

# SAP - projekt - Milijarderi

Uspjeh učenika u nastavi

Dora Bezuk, Marcela Matas, Josip Arelic, Domagoj Marinello

13.11.2022.

## Uvod

Pitanja:

1. Ima li neki kontinent statistički značajno više milijarda?
2. Jesu li milijarderi koji su naslijedili bogastvo statistički značajno bogatiji od onih koji nisu?
3. Možete li iz danih varijabli predvidjeti njihovo bogatstvo?
4. Kada biste birali karijeru isključivo prema kriteriju da se obogatite, koju biste industriju izabrali?

## Deskriptivna analiza

Potrebno je učitati podatke.

```
# Pomoćna funkcija za izbacivanje stršećih vrijednosti
remove_outliers <- function(data, data_column) {
  quartiles <- quantile(data_column, probs=c(.25, .75), na.rm = FALSE)
  IQR <- IQR(data_column)
  Lower <- quartiles[1] - 1.5*IQR
  Upper <- quartiles[2] + 1.5*IQR

  return(subset(data, data_column >= Lower & data_column <= Upper))
}

cat('\n Dimenzija podataka: ', dim(bill_data))
```

```
##
```

```
## Dimenzija podataka: 2614 22
```

```
for (col_name in names(bill_data)){
  if (sum(is.na(bill_data[,col_name])) > 0){
    cat('Ukupno nedostajućih vrijednosti za varijablu'
        ,col_name, ': ', sum(is.na(bill_data[,col_name])),'\n')
  }
}
```

```
## Ukupno nedostajućih vrijednosti za varijablu company.name : 38
## Ukupno nedostajućih vrijednosti za varijablu company.relationship : 46
## Ukupno nedostajućih vrijednosti za varijablu company.sector : 23
## Ukupno nedostajućih vrijednosti za varijablu company.type : 36
## Ukupno nedostajućih vrijednosti za varijablu demographics.gender : 34
```

```
## Ukupno nedostajućih vrijednosti za varijablu wealth.type : 22
## Ukupno nedostajućih vrijednosti za varijablu wealth.how.category : 1
## Ukupno nedostajućih vrijednosti za varijablu wealth.how.industry : 1
```

```
summary(bill_data)
```

```
##      name                rank      year      company.founded
## Length:2614      Min.   : 1.0      Min.   :1996      Min.   : 0
## Class :character  1st Qu.: 215.0    1st Qu.:2001    1st Qu.:1936
## Mode :character  Median : 430.0    Median :2014    Median :1963
##                      Mean   : 599.7    Mean   :2008    Mean   :1925
##                      3rd Qu.: 988.0    3rd Qu.:2014    3rd Qu.:1985
##                      Max.    :1565.0    Max.    :2014    Max.    :2012
## company.name      company.relationship company.sector      company.type
## Length:2614      Length:2614      Length:2614      Length:2614
## Class :character  Class :character  Class :character  Class :character
## Mode :character  Mode :character  Mode :character  Mode :character
##
##
##
## demographics.age demographics.gender location.citizenship
## Min.   : -42.00      Length:2614      Length:2614
## 1st Qu.: 47.00      Class :character  Class :character
## Median : 59.00      Mode :character  Mode :character
## Mean   : 53.34
## 3rd Qu.: 70.00
## Max.   : 98.00
## location.country code location.gdp      location.region
## Length:2614      Min.    :0.000e+00      Length:2614
## Class :character  1st Qu.:0.000e+00      Class :character
## Mode :character  Median :0.000e+00      Mode :character
##                      Mean   :1.769e+12
##                      3rd Qu.:7.250e+11
##                      Max.    :1.060e+13
## wealth.type      wealth.worth in billions wealth.how.category
## Length:2614      Min.    : 1.000      Length:2614
## Class :character  1st Qu.: 1.400      Class :character
## Mode :character  Median : 2.000      Mode :character
##                      Mean   : 3.532
##                      3rd Qu.: 3.500
##                      Max.    :76.000
## wealth.how.from emerging wealth.how.industry wealth.how.inherited
## Length:2614      Length:2614      Length:2614
## Class :character  Class :character  Class :character
## Mode :character  Mode :character  Mode :character
##
##
##
## wealth.how.was founder wealth.how.was political
## Length:2614      Length:2614
## Class :character  Class :character
## Mode :character  Mode :character
##
##
##
```

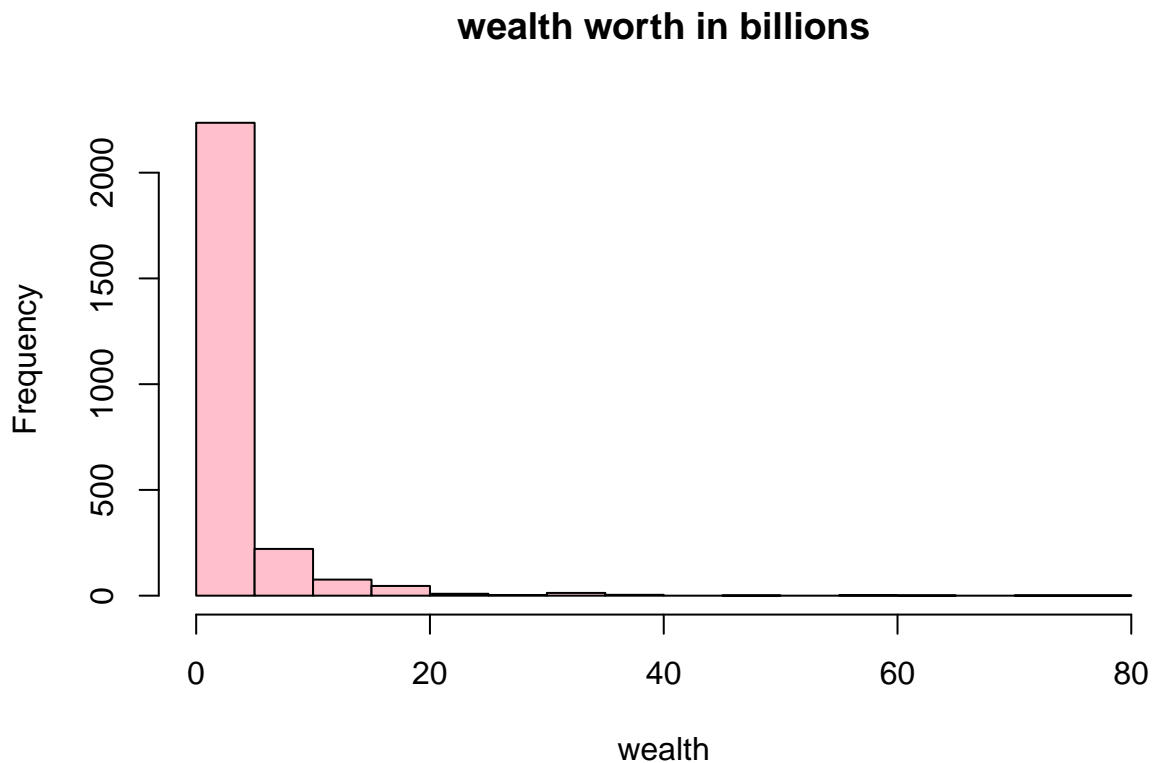
```
sapply(bill_data, class)
```

```
##           name           rank           year
##   "character"      "numeric"      "numeric"
##   company.founded  company.name  company.relationship
##   "numeric"        "character"    "character"
##   company.sector    company.type   demographics.age
##   "character"      "character"    "numeric"
##   demographics.gender location.citizenship location.country code
##   "character"      "character"    "character"
##   location.gdp      location.region  wealth.type
##   "numeric"         "character"    "character"
##   wealth.worth in billions  wealth.how.category wealth.how.from emerging
##   "numeric"              "character"    "character"
##   wealth.how.industry      wealth.how.inherited  wealth.how.was founder
##   "character"             "character"    "character"
##   wealth.how.was political
##   "character"
```

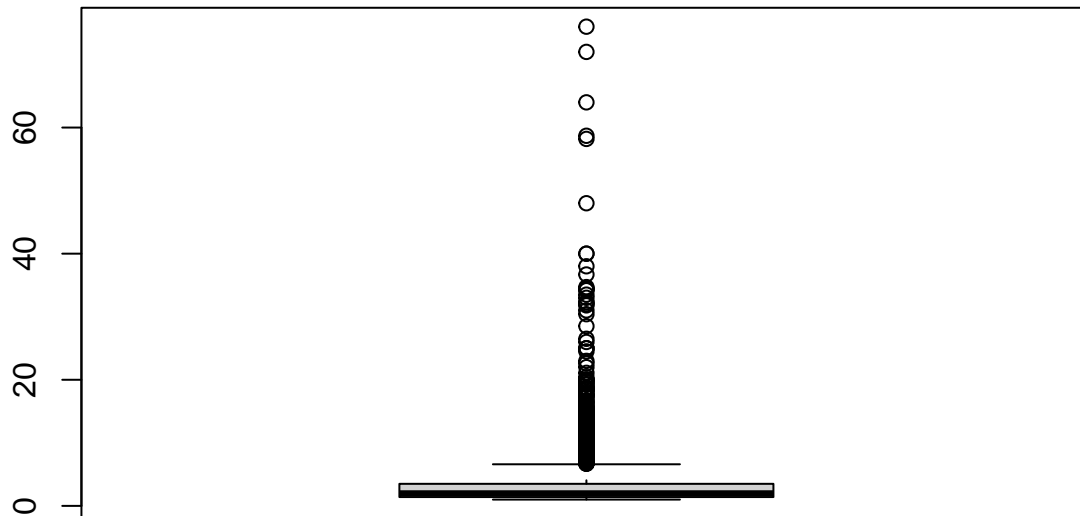
Naš dataset sastoji se od character i numeric varijabli.

Prvo promotrimo numeričke varijable.

```
hist(bill_data$`wealth.worth in billions`, main='wealth worth in billions', xlab='wealth', ylab='Frequency')
```



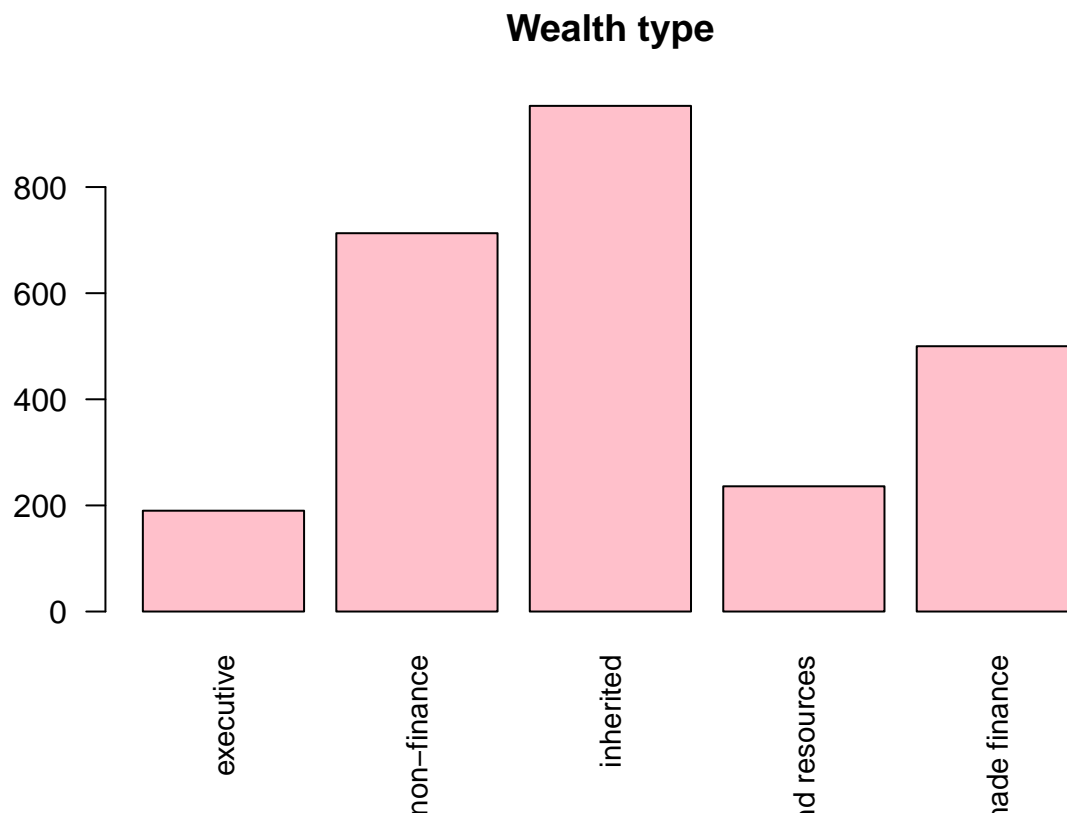
```
boxplot(bill_data$`wealth.worth in billions`)
```



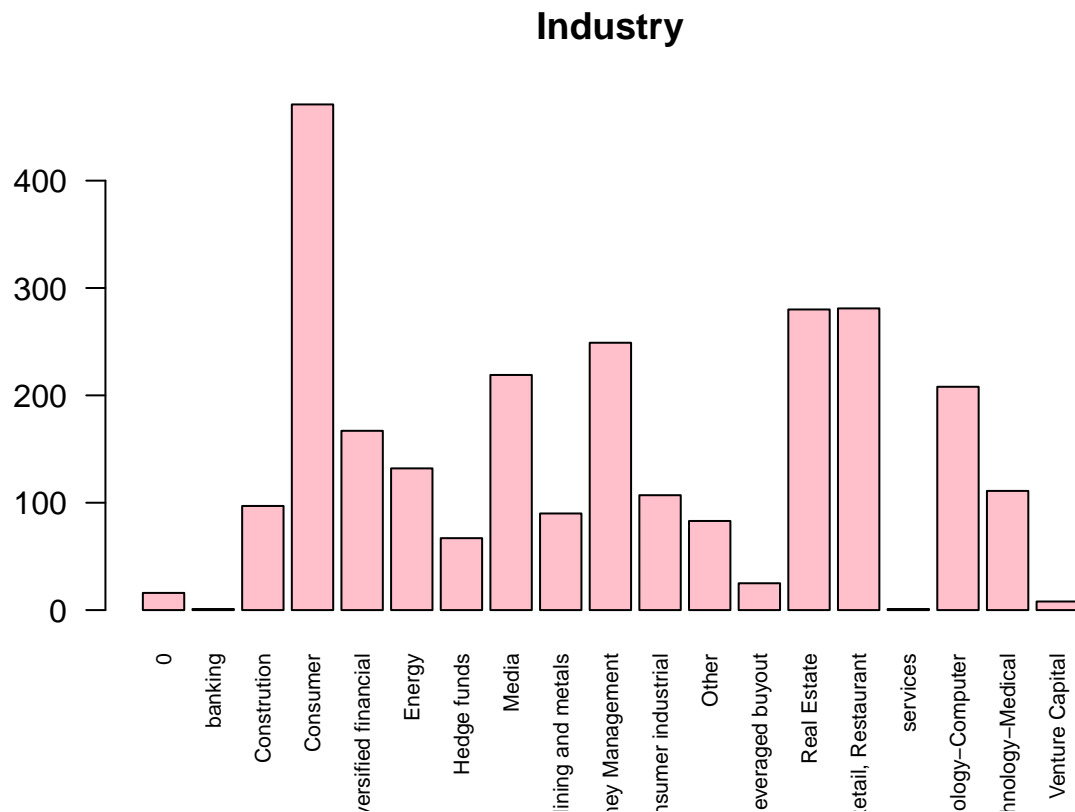
```
summary(bill_data$`wealth.worth in billions`)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      1.000   1.400   2.000   3.532   3.500   76.000
```

```
barplot(table(bill_data$wealth.type),las=2,cex.names=.9,main='Wealth type',col="pink")
```



```
barplot(table(bill_data$wealth.how.industry),las=2,cex.names=.7,main='Industry',col="pink")
```



```
print('Podjela po spolu: ')
```

```
## [1] "Podjela po spolu: "
```

```
table(bill_data$demographics.gender)
```

```
##
##      female      male married couple
##      249      2328          3
```

## Pitanja

### 1. Ima li neki kontinent statistički značajno više milijardi?

```
levels(factor(bill_data$location.region))
```

```
## [1] "0"                "East Asia"
## [3] "Europe"           "Latin America"
## [5] "Middle East/North Africa" "North America"
## [7] "South Asia"       "Sub-Saharan Africa"
```

```
class(bill_data$location.region)
```

```
## [1] "character"
```

Treba li tip stupca biti factor?

Ima li nedostajućih vrijednosti?

```
# is.na ce nam vratiti logical vektor koji ima TRUE na mjestima gdje ima NA:
sum(is.na(bill_data$location.region))
```

```
## [1] 0
```

Nema nedostajućih vrijednosti

```
table(bill_data$location.region)
```

```
##
##              0              East Asia              Europe
##              1              535              698
##      Latin America Middle East/North Africa      North America
##              182              117              992
##      South Asia      Sub-Saharan Africa
##              69              20
```

```
bill_data$location.citizenship[bill_data$location.region == "Middle East/North Africa"]
```

```
## [1] "Saudi Arabia"      "Saudi Arabia"      "Saudi Arabia"
## [4] "Saudi Arabia"      "Kuwait"            "Turkey"
## [7] "Saudi Arabia"      "Turkey"            "Kuwait"
## [10] "Saudi Arabia"      "Turkey"            "Israel"
## [13] "Turkey"            "Lebanon"           "Saudi Arabia"
## [16] "Saudi Arabia"      "Lebanon"           "Saudi Arabia"
## [19] "Saudi Arabia"      "Turkey"            "Israel"
## [22] "Israel"            "Saudi Arabia"       "Israel"
## [25] "Lebanon"           "Turkey"            "Israel"
## [28] "United Arab Emirates" "Saudi Arabia"       "Saudi Arabia"
## [31] "Israel"            "Turkey"            "United Arab Emirates"
## [34] "Israel"            "Turkey"            "Israel"
## [37] "Israel"            "United Arab Emirates" "Saudi Arabia"
## [40] "Israel"            "Israel"            "Bahrain"
## [43] "Saudi Arabia"      "Israel"            "Israel"
## [46] "Saudi Arabia"      "Saudi Arabia"       "Turkey"
## [49] "Saudi Arabia"      "Turkey"            "Israel"
## [52] "Egypt"             "Algeria"           "Egypt"
## [55] "Saudi Arabia"      "Lebanon"           "Lebanon"
## [58] "Israel"            "Turkey"            "Turkey"
## [61] "Egypt"             "Morocco"           "United Arab Emirates"
## [64] "United Arab Emirates" "Israel"            "Israel"
## [67] "Saudi Arabia"      "Egypt"             "Saudi Arabia"
## [70] "Egypt"             "Lebanon"           "Turkey"
## [73] "Turkey"           "Turkey"            "Morocco"
## [76] "Egypt"             "Saudi Arabia"       "Turkey"
## [79] "Turkey"           "Israel"            "Egypt"
## [82] "Israel"            "Turkey"            "Turkey"
## [85] "Turkey"           "Turkey"            "Turkey"
## [88] "Turkey"           "Turkey"            "Lebanon"
## [91] "Morocco"          "Turkey"            "Israel"
## [94] "Israel"            "Kuwait"            "Kuwait"
## [97] "Israel"            "Kuwait"            "Turkey"
## [100] "Turkey"           "Egypt"             "Israel"
## [103] "Morocco"          "Kuwait"            "Kuwait"
## [106] "Turkey"           "Lebanon"           "Lebanon"
## [109] "Oman"             "Israel"            "Turkey"
## [112] "Turkey"           "Oman"              "Turkey"
## [115] "Israel"            "Israel"            "Turkey"
```

Sada možemo združiti podatke ovisno o kontinentu.

Kopirajmo najprije podatke u novi data.frame kako ne bi promijenili prave vrijednosti.

```
bill_data_copy = data.frame(bill_data)
tracemem(bill_data)==tracemem(bill_data_copy)

## [1] FALSE

untracemem(bill_data_copy)
untracemem(bill_data_copy)

# Združimo Europu
for (column_name in c("Europe")){
  bill_data_copy$location.region[bill_data_copy$location.region == column_name] = "Europe";
}

# Združimo Afriku
for (column_name in c("Lebanon","Egypt","Morocco","Algeria")){
  bill_data_copy$location.region[bill_data_copy$location.citizenship == column_name] = "Africa";
}

for (column_name in c("Sub-Saharan Africa")){
  bill_data_copy$location.region[bill_data_copy$location.region == column_name] = "Africa";
}

# združimo Sjevernu Ameriku
for (column_name in c("North America")){
  bill_data_copy$location.region[bill_data_copy$location.region == column_name] = "North America";
}

# Združimo Južnu Ameriku
for (column_name in c("Latin America")){
  bill_data_copy$location.region[bill_data_copy$location.region == column_name] = "South America";
}

# Združimo Aziju
for (column_name in c("East Asia","South Asia")){
  bill_data_copy$location.region[bill_data_copy$location.region == column_name] = "Asia";
}
for (column_name in c("Saudi Arabia","Kuwait","United Arab Emirates","Israel","Turkey","Oman","Bahrain")){
  bill_data_copy$location.region[bill_data_copy$location.citizenship == column_name] = "Asia";
}

bill_data_copy

tbl = table(bill_data_copy$location.region)
print(tbl)

##
##          0          Africa          Asia          Europe North America
##          1           43          699          697           992
## South America
##          182

##continent_frequency=transform(bill_data_copy,continent_frequency=ave(seq(nrow(bill_data_copy)),location.region
```

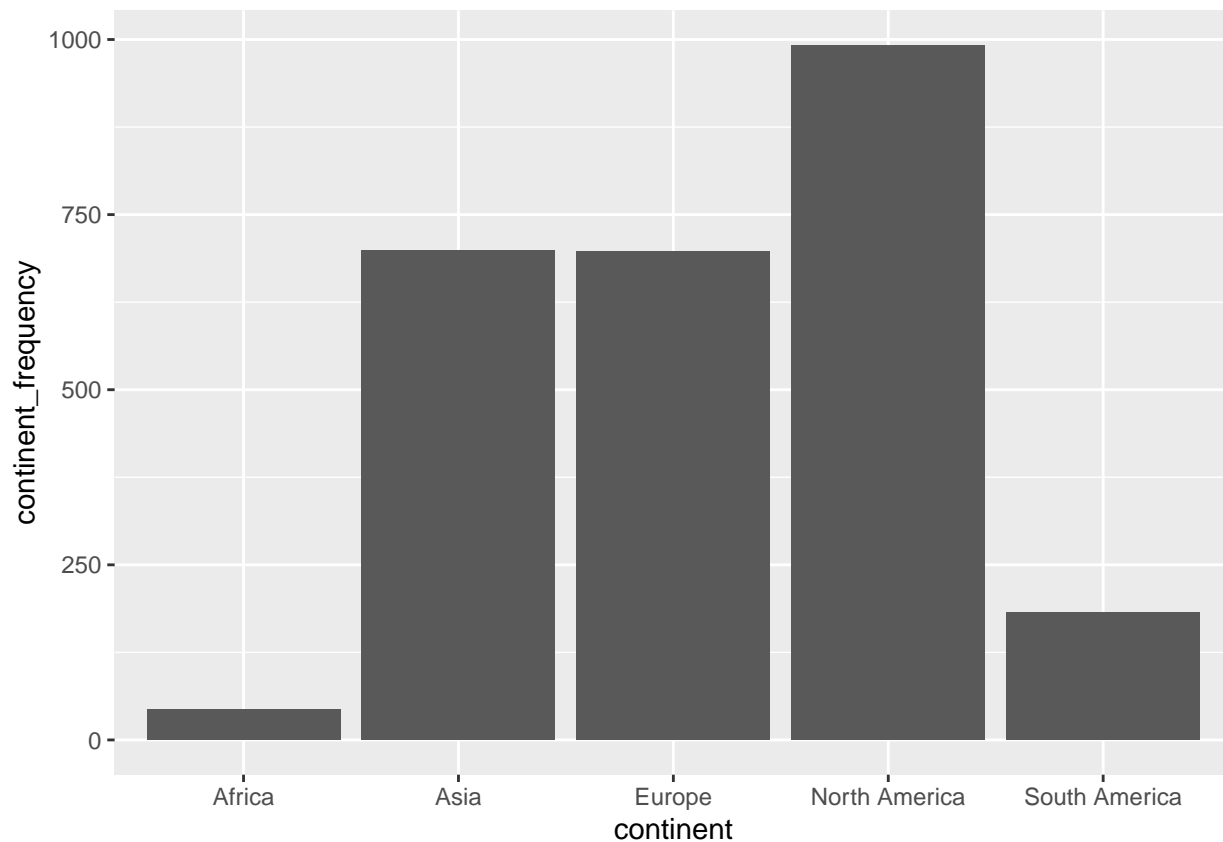
```
,FUN=length) df1=transform(bill_data_copy,continent_frequency=ave(seq(nrow(bill_data_copy)),location.region
,FUN=length)) df1
```

```
df <- data.frame(continent=c("Europe", "Asia", "Africa","North America","South America"),
                 continent_frequency=c(697, 699, 43, 992, 182))
head(df)
```

```
##      continent continent_frequency
## 1      Europe             697
## 2       Asia             699
## 3      Africa              43
## 4 North America           992
## 5 South America          182
```

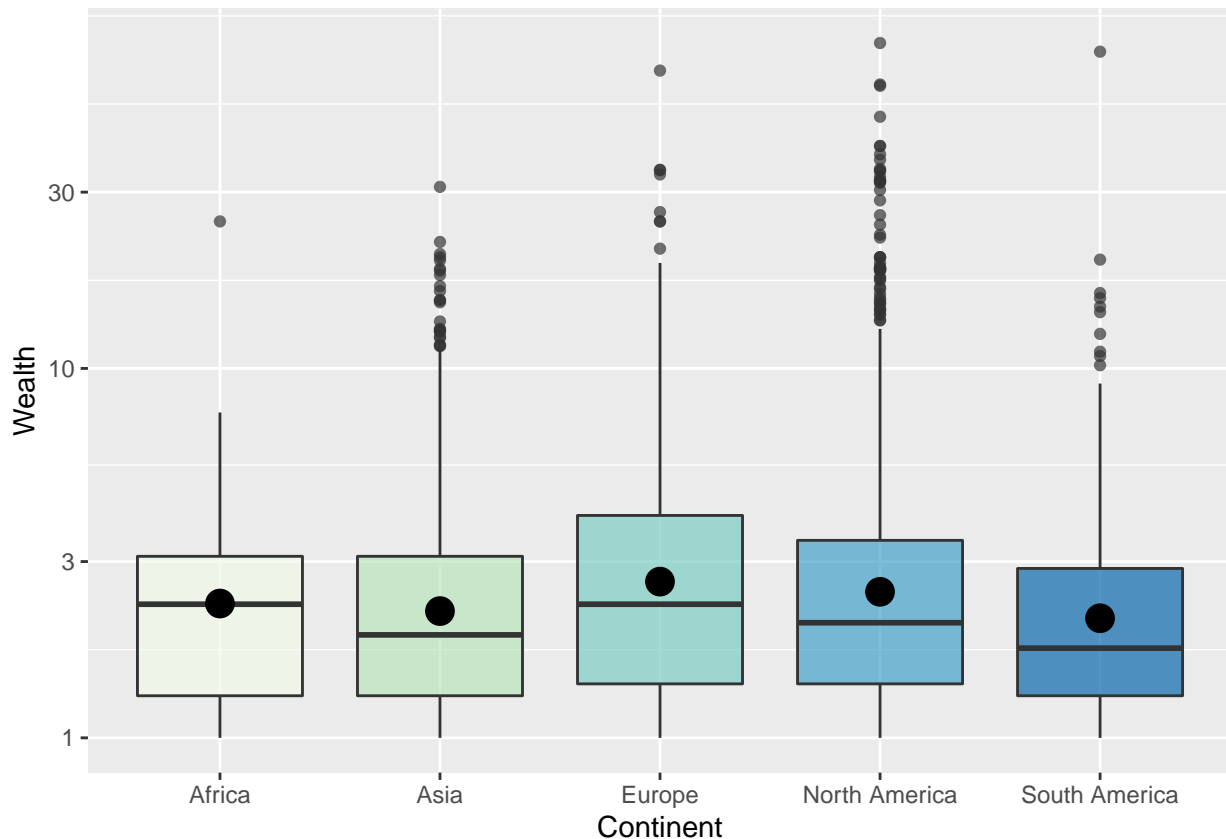
```
library(ggplot2)
```

```
# Barplot
p<-ggplot(data=df, aes(x=continent, y=continent_frequency)) +
  geom_bar(stat="identity")
p
```



```
box_edu <- ggplot(bill_data_copy %>% filter(!location.region=="0"), aes(x=location.region, y= wealth.wor
  geom_boxplot(alpha=0.7, ) + scale_y_log10() +
  stat_summary(fun=mean, geom="point", shape=20, size=7, color="black", fill="black") +
  theme(legend.position="none") + labs(x="Continent",y="Wealth")+
  scale_fill_brewer(name="Continent",palette="GnBu")
box_edu
```





Pretpostavke ANOVA-e su:

- nezavisnost pojedinih podataka u uzorcima,
- normalna razdioba podataka,
- homogenost varijanci među populacijama.

Kad su veličine grupa podjednake, ANOVA je relativno robusna metoda na blaga odstupanja od pretpostavke normalnosti i homogenosti varijanci. Ipak, dobro je provjeriti koliko su ta odstupanja velika.

Provjera normalnosti može se za svaku pojedinu grupu napraviti KS testom ili Lillieforsovom inačicom KS testa. U ovom slučaju razmatrat ćemo `location.region` kao varijablu koja određuje grupe (populacije) i `wealth` kao zavisnu varijablu.

```
# TODO: zakomentiraj ovu liniju ako ne želimo logaritmirati cijenu
```

```
wealth <- log(bill_data_copy$wealth.worth.in.billions, 2)
```

```
require(nortest)
```

```
## Loading required package: nortest
```

```
lillie.test(wealth)
```

```
##
```

```
## Lilliefors (Kolmogorov-Smirnov) normality test
```

```
##
```

```
## data: wealth
```

```
## D = 0.11777, p-value < 2.2e-16
```

```
lillie.test(wealth[bill_data_copy$location.region=='Africa'])
```

```
##
```

```
## Lilliefors (Kolmogorov-Smirnov) normality test
##
## data:  wealth[bill_data_copy$location.region == "Africa"]
## D = 0.12187, p-value = 0.112
lillie.test(wealth[bill_data_copy$location.region=='Europe'])

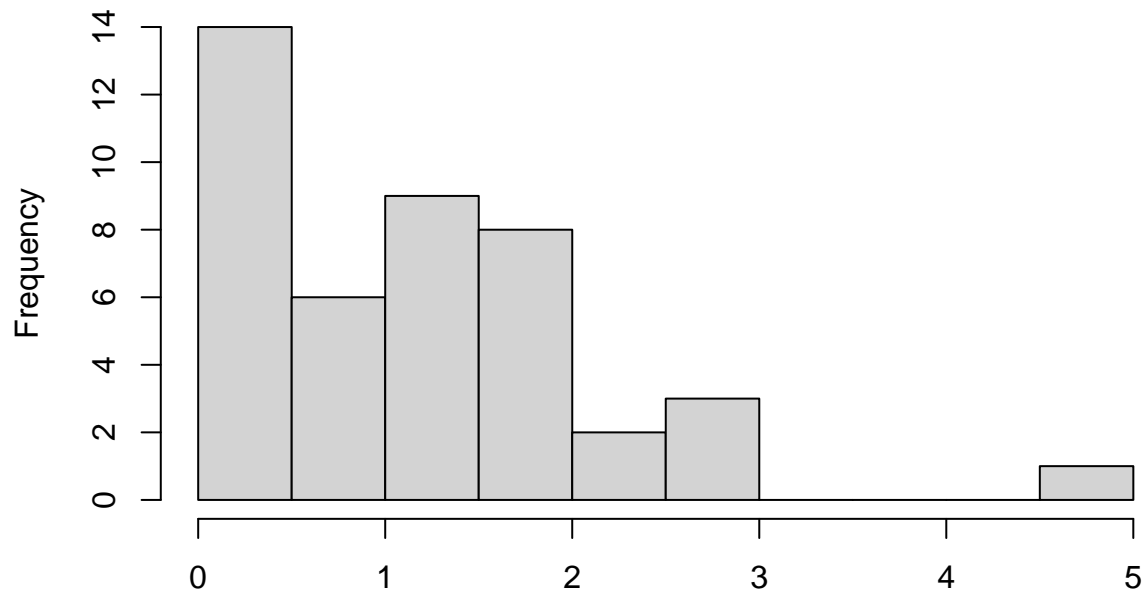
##
## Lilliefors (Kolmogorov-Smirnov) normality test
##
## data:  wealth[bill_data_copy$location.region == "Europe"]
## D = 0.099476, p-value < 2.2e-16
lillie.test(wealth[bill_data_copy$location.region=='South America'])

##
## Lilliefors (Kolmogorov-Smirnov) normality test
##
## data:  wealth[bill_data_copy$location.region == "South America"]
## D = 0.14997, p-value = 9.745e-11
lillie.test(wealth[bill_data_copy$location.region=='North America'])

##
## Lilliefors (Kolmogorov-Smirnov) normality test
##
## data:  wealth[bill_data_copy$location.region == "North America"]
## D = 0.12148, p-value < 2.2e-16
lillie.test(wealth[bill_data_copy$location.region=='Asia'])

##
## Lilliefors (Kolmogorov-Smirnov) normality test
##
## data:  wealth[bill_data_copy$location.region == "Asia"]
## D = 0.12016, p-value < 2.2e-16
hist(wealth[bill_data_copy$location.region=='Africa'])
```

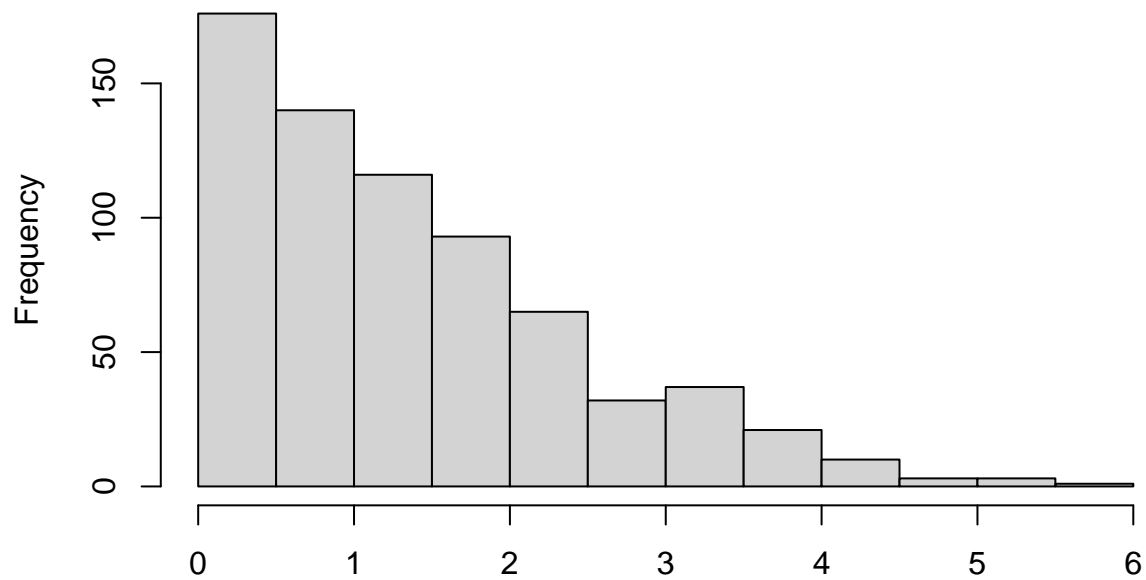
**Histogram of wealth[`bill_data_copy$location.region == "Africa"`]**



`wealth[bill_data_copy$location.region == "Africa"]`

```
hist(wealth[bill_data_copy$location.region=='Europe'])
```

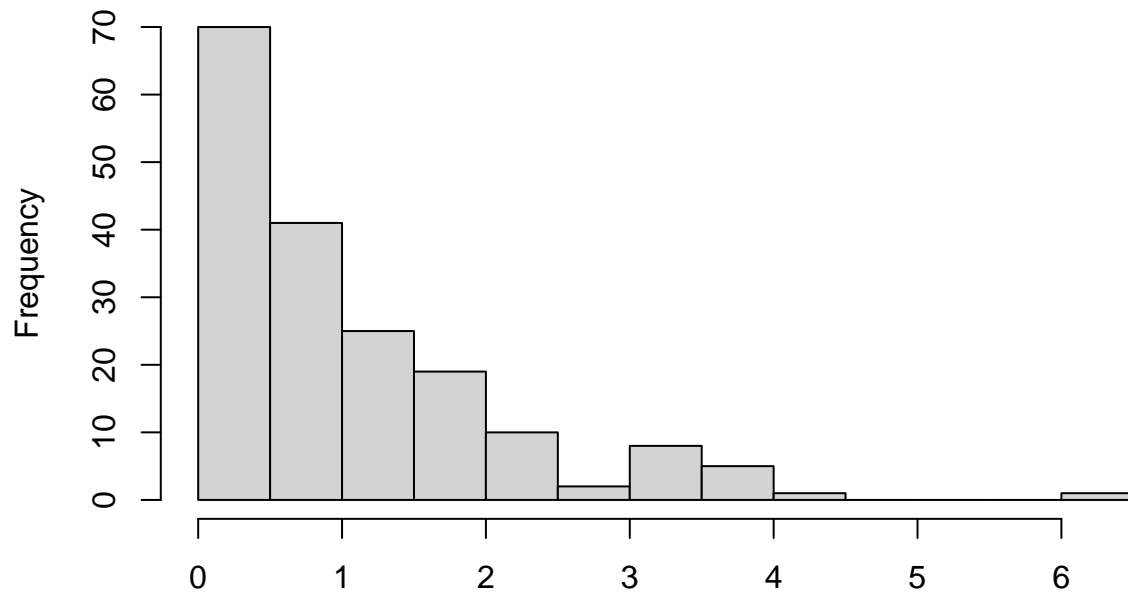
**Histogram of wealth[`bill_data_copy$location.region == "Europe"`]**



`wealth[bill_data_copy$location.region == "Europe"]`

```
hist(wealth[bill_data_copy$location.region=='South America'])
```

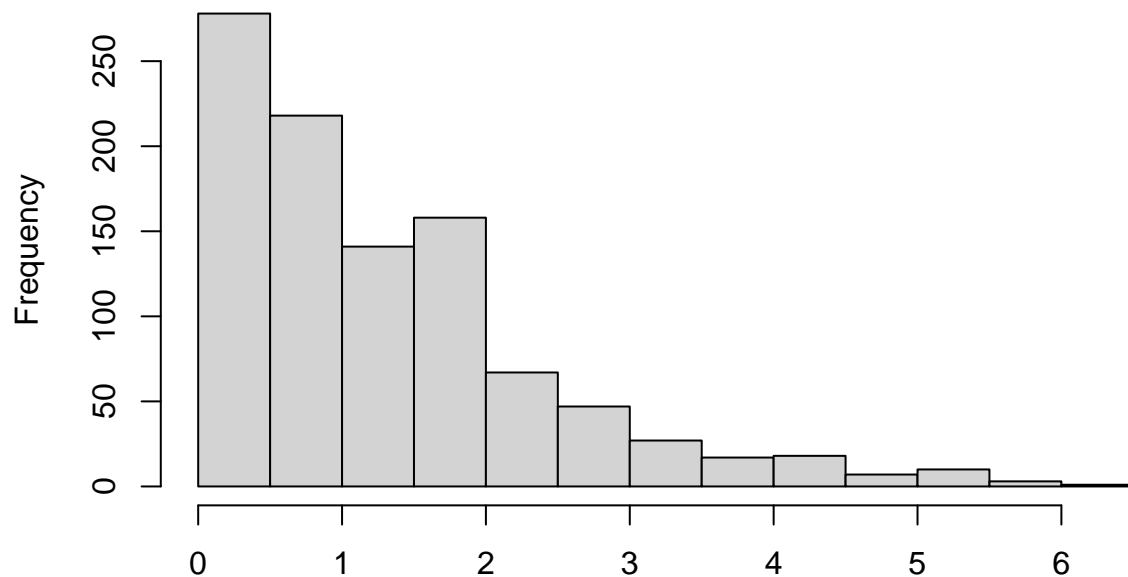
### Histogram of wealth[`bill_data_copy$location.region == "South Americ`



```
wealth[bill_data_copy$location.region == "South America"]
```

```
hist(wealth[bill_data_copy$location.region=='North America'])
```

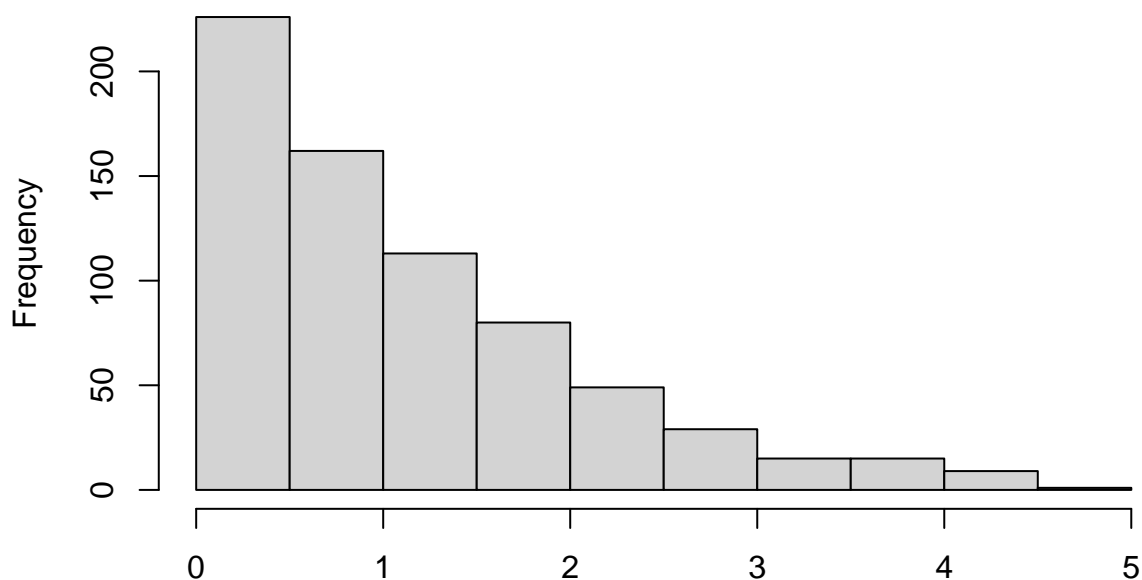
### Histogram of wealth[`bill_data_copy$location.region == "North Americ`



```
wealth[bill_data_copy$location.region == "North America"]
```

```
hist(wealth[bill_data_copy$location.region=='Asia'])
```

## Histogram of wealth[`bill_data_copy$location.region == "Asia"`]



wealth[`bill_data_copy$location.region == "Asia"`]

```
# Testiranje homogenosti varijance uzoraka Bartlettovim testom
```

```
##bartlett.test(bill_data_copy$wealth.worth.in.billions ~ bill_data_copy$location.region)
```

```
var((wealth[bill_data_copy$location.region=='Africa']))
```

```
## [1] 0.8784496
```

```
var((wealth[bill_data_copy$location.region=='Asia']))
```

```
## [1] 0.9424432
```

```
var((wealth[bill_data_copy$location.region=='Europe']))
```

```
## [1] 1.196035
```

```
var((wealth[bill_data_copy$location.region=='North America']))
```

```
## [1] 1.265199
```

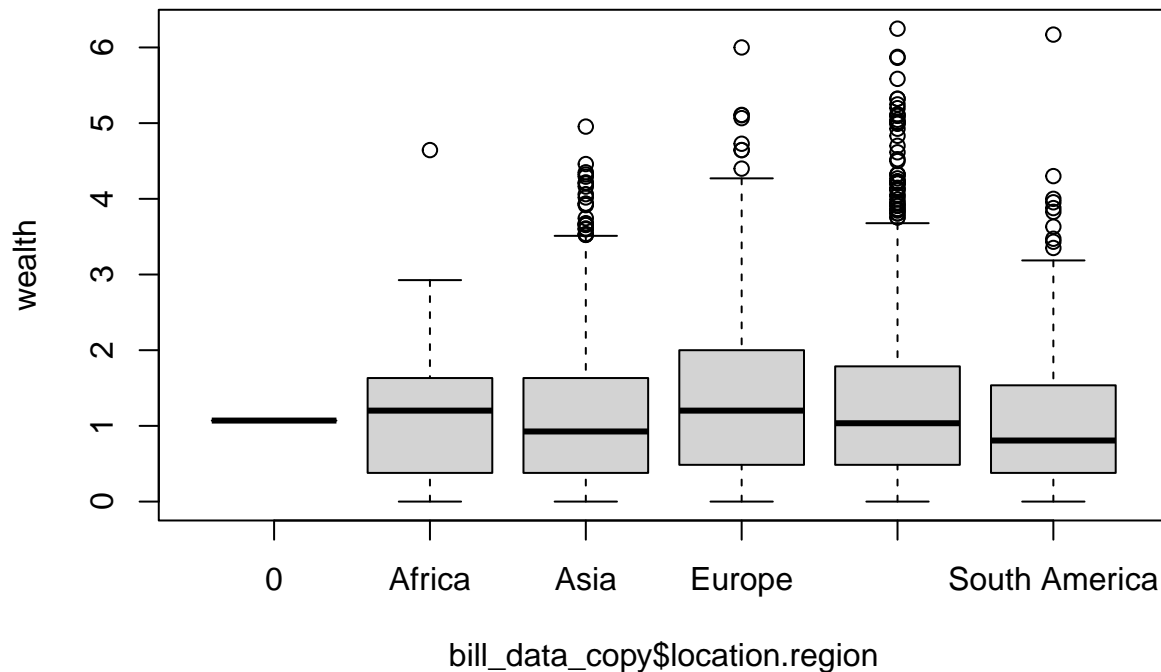
```
var((wealth[bill_data_copy$location.region=='South America']))
```

```
## [1] 1.076448
```

Provjerimo postoje li razlike u prihodima za različite razine školovanja klijenata.

```
# Graficki prikaz podataka
```

```
boxplot(wealth ~ bill_data_copy$location.region)
```



```
# Test
a = aov(wealth ~ bill_data_copy$location.region)
summary(a)

##               Df Sum Sq Mean Sq F value    Pr(>F)
## bill_data_copy$location.region    5   33.4    6.689    5.862 2.15e-05 ***
## Residuals                2608 2975.8    1.141
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

## 2. Jesu li milijarderi koji su nasljedili bogastvo statistički značajno bogatiji od onih koji nisu?

Potrebno je pripremiti podatke za obradu, razdvojiti podatke iz tablice po polju `how.inherited` u dva slučaja: `inherited` (oni koju su nasljedili bogatstvo) i `non_inherited` (oni koji nisu nasljedili bogatstvo).

```
inherited = bill_data[bill_data$wealth.how.inherited!="not inherited",]
```

```
## tracemem[0x60000272e4c0 -> 0x6000027142a0]: lapply tbl_subset_row [.tbl_df [ eval eval withVisible w
```

```
non_inherited = bill_data[bill_data$wealth.how.inherited=="not inherited",]
```

```
## tracemem[0x60000272e4c0 -> 0x600002715ea0]: lapply tbl_subset_row [.tbl_df [ eval eval withVisible w
```

Zatim je potrebno izračunati srednju vrijednost (mean) posebno za svaki slučaj uzimajući u obzir polje `worth.in billions`.

```
inherited_mean = mean(inherited$`wealth.worth in billions`)
print(inherited_mean)
```

```
## [1] 3.750756
```

```
non_inherited_mean = mean(non_inherited$`wealth.worth in billions`)
print(non_inherited_mean)
```

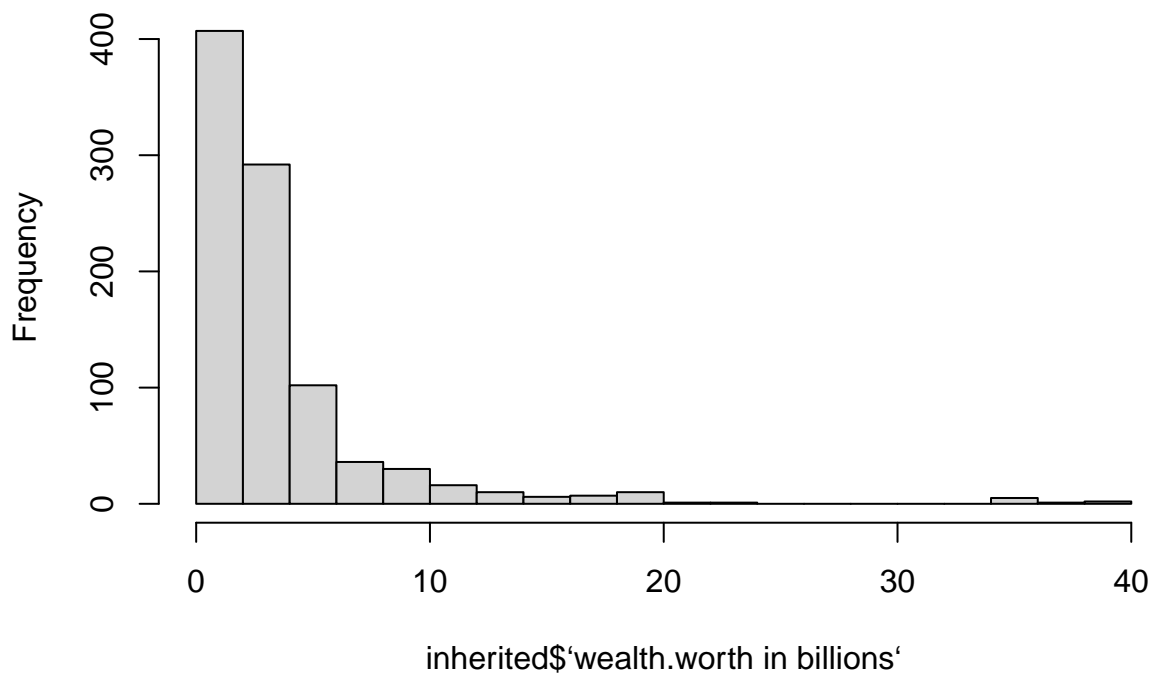
```
## [1] 3.411908
```

Na temelju male razlike u srednjim vrijednostima, ne postoje indikacije da su milijarderi koji su nasljedili bogatstvo statistički značajno bogatiji od onih koji nisu. No, navedeno je potrebno provjeriti.

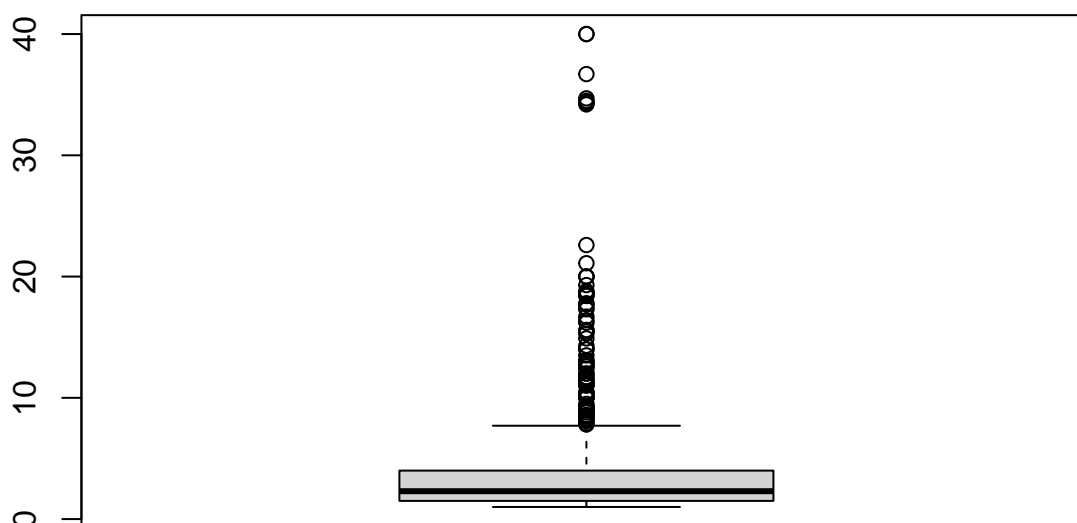
Kako bi bolje vizualizirali podatke crtamo histogram i box plot za svaki od slučajeva:

```
hist(inherited$`wealth.worth in billions`, breaks = 20)
```

**Histogram of inherited\$`wealth.worth in billions`**

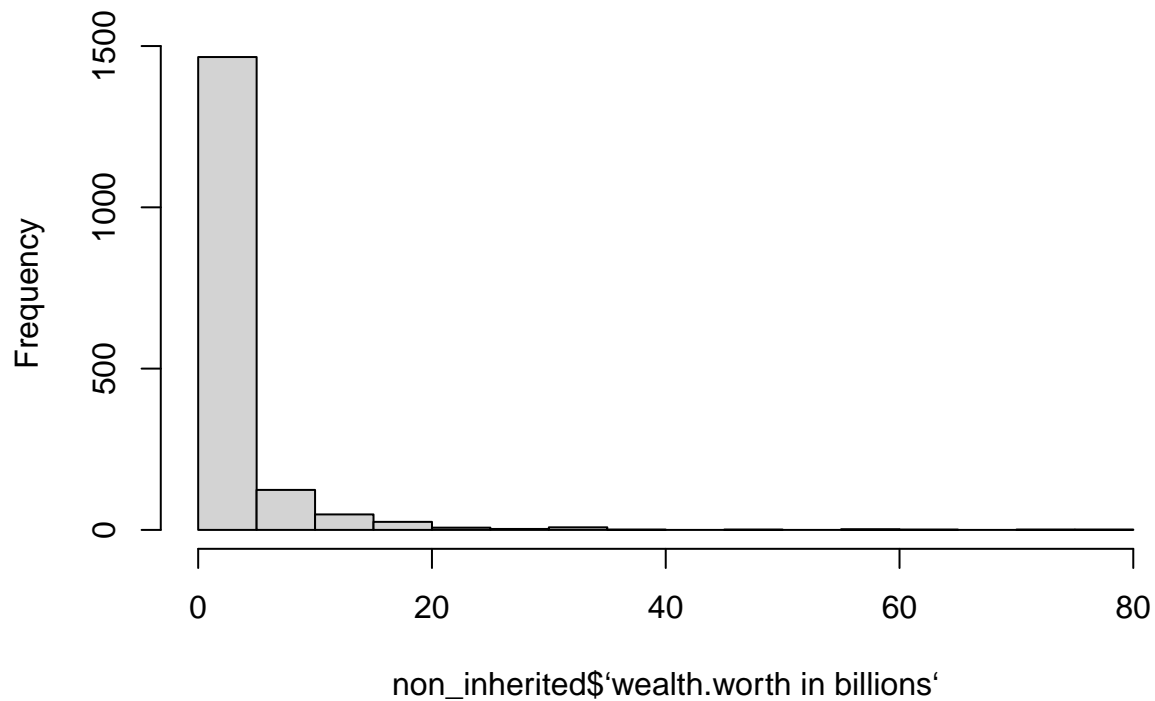


```
boxplot(inherited$`wealth.worth in billions`)
```

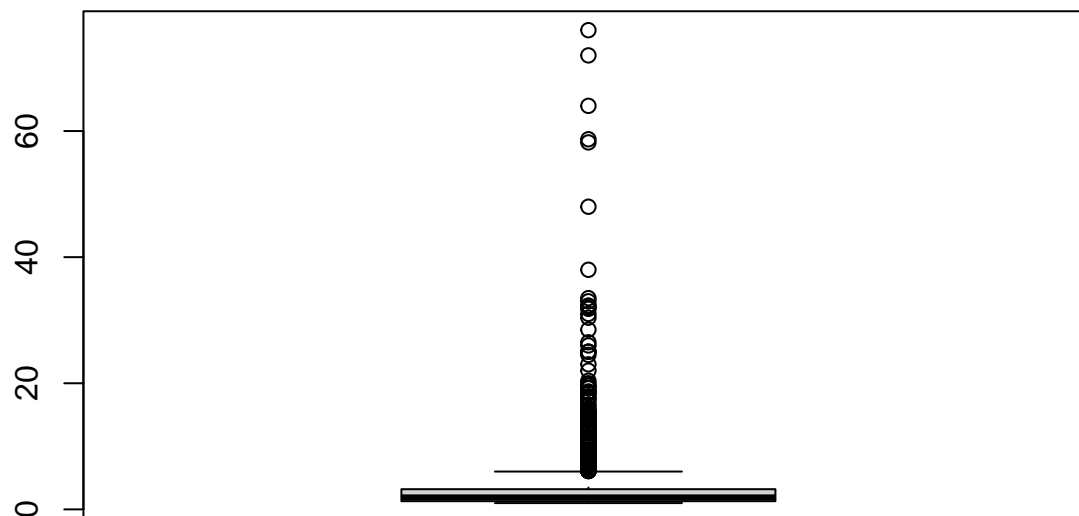


```
hist(non_inherited$`wealth.worth in billions`, breaks = 20)
```

## Histogram of non\_inherited\$`wealth.worth in billions`



```
boxplot(non_inherited$`wealth.worth in billions`)
```



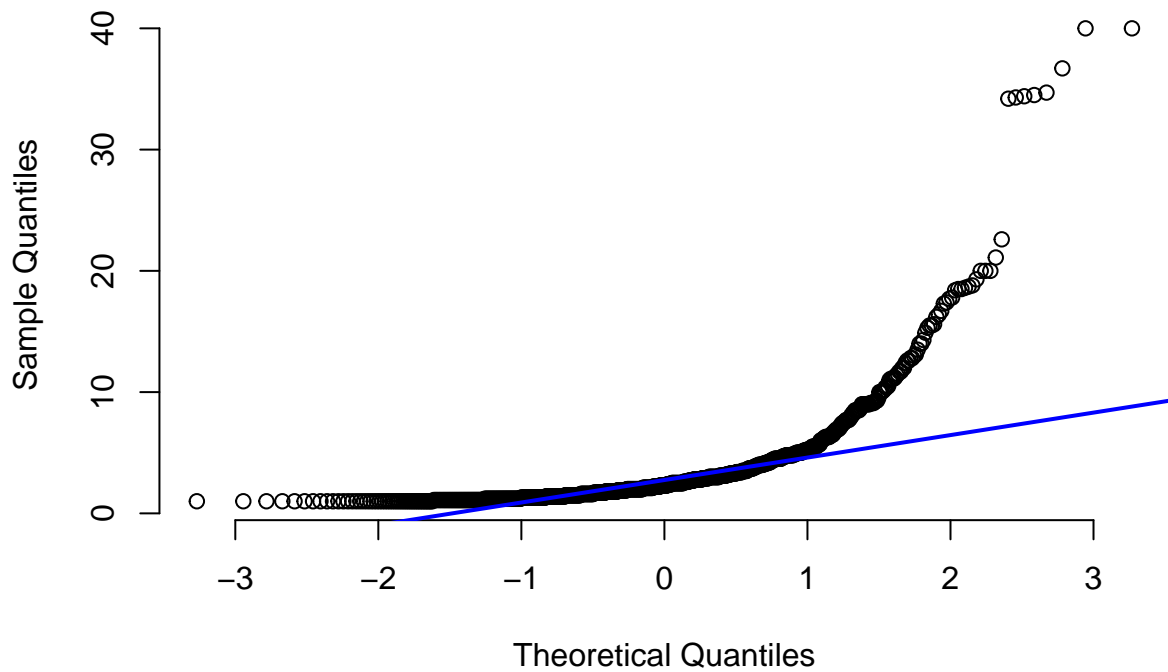
Iz prikazane vizualizacije uočavamo kako se podaci ne ravnaју po normalnoj distribuciji.

Što se može bolje vidjeti sa sljedećih prikaza:

```
qqnorm(inherited$`wealth.worth in billions`, pch = 1, frame = FALSE, main='Inherited')  
qqline(inherited$`wealth.worth in billions`, col = "blue", lwd = 2)
```

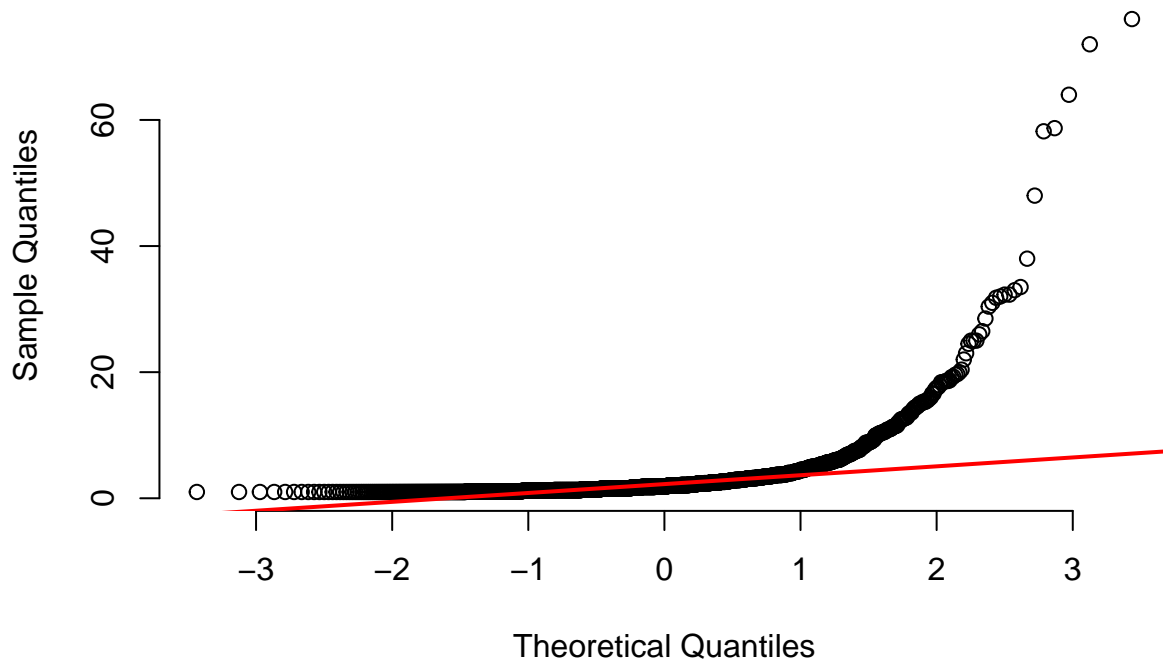


## Inherited



```
qqnorm(non_inherited$`wealth.worth in billions`, pch = 1, frame = FALSE, main = 'Non inherited')  
qqline(non_inherited$`wealth.worth in billions`, col = "red", lwd = 2)
```

## Non inherited



Ipak, uočeno je potrebno dodatno ispitati koristeći Kolmogorov–Smirnov test kojim se utvrđuje ravna li se distribucija po normalnoj razdiobi.

```
ks.test(inherited$`wealth.worth in billions`, y="pnorm")
```

```
## Warning in ks.test(inherited$`wealth.worth in billions`, y = "pnorm"): ties  
## should not be present for the Kolmogorov-Smirnov test
```

```
##  
## One-sample Kolmogorov-Smirnov test  
##  
## data: inherited$`wealth.worth in billions`  
## D = 0.84134, p-value < 2.2e-16  
## alternative hypothesis: two-sided
```

```
ks.test(non_inherited$`wealth.worth in billions`, y="pnorm")
```

```
## Warning in ks.test(non_inherited$`wealth.worth in billions`, y = "pnorm"): ties  
## should not be present for the Kolmogorov-Smirnov test
```

```
##  
## One-sample Kolmogorov-Smirnov test  
##  
## data: non_inherited$`wealth.worth in billions`  
## D = 0.84134, p-value < 2.2e-16  
## alternative hypothesis: two-sided
```

Iz dobivenih p vrijednosti u oba slučaja odbacujemo mogućnost da se distribucije ravnaju po normalnoj razdiobi.

Time je potvrđena pretpostavka da se podaci ne ravnaju po normalnoj distribuciji.

Potrebno je koristiti neparametarski test Mann–Whitney U test, koji se koristi kada se podaci se ravnaju po istim distribucijama (obje distribucije su nakošene u desno) i uzorci su nezavisni iz jedne i druge populacije (jedna osoba ne može naslijediti i nenaslijediti bogatstvo).

Hipoteze glase:

$$H_0 : \mu_1 = \mu_2$$

$$H_1 : \mu_1 > \mu_2$$

```
wilcox.test(inherited_mean, non_inherited_mean, alt = "greater")
```

```
##  
## Wilcoxon rank sum exact test  
##  
## data: inherited_mean and non_inherited_mean  
## W = 1, p-value = 0.5  
## alternative hypothesis: true location shift is greater than 0
```

Zbog p-vrijednost jednake 0.5, na temelju značajnosti od 50% ne možemo odbaciti  $H_0$  hipotezu o jednakosti prosječnih vrijednosti bogatstva u korist  $H_1$ , odnosno možemo reći da milijarderi koji su naslijedili bogatstvo nisu statistički značajno bogatiji od onih koji nisu.

### 3. Možete li iz danih varijabli predvidjeti njihovo bogatstvo?

- je li dobro tu koristiti sve milijardere s popisa 2014 + milijarderi s prethodnih popisa (ako nisu na popisu iz 2014. godine)

```
# bill_data
```

```
# Izbacujemo stupce:
```

```
# name
```

```
# company.name
# rank
# location.gdp, više od pola vrijednosti su 0 (netočan podatak)
# location.countrny.code i location.citizenship a koristimo location.region koji je veće granulacije
# wealth.how.from emerging, wealth.how.was founder, wealth.how.was political su konstantne varijable
# company.sector jer ima previše različitih vrijednosti, koje kad bi one hot encodali bi dali previše s

exclude_cols = c("name", "company.name", "rank", "location.gdp", "location.country code", "location.citizenship")

# exclude columns and sort
bill_data_clean <- bill_data %>% select(-one_of(exclude_cols)) %>% arrange(year)

# to lowercase for consistency
bill_data_clean[["company.relationship"]] <- tolower(bill_data_clean[["company.relationship"]])

# remove invalid data
bill_data_clean <- bill_data_clean %>% filter(demographics.age > 0)
bill_data_clean <- bill_data_clean %>% filter(!location.region == "0")

# inflation rate $1.00 (1996) -> $1.51 (2014), +50.9%
# inflation rate $1.00 (2001) -> $1.34 (2014), +33.7%
bill_data_clean[bill_data_clean$year == "1996", "wealth.worth in billions"] <- bill_data_clean[bill_data_clean$year == "1996", "wealth.worth in billions"] * 1.51
bill_data_clean[bill_data_clean$year == "2001", "wealth.worth in billions"] <- bill_data_clean[bill_data_clean$year == "2001", "wealth.worth in billions"] * 1.34

# Iskoristili smo godinu da ažuriramo cijene (inflacija), sad ju odbacujemo
bill_data_clean <- bill_data_clean %>% select(., -year)

# merge similar roles to avoid 1 column = 1 row data
bill_data_clean$company.relationship <- gsub(".*\\b(owner)\\b.*", "owner", bill_data_clean$company.relationship)
bill_data_clean$company.relationship <- gsub(".*(ceo|chief executive officeor|chief executive officer|chairman|founder|director|head|president).*", "ceo", bill_data_clean$company.relationship)
bill_data_clean$company.relationship <- gsub(".*(founder).*", "founder", bill_data_clean$company.relationship)
bill_data_clean$company.relationship <- gsub(".*(chair|chari).*", "chairman", bill_data_clean$company.relationship)
bill_data_clean$company.relationship <- gsub(".*(director).*", "director", bill_data_clean$company.relationship)
bill_data_clean$company.relationship <- gsub(".*(head).*", "head", bill_data_clean$company.relationship)
bill_data_clean$company.relationship <- gsub(".*(president).*", "president", bill_data_clean$company.relationship)

# drop small amount of rows with na values
bill_data_clean <- bill_data_clean %>% drop_na()

# split dataset to numeric and categorical (non-ordinal)
bill_categorical <- bill_data_clean %>% select(where(is_character))
bill_numeric <- bill_data_clean %>% select(where(is.numeric))

# one hot encode categorical data
bill_categorical_onehot = dummy_cols(bill_categorical, remove_first_dummy = TRUE, remove_selected_columns = TRUE)

# filter indicators with 5 or more rows, indicators with less than 5 would cause problems
bill_categorical_onehot <- bill_categorical_onehot[, colSums(bill_categorical_onehot) > 5]

# concat numerical and categorical columns
bill_data_clean <- bind_cols(bill_numeric, bill_categorical_onehot)

# remove variables which strongly and linearly correlate
correlation_threshold = 0.9
```

```

tmp <- cor(bill_data_clean)
tmp[upper.tri(tmp)] <- 0
diag(tmp) <- 0 # clean diagonal which is always 1
bill_data_clean <- bill_data_clean[, apply(tmp,2,function(x) all(x<= correlation_threshold))]

# remove outliers
# TODO: zakomentiraj ovu liniju ako ne želimo removeati outliere
bill_data_clean <- remove_outliers(bill_data_clean, bill_data_clean$`wealth.worth in billions`)

# extract y column for later use
wealth <- bill_data_clean$`wealth.worth in billions`

# TODO: zakomentiraj ovu liniju ako ne želimo logaritmirati cijenu
# wealth <- log(wealth, 2)

# x setup, y = wealth
normalized<-function(y) {
  x<-y[!is.na(y)]
  x<-(x - min(x)) / (max(x) - min(x))
  y[!is.na(y)]<-x
  return(y)
}

# `wealth.how.industry_Retail, Restaurant` casues fitting issues
exclude_cols = c("wealth.worth in billions", "wealth.how.industry_Retail, Restaurant")
x <- bill_data_clean %>% select(-one_of(exclude_cols))
x[, c("company.founded", "demographics.age")] <- apply(x[, c("company.founded", "demographics.age")], 2, function(x) {
  x <- x[order(colnames(x))]
  return(x)
})

model_all_vars <- lm(wealth ~ . , x)
summary(model_all_vars)

##
## Call:
## lm(formula = wealth ~ ., data = x)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.5317 -1.0244 -0.3629  0.6162  5.0657
##
## Coefficients:
##              Estimate Std. Error
## (Intercept)      1.61419    1.17790
## company.founded      0.41979    0.60953
## company.relationship_chairman -0.28734    0.20051
## company.relationship_director -0.80622    0.68723
## company.relationship_founder -0.34965    0.17998
## company.relationship_investor -0.51311    0.29097
## company.relationship_owner -0.75785    0.22154
## company.relationship_president  0.12327    0.42778
## company.type_aquired -1.29221    0.41931
## company.type_new -1.37453    0.40406
## company.type_privatization -1.61248    0.48589
## company.type_subsidiary -2.58826    0.73477

```

## demographics.age	1.26004	0.23747
## demographics.gender_male	0.19710	0.13437
## location.region_Europe	0.16762	0.10820
## `location.region_Latin America`	-0.46210	0.15787
## `location.region_Middle East/North Africa`	-0.20107	0.18424
## `location.region_North America`	0.12757	0.09931
## `location.region_South Asia`	-0.27365	0.21188
## `location.region_Sub-Saharan Africa`	0.60954	0.36632
## wealth.how.category_Financial	0.57625	0.60382
## `wealth.how.category_New Sectors`	-2.28107	1.64451
## `wealth.how.category_Non-Traded Sectors`	0.93174	0.49731
## `wealth.how.category_Resource Related`	-0.95728	0.83705
## `wealth.how.category_Traded Sectors`	-0.71926	0.69180
## wealth.how.industry_Construction	-0.39673	0.20547
## wealth.how.industry_Consumer	1.58716	0.84381
## `wealth.how.industry_Diversified financial`	0.46262	0.68373
## wealth.how.industry_Energy	1.54698	0.96578
## `wealth.how.industry_Hedge funds`	0.35839	0.69779
## wealth.how.industry_Media	0.31209	0.15984
## `wealth.how.industry_Mining and metals`	1.59869	0.97105
## `wealth.how.industry_Money Management`	0.55354	0.67792
## `wealth.how.industry_Non-consumer industrial`	1.49457	0.86078
## wealth.how.industry_Other	0.50130	0.51415
## `wealth.how.industry_Private equity/leveraged buyout`	1.12879	0.73749
## `wealth.how.industry_Real Estate`	0.41929	0.67375
## `wealth.how.industry_Technology-Computer`	3.34813	1.71775
## `wealth.how.industry_Technology-Medical`	2.79229	1.70488
## `wealth.how.industry_Venture Capital`	-0.11704	0.85116
## `wealth.how.inherited_4th generation`	0.22361	0.23883
## `wealth.how.inherited_5th generation or longer`	-0.15492	0.35896
## wealth.how.inherited_father	0.19327	0.14990
## `wealth.how.inherited_not inherited`	-0.11821	0.75791
## `wealth.how.inherited_spouse/widow`	-0.28484	0.29805
## `wealth.type_founder non-finance`	0.56035	0.19385
## wealth.type_inherited	0.41711	0.76615
## `wealth.type_privatized and resources`	0.59664	0.23540
## `wealth.type_self-made finance`	0.11468	0.21904
##	t value	Pr(> t )
## (Intercept)	1.370	0.170722
## company.founded	0.689	0.491087
## company.relationship_chairman	-1.433	0.152012
## company.relationship_director	-1.173	0.240881
## company.relationship_founder	-1.943	0.052190 .
## company.relationship_investor	-1.763	0.077981 .
## company.relationship_owner	-3.421	0.000637 ***
## company.relationship_president	0.288	0.773248
## company.type_aquired	-3.082	0.002087 **
## company.type_new	-3.402	0.000683 ***
## company.type_privatization	-3.319	0.000921 ***
## company.type_subsidary	-3.523	0.000437 ***
## demographics.age	5.306	1.25e-07 ***
## demographics.gender_male	1.467	0.142586
## location.region_Europe	1.549	0.121499
## `location.region_Latin America`	-2.927	0.003461 **

```
## `location.region_Middle East/North Africa` -1.091 0.275264
## `location.region_North America` 1.285 0.199097
## `location.region_South Asia` -1.292 0.196674
## `location.region_Sub-Saharan Africa` 1.664 0.096288 .
## wealth.how.category_Financial 0.954 0.340031
## `wealth.how.category_New Sectors` -1.387 0.165576
## `wealth.how.category_Non-Traded Sectors` 1.874 0.061140 .
## `wealth.how.category_Resource Related` -1.144 0.252916
## `wealth.how.category_Traded Sectors` -1.040 0.298608
## wealth.how.industry_Construction -1.931 0.053649 .
## wealth.how.industry_Consumer 1.881 0.060130 .
## `wealth.how.industry_Diversified financial` 0.677 0.498730
## wealth.how.industry_Energy 1.602 0.109365
## `wealth.how.industry_Hedge funds` 0.514 0.607585
## wealth.how.industry_Media 1.953 0.051021 .
## `wealth.how.industry_Mining and metals` 1.646 0.099852 .
## `wealth.how.industry_Money Management` 0.817 0.414297
## `wealth.how.industry_Non-consumer industrial` 1.736 0.082672 .
## wealth.how.industry_Other 0.975 0.329676
## `wealth.how.industry_Private equity/leveraged buyout` 1.531 0.126036
## `wealth.how.industry_Real Estate` 0.622 0.533801
## `wealth.how.industry_Technology-Computer` 1.949 0.051423 .
## `wealth.how.industry_Technology-Medical` 1.638 0.101621
## `wealth.how.industry_Venture Capital` -0.138 0.890643
## `wealth.how.inherited_4th generation` 0.936 0.349253
## `wealth.how.inherited_5th generation or longer` -0.432 0.666085
## wealth.how.inherited_father 1.289 0.197441
## `wealth.how.inherited_not inherited` -0.156 0.876070
## `wealth.how.inherited_spouse/widow` -0.956 0.339342
## `wealth.type_founder non-finance` 2.891 0.003888 **
## wealth.type_inherited 0.544 0.586215
## `wealth.type_privatized and resources` 2.535 0.011337 *
## `wealth.type_self-made finance` 0.524 0.600648
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.482 on 1938 degrees of freedom
## Multiple R-squared: 0.09995, Adjusted R-squared: 0.07766
## F-statistic: 4.484 on 48 and 1938 DF, p-value: < 2.2e-16
```

### Pronalazak najboljih prediktora na sljedeći način: fittaj linearnu regresiju na svakom indikatoru p  
 ### sortaj najbolje regressore po p vrijednosti

```
n = 10
filtered_col_names = c()
r_squares = c()
ps = c()
col_names=colnames(x)

for(i in 1:ncol(x)){

  col_name=col_names[i]
  model=lm(wealth ~ x[[col_name]]) # create model with a single regressor and predict wealth
```

```
summary_model = summary(model)

filtered_col_names <- append(filtered_col_names, col_name)
r_squares <- append(r_squares, summary_model$r.squared)
# Density, distribution function, quantile function and random generation for the F distribution with
# a.k.a get P value from f statistics
f <- summary_model$fstatistic
ps <- append(ps, pf(f[1], f[2], f[3], lower.tail=FALSE))
}

df_g_squares=data.frame(filtered_col_names, r_squares, ps)
head(df_g_squares, n=3)
```

```
##          filtered_col_names    r_squares      ps
## 1          company.founded 8.130424e-05 0.687912207
## 2 company.relationship_chairman 4.348546e-03 0.003273294
## 3 company.relationship_director 6.218927e-04 0.266527863
```

```
df_g_squares
```

```
##          filtered_col_names    r_squares
## 1          company.founded 8.130424e-05
## 2    company.relationship_chairman 4.348546e-03
## 3    company.relationship_director 6.218927e-04
## 4    company.relationship_founder 4.031686e-03
## 5    company.relationship_investor 1.402451e-03
## 6    company.relationship_owner 1.185095e-02
## 7    company.relationship_president 7.693116e-08
## 8    company.type_aquired 1.467008e-05
## 9    company.type_new 6.958026e-05
## 10    company.type_privatization 1.516366e-03
## 11    company.type_subsidiary 2.083085e-03
## 12    demographics.age 1.264222e-02
## 13    demographics.gender_male 1.590454e-06
## 14    location.region_Europe 1.613209e-03
## 15    location.region_Latin America 4.530739e-03
## 16    location.region_Middle East/North Africa 9.431594e-04
## 17    location.region_North America 4.616901e-03
## 18    location.region_South Asia 2.264762e-03
## 19    location.region_Sub-Saharan Africa 5.982409e-04
## 20    wealth.how.category_Financial 6.676925e-06
## 21    wealth.how.category_New Sectors 8.110268e-04
## 22    wealth.how.category_Non-Traded Sectors 3.157021e-03
## 23    wealth.how.category_Resource Related 1.663292e-03
## 24    wealth.how.category_Traded Sectors 1.845987e-04
## 25    wealth.how.industry_Construction 1.398578e-03
## 26    wealth.how.industry_Consumer 5.383965e-04
## 27    wealth.how.industry_Diversified financial 8.589656e-05
## 28    wealth.how.industry_Energy 3.716918e-04
## 29    wealth.how.industry_Hedge funds 1.342533e-03
## 30    wealth.how.industry_Media 5.597208e-03
## 31    wealth.how.industry_Mining and metals 9.388670e-04
## 32    wealth.how.industry_Money Management 7.218781e-04
## 33    wealth.how.industry_Non-consumer industrial 4.916271e-04
```

```

## 34                                wealth.how.industry_Other 7.636769e-04
## 35 wealth.how.industry_Private equity/leveraged buyout 7.749904e-04
## 36                                wealth.how.industry_Real Estate 3.220077e-04
## 37                                wealth.how.industry_Technology-Computer 1.049251e-05
## 38                                wealth.how.industry_Technology-Medical 2.265278e-03
## 39                                wealth.how.industry_Venture Capital 9.310569e-04
## 40                                wealth.how.inherited_4th generation 2.140269e-03
## 41                                wealth.how.inherited_5th generation or longer 8.037852e-05
## 42                                wealth.how.inherited_father 1.881069e-02
## 43                                wealth.how.inherited_not inherited 2.357067e-02
## 44                                wealth.how.inherited_spouse/widow 8.820890e-06
## 45                                wealth.type_founder non-finance 1.890736e-05
## 46                                wealth.type_inherited 2.355548e-02
## 47                                wealth.type_privatized and resources 3.681178e-03
## 48                                wealth.type_self-made finance 6.974850e-03
##                                ps
## 1 6.879122e-01
## 2 3.273294e-03
## 3 2.665279e-01
## 4 4.633888e-03
## 5 9.514366e-02
## 6 1.150257e-06
## 7 9.901416e-01
## 8 8.645184e-01
## 9 7.101904e-01
## 10 8.267516e-02
## 11 4.192585e-02
## 12 5.040078e-07
## 13 9.551979e-01
## 14 7.345843e-02
## 15 2.682592e-03
## 16 1.711795e-01
## 17 2.442123e-03
## 18 3.390440e-02
## 19 2.758214e-01
## 20 9.083576e-01
## 21 2.044727e-01
## 22 1.224519e-02
## 23 6.913027e-02
## 24 5.449896e-01
## 25 9.560201e-02
## 26 3.012312e-01
## 27 6.796953e-01
## 28 3.903795e-01
## 29 1.025104e-01
## 30 8.453764e-04
## 31 1.721573e-01
## 32 2.312617e-01
## 33 3.232196e-01
## 34 2.182112e-01
## 35 2.148315e-01
## 36 4.240270e-01
## 37 8.852636e-01
## 38 3.388406e-02

```



```
## 39 1.739529e-01
## 40 3.920606e-02
## 41 6.896011e-01
## 42 8.312478e-10
## 43 5.980060e-12
## 44 8.947415e-01
## 45 8.464061e-01
## 46 6.074959e-12
## 47 6.823784e-03
## 48 1.938178e-04
```

```
# sort (by minimal r_squares) and find top n predictors
```

```
df_top_predictors = df_g_squares[order(-df_g_squares$r_squares), ]
```

```
top_n_predictors_one_var_lin = as.vector(df_top_predictors$filtered_col_names)[1:n]
df_top_predictors
```

```
##               filtered_col_names      r_squares
## 43      wealth.how.inherited_not inherited 2.357067e-02
## 46                wealth.type_inherited 2.355548e-02
## 42      wealth.how.inherited_father 1.881069e-02
## 12                demographics.age 1.264222e-02
## 6      company.relationship_owner 1.185095e-02
## 48      wealth.type_self-made finance 6.974850e-03
## 30                wealth.how.industry_Media 5.597208e-03
## 17      location.region_North America 4.616901e-03
## 15      location.region_Latin America 4.530739e-03
## 2      company.relationship_chairman 4.348546e-03
## 4      company.relationship_founder 4.031686e-03
## 47      wealth.type_privatized and resources 3.681178e-03
## 22      wealth.how.category_Non-Traded Sectors 3.157021e-03
## 38      wealth.how.industry_Technology-Medical 2.265278e-03
## 18                location.region_South Asia 2.264762e-03
## 40      wealth.how.inherited_4th generation 2.140269e-03
## 11                company.type_subsidary 2.083085e-03
## 23      wealth.how.category_Resource Related 1.663292e-03
## 14                location.region_Europe 1.613209e-03
## 10                company.type_privatization 1.516366e-03
## 5      company.relationship_investor 1.402451e-03
## 25      wealth.how.industry_Construction 1.398578e-03
## 29      wealth.how.industry_Hedge funds 1.342533e-03
## 16      location.region_Middle East/North Africa 9.431594e-04
## 31      wealth.how.industry_Mining and metals 9.388670e-04
## 39      wealth.how.industry_Venture Capital 9.310569e-04
## 21      wealth.how.category_New Sectors 8.110268e-04
## 35      wealth.how.industry_Private equity/leveraged buyout 7.749904e-04
## 34                wealth.how.industry_Other 7.636769e-04
## 32      wealth.how.industry_Money Management 7.218781e-04
## 3      company.relationship_director 6.218927e-04
## 19      location.region_Sub-Saharan Africa 5.982409e-04
## 26      wealth.how.industry_Consumer 5.383965e-04
## 33      wealth.how.industry_Non-consumer industrial 4.916271e-04
## 28                wealth.how.industry_Energy 3.716918e-04
## 36      wealth.how.industry_Real Estate 3.220077e-04
## 24      wealth.how.category_Traded Sectors 1.845987e-04
```

```

## 27          wealth.how.industry_Diversified financial 8.589656e-05
## 1              company.founded 8.130424e-05
## 41          wealth.how.inherited_5th generation or longer 8.037852e-05
## 9              company.type_new 6.958026e-05
## 45              wealth.type_founder non-finance 1.890736e-05
## 8              company.type_aquired 1.467008e-05
## 37          wealth.how.industry_Technology-Computer 1.049251e-05
## 44              wealth.how.inherited_spouse/widow 8.820890e-06
## 20              wealth.how.category_Financial 6.676925e-06
## 13              demographics.gender_male 1.590454e-06
## 7              company.relationship_president 7.693116e-08
##              ps
## 43 5.980060e-12
## 46 6.074959e-12
## 42 8.312478e-10
## 12 5.040078e-07
## 6  1.150257e-06
## 48 1.938178e-04
## 30 8.453764e-04
## 17 2.442123e-03
## 15 2.682592e-03
## 2  3.273294e-03
## 4  4.633888e-03
## 47 6.823784e-03
## 22 1.224519e-02
## 38 3.388406e-02
## 18 3.390440e-02
## 40 3.920606e-02
## 11 4.192585e-02
## 23 6.913027e-02
## 14 7.345843e-02
## 10 8.267516e-02
## 5  9.514366e-02
## 25 9.560201e-02
## 29 1.025104e-01
## 16 1.711795e-01
## 31 1.721573e-01
## 39 1.739529e-01
## 21 2.044727e-01
## 35 2.148315e-01
## 34 2.182112e-01
## 32 2.312617e-01
## 3  2.665279e-01
## 19 2.758214e-01
## 26 3.012312e-01
## 33 3.232196e-01
## 28 3.903795e-01
## 36 4.240270e-01
## 24 5.449896e-01
## 27 6.796953e-01
## 1  6.879122e-01
## 41 6.896011e-01
## 9  7.101904e-01
## 45 8.464061e-01

```

```
## 8 8.645184e-01
## 37 8.852636e-01
## 44 8.947415e-01
## 20 9.083576e-01
## 13 9.551979e-01
## 7 9.901416e-01

# pronalazak najboljih regressora s ANOVA-om
# nađi P vrijednosti za svaki regressor
# mergaj regressore od prošlog koraka i ukočni duplikate
# dobivene regresore koristi za model

a <- anova(model_all_vars)
ps_a <- a$`Pr(>F)`
ps_a <- head(ps_a, -1) # anova returns NA for last element

ps_a_ord <- order(ps_a)
sorted_cols <- colnames(x)[order(colnames(x))]
top_predictors_anova <- sorted_cols[ps_a_ord][1:n]
cat ("Best ANOVA regressors:")
```

```
## Best ANOVA regressors:
```

```
top_predictors_anova
```

```
## [1] "company.relationship_owner"
## [2] "demographics.age"
## [3] "company.relationship_founder"
## [4] "wealth.how.inherited_father"
## [5] "company.type_subsidiary"
## [6] "location.region_Latin America"
## [7] "company.relationship_chairman"
## [8] "wealth.type_privatized and resources"
## [9] "wealth.how.industry_Technology-Computer"
## [10] "wealth.type_founder non-finance"
```

```
top_predictors = c(top_predictors_anova, top_n_predictors_one_var_lin)
top_predictors <- top_predictors[!duplicated(top_predictors)]
cat ("\nTop predictors for a new model:")
```

```
##
```

```
## Top predictors for a new model:
```

```
top_predictors
```

```
## [1] "company.relationship_owner"
## [2] "demographics.age"
## [3] "company.relationship_founder"
## [4] "wealth.how.inherited_father"
## [5] "company.type_subsidiary"
## [6] "location.region_Latin America"
## [7] "company.relationship_chairman"
## [8] "wealth.type_privatized and resources"
## [9] "wealth.how.industry_Technology-Computer"
## [10] "wealth.type_founder non-finance"
## [11] "wealth.how.inherited_not inherited"
## [12] "wealth.type_inherited"
```

```
## [13] "wealth.type_self-made finance"
## [14] "wealth.how.industry_Media"
## [15] "location.region_North America"

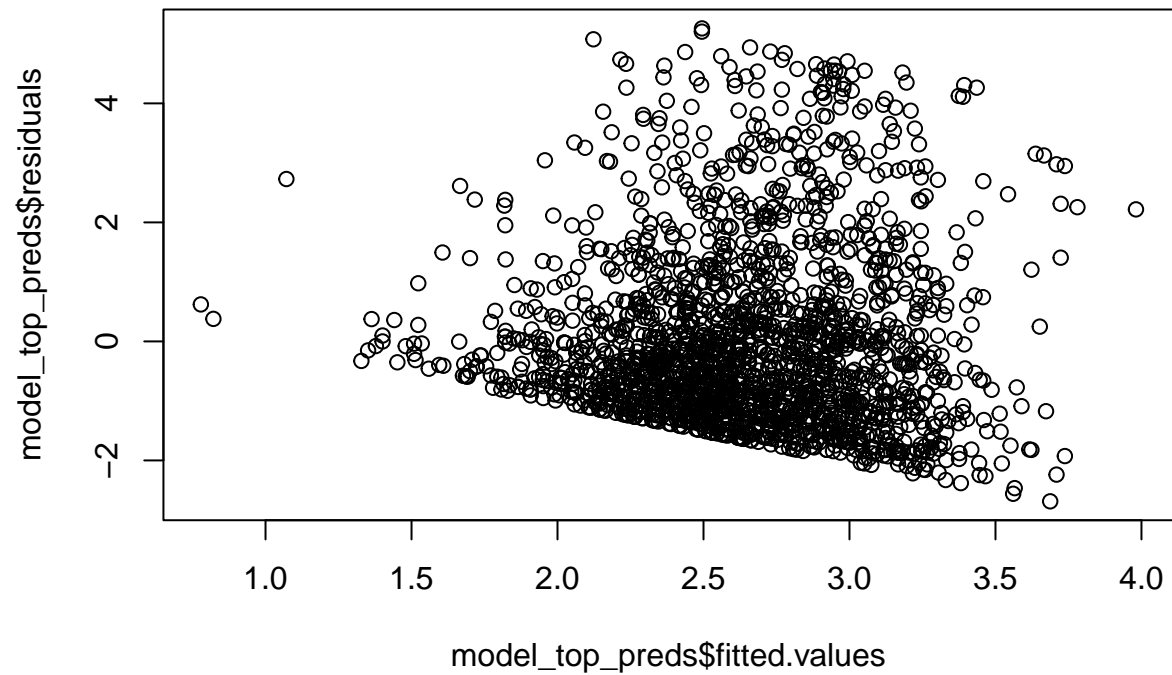
model_top_preds <- lm(wealth ~ . , x[, top_predictors])
summary(model_top_preds)

##
## Call:
## lm(formula = wealth ~ ., data = x[, top_predictors])
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.6874 -1.0582 -0.3905  0.6090  5.2597
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      1.64081    0.78452   2.091 0.036614
## company.relationship_owner -0.64196    0.20445  -3.140 0.001715
## demographics.age      1.23174    0.23070   5.339 1.04e-07
## company.relationship_founder -0.22710    0.15197  -1.494 0.135228
## wealth.how.inherited_father  0.20164    0.11973   1.684 0.092325
## company.type_subsidary    -1.21450    0.61620  -1.971 0.048869
## `location.region_Latin America` -0.49467    0.14103  -3.508 0.000462
## company.relationship_chairman -0.28553    0.18475  -1.545 0.122394
## `wealth.type_privatized and resources` 0.42688    0.18596   2.296 0.021806
## `wealth.how.industry_Technology-Computer` 0.23898    0.13633   1.753 0.079776
## `wealth.type_founder non-finance` 0.47939    0.18709   2.562 0.010469
## `wealth.how.inherited_not inherited` -0.09160    0.75409  -0.121 0.903330
## wealth.type_inherited  0.47903    0.76232   0.628 0.529825
## `wealth.type_self-made finance` 0.30609    0.17643   1.735 0.082906
## wealth.how.industry_Media  0.46363    0.12983   3.571 0.000364
## `location.region_North America` 0.07894    0.07254   1.088 0.276667
##
## (Intercept)          *
## company.relationship_owner **
## demographics.age      ***
## company.relationship_founder
## wealth.how.inherited_father .
## company.type_subsidary    *
## `location.region_Latin America` ***
## company.relationship_chairman
## `wealth.type_privatized and resources` *
## `wealth.how.industry_Technology-Computer` .
## `wealth.type_founder non-finance` *
## `wealth.how.inherited_not inherited`
## wealth.type_inherited
## `wealth.type_self-made finance` .
## wealth.how.industry_Media ***
## `location.region_North America`
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.495 on 1971 degrees of freedom
## Multiple R-squared:  0.06821,    Adjusted R-squared:  0.06112
```

```
## F-statistic: 9.619 on 15 and 1971 DF,  p-value: < 2.2e-16  
# micanjem nekih od ovih regresora se povećava Adjusted R-squared
```

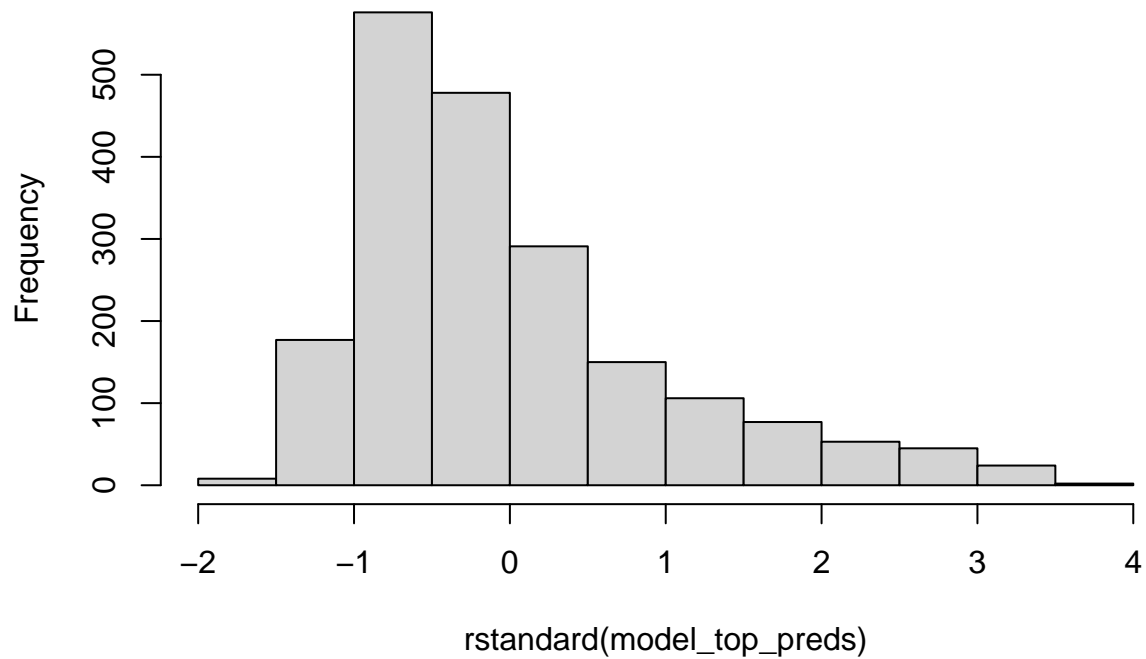
```
require(nortest)
```

```
# reziduali u ovisnosti o procjenama modela  
plot(model_top_preds$fitted.values, model_top_preds$residuals)
```



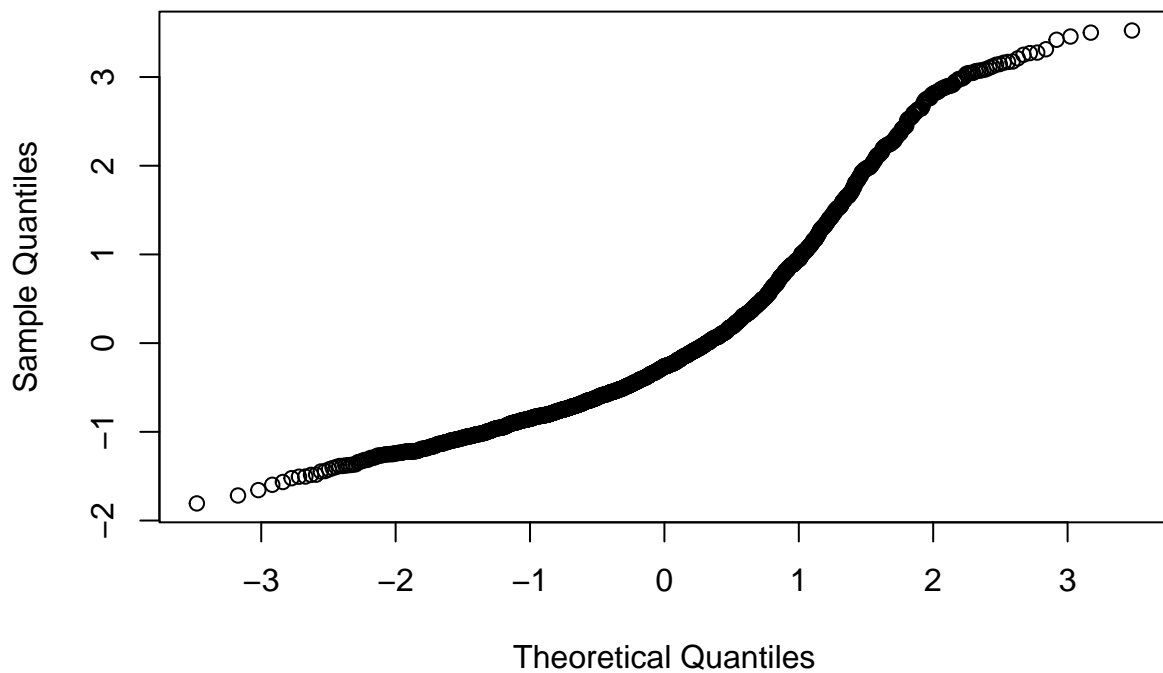
```
# provjera normalnosti reziduala  
hist(rstandard(model_top_preds))
```

**Histogram of rstandard(model\_top\_preds)**



```
qqnorm(rstandard(model_top_preds))
```

**Normal Q-Q Plot**



```
ks.test(rstandard(model_top_preds), 'pnorm')  
## Warning in ks.test(rstandard(model_top_preds), "pnorm"): ties should not be  
## present for the Kolmogorov-Smirnov test
```

```
##
## One-sample Kolmogorov-Smirnov test
##
## data: rstandard(model_top_preds)
## D = 0.12709, p-value < 2.2e-16
## alternative hypothesis: two-sided
lillie.test(rstandard(model_top_preds))
##
## Lilliefors (Kolmogorov-Smirnov) normality test
##
## data: rstandard(model_top_preds)
## D = 0.12731, p-value < 2.2e-16
```

#### 4. Kada biste birali karijeru isključivo prema kriteriju da se obogatite, koju biste industriju izabrali?

Pretpostavljamo da karijerom u određenoj industriji, a ne nasljedstvom zarađujemo novac. Zbog toga gledamo samo milijardere koji nisu naslijedili svoje bogatstvo. Također, zanimaju nas samo najnoviji milijarderi odnosno oni s popisa iz 2014. godine.

- kako prikazati trend kroz godine na grafu (dijagram paralelnih koordinata?)
- možda gledati razliku iz popisa 2014 i 2001, odnosno nove milijardere - pa napraviti raspodjelu industrija novonastalih milijardera

```
#
non_inherited_2014 <- non_inherited[non_inherited$year == 2014,]
non_inherited_2001 <- non_inherited[non_inherited$year == 2001,]
non_inherited_2014_new = bill_data[FALSE,]

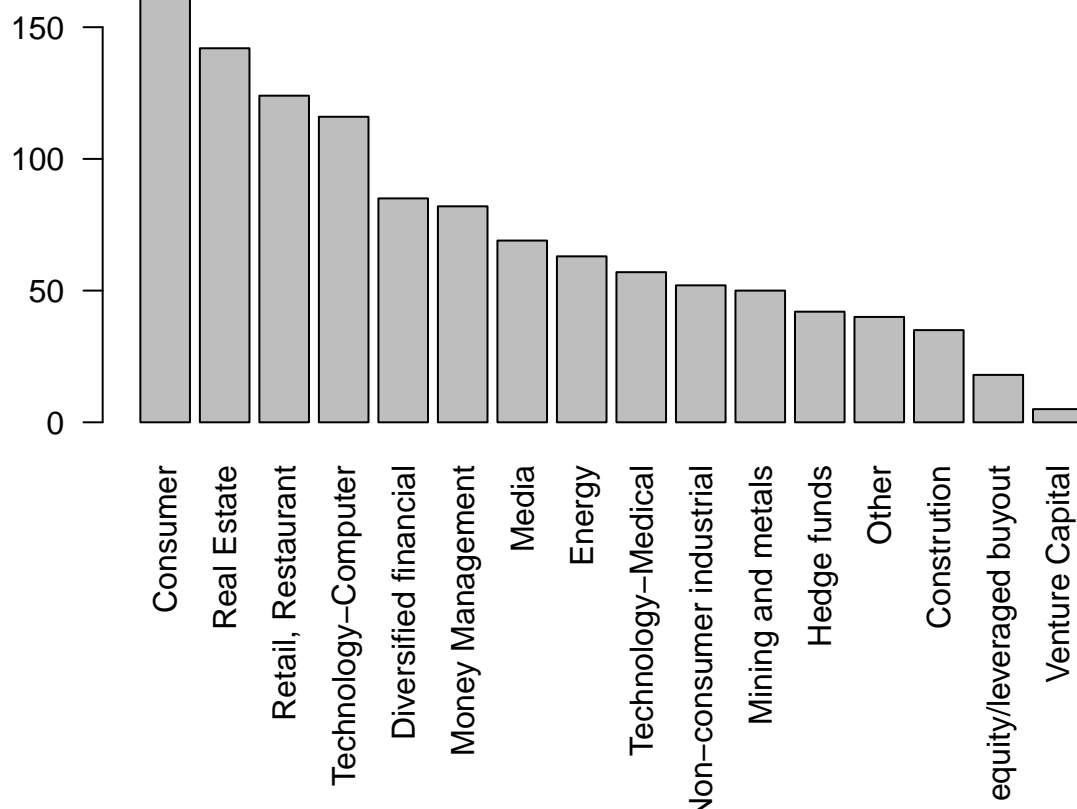
## tracemem[0x60000272e4c0 -> 0x60000272af40]: lapply tbl_subset_row [.tbl_df [ eval eval withVisible w
non_inherited_2001_old = bill_data[FALSE,]

## tracemem[0x60000272e4c0 -> 0x60000272b2c0]: lapply tbl_subset_row [.tbl_df [ eval eval withVisible w
# selekcija novonastalih milijardera iz 2014. koji nisu bili na prethodnoj listi iz 2001.
for(i in 1:nrow(non_inherited_2014)) {
  r <- non_inherited_2014[i,]
  if(sum(str_detect(non_inherited_2001$name, r[[1]])) == 0) {
    non_inherited_2014_new <- rbind(non_inherited_2014_new, non_inherited_2014[i,])
  }
}

# selekcija milijardera iz 2001. koji nisu na listi iz 2014.
for(i in 1:nrow(non_inherited_2001)) {
  r <- non_inherited_2001[i,]
  if(sum(str_detect(non_inherited_2014$name, r[[1]])) == 0) {
    non_inherited_2001_old <- rbind(non_inherited_2001_old, non_inherited_2001[i,])
  }
}

par(mar=c(10,5,1,1))
barplot(sort(table(subset(non_inherited_2014$wealth.how.industry, non_inherited_2014$wealth.how.industry
  main = "Billionaires distribution by industry in 2014 (non-inherited wealth)",
  las = 2)
```

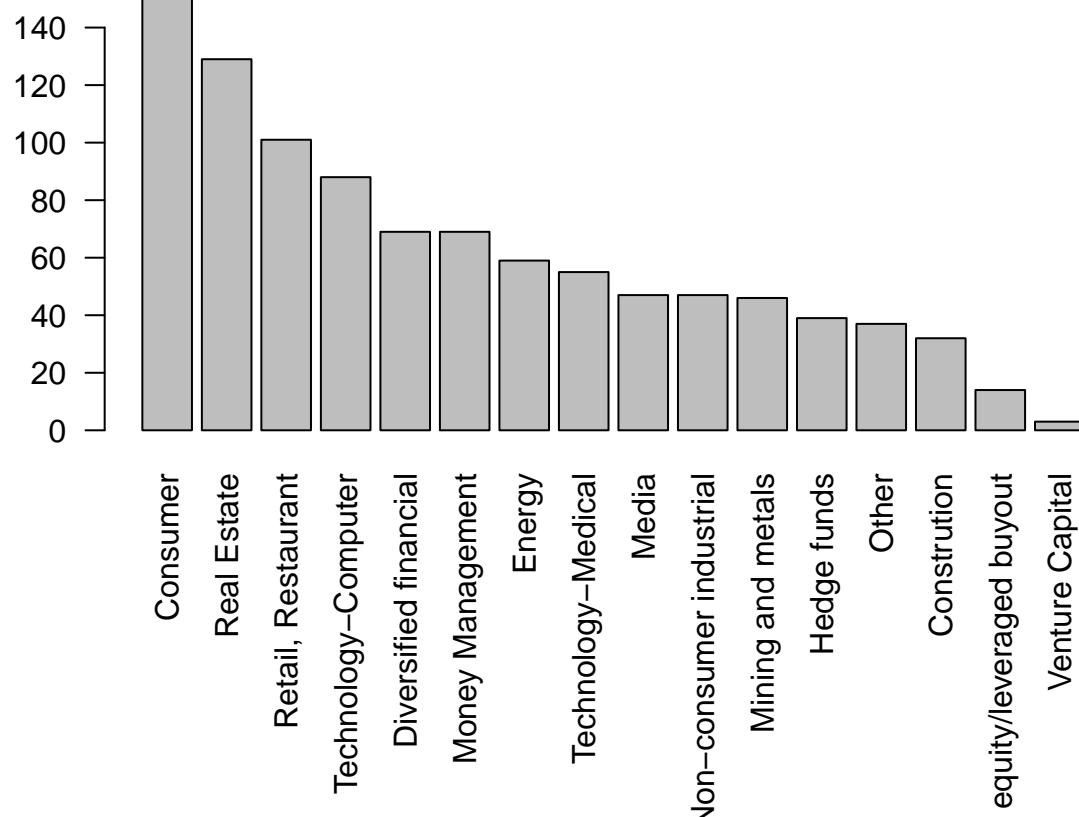
## Billionaires distribution by industry in 2014 (non-inherited wealth)



```
barplot(sort(table(subset(non_inherited_2014_new$wealth.how.industry, non_inherited_2014_new$wealth.how
  main = "Newcomer billionaires distribution by industry (non-inherited wealth)",
  las = 2)
```



## Newcomer billionaires distribution by industry (non-inherited wealth)



```
barplot(sort(table(subset(non_inherited_2001_old$wealth.how.industry, non_inherited_2001_old$wealth.how
  main = "Former billionaires distribution by industry (non-inherited wealth)",
  las = 2)
```

**Former billionaires distribution by industry (non-inherited wealth)**

