

#11

$$\sum_{k=0}^{\infty} \left[\left(\frac{2}{7} \right)^k (x+4)^{k+1} \right] = (x+4) + \left(\frac{2}{7} \right) (x+4)^2 + \left(\frac{2}{7} \right)^2 (x+4)^3 + \dots$$

is a geometric series with $r = \left(\frac{2}{7} \right) (x+4)$ and thus

converges only if

$$-1 < \frac{2}{7} (x+4) < 1$$

$$-\frac{7}{2} < x+4 < \frac{7}{2}$$

$$-\frac{15}{2} < x < -\frac{1}{2}$$

So the series has an interval of convergence of $\left(-\frac{15}{2}, -\frac{1}{2} \right)$

and a radius of convergence of $R = \frac{7}{2}$.