

10.1 #8

Circle of radius 5 centered at $(1, -2)$ is

$$(x-1)^2 + (y+2)^2 = 25$$

$$\text{or } \left(\frac{x-1}{5}\right)^2 + \left(\frac{y+2}{5}\right)^2 = 1$$

Since $\cos^2 t + \sin^2 t = 1$, we have

$$\frac{x-1}{5} = \cos t \Rightarrow x = 5\cos t + 1 \quad \text{and}$$

$$\frac{y+2}{5} = \sin t \Rightarrow y = 5\sin t - 2.$$

Check orientation: $t=0 \Rightarrow (x,y) = (6, -2)$
 $t = \frac{\pi}{2} \Rightarrow (x,y) = (1, 3)$ } Counterclockwise

[Note: To get a clockwise orientation we could replace t with $-t$.]

$$\text{So } \begin{cases} x = 5\cos t + 1 \\ y = 5\sin t - 2 \end{cases}$$

$$0 \leq t \leq 2\pi$$

↖ this gives us one revolution around the circle.