$$\begin{array}{cccc} \Gamma & & ::= & & \text{typing context} \\ & | & \cdot & & \text{empty context} \\ & | & \Gamma, x:T & & \text{cons} \end{array}$$

 $T_1 \sim_U T_2$ T_1 can can be converted into T_2

 $T_1 \sim T_2$ T_1 is consistent with T_2

$$\overline{T \sim T}$$
 CS_REFL

$$\begin{array}{ccc} \overline{?} \sim T & \text{CS_UL} \\ \hline T \sim ? & \text{CS_UR} \\ \hline \hline T_1 \sim_U T_2 & \text{CS_CONV} \\ \hline T_1 \sim T_2 & \text{CS_CONV} \\ \hline T_1 \sim T_1' & \\ \hline (T_1 \times T_2) \sim (T_1' \times T_2) & \text{CS_PAIR1} \\ \hline T_2 \sim T_2' & \\ \hline (T_1 \times T_2) \sim (T_1 \times T_2') & \text{CS_PAIR2} \\ \hline \hline T_1 \sim T_1' & \\ \hline (T_1 \rightarrow T_2) \sim (T_1' \rightarrow T_2) & \text{CS_FUN1} \\ \hline T_2 \sim T_2' & \\ \hline (T_1 \rightarrow T_2) \sim (T_1 \rightarrow T_2') & \text{CS_FUN2} \\ \hline \end{array}$$

$\Gamma \vdash t : T$ t has type T in context Γ

$$\frac{x:T\in\Gamma}{\Gamma\vdash x:T} \quad \text{VAR}$$

$$\frac{\Gamma\vdash x:T}{\Gamma\vdash ():1} \quad \text{UNIT}$$

$$\frac{\Gamma\vdash 0:\mathbb{N}}{\Gamma\vdash 0:\mathbb{N}} \quad \text{ZERO}$$

$$\frac{\Gamma\vdash t:\mathbb{N}}{\Gamma\vdash \text{succ }t:\mathbb{N}} \quad \text{SUCC}$$

$$\frac{\Gamma\vdash t_1:T_1 \quad \Gamma\vdash t_2:T_2}{\Gamma\vdash (t_1,t_2):T_1\times T_2} \quad \text{PAIR}$$

$$\frac{\Gamma\vdash t:T_1\times T_2}{\Gamma\vdash \text{proj}_1 t:T_1} \quad \text{PROJ1}$$

$$\frac{\Gamma\vdash t:T_1\times T_2}{\Gamma\vdash \text{proj}_2 t:T_2} \quad \text{PROJ2}$$

$$\frac{\Gamma,x:T_1\vdash t:T_2}{\Gamma\vdash \lambda x:T_1.t:T_1\to T_2} \quad \text{ABS}$$

$$\frac{\Gamma\vdash t_1:T_3 \quad \Gamma\vdash t_2:T_4 \quad T_3\sim_U (T_1\to T_2) \quad T_4\sim_U T_1}{\Gamma\vdash t_1 t_2:T_2}$$

$$\frac{\Gamma\vdash t_1:T_1\to T_2 \quad \Gamma\vdash t_2:T_3 \quad T_3\sim T_1}{\Gamma\vdash t_1 t_2:T_2} \quad \text{APP}$$

 $|t_1 \leadsto t_2|$ t_1 reduces to t_2

Definition rules: 31 good 0 bad Definition rule clauses: 49 good 0 bad