

$$\varphi = \neg \forall y (S(y) \rightarrow \exists z R(z)) \wedge \forall x (\forall y P(x, y) \rightarrow f(x) = d)$$

$$\models \neg \forall y (S(y) \rightarrow \exists z R(z)) \wedge \forall x (\forall a P(x, a) \rightarrow f(x) = d)$$

$$\models \exists y \neg (S(y) \rightarrow \exists z R(z)) \wedge \forall x \exists a (P(x, a) \rightarrow f(x) = d)$$

$$\models \exists y \neg \exists z (S(y) \rightarrow R(z)) \wedge \forall x \exists a (P(x, a) \rightarrow f(x) = d)$$

$$\models \exists y \forall z \forall x \exists a (\neg (S(y) \rightarrow R(z)) \wedge (P(x, a) \rightarrow f(x) = d))$$

$$\begin{aligned}
 & \neg \forall y (S(y) \rightarrow \exists z R(z)) \\
 \equiv & \exists y \neg (S(y) \rightarrow \exists z R(z)) \\
 \equiv & \exists y (S(y) \wedge \neg \exists z R(z)) \\
 \equiv & \exists y (S(y) \wedge \forall z \neg R(z)) \\
 \equiv & \exists y \forall z (S(y) \wedge \neg R(z))
 \end{aligned}$$

$$p \rightarrow q \equiv \neg p \vee q$$

$$\begin{array}{c}
 \neg \quad \quad \searrow \\
 \quad \quad \quad \exists \\
 \downarrow \\
 \neg \exists \quad ()
 \end{array}$$

$$\varphi = \underbrace{\exists x (S(x) \rightarrow \forall y (f(y) \rightarrow c))}_{\text{premise}} \rightarrow \underbrace{\neg (\forall x T(x) \vee \forall y S(y))}_{\text{conclusion}}$$

$$\# \exists x (S(x) \rightarrow \forall y (f(y) \rightarrow c)) \rightarrow \neg (\forall u T(u) \vee \forall v S(v))$$

$$\# \exists x \forall y (S(x) \rightarrow (f(y) \rightarrow c)) \rightarrow (\neg \forall u T(u) \wedge \neg \forall v S(v))$$

$$\# \exists x \forall y (S(x) \rightarrow (f(y) \rightarrow c)) \rightarrow (\exists u \neg T(u) \wedge \exists v \neg S(v))$$

$$\# \exists x \forall y (S(x) \rightarrow (f(y) \rightarrow c)) \rightarrow \exists u \exists v (\neg T(u) \wedge \neg S(v))$$

$$\# \exists x \forall y \exists u \exists v ((S(x) \rightarrow (f(y) \rightarrow c)) \rightarrow (\neg T(u) \wedge \neg S(v)))$$

$$P = (\exists x A(x) \rightarrow \forall y (f(y) \vee c)) \wedge (\exists y (g(y) \rightarrow \neg \exists x B(x)))$$

$$\models \forall x \forall y (A(x) \rightarrow (f(y) \vee c)) \wedge \neg (\exists a (g(a) \rightarrow \forall b \neg B(b)))$$

$$\models \forall x \forall y (A(x) \rightarrow (f(y) \vee c)) \wedge \neg (\exists a \forall b (g(a) \rightarrow \neg B(b)))$$

$$\models \forall x \forall y (A(x) \rightarrow (f(y) \vee c)) \wedge \forall a \exists b \neg (g(a) \rightarrow \neg B(b))$$

$$\models \forall x \forall y \forall a \exists b ((A(x) \rightarrow (f(y) \vee c)) \wedge \neg (g(a) \rightarrow \neg B(b)))$$

$$\psi = \forall x \left(\exists u R(u, x) \wedge \exists u T(u) \wedge \neg F(x) \right) \rightarrow \left(\neg \exists y S(y) \vee \exists z \neg T(z) \right)$$

$$\equiv \forall x \left((\exists v R(v, x) \wedge \exists u T(u)) \wedge \neg F(x) \right) \rightarrow (\forall y \neg S(y) \vee \exists z \neg T(z))$$

$$\equiv \forall x \left(\exists v \exists u (R(v, x) \wedge T(u)) \wedge \neg F(x) \right) \rightarrow \forall y \exists z (\neg S(y) \vee \neg T(z))$$

$$\equiv \forall x \exists v \exists u (R(v, x) \wedge T(u) \wedge \neg F(x)) \rightarrow \forall y \exists z (\neg S(y) \vee \neg T(z))$$

$$\equiv \forall x \exists v \exists u \forall y \exists z ((R(v, x) \wedge T(u) \wedge \neg F(x)) \rightarrow (\neg S(y) \vee \neg T(z)))$$