Data Analysis with augmentedRCBD

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Contents

2 R software	2
3 Getting Started	3
3.1 Installing R	3
3.2 Installing RStudio	3
3.3 The RStudio Interface	4
3.3.1 Console	5
3.3.2 Source	5
3.3.3 Environment History Connections	5
$3.3.4 \; \mathrm{Files} \mathrm{Plots} \mathrm{Packages} \mathrm{Help} \mathrm{Viewer} \;\; \ldots \;\;$	6
4 Some Basics	6
4.1 Working Directory	6
4.2 Expression and Assignment	6
4.3 Objects and Functions	7
4.3.1 Vector	
4.3.2 Factor	8
4.3.3 Matrix	10
4.3.4 List	10
4.3.5 Data Frame	11
4.3.6 Functions	11
4.4 Special Elements	12
4.5 Indexing	13
4.6 Help Documentation	15
4.7 Packages	15
4.8 Importing and Exporting Tabular Data	16
4.9 Additional Resources	17
5 Installation of augmentedRCBD	17
6 Data Format	18

7 Data Analysis for a Single Trait	20
7.1 augmentedRCBD()	21
7.2 print.augmentedRCBD()	32
7.3 describe.augmentedRCBD()	36
7.4 freqdist.augmentedRCBD()	37
7.5 gva.augmentedRCBD()	43
7.5 report.augmentedRCBD()	45
8 Data Analysis for a Multiple Traits	46
8.1 augmentedRCBD.bulk()	47
8.2 print.augmentedRCBD.bulk()	50
8.3 report.augmentedRCBD.bulk()	52
9 Citing augmentedRCBD	53
10 Session Info	54
References	54

1 Overview

The software augmentedRCBD is built on the R statistical programming language as an add-on (or 'package' in the R lingua franca). It performs the analysis of data generated from experiments in augmented randomised complete block design according to Federer, W.T. (1956, 1961). It also computes analysis of variance, adjusted means, descriptive statistics, genetic variability statistics etc. and includes options for data visualization and report generation.

This tutorial aims to educate the users in utilising this package for performing such analysis. Utilising augmentedRCBD for data analysis requires a basic knowledge of R programming language. However, as many of the intended end-users may not be familiar with R, sections 2 to 4 give a 'gentle' introduction to R, especially those aspects which are necessary to get augmentedRCBD up and running for performing data analysis in a Windows environment. Users already familiar with R can feel free to skip to section 5.



2 R software

It is a free software environment for statistical computing and graphics. It is free and open source, platform independent (works on Linux, Windows or MacOS), very flexible, comprehensive with robust interfaces for all the popular programming languages as well as databases. It is strengthened by its diverse library of



add-on packages extending its ability as well as the incredible community support. It is one of the most popular tools being used in academia today (Tippmann, 2015).

3 Getting Started

This section details the steps required to set up the R programming environment under a third-party interface called RStudio in Windows.

3.1 Installing R

New features in this version

Download and install R for Windows from http://cran.r-project.org/bin/windows/base/.

R-3.5.1 for Windows (32/64 bit)

Download R 3.5.1 for Windows (62 megabytes, 32/64 bit)

Installation and other instructions

If you want to double-check that the package you have downloaded matches the package distributed by CRAN, you can compare the md5sum of the .exe to the fingerprint on the master server. You will need a version of md5sum for windows: both graphical and command line versions are available.

Frequently asked questions

- Does R run under my version of Windows?
- How do I update packages in my previous version of R?
- Should I run 32-bit or 64-bit R?

Please see the RFAQ for general information about R and the RWindows FAQ for Windows-specific information

Other builds

- Patches to this release are incorporated in the <u>r-patched snapshot build</u>.
- A build of the development version (which will eventually become the next major release of R) is available in the r-devel snapshot build.
- Previous releases

Note to webmasters: A stable link which will redirect to the current Windows binary release is <cre>CRAN MIRROR>/bin/windows/base/release.htm.

Last change: 2018-07-02

Fig. 1: The R download location.

3.2 Installing RStudio

The basic command line interface in native R is rather limiting. There are several interfaces which enhance it's functionality and ease of use, RStudio being one of the most popular among R programmers.

 $Download\ and\ install\ RStudio\ for\ Windows\ from\ https://www.rstudio.com/products/rstudio/download/\ \#download$

Installers for Supported Platforms

Installers	Size	Date	MD5
RStudio 1.1.456 - Windows Vista/7/8/10	85.8 MB	2018-07-19	24ca3fe0dad8187aabd4bfbb9dc2b5ad
RStudio 1.1.456 - Mac OS X 10.6+ (64-bit)	74.5 MB	2018-07-19	4fc4f4f70845b142bf96dc1a5b1dc556
RStudio 1.1.456 - Ubuntu 12.04-15.10/Debian 8 (32-bit)	89.3 MB	2018-07-19	3493f9d5839e3a3d697f40b7bb1ce961
RStudio 1.1.456 - Ubuntu 12.04-15.10/Debian 8 (64-bit)	97.4 MB	2018-07-19	863ae806120358fa0146e4d14cd75be4
RStudio 1.1.456 - Ubuntu 16.04+/Debian 9+ (64-bit)	64.9 MB	2018-07-19	d96e63548c2add890bac633bdb883f32
RStudio 1.1.456 - Fedora 19+/RedHat 7+/openSUSE 13.1+ (32-bit)	88.1 MB	2018-07-19	1df56c7cd80e2634f8a9fdd11ca1fb2d
RStudio 1.1.456 - Fedora 19+/RedHat 7+/openSUSE 13.1+ (64-bit)	90.6 MB	2018-07-19	5e77094a88fdbddddddd0d35708752462

Zip/Tarballs

Zip/tar archives	Size	Date	MD5
RStudio 1.1.456 - Windows Vista/7/8/10	122.9 MB	2018-07-19	659d6bfe716d8c97acbe501270d89fa3
RStudio 1.1.456 - Ubuntu 12.04-15.10/Debian 8 (32-bit)	90 MB	2018-07-19	63117c159deca4d01221a8069bd45373
RStudio 1.1.456 - Ubuntu 12.04-15.10/Debian 8 (64-bit)	98.3 MB	2018-07-19	c53c32a71a400c6571e36c573f83dfde
RStudio 1.1.456 - Fedora 19+/RedHat 7+/openSUSE 13.1+ (32-bit)	88.8 MB	2018-07-19	f4ba2509fb00e30c91414c6821f1c85f
RStudio 1.1.456 - Fedora 19+/RedHat 7+/openSUSE 13.1+ (64-bit)	91.4 MB	2018-07-19	c60db6467421aa86c772227da0945a13

Source Code

A tarball containing source code for RStudio v1.1.456 can be downloaded from here

Fig. 2: The RStudio download location.

3.3 The RStudio Interface

On opening RStudio, the default interface with four panes/windows is visible as follows. Few panes have different tabs.

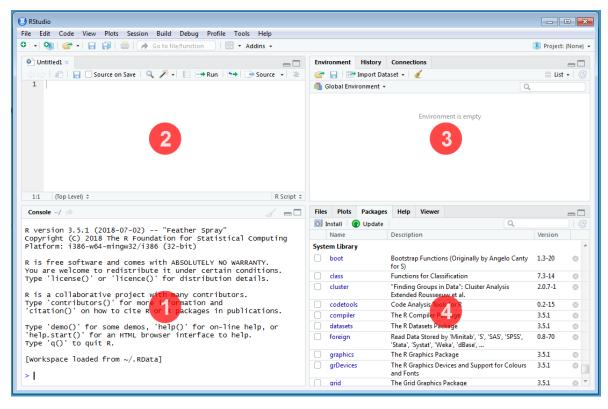


Fig. 3: The default RStudio interface with the four panes.

3.3.1 Console

This is where the action happens. Here any authentic R code typed after the '>' prompt will be executed after pressing 'Enter' to generate the output.

For example, type 1+1 in the console and press 'Enter'.

1+1

[1] 2

3.3.2 Source

This is where R Scripts (collection of code) can be created and edited. R scripts are text files with a .R extension. R Code for analysis can be typed and saved in such R scripts. New scripts can be opened by clicking 'File|New File' and selecting 'R Script'. Code can be selected from R Scripts and sent to console for evaluation by clicking 'Run' on the 'Source' pane or by pressing 'Ctrl + Enter'.

3.3.3 Environment|History|Connections

The 'Environment' tab shows the list of all the 'objects' (see section 4.3) defined in the current R session. It has also some buttons up top to open, save and clear the environment as well as few options for import of data under Import Dataset.

The 'History' tab shows a history of all the code that was previously evaluated. This is useful, if you want to go back to some code.

The 'Connections' tab helps to establish and manage connections with different databases and data sources.

3.3.4 Files|Plots|Packages|Help|Viewer

The 'Files' tab shows a sleek file browser to access the file directory in the computer with options to manage the working directory (see section 4.1) under the More button.

The 'Plots' tab shows all the plots generated in R with buttons to delete unnecessary ones and export useful ones as a pdf file or as an image file.

The 'Packages' tab shows a list of all the R add-on packages installed. The check box on the left shows whether they are loaded or not. There are also buttons to install and update R packages.

The 'Viewer' tab shows any web content output generated by an R code.

4 Some Basics

This section describes some basics to enable the users to have a working knowledge in R in order to use augmentedRCBD.

4.1 Working Directory

It is a file path to a folder on the computer which is recognised by R as the default location to read files from or write files to. The code getwd() shows the current working directory, while setwd() can be used to change the existing working directory.

```
# Print current working directory
getwd()
```

[1] "C:/Users/Computer/Documents"

```
# Set new working directory
setwd("C:/Data Analysis/")
getwd()
```

```
[1] "C:/Data Analysis/"
```

[1] 3

One key detail is that file paths in R uses forward slashes (/) as in MacOS or Linux, unlike backward slashes (\) in Windows. This needs to be considered while copying paths from default Windows file explorer.

4.2 Expression and Assignment

Expressions are instructions in the form of code to be entered after the > prompt in the console. Expressions can be a constant, an arithmetic or a condition. A more advanced and most useful expression is a function call (see section 4.3).

```
# Constant
123
[1] 123
# Arithmetic (add two numbers)
1 + 2
```

```
# Condition
34 > 25

[1] TRUE
1 == 2

[1] FALSE
# Function call (mean of a series of numbers)
mean(c(25,56,89,35))
```

[1] 51.25

Information from an expression can be stored as an 'object' (see section 4.3) by assigning a name using the operator '<-'.

```
# Assign the result of the expression 1 + 2 to an object 'a'
a <- 1 + 2
a
```

[1] 3

It is recommended to add comments to explain the code by using the '#' sign. Any code after the '#' sign will be ignored by R.

4.3 Objects and Functions

R is an object-oriented programming language (OOP). Any kind or construct created in R is an 'object'. Each object has a 'class' (shown using the class() function) and different 'attributes' which defines what operations can be done on that object. There are different types of data structure objects in R such as vectors, matrices, factors, data frames, and lists. A 'function' is also an object, which defines a procedure or a sequence of expressions.

4.3.1 Vector

A vector is a collection of elements of a single type (or 'mode'). The common vector modes are 'numeric', 'integer', 'character' and 'logical'. The c() function is used to create vectors. The functions class(), str() and length() show the attributes of vectors.

Vector modes 'numeric' stores real numbers, while 'integer' stores integers, which can be enforced by suffixing elements with 'L'.

```
# A numeric vector
a <- c(1, 2, 3.3)
class(a)

[1] "numeric"
str(a)

num [1:3] 1 2 3.3

length(a)

[1] 3

# An integer vector
b <- c(1L, 2L, 3L)
class(b)
```

```
[1] "integer"
str(b)
 int [1:3] 1 2 3
length(b)
[1] 3
The vector mode 'character' store text.
# A character vector
c <- c("one","two","three")</pre>
class(c)
[1] "character"
str(c)
 chr [1:3] "one" "two" "three"
length(c)
[1] 3
The vector mode 'logical' stores 'TRUE' OR 'FALSE' logical data.
#logical vector
d <- c(TRUE,TRUE,TRUE,FALSE,TRUE,FALSE)</pre>
class(d)
[1] "logical"
str(d)
 logi [1:6] TRUE TRUE TRUE FALSE TRUE FALSE
length(d)
[1] 6
4.3.2 Factor
A 'factor' in R stores data from categorical data in variables as different levels.
catg <- c("male", "female", "female", "male")</pre>
catg
[1] "male"
              "female" "female" "male"
                                            "male"
is.factor(catg)
[1] FALSE
# Apply the factor function
factor_catg <- factor(catg)</pre>
factor_catg
```

```
[1] male
            female female male
                                   male
Levels: female male
is.factor(factor_catg)
[1] TRUE
class(factor_catg)
[1] "factor"
str(factor_catg)
 Factor w/ 2 levels "female", "male": 2 1 1 2 2
A character, numeric or integer vector can be transformed to a factor by using the as.factor()
# Conversion of numeric to factor
a \leftarrow c(1, 2, 3.3)
class(a)
[1] "numeric"
str(a)
num [1:3] 1 2 3.3
fac_a <- as.factor(a)</pre>
class(fac_a)
[1] "factor"
str(fac_a)
Factor w/ 3 levels "1", "2", "3.3": 1 2 3
# Conversion of integer to factor
b \leftarrow c(1L, 2L, 3L)
class(b)
[1] "integer"
str(b)
 int [1:3] 1 2 3
fac_b <- as.factor(b)</pre>
class(fac_b)
[1] "factor"
str(fac_b)
 Factor w/ 3 levels "1", "2", "3": 1 2 3
# Conversion of character to factor
c <- c("one","two","three")</pre>
class(c)
[1] "character"
```

```
str(c)
 chr [1:3] "one" "two" "three"
fac_c <- as.factor(c)</pre>
class(fac_c)
[1] "factor"
str(fac_c)
 Factor w/ 3 levels "one", "three", ...: 1 3 2
4.3.3 Matrix
A 'matrix' in R is a vector with the attributes 'nrow' and 'ncol'.
# Generate 5 * 4 numeric matrix
m <- matrix(1:20, nrow = 5, ncol = 4)
     [,1] [,2] [,3] [,4]
[1,]
        1
              6
                  11
[2,]
        2
             7
                  12
                        17
[3,]
        3
            8
                 13
                        18
        4
             9
[4,]
                  14
                        19
[5,]
        5
             10
                  15
                        20
class(m)
[1] "matrix"
typeof(m)
[1] "integer"
# Dimensions of m
dim(m)
```

[1] 5 4

4.3.4 List

A 'list' is a container containing different objects. The contents of list need not be of the same type or mode. A list can encompass a mixture of data types such as vectors, matrices, data frames, other lists or any other data structure.

```
..$ : int [1:3] 1 2 3
..$ : chr [1:3] "one" "two" "three"
```

4.3.5 Data Frame

A 'data frame' in R is a special kind of list with every element having equal length. It is very important for handling tabular data in R. It is a array like structure with rows and columns. Each column needs to be of a single data type, however data type can vary between columns.

```
L <- LETTERS[1:4]
y < -1:4
z <- c("This", "is", "a", "data frame")</pre>
df \leftarrow data.frame(L, x = 1, y, z)
df
  Lxy
                  z
1 A 1 1
              This
2 B 1 2
                 is
3 C 1 3
4 D 1 4 data frame
str(df)
'data.frame': 4 obs. of 4 variables:
 L: Factor w/ 4 levels "A", "B", "C", "D": 1 2 3 4
 $ x: num 1 1 1 1
 $ y: int 1 2 3 4
 $ z: Factor w/ 4 levels "This", "a", "data frame", ...: 1 4 2 3
attributes(df)
$names
[1] "L" "x" "y" "z"
$class
[1] "data.frame"
$row.names
[1] 1 2 3 4
rownames(df)
[1] "1" "2" "3" "4"
colnames(df)
[1] "L" "x" "y" "z"
```

4.3.6 Functions

All of the work in R is done by functions. It is an object defining a procedure which takes one or more objects as input (or 'arguments'), performs some action on them and finally gives a new object as output (or 'return'). class(), mean(), getwd(), +, etc. are all functions.

For example the function mean() takes a numeric vector as argument and returns the mean as a numeric vector.

```
a \leftarrow c(1, 2, 3.3)
mean(a)
```

[1] 2.1

The user can also create custom functions. For example the function foo adds two numbers and gives the result.

```
foo <- function(n1, n2) {
  out <- n1 + n2
  return(out)
}
foo(2,3)</pre>
```

[1] 5

4.4 Special Elements

In addition to numbers and text, there are some special elements which can be included in different data objects.

NA (not available) indicates missing data.

```
x <- c(2.5, NA, 8.6)

y <- c(TRUE, FALSE, NA)

z <- c("k", NA, "m", "n", "o")

is.na(x)
```

[1] FALSE TRUE FALSE

is.na(z)

[1] FALSE TRUE FALSE FALSE

```
anyNA(x)
```

[1] TRUE

a

[1] 1.0 2.0 3.3

is.na(a)

[1] FALSE FALSE FALSE

Inf indicates infinity.

1/0

[1] Inf

NaN (Not a Number) indicates any undefined value.

0/0

[1] NaN

4.5 Indexing

The [function is used to extract elements of an object by indexing (numeric or logical). Named elements in lists and data frames can be extracted by using the \$ operator.

```
Consider a vector a.
```

```
a \leftarrow c(1, 2, 3.3, 2.8, 6.7)
# Numeric indexing
# Extract first element
a[1]
[1] 1
# Extract elements 2:3
a[2:3]
[1] 2.0 3.3
# Logical indexing
a[a > 3]
[1] 3.3 6.7
Consider a matrix m.
m <- matrix(1:9, nrow = 3, ncol = 3, byrow = TRUE)
colnames(m) <- c('a', 'b', 'c')</pre>
     a\ b\ c
[1,] 1 2 3
[2,] 4 5 6
[3,] 7 8 9
# Extract elements
m[,2] # 2nd column of matrix
[1] 2 5 8
m[3,] # 3rd row of matrix
a b c
7 8 9
m[2:3, 1:3] # rows 2,3 of columns 1,2,3
     a b c
[1,] 4 5 6
[2,] 7 8 9
m[2,2] # Element in 2nd column of 2nd row
b
5
m[, 'b'] # Column 'b'
[1] 2 5 8
```

```
m[, c('a', 'c')] # Column 'a' and 'c'
    a c
[1,] 1 3
[2,] 4 6
[3,] 7 9
Consider a list w.
w <- list(vec = a, mat = m, data = df, alist = list(b, c))</pre>
# Indexing by number
w[2] # As list structure
$mat
    a b c
[1,] 1 2 3
[2,] 4 5 6
[3,] 7 8 9
w[[2]] # Without list structure
    a b c
[1,] 1 2 3
[2,] 4 5 6
[3,] 7 8 9
# Indexing by name
w$vec
[1] 1.0 2.0 3.3 2.8 6.7
w$data
 Lxy
1 A 1 1
            This
2 B 1 2
                is
3 C 1 3
                 a
4 D 1 4 data frame
Consider a data frame df.
df
 Lxy
                 z
            This
1 A 1 1
2 B 1 2
              is
3 C 1 3
4 D 1 4 data frame
# Indexing by number
df[,2] # 2nd column of data frame
[1] 1 1 1 1
df[2] # 2nd column of data frame
 х
1 1
```

```
2 1
3 1
4 1
df[3,] # 3rd row of data frame
  Lxyz
3 C 1 3 a
df[2:3, 1:3] # rows 2,3 of columns 1,2,3
  Lxy
2 B 1 2
3 C 1 3
df[2,2] # Element in 2nd column of 2nd row
[1] 1
# Indexing by name
df$L
[1] A B C D
Levels: A B C D
df$z
[1] This
                                     data frame
Levels: This a data frame is
```

4.6 Help Documentation

The help documentation regarding any function can be viewed using the ? or help() function. The help documentation shows the default usage of the function including, the arguments that are taken by the function and the type of output object returned ('Value').

```
?ls
help(ls)
?mean
?setwd
```

4.7 Packages

Packages in R are collections of R functions, data, and compiled code in a well-defined format. They are add-ons which extend the functionality of R and at present, there are 14563 packages available for deployment and use at the official repository, the Comprehensive R Archive Network (CRAN).

Valid packages from CRAN can be installed by using the install.packages() command.

```
# Install the package 'readxl' for importing data from excel
install.packages(readxl)
```

Installed packages can be loaded using the function library().

```
# Install the package 'readxl' for importing data from excel
library(readxl)
```

\$ blk: chr "I" "I" "I" "I" ...

\$ trt: num 1 2 3 4 7 11 12 1 2 3 ...

\$ y1 : num 92 79 87 81 96 89 82 79 81 81 ...

\$ y2 : num 258 224 238 278 347 300 289 260 220 237 ...

4.8 Importing and Exporting Tabular Data

Tabular data from a spreadsheet can be imported into R in different ways. Consider some data such as in Table 1. Copy this data in to a spreadsheet editor such as MS Excel and save it as augdata.csv, a comma-separated-value file and augdata.xlsx, an Excel file in the working directory (getwd()).

Table 1: Example	data from an	experiment in	augmented	RCBD design.
------------------	--------------	---------------	-----------	--------------

blk	trt	y1	y2
Ι	1	92	258
I	2	79	224
I	3	87	238
I	4	81	278
I	7	96	347
I	11	89	300
I	12	82	289
II	1	79	260
II	2	81	220
II	3	81	237
II	4	91	227
II	5	79	281
II	9	78	311
III	1	83	250
III	2	77	240
III	3	78	268
III	4	78	287
III	8	70	226
III	6	75	395
III	10	74	450

The augdata.csv file can be imported into R using the read.csv() function or the read_csv() function in the readr package.

```
data <- read.csv(file = "augdata.csv")
str(data)

'data.frame': 20 obs. of 4 variables:
    $ blk: Factor w/ 3 levels "I", "III", "III": 1 1 1 1 1 1 1 2 2 2 ...
    $ trt: num 1 2 3 4 7 11 12 1 2 3 ...
    $ y1 : num 92 79 87 81 96 89 82 79 81 81 ...
    $ y2 : num 258 224 238 278 347 300 289 260 220 237 ...

The argument stringsAsFactors = FALSE reads the text columns as of type character instead of the default factor.

data <- read.csv(file = "augdata.csv", stringsAsFactors = FALSE)
str(data)

'data.frame': 20 obs. of 4 variables:</pre>
```

The augdata.xlsx file can be imported into R using the read_excel() function in the readxl package.

4.9 Additional Resources

To learn more about R, there are umpteen number of online tutorials as well as free courses available. Queries about various aspects can be put to the active and vibrant 'R community online.

- Online tutorials
 - http://www.cran.r-project.org/other-docs.html
 - https://bookdown.org/ndphillips/YaRrr/
- Free online courses
 - http://tryr.codeschool.com/

write.csv(x = data, file = "augdata.csv")

- https://www.datacamp.com/courses/free-introduction-to-r
- R community support
 - http://stackoverflow.com/
 - R help mailing lists: http://www.r-project.org/mail.html

5 Installation of augmentedRCBD

The package ${\tt augmentedRCBD}$ can be installed using the following functions.

```
# Install from CRAN
install.packages('augmentedRCBD', dependencies=TRUE)

# Install development version from Github
if (!require('devtools')) install.packages('devtools')
library(devtools)
install_github("aravind-j/augmentedRCBD")
```

The stable release is hosted in CRAN (see section 4.7), while the under-development version is hosted as a Github repository. To install from github, you need to use the <code>install_github()</code> function from 'devtools package.

Then the package can be loaded using the function

```
library(augmentedRCBD)
```

```
Welcome to augmentedRCBD version 0.1.1
```

- # To know how to use this package type:
 browseVignettes(package = 'augmentedRCBD')
 for the package vignette.
- # To know whats new in this version type: news(package='augmentedRCBD') for the NEWS file.
- # To cite the methods in the package type:
 citation(package='augmentedRCBD')
- # To suppress this message use:
 suppressPackageStartupMessages(library(augmentedRCBD))

6 Data Format

Certain details need to be considered for arranging experimental data for analysis using the augmentedRCBD package.

The data should be in long/vertical form, where each row has the data from one genotype per block. For example, consider the following data (Table 2) recorded for a trait from an experiment laid out in an augmented block design with 3 blocks and 12 genotypes(or treatment) with 6 to 7 genotypes/block. 8 genotypes (Test, G 5 to G 12) are not replicated, while 4 genotypes (Check, G 1 to G 4) are replicated.

Table 2: Data from an experiment in augmented RCBD design.

Block I	G12	$\mathbf{G4}$	G11	$\mathbf{G2}$	G1	G7	$\mathbf{G3}$
	82	81	89	79	92	96	87
Block II	G5	G9	_	$\mathbf{G3}$	$\mathbf{G1}$	$\mathbf{G2}$	G4
	79	78	_	81	79	81	91
Block III	$\mathbf{G4}$	$\mathbf{G2}$	$\mathbf{G1}$	G6	G10	$\mathbf{G3}$	G8
	78	77	83	75	74	78	70

This data needs to be arranged with columns showing block, genotype (or treatment) and the data of the trait for each genotype per block (Table 3).

Table 3: Data from an experiment in augmented RCBD design arranged in long-form.

Block	Treatment	Trait
Block I	G 1	92
Block I	G 2	79
Block I	G 3	87
Block I	G 4	81
Block I	G 7	96
Block I	G 11	89
Block I	G 12	82
Block II	G 1	79
Block II	G 2	81
Block II	G 3	81

Block	Treatment	Trait
Block II	G 4	91
Block II	G 5	79
Block II	G 9	78
Block III	G 1	83
Block III	G 2	77
Block III	G 3	78
Block III	G 4	78
Block III	G 8	70
Block III	G 6	75
Block III	G 10	74

The data for block and genotype (or treatment) can also be depicted as numbers (Table 4).

Table 4: Data from an experiment in augmented RCBD design arranged in long-form (Block and Treatment as numbers).

Block	Treatment	Trait
1	1	92
1	2	79
1	3	87
1	4	81
1	7	96
1	11	89
1	12	82
2	1	79
2	2	81
2	3	81
2	4	91
2	5	79
2	9	78
3	1	83
3	2	77
3	3	78
3	4	78
3	8	70
3	6	75
3	10	74

Multiple traits can be added as additional columns (Table 5).

Table 5: Data from an experiment in augmented RCBD design arranged in long-form (Multiple traits).

Block	Treatment	Trait1	Trait2
Block I	G 1	92	258
Block I	G 2	79	224
Block I	G 3	87	238
Block I	G 4	81	278
Block I	G 7	96	347

Block	Treatment	Trait1	Trait2
Block I	G 11	89	300
Block I	G 12	82	289
Block II	G 1	79	260
Block II	G 2	81	220
Block II	G 3	81	237
Block II	G 4	91	227
Block II	G 5	79	281
Block II	G 9	78	311
Block III	G 1	83	250
Block III	G 2	77	240
Block III	G 3	78	268
Block III	G 4	78	287
Block III	G 8	70	226
Block III	G 6	75	395
Block III	G 10	74	450

Data should preferably be balanced i.e. all the check genotypes should be present in all the blocks. If not, a warning is issued. The number of test genotypes can vary within a block. There should not be any missing values. Rows of genotypes with missing values for one or more traits should be removed.

Such a tabular data should be imported (see section 7.8) into R as a data frame object (see section 4.3.5). The columns with the block and treatment categorical data should of the type factor (see section 4.3.2), while the column(s) with the trait data should be of the type integer or numeric (see section 4.3.1).

7 Data Analysis for a Single Trait

Analysis of data for a single trait can be performed by using augmentedRCBD function. It generates an object of class augmentedRCBD. Such an object can then be taken as input by the several functions to print the results to console (print.augmentedRCBD), generate descriptive statistics from adjusted means (describe.augmentedRCBD), plot frequency distribution (freqdist.augmentedRCBD) and computed genetic variability statistics (gva.augmentedRCBD). All these outputs can also be exported as a MS Word report using the report.augmentedRCBD function.

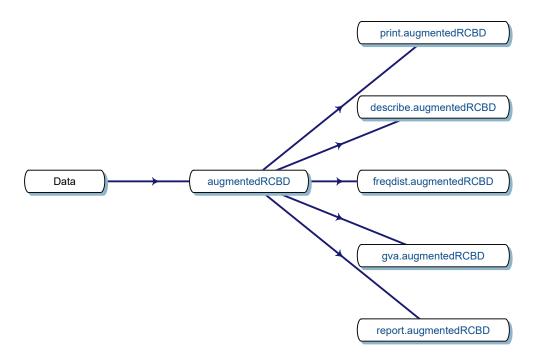


Fig. 4. Workflow for analysis of single traits with augmented RCBD.

7.1 augmentedRCBD()

Consider the data in Table 1. The data can be imported into R as vectors as follows.

The blk and trt vectors with the block and treatment data need to be converted into factors as follows before analysis.

```
# Convert block and treatment to factors
blk <- as.factor(blk)
trt <- as.factor(trt)</pre>
```

With the data in appropriate format, the analysis can be performed as follows for the trait y1 as follows.

```
Augmented Design Details
```

```
Number of blocks "3"

Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"
```

ANOVA, Treatment Adjusted

Residuals 6 161.8 26.97

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Treatment (ignoring Blocks)	11	575.7	52.33	1.940	0.215
Treatment: Check	3	52.9	17.64	0.654	0.609
Treatment: Test	7	505.9	72.27	2.679	0.125
Treatment: Test vs. Check	1	16.9	16.87	0.626	0.459
Block (eliminating Treatments)	2	69.5	34.75	1.288	0.342
Residuals	6	161.8	26.97		

Treatment Means

==========

	${\tt Treatment}$	${\tt Block}$	Means	SE	r	${\tt Min}$	Max	Adjusted Means
1	1		84.66667	3.844188	3	79	92	84.66667
2	10	3	74.00000	NA	1	74	74	77.25000
3	11	1	89.00000	NA	1	89	89	86.50000
4	12	1	82.00000	NA	1	82	82	79.50000
5	2		79.00000	1.154701	3	77	81	79.00000
6	3		82.00000	2.645751	3	78	87	82.00000
7	4		83.33333	3.929942	3	78	91	83.33333
8	5	2	79.00000	NA	1	79	79	78.25000
9	6	3	75.00000	NA	1	75	75	78.25000
10	7	1	96.00000	NA	1	96	96	93.50000
11	8	3	70.00000	NA	1	70	70	73.25000
12	9	2	78.00000	NA	1	78	78	77.25000

Coefficient of Variation

6.372367

Overall Adjusted Mean

81.0625

Standard Errors

	Std.	Error	of Diff.	CD (5%)
Control Treatment Means			4.240458	10.37603
Two Test Treatments (Same Block)			7.344688	17.97180
Two Test Treatments (Different Blocks)			8.211611	20.09309
A Test Treatment and a Control Treatment			6.360687	15.56404

${\tt Treatment\ Groups}$

===========

Method : lsd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	73.25000	5.609598	6	59.52381	86.97619	1
9	9	77.25000	5.609598	6	63.52381	90.97619	12
10	10	77.25000	5.609598	6	63.52381	90.97619	12
5	5	78.25000	5.609598	6	64.52381	91.97619	12
6	6	78.25000	5.609598	6	64.52381	91.97619	12
2	2	79.00000	2.998456	6	71.66304	86.33696	12
12	12	79.50000	5.609598	6	65.77381	93.22619	12
3	3	82.00000	2.998456	6	74.66304	89.33696	12
4	4	83.33333	2.998456	6	75.99637	90.67029	12
1	1	84.66667	2.998456	6	77.32971	92.00363	12
11	11	86.50000	5.609598	6	72.77381	100.22619	12
7	7	93.50000	5.609598	6	79.77381	107.22619	2

class(out1)

[1] "augmentedRCBD"

Similarly the analysis for the trait y2 can be computed as follows.

Augmented Design Details

```
Number of blocks "3"

Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"
```

ANOVA, Treatment Adjusted

| Df Sum Sq Mean Sq F value Pr(>F)
Block (ignoring Treatments)	2 7019	3510	12.261	0.007597
Treatment (eliminating Blocks)	11 58965	5360	18.727	0.000920
Treatment: Check	3 2150	717	2.504	0.156116
Treatment: Test and Test vs. Check	8 56815	7102	24.810	0.000473
Residuals	6 1717	286		

Block (ignoring Treatments) Treatment (eliminating Blocks)

Treatment: Check

Treatment: Test and Test vs. Check ***

Residuals

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

Df Sum Sq Mean Sq F value Pr(>F) Treatment (ignoring Blocks) 11 64708 5883 20.550 0.000707 *** Treatment: Check 2150 717 2.504 0.156116 3 Treatment: Test 7 34863 4980 17.399 0.001366 ** 27694 96.749 6.36e-05 *** Treatment: Test vs. Check 1 27694 Block (eliminating Treatments) 2 1277 639 2.231 0.188645

Residuals 6 1718 286

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Treatment Means ==========

Treatment Block Means SE r Min Max Adjusted Means 256.0000 3.055050 3 250 260 256.0000 1 1 2 10 3 450.0000 NA 1 450 450 437.6667 3 1 300.0000 NA 1 300 300 299.4167 11 12 1 289.0000 NA 1 289 289 288.4167 5 2 228.0000 6.110101 3 220 240 228.0000 6 3 247.6667 10.170764 3 237 268 247.6667 7 4 264.0000 18.681542 3 227 287 264.0000 NA 1 281 281 8 5 2 281.0000 293.9167 6 3 395.0000 NA 1 395 395 9 382.6667 7 1 347.0000 10 NA 1 347 347 346.4167 8 3 226.0000 NA 1 226 226 213.6667 11 12 9 2 311.0000 NA 1 311 311 323.9167

Coefficient of Variation

6.057617

Overall Adjusted Mean

298.4792

Standard Errors

Std. Error of Diff. CD (5%) Control Treatment Means 13.81424 33.80224 Two Test Treatments (Same Block) 23.92697 58.54719 Two Test Treatments (Different Blocks) 26.75117 65.45775 A Test Treatment and a Control Treatment 20.72137 50.70336

Treatment Groups

Method : lsd

	Treatment	Adjusted Means	SE	df	lower CI.	upper CI.	Group
8	8	J	18.274527				-
2	2	228.0000			204.0982		
3	3		9.768146	-	223.7649		_
1	1		9.768146		232.0982	279.9018	1234
4	4	264.0000	9.768146	6	240.0982	287.9018	234
12	12	288.4167	18.274527	6	243.7005	333.1328	345
5	5	293.9167	18.274527	6	249.2005	338.6328	345
11	11	299.4167	18.274527	6	254.7005	344.1328	45
9	9	323.9167	18.274527	6	279.2005	368.6328	56
7	7	346.4167	18.274527	6	301.7005	391.1328	56
6	6	382.6667	18.274527	6	337.9505	427.3828	67
10	10	437.6667	18.274527	6	392.9505	482.3828	7
cl	ass(out2)						

[1] "augmentedRCBD"

The data can also be imported as a data frame and then used for analysis. Consider the data frame data imported from Table 1 according to the instructions in section 4.8.

str(data)

Augmented Design Details

```
Number of blocks "3"

Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"
```

ANOVA, Treatment Adjusted

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

 Df
 Sum
 Sq
 Mean
 Sq
 F
 value
 Pr(>F)

 Treatment (ignoring Blocks)
 11
 575.7
 52.33
 1.940
 0.215

 Treatment: Check
 3
 52.9
 17.64
 0.654
 0.609

 Treatment: Test
 7
 505.9
 72.27
 2.679
 0.125

 Treatment: Test vs. Check
 1
 16.9
 16.87
 0.626
 0.459

 Block (eliminating Treatments)
 2
 69.5
 34.75
 1.288
 0.342

 Residuals
 6
 161.8
 26.97

Treatment Means

=========

	${\tt Treatment}$	Block	Means	SE	r	${\tt Min}$	Max	Adjusted Means
1	1		84.66667	3.844188	3	79	92	84.66667
2	10	3	74.00000	NA	1	74	74	77.25000
3	11	1	89.00000	NA	1	89	89	86.50000
4	12	1	82.00000	NA	1	82	82	79.50000
5	2		79.00000	1.154701	3	77	81	79.00000
6	3		82.00000	2.645751	3	78	87	82.00000
7	4		83.33333	3.929942	3	78	91	83.33333
8	5	2	79.00000	NA	1	79	79	78.25000
9	6	3	75.00000	NA	1	75	75	78.25000
10	7	1	96.00000	NA	1	96	96	93.50000
11	8	3	70.00000	NA	1	70	70	73.25000
12	9	2	78.00000	NA	1	78	78	77.25000

Coefficient of Variation

6.372367

Overall Adjusted Mean

81.0625

Standard Errors

 Std. Error of Diff.
 CD (5%)

 Control Treatment Means
 4.240458 10.37603

 Two Test Treatments (Same Block)
 7.344688 17.97180

 Two Test Treatments (Different Blocks)
 8.211611 20.09309

 A Test Treatment and a Control Treatment
 6.360687 15.56404

Treatment Groups

```
Method : 1sd
```

```
Treatment Adjusted Means
                                SE df lower.CL upper.CL Group
8
          8
                  73.25000 5.609598 6 59.52381 86.97619
                                                            1
9
          9
                  77.25000 5.609598 6 63.52381 90.97619
                                                            12
10
         10
                  77.25000 5.609598 6 63.52381 90.97619
                                                            12
5
          5
                  78.25000 5.609598 6 64.52381 91.97619
                                                            12
6
          6
                  78.25000 5.609598 6 64.52381 91.97619
                                                            12
2
          2
                  79.00000 2.998456 6 71.66304 86.33696
                                                            12
12
         12
                 79.50000 5.609598 6 65.77381 93.22619
                                                            12
3
          3
                 82.00000 2.998456 6 74.66304 89.33696
                                                            12
4
                 83.33333 2.998456 6 75.99637 90.67029
          4
                                                            12
1
          1
                84.66667 2.998456 6 77.32971 92.00363
                                                            12
                86.50000 5.609598 6 72.77381 100.22619
11
         11
                                                            12
          7
                  93.50000 5.609598 6 79.77381 107.22619
                                                            2
```

class(out1)

[1] "augmentedRCBD"

Augmented Design Details

```
Number of blocks "3"

Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"
```

ANOVA, Treatment Adjusted

```
Df Sum Sq Mean Sq F value
                                                              Pr(>F)
Block (ignoring Treatments)
                                    2 7019
                                                3510 12.261 0.007597
Treatment (eliminating Blocks)
                                    11 58965
                                                5360 18.727 0.000920
  Treatment: Check
                                    3
                                       2150
                                                717
                                                      2.504 0.156116
  Treatment: Test and Test vs. Check 8 56815
                                                7102 24.810 0.000473
Residuals
                                     6
                                        1717
                                                 286
```

```
Block (ignoring Treatments) **
Treatment (eliminating Blocks) ***
Treatment: Check
```

Treatment: Test and Test vs. Check ***

 ${\tt Residuals}$

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

Treatment Means

	Treatment	Block	Means	SE	r	${\tt Min}$	Max	Adjusted Means
1	1		256.0000	3.055050	3	250	260	256.0000
2	10	3	450.0000	NA	1	450	450	437.6667
3	11	1	300.0000	NA	1	300	300	299.4167
4	12	1	289.0000	NA	1	289	289	288.4167
5	2		228.0000	6.110101	3	220	240	228.0000
6	3		247.6667	10.170764	3	237	268	247.6667
7	4		264.0000	18.681542	3	227	287	264.0000
8	5	2	281.0000	NA	1	281	281	293.9167
9	6	3	395.0000	NA	1	395	395	382.6667
10	7	1	347.0000	NA	1	347	347	346.4167
11	8	3	226.0000	NA	1	226	226	213.6667
12	9	2	311.0000	NA	1	311	311	323.9167

Coefficient of Variation

6.057617

Overall Adjusted Mean

298.4792

Standard Errors

	Std.	Error	of Diff.	CD (5%)
Control Treatment Means			13.81424	33.80224
Two Test Treatments (Same Block)			23.92697	58.54719
Two Test Treatments (Different Blocks)			26.75117	65.45775
A Test Treatment and a Control Treatment			20.72137	50.70336

Treatment Groups

Method : 1sd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	${ t Group}$
8	8	213.6667	18.274527	6	168.9505	258.3828	12
2	2	228.0000	9.768146	6	204.0982	251.9018	1

```
3
          3
                   247.6667 9.768146 6 223.7649 271.5685
                                                            123
1
                   256.0000 9.768146 6 232.0982 279.9018
          1
                                                            1234
4
          4
                   264.0000 9.768146 6 240.0982 287.9018
                                                             234
         12
12
                  288.4167 18.274527 6 243.7005 333.1328
                                                              345
5
          5
                  293.9167 18.274527 6 249.2005 338.6328
                                                              345
                  299.4167 18.274527 6 254.7005 344.1328
11
         11
                                                               45
9
          9
                  323.9167 18.274527 6 279.2005 368.6328
                                                                56
7
          7
                  346.4167 18.274527 6 301.7005 391.1328
                                                                56
6
          6
                  382.6667 18.274527 6 337.9505 427.3828
                                                                 67
         10
                   437.6667 18.274527 6 392.9505 482.3828
10
                                                                  7
class(out2)
```

[1] "augmentedRCBD"

Check genotypes are inferred by default on the basis of number of replications. However, if some test genotypes are also replicated, they may also be falsely detected as checks. To avoid this, the checks can be specified by the checks argument.

Augmented Design Details

```
Number of blocks "3"

Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"
```

ANOVA, Treatment Adjusted

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

```
Df Sum Sq Mean Sq F value Pr(>F)
Treatment (ignoring Blocks)
                             11 575.7
                                         52.33
                                                1.940 0.215
 Treatment: Check
                                 52.9
                                         17.64
                                               0.654 0.609
 Treatment: Test
                              7 505.9
                                         72.27
                                                2.679 0.125
 Treatment: Test vs. Check
                                  16.9
                                         16.87
                                               0.626 0.459
                              1
Block (eliminating Treatments) 2
                                 69.5
                                               1.288 0.342
                                         34.75
Residuals
                              6 161.8
                                         26.97
```

Treatment Means

	Treatment	Block	Means	SE	r	Min	Max	Adjusted Means
1	1		84.66667	3.844188	3	79	92	84.66667
2	10	3	74.00000	NA	1	74	74	77.25000
3	11	1	89.00000	NA	1	89	89	86.50000
4	12	1	82.00000	NA	1	82	82	79.50000
5	2		79.00000	1.154701	3	77	81	79.00000
6	3		82.00000	2.645751	3	78	87	82.00000
7	4		83.33333	3.929942	3	78	91	83.33333
8	5	2	79.00000	NA	1	79	79	78.25000
9	6	3	75.00000	NA	1	75	75	78.25000
10	7	1	96.00000	NA	1	96	96	93.50000
11	8	3	70.00000	NA	1	70	70	73.25000
12	9	2	78.00000	NA	1	78	78	77.25000

Coefficient of Variation

6.372367

Overall Adjusted Mean

81.0625

Standard Errors

	Std.	Error	of Diff.	CD (5%)
Control Treatment Means			4.240458	10.37603
Two Test Treatments (Same Block)			7.344688	17.97180
Two Test Treatments (Different Blocks)			8.211611	20.09309
A Test Treatment and a Control Treatment			6.360687	15.56404

Treatment Groups

Method : 1sd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	73.25000	5.609598	6	59.52381	86.97619	1
9	9	77.25000	5.609598	6	63.52381	90.97619	12
10	10	77.25000	5.609598	6	63.52381	90.97619	12
5	5	78.25000	5.609598	6	64.52381	91.97619	12
6	6	78.25000	5.609598	6	64.52381	91.97619	12
2	2	79.00000	2.998456	6	71.66304	86.33696	12
12	12	79.50000	5.609598	6	65.77381	93.22619	12
3	3	82.00000	2.998456	6	74.66304	89.33696	12
4	4	83.33333	2.998456	6	75.99637	90.67029	12
1	1	84.66667	2.998456	6	77.32971	92.00363	12
11	11	86.50000	5.609598	6	72.77381	100.22619	12
7	7	93.50000	5.609598	6	79.77381	107.22619	2

```
# Results for variable y2 (checks specified)
out2 <- augmentedRCBD(data$blk, data$trt, data$y2, method.comp = "lsd",
                    alpha = 0.05, group = TRUE, console = TRUE,
                    checks = c("1", "2", "3", "4"))
Augmented Design Details
"3"
Number of blocks
Number of treatments
                         "12"
Number of check treatments "4"
Number of test treatments "8"
Check treatments
                         "1, 2, 3, 4"
ANOVA, Treatment Adjusted
Df Sum Sq Mean Sq F value
                                                            Pr(>F)
Block (ignoring Treatments)
                                   2
                                      7019
                                              3510 12.261 0.007597
                                              5360 18.727 0.000920
Treatment (eliminating Blocks)
                                  11 58965
  Treatment: Check
                                   3
                                      2150
                                              717
                                                    2.504 0.156116
  Treatment: Test and Test vs. Check 8 56815
                                              7102 24.810 0.000473
Residuals
                                   6
                                      1717
                                               286
Block (ignoring Treatments)
Treatment (eliminating Blocks)
  Treatment: Check
  Treatment: Test and Test vs. Check ***
Residuals
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
ANOVA, Block Adjusted
Df Sum Sq Mean Sq F value
                                                      Pr(>F)
Treatment (ignoring Blocks)
                             11 64708
                                         5883 20.550 0.000707 ***
  Treatment: Check
                             3
                                2150
                                         717
                                              2.504 0.156116
  Treatment: Test
                             7 34863
                                         4980 17.399 0.001366 **
  Treatment: Test vs. Check
                             1 27694
                                        27694 96.749 6.36e-05 ***
Block (eliminating Treatments)
                             2 1277
                                          639
                                              2.231 0.188645
Residuals
                              6
                                1718
                                          286
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Treatment Means
_____
  Treatment Block
                    Means
                                SE r Min Max Adjusted Means
               256.0000 3.055050 3 250 260
1
         1
                                                256.0000
         10
               3 450.0000
                              NA 1 450 450
2
                                                  437.6667
         11
3
              1 300.0000
                                NA 1 300 300
                                                 299.4167
         12
              1 289.0000
                                NA 1 289 289
                                                  288.4167
```

5	2		228.0000	6.110101	3	220	240	228.0000
6	3		247.6667	10.170764	3	237	268	247.6667
7	4		264.0000	18.681542	3	227	287	264.0000
8	5	2	281.0000	NA	1	281	281	293.9167
9	6	3	395.0000	NA	1	395	395	382.6667
10	7	1	347.0000	NA	1	347	347	346.4167
11	8	3	226.0000	NA	1	226	226	213.6667
12	9	2	311.0000	NA	1	311	311	323.9167

Coefficient of Variation

6.057617

Overall Adjusted Mean

298.4792

Standard Errors

 Std. Error
 of Diff.
 CD (5%)

 Control Treatment Means
 13.81424
 33.80224

 Two Test Treatments (Same Block)
 23.92697
 58.54719

 Two Test Treatments (Different Blocks)
 26.75117
 65.45775

 A Test Treatment and a Control Treatment
 20.72137
 50.70336

Treatment Groups

Method : lsd

	${\tt Treatment}$	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	213.6667	18.274527	6	168.9505	258.3828	12
2	2	228.0000	9.768146	6	204.0982	251.9018	1
3	3	247.6667	9.768146	6	223.7649	271.5685	123
1	1	256.0000	9.768146	6	232.0982	279.9018	1234
4	4	264.0000	9.768146	6	240.0982	287.9018	234
12	12	288.4167	18.274527	6	243.7005	333.1328	345
5	5	293.9167	18.274527	6	249.2005	338.6328	345
11	11	299.4167	18.274527	6	254.7005	344.1328	45
9	9	323.9167	18.274527	6	279.2005	368.6328	56
7	7	346.4167	18.274527	6	301.7005	391.1328	56
6	6	382.6667	18.274527	6	337.9505	427.3828	67
10	10	437.6667	18.274527	6	392.9505	482.3828	7

In case the large number of treatments or genotypes, it is advisable to avoid treatment comparisons with the group = FALSE argument as it will be memory and processor intensive. Further it is advised to simplify output with simplify = TRUE in order to reduce output object size.

7.2 print.augmentedRCBD()

The results of analysis in an object of class augmentedRCBD can be printed to the console as follows.

Print results for variable y1 print(out1)

Augmented Design Details

Number of blocks "3"
Number of treatments "12"
Number of check treatments "4"
Number of test treatments "8"

Check treatments "1, 2, 3, 4"

ANOVA, Treatment Adjusted

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

| Df Sum Sq Mean Sq F value Pr(>F)
Treatment (ignoring Blocks)	11 575.7	52.33	1.940	0.215
Treatment: Check	3 52.9	17.64	0.654	0.609
Treatment: Test	7 505.9	72.27	2.679	0.125
Treatment: Test vs. Check	1 16.9	16.87	0.626	0.459
Block (eliminating Treatments)	2 69.5	34.75	1.288	0.342
Residuals	6 161.8	26.97		

Treatment Means

=========

	Treatment	Block	Means	SE	r	Min	Max	Adjusted Means
1	1		84.66667	3.844188	3	79	92	84.66667
2	10	3	74.00000	NA	1	74	74	77.25000
3	11	1	89.00000	NA	1	89	89	86.50000
4	12	1	82.00000	NA	1	82	82	79.50000
5	2		79.00000	1.154701	3	77	81	79.00000
6	3		82.00000	2.645751	3	78	87	82.00000
7	4		83.33333	3.929942	3	78	91	83.33333
8	5	2	79.00000	NA	1	79	79	78.25000
9	6	3	75.00000	NA	1	75	75	78.25000
10	7	1	96.00000	NA	1	96	96	93.50000
11	8	3	70.00000	NA	1	70	70	73.25000
12	9	2	78.00000	NA	1	78	78	77.25000

Coefficient of Variation

6.372367

Overall Adjusted Mean

81.0625

Standard Errors

	Std.	Error	of Diff.	CD (5%)
Control Treatment Means			4.240458	10.37603
Two Test Treatments (Same Block)			7.344688	17.97180
Two Test Treatments (Different Blocks)			8.211611	20.09309
A Test Treatment and a Control Treatment			6.360687	15.56404

Treatment Groups

Method : 1sd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	73.25000	5.609598	6	59.52381	86.97619	1
9	9	77.25000	5.609598	6	63.52381	90.97619	12
10	10	77.25000	5.609598	6	63.52381	90.97619	12
5	5	78.25000	5.609598	6	64.52381	91.97619	12
6	6	78.25000	5.609598	6	64.52381	91.97619	12
2	2	79.00000	2.998456	6	71.66304	86.33696	12
12	12	79.50000	5.609598	6	65.77381	93.22619	12
3	3	82.00000	2.998456	6	74.66304	89.33696	12
4	4	83.33333	2.998456	6	75.99637	90.67029	12
1	1	84.66667	2.998456	6	77.32971	92.00363	12
11	11	86.50000	5.609598	6	72.77381	100.22619	12
7	7	93.50000	5.609598	6	79.77381	107.22619	2

Print results for variable y2 print(out2)

Augmented Design Details

Number of blocks "3"
Number of treatments "12"
Number of check treatments "4"
Number of test treatments "8"

Check treatments "1, 2, 3, 4"

ANOVA, Treatment Adjusted

	DΞ	Sum Sq	Mean Sq	F value	Pr(>F)
Block (ignoring Treatments)	2	7019	3510	12.261	0.007597
Treatment (eliminating Blocks)	11	58965	5360	18.727	0.000920
Treatment: Check	3	2150	717	2.504	0.156116
Treatment: Test and Test vs.	Check 8	56815	7102	24.810	0.000473

Residuals 6 1717 286

Block (ignoring Treatments) **
Treatment (eliminating Blocks) ***

Treatment: Check

Treatment: Test and Test vs. Check ***

Residuals

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

	Df	Sum Sq	Mean Sq	F value	Pr(>F)	
Treatment (ignoring Blocks)	11	64708	5883	20.550	0.000707	***
Treatment: Check	3	2150	717	2.504	0.156116	
Treatment: Test	7	34863	4980	17.399	0.001366	**
Treatment: Test vs. Check	1	27694	27694	96.749	6.36e-05	***
Block (eliminating Treatments)	2	1277	639	2.231	0.188645	
Residuals	6	1718	286			

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1

Treatment Means

_____ Treatment Block Means SE r Min Max Adjusted Means 1 256.0000 3.055050 3 250 260 256.0000 1 10 3 450.0000 2 NA 1 450 450 437.6667 3 11 1 300.0000 NA 1 300 300 299.4167 4 12 1 289.0000 NA 1 289 289 288.4167 228.0000 6.110101 3 220 240 5 2 228.0000 247.6667 10.170764 3 237 268 6 3 247.6667 7 4 264.0000 18.681542 3 227 287 264.0000 2 281.0000 5 NA 1 281 281 293.9167 8 3 395.0000 6 NA 1 395 395 9 382.6667 7 1 347.0000 NA 1 347 347 10 346.4167 8 3 226.0000 NA 1 226 226 213.6667 11

Coefficient of Variation

9

2 311.0000

6.057617

12

Overall Adjusted Mean

298.4792

Standard Errors

| Std. Error of Diff. CD (5%)
Control Treatment Means	13.81424	33.80224
Two Test Treatments (Same Block)	23.92697	58.54719
Two Test Treatments (Different Blocks)	26.75117	65.45775

NA 1 311 311

323.9167

A Test Treatment and a Control Treatment

20.72137 50.70336

Treatment Groups

Method : 1sd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	213.6667	18.274527	6	168.9505	258.3828	12
2	2	228.0000	9.768146	6	204.0982	251.9018	1
3	3	247.6667	9.768146	6	223.7649	271.5685	123
1	1	256.0000	9.768146	6	232.0982	279.9018	1234
4	4	264.0000	9.768146	6	240.0982	287.9018	234
12	12	288.4167	18.274527	6	243.7005	333.1328	345
5	5	293.9167	18.274527	6	249.2005	338.6328	345
11	11	299.4167	18.274527	6	254.7005	344.1328	45
9	9	323.9167	18.274527	6	279.2005	368.6328	56
7	7	346.4167	18.274527	6	301.7005	391.1328	56
6	6	382.6667	18.274527	6	337.9505	427.3828	67
10	10	437.6667	18.274527	6	392.9505	482.3828	7

7.3 describe.augmentedRCBD()

The descriptive statistics such as count, mean, standard error, minimum, maximum, skewness (with p-value from D'Agostino test of skewness (D'Agostino (1970))) and kurtosis (with p-value from Anscombe-Glynn test of kurtosis (Anscombe and Glynn (1983))) for the adjusted means from the results in an object of class augmentedRCBD can be computed as follows.

```
# Descriptive statistics for variable y1
describe.augmentedRCBD(out1)
```

```
$Mean

[1] 81.0625

$Std.Error

[1] 1.547002

$Std.Deviation

[1] 5.358973
```

\$Count [1] 12

[1] 73.25

\$Min

\$Max [1] 93.5

\$`Skewness(statistic)` skew z 0.9250344 1.6745760

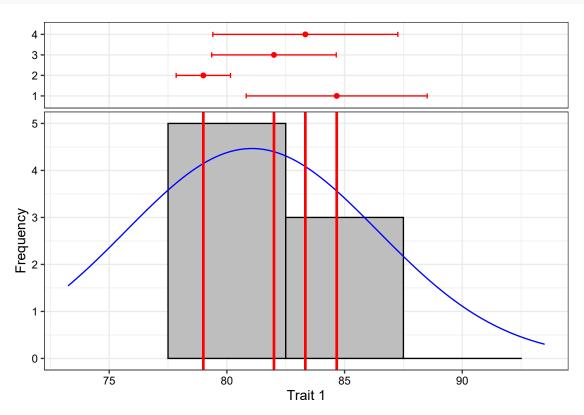
```
$`Skewness(p.value)`
[1] 0.09401746
$`Kurtosis(statistic)`
3.522807 1.282305
$`Kurtosis(p.value)`
[1] 0.1997357
# Descriptive statistics for variable y2
describe.augmentedRCBD(out2)
$Count
[1] 12
$Mean
[1] 298.4792
$Std.Error
[1] 18.92257
$Std.Deviation
[1] 65.5497
$Min
[1] 213.6667
$Max
[1] 437.6667
$`Skewness(statistic)`
     skew
0.7449405 1.3680211
$`Skewness(p.value)`
[1] 0.1713055
$`Kurtosis(statistic)`
    kurt
2.787997 0.536812
$`Kurtosis(p.value)`
[1] 0.5913975
7.4 freqdist.augmentedRCBD()
```

The frequency distribution of the adjusted means from the results in an object of class augmentedRCBD can be plotted as follows.

```
# Frequency distribution for variable y1
freq1 <- freqdist.augmentedRCBD(out1, xlab = "Trait 1")</pre>
```

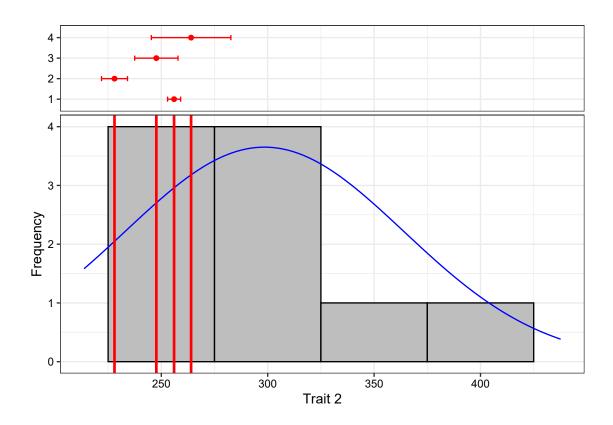
Warning: Removed 2 rows containing missing values (geom_bar).





```
# Frequency distribution for variable y2
freq2 <- freqdist.augmentedRCBD(out2, xlab = "Trait 2")</pre>
```

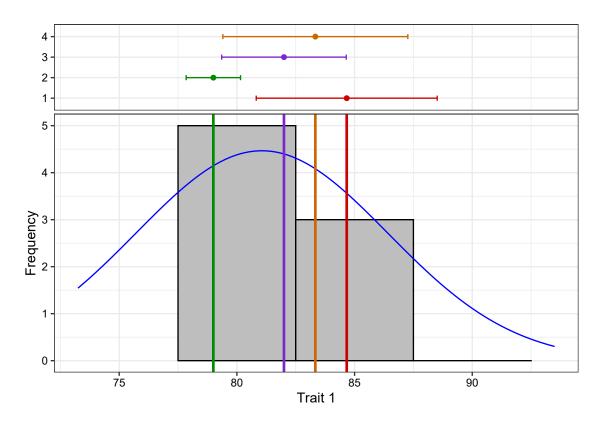
Warning: Removed 2 rows containing missing values (geom_bar). plot(freq2)



The colours for the check values may be specified using the argument check.col.

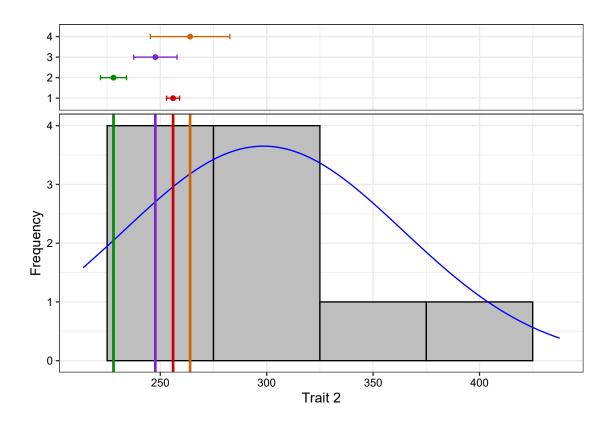
```
colset <- c("red3", "green4", "purple3", "darkorange3")
# Frequency distribution for variable y1
freq1 <- freqdist.augmentedRCBD(out1, xlab = "Trait 1", check.col = colset)</pre>
```

Warning: Removed 2 rows containing missing values (geom_bar).
plot(freq1)



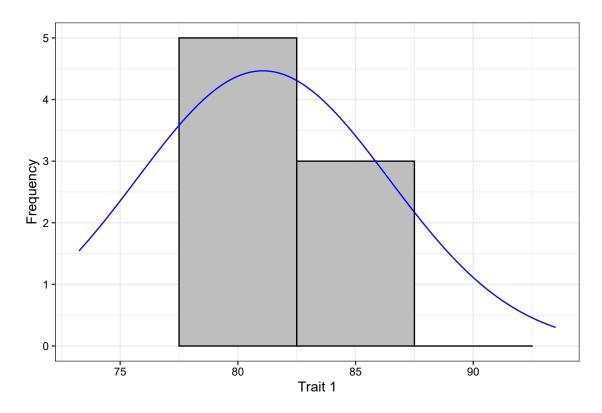
Frequency distribution for variable y2
freq2 <- freqdist.augmentedRCBD(out2, xlab = "Trait 2", check.col = colset)</pre>

Warning: Removed 2 rows containing missing values (geom_bar). plot(freq2)

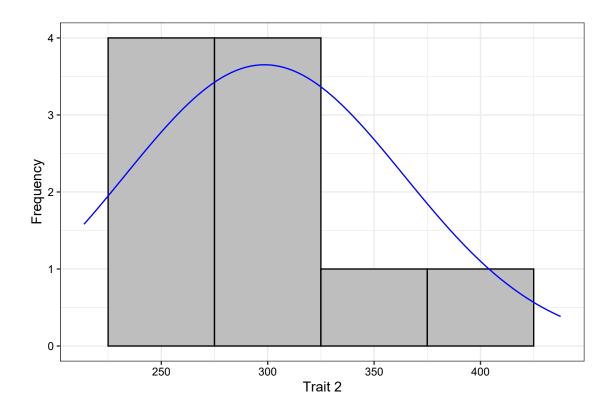


The default the check highlighting can be avoided using the argument highlight.check = FALSE.

Warning: Removed 2 rows containing missing values (geom_bar). plot(freq1)



Warning: Removed 2 rows containing missing values (geom_bar). plot(freq2)



7.5 gva.augmentedRCBD()

The genetic variability statistics such as mean, phenotypic, genotypic and environmental variation, phenotypic, genotypic and environmental coefficient of variation (Burton (1951), Burton (1952)), category of phenotypic and genotypic coefficient of variation according to Sivasubramaniam and Madhavamenon (1973), broad-sense heritability (H^2) (Lush (1940)), H^2 category according to Robinson (1966), Genetic advance (GA), genetic advance as per cent of mean (GAM) and GAM category according to Johnson et al. (1955) are computed from an object of class augmentedRCBDas follows.

```
# Genetic variability statistics for variable y1
gva.augmentedRCBD(out1)
```

```
$Mean

[1] 81.0625

$PV

[1] 72.26786

$GV

[1] 45.29563

$EV

[1] 26.97222

$GCV

[1] 8.302487
```

```
$`GCV category`
[1] "Low"
$PCV
[1] 10.48703
$`PCV category`
[1] "Medium"
$ECV
[1] 6.406759
$hBS
[1] 62.67743
$`hBS category`
[1] "High"
$GA
[1] 10.99216
$GAM
[1] 13.5601
$`GAM category`
[1] "Medium"
\# Genetic variability statistics for variable y2
gva.augmentedRCBD(out2)
$Mean
[1] 298.4792
$PV
[1] 4980.411
$GV
[1] 4694.161
$EV
[1] 286.25
$GCV
[1] 22.95435
$`GCV category`
[1] "High"
$PCV
[1] 23.64387
$`PCV category`
```

```
[1] "High"

$ECV
[1] 5.668377

$hBS
[1] 94.25248

$`hBS category`
[1] "High"

$GA
[1] 137.2223

$GAM
[1] 45.97382

$`GAM category`
[1] "High"
```

7.5 report.augmentedRCBD()

The results generated by the analysis can be exported to a MS Word file as follows.

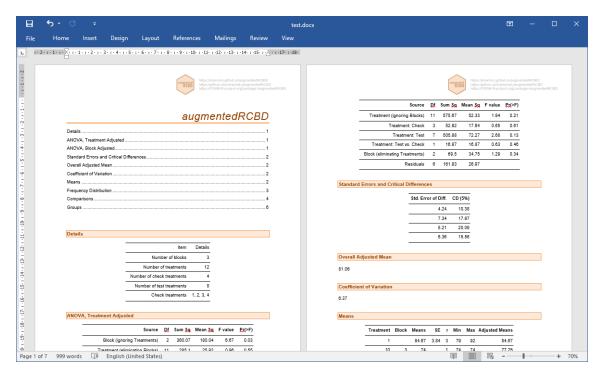


Fig. 6: MS Word report generated with report.agumentedRCBD function.

8 Data Analysis for a Multiple Traits

Analysis of data for a multiple traits simultaneously can be performed by using augmentedRCBD.bulk function. It generates an object of class augmentedRCBD.bulk. Such an object can then be taken as input by print.augmentedRCBD.bulk to print the results to console. The results can also be exported as a MS Word report using the report.augmentedRCBD.bulk function.

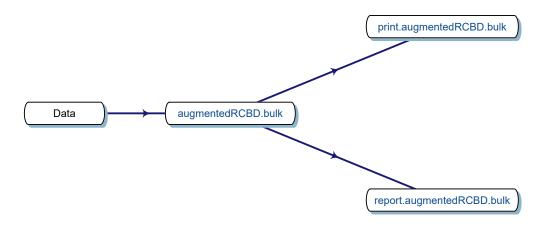


Fig. 7. Workflow for analysis of multiple traits with augmented RCBD.

8.1 augmentedRCBD.bulk()

Consider the data frame data imported from Table 1 according to the instructions in section 4.8. str(data)

```
'data.frame': 20 obs. of 4 variables:
$ blk: Factor w/ 3 levels "1","2","3": 1 1 1 1 1 1 1 2 2 2 ...
$ trt: Factor w/ 12 levels "1","2","3","4",..: 1 2 3 4 7 11 12 1 2 3 ...
$ y1 : num 92 79 87 81 96 89 82 79 81 81 ...
$ y2 : num 258 224 238 278 347 300 289 260 220 237 ...
# Convert block and treatment to factors
data$blk <- as.factor(data$blk)
data$trt <- as.factor(data$trt)
```

Rather than performing the analysis individually for each variable/trait separately using augmentedRCBD, the analysis can be performed simultaneously for for both the traits using augmentedRCBD.bulk function. It is a wrapper around the augmentedRCBD core function and its associated helper functions.

However in this case treatment comparisons/grouping by least significant difference or Tukey's honest significant difference method is not computed. Also the output object size is reduced using the simplify = TRUE argument in the augmentedRCBD function.

The logical arguments describe, freqdist and gva can be used to specify whether to generate the descriptive statistics, frequency distribution plots and genetic variability statistics respectively. If gva =

TRUE, then plots to compare phenotypic and genotypic coefficient of variation, broad sense heritability and genetic advance over mean between traits are also generated.

ANOVA for y2 computed (2/2)

Augmented Design Details

```
Number of blocks "3"

Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"

Number of traits "2"

Traits "y1, y2"
```

ANOVA, Treatment Adjusted

```
Source Df y1 y2

1 Block (ignoring Treatments) 2 180.04 * 3509.67 **

2 Treatment (eliminating Blocks) 11 25.92 ns 5360.49 **

3 Treatment: Check 3 17.64 ns 716.75 ns

4 Treatment: Test and Test vs. Check 8 29.02 ns 7101.89 **

5 Residuals 6 26.97 286.25
```

ANOVA, Block Adjusted

```
Source Df
                                                       у2
1
    Treatment (ignoring Blocks) 11 52.33 ns
                                               5882.5 **
2
               Treatment: Check 3 17.64 ns
                                               716.75 ns
3
      Treatment: Test vs. Check 1 16.87 ns 27694.41 **
                Treatment: Test 7 72.27 ns
                                              4980.41 **
5 Block (eliminating Treatments) 2 34.75 ns
                                               638.58 ns
                      Residuals 6 26.97
                                               286.25
```

Coefficient of Variation

```
_____
```

```
Trait CV
1 y1 6.37
2 y2 6.06
```

Overall Adjusted Mean

Trait Overall.adjusted.mean

1 y1 81.06

y2

298.48

Standard Errors

Comparison y1

- 1 A Test Treatment and a Control Treatment 6.36 20.72
- Control Treatment Means 4.24 13.81
- Two Test Treatments (Different Blocks) 8.21 26.75
- 4 Two Test Treatments (Same Block) 7.34 23.93

Critical Difference

alpha = 0.05Comparison у1 у2

- 1 A Test Treatment and a Control Treatment 15.56 50.7
- Control Treatment Means 10.38 33.8
- Two Test Treatments (Different Blocks) 20.09 65.46
- 4 Two Test Treatments (Same Block) 17.97 58.55

Descriptive Statistics

===========

Trait Count Mean Std.Error Std.Deviation Min Max Skewness

- y1
- 12 81.06 1.55 5.36 73.25 93.5 0.93 ns
- y2 12 298.48 18.92
- 65.55 213.67 437.67 0.74 ns

Kurtosis

- 1 3.52 ns
- 2 2.79 ns

Genetic Variability Analysis

PVGV Trait Mean EVGCV GCV.category PCV

- v1 81.06 72.27 45.3 26.97 8.3 Low 10.49
- y2 298.48 4980.41 4694.16 286.25 22.95 High 23.64

PCV.category ECV hBS hBS.category GA GAM.category

Medium 6.41 62.68 High 10.99 13.56 1 Medium

2 High 5.67 94.25 High 137.22 45.97 High

Warning Messages

Removed 2 rows containing missing values (geom_bar).

y2

Removed 2 rows containing missing values (geom_bar).

Treatment Means

Treatment y2 у1 1 84.67 256 1 2 10 77.25 437.67 3 11 86.5 299.42 4 12 79.5 288.42 5 2 79 228 6 3 82 247.67 7 4 83.33 264 8 5 78.25 293.92 6 78.25 382.67 9 10 7 93.5 346.42 8 73.25 213.67 11 9 77.25 323.92 12

8.2 print.augmentedRCBD.bulk()

The results of analysis in an object of class augmentedRCBD.bulk can be printed to the console as follows.

```
# Print results
print(bout)
```

Augmented Design Details

```
Number of blocks "3"

Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"

Number of traits "2"

Traits "y1, y2"
```

ANOVA, Treatment Adjusted

```
Source Df y1 y2

1 Block (ignoring Treatments) 2 180.04 * 3509.67 **

2 Treatment (eliminating Blocks) 11 25.92 ns 5360.49 **

3 Treatment: Check 3 17.64 ns 716.75 ns

4 Treatment: Test and Test vs. Check 8 29.02 ns 7101.89 **

5 Residuals 6 26.97 286.25
```

ANOVA, Block Adjusted

```
Source Df y1 y2

1 Treatment (ignoring Blocks) 11 52.33 ns 5882.5 **

2 Treatment: Check 3 17.64 ns 716.75 ns

3 Treatment: Test vs. Check 1 16.87 ns 27694.41 **

4 Treatment: Test 7 72.27 ns 4980.41 **

5 Block (eliminating Treatments) 2 34.75 ns 638.58 ns
```

6 Residuals 6 26.97 286.25

Coefficient of Variation

Trait CV

- y1 6.37
- y2 6.06

Overall Adjusted Mean

Trait Overall.adjusted.mean

- у1
- 81.06
- у2
- 298.48

Standard Errors

- Comparison y1 y2
- 1 A Test Treatment and a Control Treatment 6.36 20.72
- Control Treatment Means 4.24 13.81
- Two Test Treatments (Different Blocks) 8.21 26.75
- Two Test Treatments (Same Block) 7.34 23.93

Critical Difference

alpha = 0.05Comparison y1 y2

- 1 A Test Treatment and a Control Treatment 15.56 50.7
- Control Treatment Means 10.38 33.8
- Two Test Treatments (Different Blocks) 20.09 65.46
- Two Test Treatments (Same Block) 17.97 58.55

Descriptive Statistics

Trait Count Mean Std.Error Std.Deviation Min Max Skewness

- 1 y1 12 81.06 1.55 5.36 73.25 93.5 0.93 ns 2 y2 12 298.48 18.92 65.55 213.67 437.67 0.74 ns 2 y2 12 298.48

Kurtosis

- 1 3.52 ns
- 2 2.79 ns

Genetic Variability Analysis

Trait Mean PV GV EV GCV GCV.category PCV

- y1 81.06 72.27 45.3 26.97 8.3 Low 10.49
- y2 298.48 4980.41 4694.16 286.25 22.95 High 23.64 PCV.category ECV hBS hBS.category GA GAM GAM.category
- 1 Medium 6.41 62.68 High 10.99 13.56 Medium High 137.22 45.97 2 High 5.67 94.25

Treatment Means

==========		
Treatment	y1	у2
1 1	84.67	256
2 10	77.25	437.67
3 11	86.5	299.42
4 12	79.5	288.42
5 2	79	228
6 3	82	247.67
7 4	83.33	264
8 5	78.25	293.92
9 6	78.25	382.67
10 7	93.5	346.42
11 8	73.25	213.67
12 9	77.25	323.92

8.3 report.augmentedRCBD.bulk()

The results generated by the analysis can be exported to a MS Word file as follows.

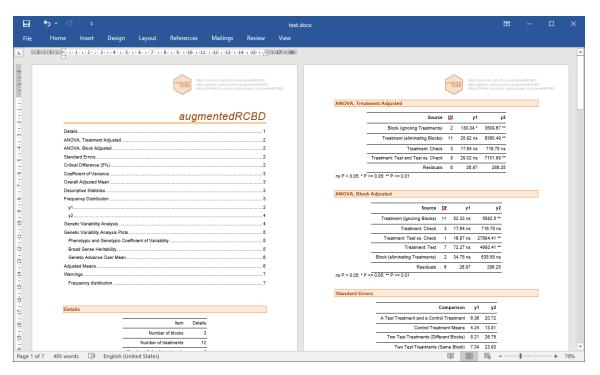


Fig. 8: MS Word report generated with report.agumentedRCBD.bulk function.

9 Citing augmentedRCBD

project by citing the package.

```
To cite the R package 'augmentedRCBD' in publications use:

Aravind, J., Mukesh Sankar, S., Wankhede, D. P., and Kaur, V.
(2019). augmentedRCBD: Analysis of Augmented Randomised
Complete Block Designs. R package version 0.1.1,
https://aravind-j.github.io/augmentedRCBD/https://cran.r-project.org/package=augmentedRCBD.

A BibTeX entry for LaTeX users is

@Manual{,
   title = {augmentedRCBD: Analysis of Augmented Randomised Complete Block Designs},
   author = {J. Aravind and S. {Mukesh Sankar} and Dhammaprakash Pandhari Wankhede and Vikender Kaur
   year = {2019},
   note = {R package version 0.1.1},
   note = {https://aravind-j.github.io/augmentedRCBD/},
   note = {https://cran.r-project.org/package=augmentedRCBD},
}
```

This free and open-source software implements academic research by the authors and co-workers. If you use it, please support the

10 Session Info

```
sessionInfo()
R version 3.6.0 (2019-04-26)
Platform: x86_64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 17763)
Matrix products: default
locale:
[1] LC_COLLATE=C
                                    LC_CTYPE=English_India.1252
[3] LC_MONETARY=English_India.1252 LC_NUMERIC=C
[5] LC_TIME=English_India.1252
attached base packages:
[1] stats
              graphics grDevices utils
                                             datasets methods
                                                                 base
other attached packages:
[1] diagram_1.6.4
                        shape_1.4.4
                                             augmentedRCBD_0.1.1
loaded via a namespace (and not attached):
 [1] zoo_1.8-6
                        tidyselect_0.2.5
                                            xfun_0.8
 [4] reshape2_1.4.3
                        purrr_0.3.2
                                            splines_3.6.0
 [7] lattice_0.20-38
                        colorspace_1.4-1
                                            htmltools_0.3.6
[10] yaml_2.2.0
                        base64enc_0.1-3
                                            survival_2.44-1.1
[13] rlang_0.4.0
                        pillar_1.4.2
                                            glue_1.3.1
[16] gdtools_0.1.9
                        uuid_0.1-2
                                            plyr_1.8.4
[19] emmeans_1.3.5.1
                        multcomp_1.4-10
                                            multcompView_0.1-7
[22] stringr_1.4.0
                        munsell_0.5.0
                                            gtable_0.3.0
[25] moments_0.14
                        zip_2.0.3
                                            mvtnorm_1.0-11
[28] codetools_0.2-16
                        coda_0.19-3
                                            evaluate_0.14
[31] labeling_0.3
                        knitr_1.23
                                            gbRd_0.4-11
[34] highr_0.8
                        TH.data_1.0-10
                                            Rcpp_1.0.1
[37] xtable_1.8-4
                        scales_1.0.0
                                            ggplot2_3.2.0
[40] digest_0.6.20
                        stringi_1.4.3
                                            dplyr_0.8.3
[43] grid_3.6.0
                        bibtex_0.4.2
                                            Rdpack_0.11-0
[46] tools_3.6.0
                        sandwich_2.5-1
                                            magrittr_1.5
[49] lazyeval 0.2.2
                        tibble 2.1.3
                                            crayon 1.3.4
[52] pkgconfig_2.0.2
                        MASS_7.3-51.4
                                            Matrix_1.2-17
[55] data.table 1.12.2 xml2 1.2.0
                                            estimability 1.3
[58] assertthat_0.2.1
                                            officer_0.3.5
                        rmarkdown_1.14
[61] flextable_0.5.5
                        R6_2.4.0
                                            compiler_3.6.0
```

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