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$$\lim_{n \rightarrow +\infty} \frac{\ln(6n)}{\ln(2n)}$$

Option 1: Divide by $\ln(n)$

$$\lim_{n \rightarrow +\infty} \frac{\ln 6 + \ln n}{\ln 2 + \ln n} \cdot \frac{\frac{1}{\ln n}}{\frac{1}{\ln n}} = \lim_{n \rightarrow +\infty} \frac{\cancel{\frac{\ln 6}{\ln n}} + 1}{\cancel{\frac{\ln 2}{\ln n}} + 1} = \frac{1}{1} = 1$$

Option 2: L'Hopital's Rule

$$\lim_{n \rightarrow +\infty} \frac{\ln(6n)}{\ln(2n)} = \lim_{n \rightarrow +\infty} \frac{\frac{6}{6n}}{\frac{2}{2n}} = \lim_{n \rightarrow +\infty} \frac{\frac{1}{n}}{\frac{1}{n}} = 1$$

So the sequence converges to 1.