

**Problem.** Using the Müller-Brown surface in the domain  $-1.5 \leq x \leq 1.0$  and  $-0.5 \leq y \leq 2.0$  write a Runge-Kutta 4 program that starting in the first order saddle point located in  $(-0.822, 0.624)$  integrates the steepest descent curve joining this point and the minimum. The initial condition is the eigenvector of the Hessian matrix of this point with negative eigenvalue,  $(x(0), y(0)) = (-0.822, 0.624)$ ;  $\mathbf{g}(x(0), y(0)) = \mathbf{v}_0$ .

Müller-Brown surface:

$$E(x, y) = \sum_{i=1}^4 A_i \exp(a_i(x - x_i^0))^2 + b_i(x - x_i^0)(y - y_i^0) + c_i(y - y_i^0)^2$$

with  $A = (-200, -100, -170, 15)$

$$a = (-1, -1, -6.5, 0.7)$$

$$b = (0, 0, 11, 0.6)$$

$$c = (-10, -10, -6.5, 0.7)$$

$$x^0 = (1, 0, -0.5, -1)$$

$$y^0 = (0, 0.5, 1.5, 1).$$