

(17) Option 1:

$$A = \int_0^{\frac{\pi}{2}} \frac{1}{2} [(2+2\cos\theta)^2 - (2\cos\theta)^2] d\theta + \int_{\frac{\pi}{2}}^{\pi} \frac{1}{2} (2+2\cos\theta)^2 d\theta$$

Option 2:

$$A = \int_0^{\pi} \frac{1}{2} (2+2\cos\theta)^2 d\theta - \underbrace{\int_0^{\frac{\pi}{2}} \frac{1}{2} (2\cos\theta)^2 d\theta}_{\substack{\text{area of semicircle of radius 1} \\ = \frac{1}{2}\pi}}$$

We'll do option 2.

$$\begin{aligned} A &= \int_0^{\pi} \frac{1}{2} (4+8\cos\theta+4\cos^2\theta) d\theta - \frac{\pi}{2} = \int_0^{\pi} (2+4\cos\theta+2\cos^2\theta) d\theta - \frac{\pi}{2} \\ &= \int_0^{\pi} (2+4\cos\theta + 2(\frac{1}{2})(1+\cos 2\theta)) d\theta - \frac{\pi}{2} = \int_0^{\pi} (3+4\cos\theta+\cos 2\theta) d\theta - \frac{\pi}{2} \\ &= 3\theta \Big|_0^{\pi} + 4\sin\theta \Big|_0^{\pi} + \frac{1}{2}\sin 2\theta \Big|_0^{\pi} - \frac{\pi}{2} = 3\pi + 0 + 0 - \frac{\pi}{2} = \frac{5\pi}{2} \end{aligned}$$