

12.1, 12.2 #7

(7) We want to find the value(s) of t so that $\vec{r}'(t)$ is a scalar multiple of $\langle 2, 8, 24 \rangle$.

$$\text{Now } \vec{r}'(t) = \langle 1, 2t, 3t^2 \rangle$$

$$\text{If } \langle 1, 2t, 3t^2 \rangle = k \langle 2, 8, 24 \rangle \text{ then } k = \frac{1}{2},$$

$$\text{so } 2t = \frac{1}{2}(8) = 4 \text{ and } 3t^2 = \frac{1}{2}(24) = 12.$$

$$\text{So } t = 2.$$

The point on the curve $\vec{r}(t) = \langle t, t^2, t^3 \rangle$
at $t = 2$ is $(2, 4, 8)$.