```
termvar, x
index, k
         ::=
                                        \operatorname{term}
                                           variable
                  \boldsymbol{x}
                  triv
                                            unit
                  \lambda x : T.t
                                           \lambda-abstraction
                                           function application
                  t_1 t_2
                                           pair constructor
                  (t_1, t_2)
                  \mathsf{fst}\;t
                                           first projection
                  \mathsf{snd}\; t
                                           second projection
                  \mathsf{succ}\ t
                                           successor function
                  (t)
                                  S
```

$$\begin{array}{cccc} \Gamma & & ::= & & & \text{typing context} \\ & | & \cdot & & \text{empty context} \\ & | & \Gamma, x:T & & \text{cons} \end{array}$$

 $T_1 \sim_U T_2$ T_1 can can be converted into T_2

 $T_1 \sim T_2$ T_1 is consistent with T_2

$$\overline{T \sim T}$$
 CS_REFL

$$\begin{array}{ccc} & \overline{?} \sim T & \text{CS_UL} \\ & \overline{T} \sim ? & \text{CS_UR} \\ & & \frac{T_1 \sim_U T_2}{T_1 \sim T_2} & \text{CS_CONV} \\ & & \frac{T_1 \sim T_1'}{(T_1 \times T_2) \sim (T_1' \times T_2)} & \text{CS_PAIR1} \\ & & \frac{T_2 \sim T_2'}{(T_1 \times T_2) \sim (T_1 \times T_2')} & \text{CS_PAIR2} \\ & & \frac{T_1 \sim T_1'}{(T_1 \to T_2) \sim (T_1' \to T_2)} & \text{CS_FUN1} \\ & & \frac{T_2 \sim T_2'}{(T_1 \to T_2) \sim (T_1 \to T_2')} & \text{CS_FUN2} \end{array}$$

$\Gamma \vdash t : T$ t has type T in context Γ

$$\frac{x:T\in\Gamma}{\Gamma\vdash x:T}\quad\text{VAR}$$

$$\overline{\Gamma\vdash triv:1}\quad\text{UNIT}$$

$$\overline{\Gamma\vdash t:\mathbb{N}}\quad\text{ZERO}$$

$$\frac{\Gamma\vdash t:\mathbb{N}}{\Gamma\vdash \text{succ }t:\mathbb{N}}\quad\text{SUCC}$$

$$\frac{\Gamma\vdash t_1:T_1\quad\Gamma\vdash t_2:T_2}{\Gamma\vdash (t_1,t_2):T_1\times T_2}\quad\text{PAIR}$$

$$\frac{\Gamma\vdash t:T_1\times T_2}{\Gamma\vdash \text{fst }t:T_1}\quad\text{FST}$$

$$\frac{\Gamma\vdash t:T_1\times T_2}{\Gamma\vdash \text{snd }t:T_2}\quad\text{SND}$$

$$\frac{\Gamma,x:T_1\vdash t:T_2}{\Gamma\vdash \lambda x:T_1.t:T_1\to T_2}\quad\text{ABS}$$

$$\frac{\Gamma\vdash t:T_1\quad T_1\sim_U T_2}{\Gamma\vdash t:T_2}\quad\text{U}$$

$$\frac{\Gamma\vdash t_1:T_1\to T_2\quad\Gamma\vdash t_2:T_3\quad T_3\sim T_1}{\Gamma\vdash t_1t_2:T_2}\quad\text{APP}$$

 $t_1 \rightsquigarrow t_2$ t_1 reduces to t_2

Definition rules: 31 good 0 bad Definition rule clauses: 49 good 0 bad