

Package ‘s525’

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Type Package

Title Implementation of common Bayesian models

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Description This package contains implementations of common Bayesian models.

Imports truncdist, MASS, coda

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s525-package	<i>Implementation of common Bayesian models</i>
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Description

This package contains implementations of common Bayesian models.

Details

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Examples

```
# simple examples of the most important functions
```

horseshoe_regression *Gibbs Sampler for Horseshoe Regression*

Description

The horseshoe regression model is given by

$$\begin{aligned} [y_i | x_i, \beta, \sigma] &\sim N(x_i^t \beta, \sigma^2), i = 1, \dots, n, \\ [\beta_j | \sigma, \lambda_j] &\sim N(0, \sigma^2 \lambda_j^2), \\ [\lambda_j | A] &\sim C^+(0, A), \\ A &\sim Uniform(0, 10), \\ p(\sigma^2) &\propto \frac{1}{\sigma^2}. \end{aligned}$$

The half-Cauchy parameter expansion is used; given by

$$\begin{aligned} [\eta_j | \gamma_j] &\sim Gamma(\frac{1}{2}, \gamma_j), \\ [\gamma_j] &\sim Gamma(\frac{1}{2}, \frac{1}{A^2}). \end{aligned}$$

Let $\eta_j = \lambda_j^{-2}$, $\tau_A = A^{-2}$, $\tau = \frac{1}{\sigma^2}$ and $\Lambda = diag(\eta_1, \dots, \eta_p)$. The full conditionals are given by:

$$\begin{aligned} [\beta | Y, X, \eta, \tau] &\sim \mathcal{N}((X'X + \Lambda)^{-1} X'Y, \tau^{-1} (X'X + \Lambda)^{-1}), \\ [\eta_j | \beta_j, \gamma_j, \tau] &\sim \exp(-\frac{\tau \beta_j^2}{2} + \gamma_j), \\ [\gamma_j | \eta_j, \tau_A] &\sim \exp(\eta_j + \tau_A), \\ [\tau_A | \gamma] &\sim Gamma(\frac{p-1}{2}, \sum \gamma_i) I_{(\frac{1}{100}, \infty)}, \\ [\tau | Y, X, \beta, \eta] &\sim Gamma(\frac{n+p}{2}, \frac{(y - X\beta)'(y - X\beta) + \beta' \Lambda \beta}{2}). \end{aligned}$$

Usage

```
horseshoe_regression <- function(  
  Y,  
  X,  
  niter = 10000)
```

Arguments

Y	n by 1
X	n by p predictor matrix
niter	number of gibbs sampling iterations

Details

This function returns the generated parameters from the gibbs sampling markov chain.

Value

beta	An niter x p matrix
lambda	An niter x p matrix
sigma	An niter x 1 matrix

Examples

```
# Load the data  
prostate.data = "https://web.stanford.edu/~hastie/ElemStatLearn/datasets/prostate.data"  
prostate = read.table(file = "prostate.data", sep="", header = TRUE)  
# Training data:  
prostate_train = prostate[which(prostate$train),-10]  
# Testing data:  
prostate_test = prostate[which(!prostate$train),-10]  
# Response:  
y = prostate_train$lpsa  
# Center and scale the data:  
y = scale(y)  
# And the predictors  
X = scale(prostate_train[,names(prostate_train) != "lpsa"])  
  
gibbs_hs <- horseshoe_regression(y, X, niter=10000)  
shrinkage_regression_plot(gibbs_hs$beta, y, X)
```

metropolis

Metropolis MCMC

Description

The metropolis algorithm is a special case of the metropolis-hastings algorithm, namely where the proposal distribution is symmetric.

Usage

```
metropolis <- function(
  rproposal,
  prob,
  niter,
  init,
  log_prob = FALSE)
```

Arguments

rproposal	rproposal(previous_val) generates a value from the proposal distribution
prob	prob(val_proposed)/prob(val_t_minus_1) forms the acceptance probability
niter	number of iterations to perform
init	vector of initial values
log_prob	whether or not prob function specifies log probabilities

Details

This function returns a niter x d matrix of values where d is the dimension of init and the dimension of each element from rproposal. The returned matrix contains all generated values of the metropolis walk.

Examples

```
vals <- metropolis(
  rproposal = function(val){ rnorm(1, mean = val, sd = 1){} },
  prob = posterior_prob,
  niter = 10000,
  init = 0)

library(coda)
plot(as.mcmc(vals))
```

Description

The probit regression model is given by

$$y_i | \pi_i \sim \text{Bernoulli}(\pi_i),$$

$$\pi_i = \Phi(x_i^t \beta),$$

$$\beta_j \sim N(0, A^2).$$

where Φ is given by the gaussian CDF.

The implemented parameter-expanded model is given by

$$y_i^* = x_i^t \beta + \epsilon_i,$$

$$\epsilon_i \sim N(0, 1),$$

$$y_i = I(y_i^* > 0).$$

The full conditional distributions are given by

$$[\beta | y, y^*, X] \sim N(Q^{-1}l, Q^{-1})$$

where $Q = X^t X + A^{-2}I$ and $l = X^t y^*$,

$$[y_i | y_i^*, \beta, X] \sim \text{sgn}(y_i, y_i^*) N(x_i^t \beta, 1)$$

where sgn is 1 if both arguments are of the same sign and zero otherwise.

Usage

```
probit_regression <- function(
  Y,
  X,
  niter,
  A = 3)
```

Arguments

Y	n by 1 vector of ones and zeros
X	n by p predictor matrix
niter	number of gibbs sampling iterations
A	A parameter. The default value is chosen to provide a reasonable range of π .

Details

This function returns a niter x p matrix of values where p is the second dimension of the predictor matrix X. The returned matrix contains all generated values of the gibbs sampling markov chain.

Examples

```
library(LearnBayes)
library(s525)

data(donner)
y = donner$survival
X = cbind(1, donner$age, donner$male)
niter <- 2000

gibbs_results <- probit_regression(y, X, niter)
```

ridge_regression

Gibbs Sampler for Ridge Regression

Description

The ridge regression model coefficients are given by

$$\arg \min_{\beta} \| Y - X\beta \|^2 + \lambda \| \beta \|^2 .$$

This is the implementation of the bayesian interpretation. Namely,

$$[y_i | x_i, \beta, \tau] \sim N(x_i^t \beta, \tau^{-1}), i = 1, \dots, n,$$

$$[\beta | \eta] \sim N(0, \eta^{-1} I),$$

$$\tau \sim \text{Gamma}(\frac{1}{100}, \frac{1}{100}),$$

$$\sigma_{\beta} \sim \text{unif}(0, A)$$

where $A = 1000$ and $\tau = \frac{1}{\sigma_{\beta}^2}$.

Usage

```
ridge_regression <- function(
  Y,
  X,
  niter = 10000)
```

Arguments

Y	n by 1
X	n by p predictor matrix
niter	number of gibbs sampling iterations

Details

This function returns the generated parameters from the gibbs sampling markov chain.

Value

beta	An niter by p matrix
sigma	An niter by 1 matrix
sigma_beta	An niter by 1 matrix

Examples

```
# Load the data
prostate.data = "https://web.stanford.edu/~hastie/ElemStatLearn/datasets/prostate.data"
prostate = read.table(file = "prostate.data", sep=" ", header = TRUE)
# Training data:
prostate_train = prostate[which(prostate$train),-10]
# Testing data:
prostate_test = prostate[which(!prostate$train),-10]
# Response:
y = prostate_train$lpsa
# Center and scale the data:
y = scale(y)
# And the predictors
X = scale(prostate_train[,names(prostate_train) != "lpsa"])

gibbs_ridge <- ridge_regression(y, X, niter=10000)
shrinkage_regression_plot(gibbs_ridge$beta, y, X, main = "Ridge Prior")
```

shrinkage_regression_plot

Plot the MC chain of regression coefficients compared to OLS.

Description

Plot the MC chain of regression coefficients compared to OLS using 95% HPD confidence intervals.

Usage

```
horseshoe_regression_plot <- function(
  beta,
  Y,
  X,
  main = "Horseshoe Prior",
  ylim = NULL)
```

Arguments

beta	n x p MCMC chain of beta coefficients.
Y	Y values used to generate beta; used as input to OLS regression
X	X values used to generate beta; used as input to OLS regression
main	Title of the plot
ylim	y range of plot

Examples

```
# Load the data
prostate.data = "https://web.stanford.edu/~hastie/ElemStatLearn/datasets/prostate.data"
prostate = read.table(file = "prostate.data", sep="", header = TRUE)
# Training data:
prostate_train = prostate[which(prostate$train),-10]
# Testing data:
prostate_test = prostate[which(!prostate$train),-10]
# Response:
y = prostate_train$lpsa
# Center and scale the data:
y = scale(y)
# And the predictors
X = scale(prostate_train[,names(prostate_train) != "lpsa"])

gibbs_hs <- horseshoe_regression(y, X, niter=10000)
shrinkage_regression_plot(gibbs_hs$beta, y, X)
```

silly

A silly and useless function

Usage

```
silly(x)
```

Arguments

```
x
```

Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (x)
{
  x + 3
}
```


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