

#9

Specifically we show why the sequence in #7

$$\left\{ \frac{2n+1}{(2n)!} \right\}_{n=1}^{+\infty} \text{ converges to } 0.$$

$$\frac{2n+1}{(2n)!} = \frac{2n}{(2n)!} + \frac{1}{(2n)!}$$

$$\begin{aligned} \text{Note that } (2n)! &= (2n)(2n-1)(2n-2) \cdots 1 \\ &= (2n)(2n-1)! \end{aligned}$$

$$\text{So } \frac{2n+1}{(2n)!} = \frac{1}{(2n-1)!} + \frac{1}{(2n)!}$$

$$\text{So } \lim_{n \rightarrow +\infty} \frac{2n+1}{(2n)!} = \lim_{n \rightarrow +\infty} \left[\frac{1}{(2n-1)!} + \frac{1}{(2n)!} \right] = 0 + 0 = 0.$$