Unit 2 Group Work PCHA 2022-23 / Dr. Kessner

Name & Pledge:

No calculator! Have fun!

1. Evaluate the following:

a)
$$\tan \frac{7\pi}{6}$$

b)
$$\sec \frac{4\pi}{3} = -2$$

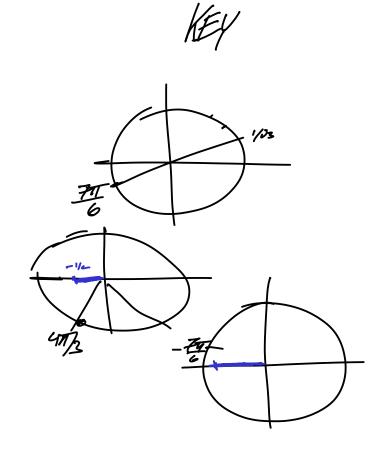
c)
$$\cos(-\frac{7\pi}{6})$$
 = $-\sqrt{3}$

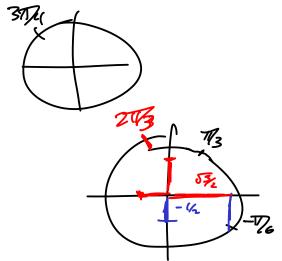
d)
$$\cot \frac{99\pi}{4} = \cot \left(\frac{96\pi}{4} + \frac{3\pi}{4} \right)$$

$$= -1$$

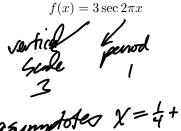
e)
$$\cos^{-1} \frac{\sin(-\frac{\pi}{6})}{-4\pi} = 2\pi$$

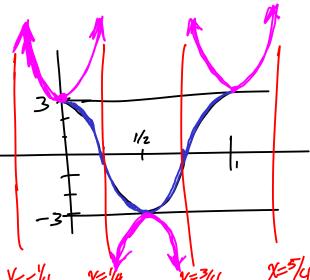
f)
$$\sin^{-1} \frac{\cos(-\frac{\pi}{6})}{\sqrt{3}} = \frac{\pi}{3}$$





2. Write down all the relevant properties (period, amplitude, shifts/scales, asymptotes) of the following trig functions, and then graph by hand.





forget to ald: domain: $X \neq 4 + \frac{n}{2} (n \in \mathbb{Z})$ range = $(-\infty, -3] \cup [3, \infty)$

$$g(x) = -3\tan \pi x$$

Asymptotes $\chi = \frac{1}{2} + \frac{1}{2} (net)$ domain $\chi \neq \frac{1}{2} + \frac{1}{2} (net)$ range R

3. Prove the identities:

$$(3c\theta - \cos\theta)^2 + \sin^2\theta = \tan^2\theta$$

$$(3c\theta - \cos\theta)^2 + \sin^2\theta = 3c^2\theta - 2\sec\theta\cos\theta + \cos^2\theta + \sin^2\theta$$

$$= -2$$

$$= -2$$

$$= -2$$

$$= -2$$

$$= -2$$

$$\frac{\sin \theta}{\sec \theta - \cos \theta} = \cot \theta$$

$$\frac{SM\theta}{SCO} = \frac{SM\theta}{cos\theta} \cdot cos\theta$$

$$= \frac{SM\theta}{1 - cos^{2}\theta}$$

$$= \frac{SM\theta}{SM^{2}\theta}$$

$$= \frac{Cos\theta}{SM\theta}$$

$$= cos\theta$$

4. Use a sum formula to find $\cos(195^{\circ})$.

$$\begin{array}{rcl}
\cos(195^{\circ}) &= \cos(135^{\circ} + 60^{\circ}) \\
&= \cos(374 \cos 73 - \sin(574 \cos 73) \\
&= (-\frac{12}{2})(\frac{1}{2}) - \frac{12}{2} &= -\frac{12}{4}
\end{array}$$

Derive the following half angle formula from the relevant double angle formula:

$$\cos u = \pm \sqrt{\frac{1 + \cos 2u}{2}}$$

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$$\cos u = -\frac{1}{2}$$

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$$\cos u = \pm \sqrt{\frac{1 + \cos 2u}{2}}$$

Use the half angle formula above to find $\cos(195^{\circ})$.

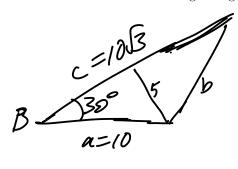
$$05/95^{\circ} = \pm \sqrt{1 + 08.390^{\circ}}$$

$$= \pm \sqrt{1 + 03.2}$$

$$= \pm \sqrt{2 + \sqrt{3}}$$

$$= \pm \sqrt{2 + \sqrt{3}}$$

5. Solve the following triangle: a = 10, $c = 10\sqrt{3}$, $B = 30^{\circ}$.



$$b^{2} = a^{2} + c^{2} - 2ac \cos B$$

$$= 100 + 300 - 2 \cdot 10 \cdot 10\sqrt{3} \cdot \frac{5}{2}$$

$$= 100$$

$$1 = 10$$

$$\frac{SinA}{a} = \frac{SinB}{b} \Rightarrow SinA = \underbrace{asnB}_{b}$$

$$= \underbrace{10 : \pm}_{10}$$

$$A = \overline{U}$$

$$A = \overline{U}$$

$$B + A = \overline{U}$$

$$B + A = \overline{U}$$

$$C = \overline{U} - A - B = 2 \overline{U}_3$$

Solve the following triangle: $a = 10, b = 10, C = 60^{\circ}$.



$$c^{2} = a^{2} + b^{2} - 2abcosC$$

$$= 100 + 100 - 200 \cdot \frac{1}{2}$$

$$= 100$$

$$|C = 10|$$

$$SinA - sinC \Rightarrow sinA = a sinC$$

$$= 10 \cdot \sqrt{7}2 = \sqrt{3}$$

$$|A = \frac{10}{3} \cdot \sqrt{7}2 = \sqrt{3}$$