

Problem 1: Holiday Planning

To compute the maximum number of attractions one can visit a dynamic programming approach is used.

The function

```
fn holiday_planning(its: Vec<Vec<usize>>, c: usize, d:usize) -> usize
```

takes as parameters:

- `itineraries`: the `c` itineraries, one for each of the `c` cities that may be visited
- `c`: the number of cities
- `d`: the number of days available

and it iteratively computes the maximum number of attractions.

The function behaves as follows:

- create the dynamic programming array `asf` (acronym for *attractions so far*)
 - `asf[i]` is the maximum number of attractions seen up to the day `i`
- we initialize `asf` as the prefix sum array of the first city
- for each itinerary:
 - create the array `asf_curr_city`, which is the prefix sum of attractions that can be seen in the current city
 - create the array `curr_asf`, which is the dynamic programming array that will be built considering the current city as a possible destination
 - for each day `day`
 - for the number of days (`prev_days`) before the current day (`day`)
 - we compute the maximum number of attractions, considering the current city, setting `curr_asf[day]` as the maximum between
 - `curr_asf[day]`: maximum number of attractions seen if there are no days spent in the current city
 - `asf_curr_city[prev_days] + asf[day - prev_days]`
 - `asf_curr_city[prev_days]`: max number of attractions seen in the current city if `prev_days` are spent there
 - `asf[day - prev_days]`: max number of attractions seen the remaining days up to the day `day` in the previous "optimal" city
 - `asf = curr_asf`: "update" the dynamic programming array with the newly computed one

Time Complexity: $O(\text{cities} \cdot \text{days}^2)$

- three nested loops:
 - the outer loop iterates over each itinerary (one for each city)
 - the middle loop iterates over each day `day` from 0 to the number of available days
 - the inner loop iterates from 0 to `day`

Space Complexity: $O(\text{days})$

- three support arrays (`asf`, `curr_asf`, `asf_curr_city`) of length `days + 1` are used

Problem 2: Design Course

To compute the maximum number of topics that can be taught in a course an adaptation to the solution of the "Longest Increasing Subsequence" is employed.

The function:

```
fn design_a_course(mut topics: Vec<(u32, u32)>) -> u32
```

takes as a parameter the array of topics, represented as pairs `(beauty, difficulty)` and returns the solution.

The function behaves as follows:

- sort the topics by their beauty
- computes the longest increasing subsequence by the difficulty, using dynamic programming:
 - define the array `lis`, where `lis[i]` is the *LIS* of the prefix `[0..i-1]` of the array
 - for each current topic *i*
 - for each topic *j* that comes before the topic *i*
 - check if:
 - the current topic *i* is harder than the topic *j* (the pedagogical constraint)
 - the current topic *i* is more interesting than the topic *j* (the students "pickiness" constraint)
 - the *LIS* of topics that ends with the topic *i* is smaller than the *LIS* of topics that ends in *j* plus the topic *i* (DP recurrence)
 - then `lis[i] = lis[j] + 1`
 - return the maximum value in `lis`

Time Complexity: $O(n^2)$

- Two nested loops: the outer loop runs for each topic, and the inner loop compares the current topic with all previous topics
 - inside the inner loop is performed a constant-time operation

Space Complexity: $O(n)$

- use an additional array of length n , `lis`, to compute the result