```
variables
x, y
i, n
          indicies
                       ::=
                                                                            expressions
                               proc pat \rightarrow cmd
                                                                           patterns
pat
                       ::=
binds
                                                                           bindings
                       ::=
α, β, σ, τ
                                                                            types
                                                                               variables
                                                                               application
                               \tau_1 \ \tau_2
                              \tau_1 \rightarrow \dots \rightarrow \tau_n
\forall x. \ \tau
                                                                               functions
                                                                               quantification
                                                                               promoted nil
                               \tau_1 ': ... ': \tau_n
                                                                               promoted cons
Γ, Δ
                                                                           contexts
                               Ø
                               \Gamma_1, \ldots, \Gamma_n
                                                                               concatenation
                                                                            commands
cmd
                               e_1 \rightarrow e_2
                                                                                arrow application (first-order)
                               e_1 \prec\!\!\!\prec e_2
                                                                                arrow application (higher-order)
                               if e then cmd_1 else cmd_2
                                                                               branching
                               case e of { alts }
                                                                               case analysis
                               let binds in cmd
                                                                               local binding
                               \lambda pat \rightarrow cmd
                                                                               command abstraction
                               cmd e
                                                                               command application
                               (e \ cmd_1 \dots cmd_n)
                                                                               control operator
                               do { stmt; cmd }
                                                                               sequencing
alts
                               \overline{pat_i \rightarrow cmd_i}^i
stmt
                                                                           statements
                       ::=
                               let binds
                               pat \leftarrow cmd
                       pattern typing
pat :: \tau \Rightarrow \Delta
                    binding typing
binds \Rightarrow \Delta
                  expression typing
\Gamma \vdash e :: \tau
                                            pat :: \tau_1 \Rightarrow \Delta
                                      \frac{\Gamma \mid \Delta \vdash_{\alpha} cmd :: '[] \rightharpoonup \tau_{2}}{\Gamma \vdash \mathbf{proc} \ pat \rightarrow cmd :: \alpha \ \tau_{1} \ \tau_{2}} \quad \mathsf{Expr\_Proc}
```

command typing

 $\Gamma \mid \Delta \vdash_{\alpha} cmd :: \sigma \rightharpoonup \tau \mid$ 

$$\begin{array}{c} \Gamma \vdash e_1 :: \alpha \left( \operatorname{STK} \llbracket \beta ' : \sigma \rrbracket \right) \tau \\ \hline \Gamma, \Delta \vdash e_2 :: \beta \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \dashv e_2 :: \sigma \rightharpoonup \tau \end{array} \end{array} \quad \mathsf{CMD\_APPF} \\ \hline \Gamma, \Delta \vdash e_1 :: \alpha \left( \operatorname{STK} \llbracket \beta ' : \sigma \rrbracket \right) \tau \\ \hline \Gamma, \Delta \vdash_{e_1} :: \beta \\ \hline \Gamma, \Delta \vdash_{e_2} :: \beta \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \dashv e_2 :: \sigma \rightharpoonup \tau \end{array} \quad \mathsf{CMD\_APPH} \\ \hline \Gamma | \Delta \vdash_{\alpha} cmd :: (\beta ' : \sigma) \rightharpoonup \tau \\ \hline \Gamma, \Delta \vdash_{e} :: \beta \\ \hline \Gamma | \Delta \vdash_{\alpha} cmd e :: \sigma \rightharpoonup \tau \end{array} \quad \mathsf{CMD\_APPC} \\ \hline pat :: \beta \Rightarrow \Delta_2 \\ \hline \Gamma | \Delta_1, \Delta_2 \vdash_{\alpha} cmd :: \sigma \rightharpoonup \tau \\ \hline \Gamma | \Delta \vdash_{\alpha_1} (\mathsf{ENV} \llbracket x, \sigma_1 \rrbracket) \tau_i \stackrel{i}{\rightarrow} \alpha \left( \mathsf{ENV} \llbracket x, \sigma_1 \rrbracket \right) \tau_1 \\ \hline \Gamma | \Delta \vdash_{\alpha_1} cmd_i :: \sigma_i \rightharpoonup \tau_i \stackrel{i}{\rightarrow} \tau \right) \\ \hline \Gamma | \Delta \vdash_{\alpha_1} (\mathsf{e} \, \overline{cmd_i}^i \mid) :: \sigma_1 \rightharpoonup \tau_1 \\ \hline binds \Rightarrow \Delta_2 \\ \hline \Gamma | \Delta_1, \Delta_2 \vdash_{\alpha} cmd :: \vdash [] \rightharpoonup \tau \\ \hline \Gamma | \Delta_1 \vdash_{\alpha} \mathsf{let} \, binds \, \mathbf{in} \, cmd :: \vdash [] \rightharpoonup \tau \\ \hline \Gamma | \Delta_1 \vdash_{\alpha} \mathsf{let} \, binds \, \mathbf{in} \, cmd :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta_1, \Delta_i \vdash_{\alpha} cmd_i :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta_1, \Delta_i \vdash_{\alpha} cmd_i :: \vdash [] \rightharpoonup \tau \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{case} \, e \, \mathsf{of} \, \{ \, \overline{pat_i} \rightarrow cmd_i^i \, \} :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{if} \, e \, \mathsf{then} \, cmd_1 :: \vdash [] \rightharpoonup \tau \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{in} \, cmd :: \vdash [] \rightharpoonup \tau \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{in} \, cmd :: \vdash [] \rightharpoonup \tau \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{cmd} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{cmd} \, :: \vdash [] \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \mathsf{do} \, \{ \, \mathsf{let} \, binds \, \mathsf{let} \, binds \, \mathsf{let} \, binds \, \mathsf{let} \, binds \, \mathsf$$

Definition rules: 11 good 0 bad Definition rule clauses: 35 good 0 bad