

$$(28) \lim_{n \rightarrow +\infty} (\sqrt{n^2 + 8n - 5} - n)$$

$\infty - \infty$ is an indeterminate form

Multiply by the conjugate

$$\lim_{n \rightarrow +\infty} (\sqrt{n^2 + 8n - 5} - n) \cdot \frac{(\sqrt{n^2 + 8n - 5} + n)}{(\sqrt{n^2 + 8n - 5} + n)}$$

$$= \lim_{n \rightarrow +\infty} \frac{\cancel{n^2} + 8n - 5 - \cancel{n^2}}{\sqrt{n^2 + 8n - 5} + n} = \lim_{n \rightarrow +\infty} \frac{8n - 5}{\sqrt{n^2 + 8n - 5} + n}$$

Now divide by $\sqrt{n^2} = n$ (if $n > 0$)

$$= \lim_{n \rightarrow +\infty} \frac{8 - \cancel{\frac{5}{n}}}{\sqrt{1 + \cancel{\frac{8}{n}} - \cancel{\frac{5}{n^2}}} + 1} = \frac{8}{\sqrt{1+1}} = 4$$

So sequence converges to 4.