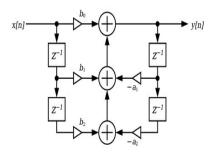
Goal: To determine the time domain response of the transfer function

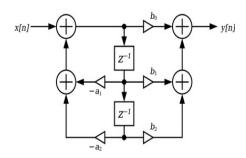
The transfer function for a linear, time-invariant, digital filter can be expressed as a transfer function in the Z-domain; if it is causal, then it has the form:^[1]

$$H(z) = rac{B(z)}{A(z)} = rac{b_0 + b_1 z^{-1} + b_2 z^{-2} + \dots + b_N z^{-N}}{1 + a_1 z^{-1} + a_2 z^{-2} + \dots + a_M z^{-M}}$$

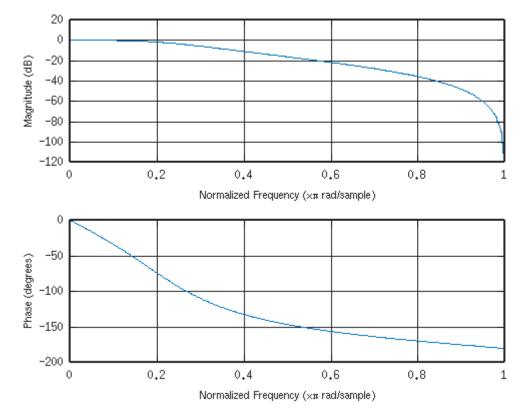
Direct Form 1



Direct Form II



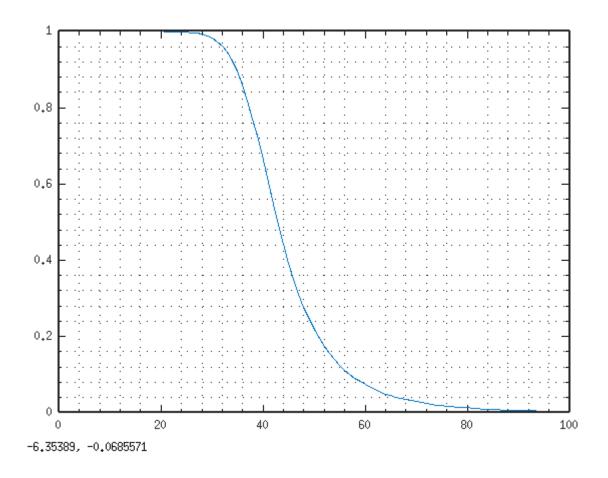
Octave filter



-0.167980, -265.000

https://www.youtube.com/watch?v=vikFFw6Hn0o

```
Adding to buttr from video above \%|H(w)| = Ao/sqrt(1+(w/wo)2n ff = (0:1000-1)*T; ww = 2*pi*ff; pow = 2*order; ww = (ww/nf); ww = (ww/nf); ww = ww(1:1000).^pow; ww = sqrt(ww + 1); ww = (ww).^-1; figure %subplot(2,1,1) plot((1:100),ww(1:100)) grid minor on
```

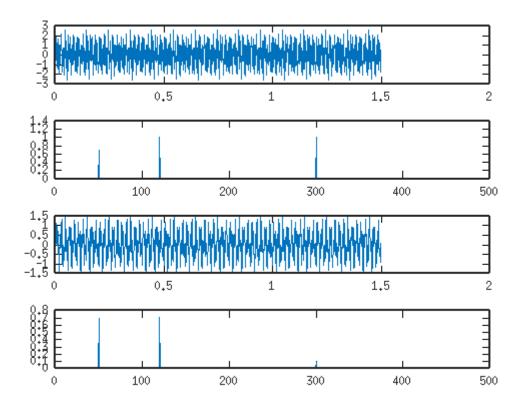


Testcase The first signal x is 3 sine waves 50, 120, and 300 Hz

The 2^{nd} is the FFT of the signal x.

The 3^{rd} is the filterd with the Butterworth filter.

The 4^{th} show that only the 50 & 120 Hz are present.



421,525, 4,77541

Starting first with order 2 a = 1.00000 -0.98241 0.34767

 $b = 0.091315 \quad 0.182630 \quad 0.091315$

[A,B,C,D] = tf2ss(b,a);

A =

5.5511e-17 3.4767e-01 -1.0000e+00 9.8241e-01

B =

-0.059568 0.272338

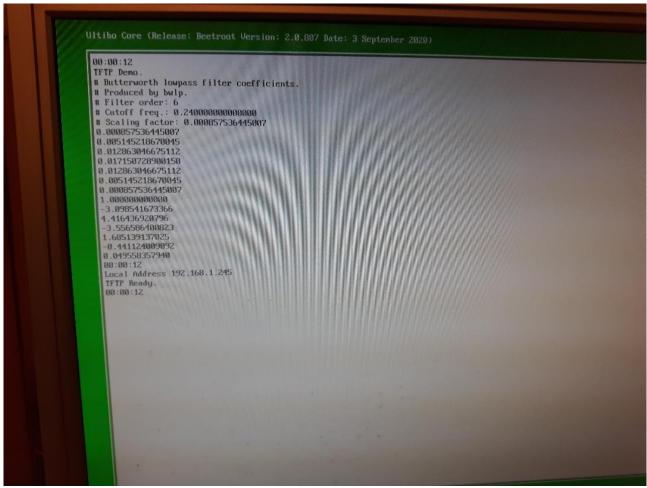
C =

0 1

D = 0.091315

butt6120lp normalize freq nf = 0.24000 zeros ans =

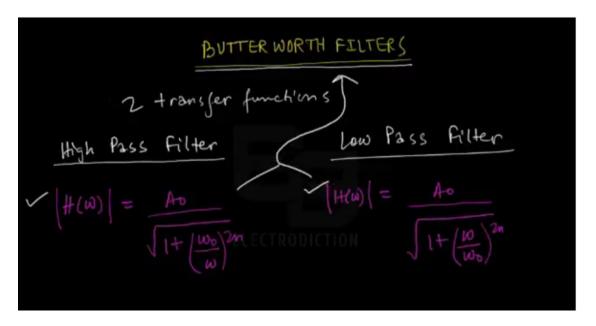
```
-1
 -1
 -1
 -1
 -1
 -1
poles
ans =
 0.61925 + 0.56170i
  0.49120 + 0.32617i
 0.43881 + 0.10665i
 0.43881 - 0.10665i
 0.49120 - 0.32617i
 0.61925 - 0.56170i
theta =
 0.73670
  0.58617
 0.23842
 -0.23842
 -0.58617
 -0.73670
b
b =
Columns 1 through 6:
 0.00085754 \quad 0.00514522 \quad 0.01286305 \quad 0.01715073 \quad 0.01286305 \quad 0.00514522
Column 7:
 0.00085754
a
a =
  1.000000 -3.098542 4.416437 -3.556586 1.685139 -0.441124 0.049558
```



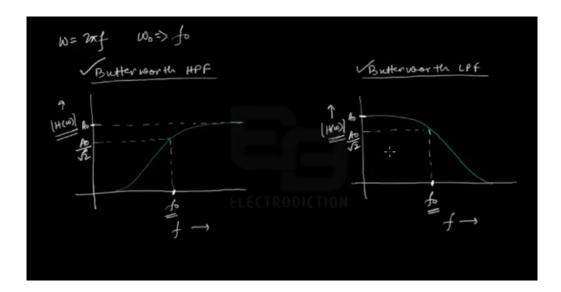
FFT 50 120 300

```
delta f 0.48828125
                  samples
                                 2048 fs
                                              1000
sample = 10*(\sin(2*pi*50*t[i]) + \sin(2*pi*120*t[i]) + \sin(2*pi*300*t[i])); //no DC
  2.104689,
              0.000000
                          102
                                 49.8046875
  7.311564,
              0.000000
                          103
  4.836622,
              0.000000
                          104
              0.000000
                          246
(
  2.750056,
                                 120.1171875
              0.000000
                          247
  8.715654,
  1.689716,
              0.000000
                          248
  2.071553,
              0.000000
                          614
                                 299.8046875
  7.257226,
              0.000000
                          615
  4.845451,
              0.000000
                          616
```

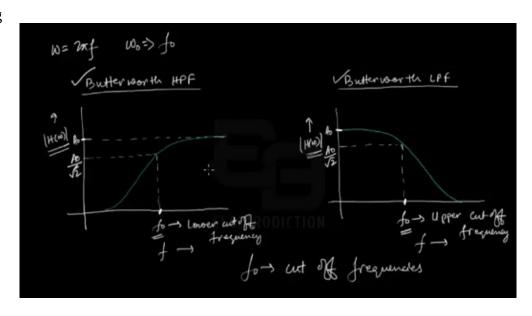
https://www.youtube.com/watch?v=vikFFw6Hn0o



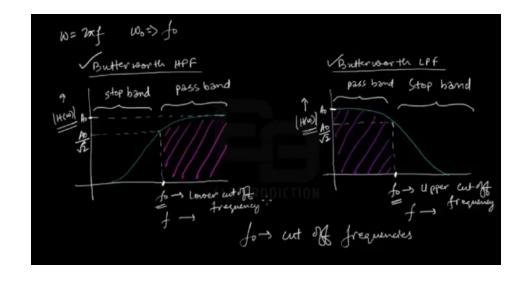
Ao Maximum gain in passbands |H(w)| normalized gain w = 2pif wo = fo wo Lower cutoff angular frequency (HPF) upper cutoff angular frequency (LPF) angular frequency of input signal n order(interger 1,2,3...)

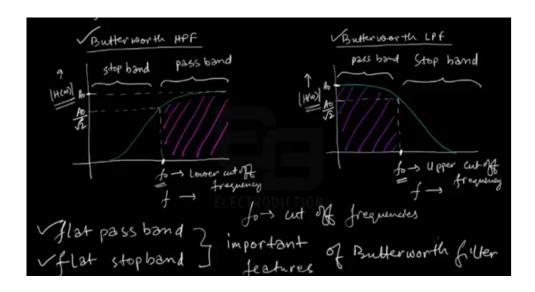


bw2.png



bw3.png





bw5.png

