```
\boldsymbol{x}
                                                                                  triv
                                                                                  box
                                                                                  unbox
                                                                                  \Lambda(X <: A).t
                                                                                  [A]t
                                                                                  \lambda(x:A).t
                                                                                  t_1 t_2
                                                                                  (t_1, t_2)
                                                                                  \mathsf{fst}\;t
                                                                                  \mathsf{snd}\; t
                                                                                  \mathsf{succ}\ t
                                                                                  case t of t_3 \rightarrow t_1, t_4 \rightarrow t_2
                                                                                  t :: t'
                                                                                                                                              S
                                                                                  (t)
  K
                                                                     ::=
  A,\ B,\ C,\ D,\ E,\ S,\ U
                                                                                  X
                                                                                  \mathsf{List}\,A
                                                                                  \forall (X <: A).B
                                                                                  SL
                                                                                  Unit
                                                                                  Nat
                                                                                  \begin{array}{c} A_1 \rightarrow A_2 \\ A_1 \times A_2 \end{array}
                                                                                                                                              S
  Γ
                                                                                 \begin{array}{l} \Gamma, X <: A \\ \Gamma, x : A \end{array}
\Gamma \vdash A : \star
                                                                             \frac{\Gamma_1 \vdash A : \star}{\Gamma_1, X <: A, \Gamma_2 \vdash X : \star}
                                                                                                                         K_{\text{-}UNIT}
                                                                                         \overline{\Gamma \vdash \mathsf{Unit} : \star}
                                                                                                                         K_{-}NAT
                                                                                          \overline{\Gamma \vdash \mathsf{Nat} : \star}
```

::=

termvar, x, y, z, f typevar, X, Y, Z index, i, j, kt, c, v, s, n

$$\frac{\Gamma \vdash R : \star}{\Gamma \vdash L \text{ist } A : \star} \quad \text{K_LIST}$$

$$\frac{\Gamma \vdash A : \star}{\Gamma \vdash L \text{ist } A : \star} \quad \text{K_LIST}$$

$$\frac{\Gamma \vdash A : \star}{\Gamma \vdash A \to B : \star} \quad \text{K_ARROW}$$

$$\frac{\Gamma \vdash A : \star}{\Gamma \vdash A \times B : \star} \quad \text{K_PROD}$$

$$\frac{\Gamma, X <: A \vdash B : \star}{\Gamma \vdash \forall (X <: A).B : \star} \quad \text{K_FORALL}$$

 $\Gamma \operatorname{Ok}$

$$\frac{\Gamma \text{ Ok} \quad \Gamma \vdash A : \star}{(\Gamma, X <: A) \text{ Ok}} \quad \text{OK_TYPEVAR}$$

$$\frac{\Gamma \text{ Ok} \quad \Gamma \vdash A : \star}{(\Gamma, x : A) \text{ Ok}} \quad \text{OK_VAR}$$

 $\Gamma \vdash A \mathrel{<:} B$

$$\frac{\Gamma \text{ Ok}}{\Gamma \vdash A <: A} \quad \text{S_REFL}$$

$$\frac{\Gamma \vdash A <: B \quad \Gamma \vdash B <: C}{\Gamma \vdash A <: C} \quad \text{S_TRANS}$$

$$\frac{X <: A \in \Gamma \quad \Gamma \text{ Ok}}{\Gamma \vdash X <: A} \quad \text{S_DVAR}$$

$$\frac{\Gamma \text{ Ok}}{\Gamma \vdash A <: T} \quad \text{S_DATS}$$

$$\frac{\Gamma \text{ Ok}}{\Gamma \vdash \text{ Nat} <: \text{SL}} \quad \text{S_DATS}$$

$$\frac{\Gamma \text{ Ok}}{\Gamma \vdash \text{ Unit} <: \text{SL}} \quad \text{S_DATS}$$

$$\frac{\Gamma \text{ Ok}}{\Gamma \vdash \text{ Unit} <: \text{SL}} \quad \text{S_DATS}$$

$$\frac{\Gamma \vdash A <: \text{SL}}{\Gamma \vdash \text{ Unit} <: \text{SL}} \quad \text{S_DATS}$$

$$\frac{\Gamma \vdash A <: \text{SL}}{\Gamma \vdash \text{ Init} \land A <: \text{SL}} \quad \text{S_DATS}$$

$$\frac{\Gamma \vdash A <: \text{SL}}{\Gamma \vdash (A \to B) <: \text{SL}} \quad \text{S_DATS}$$

$$\frac{\Gamma \vdash A <: \text{SL}}{\Gamma \vdash (A \to B) <: \text{SL}} \quad \text{S_DATS}$$

$$\frac{\Gamma \vdash A <: \text{SL}}{\Gamma \vdash (A \to B) <: \text{SL}} \quad \text{S_DATS}$$

$$\frac{\Gamma \vdash A <: \text{SL}}{\Gamma \vdash (A \to B) <: \text{SL}} \quad \text{S_DATS}$$

$$\frac{\Gamma \vdash A <: \text{SL}}{\Gamma \vdash (A \to B) <: \text{SL}} \quad \text{S_DATS}$$

$$\frac{\Gamma \vdash A <: B}{\Gamma \vdash (\text{List } A) <: (\text{List } B)} \quad \text{S_DATS}$$

$$\frac{\Gamma \vdash A_1 <: A_2 \quad \Gamma \vdash B_1 <: B_2}{\Gamma \vdash (A_1 \times B_1) <: (A_2 \times B_2)} \quad \text{S_DATS}$$

$$\frac{\Gamma \vdash A_2 <: A_1 \quad \Gamma \vdash B_1 <: B_2}{\Gamma \vdash (A_1 \to B_1) <: (A_2 \to B_2)} \quad \text{S_DATS}$$

$$\frac{\Gamma, X <: A \vdash B_1 <: B_2}{\Gamma \vdash (\forall (X <: A).B_1) <: (\forall (X <: A).B_2)} \quad \text{S_FORALL}$$

$\Gamma \vdash A \sim B$

$\Gamma \vdash t : A$

$$\frac{x:A\in\Gamma\ \Gamma\operatorname{Ok}}{\Gamma\vdash x:A}\quad \operatorname{VarP}$$

$$\overline{\Gamma\vdash \operatorname{box}:\forall(X<:\operatorname{SL}).(X\to?)}\quad \operatorname{Box}$$

$$\overline{\Gamma\vdash \operatorname{unbox}:\forall(X<:\operatorname{SL}).(?\to X)}\quad \operatorname{Unbox}$$

$$\frac{\Gamma\operatorname{Ok}}{\Gamma\vdash \operatorname{triv}:\operatorname{Unit}}\quad \operatorname{UnitP}$$

$$\frac{\Gamma\operatorname{Ok}}{\Gamma\vdash 0:\operatorname{Nat}}\quad \operatorname{ZEROP}$$

$$\frac{\Gamma\vdash t:A\quad \operatorname{nat}(A)=\operatorname{Nat}}{\Gamma\vdash \operatorname{succ}\,t:\operatorname{Nat}}\quad \operatorname{SUCC}$$

$$\frac{\Gamma\vdash t:C\quad \operatorname{nat}(C)=\operatorname{Nat}}{\Gamma\vdash t_1:A\quad \Gamma,x:\operatorname{Nat}\vdash t_2:A}\quad \operatorname{NCASE}$$

$$\frac{\Gamma\operatorname{Ok}\quad \Gamma\vdash A:\star}{\Gamma\vdash (\operatorname{case}\,t\:\operatorname{of}\,0\to t_1,(\operatorname{succ}\,x)\to t_2:A}\quad \operatorname{NCASE}$$

$$\frac{\Gamma\operatorname{Ok}\quad \Gamma\vdash A:\star}{\Gamma\vdash 1:A_1\quad \Gamma\vdash t_2:\operatorname{List}\,A_2}\quad \operatorname{EMPTY}$$

$$\frac{\Gamma\vdash t_1:A_1\quad \Gamma\vdash t_2:\operatorname{List}\,A_2}{\Gamma\vdash t_1:t_2:\operatorname{List}\,A_2}\quad \operatorname{CONS}$$

$$\frac{\Gamma\vdash t_1:A_1\quad \Gamma\vdash t_2:A_2}{\Gamma\vdash (t_1,t_2):A_1\times A_2}\quad \operatorname{PAIR}$$

$$\frac{\Gamma,x:A\vdash t:B}{\Gamma\vdash \lambda(x:A).t:A\to B}\quad \operatorname{LAM}$$

$$\frac{\Gamma,X<:A\vdash t:B}{\Gamma\vdash \Lambda(X<:A).t:\forall(X<:A).B}\quad \operatorname{LAM}$$

$$\frac{\Gamma \vdash t_1 \Rightarrow t_2 : A \times B}{\Gamma \vdash \operatorname{snd} t_1 \Rightarrow \operatorname{snd} t_2 : B} \quad \operatorname{CLSND}$$

$$\overline{\Gamma \vdash [] \Rightarrow [] : \forall (X <: \top).\operatorname{List} X} \quad \operatorname{CLEMPTY}$$

$$\frac{\Gamma \vdash t_1 \Rightarrow t_1' : A_1 \quad \Gamma \vdash t_2 \Rightarrow t_2' : \operatorname{List} A_2 \quad \Gamma \vdash A_1 \sim A_2 \quad \operatorname{caster}(A_1, A_2) = c}{\Gamma \vdash (t_1 :: t_2) \Rightarrow ((c \ t_1') :: t_2') : \operatorname{List} A} \quad \operatorname{CL-CONS}$$

$$\frac{\Gamma \vdash t_1 \Rightarrow t_1' : B \quad \Gamma, x : ?, y : \operatorname{List} ? \vdash t_2 \Rightarrow t_2' : B}{\Gamma \vdash (\operatorname{case} t \text{ of } [] \to t_1, (x :: y) \to t_2) \Rightarrow (\operatorname{case} (\operatorname{split}_{(\operatorname{List}?)} t') \text{ of } [] \to t_1', (x :: y) \to t_2') : B} \quad \operatorname{CLLCASEU}$$

$$\frac{\Gamma \vdash t \Rightarrow t : \operatorname{List} A}{\Gamma \vdash (\operatorname{case} t \text{ of } [] \to t_1, (x :: y) \to t_2) \Rightarrow (\operatorname{case} t') \text{ of } [] \to t_1', (x :: y) \to t_2') : B} \quad \operatorname{CLLCASE}$$

$$\frac{\Gamma \vdash t_1 \Rightarrow t_1' : B \quad \Gamma, x : A, y : \operatorname{List} A \vdash t_2 \Rightarrow t_2' : B}{\Gamma \vdash (\operatorname{case} t \text{ of } [] \to t_1, (x :: y) \to t_2) \Rightarrow (\operatorname{case} t') \text{ of } [] \to t_1', (x :: y) \to t_2') : B} \quad \operatorname{CLLCASE}$$

$$\frac{\Gamma \vdash t_1 \Rightarrow t_1' : B \quad \Gamma, x : A, y : \operatorname{List} A \vdash t_2 \Rightarrow t_2' : B}{\Gamma \vdash (\operatorname{case} t \text{ of } [] \to t_1, (x :: y) \to t_2') : B} \quad \operatorname{CLLCASE}$$

$$\frac{\Gamma \vdash t_1 \Rightarrow t_1' : B \quad \Gamma, x : A, y : \operatorname{List} A \vdash t_2 \Rightarrow t_2' : B}{\Gamma \vdash (\operatorname{List} A, t_1).t_1 \Rightarrow \lambda(x : A_1).t_2 : A_1 \to A_2} \quad \operatorname{CLLAM}$$

$$\frac{\Gamma \vdash t_1 \Rightarrow t_1' : ?}{\Gamma \vdash t_1 \Rightarrow t_1' : ?} \quad \operatorname{CLLAM}$$

$$\frac{\Gamma \vdash t_1 \Rightarrow t_2' : A_2}{\Gamma \vdash t_1 \Rightarrow t_1' : A_1 \to B \quad \Gamma \vdash A_2 \sim A_1 \quad \operatorname{caster}(A_2, A_1) = c}{\Gamma \vdash t_1 \Rightarrow t_1' : A_1 \to B \quad \Gamma \vdash A_2 \sim A_1 \quad \operatorname{caster}(A_2, A_1) = c} \quad \operatorname{CLAPP}$$

$$\frac{\Gamma, X : A \vdash t_1 \Rightarrow t_2 : B}{\Gamma \vdash (\Lambda(X <: A).t_1) \Rightarrow (\Lambda(X <: A).t_2) : \forall (X <: A).B} \quad \operatorname{CLLAM}$$

$$\frac{\Gamma \vdash t_1 \Rightarrow t_2 : \forall (X <: B).C \quad \Gamma \vdash A <: B}{\Gamma \vdash ([A]t_1) \Rightarrow ([A]t_2) : [A/X]C} \quad \operatorname{CLTYPEAPP}$$

Definition rules: 72 good 0 bad Definition rule clauses: 139 good 0 bad