

# Empirical Mechanism Design

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## Introduction

- Competitive Markets:
  - ▶ Price-taking behavior
  - ▶ Homogeneous goods & perfect information
  - ▶ Walrasian auctioneer
  - ✓ prices clear the market
  - ✓ first and second welfare theorems
- These conditions fail in real-world markets
- Study of market failures central in many fields in economics
  - ▶ Industrial organization: monopoly, collusion
  - ▶ Contract Theory: principal-agent with hidden types and actions
  - ▶ Labor: monopsony
  - ▶ Macro: price rigidity, agency problems
  - ▶ Market Design: congestion, auctions, matching, allocation mechanisms

## Market Design: How do markets really work?

- Abandon mythical Walrasian auctioneer
- Take market institutions seriously
  - ▶ congestion, coordination failures, other frictions
  - ▶ market failures: collusion, market power, imperfect information
  - ▶ rules, laws, political or institutional constraints
- What are participant's incentives?
- How does the market clear?
  - ▶ prices: price discovery in auctions [yesterday's lecture]
  - ▶ priority cutoffs: matching and school choice [today's lectures]
  - ▶ wait-time: queuing in organ allocation, public housing [tomorrow!]

# Market Design: Objectives

- Efficiency
  - ▶ ideal of Pareto optimality, c.f. first welfare theorem
- Fairness and distributional concerns
  - ▶ notions of fairness in the process or in the allocation
  - ▶ notions of equity achieved via redistribution, c.f. second welfare theorem
- Practicality and implementability
  - ▶ ideal of strategy-proofness
  - ▶ rules easy to codify and explain

# Market Design: Tools

- Theory: Game theory, computer science
  - ▶ Relevant equilibrium notions: stability
  - ▶ Properties: efficiency, fairness, strategy-proofness
  - ▶ identify tradeoffs: e.g. efficiency vs. equity
- Empirical Analysis: statistics, econometrics
  - ▶ Test hypothesis
  - ▶ Estimate economic primitives
  - ▶ Evaluate alternative designs
- Practice: interpersonal skills, networking
  - ▶ learn market institutions
  - ▶ propose and implement new designs

## Empirical Market Design

- Complementary to theory in evaluation of trade-offs
  - ▶ Testing theoretical predictions
  - ▶ Quantify tradeoffs
  - ▶ Analysis when theory is ambiguous
  - ▶ Document effect of designs, market failures
  - ▶ Evaluate alternative designs
- Organized marketplaces present a unique opportunity for analysis
  - ▶ Well-understood rules
  - ▶ Administrative data
- Empirical Approaches useful also in other areas of economics
  - ▶ Estimation of heterogeneous preferences and demand, e.g.,
    - ★ What do parents value in a school?
    - ★ What are the preferences of individuals for public housing?
  - ▶ Analysis of policy interventions, e.g.,
    - ★ Impact of financial aid reforms given admission mechanisms
    - ★ What are the effects of more generous public housing program?

## School Choice

- Education instrumental for economic progress and social mobility
- Public school systems aim for universal access
- Ideal of equal opportunity
  - ▶ efficiency
  - ▶ equity, fairness
- Economic inequities tilt the playing field
- Apply the market design tool-kit:
  - ▶ Theory: properties mechanisms for student allocation
  - ▶ Empirical analysis: preferences for school characteristics
  - ▶ Practice: implement new designs, inform students
- I will focus on the empirical tools

## Mechanisms in School Choice

- School districts rely on algorithms for student allocation
- Algorithms use student reports to generate allocation
- Schools have coarse priorities
- Many different algorithms implemented/studied (example):
  - ▶ Deferred acceptance (a.k.a Gale and Shapley alg)
  - ▶ Immediate acceptance (a.k.a Boston Mechanism)
  - ▶ Top-Trading Cycles
  - ▶ Serial Dictator
- Mechanisms have different properties



## Empirical Approaches - Summary

- Exploit properties of the mechanism to derive revealed preferences
- Use data on allocation for stable mechanisms
- Use data on reports for strategy-proof mechanisms
- Use data on reports + behavior for non-strategy proof mechanisms

# Challenges

- Demand estimation for schools, prestigious programs
  - ▶ Market does not clear on prices:  $D(p)$  is not the full picture
- Interpretation of data from mechanisms
- Find tractable statistical-econometric tools

## Preferences

- Students indexed by  $i$ , schools/programs indexed by  $j$

$$v_{ij} = v(\mathbf{x}_{ij}, \zeta_j, \varepsilon_{ij}) - d_{ij},$$

- ▶  $\mathbf{x}_{ij}$  observable characteristics
  - ▶  $\zeta_j$  school quality, unobserved to the econometrician but observed to students
  - ▶  $\varepsilon_{ij}$  i.i.d preference shock
  - ▶  $d_{ij}$  numeraire, e.g. distance, tuition
- Examples:
  - ▶ Simple linear model

$$v_{ij} = \overbrace{\mathbf{x}_{ij}\beta + \zeta_j}^{\delta_{ij}} - d_{ij} + \varepsilon_{ij}$$

- ▶ Random coefficient models: multiple preference shocks  $\varepsilon_{ij} = (\gamma_i, \omega_{ij})$

$$v_{ij} = \overbrace{\mathbf{x}_{ij}\beta + \zeta_j + \mathbf{x}_{ij}(\bar{\gamma}\mathbf{z}_i + \gamma_i)}^{\delta_{ij}} - d_{ij} + \omega_{ij}$$

# Outline

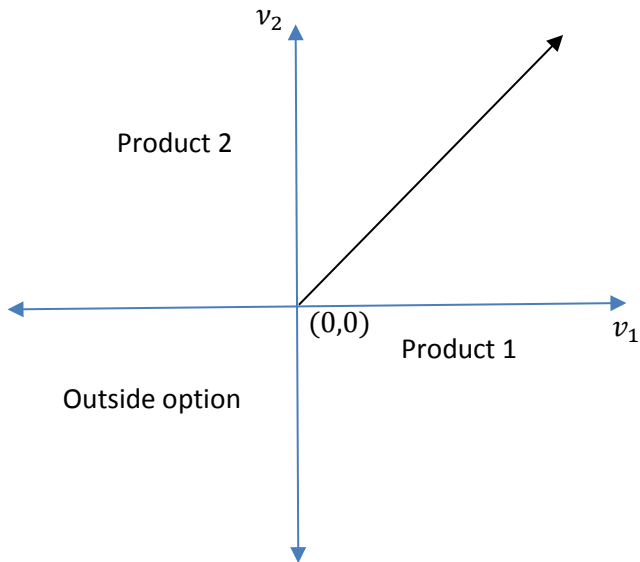
- 1 Introduction
- 2 Discrete Choice Models**
- 3 Stability
- 4 Truthful Reports
- 5 Strategic Reports
- 6 Conclusion

## Discrete Choice Models

$$v_{ij} = v(\mathbf{x}_{ij}, \zeta_j, \varepsilon_{ij}) - d_{ij},$$

- Consumer preferences for product
- Each consumer chooses the good with the maximum indirect utility
- The numeraire is usually price
- There are a variety of methods to estimate these models
- Rely on revealed preferences relations derived from observed choices

## Revealed Preferences – Discrete Choice



## Estimation Approaches – Discrete Choice

- Method of Moments (endogenous prices) [Berry 1994; Berry, Levinsohn and Pakes, 1995]
- Bayesian - Monte Carlo Markov Chain [Rossi, McCulloch and Allenby, 1996]
- Maximum Score [Manski, 1985]
- Moment Inequality [Ciliberto and Tamer, 2009; Pakes, 2010; Chernohukov, Hong and Tamer, 2007]
- Maximum Likelihood [McFadden, 1974; Train, 2004]
  - ▶ In the simple linear model, with extreme value shocks:  $\frac{\varepsilon_{ij}}{\sigma} \sim EV1$

$$v_{ij} = \overbrace{x_{ij}\beta + \zeta_j}^{\delta_{ij}} - d_{ij} + \varepsilon_{ij}$$

$$P(i \text{ chooses } j | x_{ij}; \beta) = \frac{\exp\left(\frac{1}{\sigma}(\delta_{ij} - d_{ij})\right)}{\sum_k \exp\left(\frac{1}{\sigma}(\delta_{ik} - d_{ik})\right)}$$

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## Back to School Choice

- Students cannot just pick the school that they want the most
- Prices do not clear the market
- An algorithm  $\mu = \Phi(\mathbf{R}, \mathbf{t}, \nu)$  determines the allocation given:
  - ▶ students reports:
    - ★  $R_i \in \mathcal{R}$  student  $i$ 's submitted rank-order list
    - ★  $R_{ik}$  is the school ranked in position  $k$
  - ▶ students priorities:
    - ★  $\mathbf{t}_i = (t_{i1}, \dots, t_{iJ})$  is student  $i$ 's priority,  $t_{ij}$  has finitely many values
    - ★ Tie-breaker:  $\nu_{ij}$

## Student Proposing Deferred Acceptance (DA)

- Step 1: Students apply to the first school in their list
- Step 2: Schools consider applicants and rank them according to priority. **Provisionally** hold applicants until exhausting capacity and definitively reject the rest
- Step 3: Students apply to the highest school that has not reject them
- Step 4: Schools consider new and previously held applicants and rank them according to priority. **Provisionally** hold applicants until exhausting capacity and definitively reject the rest
- Step 5 Repeat Steps 3-4 until each student (a) is tentatively held by some school; or (ii) has been rejected by all ranked schools

## Properties of DA

- Report-Specific Priority + Cutoff representation:

- ▶ Score:  $e_{ij} = f_j(R_i, t_i, v_{ij})$
- ▶ Cutoff  $p_j$  for school  $j$
- ▶ Each student is placed in the highest ranked school in

$$S(\mathbf{e}_i, \mathbf{p}) = \{j : e_{ij} > p_j\}$$

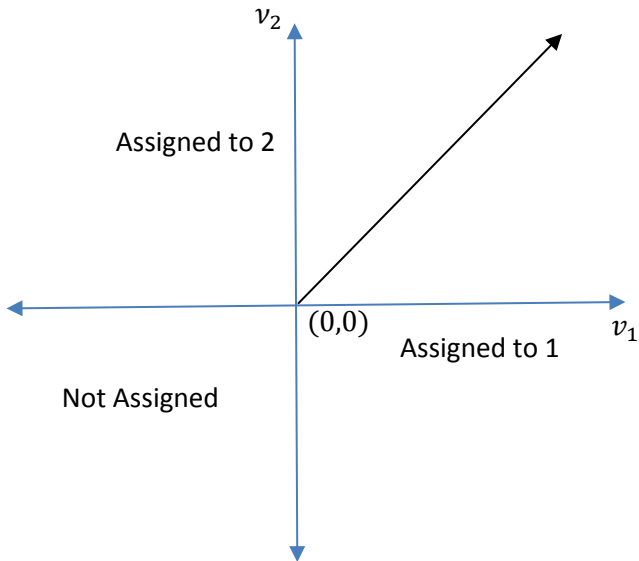
- ▶ DA: score does not depend on  $R_i$

- Deferred Acceptance has some desirable properties:

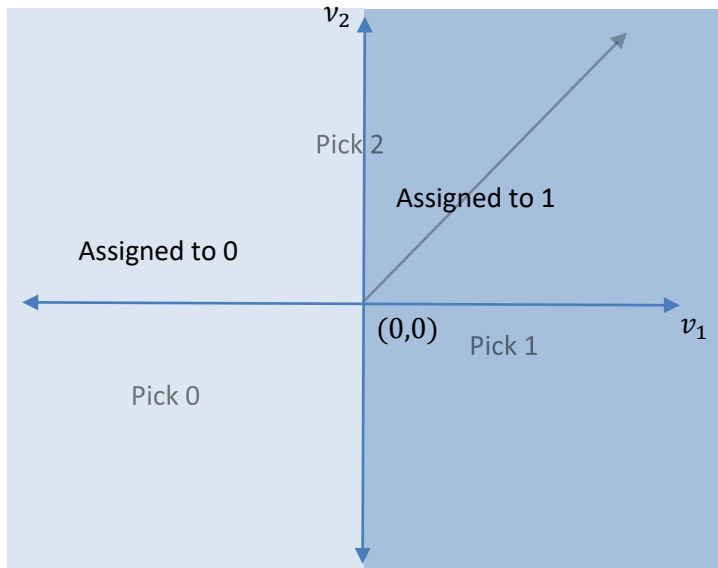
- ▶ strategy-proofness: incentives to report ordinal preferences truthfully
- ▶ stable allocation:  $i$  allocated to preferred school in  $S(\mathbf{e}_i, \mathbf{p})$

- Levels the playfield between sophisticates and naives

## Revealed Preferences – Stability – Full Choice Set



## Revealed Preferences – Stability – Restricted Choice Set



## Stability – Estimation Methods

- Logit models: build likelihood for  $\mathbb{P}(i \text{ is assigned to } j | \delta_i, d_i; \theta)$ :

$$\frac{\exp\left(\frac{1}{\sigma}(\delta_{ij} - d_{ij})\right)}{\sum_{k \in S(\mathbf{e}_i, \mathbf{p})} \exp\left(\frac{1}{\sigma}(\delta_{ik} - d_{ik})\right)}$$

- Random coefficients  $\gamma_i$ ,  $\mathbb{P}(i \text{ is assigned to } j | \mathbf{x}_j, \mathbf{z}_i; \theta)$  is:

$$\int \mathbb{P}(i \text{ is assigned to } j | \delta_i, d_i; \theta, \gamma) \phi(\gamma; \Sigma_\gamma) d\gamma.$$

- Akyol and Krishna (2017) for high-schools in Turkey
- Bucarey (2018) for colleges in Chile

## Bucarey (2018) Who pays for free college?

- In 2014 the Chilean government promised to make college free
- Low-income students already received financial aid
- Thus, low-income students' tuition was lower
- Hypothesis: If college is free for all students
  - ▶ high-income students will face same price as low-income students
  - ▶ Low-income students will be displaced from highly demanded majors
- Approach:
  - ▶ Data on student enrollment
  - ▶ DA generates a stable assignment
  - ▶ Estimate preferences
  - ▶ Simulate allocation with free-tuition
  - ▶ Who pays for free college?

# Bucarey (2018) Who pays for free college?

		Change in average:			
		Utility	Utility Net of Price	Sticker Tuition	Received Scholarship
<i>A. Common Price Coefficient Model</i>					
<b>Family Income</b>					
Poorest Quintile		-\$3,396	-\$1,180	-\$567	\$1,137
Second Quintile		-\$4,586	-\$1,454	-\$243	\$1,458
Third Quintile		-\$2,994	-\$1,109	-\$524	\$1,274
Fourth Quintile		-\$1,247	-\$776	\$630	\$2,736
Richest Quintile		-\$96	-\$490	\$1,460	\$3,484
<b>Test Scores</b>					
Lowest Quartile		-\$8,533	-\$2,485	-\$2,184	\$24
Top Quartile		\$1,955	\$178	\$3,328	\$4,515
<i>B. Income-heterogeneous Price Coefficient Model</i>					
<b>Family Income</b>					
Poorest Quintile		-\$6,530	-\$1,078	-\$506	\$1,271
Second Quintile		-\$3,684	-\$990	-\$323	\$1,379
Third Quintile		-\$1,461	-\$778	-\$25	\$1,629
Fourth Quintile		\$404	-\$572	\$675	\$3,070
Richest Quintile		\$1,486	-\$332	\$1,204	\$3,832
<b>Test Scores</b>					
Lowest Quartile		-\$10,980	-\$2,178	-\$2,160	\$34
Top Quartile		\$5,480	\$614	\$2,509	\$5,038

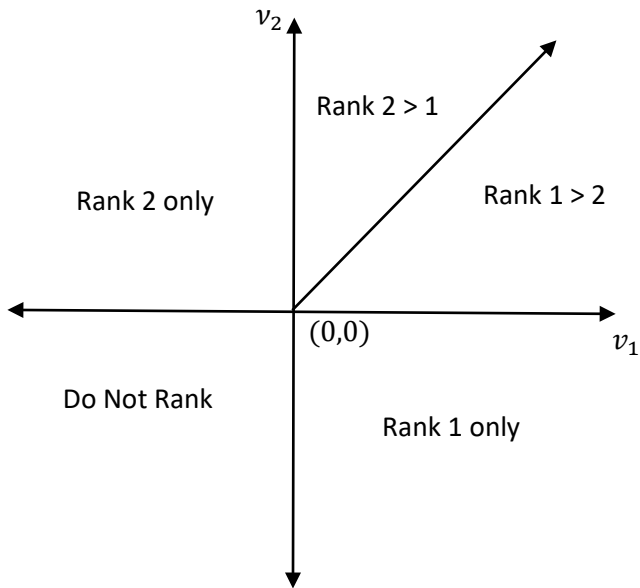
Notes: This table compares the average of the variable in each column for the free tuition case and the baseline. Utilities are expressed in dollar equivalent.



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## Revealed Preferences – Truthtelling



- In logit models, likelihood built on  $\mathbb{P}(i \text{ submits } R_i | \delta_i, d_i; \theta)$ :

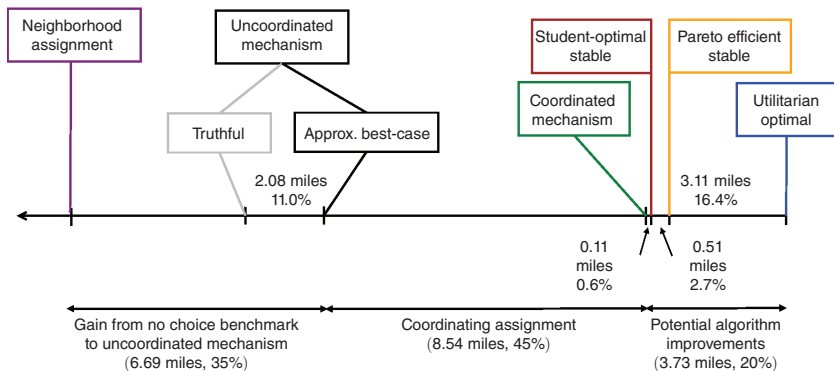
$$\prod_{k=1}^{K_i} \frac{\exp\left(\frac{1}{\sigma}(\delta_{R_{ik}} - d_{iR_{ik}})\right)}{\sum 1_{\{j \neq R_{ik'} \text{ for } k' < k\}} \exp\left(\frac{1}{\sigma}(\delta_j - d_{ij})\right)}$$

- Random coefficients  $\gamma_i$ ,  $\mathbb{P}(i \text{ submits } R_i | \delta_i, d_i; \theta)$  is:

$$\int \mathbb{P}(i \text{ submits } R_i | \delta_i, d_i; \theta, \gamma) \phi(\gamma; \Sigma_\gamma) d\gamma.$$

- Abdulkadiroglu, Agarwal and Pathak, 2017: NYC High School
- Ajayi and Sidibe, 2022: High Schools in Ghana

- Until 2003, students applied to 5 programs out of 600
- Many students were rejected and administratively placed
- In 2003 the district adopts DA
- What are the welfare effects of coordinated assignment?
- Approach:
  - ▶ Data on student reports to the DA mechanism
  - ▶ DA is strategy-proof: no gains from misreporting preferences
  - ▶ Estimate preferences assuming truthful reports
  - ▶ Simulate allocation under alternative allocation systems
    - ★ Neighborhood assignment
    - ★ Uncoordinated assignment
    - ★ Deferred Acceptance
  - ▶ Calculate aggregate welfare and distributional consequences



- Centralized (Coordinated) mechanisms perform better!

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## Manipulable Mechanisms

- Many school districts implemented manipulable centralized mechanisms
  - ▶ DA with restricted list length
  - ▶ Boston implemented the Immediate Acceptance mechanism (a.k.a Boston Mechanism)

## Restricted List DA

- The mechanism is manipulable
  - ▶ Students should rank schools according to their ordinal preferences
  - ▶ They should skip schools that are unattainable [Haeringer and Klijn 2009]
- Infer revealed preference relations from ranked schools
- How should we treat schools that are not ranked on the list?
  - ▶ Assume any ranked school is preferred to any non-ranked school?
  - ▶ Assume non-ranked schools are worse than the outside option?
  - ▶ Default back to using stability [Fack et al, 2019]?
- Alternatively, take the skipping strategy more seriously
  - ▶ Require analysis attainability of each school
  - ▶ Popular schools are harder to get
  - ▶ Not ranking a unpopular school implies dislike [Hwang, 2014]



## Immediate Acceptance (IA)

- Step 1: Students apply to the first school in their list
- Step 2: Schools consider applicants and rank them according to priority. **Immediately** admit applicants until exhausting capacity and reject the rest
- Step 3: Students apply to the highest school that has not reject them
- Step 4: Schools with spare capacity consider new applicants and rank them according to priority. **Immediately** admit applicants until exhausting capacity and reject the rest
- Step 5 Repeat Steps 3-4 until each student (a) has been accepted by some school; or (ii) has been rejected by all ranked schools

## Listening to parents

- ... if I understand the impact of Gale Shapley, and I've tried to study it and I've met with BPS staff... I understood that in fact the random number... [has] preference over your choices... [Recording from the BPS Public Hearing, 6-8-05]
- I'm troubled that you're considering a system that takes away the little power that parents have to prioritize... what you call this strategizing as if strategizing is a dirty word... [Recording from the BPS Public Hearing, 05-11-04].

## Were they right?

- Abdulkadiroglu, Che, Yasuda (2011):
  - ▶ Students have identical ordinal preferences
  - ▶ Schools have no priorities
  - ▶ IA Pareto dominates DA in ex ante welfare
  - ▶ IA may not harm but rather benefit those who do not strategize
  - ▶ IA facilitates access to good schools for students with no priority
- Preferences are important!

## Choice under uncertainty

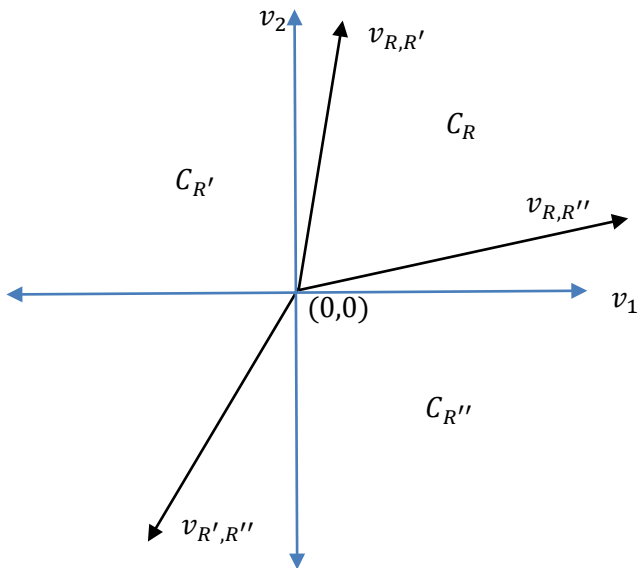
- Report  $R_i$  is associated with lottery  $L_{R_i}$
- Agents form beliefs about lotteries  $\hat{L}_{R_i}$  associated to each report
  - ▶ Rational expectations:  $\hat{L}_{R_i} = L_{R_i}$
  - ▶ Adaptive expectations  $\hat{L}_{R_i,t} = L_{R_i,t-1}$
  - ▶ Elicit beliefs through survey [Kapor, Nielsen and Zimmerman, 2018]

- Revealed Preferences:

$$\mathbf{v}_i \cdot \mathbf{L}_{R_i} \geq \mathbf{v}_i \cdot \mathbf{L}_R$$

- Thus,  $\mathbf{v}_i \in C_{R_i}$  where  $C_{R_i}$  is a cone  $\{\mathbf{v}_i \in \mathbb{R}^J : \mathbf{v}_i \cdot \Delta L_{R_i} \geq 0\}$

## Revealed Preferences – Strategic Behavior



## Strategic Behavior – Estimation Methods

- Arbitrary integration regions: Logit models lose their appeal
- Probit Models still do not provide close form solutions
- No easy way to compute the likelihood function
- Bayesian methods do not require computation of the likelihood function
  - ✓ Obtain the MLE without computing the likelihood function
    - ▶ Useful for discrete choice models [Rossi, McCulough, Allenby, 1995]
    - ▶ Can be adapted for choices over lotteries [Agarwal and Somaini, 2018]

## Bayesian Methods

- Frequentist approach:  $\log \mathcal{L}(\theta; data) := \log f(data; \theta)$ 
  - ▶  $\theta$  is a parameter
  - ▶  $\theta_{MLE} = \arg \max_{\theta} \mathcal{L}(\theta; data)$
  - ▶ Consistence and asymptotic normality of  $\theta_{MLE}$
- Bayesian Approach:  $f(\theta|data) = \frac{f(data|\theta)f(\theta)}{f(data)}$ 
  - ▶  $\theta$  is random vector
  - ▶  $f(\theta)$  is the prior [knowledge about  $\theta$ ]
  - ▶  $f(\theta|data)$  is the posterior
  - ▶  $f(data) = \int f(data|\theta) f(\theta) d\theta$
  - ▶ The posterior contains all the information we want!
  - ▶ Asymptotically Gaussian posterior irrespective of prior [Bernstein von-Mises Theorem]

# Markov Monte Carlo Chain (MCMC)

- Sampling from the posterior  $f(\theta|data)$ ?
- Sampling from conditional posteriors:
  - ▶ Suppose that  $\theta = (\theta_1, \theta_2)$
  - ▶ and  $f(\theta_1|\theta_2, data)$  and  $f(\theta_2|\theta_1, data)$  have closed-form solutions
- How to construct a MCMC?
  - ▶ pick some  $\theta_1^0$
  - ▶ sample  $\theta_2^k$  from  $f(\theta_2|\theta_1^k, data)$
  - ▶ sample  $\theta_1^{k+1}$  from  $f(\theta_1|\theta_2^k, data)$
- This algorithm is called Gibbs Sampler
  - ✓ There are other algorithms: e.g., Metropolis-Hastings, Hamiltonian Monte Carlo
- For  $k$  large enough  $\theta^k = (\theta_1^k, \theta_2^k) \sim f(\theta|data)$ 
  - ✓ Generalizes to  $\theta = (\theta_1, \theta_2, \dots, \theta_d)$



## Recall

$$v_{ij} = x_{ij} \beta_j - d_{ij} + \varepsilon_{ij}$$

where  $\varepsilon_{ij} \sim N(0, \Sigma)$ ,  $\beta \sim N(\underline{\beta}, \Sigma_\beta)$  and  $\Sigma \sim IW(u_0, S)$

• Data augmentation:  $v = \{v_{11}, v_{12}, \dots, v_{1J}, \dots, v_{ij}, \dots, v_{NJ}\}$

•  $\theta = (v, \Sigma, \beta)$

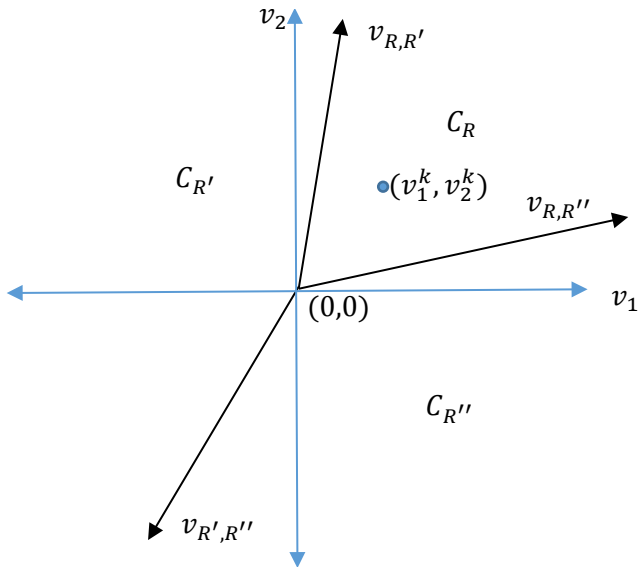
- ▶  $\beta | \Sigma, v$  has a Normal posterior
- ▶  $\Sigma | \beta, v$  has a Inverse Wishart posterior
- ▶  $v_{ij} | v_{i,-j}, \beta_j, \Sigma, C_j$  has a truncated normal posterior

• Initialize  $\Sigma_0$  and  $v^0$  so that  $v^0_i \in C_j$  for every student

• For every  $k$ :

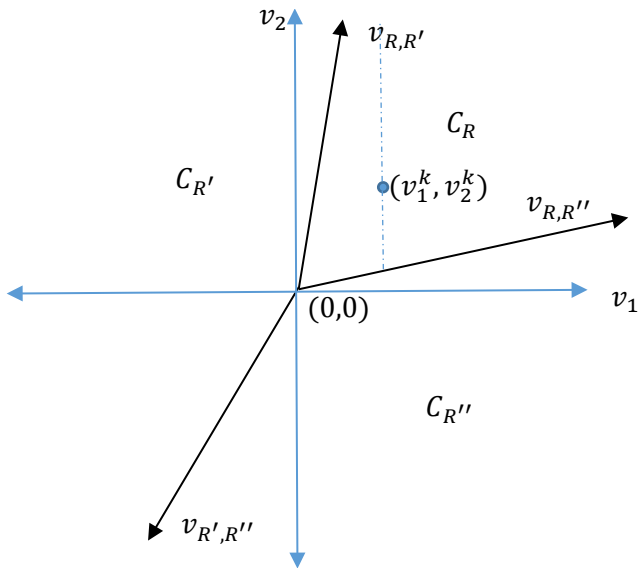
- ▶ Draw  $\beta^{k+1} | \Sigma_k, v^k$  from its normal posterior
- ▶ Draw  $\Sigma^{k+1} | \beta^{k+1}, v^k$  from its normal posterior
- ▶ “Bayesian regression” of  $v_{ij} + d_{ij}$  on  $x_{ij}$  ✓
- ▶ Update  $v^{k+1}$  given  $\beta^{k+1}, \Sigma^{k+1}$

Updating  $v^{k+1}$



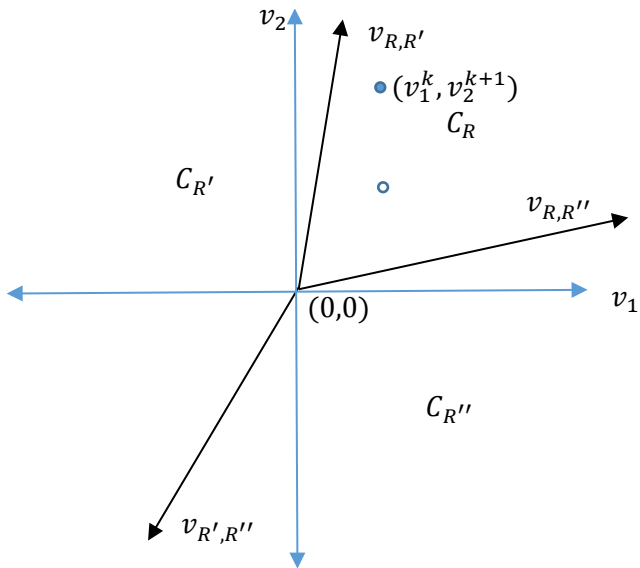
We start from the previous vector  $v^k$

Updating  $v^{k+1}$



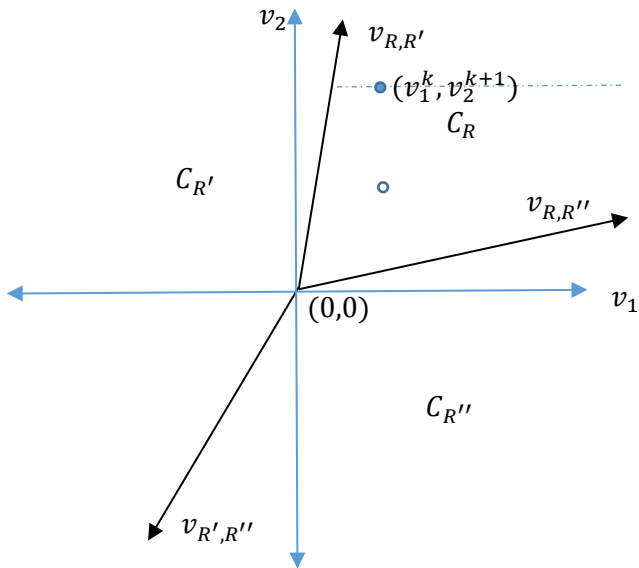
Draw  $v_2^{k+1}$  given  $v_1^k, \beta^{k+1}, \Sigma^{k+1}$  from a truncated normal

Updating  $v^{k+1}$



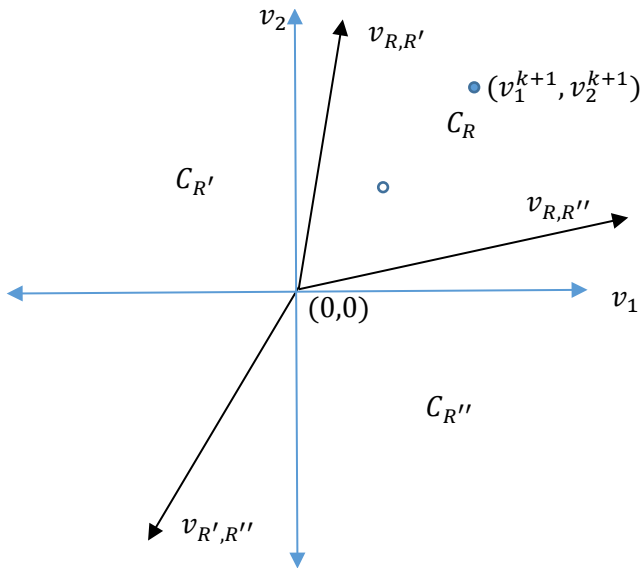
New draw of  $v_2^{k+1}$

Updating  $v^{k+1}$



Now, draw  $v_1^{k+1}$  given  $v_2^{k+1}, \beta^{k+1}, \Sigma^{k+1}$  from a truncated normal

Updating  $v^{k+1}$



Now, draw of  $v_1^{k+1}$ . We have  $v^{k+1}$ !

- Use data from the Immediate Acceptance algorithm used in Cambridge
- There are two sets of schools:
  - ▶ Competitive: they are very likely to clear in first round
  - ▶ Non-competitive: they are very likely to have spare capacity
- Incentives to pick the top rank carefully
- Provide evidence of strategic behavior
- Estimate preferences under alternative assumptions on beliefs
- Compare performance of DA vs IA

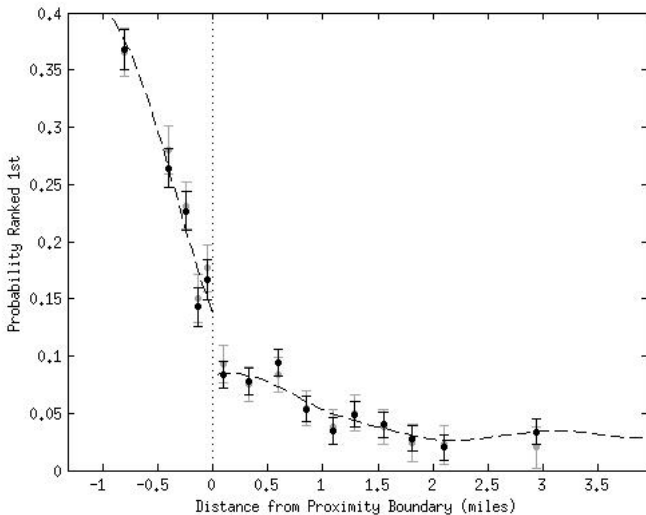
## Elementary Schools and Students

Year	2004	2005	2006	2007	2008	Average
<i>Panel A: District Characteristics</i>						
Schools	13	13	13	13	13	13
Programs	24	25	25	27	27	25.6
Seats	473	456	476	508	438	470
Students	412	432	397	457	431	426
Free/Reduced Lunch	32%	38%	37%	29%	32%	34%
Paid Lunch	68%	62%	63%	71%	68%	66%
<i>Panel B: Student's Ethnicity</i>						
White	47%	47%	45%	49%	49%	47%
Black	27%	22%	24%	22%	23%	24%
Asian	17%	18%	15%	13%	18%	16%
Hispanic	9%	11%	10%	9%	9%	10%
<i>Panel C: Language spoken at home</i>						
English	72%	73%	73%	78%	81%	76%
Spanish	3%	4%	4%	4%	3%	3%
Portuguese	0%	1%	1%	1%	1%	1%
<i>Panel D: Distances(miles)</i>						
Closest School	0.43	0.67	0.43	0.47	0.45	0.49
Average School	1.91	1.93	1.93	1.93	1.89	1.92



## Strategic Behavior

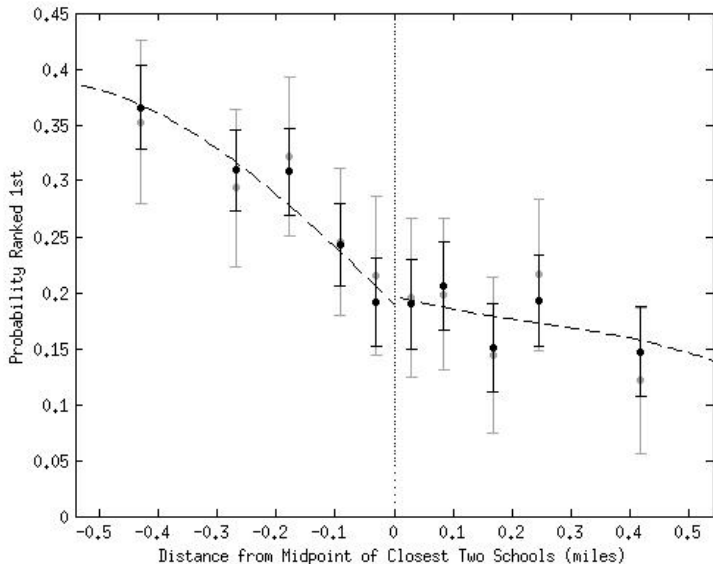
Top Rank: Proximity Boundary



✓ Difficult to explain entire response with residential sorting

## Strategic Behavior

### Placebo with Two Closest Schools



## Assignment Probabilities

- Individual faces two sources of uncertainty:
  - ▶ Own lottery draw  $v_i \sim U[0, 1]$
  - ▶ Market clearing cutoff  $p^*$  depend on all agents' actions and lotteries
- Estimate assignment probabilities by resampling  $R_{-i}, t_{-i}$ ,  $B$  times

$$\hat{L}_{R,t,j} = \frac{1}{B} \sum_{b=1}^B \int 1\{f_j(R, t, v) \geq p_j^b \text{ and } f_k(R, t, v) < p_k^b \text{ if } k \neq j\} dv$$

- ▶ **Idea:** Resampling approximation to beliefs about assignment probabilities

- ✓ Paper establishes consistency and asymptotic normality in a large market
  - ▶ Large number of students, fixed schools with increasing capacity
  - ▶ Target: Equilibrium of a limit game

## Deferred Acceptance vs. Cambridge Mechanism

	Truthful			Rational Expectations		
	All Students	Paid Lunch	Free Lunch	All Students	Paid Lunch	Free Lunch
<i>Panel A: Deferred Acceptance</i>						
Assigned to First Choice	67.7	58.2	86.6	67.9	58.1	87.5
Assigned to Second Choice	12.1	14.2	8.1	15.5	18.6	9.4
Assigned to Third Choice	5.7	8.2	0.8	5.2	7.1	1.3
<i>Panel B: Cambridge Mechanism</i>						
Assigned to First Choice	79.0	74.5	87.8	72.3	63.9	88.8
Assigned to Second Choice	6.5	6.8	6.0	14.7	18.1	7.9
Assigned to Third Choice	3.1	4.0	1.4	3.9	5.1	1.3
<i>Panel C: Deferred Acceptance vs Cambridge</i>						
Mean Utility DA - Cambridge	-0.004 (0.017)	-0.010 (0.025)	0.008 (0.006)	-0.072 (0.011)	-0.109 (0.015)	0.003 (0.013)
Std. Utility DA - Cambridge	0.230	0.280	0.047	0.171	0.142	0.197
Percent DA > Cambridge	26.8	26.0	28.3	16.5	14.2	21.1
Percent DA $\approx$ Cambridge	31.9	26.2	43.0	30.3	27.1	36.6
Percent DA < Cambridge	41.4	47.8	28.7	53.2	58.7	42.3
Percent with Justified Envy	9.93	12.69	4.46	5.6	5.1	6.4

✓ Approach evaluates assignments, ignoring potential costs of strategizing

## DA vs. Cambridge w/ Biased Beliefs

	Coarse Beliefs			Adaptive Expectations		
	All Students	Paid Lunch	Free Lunch	All Students	Paid Lunch	Free Lunch
<i>Panel A: Deferred Acceptance</i>						
Assigned to First Choice	69.7	61.0	87.1	68.4	56.9	89.1
Assigned to Second Choice	11.9	13.7	8.5	13.6	17.3	7.1
Assigned to Third Choice	4.9	6.7	1.2	5.1	7.3	1.1
<i>Panel B: Cambridge Mechanism</i>						
Assigned to First Choice	73.9	67.3	86.9	72.3	63.0	88.9
Assigned to Second Choice	10.2	11.1	8.3	12.1	15.3	6.4
Assigned to Third Choice	3.5	4.6	1.5	3.7	4.9	1.4
<i>Panel C: Deferred Acceptance vs Cambridge</i>						
Mean Utility DA - Cambridge	-0.045 (0.011)	-0.074 (0.013)	0.013 (0.016)	-0.049 (0.028)	-0.097 (0.035)	0.037 (0.040)
Std. Utility DA - Cambridge	0.174	0.146	0.207	0.213	0.142	0.282
Percent DA > Cambridge	22.6	21.3	25.1	19.1	16.5	23.9
Percent DA $\approx$ Cambridge	30.6	26.5	38.7	31.6	26.2	41.4
Percent DA < Cambridge	46.9	52.2	36.2	49.3	57.4	34.7
Percent with Justified Envy	7.1	7.8	5.6	6.7	8.0	4.4

✓ Advantage of the Cambridge mechanism are sensitive to agent information

# Outline

- 1 Introduction
- 2 Discrete Choice Models
- 3 Stability
- 4 Truthful Reports
- 5 Strategic Reports
- 6 Conclusion**

## Methods Recap

- Estimating preferences in school choice context
- General model of student's preferences
- Approach depends on the mechanism and the available data:
  - ▶ Data on final stable allocation
  - ▶ Data on truthful rank ordered lists
  - ▶ Data on strategic rank ordered lists

## Findings

- Free tuition may have regressive effects
- Big welfare effects of centralized mechanisms
- IA can increase our measure of welfare if students strategize correctly
- Difference between the mechanisms is smaller if beliefs are biased
- Similar results in Barcelona [Calsamiglia, Guell and Fu, 2018]
- Manipulable mechanism do badly if beliefs are wrong like in New Haven [Kapor, Nielsen and Zimmerman, 2018]



## Exciting avenues for research

- School choice and educational outcomes [Abdulkadiroglu, Angrist, Narita, Pathak 2017 & 2019, Abdulkadiroglu, Pathak, Schellenberg, and Walters, 2020]
- Effect of affirmative action policies [Otero, Barahona and Dobbin, 2022]
- Informing students about schools and programs [Allende, Gallego and Neilson, 2019]
- Augment with supply models: school entry and investment decisions