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Variational Inference for Inverse Reinforcement Learning with Gaussian Processes

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Masters project proposal

Date of submission placed here

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1 Introduction

briefly explain the context of the project problem

1.1 A subsection

Please note your proposal need not follow the included section headings - this is only a suggested structure. Also add subsections etc as required

2 Statement of Problem

clearly state the problem to be addressed in your forthcoming project. Explain why it would be worthwhile to solve this problem.

3 Background Survey

present an overview of relevant previous work including articles, books, and existing software products. Critically evaluate the strengths and weaknesses of the previous work.

4 Proposed Approach

state how you propose to solve the software development problem. Show that your proposed approach is feasible, but identify any risks.

5 Work Plan

show how you plan to organize your work, identifying intermediate deliverables and dates.

6 Notes on papers (to be removed)

6.1 Miscellaneous

(Directed) similarity between MDPs using restricted Boltzmann machines [6]

Chapter 6 on distance measures [23]

The PhD thesis behind maximum causal entropy [35]

6.2 Gaussian Processes

Your recommended book [28]

Simple introduction to GPs for time-series modelling [30]

Spectral kernels [33]

GPs over graphs instead of vectors (haven't actually read) [32]

Another introduction from physics (skimmed through) [18]

Learning a GP from very little data [25]

One GP for multiple correlated output variables [3]

Kernels for categorical and count data [31]

6.3 Interpretability

Learning latent factors [21]

The behaviour of Reddit users [12]

6.4 Inverse Reinforcement Learning

One of the first papers on the topic [24]

Follow-up on the previous paper [1]

Bayesian setting [27]

Learning optimal composite features [11]

The main paper [20]

A different take on IRL with GPs [26]

The paper that introduced maximum entropy into IRL [36]

IRL for large state spaces (haven't read) [7]

Multiple reward functions [10]

6.4.1 Multiple Strategies

EM clustering [2]

Structured priors [13]

There are more, but I haven't gotten to them yet.

6.5 Variational Inference

Chapter 10 on approximate inference [4]

Part IV on probabilities and inference [22]

A recent review [5]

Normalizing flows [29]

Linear VI for GPs [9]

Stochastic VI [17]

Structured stochastic VI (haven't read) [16]

Another review of recent advances [34]

Sparse VI for GP [15]

Sparse GPs [8]

IRL via deep GP [19]

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