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$$a_n = n^3 e^{-n}$$

$$a'_n = n^3 (-e^{-n}) + e^{-n} (3n^2)$$

$$= n^2 e^{-n} (-n + 3)$$

$$= \underbrace{n^2 e^{-n}}_{>0} \underbrace{(3-n)}_{\geq 0 \text{ for } n=1,2,3}$$

$$< 0 \text{ for } n \geq 4$$

So  $a'_n < 0$  for  $n \geq 4$ , i.e. the sequence  
is eventually (strictly) decreasing.