

DFT of $x(n)$ is given by

$$X(K) = \sum_{n=0}^{N-1} x(n) W_N^{nK} \quad N = 8$$

$$x(n) = \{4, 3, 2, 6, 8, 4, 6, 3\}$$

$$X(K) = \sum_{n=0}^7 x(n) W_8^{nK}$$

Using direct calculation method

$$W_8^0 = 1 \quad W_8^1 = 0.707 - 0.707j \quad W_8^2 = -j \quad W_8^3 = -0.707 - 0.707j$$

$$W_8^4 = -1 \quad W_8^5 = -0.707 + 0.707j \quad W_8^6 = j \quad W_8^7 = 0.707 + 0.707j$$

$$X(0) = 4 + 3 + 2 + 6 + 8 + 4 + 6 + 3 = 36$$

$$X(1) = 4 + 3W_8^1 + 2W_8^2 + 6W_8^3 + 8W_8^4 + 4W_8^5 + 6W_8^6 + 3W_8^7 = -6.82 + 2.58j$$

$$X(2) = 4 + 3W_8^2 + 2W_8^4 + 6W_8^6 + 8W_8^8 + 4W_8^{10} + 6W_8^{12} + 3W_8^{14} = 4 + 2j$$

$$X(3) = 4 + 3W_8^3 + 2W_8^6 + 6W_8^9 + 8W_8^{12} + 4W_8^{15} + 6W_8^{18} + 3W_8^{21} = -1.17 - 5.41j$$

$$X(4) = 4 + 3W_8^4 + 2W_8^8 + 6W_8^{12} + 8W_8^{16} + 4W_8^{20} + 6W_8^{24} + 3W_8^{28} = 4$$

$$X(5) = -1.17 + 5.41j = X^*(3) \quad (\text{Conjugate Symmetry Property})$$

$$X(6) = 4 - 2j = X^*(2)$$

$$X(7) = -6.82 - 2.58j = X^*(1)$$

$$X(K) = \{36, -6.82 + 2.58j, 4 + 2j, -1.17 - 5.41j, 4, -1.17 + 5.41j, 4 - 2j, -6.82 - 2.58j\}$$

Same in matlab

IDFT

$$X(K) = \sum_{n=0}^{N-1} x(n) W_N^{nK} \times \frac{1}{N} \quad N = 8$$

IDFT using DFT

$$x(n) = \left\{ \sum_{K=0}^{N-1} X^*(K) W_N^{Kn} \right\}^*$$

$$X(K) = \{36, -6.82+2.58j, 4+2j, -1.17-5.41j, 4, \\ -1.17+5.41j, 4-2j, -6.82-2.58j\}$$

$$X^*(K) = \{36, -6.82-2.58j, 4-2j, -1.17+5.41j, 4, \\ -1.17-5.41j, 4+2j, -6.82+2.58j\}$$

$$x(0) = 36 - 6.82 - 2.58j + 4 - 2j - 1.17 + 5.41j + 4 - 1.17 - 5.41j + 4 + 2j - 6.82 + 2.58j = 4$$

$$x(1) = 36 + (-6.82-2.58j)W_8^1 + (4-2j)W_8^2 + (-1.17+5.41j)W_8^3 + (4)W_8^4 + (-1.17-5.41j)W_8^5 + (4+2j)W_8^6 + (-6.82+2.58j)W_8^7 = 3$$

$$x(2) = 36 + (-6.82-2.58j)W_8^2 + (4-2j)W_8^4 + (-1.17+5.41j)W_8^6 + (4)W_8^8 + (-1.17-5.41j)W_8^{10} + (4+2j)W_8^{12} + (-6.82+2.58j)W_8^{14} = 2$$

$$x(3) = 36 + (-6.82-2.58j)W_8^3 + (4-2j)W_8^6 + (-1.17+5.41j)W_8^9 + (4)W_8^{12} + (-1.17-5.41j)W_8^{15} + (4+2j)W_8^{18} + (-6.82+2.58j)W_8^{21} = 6$$

$$x(4) = 36 + (-6.82-2.58j)W_8^4 + (4-2j)W_8^8 + (-1.17+5.41j)W_8^{12} + (4)W_8^{16} + (-1.17-5.41j)W_8^{20} + (4+2j)W_8^{24} + (-6.82+2.58j)W_8^{28} = 8$$

$$x(5) = 36 + (-6.82-2.58j)W_8^5 + (4-2j)W_8^{10} + (-1.17+5.41j)W_8^{15} + (4)W_8^{20} + (-1.17-5.41j)W_8^{25} + (4+2j)W_8^{30} + (-6.82+2.58j)W_8^{35} = 4$$

Same

$$x(6) = 36 + (-6.82 - 2.58j)W_8^6 + (4 - 2j)W_8^{12} + (-1.17 + 5.41j)W_8^{18} + (4)W_8^{24} + (-1.17 - 5.41j)W_8^{30} + (4 + 2j)W_8^{36} + (-6.82 + 2.58j)W_8^{42} = 6$$

$$x(7) = 36 + (-6.82 - 2.58j)W_8^7 + (4 - 2j)W_8^{14} + (-1.17 + 5.41j)W_8^{21} + (4)W_8^{28} + (-1.17 - 5.41j)W_8^{35} + (4 + 2j)W_8^{42} + (-6.82 + 2.58j)W_8^{49} = 3$$

$$x(n) = \{4, 3, 2, 6, 8, 4, 6, 2\}$$

↑

DTFT

$$X(e^{j\omega}) = \sum_{n=-\infty}^{\infty} x(n)e^{-j\omega n}$$

$$= \sum_{n=0}^7 x(n)e^{-j\omega n}$$

$$= x(0) + x(1)e^{-j\omega} + x(2)e^{-2j\omega} + x(3)e^{-3j\omega} + x(4)e^{-4j\omega} + x(5)e^{-5j\omega} + x(6)e^{-6j\omega} + x(7)e^{-7j\omega}$$