

DFT $x(n) = \{4, 3, 2, 6, 8, 4, 6, 3\}$

$$X(K) = \sum_{n=0}^{N-1} x(n) \omega_N^{nK} \quad \underline{N=8}$$

$$\therefore X(K) = \sum_{n=0}^{7} x(n) \omega_8^{nK}$$

Using direct calculation method.

$$\omega_8^0 = 1 \quad \omega_8^1 = 0.707 - 0.707j \quad \omega_8^2 = -j \quad \omega_8^3 = -0.707 - 0.707j$$

$$\omega_8^4 = -1 \quad \omega_8^5 = -0.707 + 0.707j \quad \omega_8^6 = j \quad \omega_8^7 = 0.707 + 0.707j$$

$$X(0) = 4 + 3 + 2 + 6 + 8 + 4 + 6 + 3 = \underline{36}$$

$$X(1) = 4 + 3\omega_8^1 + 2\omega_8^2 + 6\omega_8^3 + 8\omega_8^4 + 4\omega_8^5 + 6\omega_8^6 + 3\omega_8^7 = -6.82 + 2.58j$$

$$X(2) = 4 + 3\omega_8^2 + 2\omega_8^4 + 6\omega_8^6 + 8\omega_8^8 + 4\omega_8^{10} + 6\omega_8^{12} + 3\omega_8^{14} = 4 + 2j$$

$$X(3) = 4 + 3\omega_8^3 + 2\omega_8^6 + 6\omega_8^9 + 8\omega_8^{12} + 4\omega_8^{15} + 6\omega_8^{18} + 3\omega_8^{21} = -1.17 - 5.41j$$

$$X(4) = 4 + 3\omega_8^4 + 2\omega_8^8 + 6\omega_8^{12} + 8\omega_8^{16} + 4\omega_8^{20} + 6\omega_8^{24} + 3\omega_8^{28} = \underline{4}$$

$$X(5) = 4 + 3\omega_8^5 + 2\omega_8^{10} + 6\omega_8^{15} + 8\omega_8^{20} + 4\omega_8^{25} + 6\omega_8^{30} + 3\omega_8^{35} = -1.17 + 5.41j$$

$$X(6) = 4 - 2j \quad (\text{conjugate of } X(2)) \quad (\text{conjugate symmetry property})$$

$$X(7) = \underline{-6.82 - 2.58j}$$

Same in matlab

IDFT using DFT.

$$X(K) = \sum_{n=0}^{N-1} x(n) \omega_N^{Kn} \quad N=8$$

$$\text{Now } x(n) = \left\{ \sum_{K=0}^{N-1} X(K) \omega_N^{Kn} \right\}$$

$$X(K) = \{36, -6.82 + 2.85j, 4 + 2j, -1.17 + 5.41j, 4, -1.17 + 5.41j, 4 - 2j, -6.82 - 2.58j\}$$

$$X^*(K) = \{36, -6.82 - 2.85j, 4 - 2j, -1.17 - 5.41j, 4, -1.17 - 5.41j, 4 + 2j, -6.82 + 2.58j\}$$

$$x(0) = 36 - 6.82 - 2.85j + 4 - 2j - 1.17 - 5.41j + 4 - 1.17 - 5.41j + 4 + 2j - 6.82 + 2.58j = \underline{4}$$

$$x(1) = 36 + (-6.82 + 2.85j) \omega_8^1 + (4 + 2j) \omega_8^2 + (-1.17 + 5.41j) \omega_8^3 + 4 \omega_8^4 + (-1.17 + 5.41j) \omega_8^5 + (4 - 2j) \omega_8^6 + (-6.82 - 2.58j) \omega_8^7 = 3$$

$$x(2) = 2$$

$$x(5) = 4$$

$$x(3) = 6$$

$$x(6) = 6$$

$$x(4) = 8$$

$$x(7) = \underline{\underline{3}}$$

$$x(n) = \{ \underset{\uparrow}{4}, 3, 2, 6, 8, 4, 6, 3 \}$$