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Center of Optics and Optoelectronics

VE 320 – Summer 2012 Introduction to Semiconductor Device

Schottky Diode

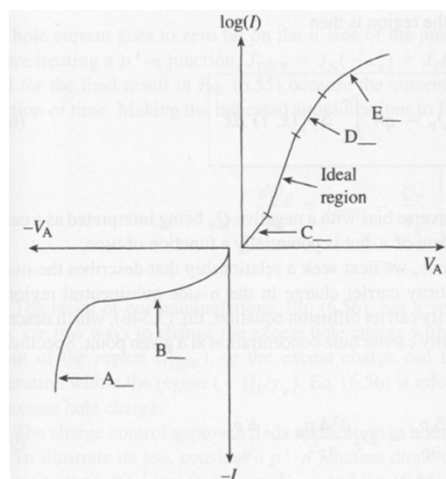
Instructor: Professor Hua Bao

NANO ENERGY LAB

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PN Junction Diode, non-ideal



1. Photogeneration
2. Thermal recombination in the depletion region
3. Avalanching and/or Zener process
4. Low-level injection
5. Depletion approximation
6. Thermal generation in the depletion region
7. Band bending
8. Series resistance
9. $V_A > V_{bi}$
10. High-level injection

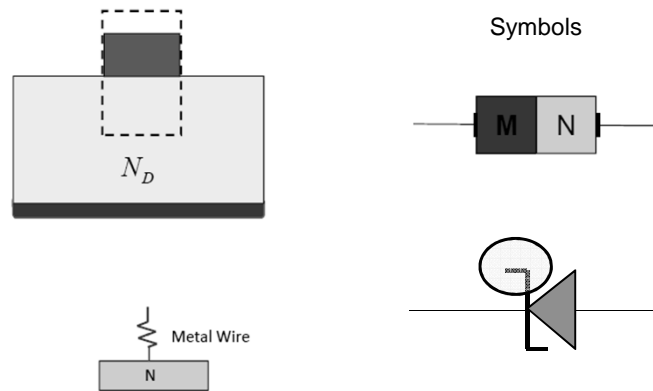


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Metal-semiconductor Diode



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Electrostatic and DC

$$\nabla \cdot \mathbf{D} = q(p - n + N_D^+ - N_A^-) \longrightarrow \text{Electrostatic}$$

$$\frac{\partial n}{\partial t} = \frac{1}{q} \nabla \cdot \mathbf{J}_N - r_N + g_N$$

$$\mathbf{J}_N = qn\mu_N\mathcal{E} + qD_N\nabla n$$

$$\frac{\partial p}{\partial t} = -\frac{1}{q} \nabla \cdot \mathbf{J}_P - r_P + g_P$$

$$\mathbf{J}_P = qp\mu_P\mathcal{E} - qD_P\nabla p$$

DC/AC/Transient

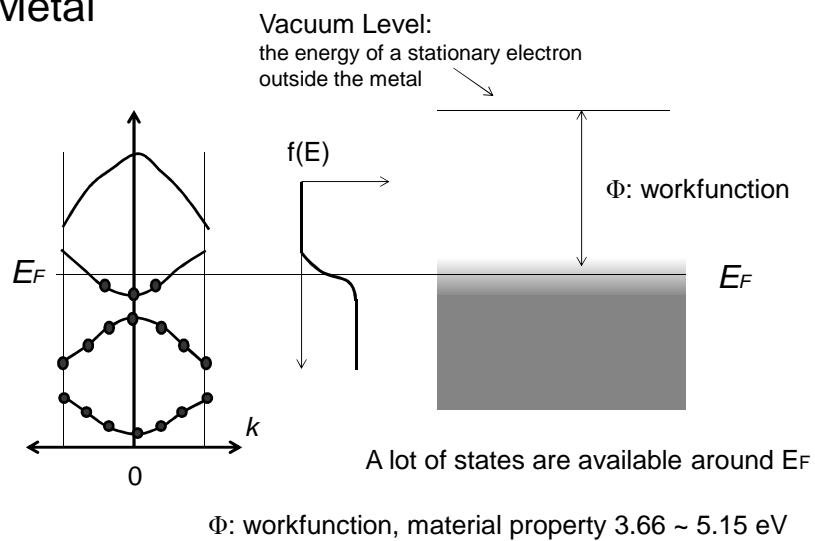


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Metal

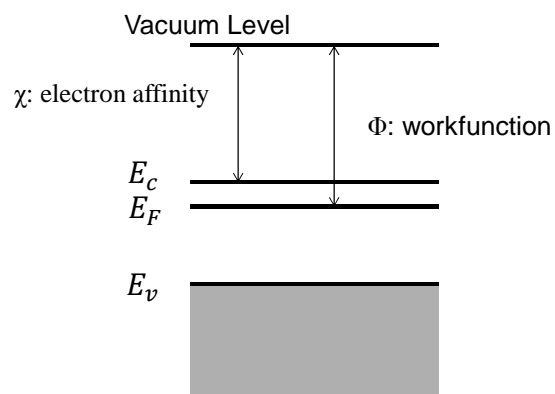


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Semiconductor



χ : electron affinity is a material property. 4.03 eV for silicon.
Workfunction of semiconductor depends on doping level

$$\Phi_S = \chi + (E_c - E_F)$$

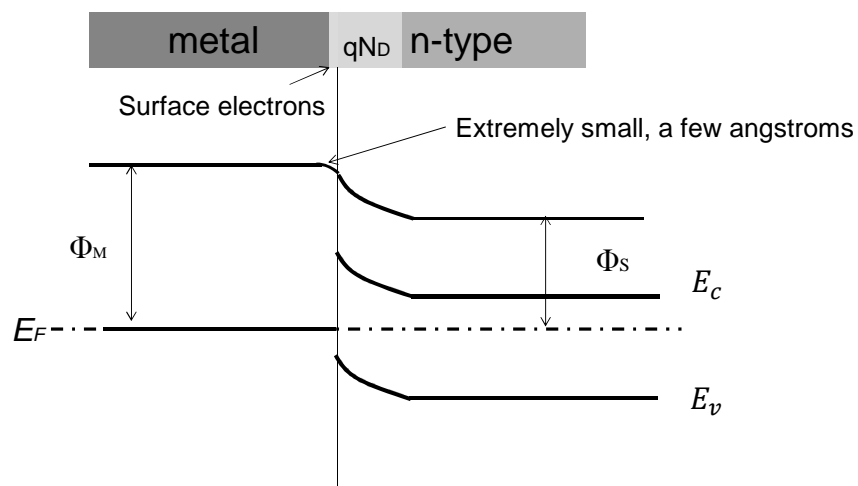


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Form a Diode/Band Diagram

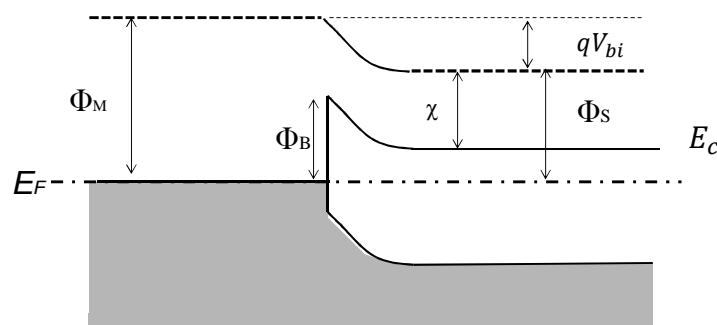


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Band Diagram



$$\Phi_B = \Phi_M - \chi$$

$$V_{bi} = \frac{1}{q} [\Phi_B - (E_c - E_F)_{FB}]$$

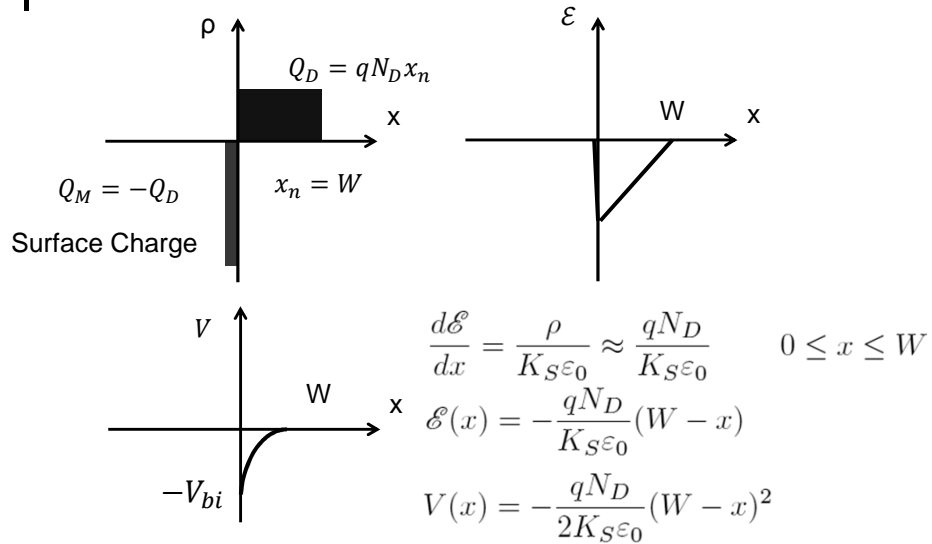


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Analytical Solution

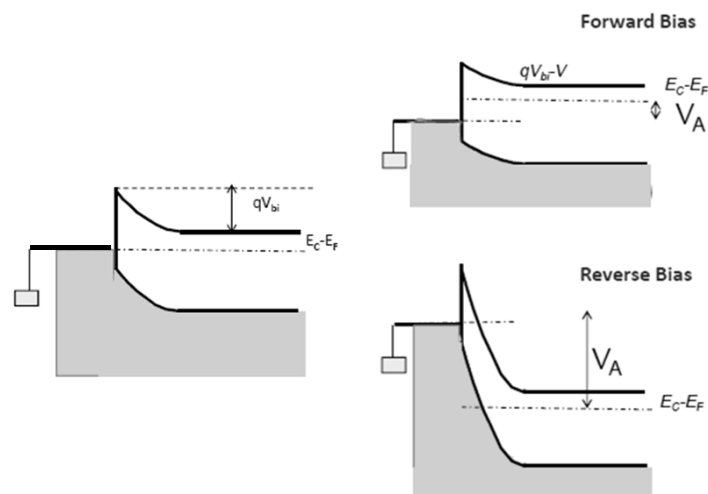


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Band Diagram with Bias



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Depletion Width



Depletion width varies with the applied potential V_A

$$-(V_{bi} - V_A) = -\frac{qN_D}{2K_S\epsilon_0} W^2$$

$$W = \left[\frac{2K_S\epsilon_0}{qN_D} (V_{bi} - V_A) \right]^{1/2}$$

This solution is similar to a $p^+ - n$ junction

$$W = \sqrt{\frac{2K_S\epsilon_0}{q} \left(\frac{N_A + N_D}{N_A N_D} \right) (V_{bi} - V_A)}$$

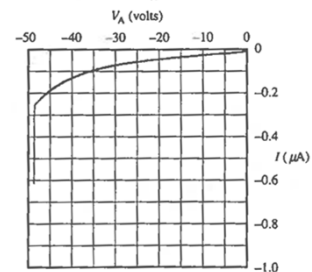
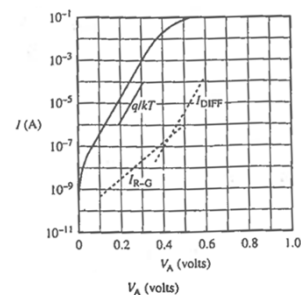
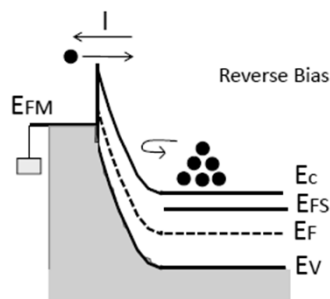
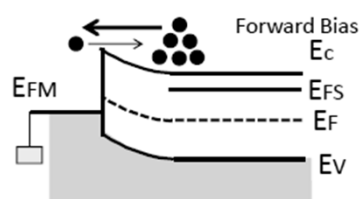


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I-V Characteristics

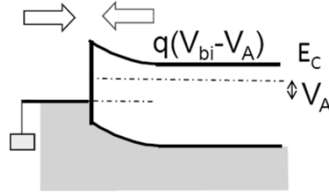


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Simple Approach



$$J_T(V_A) = J_{m \rightarrow s}(V_A) - J_{s \rightarrow m}(V_A)$$

$$= J_{m \rightarrow s}(0) - J_{s \rightarrow m}(V_A)$$

$$J_T(V_A = 0) = 0 = J_{m \rightarrow s}(0) - J_{s \rightarrow m}(0) \quad (\text{detailed balance})$$

$$\Rightarrow J_{m \rightarrow s}(0) = J_{s \rightarrow m}(0)$$

$$J_T(V_A) = J_{s \rightarrow m}(0) - J_{s \rightarrow m}(V_A)$$



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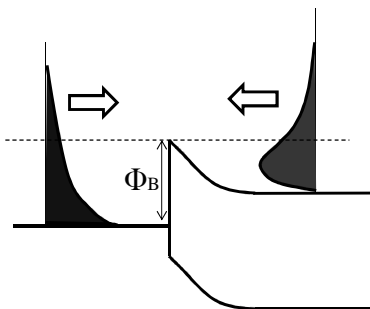
Semiconductor to Metal Flux

$$J_{m \rightarrow s}(V_A) = -q \frac{n_m}{2} e^{-\frac{q\Phi_B}{kT}} v_{th}$$

$$J_{s \rightarrow m}(V_A) = -q \frac{n_s}{2} e^{-\frac{q(V_{bi} - V_A)}{kT}} v_{th}$$

$$= -q \frac{n_s v_{th}}{2} e^{-\frac{qV_{bi}}{kT}} \times e^{\frac{qV_A}{kT}}$$

$$= -q \frac{n_m v_{th}}{2} e^{-\frac{q\Phi_B}{kT}} e^{\frac{qV_A}{kT}}$$



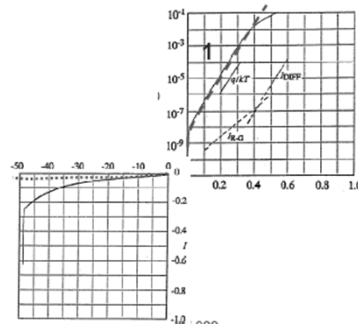
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Total Flux

$$J_T = J_{s \rightarrow m}(0) - J_{s \rightarrow m}(V_A) = \frac{qn_m v_{th}}{2} e^{\frac{-q\Phi_m}{kT}} \left[e^{\frac{qV_A}{kT}} - 1 \right]$$

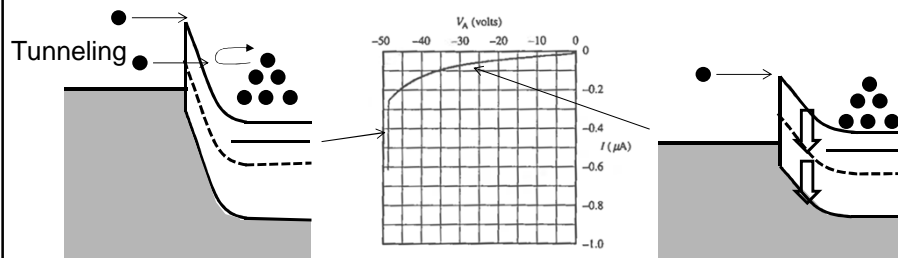
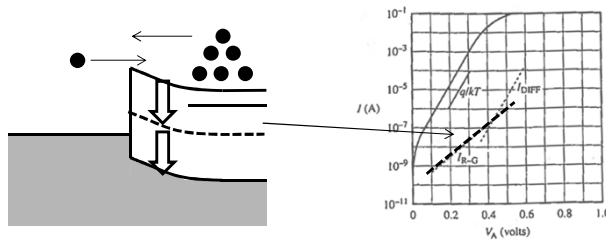


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Recombination/Generation/Impact-ionization

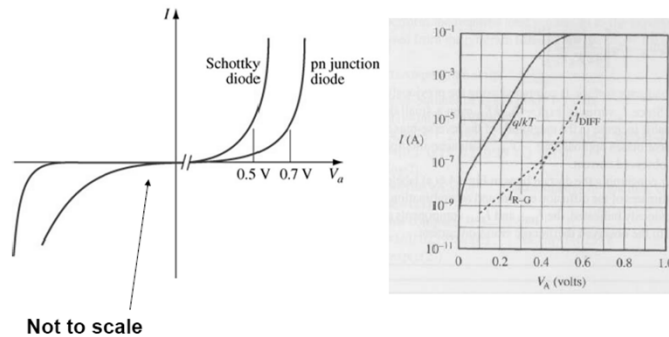


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Comparing to PN Junction Diode



- smaller V_{bi}
- faster in charging/discharging during transient as no accumulation of minority carrier necessary
- no high-level injection problem
- ideality factor close to 1 (ideal case)
- lower breakdown voltage



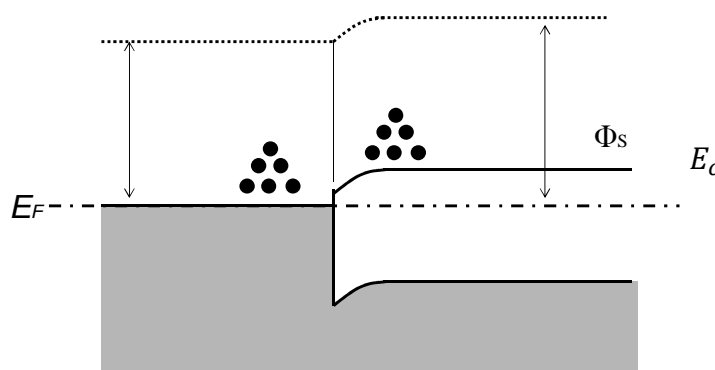
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Ohmic Contact

We have assumed $\Phi_M > \Phi_S$, what happens if $\Phi_M < \Phi_S$



No barrier from semiconductor to metal.
Small barrier vanishes with even relatively small reverse bias.
This is non-rectifying or ohmic-like.



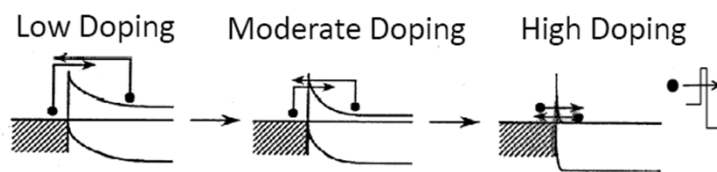
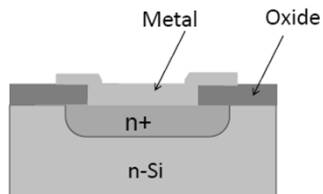
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Tunneling Ohmic Contacts

$$\Phi_M > \Phi_S$$



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Summary

- M-S contact can be rectifying or ohmic-like.
- M-S diode electrostatics is similar to a p-n junction diode with one-side heavy doping.



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