## Family History and Life Insurance

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IRE (HEC) - CREEI Seminair, February 2021

https://arxiv.org/abs/2006.08446



### Family History & Risk

The New Hork Times

OP-ED CONTRIBUTOR

# My Medical Choice

By Angelina Jolie

May 14, 2013



LOS ANGELES

MY MOTHER fought cancer for almost a decade and died at 56. She held out long enough to meet the first of her grandchildren and to hold them in her arms. But my other children will never have the chance to know her and experience how loving and gracious she was.

We often speak of "Mommy's mommy," and I find myself trying to explain the illness that took her away from us. They have asked if the same could happen to me. I have always told them not to worry, but the truth is I carry a "faulty" gene, BRCA1, which sharply increases my risk of developing breast cancer and ovarian cancer.

My doctors estimated that I had an 87 percent risk of breast cancer and a 50 percent risk of ovarian cancer, although the risk is different in the case of each woman.

2013 Angelina Jolie risk of developing cancers family history Angelina Jolie lost 8 family members to cancer

Interesting debates related to predictive probabilities, risk, insurance and prevention

# 'Family History' & Insurance Forms

Family History: (Please Note The Family Mem							
Breast Cancer:							
		Genetic Disorders: High Blood Pressure:					
	Lung Cancer:						
		Other Cancer:					
Ovarian Cancer:							
Stroke/DVT/Clotting/Bleeding Disorder:							
Other:	Uterine Cancer:						
Family History (family history is a consider		(0 ( "					
To your knowledge, is there any family hi							
cerebrovascular disease, heart disease,	stroke, diabetes, or cancer?	Yes □ No □					
If yes, provide full details:							
☐ Father: Impairment	Age at Onset Age	e at Death (if deceased)					
☐ Mother: Impairment Age at Onset Age at Death (if deco							
☐ Siblings: Impairment							
FAMILY HISTORY: Please check the box if you		AND NOW					
Diabetes High Blood Pressure Heart Attack, Cancer Alzheimer's Family Histor	Heart Disease Blood Clots or Stroke y Unknown Mental Illness	☐ Tuberculosis ☐ Epilepsy/Seizure					
Any other major conditions?	y Chandra Times	E. Epitepsy Season					
Any other major conditions:							
If you answered Yes to any of the above, please explain							
Are you currently being treated for medical conditions?	☐ Yes ☐ No ☐ If yes, please list:						
Family Medical History							
Age	Diseases	If Deceased, Cause of Death					
Father							
Mother							
Siblings							
Spouse		82					
Children		2					







## Agenda

Motivations **Existing Literature** Longitudinal & Collaborative Data Genealogical Data 'Family History' & Life Insurance Husband-Wife Children-Parents **Grand Children-Grandparents** 



Using genealogical trees to understand dependencies in life spans and quantify the impact on (life related) insurance premiums

### Literature on Family and Insurance

- Parkes et al. (1969) 4,486 widowers of 55 yearsold (and older) to confirm the broken heart syndrom
- ► Frees et al. (1996): 14,947 insurance contracts, Canadian insurance company, in force in 1988-1993
  - → censoring problem used also in Carriere (1997), Youn and Shemyakin (1999), Shemyakin and Youn (2001)
  - in Luciano et al. (2008), subset of 11,454 contracts, born before 1920 (male) and 1923 (female)
- ▶ Denuit et al. (2001): selected two cemeteries in Brussels (Koekelberg and Ixelles / Elsene) and collected the ages at death of 533 couples buried there

## Longitudinal Data

#### Longitudinal data have been used in many demographic projects

- ► Matthijs and Moreels (2010) (COR\*), Antwerp, Belgium,  $1846-1920. \approx 125k$  events.  $\approx 57k$  individuals
- Mandemakers (2000), Netherlands, 1812–1922,  $\approx 77k$ indivivuals
- ▶ Bouchard et al. (1989) (BALSAC), Québec, Canada, since  $17^{\text{th}}$  century,  $\approx 2M$  events,  $\approx 575k$  individuals
- ▶ Bean et al. (1978), mainly Utah, USA, since 18<sup>th</sup> century.  $\approx 1.2M$  individuals

#### Collaborative Data

#### as well as collaborative data

- ► Fire and Elovici (2015) with data from WikiTree.com +1M profiles (unknown number of individuals)
- ► Cummins (2017) with data from FamilySearch.org, +1.3M individuals
- Gergaud et al. (2016) with biography from wikipedia, +1.2Mindividuals
- ► Kaplanis et al. (2018) with data from Geni.com, 13M individuals

### Genealogical Data

Charpentier and Gallic (2020a) comparing our collaborative based dataset (238,009 users, 1,547,086 individual born in [1800, 1805)), with official historical data

П	ID_user		ID_np	ID_num	Name	e tabular	Surname	Sex	Date_b
1	daage		besnard jean 1	575	BESN	IARD	Jean	1	18000227
2	denisgallie	enne	besnard louis 1	22771	BESN	IARD	Louis	1	18040603
3	domiassi		besnard jean	1748	BESN	IARD	Jean	1	18000227
4	dutheilfr		besnard pierre	729	BESN	IARD	Pierre	1	18001221
5	dvivier1		besnard louis 1	65196	BESN	IARD	Louis	1	18001215
$\equiv$									
	Date_d	Type	Location	Lat		Long	ID_num_	_m I	D_num_p
1	16810000	NM	Longué, 0180	47.3	7806 -	-0.10806	4457		74
	1001000								
2	18831027		Cunault, 49350	47.3		-0.15389	994	1	.620
2	18831027				0833 -		994	1	.620
2	18831027	ND	Cunault, 49350	47.3	0833 <i>-</i>	-0.15389			620

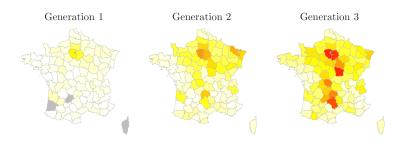
with children, up to 3 generations

- ▶ 402 190 children
- ▶ 286 071 grand-children
- ▶ 222 103 grand-grand-children

Intensive study on exhaustivity & consistency of data

## Genealogical Data

#### Charpentier and Gallic (2020b) on generational migration

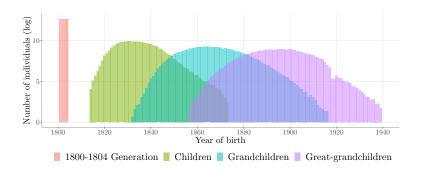


(here Generation 0 was born in Paris)



# Genealogical Data & "Generations"

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Initial starting generation (born in [1800, 1805)), children (born \sim [1815, 1870)), grand-children (born \sim [1830, 1915)), grand-grand-children (born \sim [1850, 1940))
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## Demographic & Insurance Notations

$${}_{t} P_{x} = \mathbb{P}[T(x) > t] = \mathbb{P}[T - x > t | T > x] = \frac{\mathbb{P}[T > t + x]}{\mathbb{P}[T > x]} = \frac{S(x + t)}{S(x)}.$$

curtate life expectancy for  $T_x$  is defined as

$$e_{\mathsf{x}} = \mathbb{E}(\lfloor T_{\mathsf{x}} \rfloor) = \mathbb{E}(\lfloor T - \mathsf{x} \rfloor | T > \mathsf{x}) = \sum_{t=0}^{\infty} t_t p_{\mathsf{x}} \cdot q_{\mathsf{x}+t} = \sum_{t=1}^{\infty} t p_{\mathsf{x}},$$

actuarial present value of the annuity of an individual age (x) is

$$\mathbf{a}_{\mathsf{x}} = \sum_{k=1}^{\infty} \nu^{k}{}_{k} p_{\mathsf{x}} \text{ or } \mathbf{a}_{\mathsf{x}:\overline{\mathsf{n}}} = \sum_{k=1}^{n} \nu^{k}{}_{k} p_{\mathsf{x}},$$

and whole life insurance (see Bowers et al. (1997))

$$A_{\mathsf{x}} = \sum_{k=1}^{\infty} \nu^{k} _{k} p_{\mathsf{x}} \cdot q_{\mathsf{x}+k} \text{ or } A^{1}_{\mathsf{x}:\overline{\mathsf{n}}} = \sum_{k=1}^{n} \nu^{k} _{k} p_{\mathsf{x}} \cdot q_{\mathsf{x}+k}.$$

# Historical Mortality

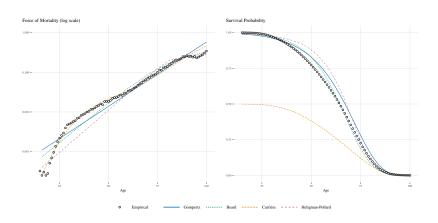
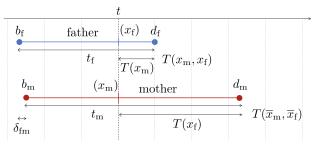


Figure 1: Survival distribution  $_tp_0 = \mathbb{P}[T > t]$  and force of mortality  $_1q_x = \mathbb{P}[T \le x + 1 | T > x]$  (log scale), against historical data.

	birth $(b_{\rm f})$	death $(d_{\rm f})$	age $(t_{\rm f})$	birth $(b_{m})$	death $(d_m)$	age $(t_{ m m})$
i	$b_{f,i}$	$d_{f,i}$	$t_{f,i}$	$b_{m,i}$	$d_{m,i}$	$t_{m,i}$
1	1800-05-04	1835-02-22	34.80356	1762-07-01	1838-01-19	75.55099
2	1778-02-09	1841-02-02	62.97878	1758-07-05	1825-08-03	67.07734
3	1771-01-18	1807-01-17	35.99452	1752-12-28	1815-10-31	62.83641
4	1768-07-01	1814-10-15	46.28611	1768-07-01	1830-12-06	62.42847
5	1766-07-01	1848-01-12	81.53046	1767-02-10	1851-04-22	84.19165
6	1769-06-28	1836-08-28	67.16496	1773-12-17	1825-02-15	51.16222

Table 1: Dataset for the joint life model, father/husband (f) and mother/spouse (m)



# Husband-Wife dependencies - Temporal Stability

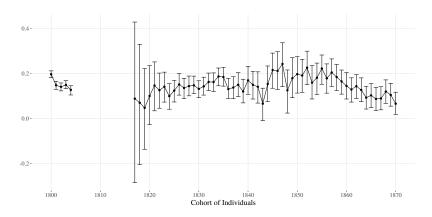


Figure 2: Spearman correlation  $(T_f, T_m)$  - per year of birth of the father.

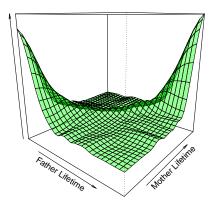


Figure 3: Nonparametric estimation of the copula density,  $(T_f, T_m)$ .

(using Geenens et al. (2017) estimate) Here  $\widehat{\rho_S}=0.168,\,95\%$  confidence interval (0.166; 0, 171)

Multiple life quantities, e.g. annuities and (whole) life insurance,

$$\mathbf{a_{x}} = \sum_{k=1}^{\infty} \nu^{k}{}_{k} p_{x_{\mathrm{f}}} - \sum_{k=1}^{\infty} \nu^{k}{}_{k} p_{x_{\mathrm{f}}, x_{\mathrm{m}}}, \ \ \text{and} \ \ \mathbf{A_{x}} = \sum_{k=1}^{\infty} \nu^{k}{}_{k} p_{x_{\mathrm{f}}} - \sum_{k=1}^{\infty} \nu^{k}{}_{k} p_{x_{\mathrm{f}}, x_{\mathrm{m}}}$$

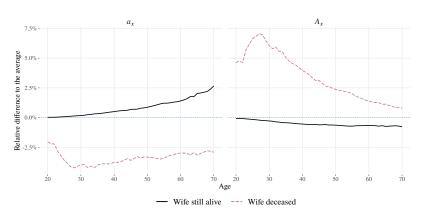


Figure 4: Annuities  $a_x$  and (whole) life insurance  $A_x$ .

Multiple life quantities, e.g. widow's pension,

$$\mathbf{a_{m|f}} = \sum_{k=1}^{\infty} \nu^k_{\ k} p_{\mathbf{x_f}} - \sum_{k=1}^{\infty} \nu^k_{\ k} p_{\mathbf{x_f},\mathbf{x_m}}, \ \text{ where } _t p_{\mathbf{x_f},\mathbf{x_m}} = \mathbb{P}\big[T_{\mathbf{x_f}} > t, T_{\mathbf{x_m}} > t, \big]$$

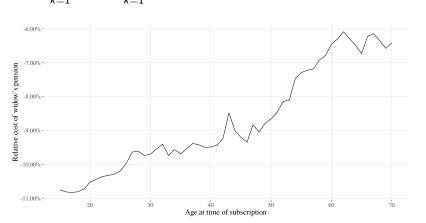


Figure 5: Widow's pension,  $a_{m|f}$  (relative to independent case  $a_{m|f}^{\perp}$ ).

#### Children-Parents

"inheritance of longevity" coined in Pearl (1931)

"the life spans of parents and children appear only weakly related, even though parents affect their children's longevity through both genetic and environmental influences" Vaupel (1988)

"the chance of reaching a high age is transmitted from parents to children in a modest, but robust way" Vågerö et al. (2018)

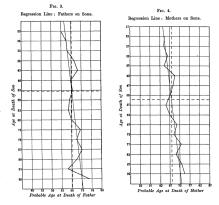


Figure 6: Son vs. parents Beeton and Pearson (1901).

#### Children-Parents

### Beeton and Pearson (1901), regression of $T_{x_c}$ given $T_{x_f}$ or $T_{x_m}$

slope: Daughter-mother 0.1968 [0.1910,0.20260] Son-mother 0.1791 [0.1737,0.18443] Daughter-father 0.1186 [0.1122,0.12507] Son-father 0.1197 [0.1138, 0.12567]

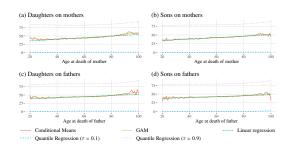


Figure 7: Age of the children given information relative to the parents.

#### Children-Parents

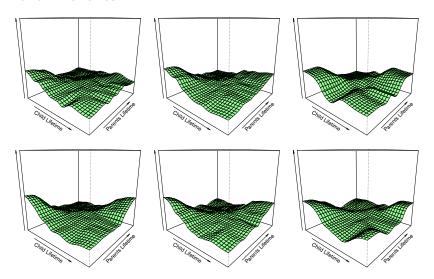


Figure 8: Copula density, children and father/mother/min/max.

# Children-Parents, life expectancy

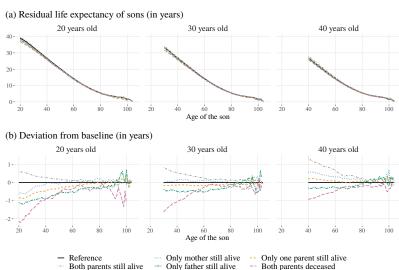


Figure 9: Residual life expectancy  $e_x$  with information about parents at age 20, 30 or 40.

### Children-Parents, annuities and insurance

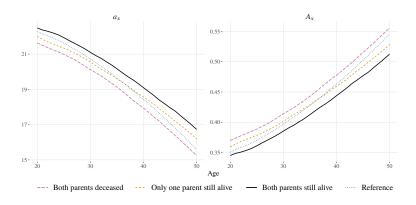


Figure 10: Annuity  $a_x$  and whole life insurance  $A_x$ , given information about the number of parents still alive, when child has age x.

### Children-Parents, annuities and insurance

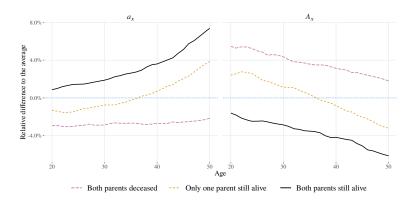


Figure 11: Annuity  $a_x$  and whole life insurance  $A_x$ , given information about the number of parents still alive, when child has age x (relative difference).

## Children-Grandparents

won Emily Choi (2020), "little is known about whether and how intergenerational relationships influence older adult mortality"

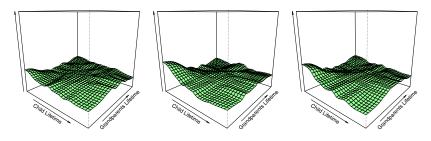


Figure 12: Copula density, children and grandparents min/max/mean.

# Children-Grandparents, life expectancy

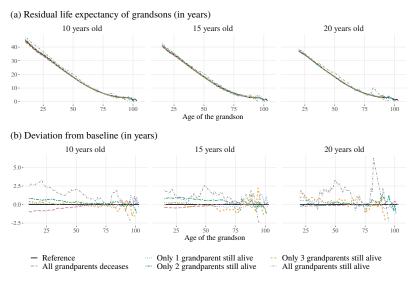


Figure 13: Residual life expectancy  $e_x$  with information about grandparents, at age 10, 15 or 20.

## Children-Grandparents, annuities and insurance

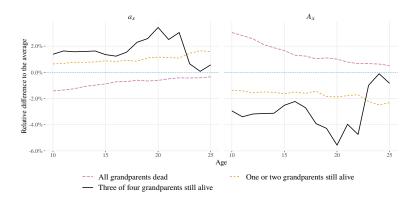


Figure 14: Annuity  $a_x$  and whole life insurance  $A_x$ , given information about the number of grandparents still alive, when child has age x.

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