TAX EVASION ON A SOCIAL NETWORK

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- 4. Responses to Intervention
- 5. Conclusions



COMPLIANCE AND REFERENCE DEPENDENCE

- → We relate non compliant behaviour to a body of evidence on the importance of positional concerns (keeping up with the Jones)
- → Tax evasion may be used to improve agents' relative standing
- → As a consequence, the choice on how much to evade is affected by social interaction
- → New project studying tax evasion that builds on a previous TARC project on tax avoidance

→ Tax evasion causes significant losses of public revenues (4.4 bn. £ in UK)

→ Growing interest by tax agencies on understanding evasion so to design efficient deterrence measures

Rich literature using different approaches to study evasion decision and optimal policies

RELATED LITERATURE

- → Kahneman and Tversky 1979 Reference dependence of utility
- → Gali 1994 "Keeping up with the Jones"
- → Myles and Naylor 1996
 Tax evasion and group conformity
- → Bianconi and Barabási 2001 Social network modelling
- → Alm , Bloomquist, McKee 2017 Peer effects in compliance decision

Introduction Model Optimal Evasion Responses to Intervention Conclusions

MODELLING FEATURES

Provide a model where:

- → Agents differ in income, reference group and probability of detection
- → Taxpayers may engage in risky tax evasion
- → **Self** and **social** comparison shape the reference income
- → **Social** comparison depends on agents' **social network**

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RESEARCH QUESTIONS

- → Our analysis has focused on **four** questions:
 - Is it possible to characterize optimal evasion and how do changes in the exogenous parameters (income, risk aversion, etc.) affect it?
 - 2. Is self comparison able to replicate the dynamic profile of the response of evasion to an effective anti-evasion intervention as observed empirically?
 - 3. Is it possible to characterize the direct and indirect **revenue effects** of interventions?
 - 4. How much does the availability of more information (especially related to social network) improves the capacity of a tax authority to infer revenue effects?



MODELLING OF EVASION

- \rightarrow We define evasion E_{it} as the **liabilities under-declarerd** by taxpayer i at time t
- → Evasion is a **risky** activity:
 - → The tax agency may detect evasion
 - ightarrow If evasion is detected, a **fine** f proportional to the evaded tax debt is also imposed

TAX AGENCY ACTIVITY

- → The **tax agency** is assumed to be actively seeking to detect and **shut-down** evasion
- \rightarrow There is a (compound) probability, p_i , that
 - \rightarrow Taxpayer *i* is discovered under declaring
 - → The tax agency is successful in recovering revenues

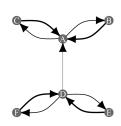
TAXPAYERS CHARACTERISTICS

- → Taxpayers are **distinguished** by:
 - \rightarrow Exogenous Income W_i
 - \rightarrow Probability of successful anti-evasion intervention p_i
 - → Who they compare to in the social network ("reference group")

SOCIAL NETWORK AS AN ADJACENCY MATRIX

Matrix form of a weighted directed network

Directed Network



NFTWORK STRUCTURE

- → The network is **generated** using the Bianconi-Barabási fitness model
 - → Taxpayers with **higher wealth** have an higher probability of making new connections
 - → Taxpayers already **heavily connected** have an higher probability of making new connections (sublinear preferential attachment, $\phi < 1$)

Formally:

$$\Pi_i = \frac{W_i[d^{in}(i)]^{\phi}}{\sum_{j \in \mathcal{N}} W_j[d^{in}(j)]^{\phi}}$$

The resulting social networks resembles the ones observed empirically

SOCIAL INTERACTION

- → Taxpayers do their evasion decision based on a benchmark or "reference" level of income
- → Reference income depends upon :
 - \rightarrow **Self**: habit consumption h_{it}
 - some function of past consumption $C_{it-\mathbf{T}}$
 - → Social: The (weighted) average consumption of individuals in a taxpayer's social network

Taxpayer i expected after-tax income when evading E_{it} is:

$$q_{it} = X_i + [1 - p_i f] E_{it}$$

We can then define:

$$Z_{it} = \iota_h h_{it} + \iota_s \mathbf{g}_i \mathbf{q}_t$$

And reference income:

$$R_{it} = R_{i,t-1} + \varsigma_R \left[Z_{it} - R_{i,t-1} \right]$$

where:

 $X_i = (1 - t) W_i$

 ι_h, ι_s

 \mathbf{g}_i

 $\varsigma_R \in (0,1)$

Honest after-tax income

Self and social comparison parameters

Weights of i's reference group

Reference consumption reactiveness



$$\max_{E_i} \mathbb{E}\left(U_{it}\right) \equiv \left[1 - p_i\right] U(C_{it}^n - R_{it}) + p_i \left[U(C_{it}^a - R_{it})\right]$$

After-tax income if not audited

$$C_{it}^n \equiv X_i + E_{it}$$

After-tax income if audited

$$C_{it}^a \equiv C_{it}^n - (1+f)E_{it}$$

Utility is linear-quadratic

$$\mathit{U}(z) = \mathit{z}[\mathit{b} - \tfrac{\mathit{az}}{2}]$$

Optimal Evasion at an interior solution is:

$$E_{it}^* = \frac{1 - p_i f}{a \zeta_i} \{ a[\mathbf{R}_{it} - X_i] + b \}, \zeta_i > 0$$

ACCOUNTING FOR SOCIAL NETWORK

Expanding E_{it}^* using the definitions of R_{it} , Z_{it} and q_{it} we solve à la **Cournot-Nash**:

$$E_{it} = \alpha_{it} + \varsigma_R \iota_s \sum_{j \neq i} m_{ij} E_{jt} =$$

$$\mathbf{E} = \boldsymbol{\alpha}_t + \mathbf{M} \boldsymbol{\beta} \mathbf{E}$$

Where:

$$m_{ij} = \frac{[1 - p_i f][1 - p_j f]}{\zeta_i} g_{ij}$$
$$\beta_{ii} = \varsigma_R \iota_s$$
$$\alpha_{i1,t} = \frac{1 - p_i f}{a \zeta_i} \{b - a[X_i - R(h_{it}, \mathbf{X})]\}$$

WEIGHTED BONACICH CENTRALITY AND EVASION

The nash equilibrium is then:

$$\mathbf{E_t} = [\mathbf{I} - \mathbf{M}\boldsymbol{\beta}]^{-1} \boldsymbol{\alpha}_t = b(\mathbf{M}, \boldsymbol{\beta}, \boldsymbol{\alpha}_t)$$

 $b(\mathbf{M}, \boldsymbol{\beta}, \boldsymbol{\alpha}_t)$ is the weighted Bonacich centrality defined on:

M Edge weights scaled by relative ER of E_i

 β Scales weight of longer paths

Weights centrality by agent characteristics α_t

Under the condition:

 $I > \rho(G) \beta$ Largest absolute value of G eigenvalues small enough

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OPTIMAL EVASION

- → Key theoretical result is that evasion is closely related to the concept of "Bonacich" Network Centrality
 - → More "central" taxpayers evade more
- → Network centrality is a concept developed in sociology
 - → Measures the amount of influence/power players have within a network

COROLLARIES

Corollary 1

If the probability of audit is equal among taxpayers, i.e. $p_i = p_i$ then:

$$\mathbf{E_t} = b(\mathbf{M}, \boldsymbol{\omega}, \boldsymbol{\alpha}_t)$$

Where:

$$\omega_{ii} = \frac{\iota_s \varsigma_R [1-pf]^2}{\zeta}$$

Corollary 2

In a steady state of the model consumption satisfies

$$\mathbf{C}^{SS} = \mathbf{C}^{n,SS} = \mathbf{X} + \mathbf{E}^{SS}.$$

Steady state evasion \mathbf{E}^{SS} , is then given by the vector of Bonacich centralities, $\mathbf{b}(\mathbf{M}, \boldsymbol{\beta}, \boldsymbol{\alpha}^{SS})$, with

$$\alpha_i^{SS} = \frac{1 - p_i f}{a \zeta_i} \left\{ b - a \left[X_i - R \left(h_i^{SS}, \mathbf{X} \right) \right] \right\}$$

COMPARATIVE STATICS: CONTEMPORANEOUS AND DELAYED

A marginal parameter change entails contemporaneous and delayed effects on the steady state of the model:

- 1. The contemporaneous effect $\frac{\partial E_i^{SS}}{\partial z}$ is not accounting for delayed effects
- 2. The full effect $\frac{dE_i^{SS}}{dz}$ includes also the delayed effect caused by adjustments of habit consumption

Lemma 1

$$\text{if} \ \ \frac{\partial X_i}{\partial z} \frac{\partial E_i^{SS}}{\partial z} \geq 0 \quad \text{then} \quad sign\left(\frac{dE_i^{SS}}{dz}\right) = sign\left(\frac{\partial E_i^{SS}}{\partial z}\right)$$

It is sufficient to have same sign for $\partial E_i^{SS}/\partial z$, and steady state consumption, $\partial C_i^{SS}/\partial z$

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MONOTONE COMPARATIVE STATICS

Habit consumption	+	Other's Income	+/0
Own comparison	+	Social comparison	+/0
Own audit prob.	_	Others audit prob.	-/0
Risk Aversion	_	Tax rate	+
Fine	_		

Monotone comparative statics for interior E_i^*

These results apply both to contemporaneous and full effects

have opposite signs

→ In the case of income, contemporary and delayed effects

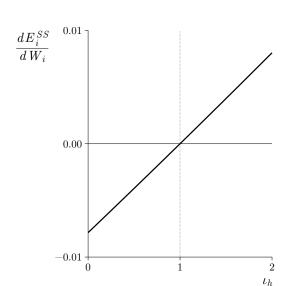
- → The contemporaneous effect causes evasion to fall due to the increased income, i.e. $\frac{\partial E_i^{SS}}{\partial X_{\cdot}} < 0$
- → However, the delayed effect causes an increase in habit **consumption** $\frac{dC_{i}^{SS}}{dX_{i}} < 0$ that as a positive effect on evasion.

This allows our model to replicate the observed behaviour

of evasion increasing in income $\frac{dE_i^{SS}}{dX}>0$

EVASION VS. CONCERN FOR HABIT

The higher a taxpayer's concern for habit i_h the more evasion increases in income





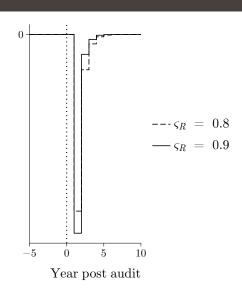
DYNAMIC RESPONSE TO LEGAL INTERVENTION

- → Empirical evidence shows a persistent dynamic behavioural response to interventions
- → The literature argued that belief updating may be driving this evidence
- → We show that self-comparison is able to replicate the same dynamic
- \rightarrow Calibrating the persistence ς_R it is possible to closely match the behaviour observed in reality

RESPONSE TO LEGAL INTERVENTION VS. PERSISTENCE

 ΔE

- → Here periods interpreted as years
- → Deterrence is maximal after the intervention and slowly fades
- → With high levels of persistence the dynamic behavioural response lasts
 ≈ 4 years



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INTERVENTION REVENUE EFFECTS

How does an audit to a taxpayer affect the steady-state evasion of the model?

1. Direct effect \mathbf{E}_{i}^{SS}

On targeted taxpayer, by averting attempted evasion

2. Indirect effects I_{ij}

Expected additional revenue that arises **from future changes** in evasion behaviour

- $\rightarrow I_{ii}$ from the audited tapayer
- $\rightarrow I_{ii}$ from non-audited taxpayers
 - o $oldsymbol{\Sigma}_i = \sum_{j \in \mathcal{N} \setminus i} I_{ij}$ aggregate cross indirect effect
- → Indirect effects 2X-6X direct ones

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TAX AGENCY'S INFERENCE PROBLEM

- ightarrow Tax authorities engage in inferring both **direct effects** ${f E}^{SS}$ and **aggregate gross indirect effects** ${f \Sigma}$
 - → Taxpayers usually ranked by discriminant function and audited sequentially until budget is exhausted
- \rightarrow Crucial information for tax authorities is correct rank of \mathbf{E}^SS and Σ
 - → Optimal audit targeting if tax authorities were able to exactly infer rankings of direct and indirect effects.

Tax authorities require measures that are ordinally equivalent to direct and indirect effects

$$\mathbf{A} \sim \mathbf{B} \iff A_{i1} \geqslant A_{j1} \Leftrightarrow B_{i1} \geqslant B_{j1} \forall i, j$$

MEASURES ORDINALLY EQUIVALENT TO REVENUE EFFECTS

The indirect revenue effects of conducting a single audit of i satisfy:

$$\mathbf{I}_i \sim Diag[\mathbf{b}(\mathbf{M}, \boldsymbol{\beta}, \boldsymbol{\alpha}^{SS})]\mathbf{b}(\mathbf{M}, \boldsymbol{\beta}, \boldsymbol{\rho}_i^{SS})$$

where
$$\mathbf{b}(\mathbf{M}, \boldsymbol{\beta}, \boldsymbol{\alpha}^{SS}) \equiv \mathbf{E}_i^{SS}$$
 and $\boldsymbol{\rho}_i^{SS} = \frac{\partial \boldsymbol{\alpha}^{SS}}{\partial C_i^{SS}}$

Sizes of the **own** and **cross indirect** effects are **ordinally equivalent** to the product of the steady state level of evasion and a new measure of **Bonacich centrality**

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INFERENCE OF REVENUE EFFECTS

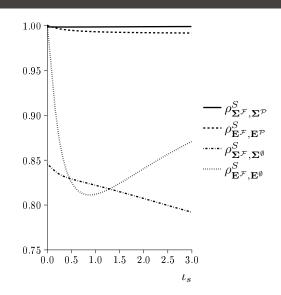
- \rightarrow When there is full observability \mathcal{F} it is possible to exactly determine direct (\mathbf{E}^{SS}) and cross indirect ($\mathbf{\Sigma}$) effects
- → Tax agencies infer revenue effects under limited observability

How valuable is **network information**?

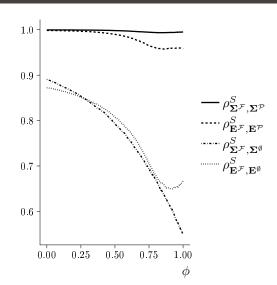
- → Two cases considered:
 - 1. Partial observability (\mathcal{P}) : The tax agency observes the reference groups of taxpayers but has no information on the comparison intensity
 - 2. **No observability** (\emptyset): Everybody attaches equal importance to all the other taxpayers
- ightarrow We assess the role of network information in prediction using a the **Spearman rank correlation coefficient**, i.e. $ho_{{f FP},{f E}\emptyset}^S$

INFERENCE ACCURACY AND SOCIAL COMPARISON

- → Accuracy improves significantly from the no network observability Ø to partial observability P
- → Higher concern for social comparison
 \(\textit{\ell}_s\) decrease
 accuracy



- Accuracy improves significantly from the no network observability ∅ to partial observability \mathcal{P}
- → Stronger preferential attachment ϕ decreases accuracy





Introduction Model Optimal Evasion Responses to Intervention Conclusions

CONCLUDING REMARKS

- → Social interaction may heavily affect evasion behaviour
- → Self comparison is able to replicate the persistent dynamic response of evasion to intervention observed empirically
- → Different Bonacich measures of centrality characterize optimal evasion and revenues effects from auditing
- → Social network information improve significantly the prediction of revenues effects from interventions

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FURTHER RESEARCH

- → Quantify the additional **revenue recovered using network** information
- → Extend the analysis to **crime** as a whole
- → Analyse how adding or removing taxpayers (detention) may affect compliance

Thank You!

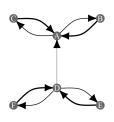
Questions?

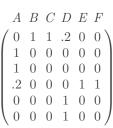
SOCIAL NETWORK AND MATRIX REPRESENTATION

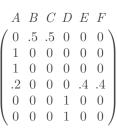
Undirected Network Weighted Network Directed Network











For an **arbitrary** twice differentiable **utility function** considering the FO linear approximation around a Nash equilibrium to the set of FOC. it is:

$$\mathbf{E}_t = \mathbf{J}\mathbf{E}_t + \widehat{\boldsymbol{lpha}}_t = [\mathbf{I} - \mathbf{J}]^{-1}\,\widehat{\boldsymbol{lpha}}_t = \left[\sum_{k=0}^{\infty} \mathbf{J}^k
ight]\widehat{\boldsymbol{lpha}}_t$$

Where ${f J}$ is a matrix of coefficients measuring actions' interactions

A solution is a again in the form of a weighted Bonacich centrality measure

TAXPAYERS' INTERACTION AS A GAME

The game arising from taxpayers interaction is:

Smooth Supermodular Game (Milgrom and Roberts 1990)

Bounds on strategies

Differentiability

Strategic Complements

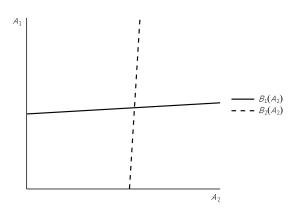
$$E_{it} \in (0, tW_i)$$

$$\mathbb{E}[U_i]$$
 is of class C^2

$$\frac{\partial^2 \mathbb{E}[U]_i}{\partial E_{it} \partial E_{it}} \ge 0$$

BEST RESPONSE

Quadratic utility leads to linear best response



Positive slope of best response functions follows from strategic complementarity in E_{it} , E_{it}

MONOTONE COMPARATIVE STATICS

Smooth Supermodular Games can be analyzed using **Monotone comparative statics**

Following Quah (2007) we exploit the **weaker** condition of **local supermodularity** around the Nash equilibrium point:

Then, for a given parameter z, it holds:

$$\left. \frac{\partial^2 \mathbb{E}[U]_i}{\partial E_i \partial z} \right|_{E_i = E_i^*} \ge 0 \Leftrightarrow \left. \frac{\partial E_i^*}{\partial z} \right|_{E_i = E_i^*} > 0$$

$$\ge 0 \text{ if } \left. \frac{\partial^2 \mathbb{E}[U]_i}{\partial E_i \partial z} \right|_{E_i = E_i^*} > 0$$

$$\ge 0 \text{ if } \left. \frac{\partial^2 \mathbb{E}[U]_i}{\partial E_i \partial z} \right|_{E_i = E_i^*} = 0$$

MONOTONE COMPARATIVE STATICS

	E_i^*		E_i^*
h_{it}	+	X_j	+/0
ι_h	+	ι_s	+/0
p_i	_	p_j	-/0
f	_	t	+
\underline{a}	_	b	+

Monotone comparative statics for interior E_i^*

These results apply in the short and long run

MEASURES ORDINALLY EQUIVALENT TO REVENUE EFFECTS

Understanding why:

$$\mathbf{I}_i \sim \mathbf{E}_i^{SS} \mathbf{b}(\mathbf{M}, oldsymbol{eta}, oldsymbol{
ho}_i^{SS})$$

- \rightarrow The size of the indirect effect I_{ij} is ordinally equivalent to the size of the initial deviation
 - → convergence of evasion back to its steady state value is at a uniform rate for all affected taxpayers
- → Initial effect can be decomposed linearly as the product of:
 - ightarrow marginal effect of a change in *i*'s consumption on *j*'s evasion $\partial E_i^{SS}/\partial C_i^{SS} = b_{j1}(\mathbf{M}, \boldsymbol{\beta}, \boldsymbol{\rho}_i^{SS})$
 - \rightarrow change in *i*'s consumption $b_{i1}(\mathbf{M}, \boldsymbol{\beta}, \boldsymbol{\rho}_i^{SS})E_i^{SS}$

Corollary 3

$$\Sigma \sim \chi$$
 where $\chi_{i1} = \sum_{k \in \mathcal{N}} b_{k1}(\mathbf{M}, \boldsymbol{\beta}, \boldsymbol{\rho}_i^{SS}) E_i^{SS}$