Dynamic College Admissions

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Outline

Introduction

Empirical facts

Model

Counterfactuals

Conclusions

▶ Higher Education is both a valuable and scarce resource

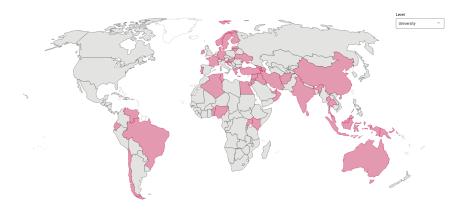
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 - Many students switch their majors or colleges and many dropout
- Several countries organize their college admissions via centralized assignment mechanisms

Figure 1: Centralized Systems in College Admissions



Source: Neilson, 2022

Research Question

Can centralized assignment mechanisms affect students' outcomes, such as their decisions to dropout and switch majors or colleges?

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 - Excess demand + colleges care about retention → crowd-out externality
 - Ex-ante inefficient to assign students to lower-ranked programs



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 - ▶ Reducing incentives to switch ↑ ex-post mismatches

Learning Mismatching

Model

Data

Learning

Mismatching

Model

 Signals about match-quality through college grades

Data

Correlation between college grades and students' outcomes

Learning

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Mismatching

- Idiosyncratic preferences for majors/colleges are persistent
- Common prior
- Correlation patterns within initial preferences
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- Results
 - Learning: 45% of switchings
 - Signaling mechanism: switchings ↓ 33%, retention rates ↑ 8%, and welfare ↑ equivalent of a 19% reduction in average tuition

Empirical analysis on centralized assignment mechanisms:
 Fack et al. (2015), Abdulkadiroğlu et al. (2017), He (2012), He (2012), Agarwal and Somaini (2018), Calsamglia et al. (2018), Kapor et al. (2017), Kapor et al. (2020), Larroucau and Ríos (2018), Luflade (2017), Ajayi and Sidibe (2017), Waldinger (2021), Agarwal et al. (2020), Narita (2018), Carvalho et al. (2019), Magnac and He (2019), among others.

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Semi-centralized market:

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Data:

- Surveys: top-true preferences and subjective beliefs
- Admission process + Enrollment + College grades + Avg. wages



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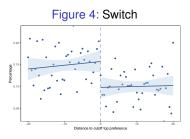
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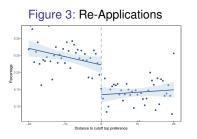
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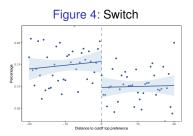
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Figure 3: Re-Applications



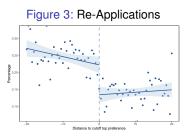
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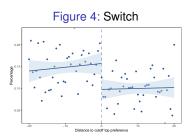




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- ▶ Between 25%-50% move up in their initial preferences

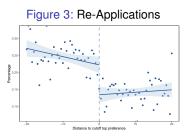
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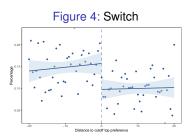




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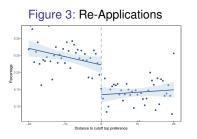
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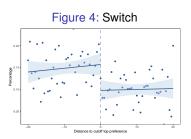


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- Students assigned to lower-ranked programs face lower retention rates (Switching stats)
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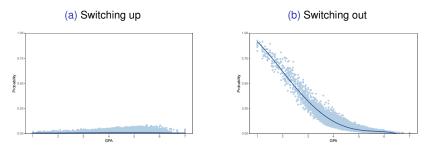
Forward-looking



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Learning: grades and outcomes

- Surveys: 60% of re-applicants change top-true preference
- Correlation patterns between grades and outcomes:



- Switching up is uncorrelated with grades
- Switching out is negatively correlated with grades



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Stage 1: students receive their scores and preference shocks

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- (iii) Update beliefs about match-qualities → abilities (Stage 1 repeats)

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Stage 3: after period two:

- (i) Face a sequence of dropout and graduation probabilities
- (ii) Students who graduate enter the labor force



Students are characterized by:

- ► Known major and college preferences α_{im_j} and α_{ik_j}
- ▶ Known subject-specific ability $A_i = (A_{is_m}, A_{is_v})$
- ▶ Unknown subject-specific ability , $A_i^u = (A_{is_m}^u, A_{is_v}^u)$, and major-specific ability $A_{im_j}^u$

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Ability in program *j* is given by:

$$A^u_{ij} = A^u_{im_j} + \sum_{l \in \{s_m, s_v\}} \underbrace{\omega_{jl}}_{ ext{admission weights}} A^u_{il}, \quad A_{ij} = \sum_{l \in \{s_m, s_v\}} \omega_{jl} A_i$$

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- Comparative and absolute advantages in abilities
- Correlated learning

Assumption (Bayesian Updating)

Students have rational expectations over the population distribution of unknown abilities for program *j*, and

$$A_{il}^u \sim N(0, \sigma_s^2) \quad \forall i, l \in \{s_m, s_v\}, \quad A_{im_j}^u \sim N(0, \sigma_m^2)$$

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Learning

Students learn about A_i^u from their college GPA:

$$G_{ijt} = f\left(m_j, A_{ij}, Z_i^g, \alpha_{im_j}, \alpha_{ik_j}, A_{ij}^u, \varepsilon_{ij}^g\right),$$

where $\varepsilon_{\it ijt}^{\it g}$ is a white noise, distributed $\it N(0,\sigma_g^2)$



Flow utility

$$u_{\mathit{ijt}} = lpha_{\mathit{fe}_{\mathit{j}}} + \underbrace{lpha_{\mathit{im}_{\mathit{j}}} + lpha_{\mathit{ik}_{\mathit{j}}}}_{\mathit{unobserved heterogeneity}} + Z^{\mathit{u}}_{\mathit{ij}} lpha - C_{\mathit{ijt}} + arepsilon_{\mathit{ijt}},$$

with

$$Z_{ij}^{u} \alpha = \alpha_1 A_{ij} + \alpha_2 \underbrace{\bar{A}_j}_{\text{program quality}} + \alpha_3 D_{ij} + \alpha_4 \underbrace{\frac{(A_{ij} - A_j)}{\bar{\sigma}_j}}_{\text{Relative position}}$$

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 $ightharpoonup arepsilon_{ijt} \sim \mathsf{T1EV}(1) \text{ and } u_{i0t} = 0$

Mixture

- (i) Weak truth-tellers (ρ): report true preferences
- (ii) Strategic (1 ρ): $R_{it} \in \operatorname{argmax}_{R' \in \mathcal{R}, |R'| < K} U(R')$

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Assumptions

- Rational Expectations over cutoffs' distributions + independence
- 2. Do not apply to programs unless it is strictly profitable to do so

$$U(R_{it}) = p_{iR(1)t} \cdot v_{iR(1)t} + (1 - p_{iR(1)t}) \cdot p_{iR(2)t} \cdot v_{iR(2)t} + \ldots + \prod_{l=1}^{k-1} (1 - p_{iR(l)t}) \cdot p_{iR(K)t} \cdot v_{iR(K)t}.$$

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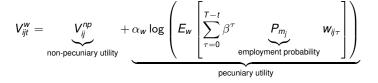
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3. Enroll in their assigned program with an exogenous probability

$$v_{ikt} = P_{it}^e \cdot V_{ikt} + \left(1 - P_{it}^e\right) \cdot \max\{V_{i0t}, V_{ijt}\}$$

Utility in the workforce



Utility in the workforce

$$V_{ijt}^{\textit{w}} = \underbrace{V_{ij}^{\textit{np}}}_{\textit{non-pecuniary utility}} + \underbrace{\alpha_{\textit{w}} \log \left(E_{\textit{w}} \left[\sum_{\tau=0}^{T-t} \beta^{\tau} \underbrace{P_{\textit{m}_{j}}}_{\textit{employment probability}} W_{ij\tau} \right] \right)}_{\textit{pecuniary utility}}$$

where

$$\log(w_{ijt}|\tau) = f\left(m_j, \bar{A}_{k_j}, \underbrace{G_{ij}\left(A_{ij}, A^u_{ij}\right)}_{\text{grades}}, Z^w_i, \underbrace{\Lambda_{m_j\tau}, \epsilon^w_{ijt}}_{\text{tenure}}\right)$$

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 $ightharpoonup V_0(X_{i0},t)$ is the value function of dropping out

Estimation

Two-Step Procedure

Step 1: estimate beliefs on admission, future dropout, enrollment, graduation, and employment probabilities from the data.

Step 2: estimate the model parameters via Indirect Inference (II), taking students' beliefs as given.

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Table 4: Estimation Results - Parameters

Parameters	Values	Std
Share of strategic ROLs	0.74	[0.022]
Variance idiosyncratic preferences by major Major prior variance Subject prior variance Grade shock variance	15.69 0.34 0.48 0.08	[0.913] [0.032] [0.103] [0.04]

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Table 4: Estimation Results - Parameters

Parameters	Values	Std
Share of strategic ROLs	0.74	[0.022]
Variance idiosyncratic preferences by major Major prior variance Subject prior variance Grade shock variance	15.69 0.34 0.48 0.08	[0.913] [0.032] [0.103] [0.04]

► Learning: 45% of switchings

Outline

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Conclusions

Counterfactuals

Assignment mechanism

1. Constrained Deferred Acceptance with constraint K

Assignment mechanism

- 1. Constrained Deferred Acceptance with constraint K
 - Opportunity cost of including programs in the list

Assignment mechanism

- 1. Constrained Deferred Acceptance with constraint K
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- 2. Deferred Acceptance with signal and score bonus φ

Assignment mechanism

- 1. Constrained Deferred Acceptance with constraint K
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 - Opportunity cost of signaling a unique program in the list

Assignment mechanism

- 1. Constrained Deferred Acceptance with constraint *K*
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Re-application rules

1. Switching score penalty ψ (Turkey)

Assignment mechanism

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- 1. Switching score penalty ψ (Turkey)
 - Decreases the continuation value of switchings

Assignment mechanism

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- 1. Switching score penalty ψ (Turkey)
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- 1. Switching score penalty ψ (Turkey)
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Assignment mechanism

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Re-application rules

- 1. Switching score penalty ψ (Turkey)
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Challenges

- ► How would beliefs change? → equilibrium
- ► How will naive students behave? → bounds

Assignment mechanisms



Assignment mechanisms

		Co	nstrained	DA	CADA
Outcome	Baseline	K = 3	K = 2	K = 1	
Reapplicants [%]	34.27	0.35	1.62	10.01	
Program switchings [%]	6.48	-0.40	0.66	20.74	
Retakes PSU [%]	21.62	0.44	3.05	16.34	
Dropouts - first year [%]	3.70	-0.54	-1.48	-11.76	
Applicants in first period [%]	62.24	0.06	0.33	1.23	
Enrolls same program [%]	31.64	-0.13	-0.98	-12.14	
Assigned to top true preference [%]	10.46	0.76	2.38	-9.59	
Unassigned in first period [%]	44.17	0.33	1.09	9.69	
Difference in Ex Post Welfare Rela	tive to Bas	eline (in	millions	of Chilean	pesos)
Overall	-	0.01	-0.08	-1.95	

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Assignment mechanisms

		Constrained DA		CADA	
Outcome	Baseline		$\varphi = 10\%$	$\varphi =$ 20%	$\varphi = 30\%$
Reapplicants [%]	34.27		-11.80	-20.92	-26.32
Program switchings [%]	6.48		-22.28	-32.84	-39.10
Retakes PSU [%]	21.62		-23.30	-34.70	-40.48
Dropouts - first year [%]	3.70		11.61	16.88	20.41
Applicants in first period [%]	62.24		1.04	1.73	2.24
Enrolls same program [%]	31.64		7.20	10.61	12.95
Assigned to top true preference [%]	10.46		16.20	22.60	23.84
Unassigned in first period [%]	44.17		-4.26	-6.30	-7.79
Difference in Ex Post Welfare Rela	tive to Basel	ine (in millions of Chile	ean pesos)		
Overall	-	•	0.62	0.77	0.78

- Constrained DA: ~ top-true, ↑ switchings, ↑ unassigned, ↓ welfare
- Signaling (CADA): ↑ top-true, ↓ switchings, ↑ retention, ↑ welfare

Assignment mechanisms

		Constrained DA		CADA	
Outcome	Baseline		$\varphi = 10\%$	$\varphi =$ 20%	$\varphi = 30\%$
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		٦	Turkish Rules		Finnish Rules
Outcome	Baseline	$\psi=$ 10%	$\psi=$ 20%	$\psi = 30\%$	
Reapplicants [%]	34.27	-16.81	-29.63	-36.41	
Program switchings [%]	6.48	-33.16	-51.53	-63.34	
Retakes PSU [%]	21.62	-18.18	-27.79	-32.95	
Dropouts - first year [%]	3.70	4.22	5.70	6.92	
First enrollment in second period [%]	13.01	4.46	6.38	7.04	
Enrolls same program [%]	31.64	5.90	9.07	11.17	
Assigned to top true preference [%]	10.46	13.39	19.80	21.95	
Unassigned in first period [%]	44.17	0.27	0.59	0.72	
Difference in Ex-Post Welfare Relati	ive to Base	line (in mil	lions of Ch	ilean pesos)	
Overall	-	0.45	0.65	0.68	

Re-application rules

		٦	s	Finnish Rules	
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Retakes PSU [%]	21.62		-17.23	-24.34	-25.04
Dropouts - first year [%]	3.70		0.82	-0.53	-2.29
First enrollment in second period [%]	13.01		5.57	8.84	12.18
Enrolls same program [%]	31.64		4.39	5.40	5.46
Assigned to top true preference [%]	10.46		19.51	28.26	29.62
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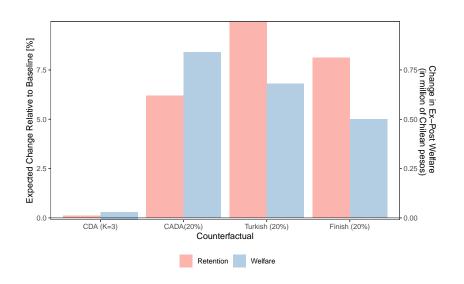
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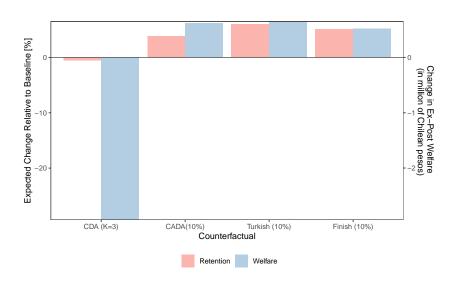
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All students behave strategically



26% of students behave as truth-tellers



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Take-Aways

(i) Analyzed the trade-offs of designing matching markets

Take-Aways

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 - Private information about their preferences

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- (i) Analyzed the trade-offs of designing matching markets
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 - Learn over time about their match-qualities

Take-Aways

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 - Leveraging dynamic incentives or incorporating signals

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 - Face dynamic considerations
 - Balancing learning and initial mismatches
- (ii) Centralized systems can improve students' outcomes
 - Eliciting intensity on students' preferences
 - Leveraging dynamic incentives or incorporating signals
 - Lack of sophistication reduces efficiency and welfare gains

Take-Aways

- (i) Analyzed the trade-offs of designing matching markets
 - Private information about their preferences
 - Learn over time about their match-qualities
 - Face dynamic considerations
 - Balancing learning and initial mismatches
- (ii) Centralized systems can improve students' outcomes
 - Eliciting intensity on students' preferences
 - Leveraging dynamic incentives or incorporating signals
 - Lack of sophistication reduces efficiency and welfare gains

Ongoing Research

Information policies: helping students to submit optimal applications

Thank you!

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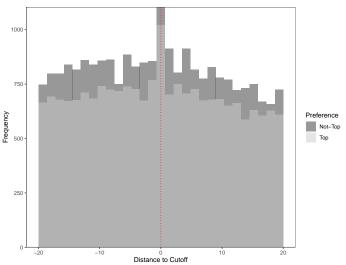
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choice systems.

Preference of assignment

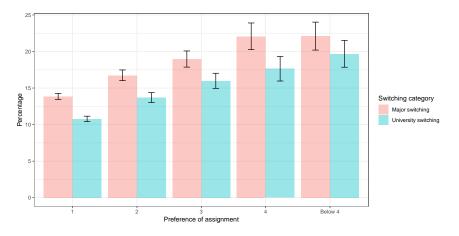
Figure 10: Distribution of preference of assignment





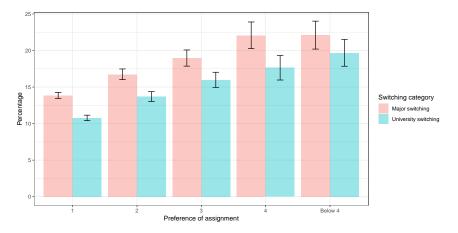
Mismatching

Switchings stats



Mismatching

Switchings stats



 Students assigned to lower preferences face higher switching probabilities



Switchings

Figure 11: Switching statistics 25 20 Switching category Percentage 91 Dropout Stopout Major switching University switching Program switching Below 4 Preference of assignment

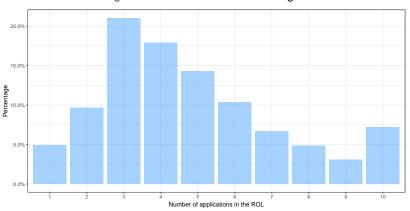
RDD

Figure 12: Timeline of the Centralized Process



Applications

Figure 13: Distribution of ROLs length

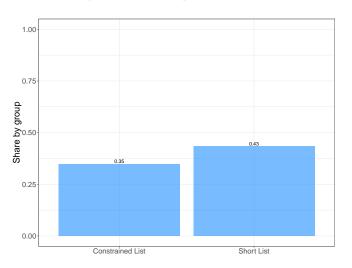


Chilean system

Misreporting preferences

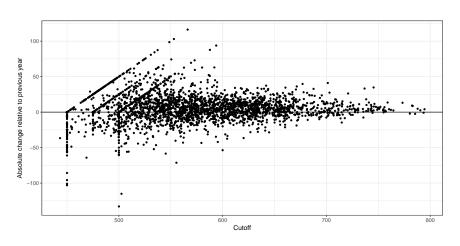
Survey - Admission Process 2019

Figure 14: Percentage of truth-tellers



Uncertainty

Figure 15: Variation in cutoffs - from 2013 to 2014

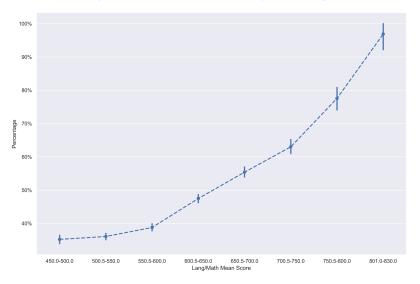


Subjective beliefs

Evidence

Survey - Admission Process 2019

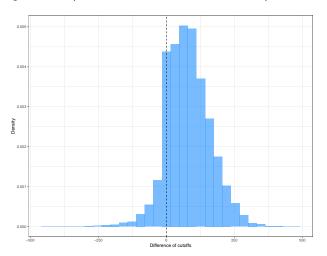
Figure 16: Share of truth-tellers by score range



Evidence

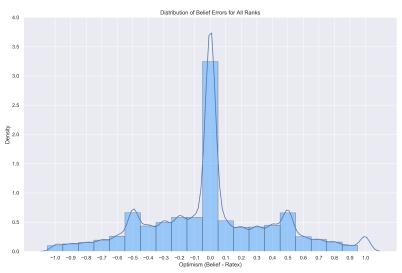
Survey - Admission Process 2019

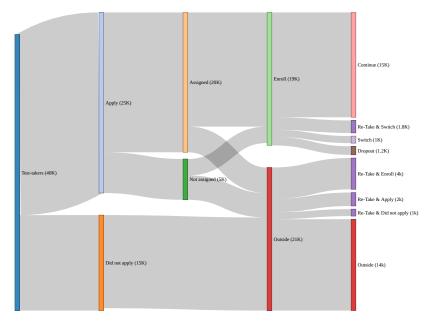
Figure 17: Expected cutoffs most desired vs. first preference

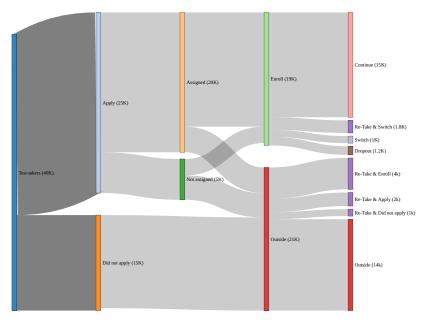


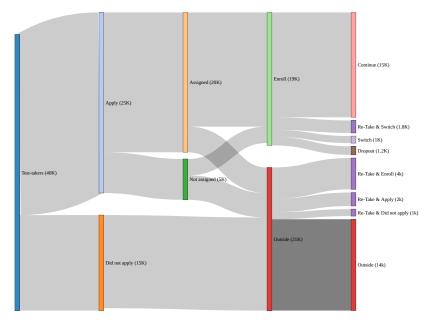
Subjective beliefs

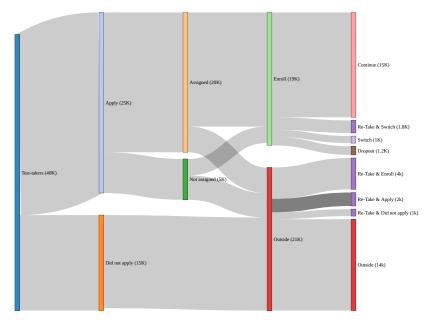
Figure 18: Subjective beliefs

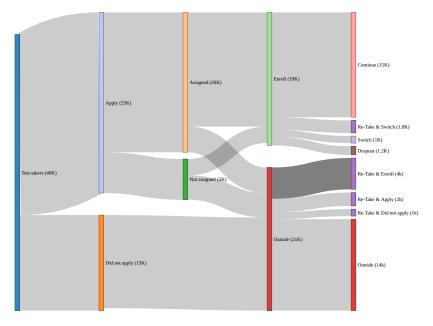


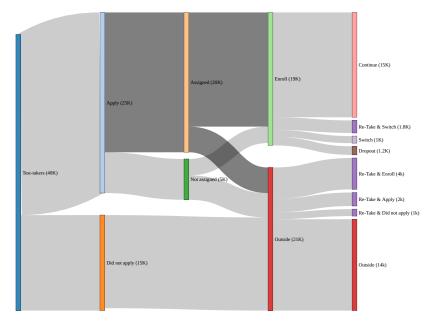


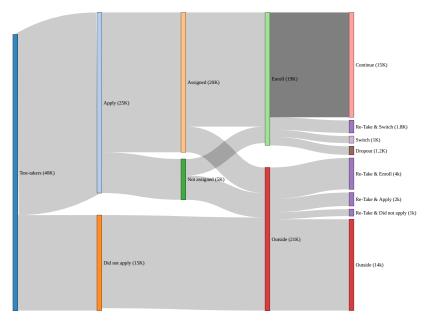


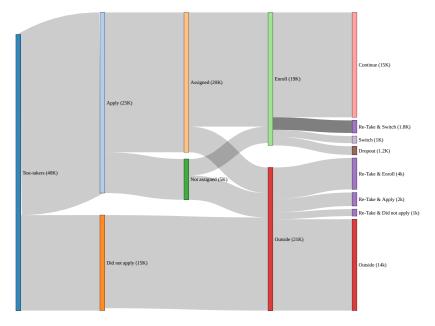


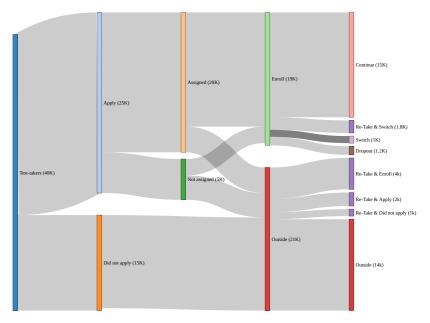


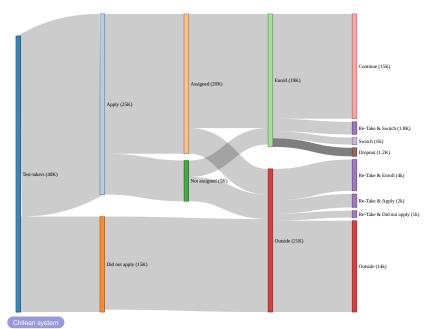






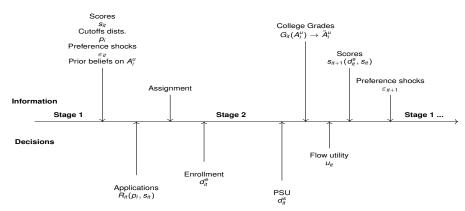






Timeline

► Stages 1, 2: repeat from $t = 1, ..., \bar{t}$



Stage 3: At \bar{t} , students face an exogenuous graduation probability, P_{ijt}^g and receive their lifetime earnings.



RDD Results

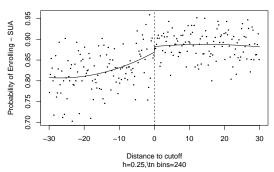
	Enroll - System		Enroll - SUA		Enroll - Top		Re-Apply	
	(1)	(2)	(1)	(2)	(1)	(2)	(1)	(2)
Above cutoff	0.014 (0.013)	0.014 (0.013)	0.016 (0.012)	0.017 (0.012)	0.493*** (0.013)	0.494*** (0.013)	-0.081*** (0.015)	-0.076*** (0.017)
Program FE	No	Yes	No	Yes	No	Yes	No	Yes
Observations R ²	38,928 0.008	38,928 0.008	38,928 0.005	38,928 0.005	38,928 0.539	38,928 0.539	38,928 0.017	38,928 0.020
Note:						*p<	0.1; **p<0.05	: ***p<0.01

RDD

Sample selection problem

- Interested in other outcome variables: Dropout, Stopout, Switches → selection problem
 - Outcomes only observed for students who enroll

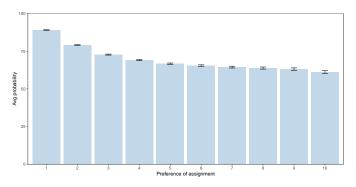




Mismatching

Survey: "What is the probability that you will remain enrolled in each of your preferences?"

Figure 20: Average "perceived" program-retention probability



Forward-looking behavior: anticipate future switches

Mismatching: match-effects

$$P_{ij} = \alpha_i + \alpha_j + X_{ij}\beta + \beta_R R_i(j) + \varepsilon_{ij}$$
 (1)

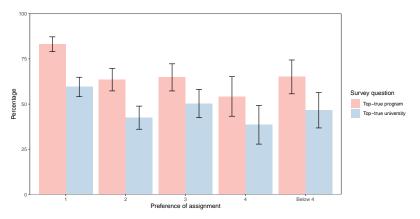
Table 8: Two-way Fixed Effects Regression Results

	Dependent variable: Prob. of Persistence
Preference 2	-9.891***
Preference 3	-16.844***
Preference 4	-21.355***
Preference 5	-24.831***
Preference 6	-27.148***
Preference 7	-29.164***
Preference 8	-30.329***
Preference 9	-31.995***
Preference 10	-34.757***
Constant	89.181***
Observations	159,894
R^2	0.095
Adjusted R ²	0.095

Note: Significance reported: * p < 0.1; *** p < 0.05; *** p < 0.01.

Learning

Figure 21: Percentage of re-applicants that change their top-true preference



Close to 60% of re-applicants change their top-true preference

Learning

Table 9: Effect of Grades on Outcomes

	Re-Take PSU	Re-Apply	Switch Program	GPA
GPA	-0.904***	-0.903***	-1.221***	-
	(0.018)	(0.018)	(0.019)	-
Preference 2	0.653***	0.651***	0.163***	-0.057***
	(0.040)	(0.040)	(0.038)	(0.011)
Preference 3	0.922***	0.923***	0.352***	-0.061***
	(0.050)	(0.050)	(0.050)	(0.015)
Preference 4	1.201***	1.202***	0.562***	-0.070***
	(0.070)	(0.070)	(0.071)	(0.022)
Preference 5	1.116***	1.116***	0.523***	-0.013
	(0.103)	(0.103)	(0.102)	(0.032)
Preference Below 5	1.098***	1.099***	0.454***	-0.113***
	(0.112)	(0.112)	(0.115)	(0.035)
Observations	39,275	39,275	39,275	39,275

Learning: grades and outcomes

Table 10: Effect of Grades on Outcomes

	Re-Take PSU	Re-Apply	Switch Program	GPA
GPA	-0.904***	-0.903***	-1.221***	_
	(0.018)	(0.018)	(0.019)	-
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Preference Below 5	1.098***	1.099***	0.454***	-0.113***
	(0.112)	(0.112)	(0.115)	(0.035)
Observations	39,275	39,275	39,275	39,275

Grades are negatively correlated with switching outcomes



Learning: grades and outcomes

Table 11: Effect of Grades on Outcomes

	Re-Take PSU	Re-Apply	Switch Program	GPA
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	(0.112)	(0.112)	(0.115)	(0.035)
Observations	39,275	39,275	39,275	39,275

▶ Preference of assignment has a small negative correlation with grades



Model solution

Period t = 3:

$$\begin{split} V_{ijt}(\mu_{ij2},\tau_{ijt}) &= E_t \left[\sum_{t'=\tau_{ijt}+1}^{T_f} P^g_{ijt'} \left(\mathbb{E}_{\varepsilon} \left[\sum_{t''=0}^{t'-(\tau_{ijt}+1)} \beta^{t''} u_{ij(t+t'')} \right] + \beta^{t'-\tau_{ijt}} \underbrace{V^w_{ij(t+t'-\tau_{ijt})}(\mu_{ij2})}_{\text{Value fcn Labor market}} \right) \right] \\ &+ E_t \left[\sum_{t'=\tau_{ijt}+1}^{T_f} P^d_{ijt'} \left(\mathbb{E}_{\varepsilon} \left[\sum_{t''=0}^{t'-(\tau_{ijt}+1)} \beta^{t''} u_{ij(t+t'')} \right] + \beta^{t'-\tau_{ijt}} \underbrace{V_{i0(t+t'-\tau_{ijt})}}_{\text{Value fcn Dropout}} \right) \right] \end{split}$$

Period t = 2:

Indirect utility of enrolling in *j*:

$$V_{ijt}(\mu_{ij2},\tau_{ijt}) = u_{ijt} - \mathbb{1}_{\{(j\neq 0)\cap(\tau_{ijt}=0)\}}C^e + \beta\mathbb{E}_{\varepsilon}\left[V_{ijt+1}(\mu_{ij2},\tau_{ijt+1})\right]$$

Model solution

Period t = 1:

$$\begin{aligned} V_{\mathit{ijt}}(\mu_{\mathit{ij1}},\tau_{\mathit{ijt}},\vec{s}_{\mathit{it}}) &= \max_{d_{\mathit{it}}^s} E_0 \Big[u_{\mathit{ijt}} - d_{\mathit{it}}^s C^{\mathit{psu}} - \mathbb{1}_{\{j \neq 0\}} C^e + \\ \beta \int_{a_{\mathit{ij1}}} \int_{\vec{s}_{\mathit{it+1}}} \underbrace{EmaxROL(\tau_{\mathit{ijt}} + 1, \vec{s}_{\mathit{it+1}}, \mu_{\mathit{i2}}(a_{\mathit{ij1}}))}_{\text{continuation value of reapplications}} \underbrace{d\pi(a_{\mathit{ij1}})}_{\text{signal}} \underbrace{dF(\vec{s}_{\mathit{it+1}} | \vec{s}_{\mathit{it}}, d_{\mathit{it}}^s)}_{\text{future scores}} \Big] \end{aligned}$$

Application

Counterfactuals Mechanisms

Counterfactuals Re-applications

Pairwise-stability

Proposition (Fack et al (2018))

In a large market, the allocation of Constrained DA satisfies pairwise-stability, i.e,

$$\mu(i|\varepsilon_i, \{P_j\}_{j \in \mathcal{J}}) = \operatorname*{argmax}_{j \in J_i(\{P_j\}_{j \in \mathcal{J}})} \bar{u}_{ij} + \varepsilon_{ij}$$

$$J_i(\{P_j\}_{j\in\mathcal{J}}):=\{j\in\mathcal{J}:s_{ij}\geq P_j\}\bigcup\{j=0\}$$

Proposition (EmaxROL)

$$\textit{EmaxROL} = \mathbb{E}_{\{P_j\}_{j \in \mathcal{J}}} \left[\log \left(\sum_{j \in J_i(\{P_j\}_{j \in \mathcal{J}})} \exp \left(\bar{u}_{ij}\right) \right) + \gamma \right]$$

Identification

Bootstrap

Agarwal and Somaini (2018) show that a consistent estimator of these beliefs can be obtained using the following bootstrap procedure:

- For each period t and each bootstrap simulation b = 1, ..., B,
 - Sample with replacement a set N_t^b of N_t students with their corresponding ROLs and scores.
 - ▶ Run the mechanism to obtain the allocation μ_t^b .
 - ▶ Obtain the set of cutoffs $\left\{ \bar{\mathbf{s}}_{jt}^{b}\right\} _{j\in J}$ from the allocation μ_{t}^{b} , i.e., for each $j\in J$,

$$\bar{\mathbf{s}}_{jt}^b = \min\left\{\mathbf{s}_{ijt}: i \in N_t^b, \ \mu_t^b(i) = j\right\}$$

▶ We can estimate the admission probability of student $i \in N_t$ in program $j \subset J$ as

$$\hat{
ho}_{ijt} = rac{1}{B} \sum_{b=1}^{B} \mathbb{1}_{\left\{s_{ijt} \geq \bar{s}_{jt}^{b}
ight\}}$$

We estimate these probabilities running B = 10,000 bootstrap simulations for every application process

Goodness of fit

Table 12: Correlation between grades and outcomes

	Model	Data
Dropout	-0.055	-0.086
Switching programs	-0.152	-0.148
Switching broad majors	-0.092	-0.075
Switching majors	-0.172	-0.107
Switching math type	-0.079	-0.044
Switching Up	-0.008	0.002
Switching Down	-0.029	-0.032
Switching Out feasible	-0.084	-0.089
Switching Out unfeasible	-0.032	-0.011

Table 13: Causal effect RDDs

	Model	Data
RDD switch program 1 (level)	0.205	0.1622
RDD switch program 1 (coeff.)	-0.07	-0.0478
RDD reapplications 1 (level)	0.488	0.2261
RDD reapplications 1 (coeff.)	-0.104	-0.0840

Indirect Inference Algorithm: Computing $Q(\theta)$

input: Value of the structural parameters θ , and first-stage estimates \hat{p} , \hat{P}^e , \hat{P}^d , \hat{P}^g , and \hat{P}^w . **output**: Value of the objective function $Q(\theta)$

```
foreach student i in the sample do
      foreach simulation m_{rc} \in \{1, ..., N_{rc}\} do
             Draw a vector of random coefficients \alpha_i^{m_{rc}};
             Solve the model by backward-induction:
             foreach simulation m_s \in \{1, ..., N_s\} do
                   foreach state do
                          Draw a vector of preference shocks \varepsilon_i^{m_S, m_{rc}}, enrollment shocks \varepsilon_i^{e, m_S, m_{rc}},
                            wage shocks \epsilon_i^{m_S,m_{rc}}, vector of random cutoff scores P^{m_S,m_{rc}} from the
                            empirical distribution of cutoffs, vector of PSU score shocks v_i^{m_S, m_{rc}},
                            vector of unknown abilities A_i^{u,m_S,m_{rc}}, and grade shocks \varepsilon_i^{g,m_S,m_{rc}};
                   end
                    Forward-simulate the model and obtain a set of outcomes y_i^{m_s, m_{rc}};
      end
end
foreach m_s \in \{1, ..., N_s\} and m_{rc} \in \{1, ..., N_{rc}\} do
      Estimate the auxiliary model parameters, \hat{\beta}^{m_s,m_{rc}}(\theta), on the simulated sample;
end
Compute \bar{\beta}(\theta) = \frac{1}{N_{rc} \times N_s} \sum_{m_{rc}} \sum_{m_s} \hat{\beta}^{m_s, m_{rc}}(\theta);
Return Q(\theta) := (\bar{\beta}(\theta) - \hat{\beta})^T W(\bar{\beta}(\theta) - \hat{\beta});
```

Table 14: Estimation moments

Moment description	Targeted parameters
Share of students who retake the PSU	Cpsu
Share of students who dropout by gender and income level	$\{\alpha_d\}_d$, α^w , C^e , σ_s^2
Grade auxiliary models' coefficients	γ, σ_q^2
Wage auxiliary models' coefficients	λ
Switchings and dropout auxiliary models' coefficients	γ, σ_g^2 λ $\sigma_g^2, \sigma_m^2, \sigma_s^2, \alpha_4^w$ $V_{\alpha^m}, V_{\alpha^k}, C^e$
RDD auxiliary models' coefficients	$V_{\alpha^m}, V_{\alpha^k}, C^e$
Share of students who reapply	
Share of students who switch programs	σ_m^2 , σ_s^2 , V_{α^m} , V_{α^k} , C^{θ}
Share of students who switch majors	σ_m^2, V_{α^m}
Share of students who switch majors within math-types	σ_m^2 , V_{α^m}
Share of students who switch math-types within majors	$\sigma_{\rm e}^2$
Share of students who switch college-types	$\sigma_{m}^{2}, \sigma_{n}^{2}, V_{\alpha^{m}}$ $\sigma_{m}^{2}, V_{\alpha^{m}}$ $\sigma_{m}^{2}, V_{\alpha^{m}}$ σ_{s}^{2} $V_{\alpha^{k}}$
Share of students who dropout at the end of the first year of college	α^{w}
Share of students who choose the outside option every year	$\alpha^{\mathbf{w}}$
Share of students who start college in the second year	
Share of students who remain in the same program after two years	
Share of top-reported preferences by program	$\{\alpha_{fe}\}_{j}$
Share of students whose top-reported preference is their top-true preference in R ₁	ρ
Share of students whose top-reported preference is their top-true preference in R ₂	ρ
Share of students whose top-reported preference has zero admission probability	ρ
Share of students with a positive risk of being unassigned given R ₁	ρ
Share of ROLs R ₁ with length 10	ρ
Share of ROLs R ₂ with length 10	ρ
Share of students assigned to their top-true preference in the first period	ρ
Share of students who apply in the first year	
Share of students who apply in the second year	
Share of reapplications that change in their top-true preference	σ_m^2 , σ_s^2 , V_{α^m} , V_{α^k}
Shares of majors within R ₁	V_{α^m}
Shares of college-types within R ₁	V_{α^k}
Shares of majors within R ₂	V_{α^m}
Shares of college-types within R ₂	V_{α^k}

Table 15: Estimation moments

Moment description	Targeted parameters
Norm of the difference between the vectors of college-type	V_{α^k}
shares for students who reapply	a
Norm of the difference between the vectors	σ_m^2 , V_{α^m}
of major shares for students who reapply	- m, • α
1 Norm of the difference between the vectors of ω shares for students who reapply	σ_s^2 , V_{α^m} , V_{α^k}
Correlation between first-year grades and the norm of the difference between the vectors	σ_m^2 , σ_a^2
of major shares for students who reapply	- m, - y
1 Correlation between first-year grades and the norm of	σ_s^2 , σ_q^2
the difference between the vectors of ω shares for students who reapply	
Share of applications by major and college-type, grouped by gender in R ₁	Δ^m , Δ^k
Share of applications by major and college-type, grouped by gender in R ₂	Δ^m , Δ^k
Share reapplications from top-reported preferences	
Share reapplications from top-true preferences	
Mean of tuition for top-reported preferences, grouped by students' scores and income groups	$\{\alpha_c\}_c$
Mean of observed ability for top-reported preferences	α_1
Mean of average observed ability at the college level for top-reported preferences	α_2
Mean of distance for top-reported preferences	α_3
Mean of relative observed ability position for topreported preferences	α_4
Mean and variance of $\log\left(\frac{s_{\ell+1}}{s_\ell}\right)$ for positive PSU scores	$\{\alpha_I\}_I$, σ_{psu}
Mean and variance of $\log \left(\frac{S_{k+1}}{S_t}\right)$ for PSU scores wit zero value in the first year	$\{\alpha_{0I}\}_I$, σ_{psu}

Table 16: Estimation Results - Parameters

Parameters	Values	Std
Application behavior and Dropout		
Share of strategic ROLs $(1 - \rho)$	0.74	[0.022]
Cost of retaking PSU (Cpsu)	4.46	[0.219]
Dropout flow-utility for females ($\alpha_{female}^{dropout}$)	19	[1.262]
Dropout flow-utility for males $(\alpha_{male}^{dropout})$	41.8	[1.756]
Dropout flow-utility for low-income ($\alpha_{low-income}^{dropout}$)	15.8	[0.83]
First-time enrollment cost (Ce)	32.16	[0.944]
Flow-utility and Priors		
Tuition (α_c)	-0.14	[0.049]
Relative position (α_4)	-0.28	[0.022]
Distance (α_3)	-1.09	[0.056]
Student observed ability (α_1)	12.92	[0.86]
Program observed ability (\alpha_2)	4.65	[0.26]
Gender effect by major (Δ^m)	(-4.93 -2.46 3.28 1.48)	([0.363][0.171][0.256][0.237]
Variance major random coefficient (σ_{α}^{2m})	15.69	[0.913]
Income effect by college (Δ^k)	(-0.11 -0.12 9.06)	([0.215],[0.218],[0.449])
Variance college random coefficient (σ_{α}^{2k})	0.43	[0.075]
Major prior variance (σ_m^2)	0.34	[0.032]
Subject prior variance (σ_s^2)	0.48	[0.103]

Notes: the order of majors is Social Sciences, Science, Education and Humanities, and Health.

The order of colleges is CRUCH-Public, CRUCH-Private, and Non-CRUCH.



Table 17: Estimation Results - Parameters

Parameters	Values	Std
Grade equations		
Constant by major (γ_{1m_i})	(3.91 4.32 3.81 3.43)	([0.105][0.229][0.14][0.208])
Student observed ability (γ_2)	0.52	[0.053]
Gender effect (γ_3)	0.36	[0.052]
Random coefficient effect on grades (major) (γ_4)	0.05	[0.015]
Grade shock variance (σ_g^2)	0.08	[0.04]
Evolution of scores		
Std. of ν (σ_{psu})	0.1	[0.007]
Mean prop. change $(\{\alpha_i\}_i)$	(1.06 1.07 1.05 1.02)	([0.004][0.007][0.006][0.001])
Mean prop. change from zero score ($\{\alpha_{0l}\}_l$)	(1.07 1.08)	([0.024][0.021])
Non-pecuniary work utility		
Major random coefficient (α_1^w)	8.72	[0.363]
Student observed ability (α_2^{W})	71.58	[2.688]
College observed ability (α_3^w)	-1.86	[0.592]
Non-pecuniary work value of unknown ability (α_4^w)	178.57	[6.852]
Pecuniary work utility parameter (α_5^w)	75.95	[5.247]
Wage parameters		
Constant by major (λ_{1m_i})	(1.78 1.17 1.07 1.63)	([0.073],[0.083],[0.1],[0.059])
College observed ability (λ_2)	0.03	[0.011]
Grades (λ_3)	0.13	[0.017]
Gender effects (λ_4)	-0.19	[0.094]
Wage shock variance (σ_w^2)	0.68	[80.0]
Wage growth		
Linear term by major (λ_{5m_i})	(0.11 0.18 0.14 0.24)	(-)
Quadratic term by major (λ_{6m_i})	(0 -0.01 -0.01 -0.02)	(-)

Notes: the order of majors is Social Sciences, Science, Education and Humanities, and Health.

The order of colleges is CRUCH-Public, CRUCH-Private, and Non-CRUCH.



Switching equations:

$$O_{ij} = \beta_{1m_j}^o + \beta_2^o A_{ij} + \beta_3^o Z_i^g + \underbrace{\beta_4^o \mathbbm{1}\{j = R_{1i}(1)\} + \beta_5^o s_{1im_j} + \beta_6^o s_{1ik_j}}_{\text{correlated with } \alpha_{im_j} \qquad \alpha_{ik_j}} + \underbrace{\beta_7^o G_{ij1}}_{\text{correlated with } A_{ij}^o} + \underbrace{\beta_7^o G_{ij1}}_{\text{correlated with } A_{ij}^o} + \underbrace{\beta_7^o G_{ij1}}_{\text{correlated with } A_{ij}^o}$$

Grade equations:

$$\begin{split} G_{ij1} &= \beta_{1m_j}^{\gamma} + \beta_2^{\gamma} A_{ij} + \beta_3^{\gamma} Z_i^{g} + \underbrace{\beta_4^{\gamma} \mathbb{1}\{j = R_{1i}(\mathbf{1})\} + \beta_5^{\gamma} \mathbf{s}_{1im_j} + \beta_6^{\gamma} \mathbf{s}_{1ik_j}}_{\text{correlated with } \alpha_{im_j} \quad \alpha_{ik_j}} + \varepsilon_{ij1}^{g}, \\ G_{ij2} &= \left(\beta_7^{\gamma} + \beta_8^{\gamma} S\right) G_{ij1} + \beta_9^{\gamma} + \gamma_{10} S + \varepsilon_{ij2}^{g}. \end{split}$$

Pecuniary:

$$\begin{split} \log(\bar{\textit{w}}_{\textit{J}(\tau=4)}) &= \beta_{1\textit{m}_{\textit{j}}}^{\lambda} + \beta_{2}^{\lambda} \bar{\textit{A}}_{\textit{k}_{\textit{j}}} + \beta_{3}^{\lambda} \bar{\textit{G}}_{\textit{j}} + \beta_{4}^{\lambda} \bar{\textit{Z}}^{\textit{w}} + \epsilon_{\textit{J}(\tau=4)}, \\ \log(\bar{\textit{w}}_{\textit{m}_{\textit{j}}\tau}) &= \beta_{5\textit{m}_{\textit{j}}}^{\lambda} + \beta_{6\textit{m}_{\textit{j}}}^{\lambda} \tau + \beta_{7\textit{m}_{\textit{j}}}^{\lambda} \tau^{2} + \epsilon_{\textit{m}_{\textit{j}}\tau}, \end{split}$$

Non-pecuniary:

$$y_{ij} = \beta_1^{w} \mathbf{S}_{1im_j} + \beta_2^{w} \mathbb{1}\{j = R_{1i}(1)\} + \beta_3^{w} A_{ij} + \beta_4^{w} \bar{A}_{k_j} + \beta_5^{w} Z_i^g + \varepsilon_{ij}^{w}$$