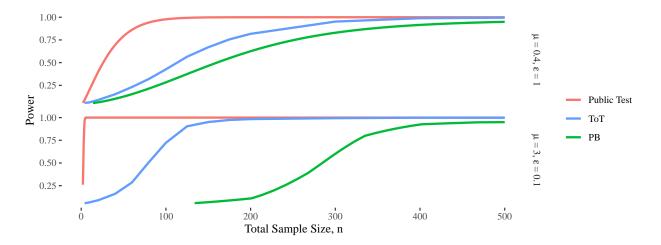
## Figures from ArXiv Version of Paper

The code in this document creates the plots in the text of the ArXiv version of the paper (as of March 2023) using the saved power computations in the figures folder.

The following creates Figure 2 comparing ToT to PB.

```
Figure_2 <- read_csv("figures_data/Figure_2.csv", show_col_types = FALSE)

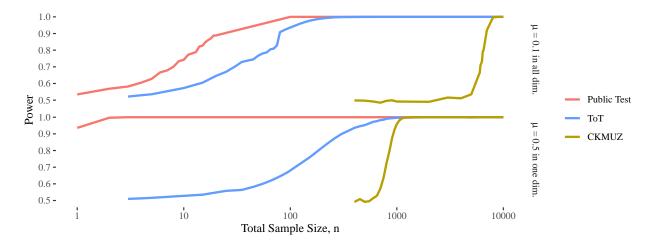
Figure_2 %>%
    # Adjust Order of Tests in Legend
    mutate(test = factor(test, levels = c("Public Test", "ToT", "PB"))) %>%
    # Create a Variable of Facet Labels
    mutate(eff = paste0("mu*' = ", eff,", '*epsilon*' = ", eps,"'")) %>%
    ggplot(aes(x = n, y = power, color = test)) +
    geom_line(linewidth = 1) +
    facet_grid(rows = vars(eff), labeller = label_parsed) +
    scale_color_manual(values = plot_colors[c(1,5,3)]) +
    labs(x = "Total Sample Size, n", y = "Power", color = "") +
    theme_tufte()
```



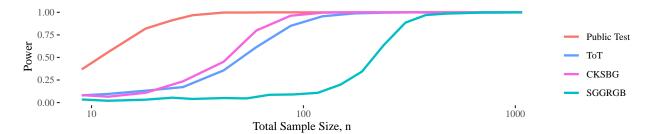
The following creates Figure 3 comparing ToT to CKMUZ.

```
Figure_3 <- read_csv("figures_data/Figure_3.csv", show_col_types = FALSE)

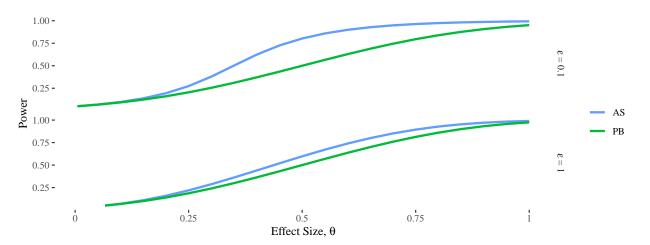
Figure_3 %>%
    # Adjust Order of Tests in Legend
    mutate(test = factor(test, levels = c("Public Test", "ToT", "CKMUZ"))) %>%
```



The following creates Figure 4 comparing ToT to CKSBG and SGGRGB.



The following creates Figure 5 in the appendix comparing AS to PB.



The following creates Figures 6-7 in the appendix comparing ToT to PB.

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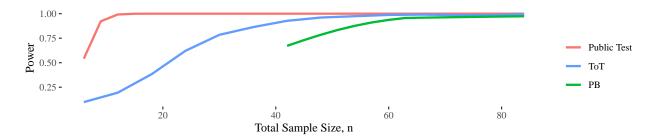
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The following creates Figures 8-12 in the appendix comparing ToT to CKMUZ.

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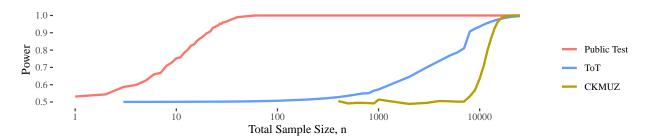
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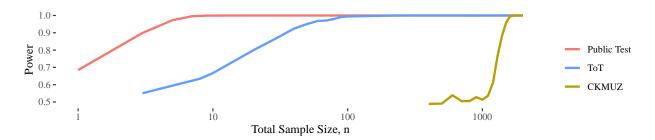
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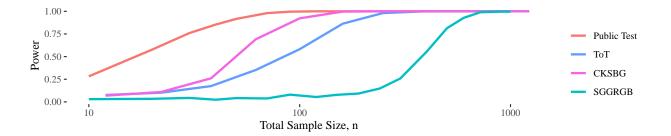
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mutate(test = factor(test, levels = c("Public Test", "ToT",
                                          "CKSBG", "SGGRGB"))) %>%
  ggplot(aes(x = n, y = power, color = test)) + geom_line(linewidth = 1) +
  labs(x = "Total Sample Size, n", y = "Power", color = "") +
  scale_x_log10() + theme_tufte() +
  scale_color_manual(values = plot_colors[c(1,5,6,4)])
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ggsave("ArXiv_plots/Fig14.pdf", width = 6.75, height = 1.75,
       dpi=600, units = "in")
Figure_15 <- read_csv("figures_data/Figure_15.csv", show_col_types = FALSE)
Figure_15 %>%
  filter(n <= 1226) %>%
  filter(test %in% c("pub", "Private KW", "Private ANOVA",
                      "Test of tests")) %>%
  mutate(test = case_when(test == "pub" ~ "Public Test",
                           test == "Private ANOVA" ~ "SGGRGB",
                           test == "Private KW" ~ "CKSBG",
                           test == "Test of tests" ~ "ToT")) %>%
  mutate(test = factor(test, levels = c("Public Test", "ToT",
                                          "CKSBG", "SGGRGB"))) %>%
  ggplot(aes(x = n, y = power, color = test)) + geom_line(linewidth = 1) +
  labs(x = "Total Sample Size, n", y = "Power", color = "") +
  scale_x_log10() + theme_tufte() +
  scale_color_manual(values = plot_colors[c(1,5,6,4)])
  1.00 -
  0.75 -
                                                                                      Public Test
                                                                                      ToT
  0.50 -
                                                                                      CKSBG
  0.25 -
                                                                                     SGGRGB
  0.00 -
                                                                          1000
                                   Total Sample Size, n
ggsave("ArXiv_plots/Fig15.pdf", width = 6.75, height = 1.75,
       dpi=600, units = "in")
Figure_16 <- read_csv("figures_data/Figure_16.csv", show_col_types = FALSE)
Figure_16 %>%
```

