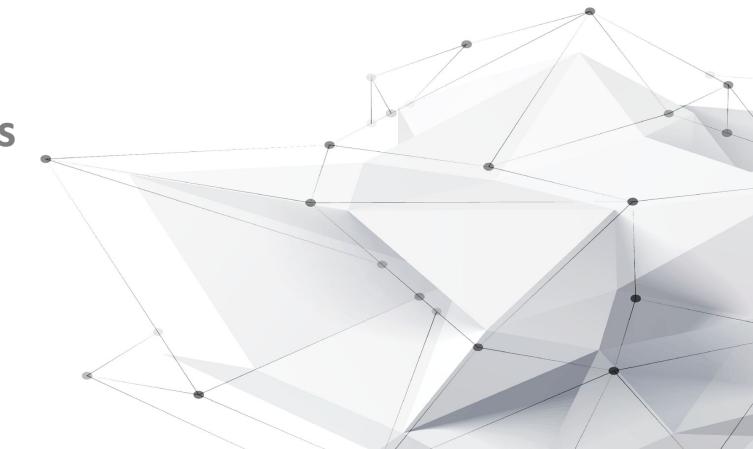


# Fall 2018 MET 211 Group 7: Torsion

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Polytechnic Institute



# Lab 2: Directions

1. Verify the **torque/twist relation** given in the text.
2. Investigate the **deflection vs. torque characteristics** of a given rod (hollow or solid; wood, steel or aluminum).
3. Determine whether the **theoretical relation in the text is a reasonable model** of the actual behavior.

# Lab 2: Parameters

## 1. Verify the torque/twist relation given in the text

### Given

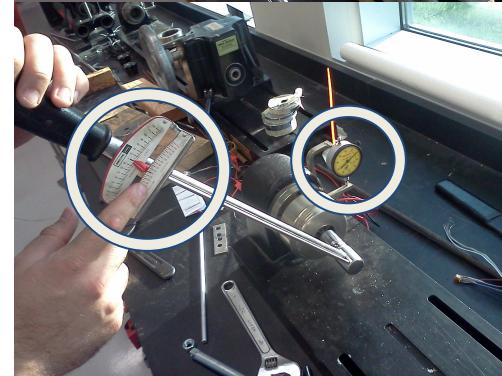
- 0.5 in (12.7 mm) Solid Aluminum Rod
- Torsion Tester - Room N1162
- 0.5 in Torque Wrench for test stand calibration



Aluminum Rod in Test Stand

### Find

- Theoretical Amount of deflection that occurs from torque
- Compare relationships from theoretical values with observed values



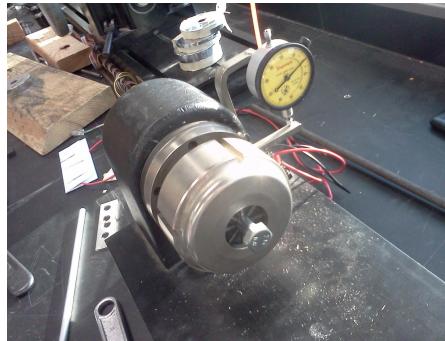
Calibration with Torque Wrench

# Lab 2: Deflection vs. Torque?

2. Investigate the deflection vs. torque characteristics of a given rod solid aluminum.

## Method

- **Calibration:** Used torque wrench to find relationship between torque (in Nm) translation and deflection gauge reading (in mm) at different torque levels
- Marked zero point on tape placed on turning chuck, applied torque to rod in 0.1 mm increments at the dial
- **Removed tape (rotating) and measured length difference corresponding to rotational circumference transversal (in mm)**

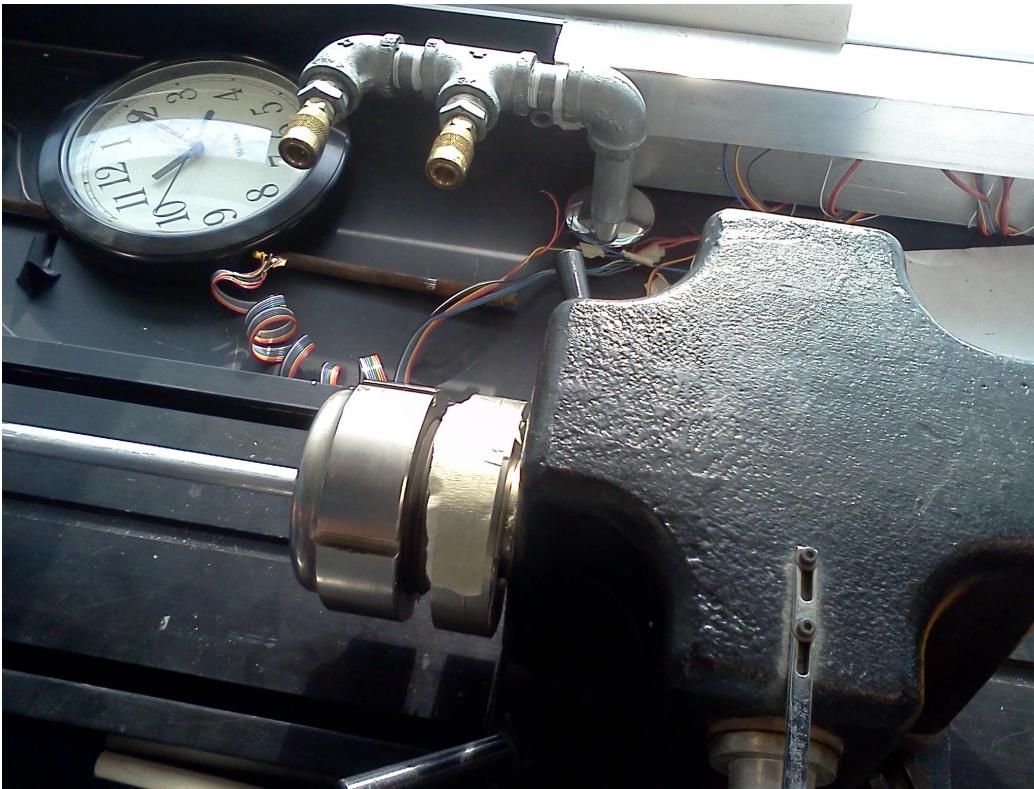


Torque  
Translation  
Reading

Direct Marking Readings



# Lab 2: Testing Close Up



# Lab 2: Equations 1 - Compute J

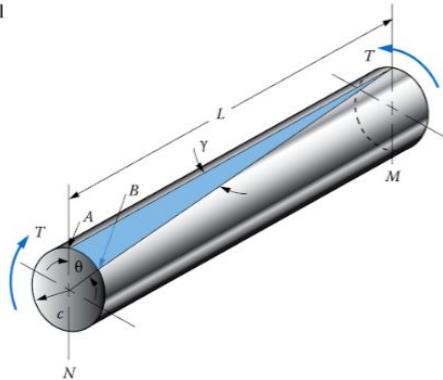
## Compute J (Polar Moment of Inertia)

$$J = \frac{\pi * D^4}{32}$$

J = polar moment of inertia (in mm<sup>4</sup>)

D = diameter of circular bar (in mm)

**FIGURE 4-18** Torsional deformation in a circular bar.



**TABLE 4-4** Shear modulus of elasticity, G.

Material	Shear modulus, G	
	GPa	psi
Plain carbon and alloy steels	80	$11.5 \times 10^6$
Stainless steel type 304	69	$10.0 \times 10^6$
Aluminum 6061-T6	26	$3.75 \times 10^6$
Beryllium copper	48	$7.0 \times 10^6$
Magnesium	17	$2.4 \times 10^6$
Titanium alloy	43	$6.2 \times 10^6$

# Lab 2: Equations 2 - Compute Angle (rad)

## Compute Angle of Twist of a Circular Member

End of shaft M is fixed and torque T is applied to other end. Shaft will twist between two ends at angle  $\theta$  (theta).

$$\theta = \frac{TL}{JG} \times \frac{(10^3 \text{ mm})^3}{1 \text{ m}^3} = \text{rad}$$

$\theta$  = resulting angle of twist (in radians)

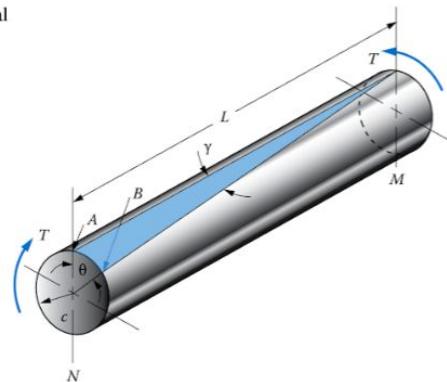
T = torque (in N \* m)

L = initial length (in mm)

J = polar moment of inertia (in mm<sup>4</sup>)

G = shear modulus of elasticity (in GPa)

**FIGURE 4-18** Torsional deformation in a circular bar.



**TABLE 4-4** Shear modulus of elasticity, G.

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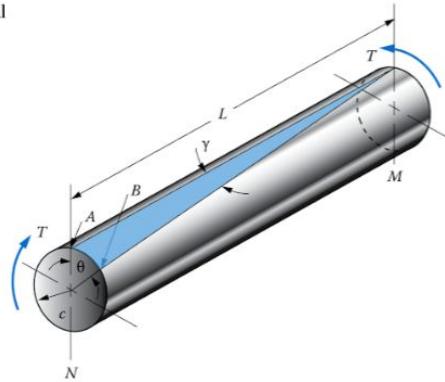
# Lab 2: Equations 3 - Compute Angle (deg)

## Compute Angle in Degrees

$$\theta = \text{rad} \times \frac{180(\text{deg})}{\pi(\text{rad})} = \text{deg}$$

$\theta$  = resulting angle of twist (in degrees)

**FIGURE 4-18** Torsional deformation in a circular bar.



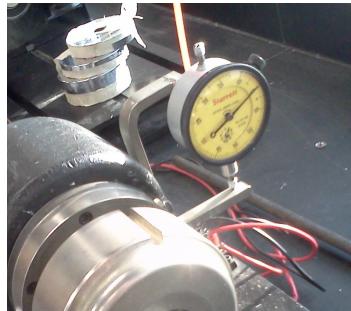
**TABLE 4-4** Shear modulus of elasticity,  $G$ .

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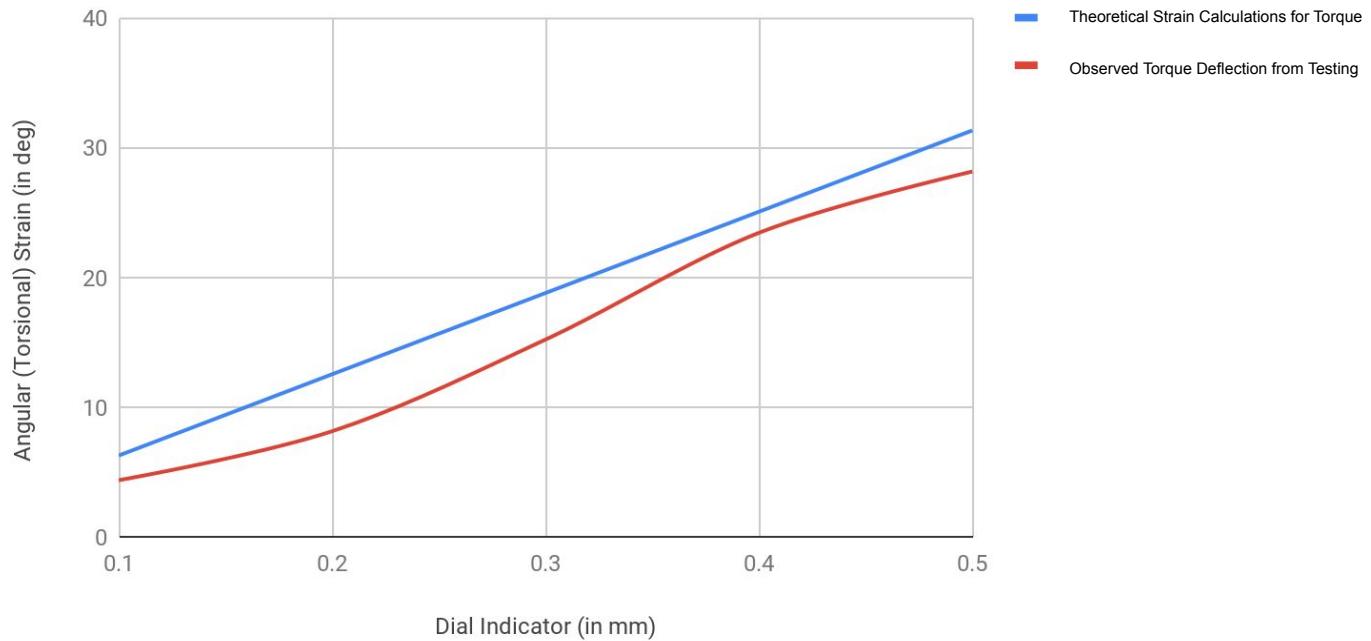
# Lab 2: Deflection Results

## Calculations from Torque Translation vs Loading End Deflection

Dial Reading (mm)	Calculated Torque (N-m)	Measured from Tape (mm)	From Torque (Theoretical in Degrees) $= (180*1000*T*L)/(PI*J*G)$	From Tape (Visual Measure in Degrees) $= 360*\text{Measured/Circumference}$	Percent Difference $= (\text{Theoretical} - \text{Visual}) / (\text{Theoretical} * 100)$
0.1	7.951	3.87	6.263	4.360	30.385
0.2	15.902	7.22	12.525	8.135	35.050
0.3	23.854	13.49	18.787	15.200	19.093
0.4	31.805	20.79	25.050	23.425	6.487
0.5	39.756	24.98	31.312	28.146	10.111



# Lab 2: Dial Indicator vs. Angular Strain



# Lab 2: Theoretical Reasonable?

3. Determine whether the theoretical relation in the text is a reasonable model of the actual behavior.

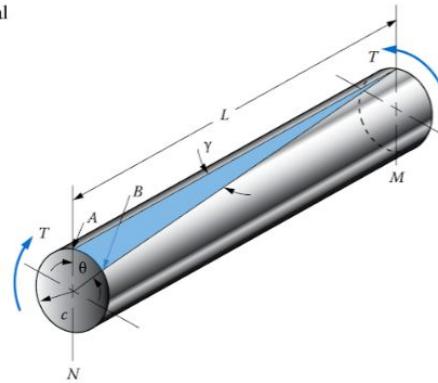
## Confounding Variables & Sources of Error:

- Slippage in the torsion chucks
- Uncertainty of Material Specs
- Precision of Tape Markings and interpretation of measurements
- Torque Wrench readings

## Reasonable?

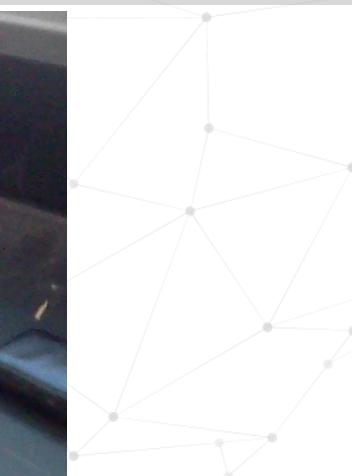
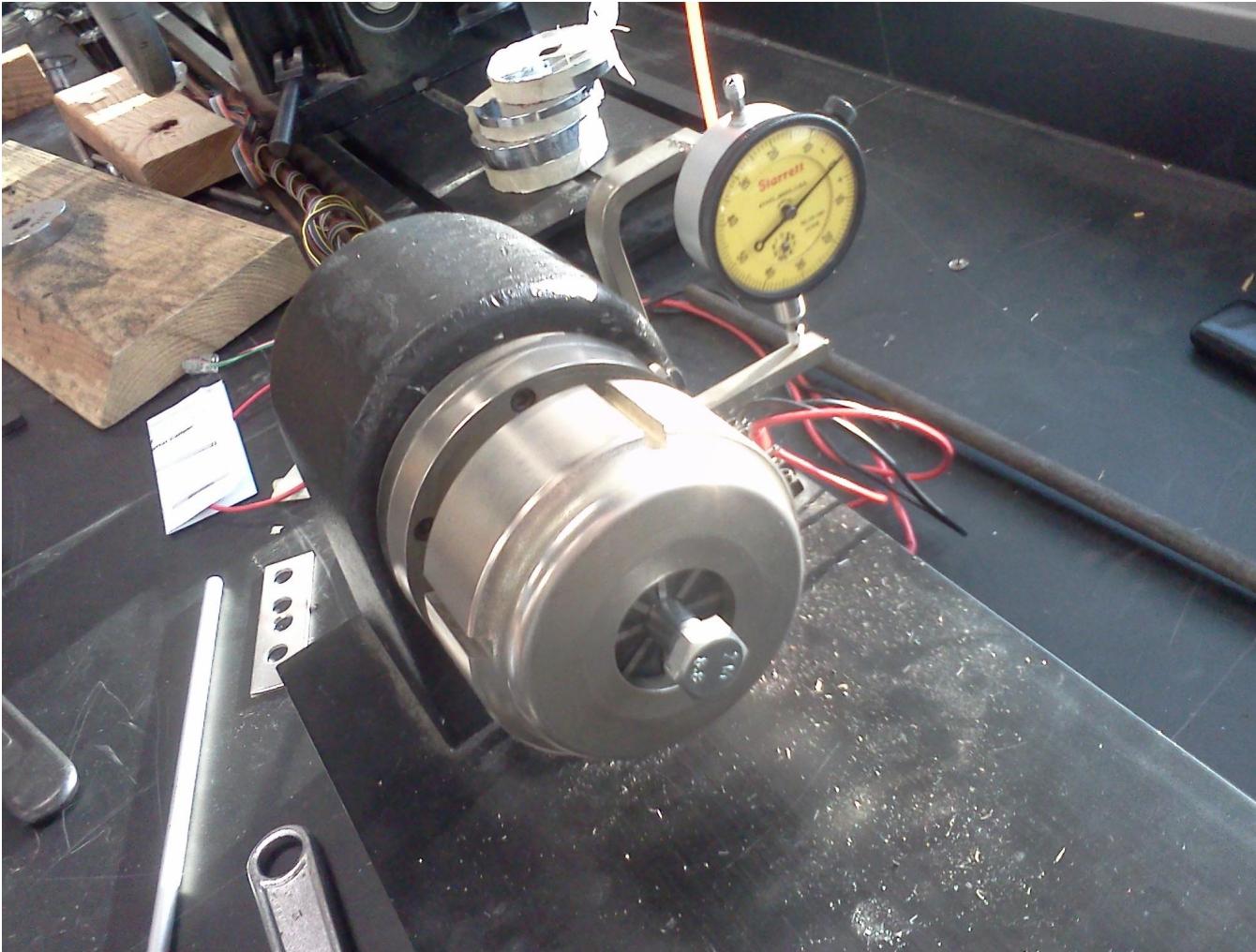
- Somewhat with a 20.225% average higher difference from theoretical to observed, more measurements are needed to decrease uncertainty

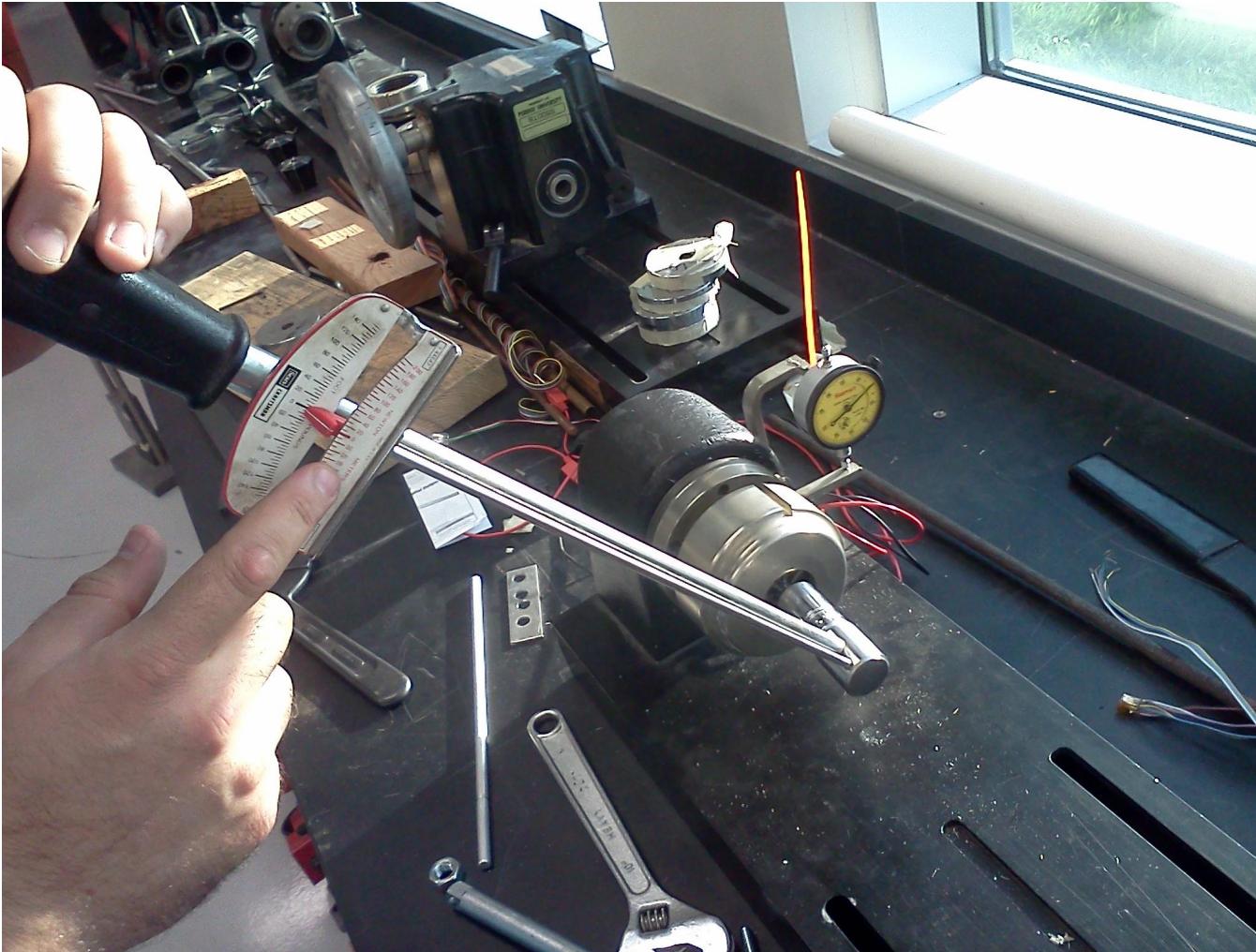
**FIGURE 4-18** Torsional deformation in a circular bar.

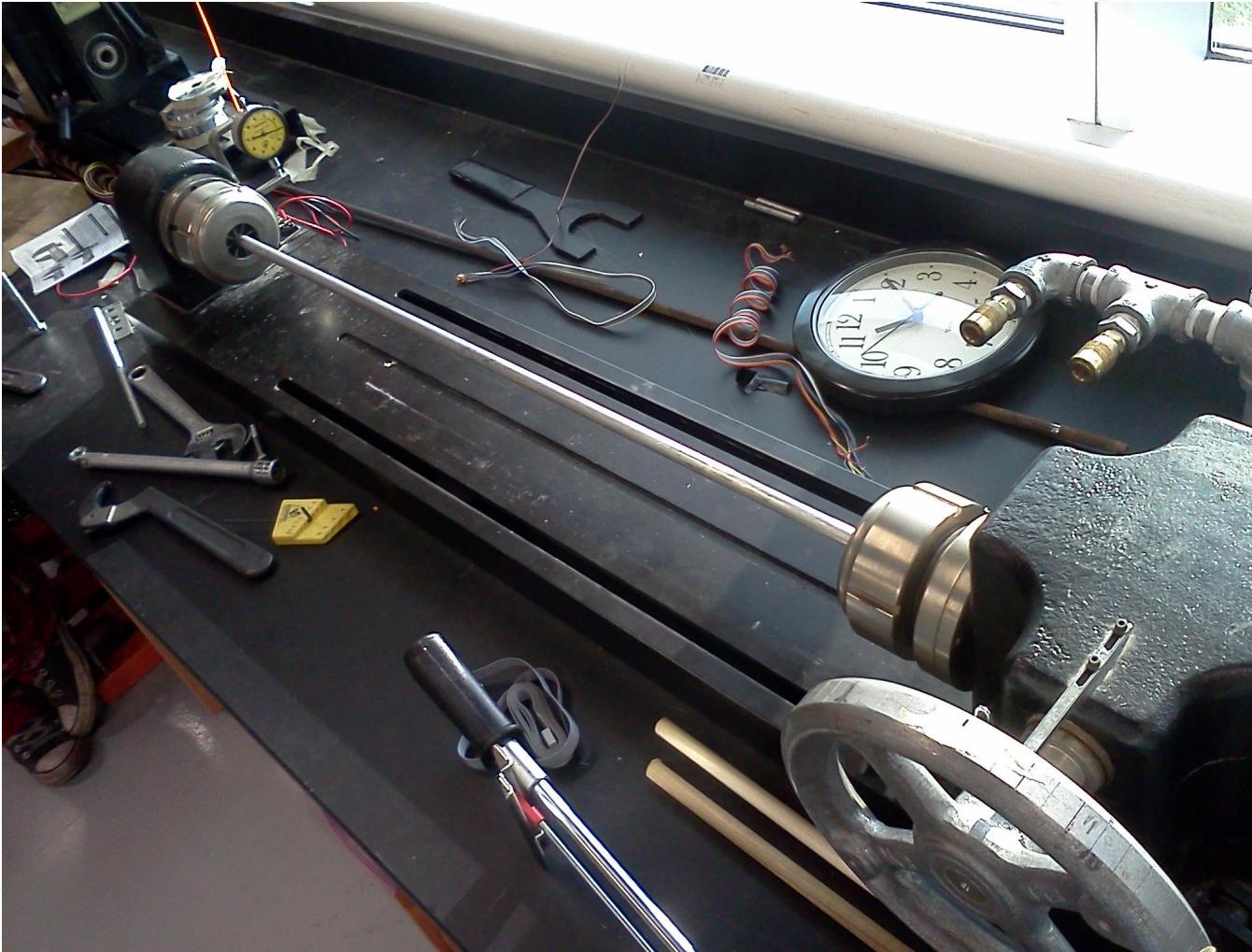


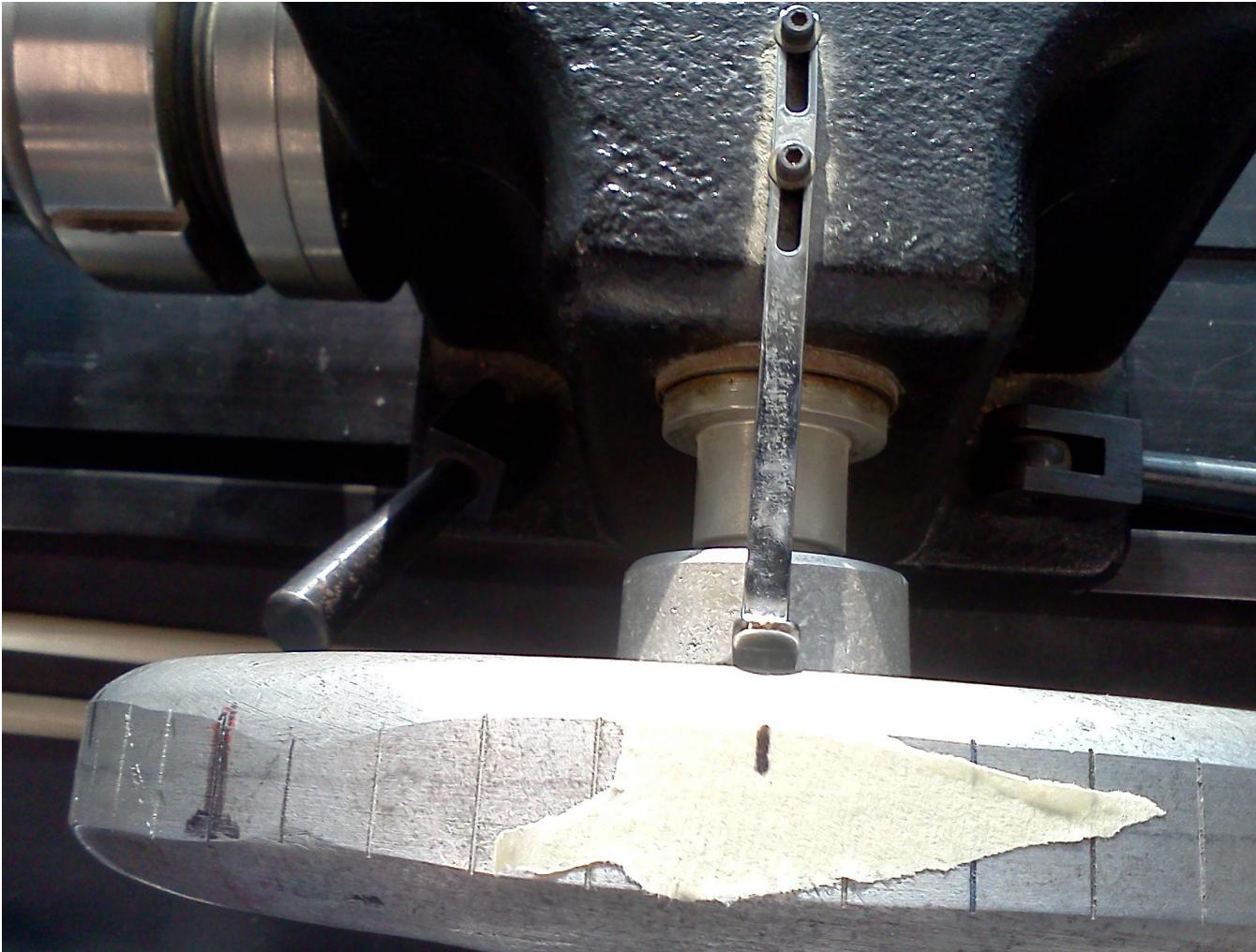
$$J = \frac{\pi * D^4}{32} \quad \theta = \frac{TL}{JG} \times \frac{(10^3 mm)^3}{1 m^3} = rad$$

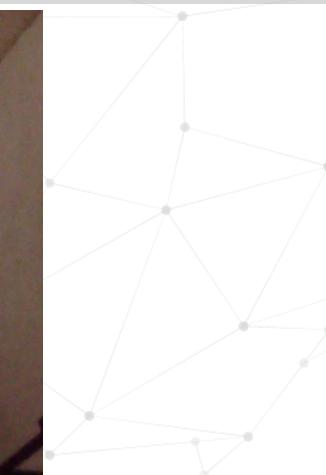
$$\theta = rad \times \frac{180(deg)}{\pi(rad)} = deg$$

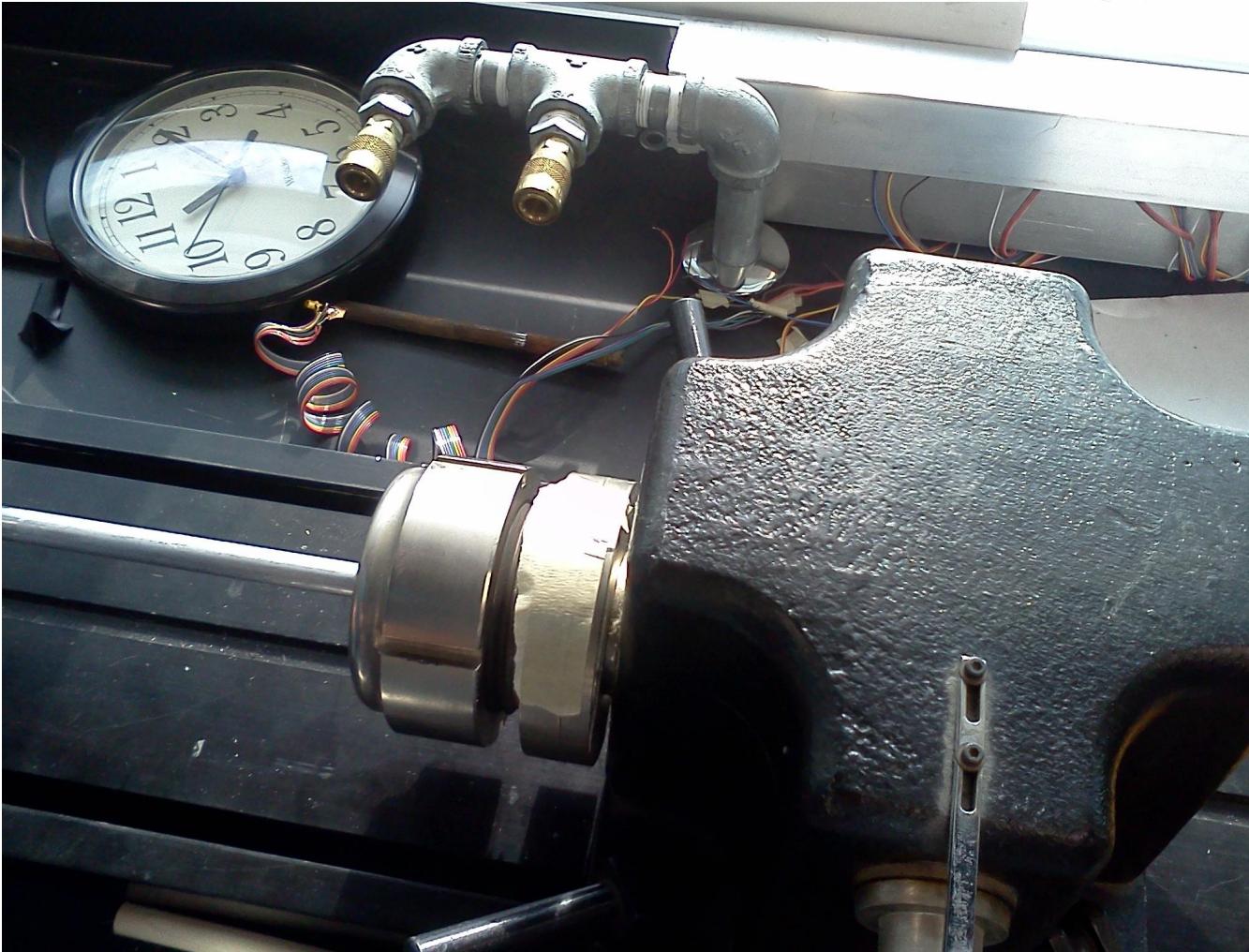














per Sich A1 rand Solid

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0.500  
.497  
.501  
.499

} Dia

~~35-15/16 in~~

35-15/16 in

4.0041 in

Dia 4.000 in

.045  
.04415

dial .01 mm.

circumference  
cm ~~319.186 mm~~

divide by  
circumference  
multiply by  
360°

tape mm

13.49 mm

7.22 mm

20.79 mm

3.87 mm

~~45.00 mm~~  
~~45 = .45 mm~~

20 Nm

28

40 Nw

56

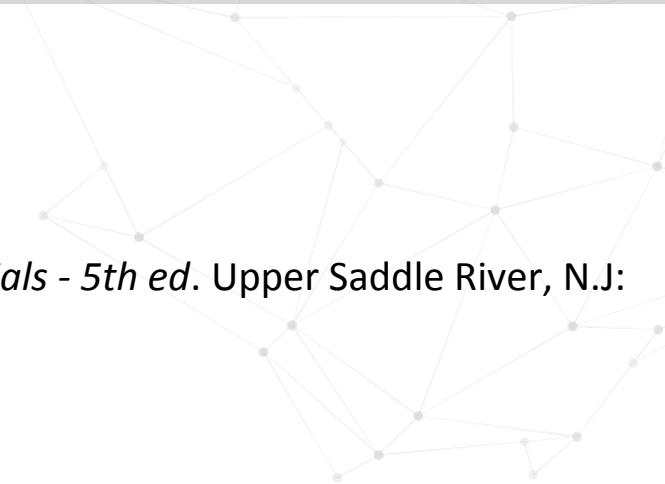
10 Nm

9 mm



# Lab2: References

[textbook] Mott, Robert L. *Applied strength of materials - 5th ed.* Upper Saddle River, N.J: Pearson/Prentice Hall, 2008. Print.



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