

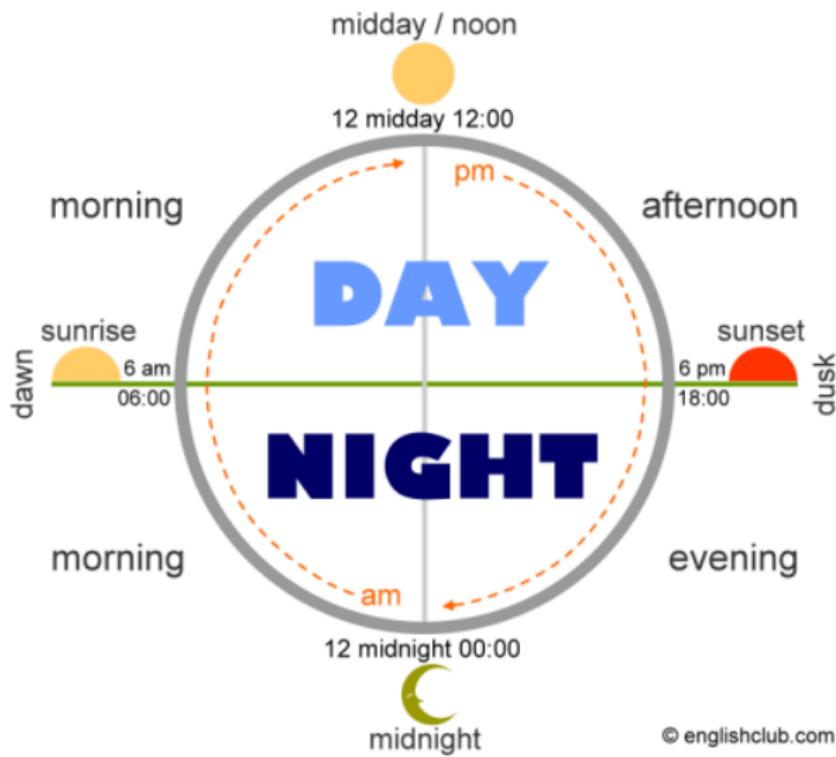
Field Regions and Power Patterns of Infinitesimal Dipole

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<http://dspandlinux.com>

June 28, 2012

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Antenna radiation zoning

Infinitesimal Dipole ($I \ll \lambda$)

- Near-Field ($kr \ll 1$)
- Intermediate-Field ($kr > 1$)
- Far-Field ($kr \gg 1$)



Why ?

How ?

What ?

Outline

E

$$E_r = \eta \frac{l_0 / \cos \theta}{2\pi r^2} [1 + \frac{1}{jkr}] e^{-jkr}$$

$$E_\theta = j\eta \frac{k l_0 / \sin \theta}{4\pi r} [1 + \frac{1}{jkr} - \frac{1}{(kr)^2}] e^{-jkr}$$

$$E_\phi = 0$$

H

$$H_r = H_\theta = 0$$

$$H_\phi = j \frac{k l_0 / \sin \theta}{4\pi r} [1 + \frac{1}{jkr}] e^{-jkr}$$

Outline

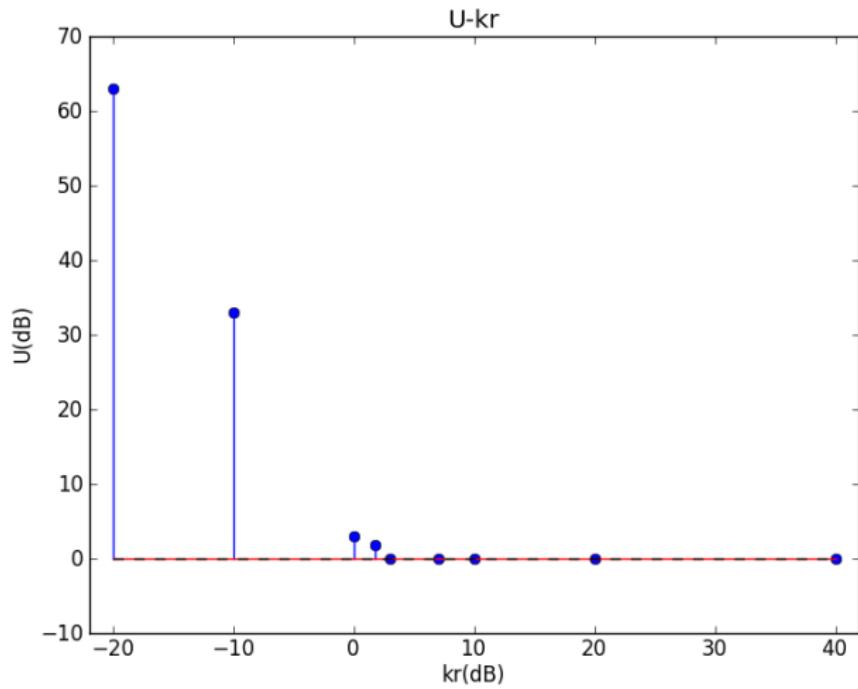
Poynting vector

$$\begin{aligned}\mathbf{W} &= \frac{1}{2}(\mathbf{E} \times \mathbf{H}^*) = \frac{1}{2}(\hat{\mathbf{a}}_r E_r + \hat{\mathbf{a}}_\theta E_\theta) \times (\hat{\mathbf{a}}_\phi H_\phi^*) \\ &= \frac{1}{2}(\hat{\mathbf{a}}_r E_\theta H_\phi^* - \hat{\mathbf{a}}_\phi E_r H_\phi^*)\end{aligned}$$

Power

$$\begin{aligned}P &= \frac{1}{2} \iint_s \mathbf{E} \times \mathbf{H}^* \cdot d\mathbf{s} = \eta\left(\frac{\pi}{3}\right) \left|\frac{I_0 l}{\lambda}\right|^2 \left[1 - j\frac{1}{(kr)^3}\right] \\ &= P_{rad} + j2\omega(\tilde{W}_m - \tilde{W}_e)\end{aligned}$$

Outline



Near-Field Region

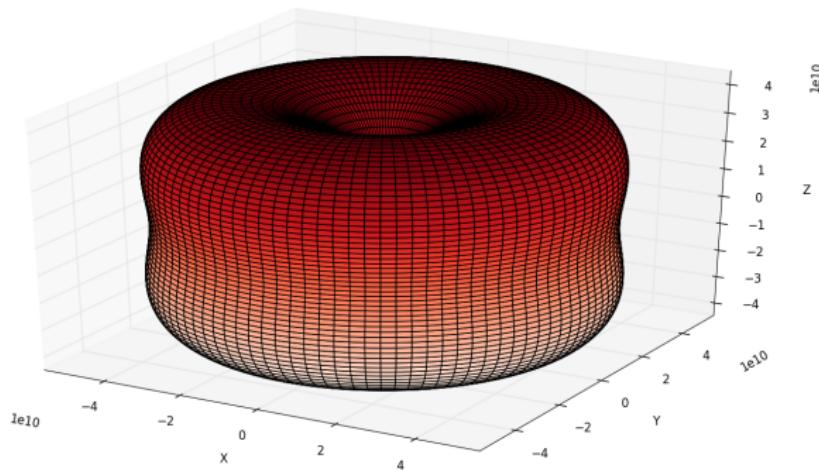
$$\left. \begin{array}{l} E_r \simeq -j\eta \frac{I_0 I e^{-jkr}}{2\pi kr^3} \cos \theta \\ E_\theta \simeq -j\eta \frac{I_0 I e^{-jkr}}{1\pi kr^3} \sin \theta \\ E_\phi = H_r = H_\theta = 0 \\ H_\phi \simeq \frac{I_0 I e^{-jkr}}{4\pi r^2} \sin \theta \end{array} \right\} \quad kr \ll 1 \quad (1)$$

if $f = 10GHz, kr = 0.1$, then

$$k = \frac{2\pi}{\lambda} = \frac{2\pi f}{c} \simeq 209.4$$

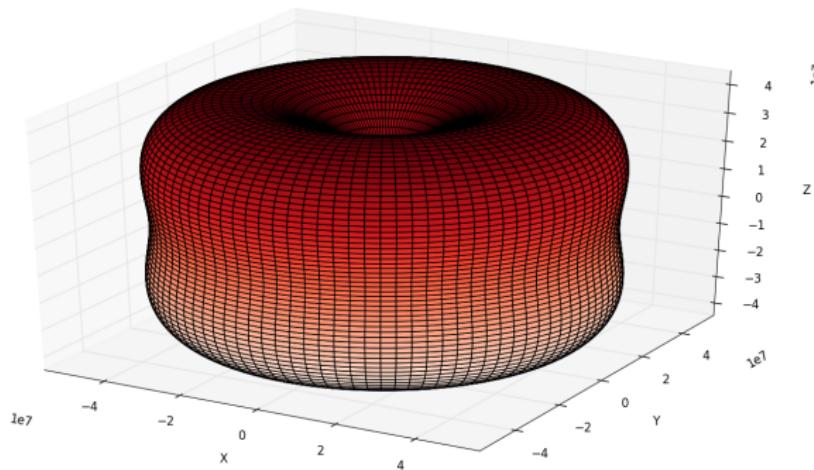
$$\text{so } r = 0.000477m$$

Patten of Near-Field Region



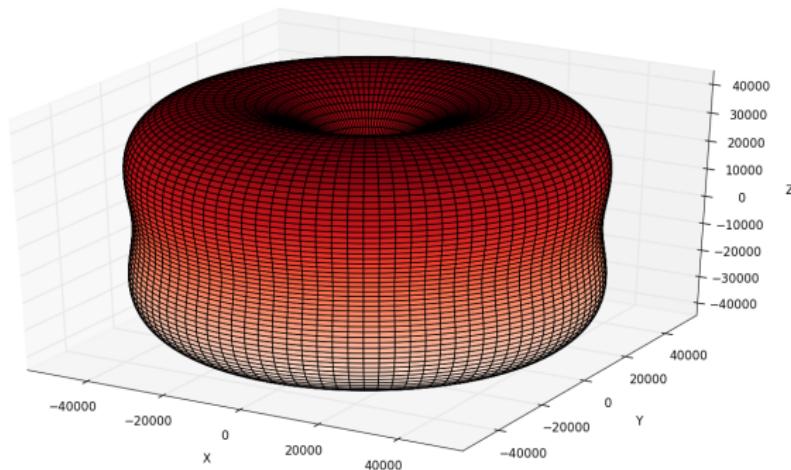
$$kr=0.01$$

Patten of Near-Field Region



$$kr=0.1$$

Patten of Near-Field Region

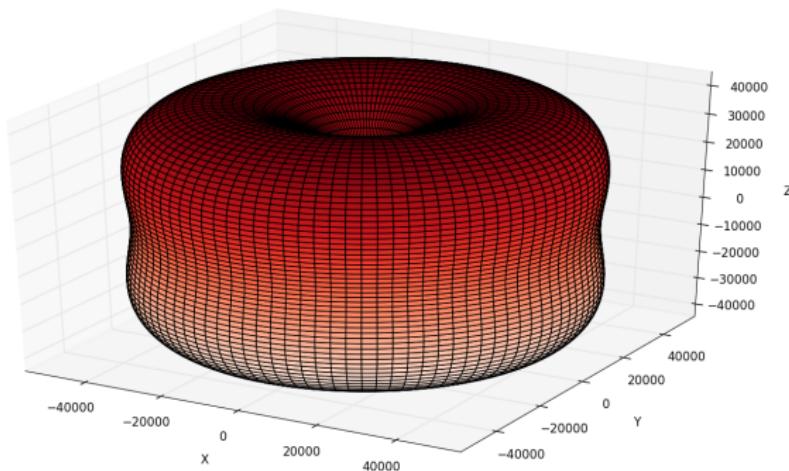


$kr=1$

Patten of Intermediate-Field Region

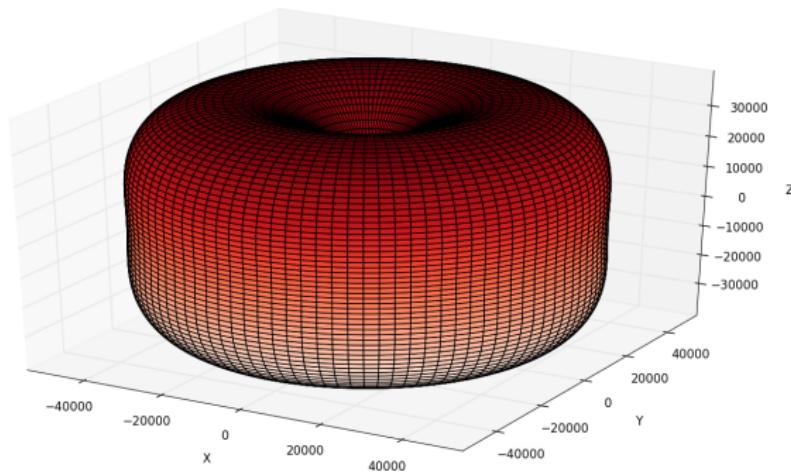
$$\left. \begin{array}{l} E_r \simeq \eta \frac{I_0 l e^{-jkr}}{1\pi r^1} \cos \theta \\ E_\theta \simeq j\eta \frac{k I_0 l e^{-jkr}}{4\pi r} \sin \theta \\ E_\phi = H_r = H_\theta = 0 \\ H_\phi \simeq j \frac{k I_0 l e^{-jkr}}{4\pi r} \sin \theta \end{array} \right\} kr > 1 \quad (2)$$

Patten of Intermediate-Field Region



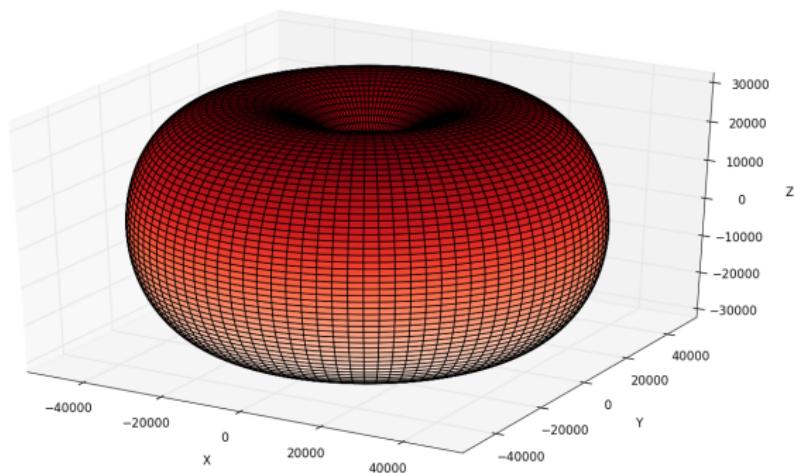
$$kr=1$$

Patten of Intermediate-Field Region



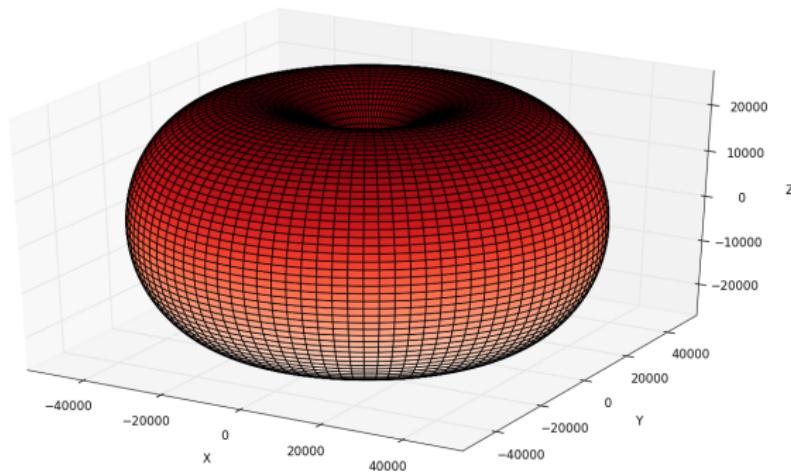
$kr=1.1$

Patten of Intermediate-Field Region



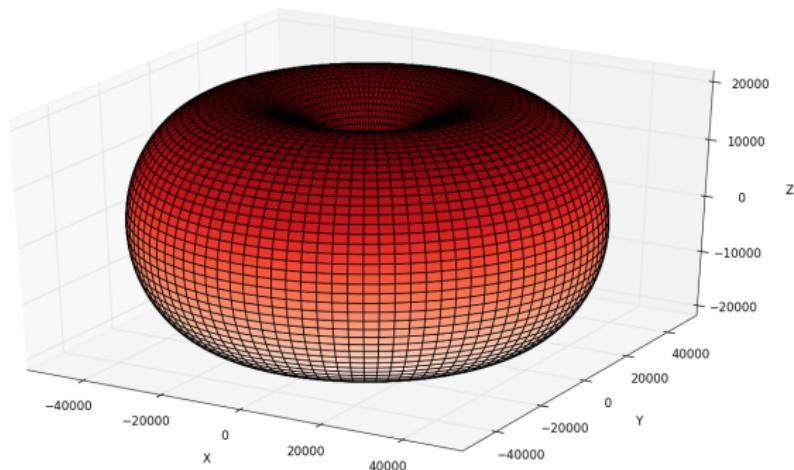
$$kr=1.5$$

Patten of Intermediate-Field Region



$kr=2$

Patten of Intermediate-Field Region

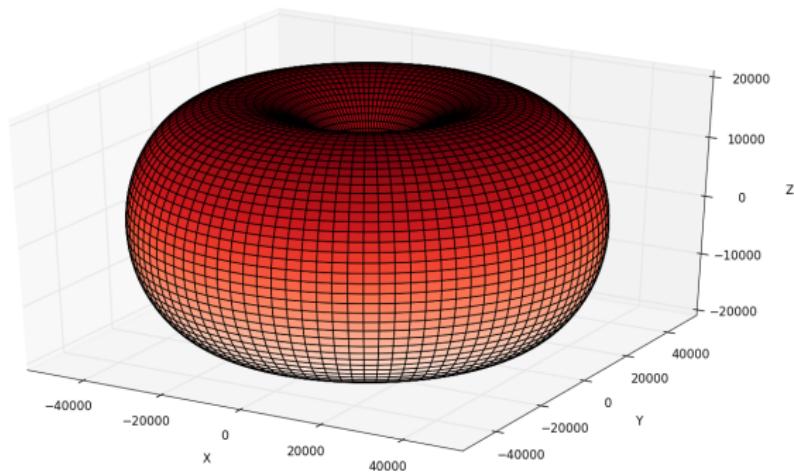


$kr=5$

Far-Field Region

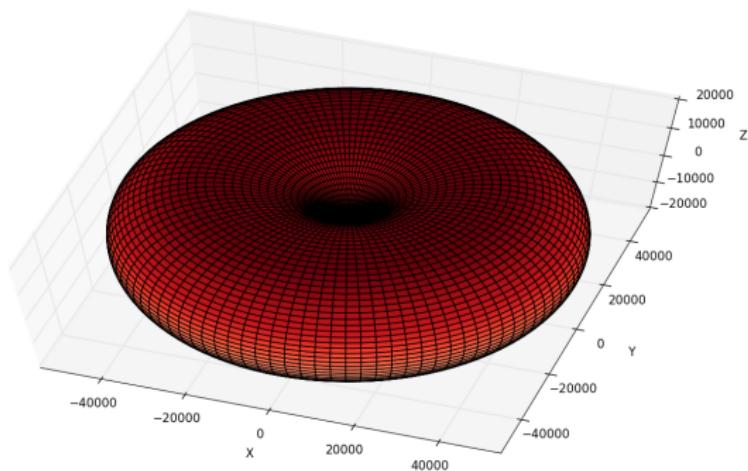
$$\left. \begin{array}{l} E_\theta \simeq j\eta k \frac{I_0 l e^{-jkr}}{4\pi r} \sin \theta \\ E_r = E_\phi = H_r = H_\theta = 0 \\ H_\phi \simeq j \frac{k l_0 l e^{-jkr}}{4\pi r} \sin \theta \end{array} \right\} kr \gg 1 \quad (3)$$

Patten of Far-Field Region



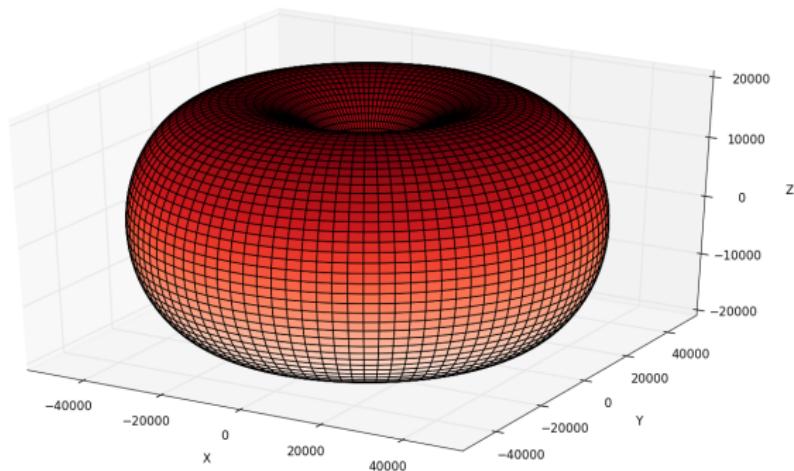
$kr=10$

Patten of Far-Field Region



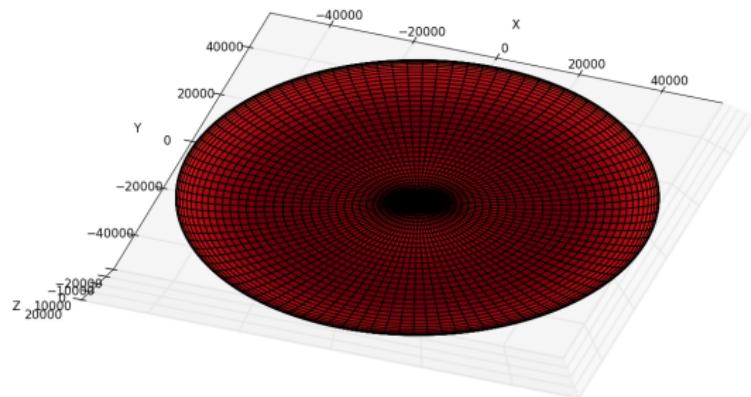
$kr=10$

Patten of Far-Field Region



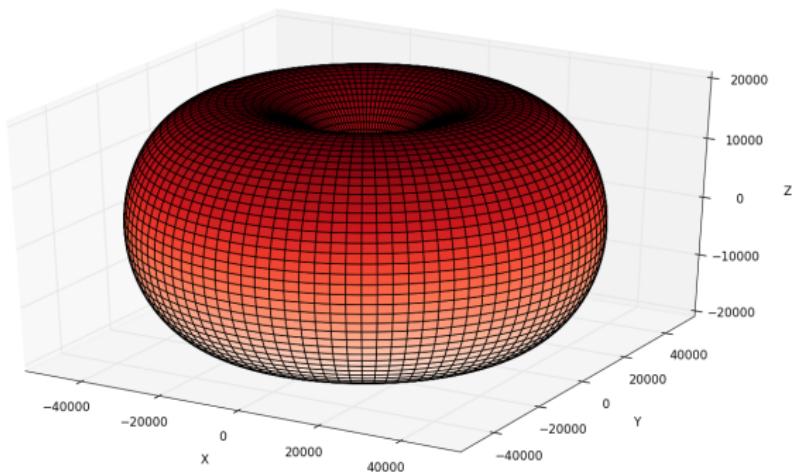
$kr=100$

Patten of Far-Field Region



$kr=100$

Patten of Far-Field Region



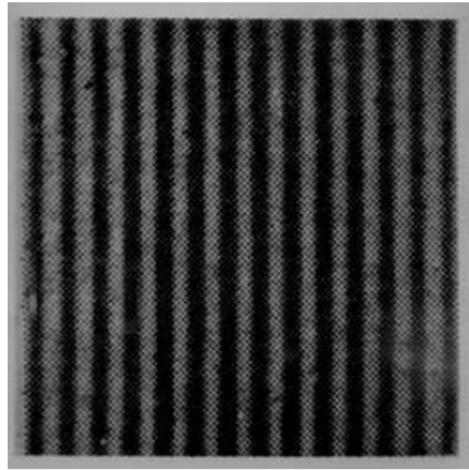
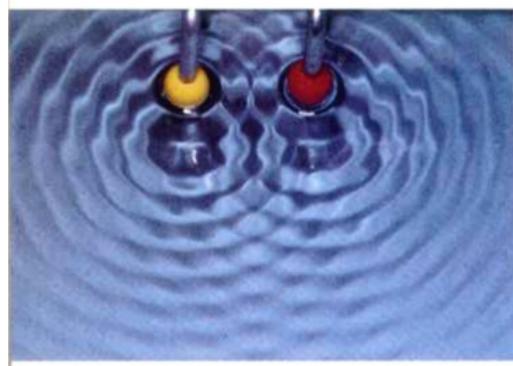
$kr=10000$

flapdoodle

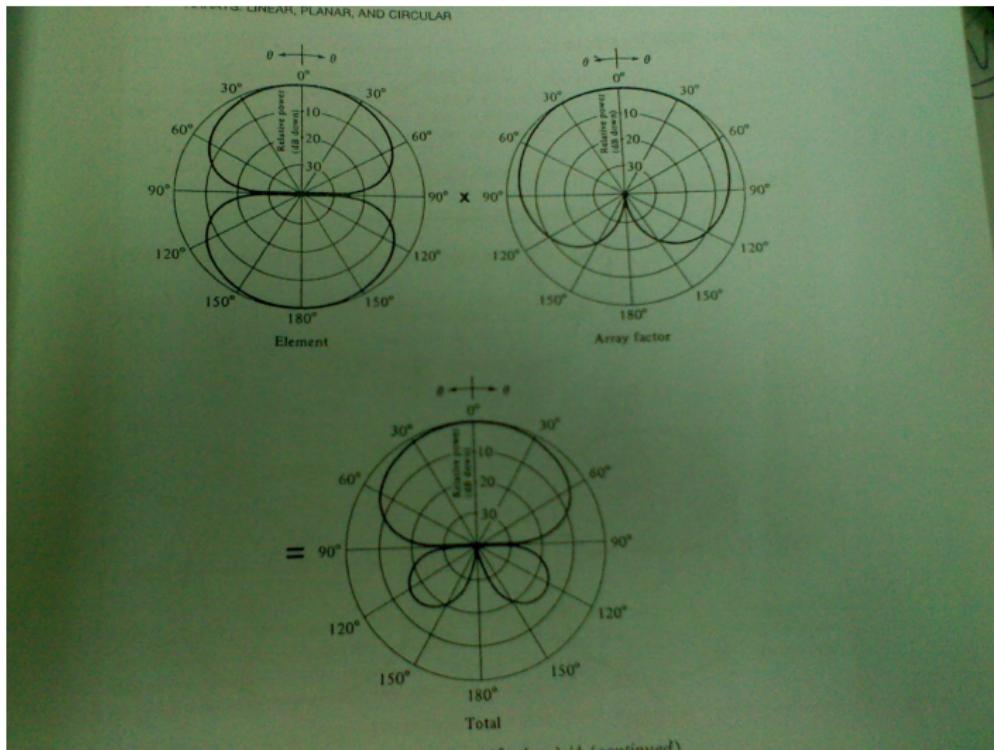


Sidelobe

Interference \Rightarrow Sidelobe



Array Factor



Fourier transform

A

$$\mathbf{A}(x, y, z) = \frac{\mu}{4\pi} \int_C \mathbf{l}_e(x', y', z') \frac{e^{-jkR}}{R} dl'$$

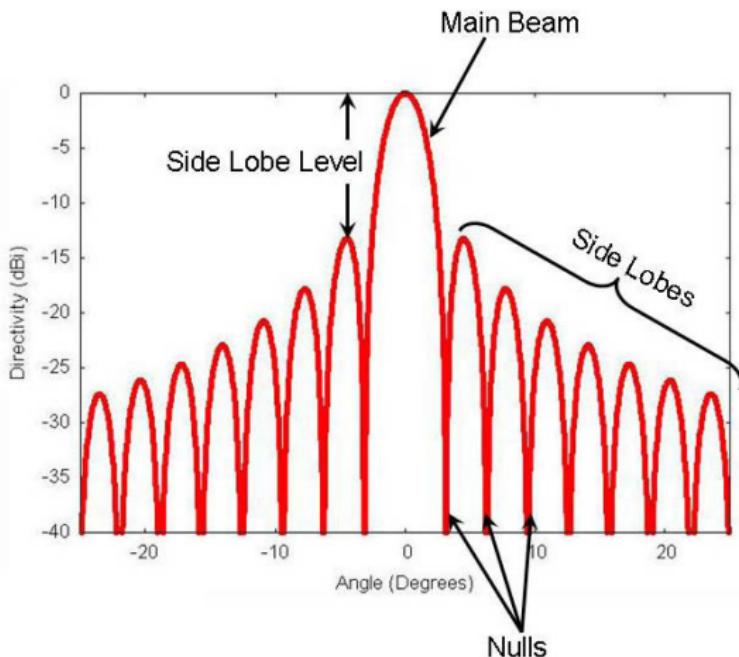
$$R \simeq r - z' \cos \theta$$



E_θ

$$E_\theta = \int_{-l/2}^{+l/2} dE_\theta = j\eta \frac{ke^{-jkr}}{4\pi r} \sin \theta \left[\int_{-l/2}^{+l/2} l_e(x', y', z') e^{j kz' \cos \theta} dz' \right]$$

$$\text{Radiation Pattern (in units of } dB) \propto 10 \log_{10} \left(\left| \frac{\sin X}{X} \right| \right)$$



a rectangular aperture antenna radiation pattern

Thank
You!