## 1 Apparent Balanced Growth in $\mathfrak{c}$ and $\mathbf{cov}(c, \mathbf{p})$

Section 4.2 demonstrates some propositions under the assumption that, when an economy satisfies the GIC, there will be constant growth factors  $\Omega_{\rm c}$  and  $\Omega_{\rm cov}$  respectively for  ${\mathfrak c}$  (the average value of the consumption ratio) and  ${\rm cov}(c,{\bf p})$ . In the case of a Szeidlinvariant economy, the main text shows that these are  $\Omega_{\rm c}=1$  and  $\Omega_{\rm cov}=G$ . If the economy is Harmenberg- but not Szeidl-invariant, no proof is offered that these growth factors will be constant.

## 1.1 $\log c$ and $\log (\operatorname{cov}(c, \mathbf{p}))$ Grow Linearly

Figures 1 and 2 plot the results of simulations of an economy that satisfies Harmenberg- but not Szeidl-invariance with a population of 4 million agents over the last 1000 periods (of a 2000 period simulation). The first figure shows that  $\log \mathfrak{c}$  increases apparently linearly. The second figure shows that  $\log(-\operatorname{cov}(c,\mathbf{p}))$  also increases apparently linearly. (These results are produced by the notebook ApndxBalancedGrowthcNrmAndCov.ipynb).

<sup>&</sup>lt;sup>1</sup>For an exposition of our implementation of Harmenberg's method, see this supplemental appendix.



Figure 1 Appendix:  $\log \mathfrak{c}$  Appears to Grow Linearly



**Figure 2** Appendix:  $\log (-\cos(c, \mathbf{p}))$  Appears to Grow Linearly