Aggregated sampling output

November 20, 2020

Dataset: experimental_data_eGFP, model type: ODE

Trajectories without pathologies

e.g. no divergent transitions, no max_treedepth exceeded, no Rhat > 1.1, no n_eff < 100 number of trajectories without pathologies (out of 100):

[1] 33

indices of trajectories without pathologies:

[1] 3 8 10 11 18 20 22 23 26 28 30 31 33 35 38 40 41 46 51 52 53 54 55 60 62 [26] 63 71 74 77 88 94 97 98

no pathologies for a subset of the parameters

parameters considered:

[1] "t0" "sigma" "scale"

[4] "offset" "prod_theta2_m0_scale"

number of trajectories without pathologies (out of 100):

[1] 76

indices of trajectories without pathologies:

| [1] | 3 | 4 | 5 | 6 | 8 | 9 | 10 | 11 | 12 | 14 | 17 | 18 | 20 | 22 | 23 | 26 | 27 | 28 | 29 |
|------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|-----|
| [20] | 30 | 31 | 33 | 34 | 35 | 37 | 38 | 40 | 41 | 43 | 45 | 46 | 48 | 49 | 50 | 51 | 52 | 53 | 54 |
| [39] | 55 | 57 | 60 | 62 | 63 | 64 | 65 | 68 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 |
| [58] | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

Divergent transitions

| numof.divtransitions | Freq |
|----------------------|------|
| 0 | 99 |
| 1 | 1 |

total number of trajectories with div. transitions: 1 indices of trajectories with div. transitions: 58

Maximum tree depth exceeded

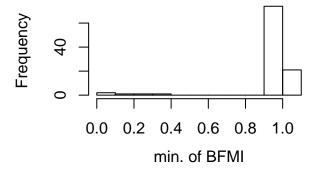
| numof.max.t.dexceeded | Freq |
|-----------------------|------|
| 0 | 97 |

| numof.max.t.dexceeded | Freq |
|-----------------------|------|
| 2500 | 3 |

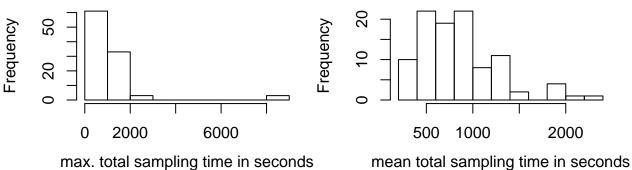
total number of trajectories were max. tree depth was exceeded: 3 indices of trajectories were max. tree depth was exceeded: 1 24 56

Bayesian fraction of missing information (BFMI)

| numof.low.BFMI | Freq |
|----------------|------|
| 0 | 97 |
| 1 | 3 |



Total sampling time



R-hat total number of trajectories with very high Rhat (> 1.1) (out of 100) $\cite{1}$ 65

number of trajectories with high Rhat per parameter (out of 100)

| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | |
|---|-----|
| | 1.1 |
| theta[2] 3 | 54 |
| ······ | 1 |
| theta[3] 58 | 53 |
| m0 1 | 0 |
| sigma 19 | 14 |
| scale 3 | 2 |
| offset 23 | 20 |

| | Rhat > 1.02 | Rhat > 1.1 |
|---------------------------|---------------|------------|
| $\overline{\mathrm{t0}}$ | 23 | 23 |
| $prod_theta2_m0$ | 0 | 0 |
| $prod_theta2_scale$ | 1 | 1 |
| $prod_m0_scale$ | 2 | 1 |
| $prod_theta2_m0_scale$ | 23 | 22 |
| $x2_sim[180]$ | 0 | 0 |

number of parameters with high Rhat per trajectory (out of 13)

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 9 | 12 | 13 | 14 | 15 | 16 | 17 | 19 | 21 | 24 | 25 | 27 | 29 |
|---------------------------------|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|
| $\overline{\text{Rhat} > 1.02}$ | 9 | 6 | 2 | 2 | 2 | 2 | 6 | 2 | 2 | 6 | 2 | 6 | 3 | 2 | 5 | 4 | 10 | 4 | 2 | 2 |
| Rhat > 1.1 | 8 | 6 | 0 | 2 | 2 | 2 | 6 | 2 | 2 | 4 | 2 | 6 | 3 | 2 | 5 | 2 | 8 | 4 | 2 | 2 |

| | 32 | 34 | 36 | 37 | 39 | 42 | 43 | 44 | 45 | 47 | 48 | 49 | 50 | 56 | 57 | 59 | 61 | 64 | 65 | 66 |
|-------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Rhat > 1.02 | 4 | 2 | 5 | 2 | 4 | 6 | 2 | 6 | 2 | 4 | 2 | 2 | 2 | 9 | 2 | 4 | 3 | 2 | 2 | 4 |
| Rhat > 1.1 | 3 | 2 | 4 | 2 | 3 | 4 | 2 | 6 | 2 | 4 | 2 | 0 | 2 | 7 | 2 | 3 | 1 | 2 | 2 | 4 |

| | 67 | 68 | 69 | 70 | 72 | 73 | 75 | 76 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 89 | 90 |
|-------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Rhat > 1.02 | 6 | 2 | 6 | 6 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| Rhat > 1.1 | 4 | 2 | 6 | 6 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |

theta[1]

number of trajectories with Rhat > 1.02: 58

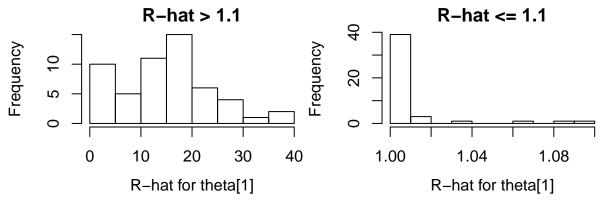
indizes of trajectories with Rhat > 1.02:

1 2 3 4 5 6 7 9 12 13 14 15 17 19 24 27 29 34 36 37 42 43 44 45 48 49 50 56 57 64 65 67 68 69 70 72 73

number of trajectories with Rhat > 1.1: 54

indices of trajectories with Rhat > 1.1:

1 2 4 5 6 7 9 12 14 15 17 19 24 27 29 34 36 37 43 44 45 48 50 56 57 64 65 67 68 69 70 72 73 75 76 78 79



theta[2]

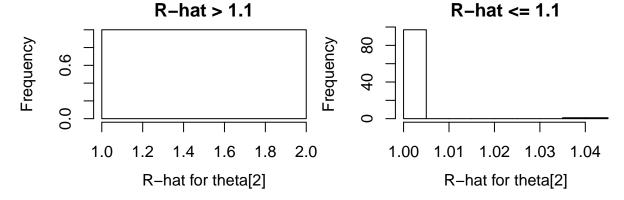
number of trajectories with Rhat > 1.02:

3

indizes of trajectories with Rhat > 1.02:
1 24 56

number of trajectories with Rhat > 1.1: 1

indices of trajectories with Rhat > 1.1:



theta[3]

number of trajectories with Rhat > 1.02: 58

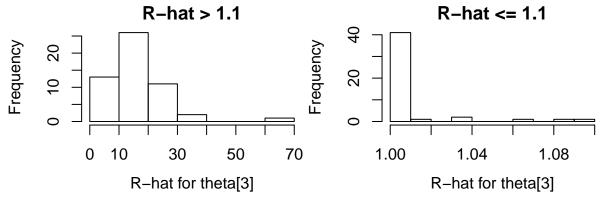
indizes of trajectories with Rhat > 1.02:

1 2 3 4 5 6 7 9 12 13 14 15 17 19 24 27 29 34 36 37 42 43 44 45 48 49 50 56 57 64 65 67 68 69 70 72 73

number of trajectories with Rhat > 1.1: 53

indices of trajectories with Rhat > 1.1:

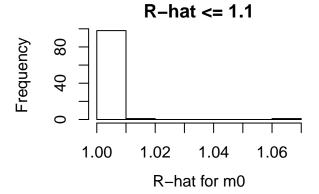
1 2 4 5 6 7 9 12 14 15 17 19 24 27 29 34 36 37 43 44 45 48 50 56 57 64 65 68 69 70 72 73 75 76 78 79 80



m0

number of trajectories with Rhat > 1.02:

indizes of trajectories with Rhat > 1.02: 24



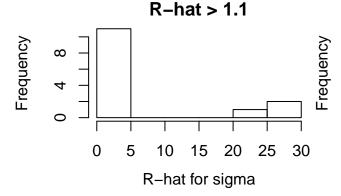
sigma

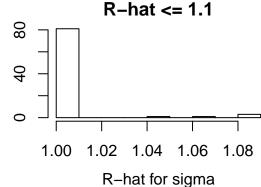
number of trajectories with Rhat > 1.02: 19

indizes of trajectories with Rhat > 1.02: 1 2 7 13 15 21 24 25 32 39 42 44 47 56 59 66 67 69 70

number of trajectories with Rhat > 1.1: 14

indices of trajectories with Rhat > 1.1: 1 2 7 13 15 24 25 42 44 47 56 66 69 70





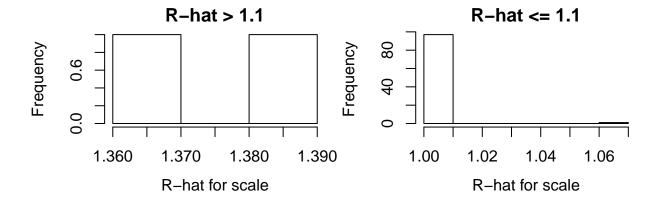
scale

number of trajectories with Rhat > 1.02:

indizes of trajectories with Rhat > 1.02:
1 24 56

number of trajectories with Rhat > 1.1: 2

indices of trajectories with Rhat > 1.1: 1 56



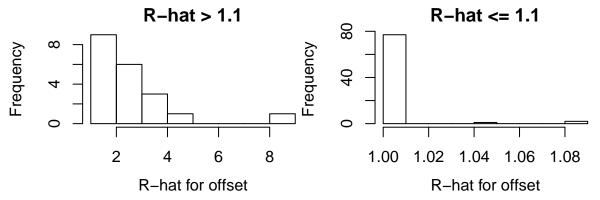
offset

number of trajectories with Rhat > 1.02: 23

indizes of trajectories with Rhat > 1.02:
1 2 7 13 15 16 19 21 24 25 32 36 39 42 44 47 56 59 61 66 67 69 70

number of trajectories with Rhat > 1.1: 20

indices of trajectories with Rhat > 1.1:
1 2 7 13 15 16 19 24 25 32 39 42 44 47 56 59 66 67 69 70



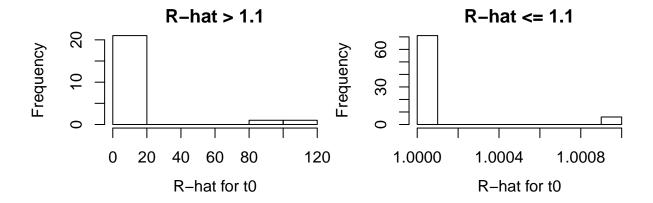
 $\mathbf{t0}$

number of trajectories with Rhat > 1.02: 23

indizes of trajectories with Rhat > 1.02: 1 2 7 13 15 16 19 21 24 25 32 36 39 42 44 47 56 59 61 66 67 69 70

number of trajectories with Rhat > 1.1: 23

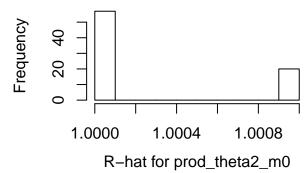
indices of trajectories with Rhat > 1.1:
1 2 7 13 15 16 19 21 24 25 32 36 39 42 44 47 56 59 61 66 67 69 70



 $prod_theta2_m0$

no Rhat > 1.02





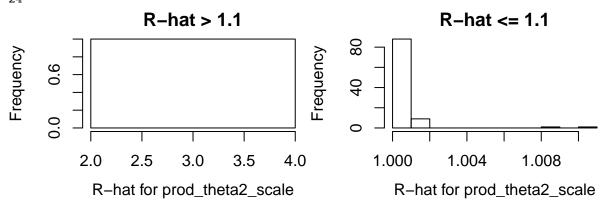
 ${\bf prod_theta2_scale}$

number of trajectories with Rhat > 1.02:

indizes of trajectories with Rhat > 1.02:
24

number of trajectories with Rhat > 1.1: 1

indices of trajectories with Rhat > 1.1: 24



prod_m0_scale

number of trajectories with Rhat > 1.02:

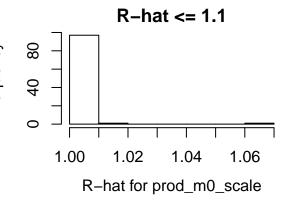
indizes of trajectories with Rhat > 1.02:
1 56

number of trajectories with Rhat > 1.1: 1

indices of trajectories with Rhat > 1.1:

R-hat > 1.1

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 $prod_theta2_m0_scale$

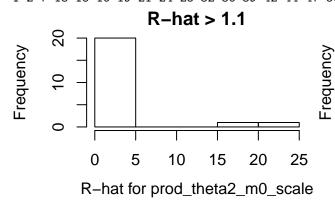
number of trajectories with Rhat > 1.02: 23

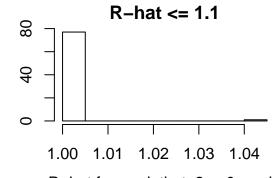
indizes of trajectories with Rhat > 1.02:

1 2 7 13 15 16 19 21 24 25 32 36 39 42 44 47 56 59 61 66 67 69 70

number of trajectories with Rhat > 1.1: 22

indices of trajectories with Rhat > 1.1:
1 2 7 13 15 16 19 21 24 25 32 36 39 42 44 47 56 59 66 67 69 70





R-hat for prod_theta2_m0_scale

 $x2_sim[180]$

no Rhat > 1.02

R-hat <= 1.1 \[\frac{1.0000}{0.0004} \] 1.0000 \] R-hat for x2_sim[180]

Effective sample size (ESS)

total number of trajectories with low ESS (< 100) (out of 100)

[1] 66

number of trajectories with low ESS (< 100) per parameter (out of 100)

| | n_eff < 100 |
|---------------------------|-------------|
| theta[1] | 54 |
| theta[2] | 3 |
| theta[3] | 55 |
| m0 | 1 |
| sigma | 19 |
| scale | 3 |
| offset | 22 |
| t0 | 23 |
| $prod_theta2_m0$ | 0 |
| $prod_theta2_scale$ | 1 |
| $prod_m0_scale$ | 2 |
| $prod_theta2_m0_scale$ | 22 |
| x2_sim[180] | 0 |

number of parameters with low ESS (< 300) per trajectory (out of 13)

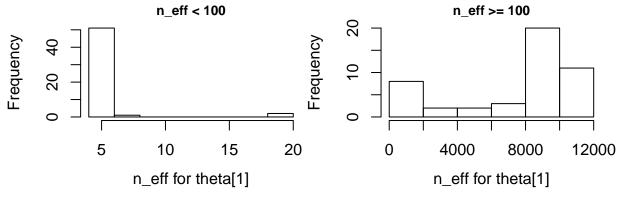
| | 1 | 2 | 4 | 5 | 6 | 7 | 9 | 12 | 13 | 14 | 15 | 16 | 17 | 19 | 21 | 24 | 25 | 27 | 29 | 32 | |
|----------------------------|----|----|----|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| $n_{eff} < 100$ | 9 | 6 | 2 | 2 | 2 | 6 | 2 | 2 | 4 | 2 | 6 | 3 | 2 | 5 | 4 | 10 | 4 | 2 | 2 | 4 | |
| | | | | | | | | | | | | | | | | | | | | | |
| | 34 | 36 | 37 | 3 | 9 | 42 | 43 | 44 | 45 | 47 | 48 | 49 | 50 | 56 | 57 | 59 | 61 | 64 | 65 | 66 | 67 |
| n_eff < 100 | 2 | 5 | 2 | | 4 | 4 | 2 | 6 | 2 | 4 | 2 | 1 | 2 | 9 | 2 | 4 | 1 | 2 | 2 | 4 | 6 |
| | | | | | | | | | | | | | | | | | | | | | |
| | 68 | 69 | 70 | 7 | 2 | 73 | 75 | 76 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 89 | 90 | 91 |
| $\overline{n_{eff} < 100}$ | 2 | 6 | 6 | | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |

theta[1]

number of trajectories with n_eff < 100: 54</pre>

indices of trajectories with $n_{eff} < 100$:

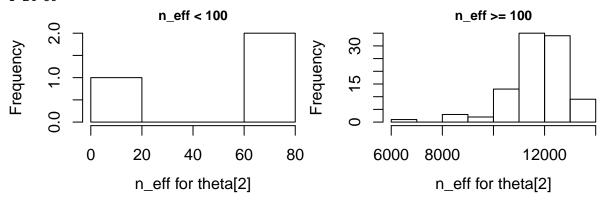
 $1 \ 2 \ 4 \ 5 \ 6 \ 7 \ 9 \ 12 \ 14 \ 15 \ 17 \ 19 \ 24 \ 27 \ 29 \ 34 \ 36 \ 37 \ 43 \ 44 \ 45 \ 48 \ 50 \ 56 \ 57 \ 64 \ 65 \ 67 \ 68 \ 69 \ 70 \ 72 \ 73 \ 75 \ 76 \ 78 \ 79$



theta[2]

number of trajectories with $n_{eff} < 100$: 3

indices of trajectories with n_eff < 100: 1 24 56

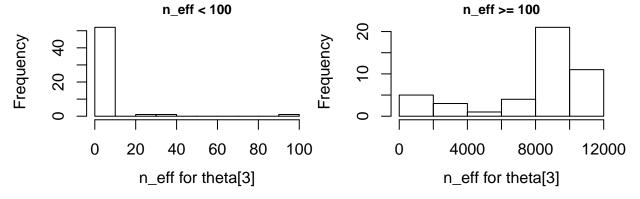


theta[3]

number of trajectories with n_eff < 100: 55</pre>

indices of trajectories with $n_{eff} < 100$:

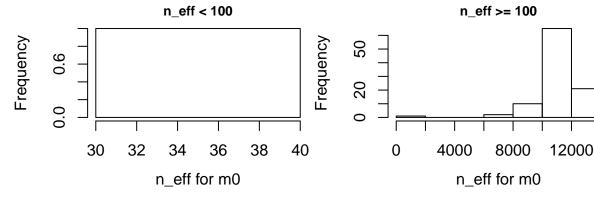
1 2 4 5 6 7 9 12 14 15 17 19 24 27 29 34 36 37 43 44 45 48 49 50 56 57 64 65 67 68 69 70 72 73 75 76 78



m0

number of trajectories with n_eff < 100:</pre>

indices of trajectories with $n_{eff} < 100$: 24

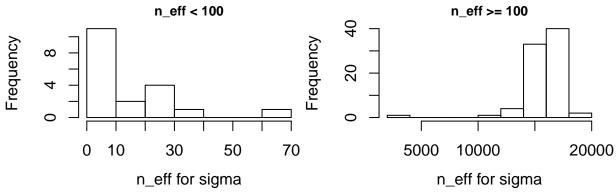


sigma

number of trajectories with n_eff < 100: 19</pre>

indices of trajectories with $n_{eff} < 100$:

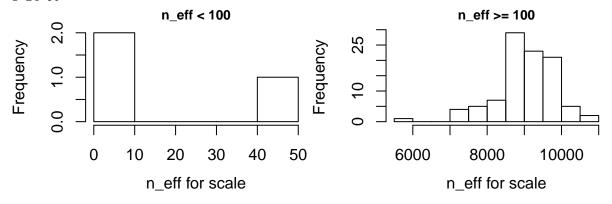
 $1 \ 2 \ 7 \ 13 \ 15 \ 21 \ 24 \ 25 \ 32 \ 39 \ 42 \ 44 \ 47 \ 56 \ 59 \ 66 \ 67 \ 69 \ 70$



scale

number of trajectories with $n_{eff} < 100$: 3

indices of trajectories with $n_{eff} < 100$: 1 24 56

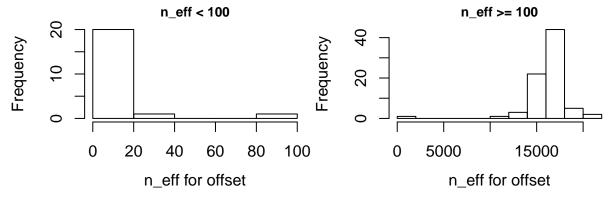


offset

number of trajectories with $n_{eff} < 100$: 22

indices of trajectories with $n_{eff} < 100$:

1 2 7 13 15 16 19 21 24 25 32 36 39 42 44 47 56 59 66 67 69 70

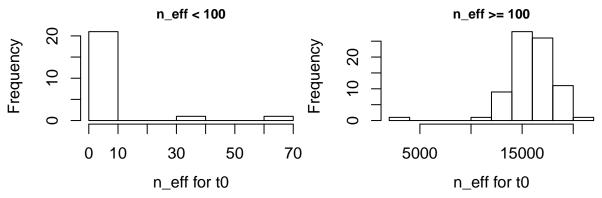


 $\mathbf{t0}$

number of trajectories with n_eff < 100: 23</pre>

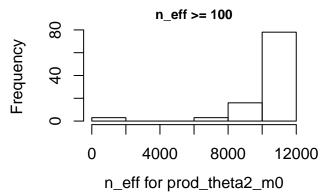
indices of trajectories with $n_{eff} < 100$:

1 2 7 13 15 16 19 21 24 25 32 36 39 42 44 47 56 59 61 66 67 69 70



 $prod_theta2_m0$

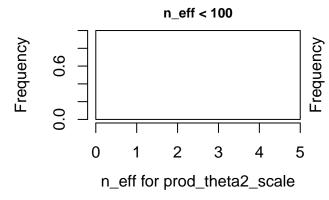
 $no n_eff < 100$

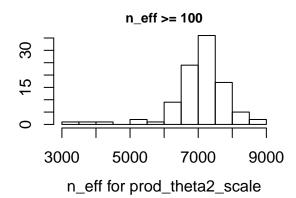


prod_theta2_scale

number of trajectories with n_eff < 100:</pre>

indices of trajectories with $n_{eff} < 100$: 24

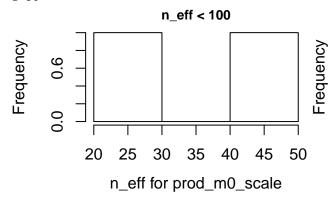


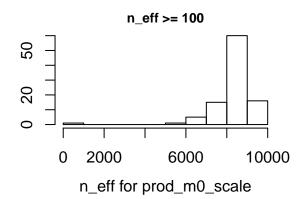


prod_m0_scale

number of trajectories with n_eff < 100:</pre>

indices of trajectories with n_eff < 100: 1 56 $\,$



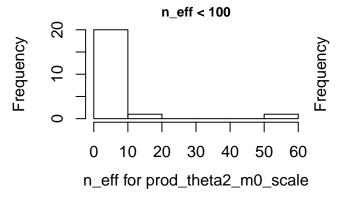


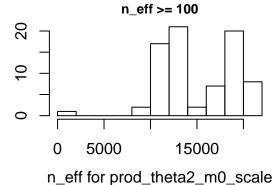
prod_theta2_m0_scale

number of trajectories with n_eff < 100: 22</pre>

indices of trajectories with $n_{eff} < 100$:

1 2 7 13 15 16 19 21 24 25 32 36 39 42 44 47 56 59 66 67 69 70





Find problematic trajectories and parameters

n_eff for x2_sim[180]

Are there any trajectories and parameters for which n_eff is below the threshold, but Rhat does not exceed the threshold?

[1] FALSE

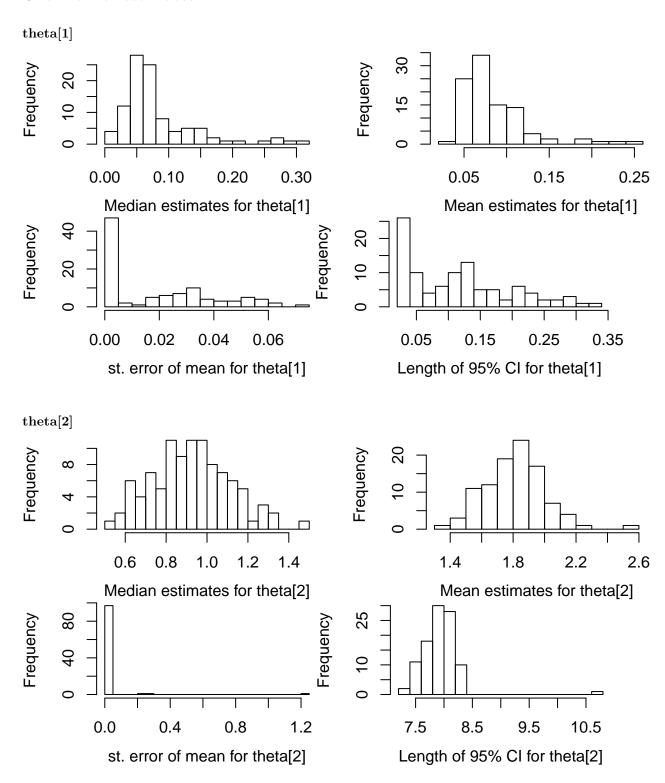
parameters per trajectories with very high Rhat

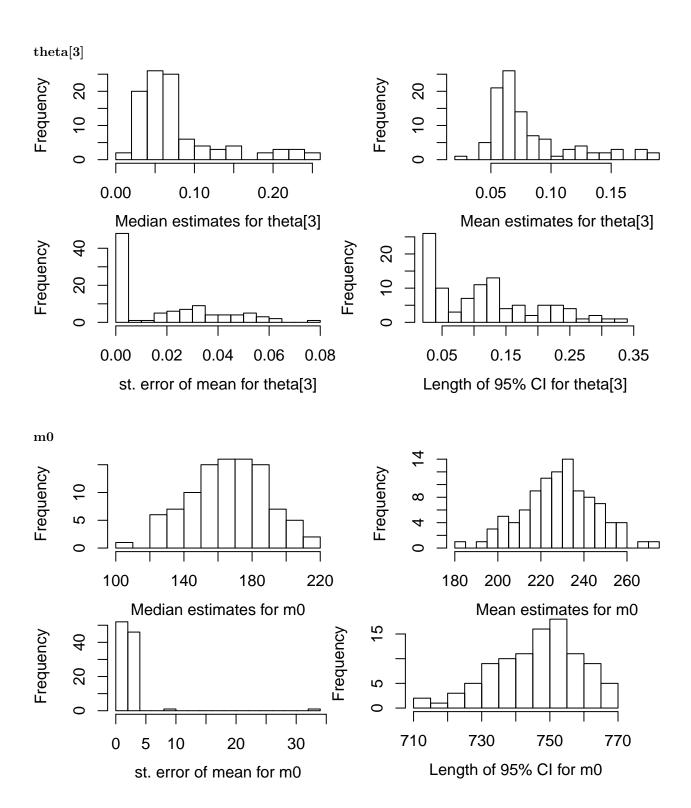
```
theta[1]
             theta[3]
                        sigma scale offset t0 prod_m0_scale prod_theta2_m0_scale
1:
              theta[3]
                        sigma offset t0 prod_theta2_m0_scale
2:
    theta[1]
4:
    theta[1]
              theta[3]
5:
    theta[1]
              theta[3]
6:
    theta[1]
              theta[3]
7:
    theta[1]
              theta[3]
                        sigma offset t0 prod_theta2_m0_scale
9:
    theta[1] theta[3]
12:
     theta[1] theta[3]
     sigma offset t0
                        prod_theta2_m0_scale
13:
14:
     theta[1] theta[3]
15:
     theta[1] theta[3] sigma offset t0 prod_theta2_m0_scale
16:
      offset t0 prod theta2 m0 scale
17:
     theta[1] theta[3]
19:
     theta[1] theta[3] offset t0 prod_theta2_m0_scale
21:
     t0 prod_theta2_m0_scale
24:
     theta[1] theta[2] theta[3] sigma offset t0 prod_theta2_scale prod_theta2_m0_scale
25:
     sigma offset t0 prod_theta2_m0_scale
     theta[1] theta[3]
27:
29:
     theta[1] theta[3]
     offset t0 prod_theta2_m0_scale
32:
34:
     theta[1] theta[3]
36:
     theta[1] theta[3]
                         t0 prod_theta2_m0_scale
37:
     theta[1] theta[3]
39:
     offset t0 prod_theta2_m0_scale
42:
      sigma offset t0 prod_theta2_m0_scale
43:
     theta[1] theta[3]
44:
     theta[1]
               theta[3]
                        sigma offset t0 prod_theta2_m0_scale
45:
              theta[3]
     theta[1]
47:
     sigma offset t0 prod_theta2_m0_scale
48:
     theta[1] theta[3]
50:
     theta[1]
               theta[3]
56:
     theta[1]
              theta[3]
                        sigma scale offset t0 prod_theta2_m0_scale
     theta[1] theta[3]
57:
```

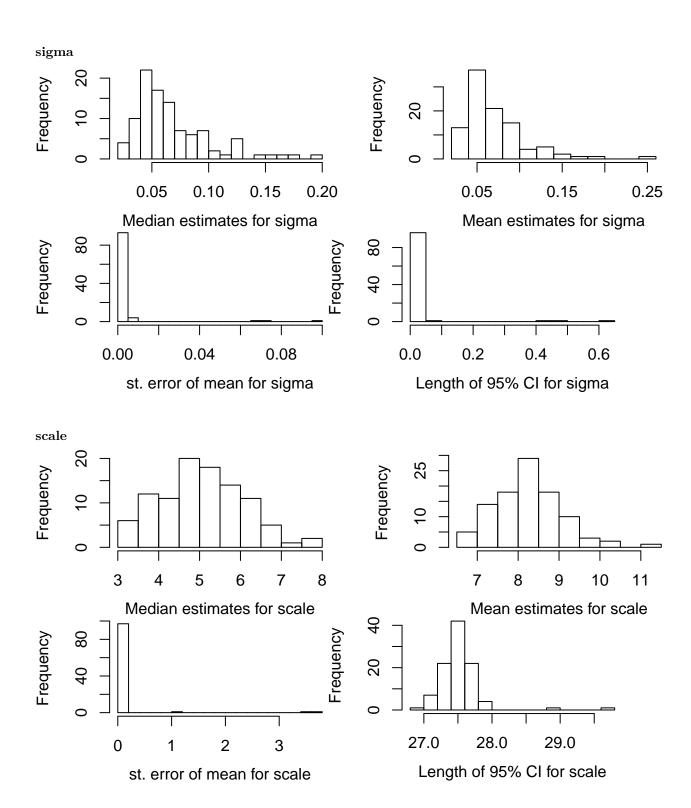
```
59:
     offset t0 prod_theta2_m0_scale
61:
     t0
     theta[1] theta[3]
64:
65:
     theta[1] theta[3]
     sigma offset t0 prod_theta2_m0_scale
66:
67:
     theta[1] offset t0 prod_theta2_m0_scale
68:
     theta[1] theta[3]
69:
                       sigma offset t0 prod_theta2_m0_scale
     theta[1] theta[3]
70:
     theta[1] theta[3]
                        sigma offset t0 prod_theta2_m0_scale
72:
     theta[1] theta[3]
73:
     theta[1] theta[3]
75:
     theta[1] theta[3]
76:
     theta[1] theta[3]
78:
     theta[1] theta[3]
79:
     theta[1] theta[3]
80:
     theta[1] theta[3]
81:
     theta[1] theta[3]
82:
     theta[1] theta[3]
83:
     theta[1] theta[3]
84:
     theta[1] theta[3]
85:
     theta[1] theta[3]
86:
     theta[1] theta[3]
87:
     theta[1] theta[3]
89:
     theta[1] theta[3]
90:
     theta[1] theta[3]
91:
     theta[1] theta[3]
92:
     theta[1] theta[3]
93:
     theta[1] theta[3]
95:
     theta[1] theta[3]
96:
     theta[1] theta[3]
99:
     theta[1] theta[3]
100:
      theta[1] theta[3]
unique combinations:
number of unique combinations: 12
combinations and number of their occruence:
1 : theta[1] theta[3] sigma scale offset t0 prod_m0_scale prod_theta2_m0_scale
6 : theta[1] theta[3] sigma offset t0 prod_theta2_m0_scale
42 : theta[1] theta[3]
 : sigma offset t0 prod_theta2_m0_scale
  : offset t0 prod_theta2_m0_scale
  : theta[1] theta[3] offset t0 prod_theta2_m0_scale
  : t0 prod theta2 m0 scale
  : theta[1] theta[2] theta[3] sigma offset t0 prod_theta2_scale prod_theta2_m0_scale
  : theta[1] theta[3] t0 prod_theta2_m0_scale
 : theta[1] theta[3] sigma scale offset t0 prod_theta2_m0_scale
1
1
```

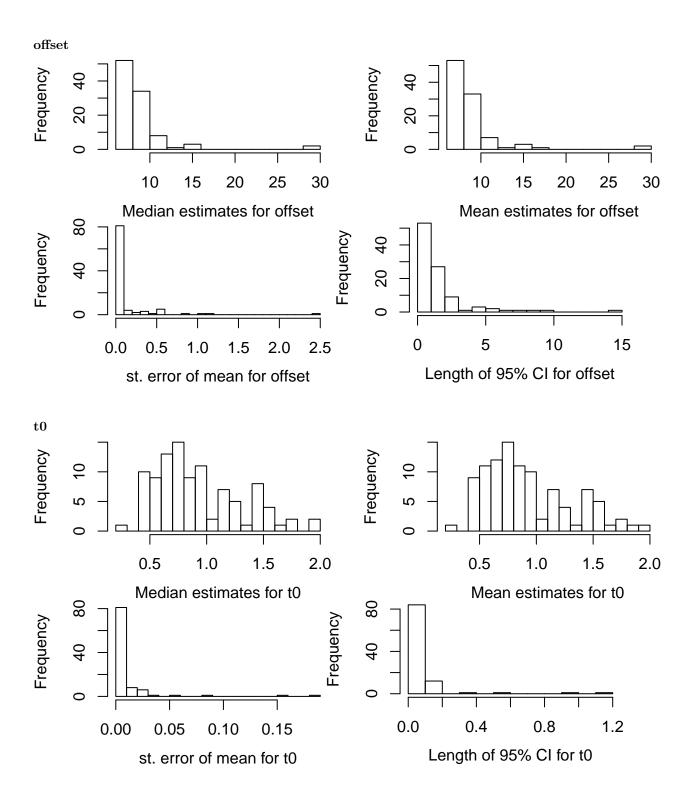
: theta[1] offset t0 prod_theta2_m0_scale

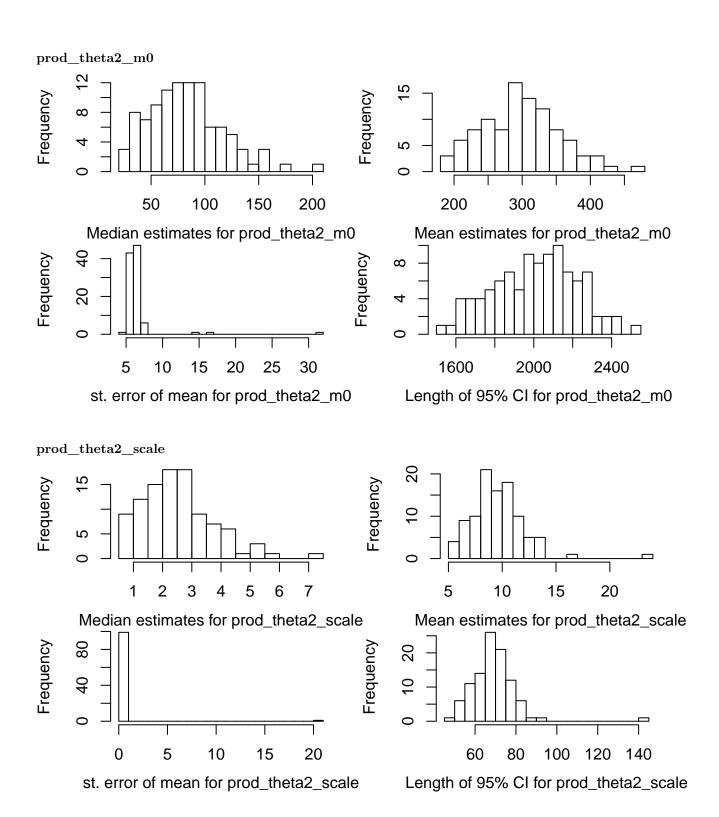
Overview of estimates

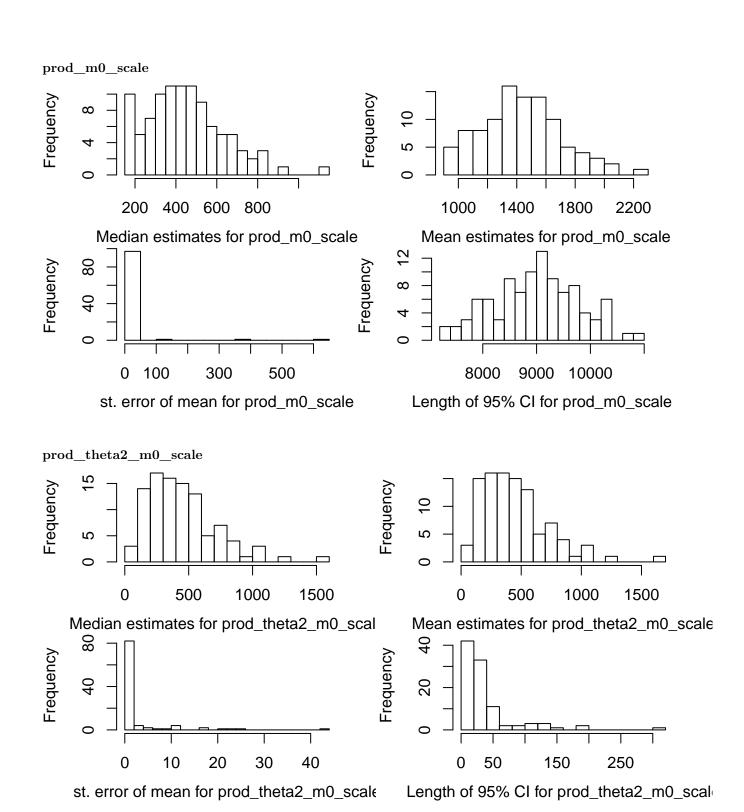


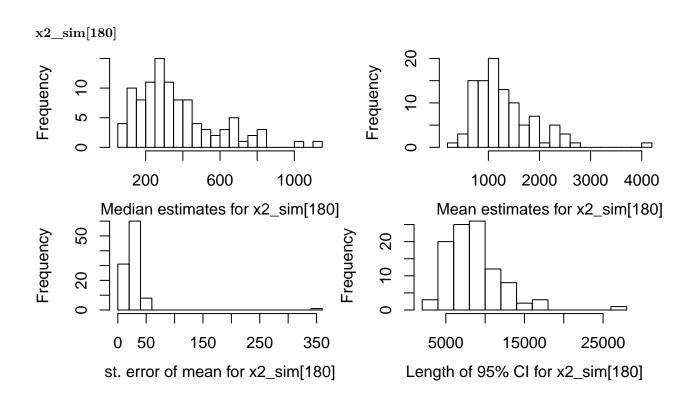












Summary of length of 95% credible intervals (CIs)

Here we give the median, standard deviation (sd), and coefficient of variation (cv) of the length of the 95% CIs.

For simulated data (where the true parameter values are known), we also give the number of times that the CI covers the true value and median, sd, and cv of the length of those 95% CIs that cover the true value.

| | $\rm median_l_CI$ | sd_l_CI | cv_l_CI |
|----------------------|---------------------|----------|---------|
| theta[1] | 0.108 | 0.081 | 0.709 |
| theta[2] | 7.909 | 0.360 | 0.045 |
| theta[3] | 0.107 | 0.081 | 0.706 |
| m0 | 747.712 | 12.580 | 0.017 |
| sigma | 0.013 | 0.087 | 2.795 |
| scale | 27.503 | 0.324 | 0.012 |
| offset | 0.960 | 2.097 | 1.269 |
| t0 | 0.023 | 0.158 | 2.288 |
| $prod_theta2_m0$ | 2032.461 | 216.245 | 0.108 |
| prod_theta2_scale | 68.384 | 11.374 | 0.165 |
| $prod_m0_scale$ | 9093.220 | 790.197 | 0.088 |
| prod_theta2_m0_scale | 24.097 | 46.816 | 1.224 |
| x2_sim[180] | 8057.837 | 3622.160 | 0.417 |

The following table shows the values of the median of the length of the CIs divided by the median of each sample

$$m_1 = \text{median}\left(\frac{q_i(0.975) - q_i(0.025)}{q_i(0.5)}\right),$$

the median of the length of the CIs divided by the mean of each sample

$$m_1 = \text{median}\left(\frac{q_i(0.975) - q_i(0.025)}{sample_mean}\right),$$

as well as the median of the length of the CIs divided by the median of the medians of the sample

$$m_3 = \frac{\text{median}(q_i(0.975) - q_i(0.025))}{\text{median}(q_i(0.5))}.$$

and (if applicable) the median of the length of the CIs divided by the true value

$$m_4 = \frac{\text{median}(q_i(0.975) - q_i(0.025))}{\text{true value}}.$$

| | m_1 | m_2 | m_3 |
|---------------------------|-------|------|-------|
| theta[1] | 0.98 | 1.26 | 1.71 |
| theta[2] | 8.49 | 4.38 | 8.43 |
| theta[3] | 1.04 | 1.31 | 1.75 |
| m0 | 4.44 | 3.25 | 4.45 |
| sigma | 0.21 | 0.21 | 0.22 |
| scale | 5.44 | 3.35 | 5.44 |
| offset | 0.11 | 0.11 | 0.12 |
| t0 | 0.03 | 0.03 | 0.03 |
| $prod_theta2_m0$ | 25.97 | 6.79 | 25.27 |
| $prod_theta2_scale$ | 28.79 | 7.32 | 28.29 |
| $prod_m0_scale$ | 20.86 | 6.45 | 21.37 |
| $prod_theta2_m0_scale$ | 0.06 | 0.06 | 0.06 |
| x2_sim[180] | 25.94 | 6.77 | 26.11 |