testingMC

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Testing MC Notebook

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In this notebook different aspects of the Monte Carlo program will be tested separatedly to secure all works well and is as optimized as possible.

```
[1]: import numpy as np
import matplotlib.pyplot as plt
import scipy as sp
%matplotlib inline
```

Testing the rotation matrices and visualization of coordinates

```
[2]: def rotate(Ax,Ay,Az,testCoord,atype="deg"):
              """Rotates the molecule a specified angle (in degrees) for each main_{\sqcup}
      ⇔axis."""
             atype = atype.lower()
              if atype == "deg" or atype == "d": Ax,Ay,Az = np.radians(Ax),np.
      →radians(Ay),np.radians(Az)
             elif atype == "rad" or atype == "r": pass
              else: raise TypeError("Angle type not detected. Choose deg for degrees,
      ⇔or rad for radians.")
              # Rotation matrices
             Rx = np.array([[1,0,0],[0,np.cos(Ax),-np.sin(Ax)],[0,np.sin(Ax),np.
      \hookrightarrowcos(Ax)]])
             Ry = np.array([[np.cos(Ay), 0, np.sin(Ay)], [0, 1, 0], [-np.sin(Ay), 0, np.
      ⇔cos(Ay)]])
             Rz = np.array([[np.cos(Az),-np.sin(Az),0],[np.sin(Az),np.
      \hookrightarrowcos(Az),0],[0,0,1]])
              # Rotates the molecule the specified angles
             for i in range(3):
                  for _,R in enumerate([Rx,Ry,Rz]):
                      ctemp = testCoord[i].copy()
                      testCoord[i] = np.dot(R,ctemp)
     def draw(coord,ax):
```

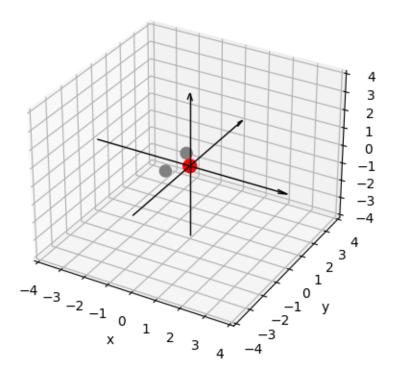
```
ax.scatter(coord.T[0],coord.T[1],coord.T[2], sizes=(100,75,75),_u

c=("red","grey","grey"), alpha=True)

# Testing Rotation
```

```
[3]: # Testing Rotation
     axes = np.array([[1,0,0],[0,1,0],[0,0,1]])
     water = np.array([[0.,0.,0.],[0.75669,0.58589,0.],[-0.75669,0.58589,0.]])
     coord = water
     rotate(0,0,90,coord)
     print(coord)
     # Testing Visualization
     fig = plt.figure()
     ax = plt.axes(projection="3d")
     draw(coord,ax)
     lim = 4 \#box \ limit
     ax.quiver(-lim, 0, 0, 2*lim, 0, 0, color='k',lw=1, arrow_length_ratio=0.05)
     ⇔# x-axis
     ax.quiver(0, -lim, 0, 0, 2*lim, 0, color='k', lw=1, arrow_length_ratio=0.05)
      ⇔# y-axis
     ax.quiver(0, 0, -lim, 0, 0, 2*lim, color='k', lw=1, arrow_length_ratio=0.05)
      \Rightarrow# z-axis
     ax.set_xlim(-lim,lim);ax.set_ylim(-lim,lim);ax.set_zlim(-lim,lim)
                                                                                      ш
     →# Box limits
     ax.set_xlabel("x");ax.set_ylabel("y");ax.set_zlabel("z")
                                                                                      Ш
      →# Axis Labels
```

[3]: Text(0.5, 0, 'z')



```
[5]: def coulomb(qi,qj,r):
    """Returns coulomb energy between i-j pair."""
    kcal = 332.0 #To return the results in kcal/mol
    return kcal*qi*qj/r
```

```
def vdW(A,B,r):
   """Returns Van der Waals energy between i-j pair."""
   return A/r**12 - B/r**6
def looping(coord1,coord2):
        """Gets energy by looping each molecule coordinates"""
       n1 = len(coord1)
       n2 = len(coord2)
       E, Eelec, Evdw = 0,0,0
       for i in range(n1):
                               # For each atom in molecule 1
            for j in range(n2): # For each atom in molecule 2
               r = np.linalg.norm(coord2[j]-coord1[i])
                # Calculadas a pares de c[1]-c[2] (no energias interas)
                Evdw += vdW(A[i][j],B[i][j],r)
                Eelec += coulomb(q[i],q[j],r)
       E = Eelec+Evdw
       return E, Eelec, Evdw
def numpyHand(coord1,coord2):
    """Gets energy using numpy arrays broadcasting and matrix operations"""
   diff = coord1-coord2[:,None]
   distances = np.sqrt((diff**2).sum(axis=-1)).T
   Evdw = (A/distances**12 - B/distances**6).sum()
   Eelec = (332.0*Q/distances).sum()
   E = Evdw + Eelec
   return E, Eelec, Evdw
def numpyLinalg(coord1,coord2):
    """Same as NumpyHand but using linalg.norm"""
   diff = coord1-coord2[:,None]
   distances = np.linalg.norm(diff, axis=-1).T
   Evdw = (A/distances**12 - B/distances**6).sum()
   Eelec = (332.0*Q/distances).sum()
   E = Evdw + Eelec
   return E, Eelec, Evdw
def scipycdist(coord1,coord2):
    """Gets energies with SciPy cdist"""
   distances = sp.spatial.distance.cdist(coord1,coord2)
```

```
Evdw = (A/distances**12 - B/distances**6).sum()
Eelec = (332.0*Q/distances).sum()
E = Evdw + Eelec
return E,Eelec,Evdw
```

```
[6]: #Comprobamos que los diferentes métodos den la misma energia
for method in [looping,numpyHand,numpyLinalg,scipycdist]:
    print(method.__name__)
    E,Eelec,Evdw = method(coord1,coord2)
    print(E,Eelec,Evdw)
# Todo OK
```

```
looping
```

- -6.765029430161267 -8.570967413591175 1.805937983429908 numpyLinalg
- -6.765029430161267 -8.570967413591175 1.805937983429908 scipycdist
- -6.765029430161267 -8.570967413591175 1.805937983429908

Here will be tested the scaling and time consumption of the different energy calculation functions. Since with the Monte Carlo program a lots of steps and calculations are performed, it is important to optimize the code as much as possible to bring faster results. As we know, Python by itself is pretty slow and libraries such as NumPy or SciPy do a better job when dealing with array/matrix calculations.

For that reason, a method using matrices to calculate the pair-distances and energies is chosed to get faster results. Below are tested different implementations of this new method using NumPy arrays and broadcasting and the cdist() SciPy function.

```
[123]: #Miramos cuanto tardan y escalado segun el numero de coordenadas
nPoints = np.logspace(1,4,10)
times = [[] for _ in range(4)]
for n in nPoints:
    coord1 = np.random.uniform(1,2,size=(int(n),3))
    coord2 = np.random.uniform(1,2,size=(int(n),3))
    A = np.random.uniform(1,2,size=(int(n),int(n)))
    B = np.random.uniform(1,2,size=(int(n),int(n)))
    q = np.random.uniform(-1,1,size=(int(n)))
    Q = np.dot(q[:,None],q[:,None].T)

for i,method in enumerate([looping,numpyHand,numpyLinalg,scipycdist]):
        print(method.__name__)
        t = %timeit -o method(coord1,coord2)
        times[i].append(t.average)
```

looping

- 471 $\mu s \pm 392$ ns per loop (mean \pm std. dev. of 7 runs, 1,000 loops each) numpyHand
- 31.1 μ s \pm 84.8 ns per loop (mean \pm std. dev. of 7 runs, 10,000 loops each) numpyLinalg
- $32.8~\mu s~\pm~37.3~ns$ per loop (mean $\pm~std.~dev.$ of 7 runs, 10,000 loops each) scipycdist
- 19.7 μs \pm 17.9 ns per loop (mean \pm std. dev. of 7 runs, 100,000 loops each) looping
- 2.08 ms \pm 8.53 μ s per loop (mean \pm std. dev. of 7 runs, 100 loops each) numpyHand
- $49.5~\mu s~\pm~33.7~ns$ per loop (mean $\pm~std.~dev.$ of 7 runs, 10,000 loops each) numpyLinalg
- $51.5 \ \mu s \ \pm \ 57.6 \ ns$ per loop (mean $\pm \ std.$ dev. of 7 runs, 10,000 loops each) scipycdist
- $36.8 \ \mu s \ \pm \ 22.8 \ ns$ per loop (mean $\pm \ std.$ dev. of 7 runs, 10,000 loops each) looping
- 9.92 ms \pm 12.3 μ s per loop (mean \pm std. dev. of 7 runs, 100 loops each) numpyHand
- 164 μs \pm 532 ns per loop (mean \pm std. dev. of 7 runs, 10,000 loops each) numpyLinalg
- 169 $\mu s \pm 3.22~\mu s$ per loop (mean \pm std. dev. of 7 runs, 10,000 loops each) scipycdist
- 121 μs \pm 800 ns per loop (mean \pm std. dev. of 7 runs, 10,000 loops each) looping
- 46.6 ms \pm 97.9 μ s per loop (mean \pm std. dev. of 7 runs, 10 loops each) numpyHand
- 684 μs \pm 542 ns per loop (mean \pm std. dev. of 7 runs, 1,000 loops each) numpyLinalg
- 697 $\mu s \pm 8.2 \ \mu s$ per loop (mean \pm std. dev. of 7 runs, 1,000 loops each) scipycdist
- 500 $\mu s \pm 1.28 \ \mu s$ per loop (mean \pm std. dev. of 7 runs, 1,000 loops each) looping
- 215 ms \pm 1.03 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each) numpyHand
- $4.36~\mathrm{ms}~\pm~273~\mathrm{\mu s}$ per loop (mean $\pm~\mathrm{std}$. dev. of 7 runs, 100 loops each) numpyLinalg
- $4.17~\text{ms}~\pm~129~\mu\text{s}$ per loop (mean $\pm~\text{std}.$ dev. of 7 runs, 100 loops each) scipycdist
- 2.29 ms \pm 10.9 μ s per loop (mean \pm std. dev. of 7 runs, 100 loops each) looping
- 1.01 s \pm 3.86 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each) numpyHand
- 21.8 ms \pm 116 μ s per loop (mean \pm std. dev. of 7 runs, 10 loops each) numpyLinalg

```
21.9 ms ± 87.8 µs per loop (mean ± std. dev. of 7 runs, 10 loops each)
scipycdist
14.8 \text{ ms} \pm 199 \text{ } \mu \text{s} per loop (mean \pm std. dev. of 7 runs, 100 loops each)
looping
4.67 \text{ s} \pm 14.3 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
numpyHand
144 ms \pm 90.7 ms per loop (mean \pm std. dev. of 7 runs, 10 loops each)
numpyLinalg
107 ms ± 586 µs per loop (mean ± std. dev. of 7 runs, 10 loops each)
scipycdist
68.3 \text{ ms} \pm 1.04 \text{ ms} \text{ per loop (mean} \pm \text{ std. dev. of 7 runs, 10 loops each)}
21.7 \text{ s} \pm 114 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
numpyHand
510 ms \pm 9.14 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)
numpyLinalg
501 ms \pm 4.28 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)
scipycdist
299 ms \pm 3.09 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)
looping
1min 41s ± 770 ms per loop (mean ± std. dev. of 7 runs, 1 loop each)
numpyHand
2.57 \text{ s} \pm 37.8 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
numpyLinalg
2.53 s \pm 13 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)
scipycdist
1.39 \text{ s} \pm 14.9 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
looping
7min 48s \pm 817 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)
numpyHand
12.3 s \pm 102 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)
numpyLinalg
12.2 \text{ s} \pm 144 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
scipycdist
6.4 \text{ s} \pm 19.2 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
```

As you can see in the plot below, each method scales with N2 (N = number of coordinates in molecule), as expected, but the time used by the simple looping method using native Python is much higher than the ones using numpy arrays and matrix calculations. For that reason, in order to make the program as faster and optimized as posible, the arrays/matrices method will be used in the Monte Carlo program.

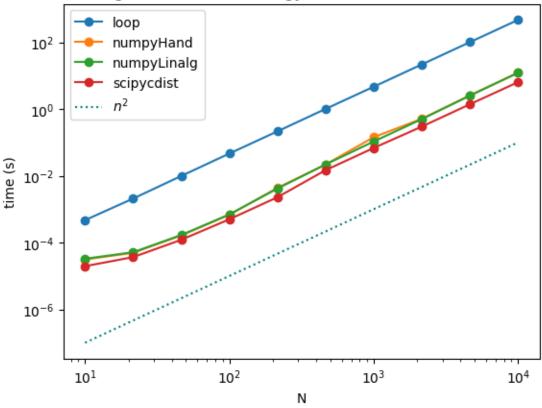
```
[132]: # Ploting df columns (timepoints)
for time in times:
    plt.loglog(nPoints,time, "o-")

# Ploting n**2 dependencies (adjusted to fit plot)
plt.plot(nPoints,nPoints**2*1e-9,":", c="teal")
```

```
# Plot settings
plt.xlabel("N"); plt.ylabel("time (s)")
plt.title("Scaling of the different energy functions with coordinates N")
plt.legend(["loop","numpyHand","numpyLinalg","scipycdist",r"$n^2$"])
```

[132]: <matplotlib.legend.Legend at 0x24b58a1a560>

Scaling of the diferent energy functions with coordinates N



```
[136]: # Miramos cuanto tardan y escalado segun el numero de steps
nPoints2 = np.logspace(1,5,8)
times2 = [[] for _ in range(4)]

coord1 = np.random.uniform(1,2,size=(3,3))
coord2 = np.random.uniform(1,2,size=(3,3))
A = np.random.uniform(1,2,size=(3,3))
B = np.random.uniform(1,2,size=(3,3))
q = np.random.uniform(-1,1,size=(3))
Q = np.dot(q[:,None],q[:,None].T)
```

```
for n in nPoints2:
     for i,method in enumerate([looping,numpyHand,numpyLinalg,scipycdist]):
         print(method.__name__)
         t = %timeit -o for _ in range(int(n)): method(coord1,coord2)
         times2[i].append(t.average)
times2 = np.array(times2)
looping
737 \mu s \pm 3.29 \ \mu s per loop (mean \pm std. dev. of 7 runs, 1,000 loops each)
numpyHand
331 \mu s \pm 2.17 \mu s per loop (mean \pm std. dev. of 7 runs, 1,000 loops each)
numpyLinalg
227 \mu s \pm 21.6 \ \mu s per loop (mean \pm std. dev. of 7 runs, 1,000 loops each)
scipycdist
153 \mu s \pm 1.67 \mu s per loop (mean \pm std. dev. of 7 runs, 10,000 loops each)
looping
1.6 \text{ ms} \pm 10.5 \text{ } \mu\text{s} per loop (mean \pm std. dev. of 7 runs, 1,000 loops each)
numpyHand
741 \mu s \pm 11.4 \mu s per loop (mean \pm std. dev. of 7 runs, 1,000 loops each)
numpyLinalg
812 \mu s \pm 11.4 \mu s per loop (mean \pm std. dev. of 7 runs, 1,000 loops each)
scipycdist
559 \mu s \pm 1.59 \mu s per loop (mean \pm std. dev. of 7 runs, 1,000 loops each)
6.02 \text{ ms} \pm 93.5 \text{ } \mu \text{s} \text{ per loop (mean} \pm \text{ std. dev. of 7 runs, 100 loops each)}
numpyHand
2.71 ms \pm 8.91 \mus per loop (mean \pm std. dev. of 7 runs, 100 loops each)
numpyLinalg
2.94 ms \pm 22.3 \mus per loop (mean \pm std. dev. of 7 runs, 100 loops each)
scipycdist
2.11 ms \pm 57.3 \mus per loop (mean \pm std. dev. of 7 runs, 100 loops each)
22.8 ms ± 627 µs per loop (mean ± std. dev. of 7 runs, 10 loops each)
numpyHand
10.2 \text{ ms} \pm 18.9 \text{ } \mu \text{s} \text{ per loop (mean} \pm \text{ std. dev. of 7 runs, } 100 \text{ loops each)}
numpyLinalg
11.2 ms \pm 225 \mus per loop (mean \pm std. dev. of 7 runs, 100 loops each)
scipycdist
7.8 \text{ ms} \pm 19.5 \text{ } \mu \text{s} per loop (mean \pm std. dev. of 7 runs, 100 loops each)
83.4 ms ± 408 µs per loop (mean ± std. dev. of 7 runs, 10 loops each)
numpyHand
38.2 ms \pm 335 \mus per loop (mean \pm std. dev. of 7 runs, 10 loops each)
numpyLinalg
42.3 \text{ ms} \pm 1.25 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 10 loops each)
scipycdist
29.6 ms ± 470 µs per loop (mean ± std. dev. of 7 runs, 10 loops each)
looping
```

```
309 ms ± 1.45 ms per loop (mean ± std. dev. of 7 runs, 1 loop each)
numpyHand
145 ms \pm 2.23 ms per loop (mean \pm std. dev. of 7 runs, 10 loops each)
numpyLinalg
156 ms \pm 2.39 ms per loop (mean \pm std. dev. of 7 runs, 10 loops each)
scipycdist
109 ms ± 566 µs per loop (mean ± std. dev. of 7 runs, 10 loops each)
looping
1.17 s \pm 8.13 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)
numpyHand
527 \text{ ms} \pm 3.04 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
numpyLinalg
575 ms \pm 5.59 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)
scipycdist
414 ms \pm 5.77 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)
looping
4.37 \text{ s} \pm 39.3 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
numpyHand
2.02 \text{ s} \pm 26.2 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
numpyLinalg
2.13 \text{ s} \pm 18.7 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
scipycdist
1.54 \text{ s} \pm 26 \text{ ms} per loop (mean \pm std. dev. of 7 runs, 1 loop each)
```

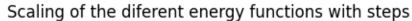
Here, you can also see the scaling and time with the number of steps. As expected all scale linearly with N. Again, using the normal loop method gives slower results than using NumPy or SciPy.

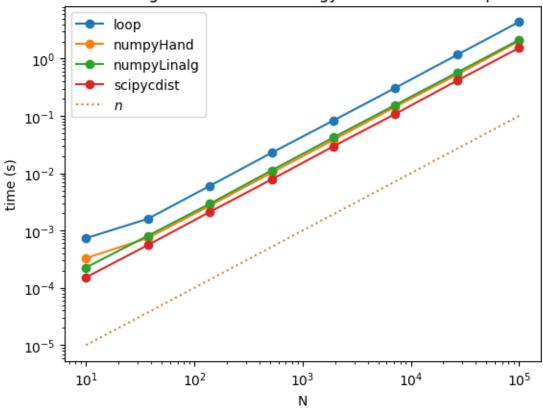
```
[137]: # Ploting df columns (timepoints)
for time in times2:
    plt.loglog(nPoints2,time, "o-")

# Ploting n dependencies (adjusted to fit plot)
plt.plot(nPoints2,(nPoints2)*1e-6,":", c="peru")

# Plot settings
plt.xlabel("N"); plt.ylabel("time (s)")
plt.title("Scaling of the diferent energy functions with steps")
plt.legend(["loop","numpyHand","numpyLinalg","scipycdist",r"$n$"])
```

[137]: <matplotlib.legend.Legend at 0x24b5657d3f0>





Instead of double looping over the coordinates to calculate the energies pair by pair (very slow), you can use arrays and broadcasting to work with matrices and faster. Below are a few examples.

```
[27]: #Para poder haver vector x vector.T = matrix hay que añadir nueva dimensión_
      ⇔(vector[:,None])
      Qij = np.dot(q[:,None],q[:,None].T)
      print(Qij)
      #Lo mismo pasa con sumas/restas
      Qijr = (q[:,None]-q[:,None].T)
      print(Qijr)
     [[ 0.695556 -0.347778 -0.347778]
      [-0.347778
                  0.173889 0.173889]
      [-0.347778
                  0.173889 0.173889]]
     [[ 0.
              -1.251 -1.251]
      [ 1.251 0.
                      0.
                           ]
      [ 1.251 0.
                      0.
                           ]]
[10]: #Se puede calcular la matriz de distancias con arrays y broadcasting
      diff1 = coord1-coord2[:,None]
```

```
diff1 = diff1**2
      diff1 = diff1.sum(axis=-1)
      diff1 = np.sqrt(diff1)
      print(diff1.T)
     [[2.74143849 3.3613768 3.35939652]
      [1.77169806 2.42455625 2.42214822]
      [3.05079563 3.68923041 3.69204577]]
[92]: #Lo mismo pero mas resumido
      diff = coord1-coord2[:,None]
      distances = np.sqrt((diff**2).sum(axis=-1)).T
      print(distances)
     [[2.74143849 3.3613768 3.35939652]
      [1.77169806 2.42455625 2.42214822]
      [3.05079563 3.68923041 3.69204577]]
[88]: #Lo mismo pero utilizando np.linalq.norm
      diff = coord1-coord2[:,None]
      distances = np.linalg.norm(diff, axis=-1).T
      print(distances)
     [[2.74143849 3.3613768 3.35939652]
      [1.77169806 2.42455625 2.42214822]
      [3.05079563 3.68923041 3.69204577]]
[93]: #SciPy tiene cdist que pinta bien
      distances = sp.spatial.distance.cdist(coord1,coord2)
      print(distances)
      print(A/distances)
     [[2.74143849 3.3613768 3.35939652]
      [1.77169806 2.42455625 2.42214822]
      [3.05079563 3.68923041 3.69204577]]
     [[2.12273799e+05 9.76734804e+01 9.77310564e+01]
      [1.85312260e+02 4.00727309e-06 4.01125700e-06]
      [1.07616966e+02 2.63357338e-06 2.63156515e-06]]
```