Practice Midterm 2, MA 351 Section: Summer 2016

Name: PUID: Exam

No calculators may be used on this exam.

Problem	Possible	Points
Number	Points	Earned
I	50pts	
II	25pts	
III	25pts	
Total Points	100pts	

I (50pts)

Answer the following questions by clearly circling your answers. No partial credit is awarded for the questions in Part I

(1) Consider the subspace of $\mathbb{C}^{4\times 1}$:

What is the dimensions of W^{\perp} ?

- (a) 0
- (b) 1
- (c) 2
- (d) 3
- (e) 4

(2) Suppose **A** is 3×5 matrix such that Rank**A** = 3. Which of the following statement is TRUE? (circle all that applies)

- (a) The rank of \mathbf{A}^{\top} is 5
- (b) The dimensions of the null space of \mathbf{A}^{\top} is 2
- (c) $\mathbf{A} \cdot \mathbf{x} = \mathbf{0}$ only admit as a solution the trivial solution
- (d) The rows of ${\bf A}$ are linearly dependent
- (e) The columns of **A** are linearly dependent

(3) The dimension of the vector space of all 4×4 Hermitian matrices is

- (a) 12
- (b) 16
- (c) 10
- (d) 8
- (e) 6

(4) Let ${\bf A}$ be a 7×3 matrix such that its null space is spanned by the

vectors

$$\left(\begin{array}{c}1\\2\\0\end{array}\right),\,\left(\begin{array}{c}2\\1\\0\end{array}\right),\,\left(\begin{array}{c}1\\-1\\0\end{array}\right)$$

consequently the rank of A is

- (a) 1
- (b) 2
- (c) 3
- (d) 4
- (e) 6

(6) Consider the linear system

$$\left(\begin{array}{cc} 1 & a \\ 2 & a^2 - 3 \end{array}\right) \cdot \left(\begin{array}{c} x_1 \\ x_1 \end{array}\right) = \left(\begin{array}{c} 2 \\ \frac{a+5}{2} \end{array}\right).$$

Determine all values of the parameter a for which the linear system above has NO solutions.

- (a) $a = \pm \sqrt{3}$
- (b) a = -5
- (c) a = -3
- (d) a = 3
- (e) $a \neq 3$
- (f) none of the above

II (25pts)

Find the least square solution

$$\begin{pmatrix} 1 & -3 & 5 \\ 2 & 0 & 4 \\ 3 & 1 & 5 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{pmatrix} 1 \\ 4 \\ 9 \end{pmatrix}.$$

Show all your work in detail and clarity.

Answer:

III (25pts)

Let $\mathbf{A} \in \mathbb{C}^{n \times n}$ having distinc eigenvalues, give a detail of proof of the fact that the eigenvector must be linearly independent.

