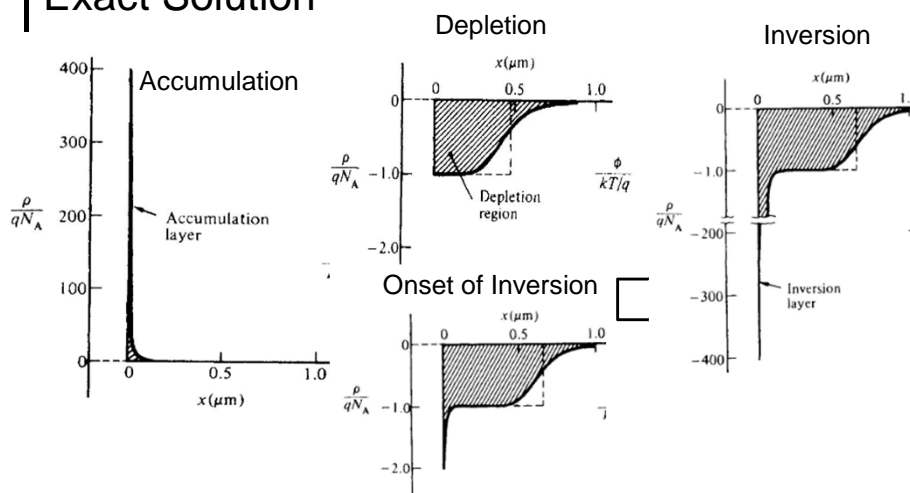


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## Exact Solution



We can invoke the depletion approximation. The mobile charges can be treated as a delta function.



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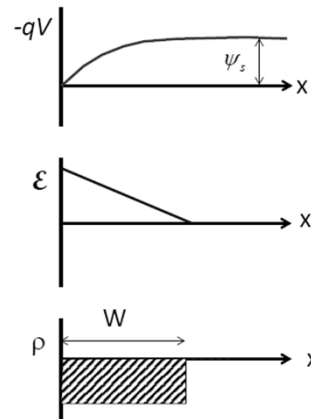
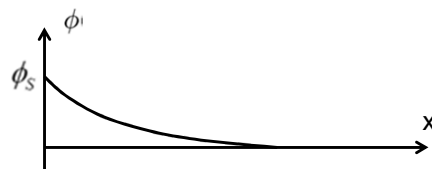


## (Depletion) Potential, Field, Charges

$$\rho = -qN_A$$

$$\mathcal{E}(x) = -\frac{d\phi}{dx} = \frac{qN_A}{K_S\epsilon_0}(W - x)$$

$$\phi(x) = \frac{qN_A}{2K_S\epsilon_0}(W - x)^2$$



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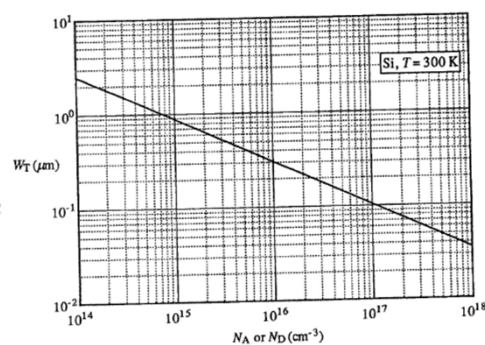
## Maximum Depletion Width

Depletion width changes slowly beyond inversion

$$W = \left[ \frac{2K_S\epsilon_0}{qN_A} \phi_s \right]^{1/2}$$

At inversion transition

$$W_T = \left[ \frac{2K_S\epsilon_0}{qN_A} (2\phi_F) \right]^{1/2}$$



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## Gate Voltage

Voltage drop  $V_G = \phi_S + V_{ox}$

No charge in the oxide  $\mathcal{E}_{ox} = \frac{K_S}{K_O} \mathcal{E}_S$

$V_G = \phi_S + \frac{K_S}{K_O} x_o \mathcal{E}_S$

$\mathcal{E}_S = \left[ \frac{2qN_A}{K_S \epsilon_0} \phi_S \right]^{1/2} \rightarrow V_G = \phi_S + \frac{K_S}{K_O} x_o \sqrt{\frac{2qN_A}{K_S \epsilon_0} \phi_S}$

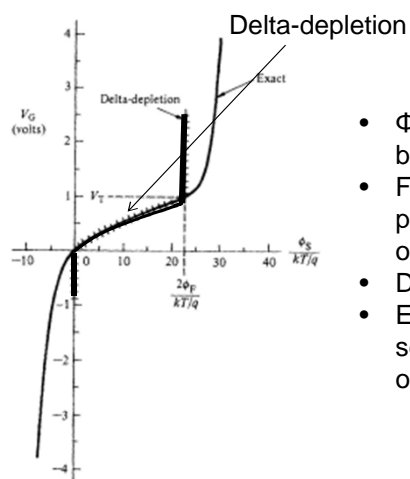


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## Exact Solution



- $\Phi_s$  changes with  $V_G$  in the depletion bias
- For accumulation and inversion, potential drop is mostly across the oxide layer
- Depletion bias is only 1 V in extent
- Electrical property of the semiconductor changes drastically over a narrow range of voltages.



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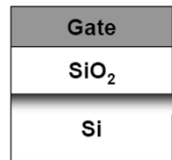
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## C-V Characteristics

MOS: 2 capacitors in series

- Oxide capacitance
- Semiconductor capacitance

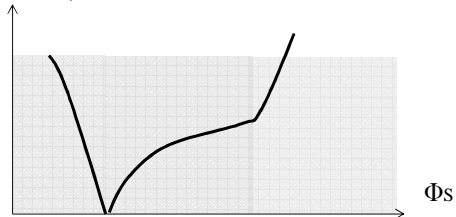


$$C = \frac{C_O C_S}{C_O + C_S}$$

$$C_O = \frac{K_O \epsilon_0 A_G}{x_o}$$

$$C_S = \frac{K_S \epsilon_0 A_G}{W}$$

$Q_s$  (log scale)



accumulation Depletion Inversion

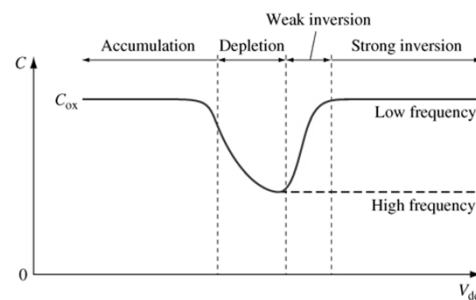
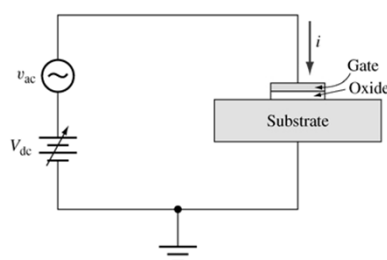


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## Capacitance



Accumulation: majority carrier response very fast to applied bias  
Inversion: the R-G of minority carriers are slower

$$C = \begin{matrix} C_O & \frac{C_O}{1 + \frac{K_O W}{K_S x_o}} & C_O & \frac{C_O}{1 + \frac{K_O W_T}{K_S x_o}} \\ \text{acc} & \text{depl} & \text{Inv (low f)} & \text{Inv (high f)} \end{matrix}$$



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## Depletion

With depletion bias,  $C$  is a function of  $W$ .

$$C = \frac{C_O}{1 + \frac{K_O W}{K_S x_o}}$$

It should be expressed in terms of  $V_G$

$$W = \frac{K_S}{K_O} x_o \left[ \sqrt{1 + \frac{V_G}{V_\delta}} - 1 \right]$$

$$V_\delta = \frac{q K_S x_o^2}{2 K_O^2 \epsilon_0} N_A$$

$$C = \frac{C_O}{\sqrt{1 + V_G/V_\delta}} \quad (\text{depletion bias})$$

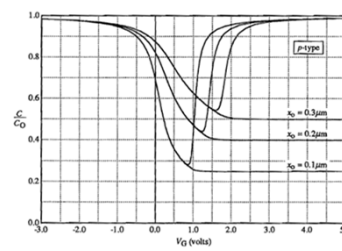
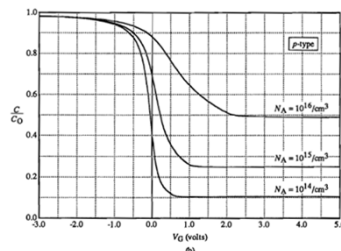
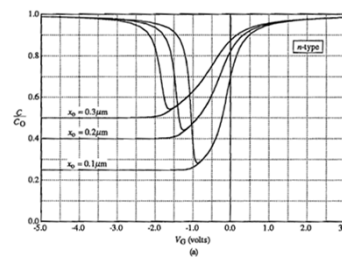
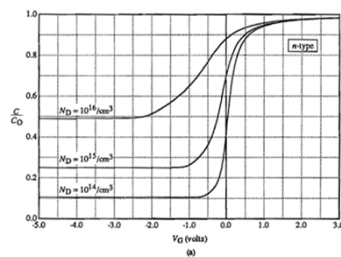


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## Doping and Oxide Thickness



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