

Aggregated sampling output

November 20, 2020

Dataset: experimental_data_d2eGFP, model type: SDE

Trajectories without pathologies

e.g. no divergent transitions, no max_tredepth exceeded, no Rhat > 1.1, no n_eff < 100

number of trajectories without pathologies (out of 100):

[1] 63

indices of trajectories without pathologies:

```
[1]  1  2  4  5  6  7  9 10 11 12 15 17 18 20 21 22 23 25 26 27 28 29 30 31 32
[26] 34 37 38 39 41 42 44 45 46 52 55 57 58 61 63 65 66 69 70 71 73 74 75 77 78
[51] 80 81 82 83 85 86 91 92 95 96 97 98 99
```

no pathologies for a subset of the parameters

parameters considered:

```
[1] "theta[1]"          "theta[3]"          "sigma"
[4] "scale"             "offset"            "prod_theta2_m0"
[7] "prod_theta2_m0_scale"
```

number of trajectories without pathologies (out of 100):

[1] 84

indices of trajectories without pathologies:

```
[1]  1  2  3  4  5  6  7  9 10 11 12 13 14 15 17 18 19 20 21 22 23 24 25 26 27
[26] 28 29 30 31 32 34 37 38 39 40 41 42 43 44 45 46 47 48 49 52 53 54 55 57 58
[51] 59 60 61 63 65 66 67 69 70 71 72 73 74 75 77 78 80 81 82 83 85 86 88 89 90
[76] 91 92 93 94 95 96 97 98 99
```

Divergent transitions

| num..of.div..transitions | Freq |
|--------------------------|------|
| 0 | 90 |
| 8 | 2 |
| 10 | 1 |
| 14 | 1 |
| 20 | 1 |
| 22 | 1 |
| 30 | 1 |
| 41 | 1 |
| 72 | 1 |
| 540 | 1 |

total number of trajectories with div. transitions: 10
indices of trajectories with div. transitions:
16 33 35 36 50 56 76 79 87 100

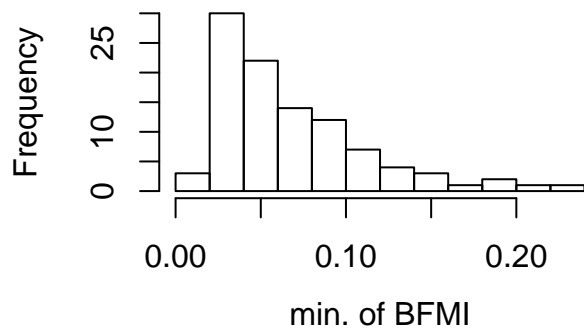
Maximum tree depth exceeded

| num..of.max.t.d..exceeded | Freq |
|---------------------------|------|
| 0 | 95 |
| 1 | 1 |
| 10 | 1 |
| 20 | 1 |
| 21 | 1 |
| 59 | 1 |

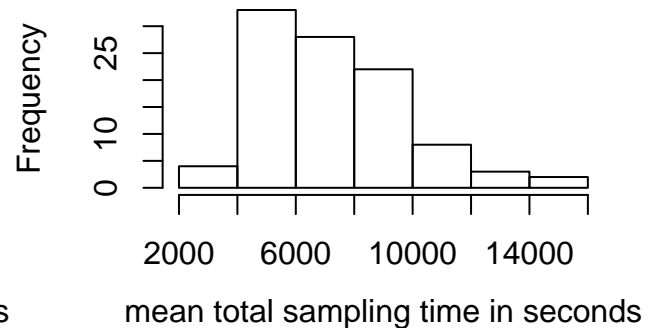
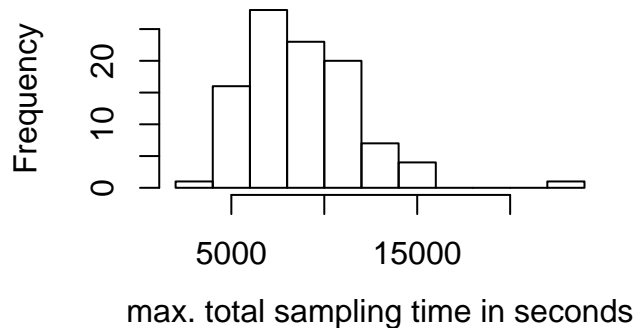
total number of trajectories were max. tree depth was exceeded: 5
indices of trajectories were max. tree depth was exceeded:
8 35 51 62 68

Bayesian fraction of missing information (BFMI)

| num..of.low.BFMI | Freq |
|------------------|------|
| 0 | 2 |
| 1 | 3 |
| 3 | 1 |
| 5 | 1 |
| 6 | 2 |
| 7 | 1 |
| 8 | 90 |



Total sampling time



R-hat

total number of trajectories with very high Rhat (> 1.1) (out of 100)

[1] 25

number of trajectories with high Rhat per parameter (out of 100)

| | Rhat > 1.02 | Rhat > 1.1 |
|----------------------|---------------|--------------|
| theta[1] | 28 | 1 |
| theta[2] | 46 | 2 |
| theta[3] | 46 | 1 |
| m0 | 65 | 18 |
| sigma | 1 | 0 |
| scale | 52 | 1 |
| offset | 0 | 0 |
| prod_theta2_m0 | 49 | 2 |
| prod_theta2_scale | 63 | 1 |
| prod_m0_scale | 57 | 11 |
| prod_theta2_m0_scale | 8 | 0 |
| x[180,1] | 73 | 23 |
| x[180,2] | 56 | 2 |

number of parameters with high Rhat per trajectory (out of 13)

| | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 13 | 14 | 15 | 16 | 17 | 19 | 22 | 23 | 24 | 25 | 28 |
|---------------|---|---|---|----|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|
| Rhat > 1.02 | 8 | 5 | 3 | 10 | 1 | 5 | 9 | 8 | 4 | 9 | 5 | 7 | 6 | 3 | 8 | 3 | 4 | 5 | 6 | 3 |
| Rhat > 1.1 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 0 | 0 | 3 | 3 | 0 | 3 | 0 | 2 | 0 | 0 | 0 | 0 | 0 |

| | 29 | 32 | 33 | 34 | 35 | 36 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 |
|---------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Rhat > 1.02 | 3 | 4 | 10 | 8 | 9 | 3 | 4 | 10 | 3 | 6 | 9 | 9 | 1 | 2 | 7 | 9 | 10 | 9 | 8 | 5 |
| Rhat > 1.1 | 0 | 0 | 0 | 0 | 3 | 0 | 0 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 3 | 1 | 3 | 0 | 0 |

| | 53 | 54 | 55 | 56 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 71 | 72 | 75 | 76 |
|---------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Rhat > 1.02 | 10 | 9 | 5 | 9 | 2 | 10 | 7 | 5 | 10 | 8 | 11 | 7 | 7 | 11 | 2 | 6 | 2 | 10 | 5 | 7 |
| Rhat > 1.1 | 0 | 0 | 0 | 3 | 0 | 2 | 2 | 0 | 3 | 0 | 7 | 0 | 0 | 3 | 0 | 0 | 0 | 1 | 0 | 0 |

| | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 |
|---------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Rhat > 1.02 | 5 | 10 | 6 | 4 | 8 | 3 | 8 | 10 | 3 | 5 | 8 | 7 | 10 | 9 | 8 | 5 | 7 | 10 | 3 | 5 |
| Rhat > 1.1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 2 | 0 | 0 | 1 | 0 | 0 | 2 | 3 | 0 | 0 |

theta[1]

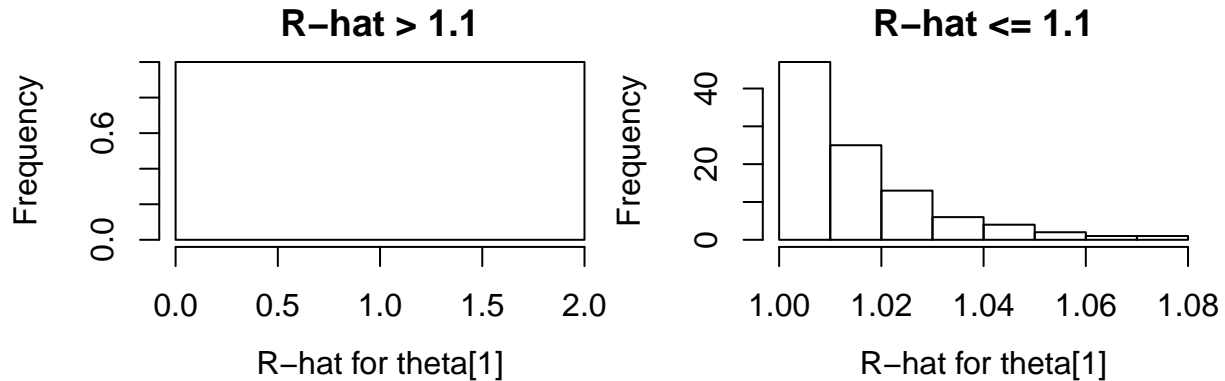
number of trajectories with Rhat > 1.02 : 28

indizes of trajectories with Rhat > 1.02 :

5 8 9 19 33 40 44 47 49 51 53 56 59 60 61 62 64 66 67 72 78 83 84 89 93 96 97 100

number of trajectories with $R_{\text{hat}} > 1.1$: 1

indices of trajectories with $R_{\text{hat}} > 1.1$:
64



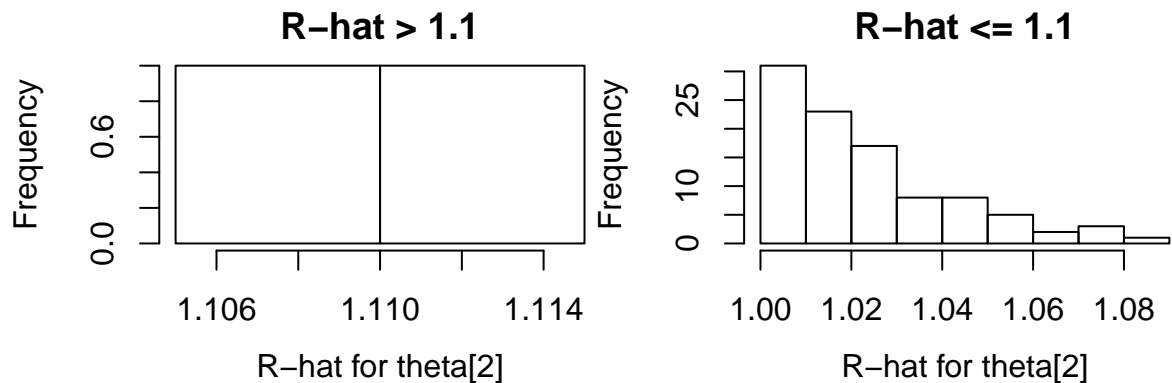
$\theta[2]$

number of trajectories with $R_{\text{hat}} > 1.02$: 46

indices of trajectories with $R_{\text{hat}} > 1.02$:
2 3 5 7 8 13 14 16 19 24 25 33 35 40 43 47 48 49 50 51 53 54 55 56 59 60 62 63 64 67 69 72 76 77 78 79 8

number of trajectories with $R_{\text{hat}} > 1.1$: 2

indices of trajectories with $R_{\text{hat}} > 1.1$:
64 100



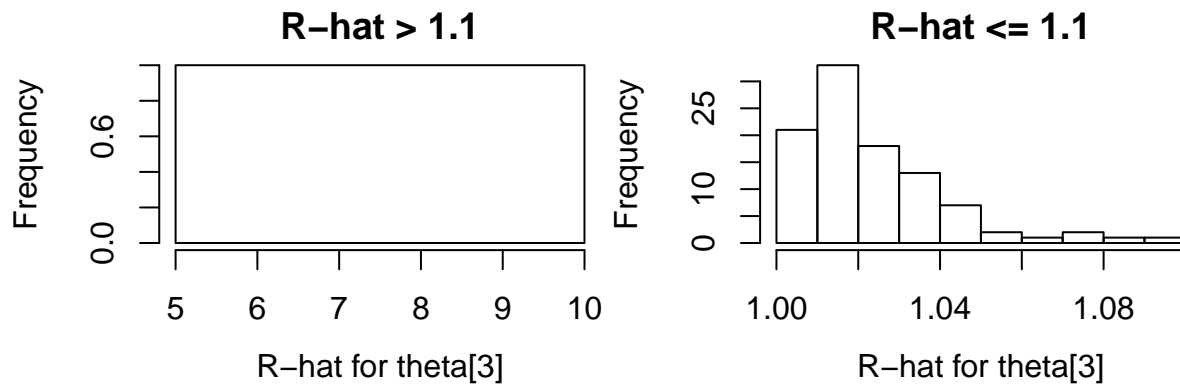
$\theta[3]$

number of trajectories with $R_{\text{hat}} > 1.02$: 46

indices of trajectories with $R_{\text{hat}} > 1.02$:
5 6 8 9 15 19 22 23 33 34 35 40 43 44 47 49 51 53 54 56 59 60 61 62 63 64 65 66 67 68 69 72 78 83 84 86

number of trajectories with $R_{\text{hat}} > 1.1$: 1

indices of trajectories with $R_{\text{hat}} > 1.1$:
64



m0

number of trajectories with Rhat > 1.02: 65

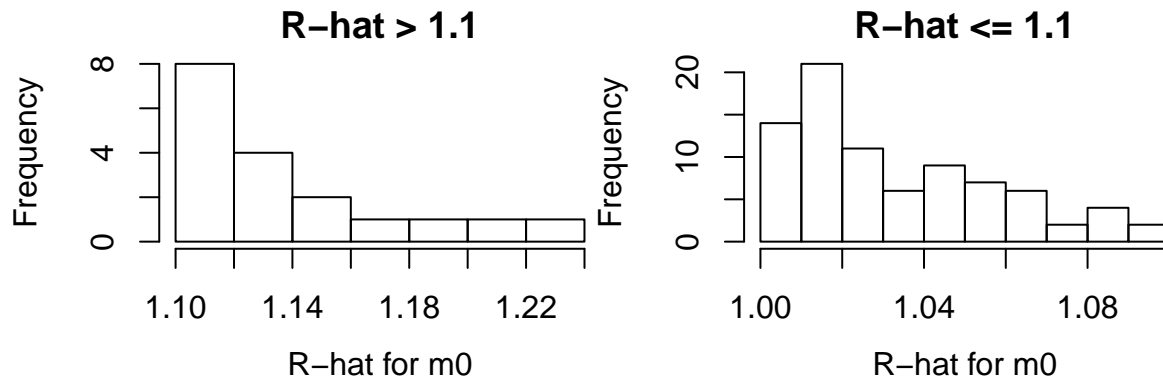
indices of trajectories with Rhat > 1.02:

2 3 4 5 7 8 9 13 14 15 16 19 22 23 24 28 33 34 35 36 40 42 43 44 47 48 49 50 51 52 53 54 55 56 58 59 60

number of trajectories with Rhat > 1.1: 18

indices of trajectories with Rhat > 1.1:

3 13 14 16 19 35 40 48 50 56 59 60 62 67 87 93 94 100

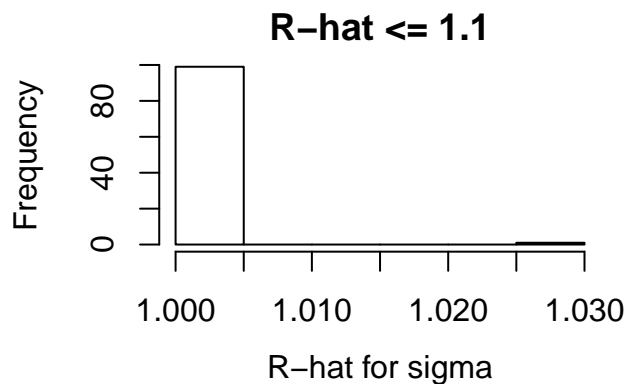


sigma

number of trajectories with Rhat > 1.02: 1

indices of trajectories with Rhat > 1.02:

64



scale

number of trajectories with $R_{\text{hat}} > 1.02$: 52

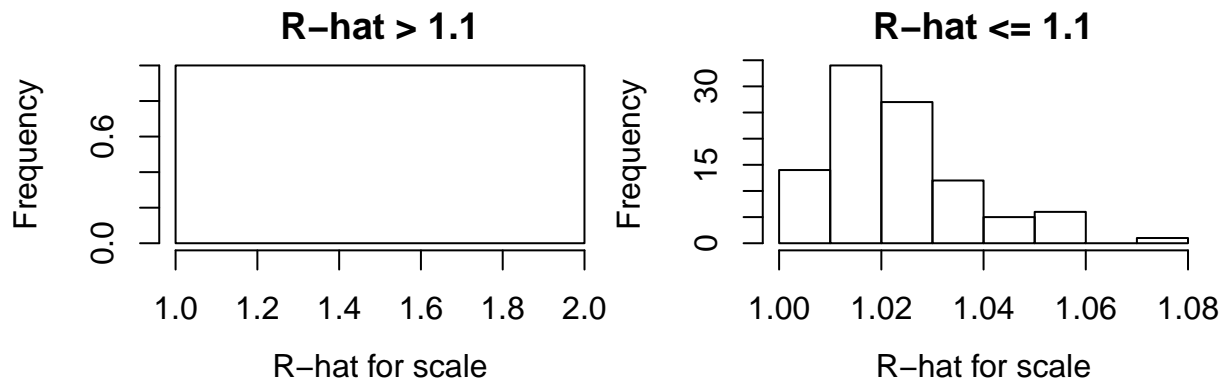
indices of trajectories with $R_{\text{hat}} > 1.02$:

2 5 8 9 10 13 15 16 17 19 25 29 32 33 34 35 39 40 41 43 44 45 48 49 50 51 52 53 54 56 59 62 63 64 65 66

number of trajectories with $R_{\text{hat}} > 1.1$: 1

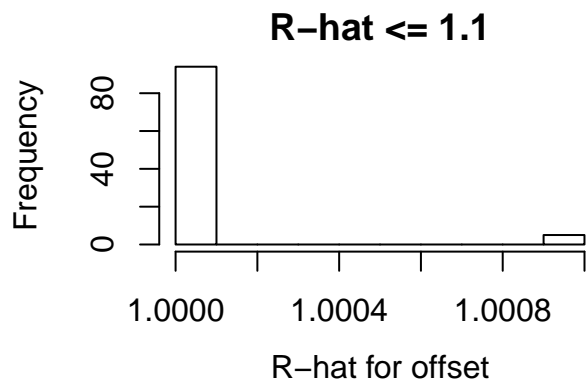
indices of trajectories with $R_{\text{hat}} > 1.1$:

64



offset

no $R_{\text{hat}} > 1.02$



prod_theta2_m0

number of trajectories with $R_{\text{hat}} > 1.02$: 49

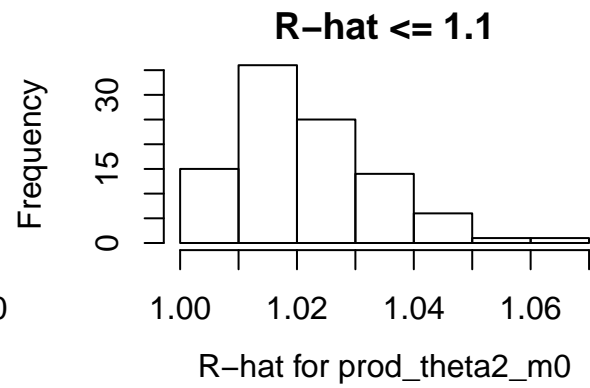
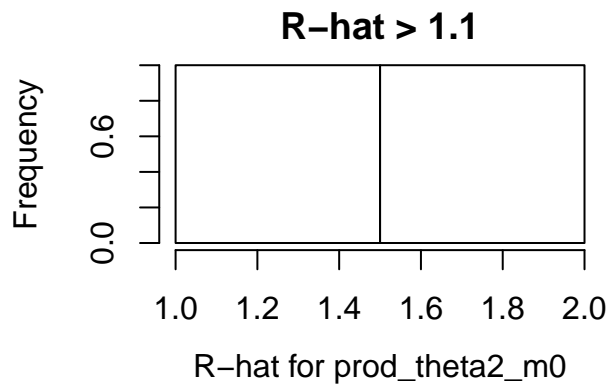
indices of trajectories with $R_{\text{hat}} > 1.02$:

2 5 8 9 10 13 15 17 25 29 32 33 34 39 40 41 42 43 44 46 48 49 50 53 54 59 61 62 64 65 66 67 72 75 78 80

number of trajectories with $R_{\text{hat}} > 1.1$: 2

indices of trajectories with $R_{\text{hat}} > 1.1$:

8 64



prod_theta2_scale

number of trajectories with Rhat > 1.02: 63

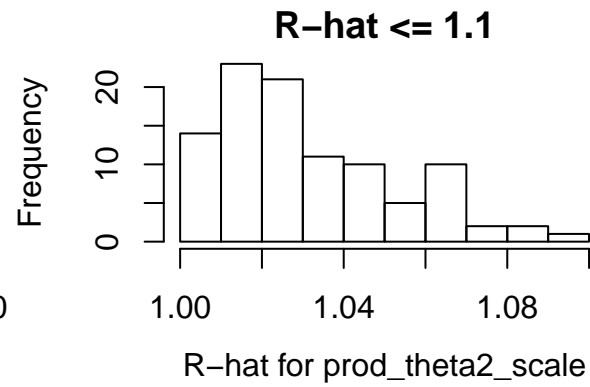
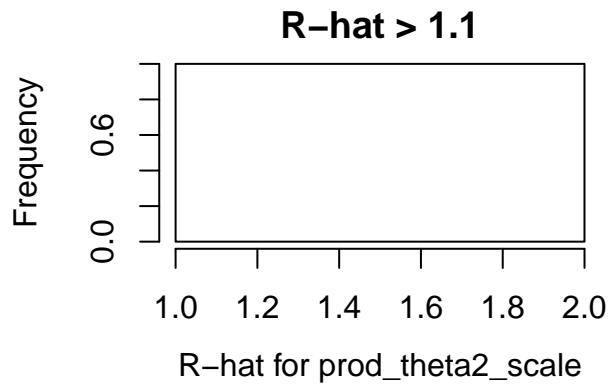
indices of trajectories with Rhat > 1.02:

2 3 5 7 8 13 14 15 16 19 23 24 32 33 34 35 40 42 43 44 47 48 49 50 51 52 53 54 55 56 59 60 62 63 64 65 6

number of trajectories with Rhat > 1.1: 1

indices of trajectories with Rhat > 1.1:

100



prod_m0_scale

number of trajectories with Rhat > 1.02: 57

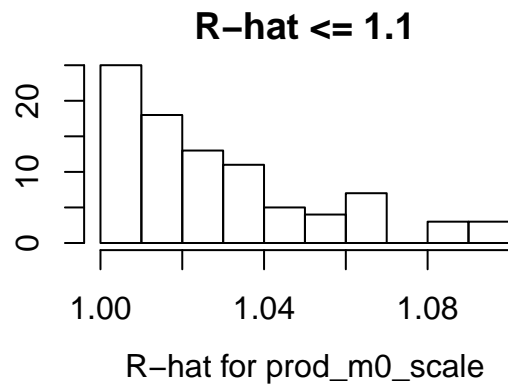
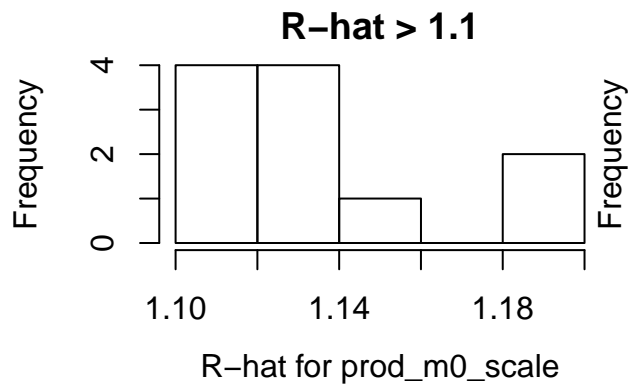
indices of trajectories with Rhat > 1.02:

2 3 4 5 7 9 13 14 16 19 24 25 28 33 34 35 36 39 40 42 43 44 47 48 49 50 51 52 53 54 55 56 59 60 62 63 64

number of trajectories with Rhat > 1.1: 11

indices of trajectories with Rhat > 1.1:

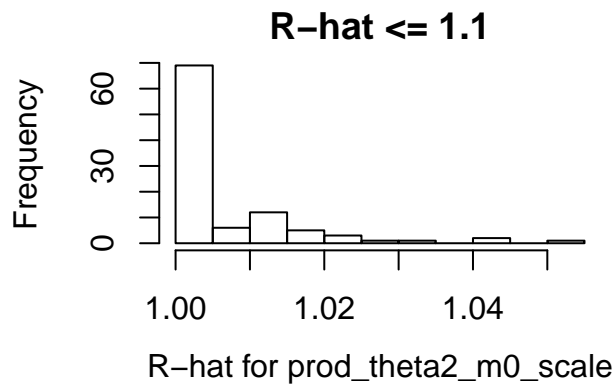
13 14 16 35 48 50 56 62 67 94 100



`prod_theta2_m0_scale`

number of trajectories with Rhat > 1.02: 8

indices of trajectories with Rhat > 1.02:
13 35 48 50 67 90 94 100



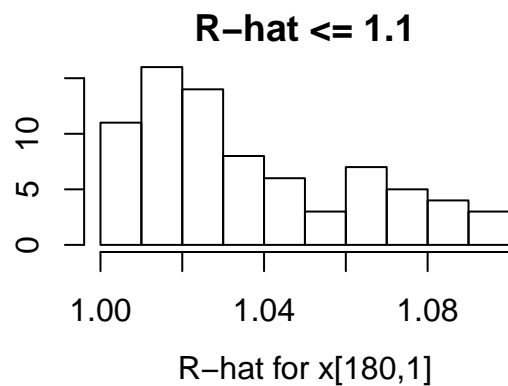
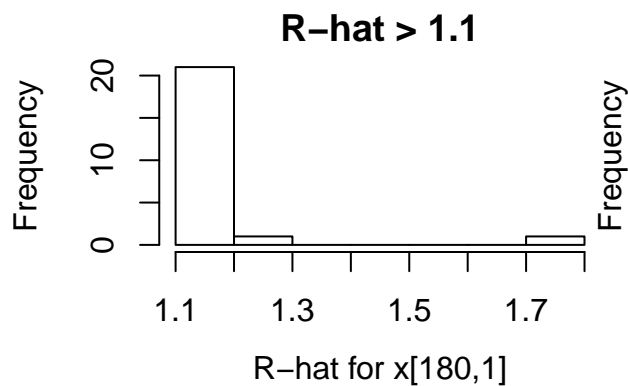
`x[180,1]`

number of trajectories with Rhat > 1.02: 73

indices of trajectories with Rhat > 1.02:
2 3 4 5 7 8 9 10 13 14 15 16 19 22 23 24 25 28 33 34 35 36 40 42 43 44 47 48 49 50 51 52 53 54 55 56 58

number of trajectories with Rhat > 1.1: 23

indices of trajectories with Rhat > 1.1:
13 14 16 19 35 40 47 48 49 50 56 59 60 62 64 67 72 84 87 90 93 94 100



x[180,2]

number of trajectories with Rhat > 1.02: 56

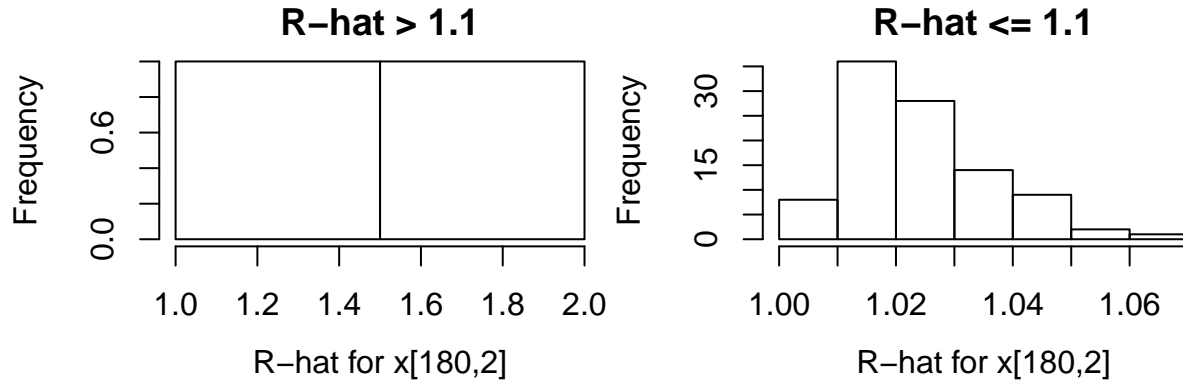
indices of trajectories with Rhat > 1.02:

2 5 8 9 10 13 15 17 25 29 32 33 34 35 39 40 41 42 43 44 46 48 49 50 53 54 56 59 61 62 63 64 65 66 67 71

number of trajectories with Rhat > 1.1: 2

indices of trajectories with Rhat > 1.1:

8 64



Effective sample size (ESS)

total number of trajectories with low ESS (< 100) (out of 100)

[1] 31

number of trajectories with low ESS (< 100) per parameter (out of 100)

| | n_eff < 100 |
|----------------------|-------------|
| theta[1] | 1 |
| theta[2] | 2 |
| theta[3] | 2 |
| m0 | 22 |
| sigma | 0 |
| scale | 1 |
| offset | 0 |
| prod_theta2_m0 | 2 |
| prod_theta2_scale | 4 |
| prod_m0_scale | 16 |
| prod_theta2_m0_scale | 0 |
| x[180,1] | 29 |
| x[180,2] | 2 |

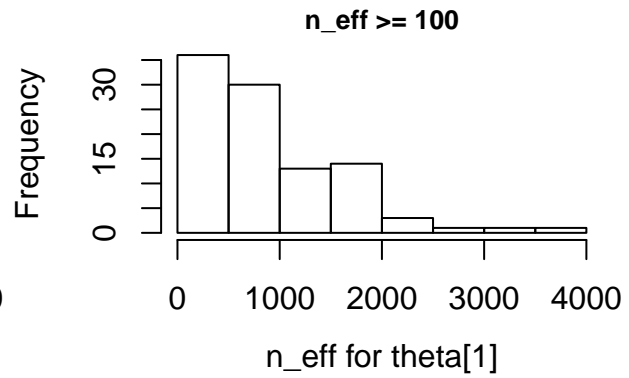
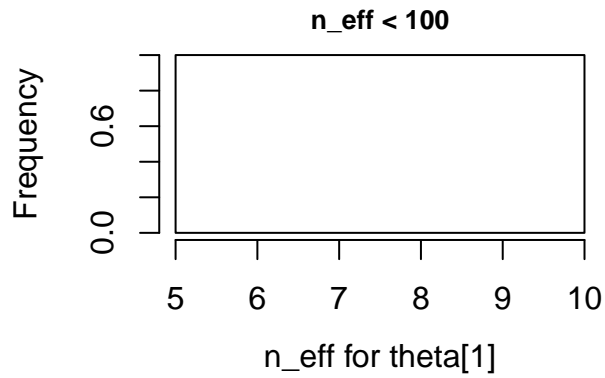
number of parameters with low ESS (< 300) per trajectory (out of 13)

| | 8 | 13 | 14 | 16 | 19 | 24 | 35 | 40 | 43 | 47 | 48 | 49 | 50 | 53 | 54 | 56 | 59 | 60 | 62 | 64 |
|-------------|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| n_eff < 100 | 3 | 3 | 3 | 3 | 2 | 1 | 3 | 3 | 3 | 1 | 3 | 2 | 3 | 1 | 1 | 3 | 3 | 2 | 3 | 7 |

`theta[1]`

number of trajectories with `n_eff < 100`: 1

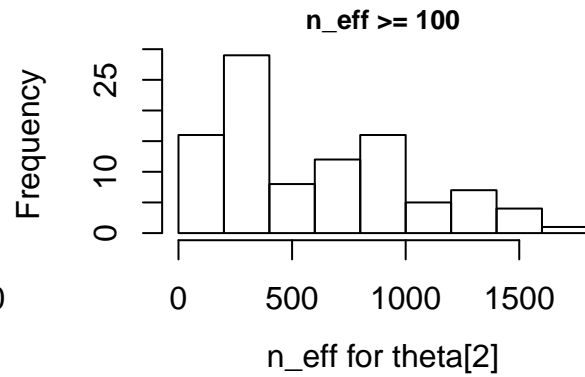
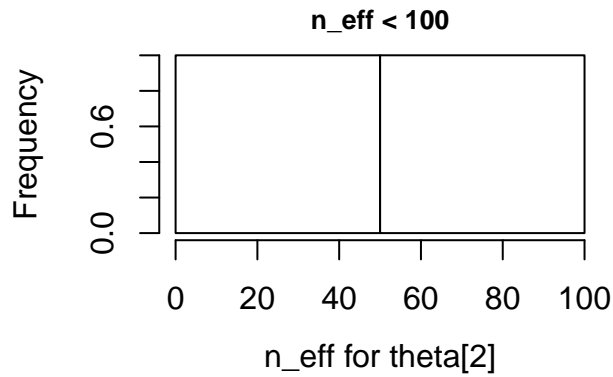
indices of trajectories with `n_eff < 100`:
64



`theta[2]`

number of trajectories with `n_eff < 100`: 2

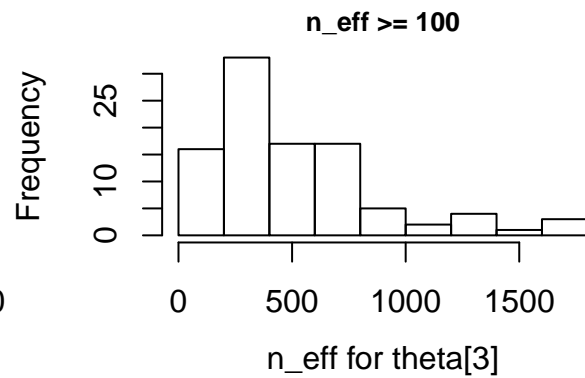
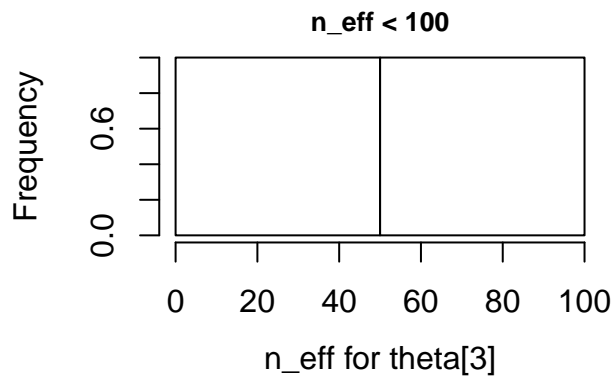
indices of trajectories with `n_eff < 100`:
64 100



`theta[3]`

number of trajectories with `n_eff < 100`: 2

indices of trajectories with `n_eff < 100`:
64 84

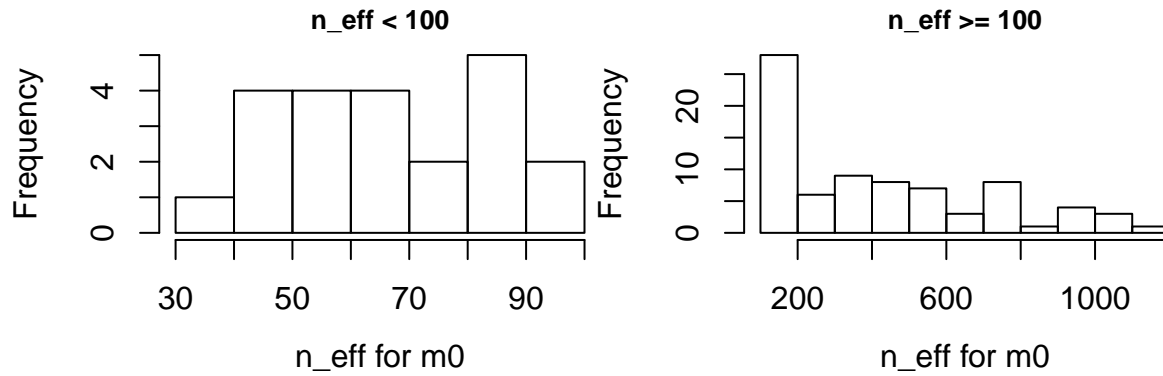


m0

number of trajectories with $n_{\text{eff}} < 100$: 22

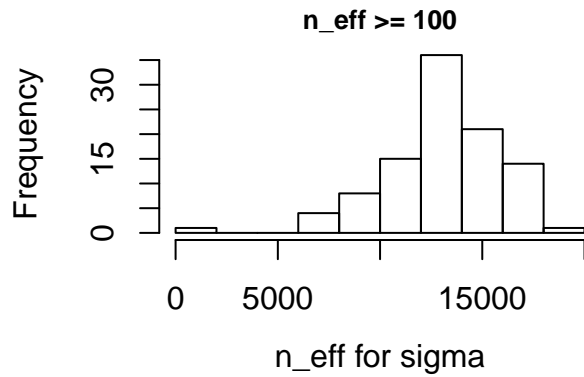
indices of trajectories with $n_{\text{eff}} < 100$:

13 14 16 19 35 40 43 48 49 50 56 59 60 62 67 76 79 87 88 90 93 100



sigma

no $n_{\text{eff}} < 100$

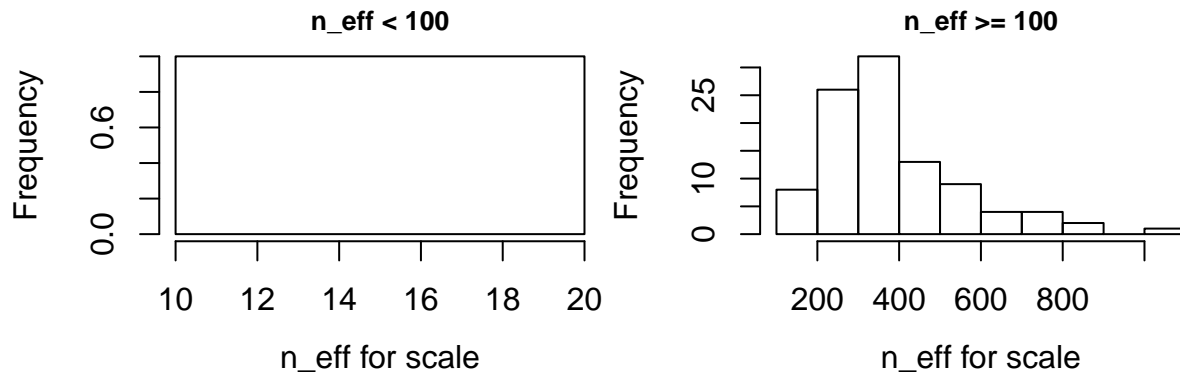


scale

number of trajectories with $n_{\text{eff}} < 100$: 1

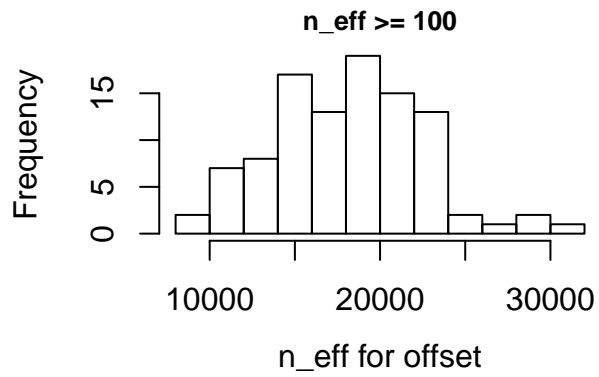
indices of trajectories with $n_{\text{eff}} < 100$:

64



offset

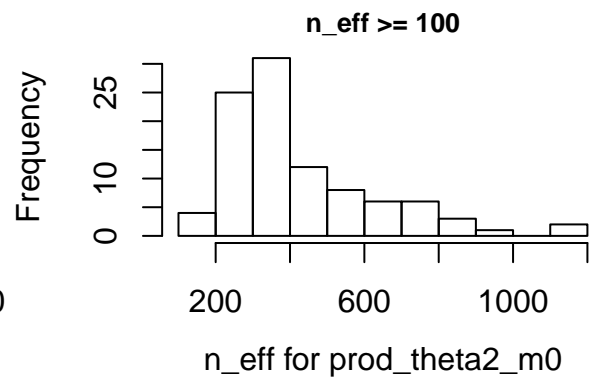
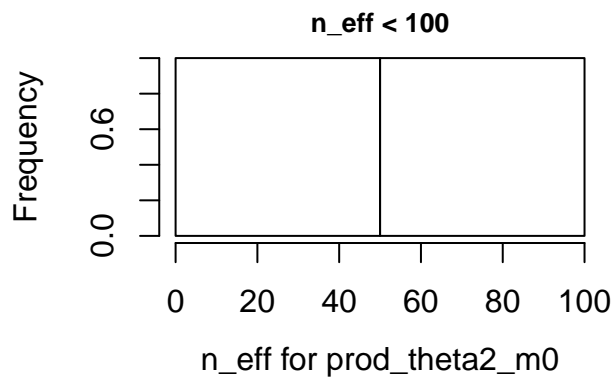
no $n_{\text{eff}} < 100$



prod_theta2_m0

number of trajectories with $n_{\text{eff}} < 100$: 2

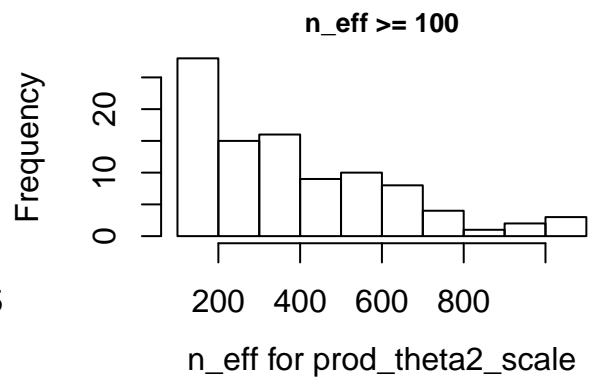
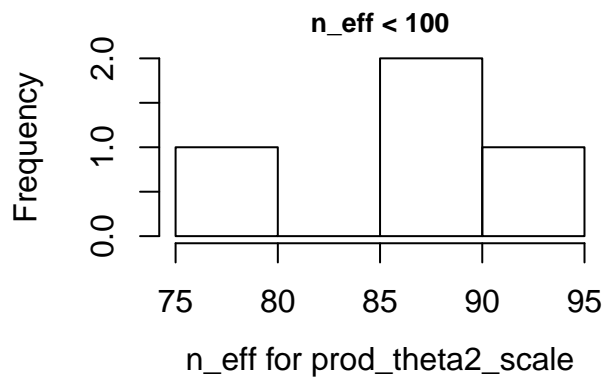
indices of trajectories with $n_{\text{eff}} < 100$:
8 64



prod_theta2_scale

number of trajectories with $n_{\text{eff}} < 100$: 4

indices of trajectories with $n_{\text{eff}} < 100$:
8 43 87 100

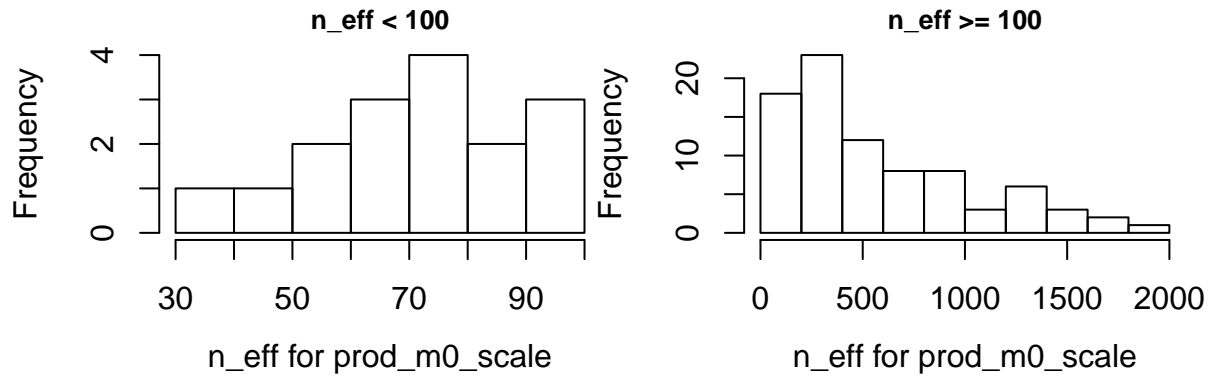


prod_m0_scale

number of trajectories with n_eff < 100: 16

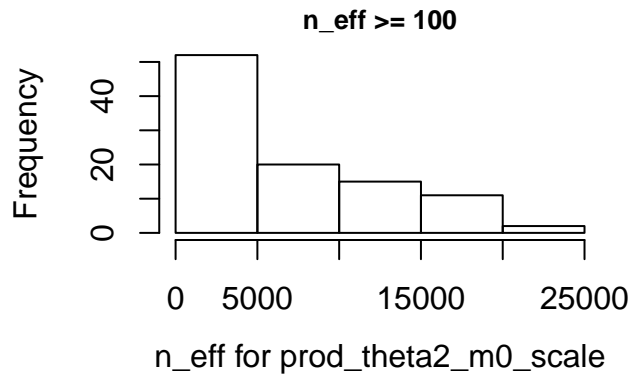
indices of trajectories with n_eff < 100:

13 14 16 35 40 48 50 56 59 62 67 76 79 87 93 100



prod_theta2_m0_scale

no n_eff < 100

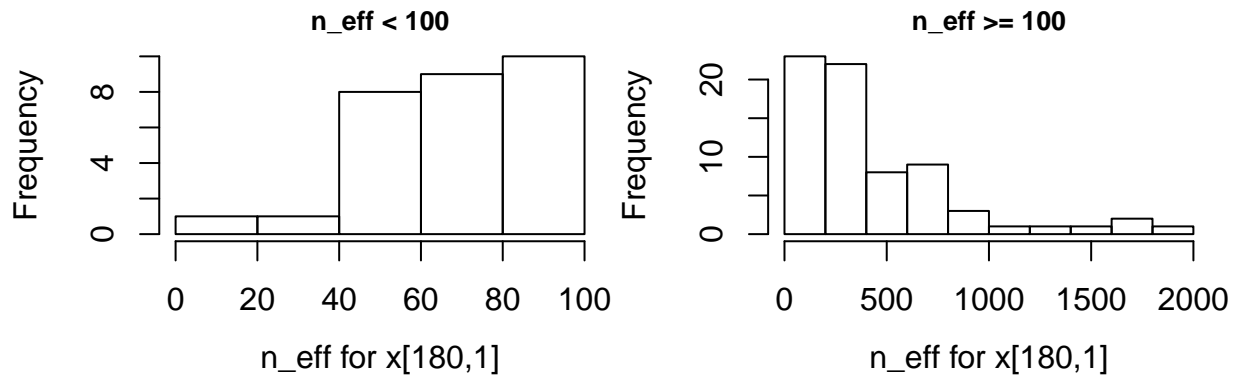


x[180,1]

number of trajectories with n_eff < 100: 29

indices of trajectories with n_eff < 100:

13 14 16 19 24 35 40 43 47 48 49 50 53 54 56 59 60 62 64 67 72 79 84 87 88 89 90 93 100

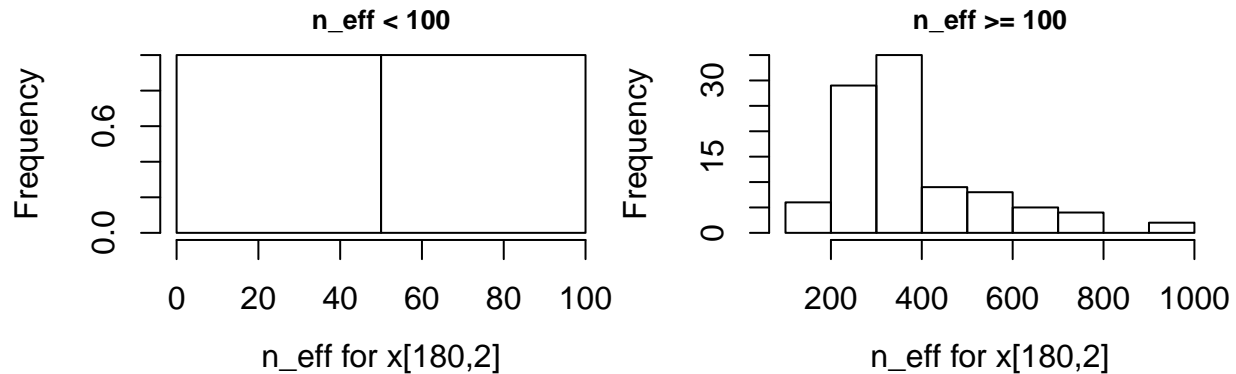


```
x[180,2]
```

```
number of trajectories with n_eff < 100:    2
```

```
indices of trajectories with n_eff < 100:
```

```
8 64
```



Find problematic trajectories and parameters

Are there any trajectories and parameters for which `n_eff` is below the threshold, but `Rhat` does not exceed the threshold?

```
## [1] FALSE
```

parameters per trajectories with very high `Rhat`

```
3:  m0
8:  prod_theta2_m0  x[180,2]
13: m0  prod_m0_scale  x[180,1]
14: m0  prod_m0_scale  x[180,1]
16: m0  prod_m0_scale  x[180,1]
19: m0  x[180,1]
35: m0  prod_m0_scale  x[180,1]
40: m0  x[180,1]
47: x[180,1]
48: m0  prod_m0_scale  x[180,1]
49: x[180,1]
50: m0  prod_m0_scale  x[180,1]
56: m0  prod_m0_scale  x[180,1]
59: m0  x[180,1]
60: m0  x[180,1]
62: m0  prod_m0_scale  x[180,1]
64: theta[1]  theta[2]  theta[3]  scale  prod_theta2_m0  x[180,1]  x[180,2]
67: m0  prod_m0_scale  x[180,1]
72: x[180,1]
84: x[180,1]
87: m0  x[180,1]
90: x[180,1]
93: m0  x[180,1]
94: m0  prod_m0_scale  x[180,1]
100: theta[2]  m0  prod_theta2_scale  prod_m0_scale  x[180,1]
```

unique combinations:

```
number of unique combinations:  7
```

```
combinations and number of their occurence:
```

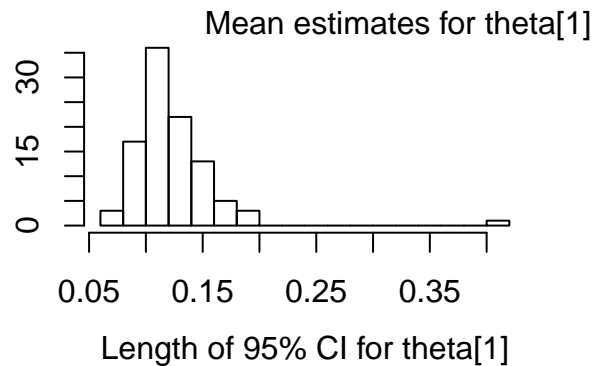
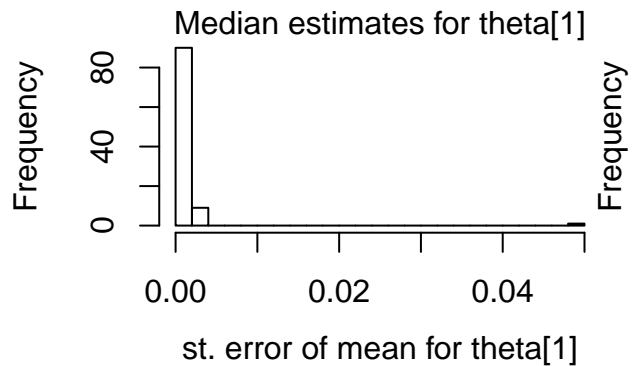
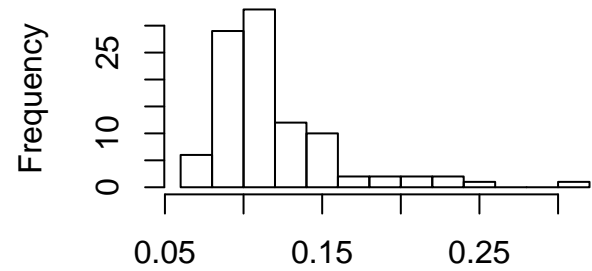
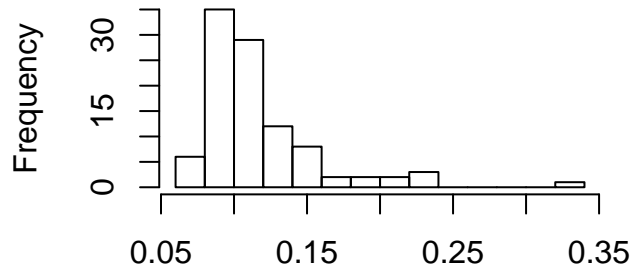
```

1 : m0
1 : prod_theta2_m0 x[180,2]
10 : m0 prod_m0_scale x[180,1]
6 : m0 x[180,1]
5 : x[180,1]
1 : theta[1] theta[2] theta[3] scale prod_theta2_m0 x[180,1] x[180,2]
1 : theta[2] m0 prod_theta2_scale prod_m0_scale x[180,1]

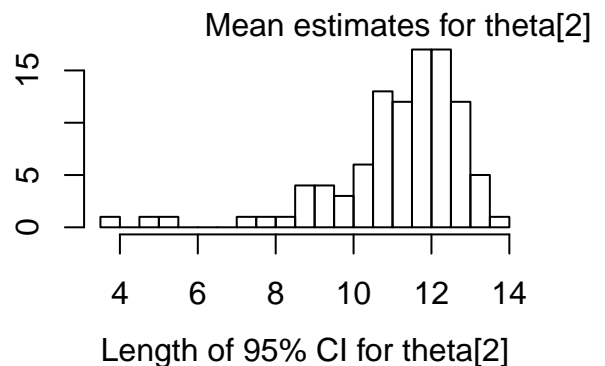
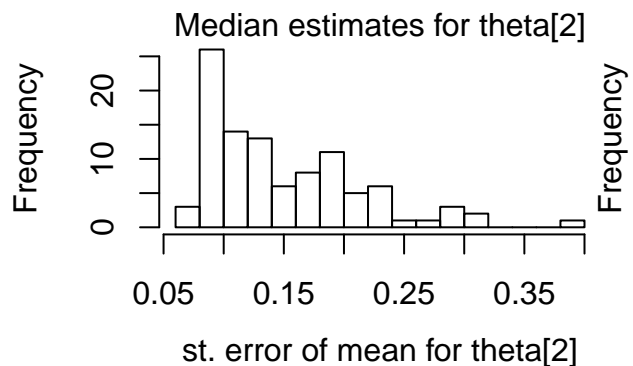
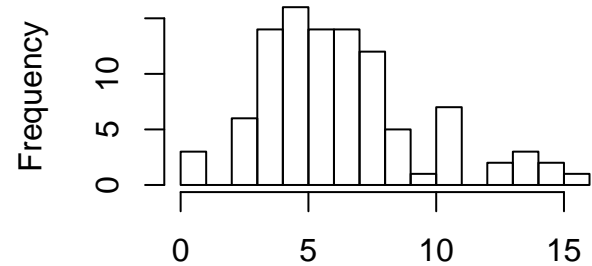
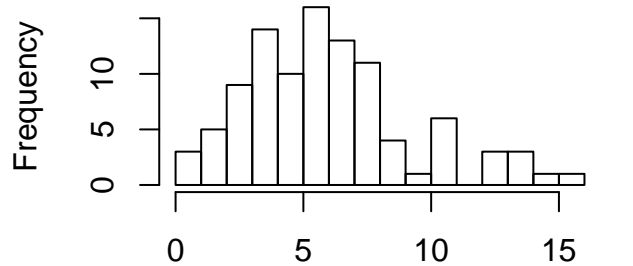
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Overview of estimates

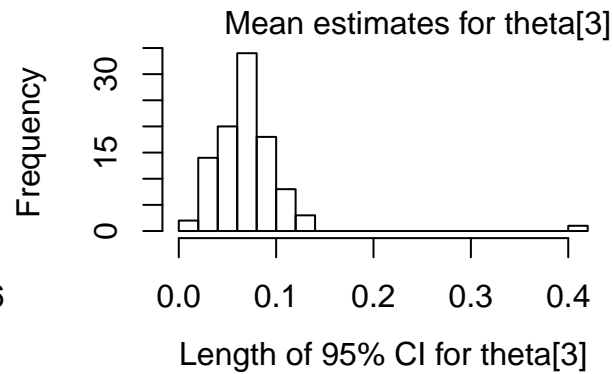
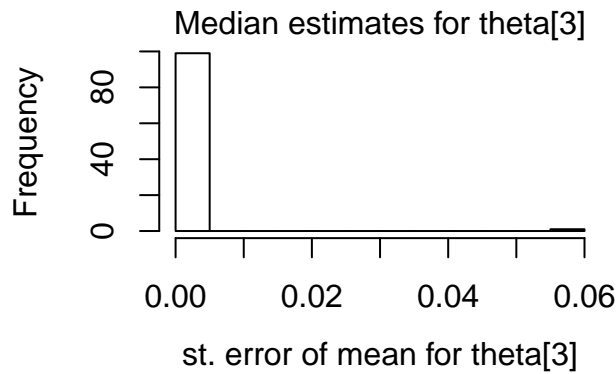
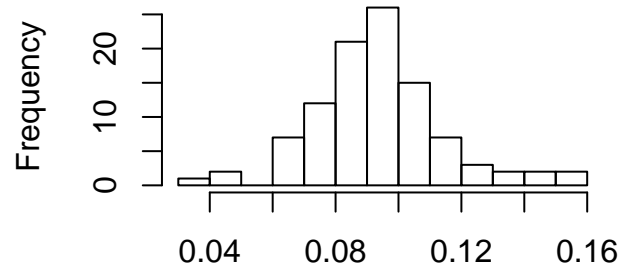
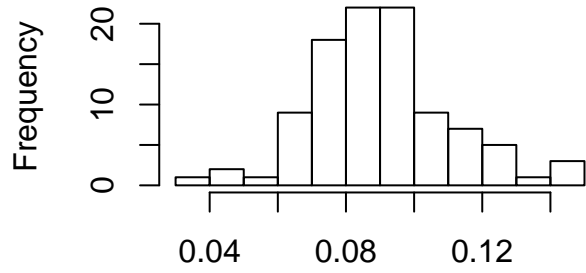
theta[1]



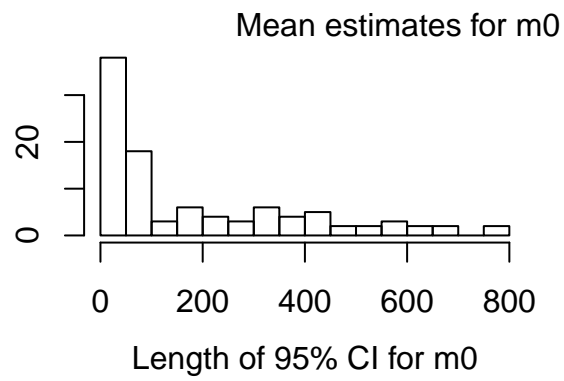
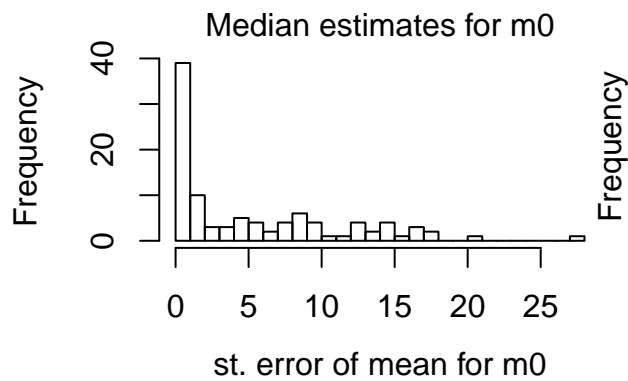
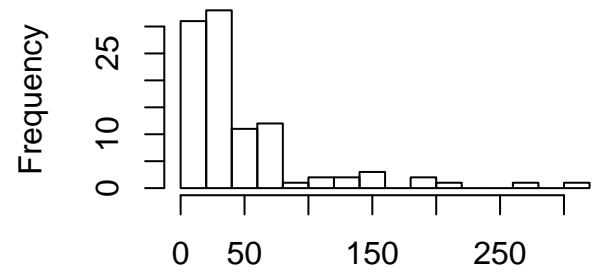
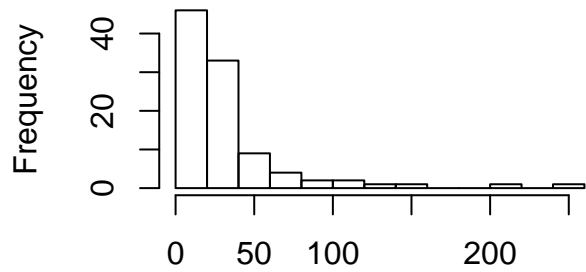
theta[2]



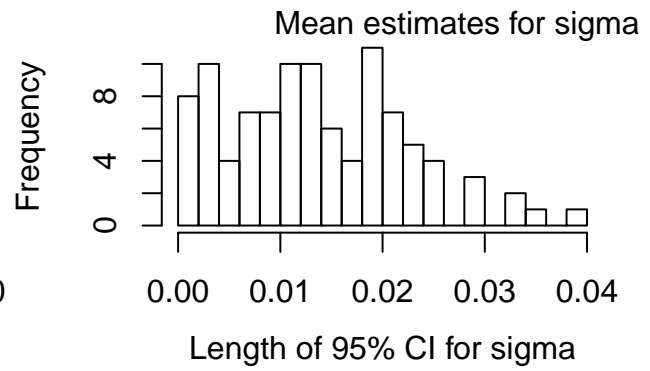
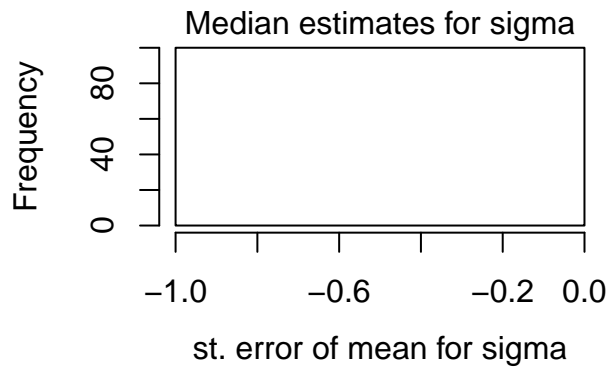
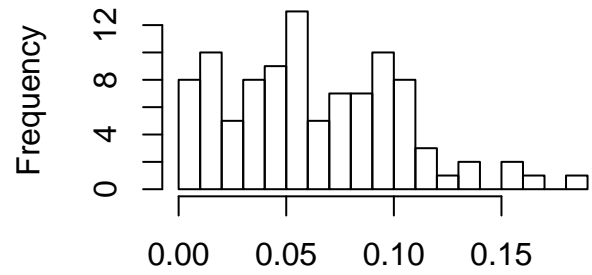
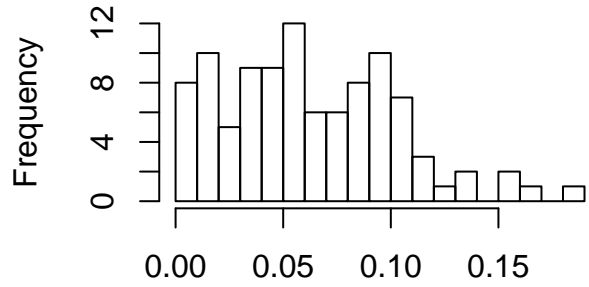
theta[3]



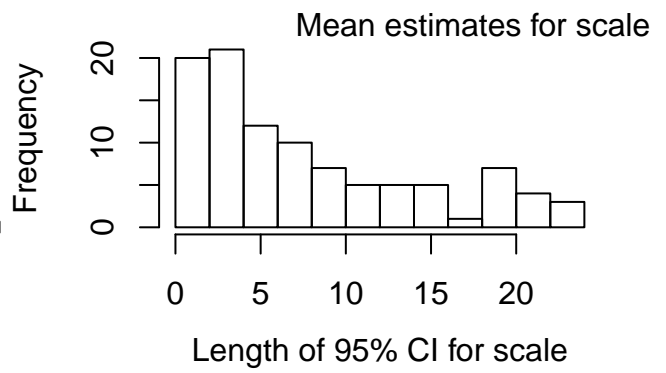
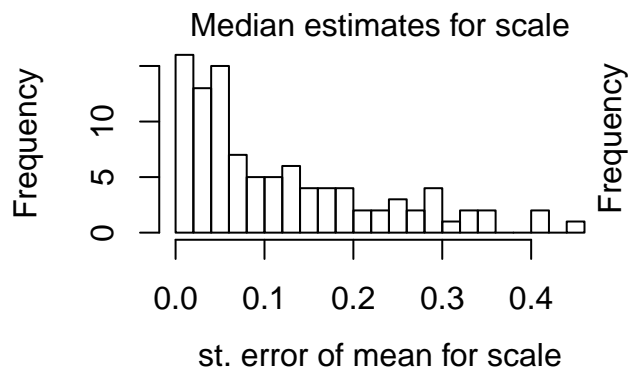
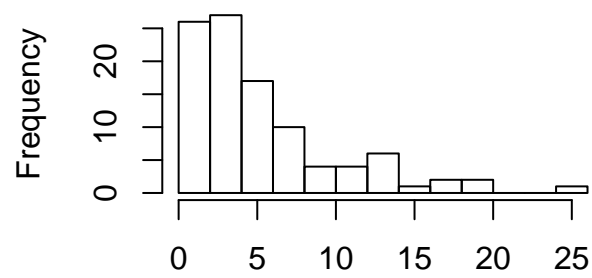
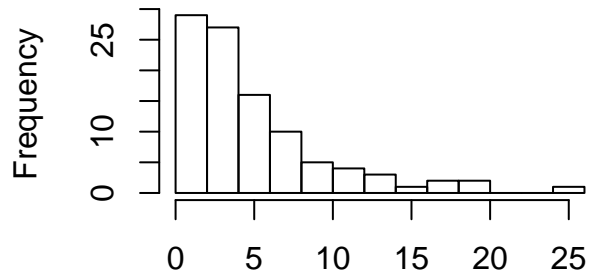
m0



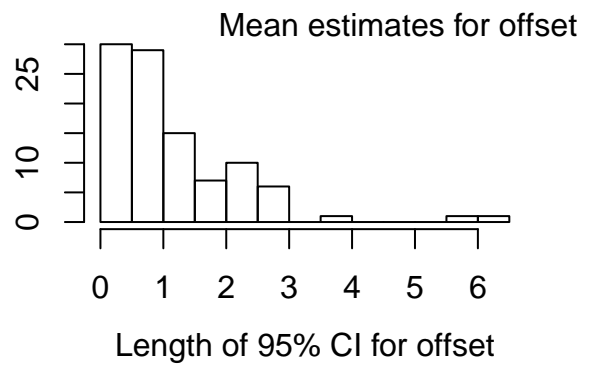
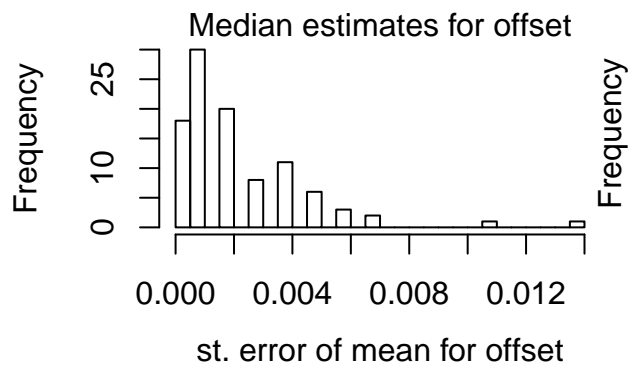
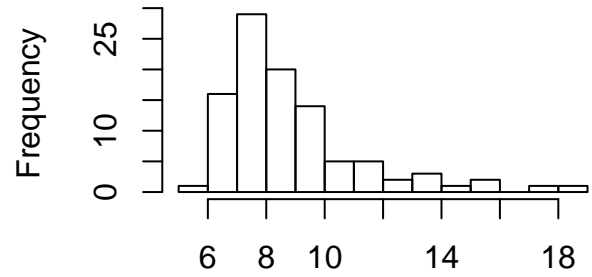
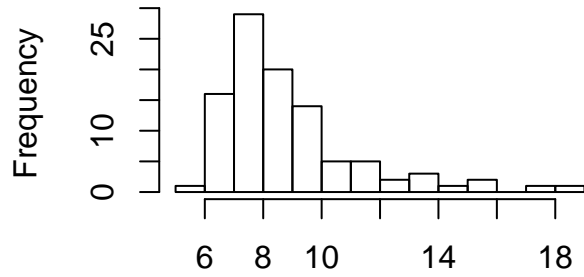
sigma



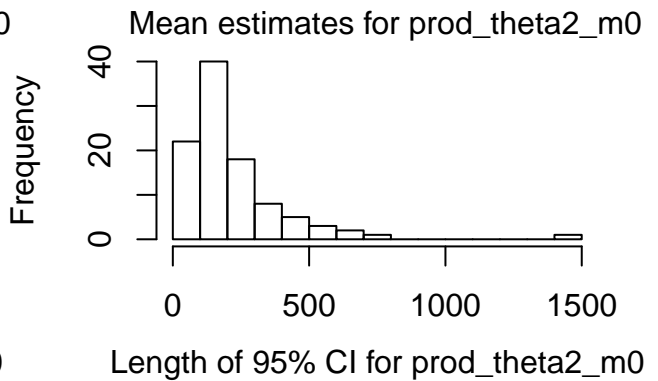
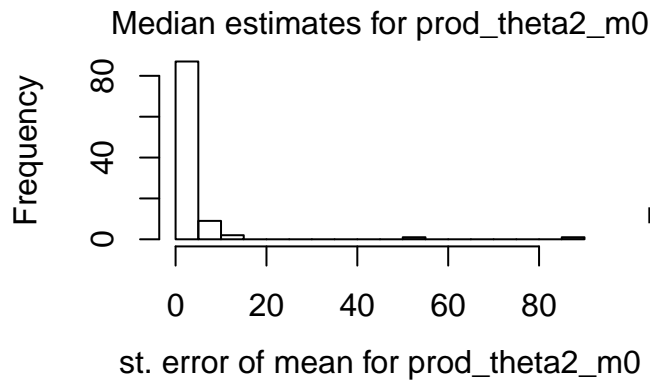
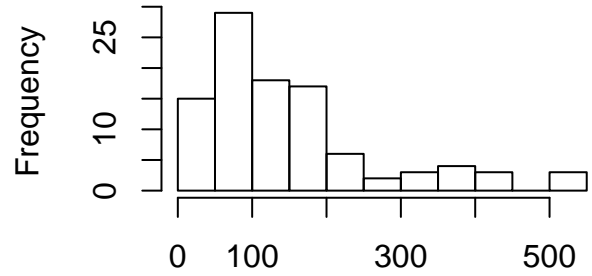
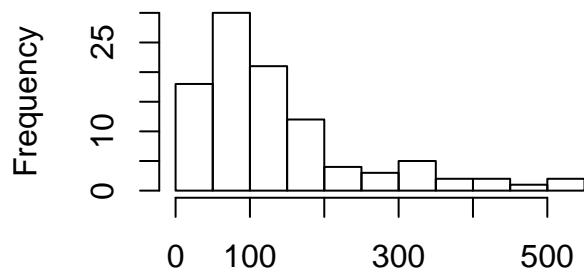
scale



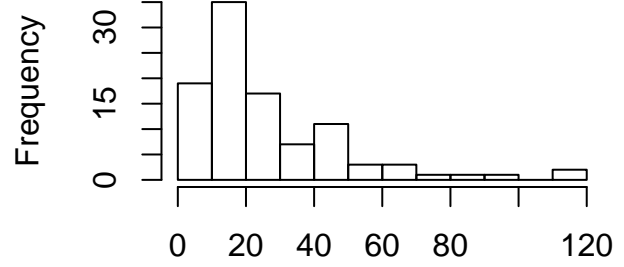
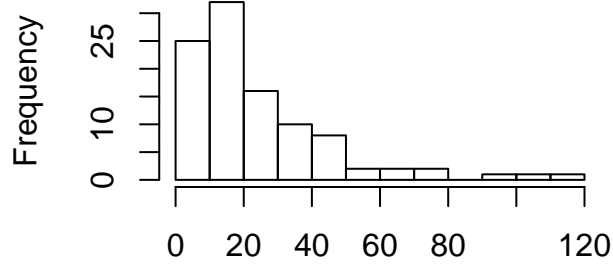
offset



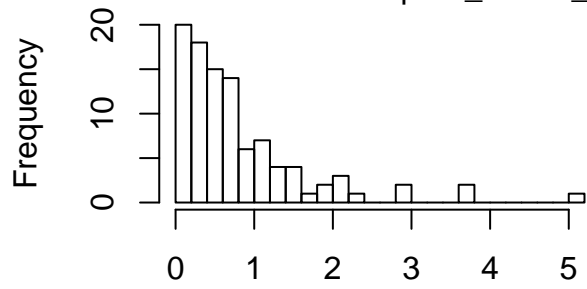
prod_theta2_m0



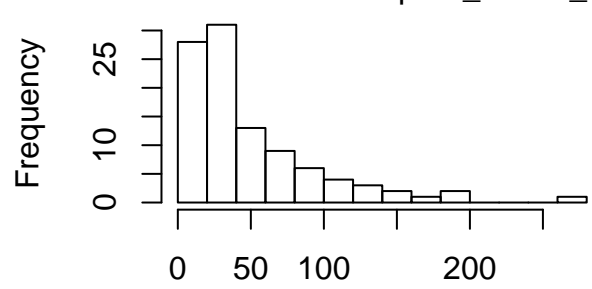
prod_theta2_scale



Median estimates for prod_theta2_scale



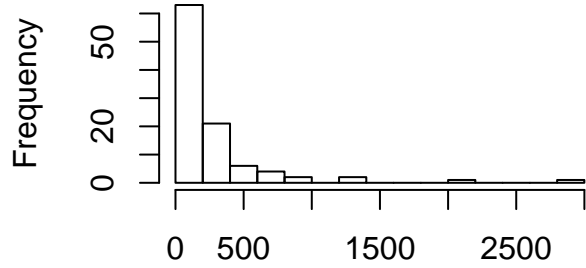
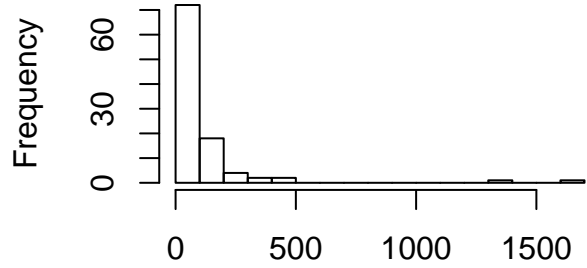
Mean estimates for prod_theta2_scale



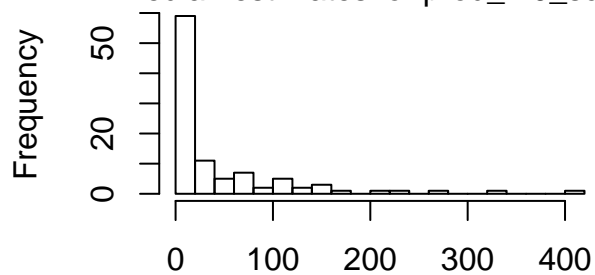
st. error of mean for prod_theta2_scale

Length of 95% CI for prod_theta2_scale

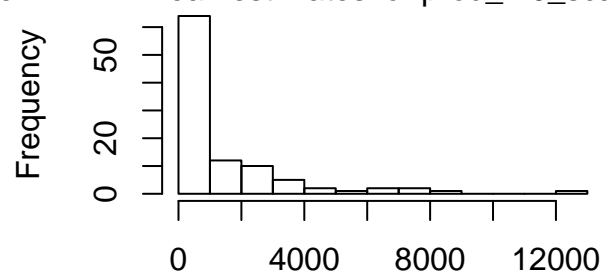
prod_m0_scale



Median estimates for prod_m0_scale



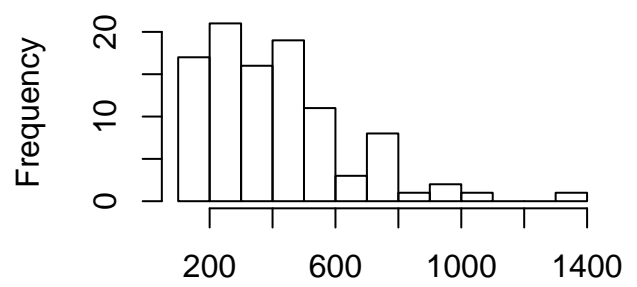
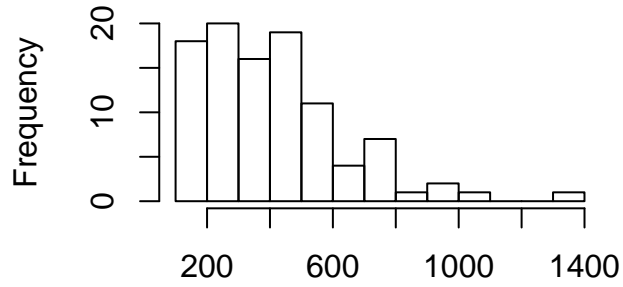
Mean estimates for prod_m0_scale



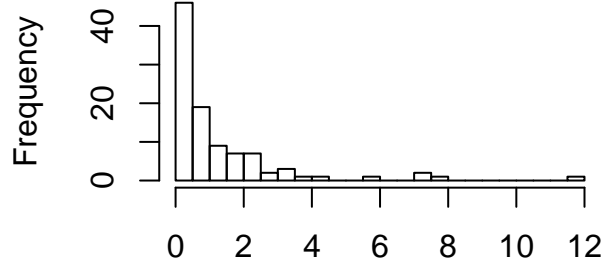
st. error of mean for prod_m0_scale

Length of 95% CI for prod_m0_scale

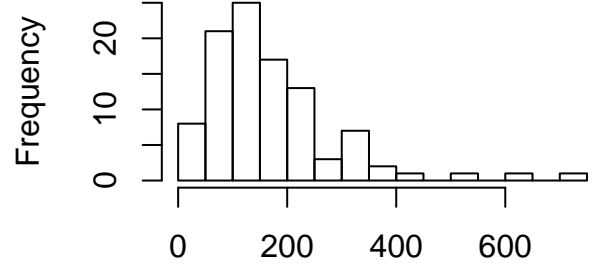
prod_theta2_m0_scale



Median estimates for prod_theta2_m0_scale



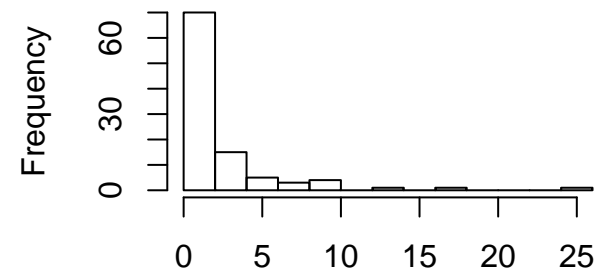
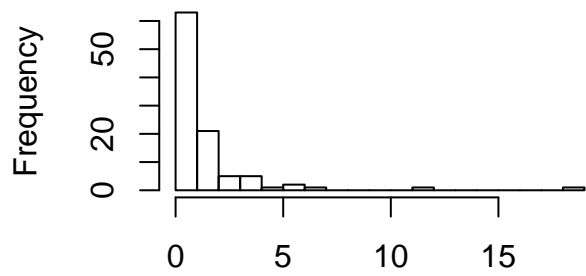
Mean estimates for prod_theta2_m0_scale



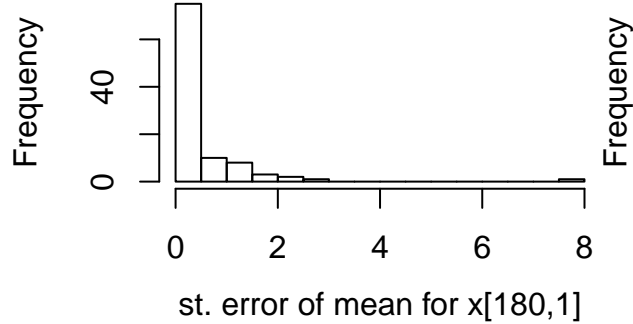
st. error of mean for prod_theta2_m0_scale

Length of 95% CI for prod_theta2_m0_scale

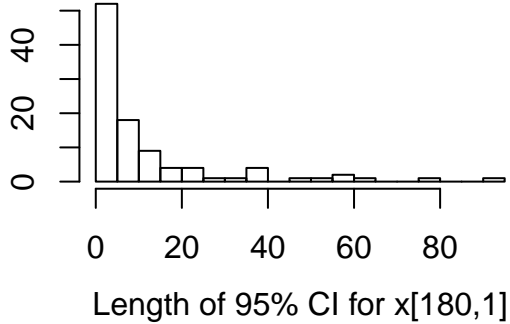
x[180,1]



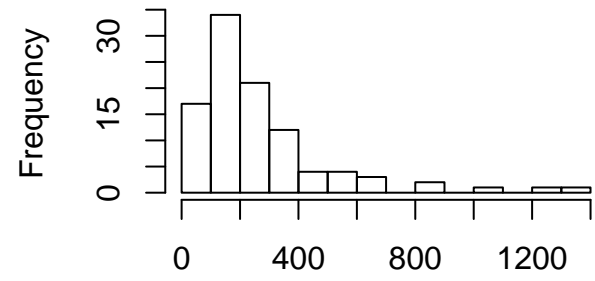
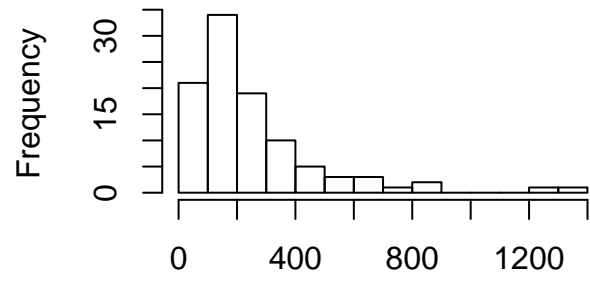
Median estimates for x[180,1]



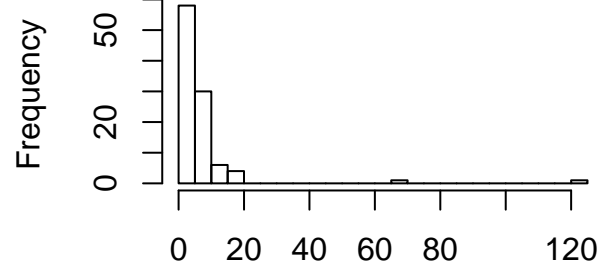
Mean estimates for x[180,1]



$x[180,2]$



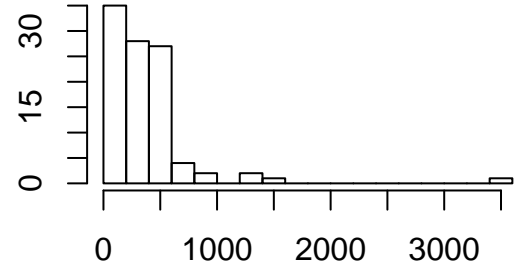
Median estimates for $x[180,2]$



st. error of mean for $x[180,2]$

Frequency

Mean estimates for $x[180,2]$



Length of 95% CI for $x[180,2]$

Summary of length of 95% credible intervals (CIs)

Here we give the median, standard deviation (sd), and coefficient of variation (cv) of the length of the 95% CIs.

For simulated data (where the true parameter values are known), we also give the number of times that the CI covers the true value and median, sd, and cv of the length of those 95% CIs that cover the true value.

| | median_l_CI | sd_l_CI | cv_l_CI |
|----------------------|-------------|----------|---------|
| theta[1] | 0.115 | 0.039 | 0.318 |
| theta[2] | 11.613 | 1.733 | 0.155 |
| theta[3] | 0.067 | 0.042 | 0.591 |
| m0 | 76.558 | 205.436 | 1.094 |
| sigma | 0.013 | 0.009 | 0.609 |
| scale | 5.514 | 6.588 | 0.842 |
| offset | 0.788 | 1.077 | 0.956 |
| prod_theta2_m0 | 172.022 | 194.621 | 0.892 |
| prod_theta2_scale | 34.956 | 47.579 | 0.943 |
| prod_m0_scale | 482.870 | 2205.642 | 1.545 |
| prod_theta2_m0_scale | 145.181 | 120.006 | 0.694 |
| x[180,1] | 4.546 | 17.059 | 1.434 |
| x[180,2] | 310.450 | 405.595 | 1.053 |

The following table shows the values of the median of *the length of the CIs divided by the median of each sample*

$$m_1 = \text{median} \left(\frac{q_i(0.975) - q_i(0.025)}{q_i(0.5)} \right),$$

the median of *the length of the CIs divided by the mean of each sample*

$$m_1 = \text{median} \left(\frac{q_i(0.975) - q_i(0.025)}{\text{sample_mean}} \right),$$

as well as the median of the length of the CIs divided by *the median of the medians of the sample*

$$m_3 = \frac{\text{median}(q_i(0.975) - q_i(0.025))}{\text{median}(q_i(0.5))}.$$

and (if applicable) the median of *the length of the CIs divided by the true value*

$$m_4 = \frac{\text{median}(q_i(0.975) - q_i(0.025))}{\text{true value}}.$$

| | m_1 | m_2 | m_3 |
|----------------------|------|------|------|
| theta[1] | 1.07 | 1.05 | 1.11 |
| theta[2] | 2.15 | 2.03 | 2.14 |
| theta[3] | 0.74 | 0.72 | 0.75 |
| m0 | 3.65 | 2.78 | 3.59 |
| sigma | 0.22 | 0.22 | 0.22 |
| scale | 1.61 | 1.49 | 1.56 |
| offset | 0.10 | 0.10 | 0.09 |
| prod_theta2_m0 | 1.59 | 1.49 | 1.66 |
| prod_theta2_scale | 2.19 | 2.02 | 2.14 |
| prod_m0_scale | 5.99 | 3.71 | 6.86 |
| prod_theta2_m0_scale | 0.39 | 0.39 | 0.38 |
| x[180,1] | 5.91 | 3.87 | 5.94 |
| x[180,2] | 1.61 | 1.51 | 1.71 |