

12.1, 12.2 #8

$$(a) \quad \vec{r}_1(t) = \vec{r}_2(t) \implies \begin{aligned} t^2 &= 5t - 6 \\ 2t + 3 &= t^2 \\ t^2 &= 9 \end{aligned}$$

Only $t=3$ satisfies all three equations.

At $t=3$ the point on $\vec{r}_1(t)$ and $\vec{r}_2(t)$ is $(9, 9, 9)$.

(b) The angle θ between their paths is the angle between the tangent vectors at $t=3$.

$$\vec{r}_1'(t) = \langle 2t, 2, 2t \rangle \implies \vec{r}_1'(3) = \langle 6, 2, 6 \rangle$$

$$\vec{r}_2'(t) = \langle 5, 2t, 0 \rangle \implies \vec{r}_2'(3) = \langle 5, 6, 0 \rangle$$

$$\cos \theta = \frac{\langle 6, 2, 6 \rangle \cdot \langle 5, 6, 0 \rangle}{\sqrt{6^2 + 2^2 + 6^2} \sqrt{5^2 + 6^2 + 0^2}} = \frac{42}{\sqrt{76} \sqrt{61}}$$