# Knowledge Space Theory Input and Output

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#### Abstract

This document explains basic read and write operations for knowledge structures and knowledge spaces available in R through the **kstIO** package.

Knowledge Space Theory (Doignon and Falmagne, 1999) is a set- and order-theoretical framework, which proposes mathematical formalisms to operationalize knowledge structures in a particular domain. There exist several R packages for knowledge space theory, namely **kst**, **pks**, and **DAKS** which use different forms of representations for knowledge spaces and structures. The **kstIO** package provides functions for reading and writing those structures from/to files.

## 1 File Formats

Over time and in different research groups with knowledge space theory, different file formats have evolved.

#### 1.1 Matrix Format

The probably simplest and most direct approach is to store the information in a binary ASCII matrix where a "1" in row i and column j means that item j is element of state/response pattern i.

There is no separating character between the columns, and there should be no trailing whitespace at the end of the line. The last line of the matrix must carry an EndOfLine - in most editors (except vi) this means an empty line after the matrix.

### 1.2 KST Tools Format

This format (Hockemeyer, 2001) extends the matrix format by two preceding header lines containing the number of items and the number of states/response patterns, respectively.

#### 1.3 SRBT Tools Format

This format (Pötzi and Wesiak, 2001) extends the KST tools format by yet another preceding header line with format and content metadata. This new header line has the format

#### #SRBT v2.0 <struct> ASCII <comment>

where <struct> specifies the type of data stored in the file and <comment> is an optional arbitrary comment.

The following data types are supported by the respective kstIO functions:

- basis
- data
- space
- structure

### 1.4 Base Files

For base files, some special rules apply. They are available only in KST and SRBT tools format. Their matrix part differs from the other files in that it contains "0", "1", and "2". A "1" means that the state is minimal for the item and a "2" means that it is not (but contains the item). A "0" stands (as always) for the state not containing the item.

For kbase files, the encoding information "ASCII" is missing because kbase files are always in ASCII format.

**Note:** While the respective functions in **kst** and **kstIO** use the term *base* in their names, the sstruct> term in the SRBT header line is *basis*.

## 1.5 Example

Below, you see an example of a small knowledge structure file in SRBT format.

```
#SRBT v2.0 structure ASCII
3
5
000
100
110
101
111
```

## 1.6 Binary File Formats

The KST and SRBT Tools User Manuals (Hockemeyer, 2001; Pötzi and Wesiak, 2001) define also binary file formats. These formats are not (yet) supported by the **kstIO** package.

## 2 Output functions

There are four output functions in the kstIO package.

```
write_kbase()write_kdata()write_kspace()write_kstructure()
```

These functions have the same calling scheme

```
write_kXXX(x, filename, format="SRBT")
```

where x denotes the data structure to be written, filename the name of the file to be created, and format the file format ("SRBT", "KST", or "matrix" as described in Section 1 above. The knowledge structure or knowledge space can be in set-based format (classes kspace or kstructure) or in matrix format. Please note that for bases, only the SRBT and KST formats are valid.

```
> # Obtain data from the pks package
> data(DoignonFalmagne7)
> ksp <- kspace(kstructure(as.pattern(DoignonFalmagne7$K, as.set=TRUE)))
> b <- kbase(ksp)
> d <- as.binmat(DoignonFalmagne7$N.R)
> ksp
```

```
{{}, {"a"}, {"b"}, {"a", "b"}, {"a", "b", "c"}, {"a", "b", "d"}, {"a",
 "b", "c", "d"}, {"a", "b", "c", "e"}, {"a", "b", "c", "d", "e"}}
> b
{{"a"}, {"b"}, {"a", "b", "c"}, {"a", "b", "d"}, {"a", "b", "c", "e"}}
> d
      a b c d e
 [1,] 0 0 0 0 0
 [2,] 1 0 0 0 0
 [3,] 0 1 0 0 0
 [4,] 0 0 1 0 0
 [5,] 0 0 0 1 0
 [6,] 0 0 0 0 1
 [7,] 1 1 0 0 0
 [8,] 1 0 1 0 0
 [9,] 1 0 0 1 0
[10,] 1 0 0 0 1
[11,] 0 1 1 0 0
[12,] 0 1 0 1 0
[13,] 0 1 0 0 1
[14,] 0 0 1 1 0
[15,] 0 0 1 0 1
[16,] 0 0 0 1 1
[17,] 1 1 1 0 0
[18,] 1 1 0 1 0
[19,] 1 1 0 0 1
[20,] 1 0 1 1 0
[21,] 1 0 1 0 1
[22,] 1 0 0 1 1
[23,] 0 1 1 1 0
[24,] 0 1 1 0 1
[25,] 0 1 0 1 1
[26,] 0 0 1 1 1
[27,] 1 1 1 1 0
[28,] 1 1 1 0 1
[29,] 1 1 0 1 1
[30,] 1 0 1 1 1
[31,] 0 1 1 1 1
[32,] 1 1 1 1 1
> # Write data to files
> write_kstructure(ksp, "DF7.struct")
> write_kspace(ksp, "DF7.space", format="matrix")
> write_kbase(b, "DF7.bas", format="KST")
> write_kdata(d, "DF7.data", format="SRBT")
The resulting base file, for example, looks like the following:
> txt <- readLines("DF7.bas")</pre>
> for (i in txt)
    cat(paste(i, "\n", sep=""))
```

```
5
5
10000
01000
22100
22010
22201
```

## 3 Input Functions

There are four input functions in the **kstIO** package.

- read\_kbase()
- read\_kdata()
- read\_kspace()
- read\_kstructure()

These functions have the same calling scheme

```
d <- read_kXXX(filename, format="SRBT")</pre>
```

where filename denotes the file to be read and format the file format ("SRBT", "KST", or "matrix" as described in Section 1 above, or "auto" (default) for automatic format detection. Please note that automatic format detection works slightly heuristically and therefore might err between "KST" and "matrix" formats under rare circumstances.

The return values depend on the type of file to be read: for read\_kspace() and read\_kstructure() it is a list containing of two element, matrix and sets containing the read knowledge structure/space as a binary matrix and in set-based form (i.e. as object of class kspace or kstructure), respectively. For read\_kbase(), an object of class kbase is returned and for read\_kdata() a binary matrix.

- > # Read the data files stored before
  > read\_kstructure("DF7.struct", format="SRBT")
- \$matrix

	[,1]	[,2]	[,3]	[,4]	[,5]
[1,]	0	0	0	0	0
[2,]	1	0	0	0	0
[3,]	0	1	0	0	0
[4,]	1	1	0	0	0
[5,]	1	1	1	0	0
[6,]	1	1	0	1	0
[7,]	1	1	1	1	0
[8,]	1	1	1	0	1
[9,]	1	1	1	1	1

#### \$sets

```
{{}, {"a"}, {"b"}, {"a", "b"}, {"a", "b", "c"}, {"a", "b", "d"}, {"a", "b", "c", "d"}, {"a", "b", "c", "d", "e"}}
```

> read\_kspace("DF7.space", format="matrix")

```
[,1] [,2] [,3] [,4] [,5]
 [1,]
 [2,]
                              0
                                    0
                 0
                        0
           1
 [3,]
           0
                              0
                                    0
 [4,]
                              0
                                    0
           1
                 1
                        0
 [5,]
           1
                                    0
 [6,]
                                    0
           1
                        0
                              1
                 1
 [7,]
           1
                              1
                                    0
                 1
                        1
                              0
                                    1
 [8,]
           1
                 1
                        1
 [9,]
           1
                 1
                        1
                              1
                                    1
$sets
{{}, {"a"}, {"b"}, {"a", "b"}, {"a", "b", "c"}, {"a", "b", "d"}, {"a",
 "b", "c", "d"}, {"a", "b", "c", "e"}, {"a", "b", "c", "d", "e"}}
> read_kbase("DF7.bas", format="auto")
 \{ \{ \text{"a"}\}, \ \{ \text{"b"}\}, \ \{ \text{"a"}, \ \text{"b"}, \ \{ \text{"a"}, \ \text{"b"}, \ \text{"d"}\}, \ \{ \text{"a"}, \ \text{"b"}, \ \text{"c"}, \ \text{"e"} \} \} 
> read_kdata("DF7.data")
       [,1] [,2] [,3] [,4] [,5]
 [1,]
 [2,]
           1
                 0
                        0
                              0
                                    0
 [3,]
           0
                 1
                        0
                              0
                                    0
                                    0
 [4,]
           0
                 0
                              0
                        1
 [5,]
           0
                 0
                              1
                                    0
 [6,]
           0
                 0
                        0
                              0
                                    1
 [7,]
           1
                 1
                        0
                              0
                                    0
 [8,]
           1
                 0
                              0
                                    0
 [9,]
           1
                 0
                        0
                              1
                                    0
[10,]
           1
                        0
                              0
                 0
                                    1
[11,]
           0
                              0
                                    0
                 1
                        1
[12,]
           0
                              1
                                    0
[13,]
           0
                 1
                        0
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                                    1
[14,]
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                              1
                                    0
[15,]
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                 0
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                                    1
                        1
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[16,]
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[17,]
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[18,]
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[19,]
           1
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[20,]
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[21,]
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           1
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[22,]
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                        0
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[23,]
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[24,]
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[25,]
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[26,]
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                                    1
[27,]
           1
                 1
                              1
                                    0
[28,]
                              0
           1
                 1
                        1
                                    1
[29,]
           1
                        0
                              1
                 1
                                    1
[30,]
           1
                 0
                        1
                              1
                                    1
[31,]
           0
                                    1
                 1
                              1
[32,]
                              1
                                    1
           1
                 1
```

\$matrix

## References

- J.-P. Doignon and J.-C. Falmagne. Knowledge Spaces. Springer-Verlag, Berlin, 1999.
- C. Hockemeyer. KST Tools User Manual, 2nd edition, 2001. URL https://kst.hockemeyer.at/techreports/KST-Tools\_TechRep\_FWF01.pdf.
- S. Pötzi and G. Wesiak. SRbT Tools User Manual, 2001. URL https://kst.hockemeyer.at/techreports/SRBT-Tools\_TechRep\_FWF01.pdf.

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