

Time Difference of Arrival Localization Testbed: Development, Calibration, and Automation

GRCon 2017

**Intelligent Digital Communications
Georgia Tech VIP Team**



Overview

- Introduction
 - IDC Team
 - Stadium Testbed
- RFSN Control Center (RFSNCC)
 - Why?
 - How?
- Lab Setup and ToA Calibration
 - Why?
 - Experiment Setup
 - Results



Introduction

Hayden Flinner

IDC Team Purpose

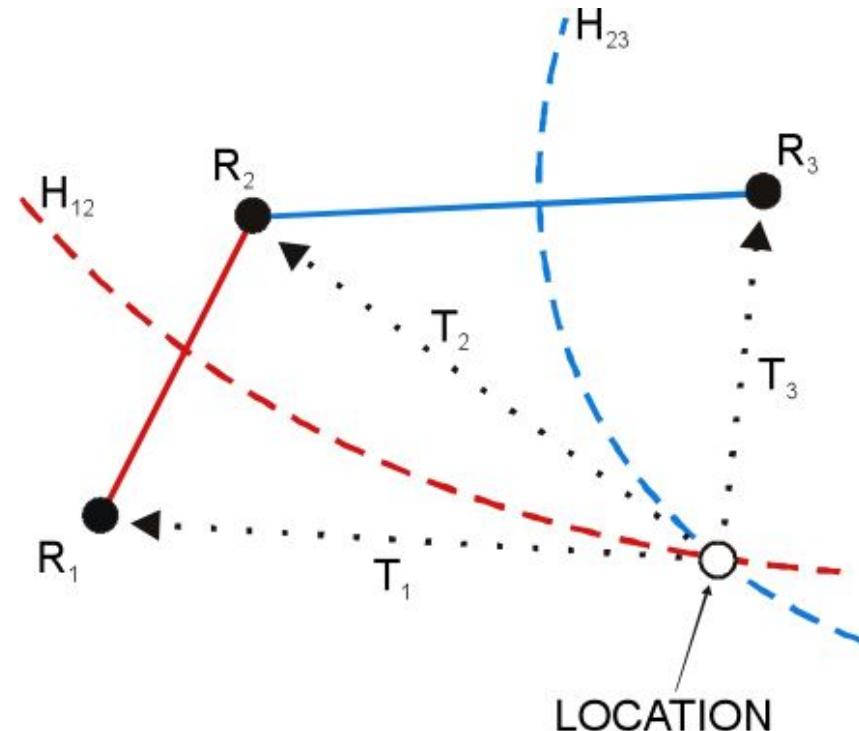
- IDC is using software defined radio to enhance spectrum utilization
 - Radio frequency (RF) spectrum is a valuable, limited resource
 - Analyzing how devices interact over RF spectrum allows us to find ways to improve communication in an optimal manner

Localization

- Using SDR to develop localization algorithms for Extreme Emitter Density environments (10k-100k people/km²)
- Recorded terabytes of time synchronous RF IQ data, during football games, at the GT football stadium to assist in algorithm development

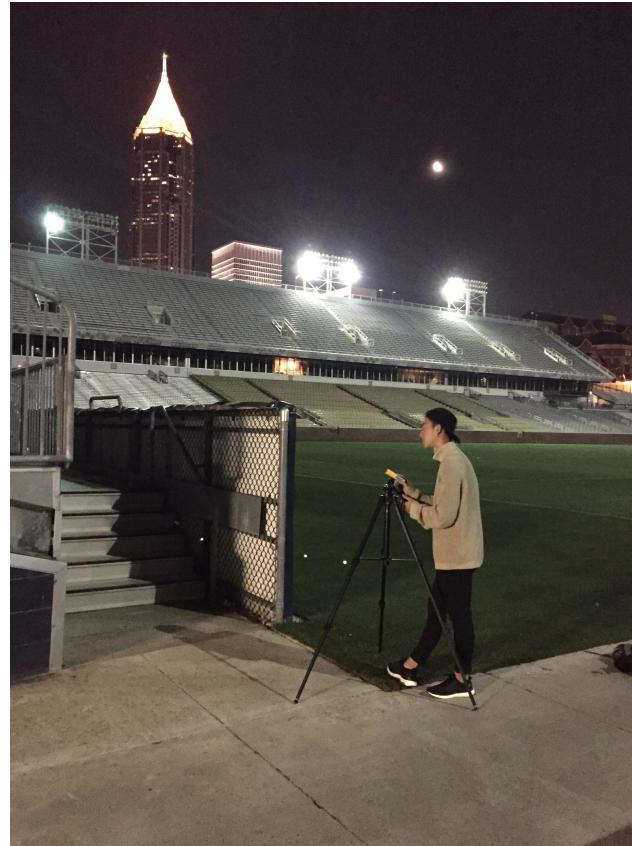
TDoA Localization

- Assuming time-synced nodes:
 - Record ToAs
 - Take differences
 - Apply $\Delta d = c\Delta t$

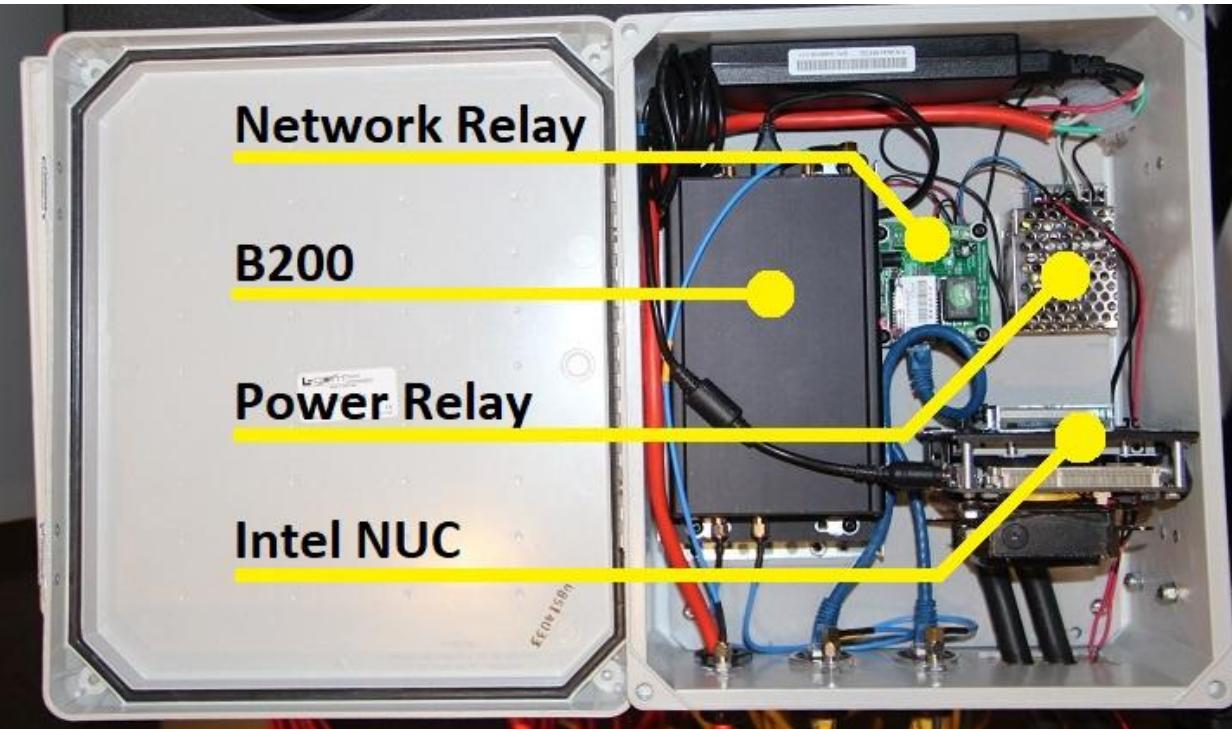


Stadium Testbed

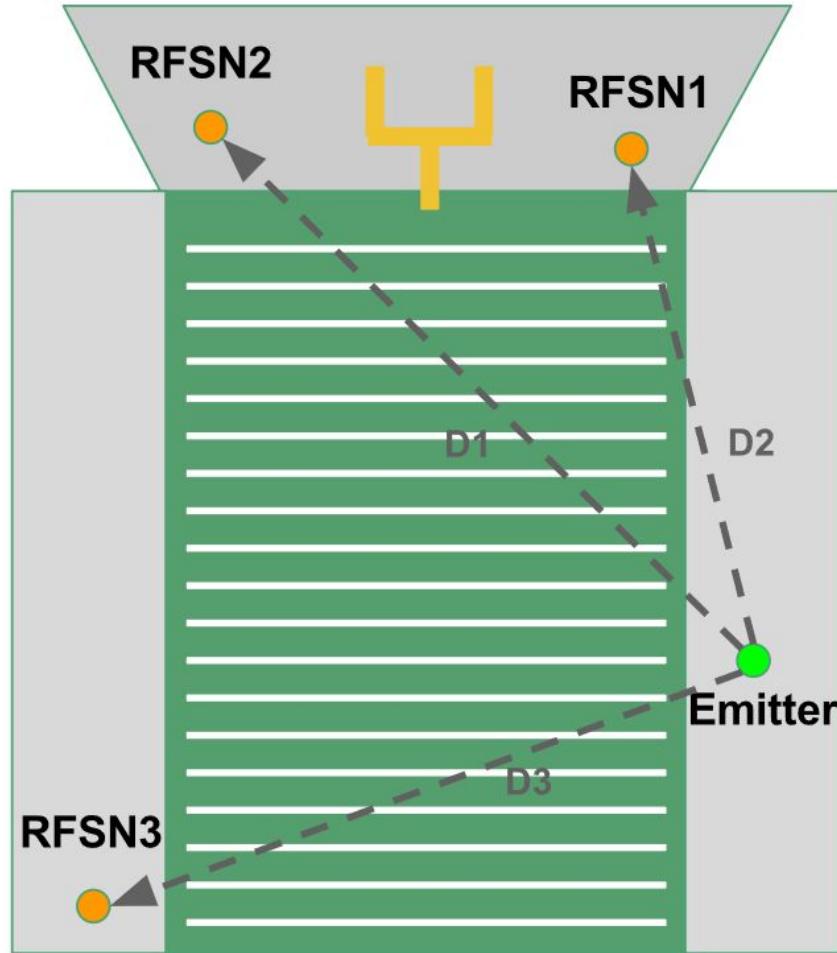
Hayden Flinner



RF Sensor Node (RFSN)



Stadium Testbed



2 Mobile Nodes



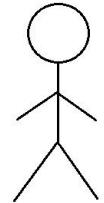


RFSN Control Center (RFSNCC)

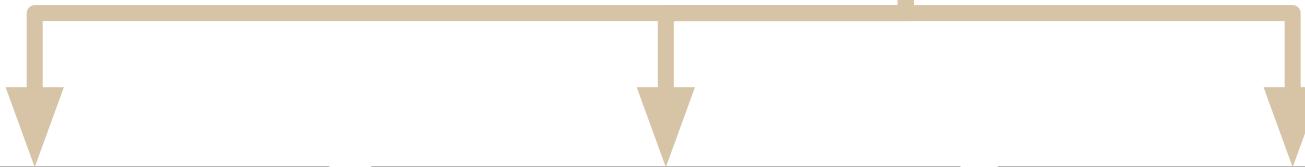
Why RFSNCC?

1. Currently 3 fixed nodes - Goal 10+
2. Logging into each machine and running long series of time-synced record commands is not scalable
 - a. Excessive man-hours
 - b. Error-prone
3. Maintaining RF IQ dataset and associated metadata is tedious

Initial Plan



Upload Schedule



RFSN1

RFSN2

...

Current Site

CSV Scheduling

[CSV Formatting Reference](#)

Choose File No file chosen

Schedule Recording Form

| Session Name | Starting Path (/path/) | Log Name (test.log) | Start Early (sec) | Sample Rate (samples/sec) |
|--------------|------------------------|---------------------|-------------------|---------------------------|
| Spring17Test | /spring17/test/ | log.txt | 60 | 25e6 |

RFSN Node 1 RFSN Node 2 RFSN Node 3

Time Offset (min)

5

| Date | Time | Length (sec) | Gain (db) | Frequency (hz) |
|------------|----------|--------------|-----------|----------------|
| 04/21/2017 | 03:00 AM | 5 | 55 | 2.4E+9 |
| 04/21/2017 | 03:05 AM | 5 | 55 | 2.4E+9 |
| 04/21/2017 | 03:10 AM | 5 | 55 | 2.4E+9 |
| 04/21/2017 | 03:15 AM | 5 | 55 | 2.4E+9 |
| 04/21/2017 | 03:20 AM | 5 | 55 | 2.4E+9 |

Current Site

RFSNS

| RFSN | Power | Status |
|-------------|-------------------------------------|-------------------------------------|
| RFSN Node 1 | RFSN Node 1: ON/OFF | Click to see Status |
| RFSN Node 2 | RFSN Node 2: ON/OFF | Click to see Status |
| RFSN Node 3 | RFSN Node 3: ON/OFF | Click to see Status |

Architecture



ANGULARJS
by Google

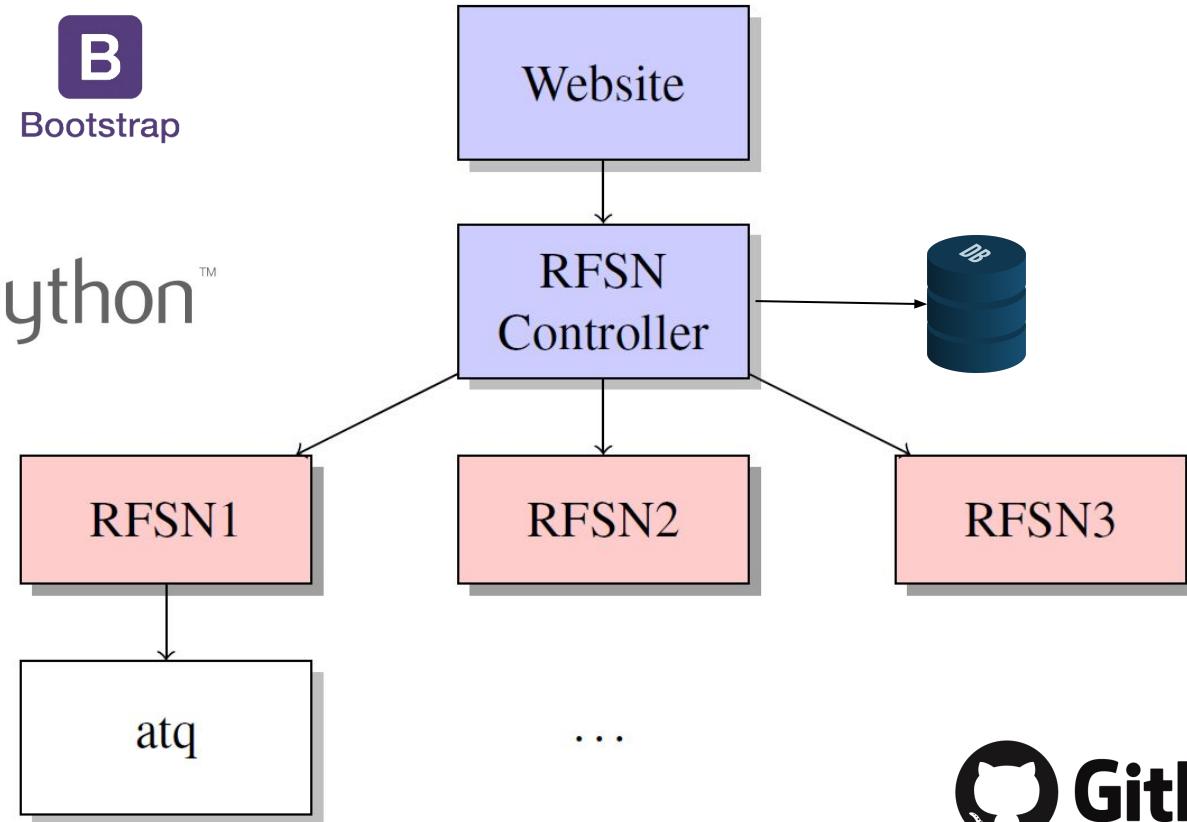
B
Bootstrap

django

python™



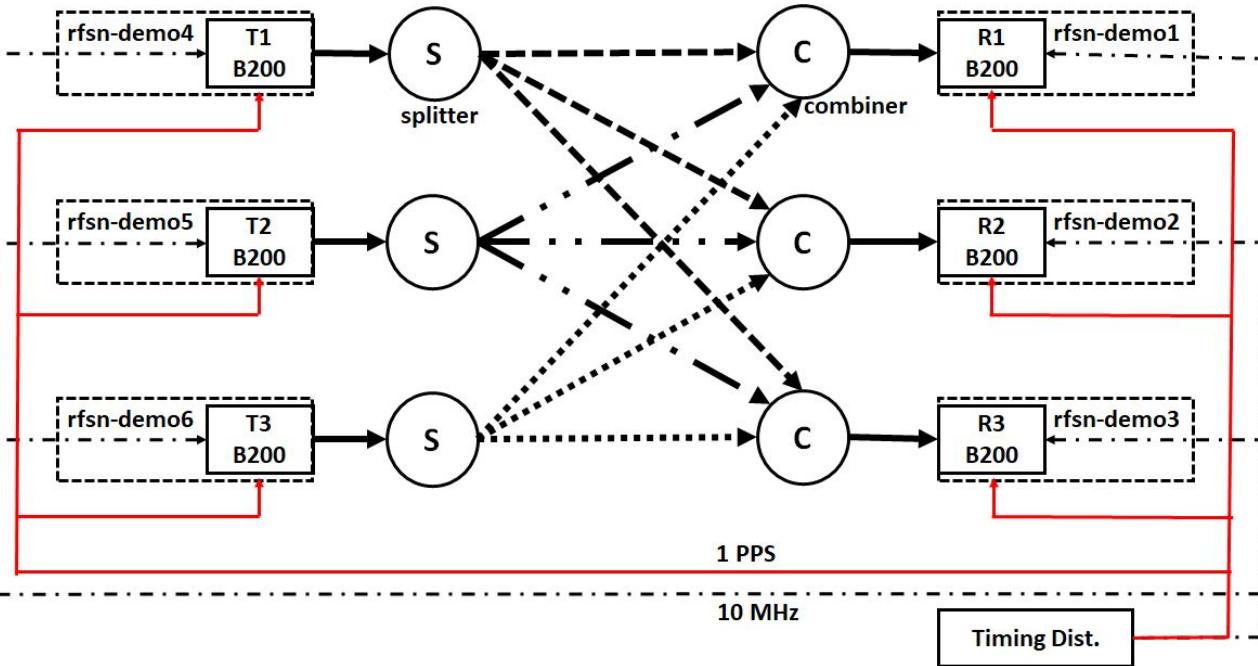
ubuntu





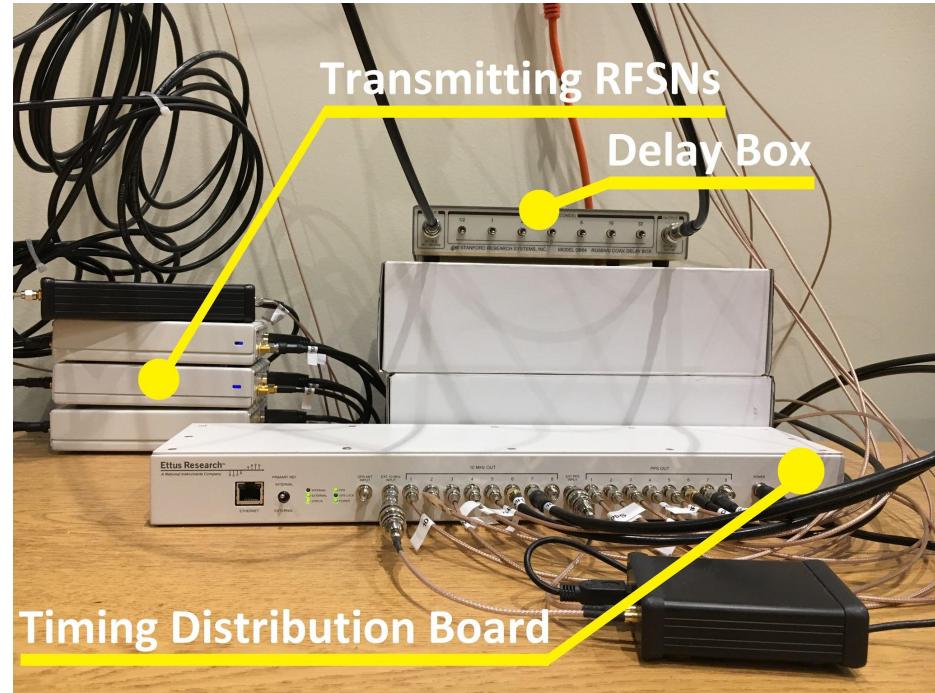
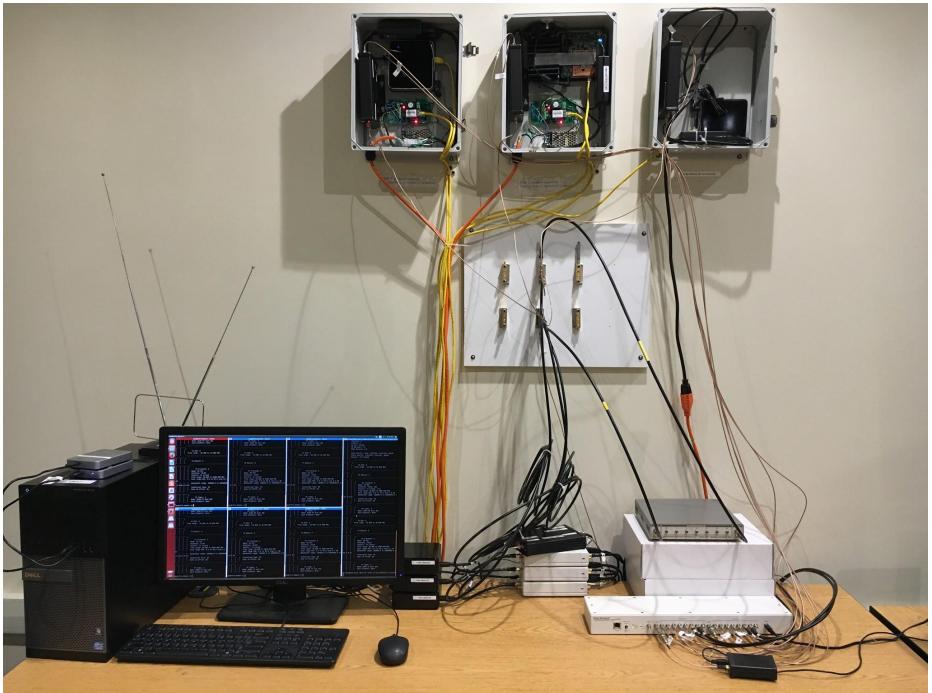
Lab Setup and ToA Calibration

Why a Lab Testbed?



- Wired nodes provide controlled test environment.
- Easier to vary cable lengths to test emitter/receiver positions than to run around stadium

Lab Testbed



Why Calibration Experiment?

- Verify that ToAs being recorded are plausible
- Remove delay inherent to USRPs for more accurate location measurements

Cramer-Rao Lower Bound (CRLB)

- CRLB for the standard deviation of the TDoA is theoretic limit on how accurate results can be

$$\sigma^2(\hat{t}_2 - \hat{t}_1) \geq \frac{1}{4\pi^2(SNR_{linear})\beta_{rms}^2} \quad (s^2)$$

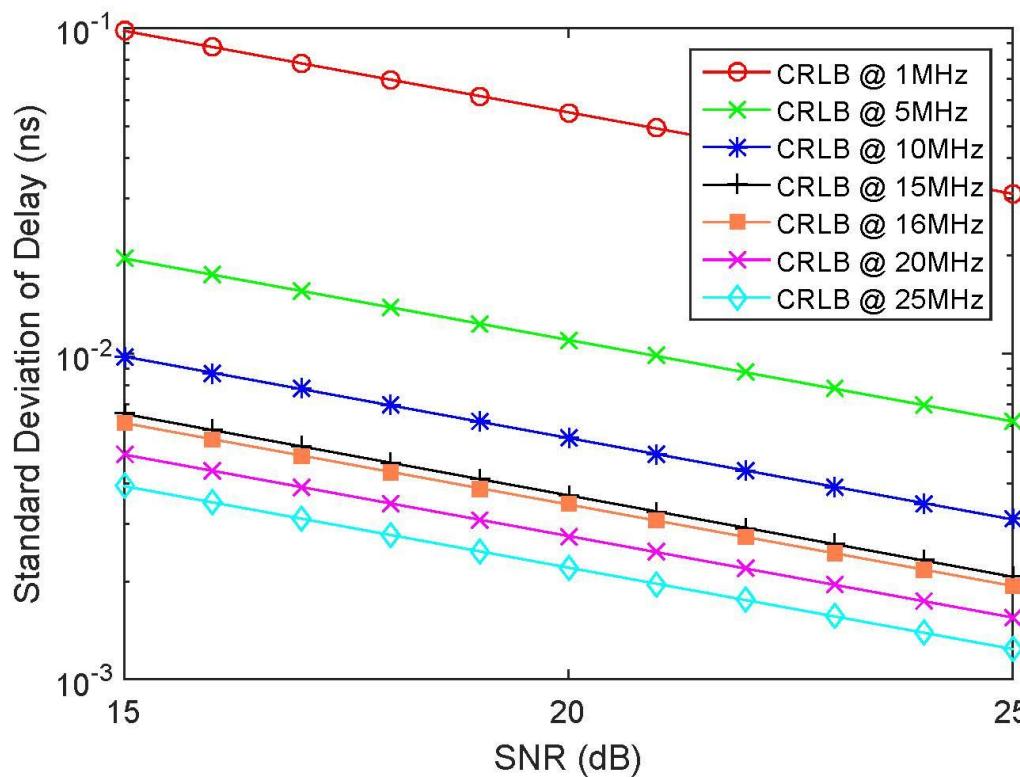
$$\beta_{rms} = \frac{\beta}{\sqrt{12}} \quad \begin{aligned} \beta &\text{ is the BW} \\ \hat{t}_n &\text{ is the unknown ToA at sensor } i \end{aligned}$$

$$SNR_{linear} = 10^{\frac{SNR_{dB}}{10}}$$

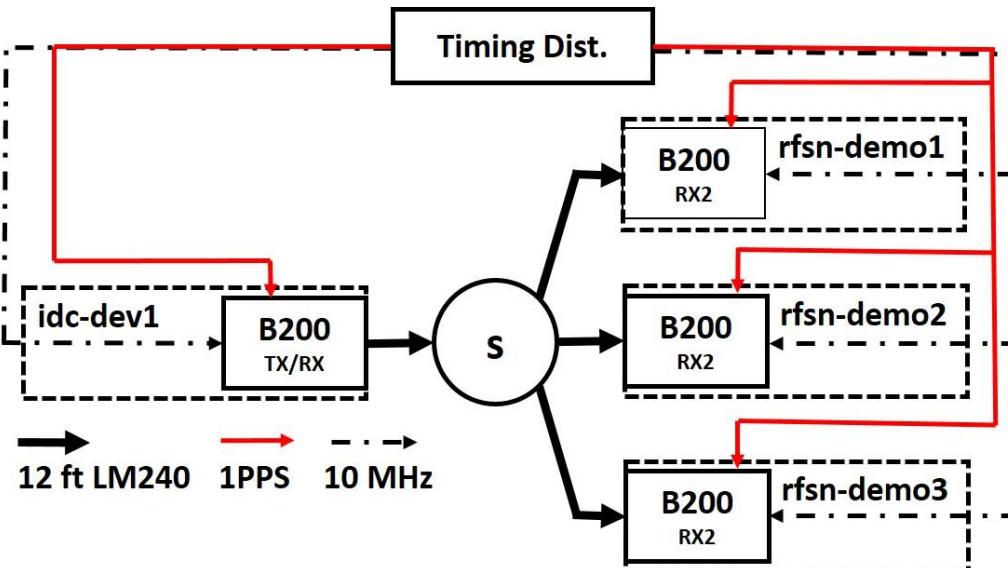
$$SNR_{dB} = 10 \log_{10} \left(\frac{\sum |X_i|^2}{\sigma_{noise}^2} \right)$$

Cramer-Rao Lower Bound (CRLB)

Relationship between CRLB and bandwidth



Q: Does our testbed give us sane results?

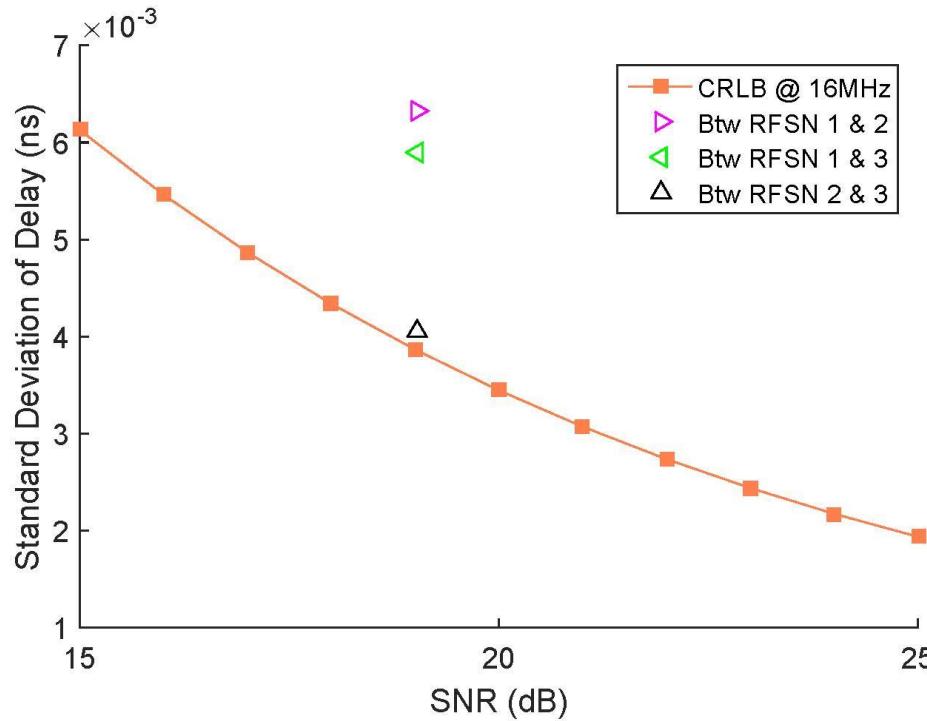


| TDoA -> | Btw 1 & 2 | Btw 1 & 3 | Btw 2 & 3 |
|-----------------------------|-----------|-----------|-----------|
| Mean (ns) | 18.228 | 26.440 | 8.213 |
| Variance (ns ²) | 4.004E-5 | 3.478E-5 | 1.644E-5 |
| Std Dev (ns) | 6.327E-3 | 5.898E-3 | 4.054E-3 |
| MSE (ns ²) | 7.241E-5 | 3.506E-5 | 5.508E-5 |
| SNR (dB) | 79.904 | 80.279 | 80.279 |

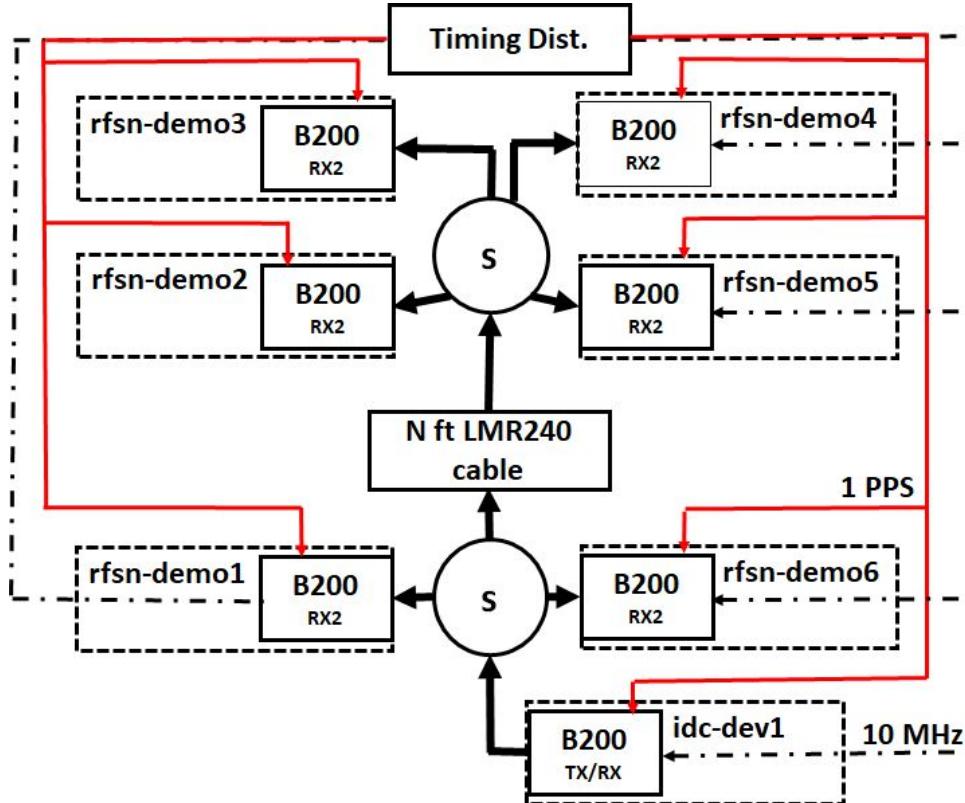
- TX sampling rate: 16 Msps
- RX sampling rate: 16 Msps with 32 MHz master clock.

A: Yes! Std. Devs. above CRLB!

SD of TDoA data plotted against its CRLB at 16 MHz sampling bandwidth



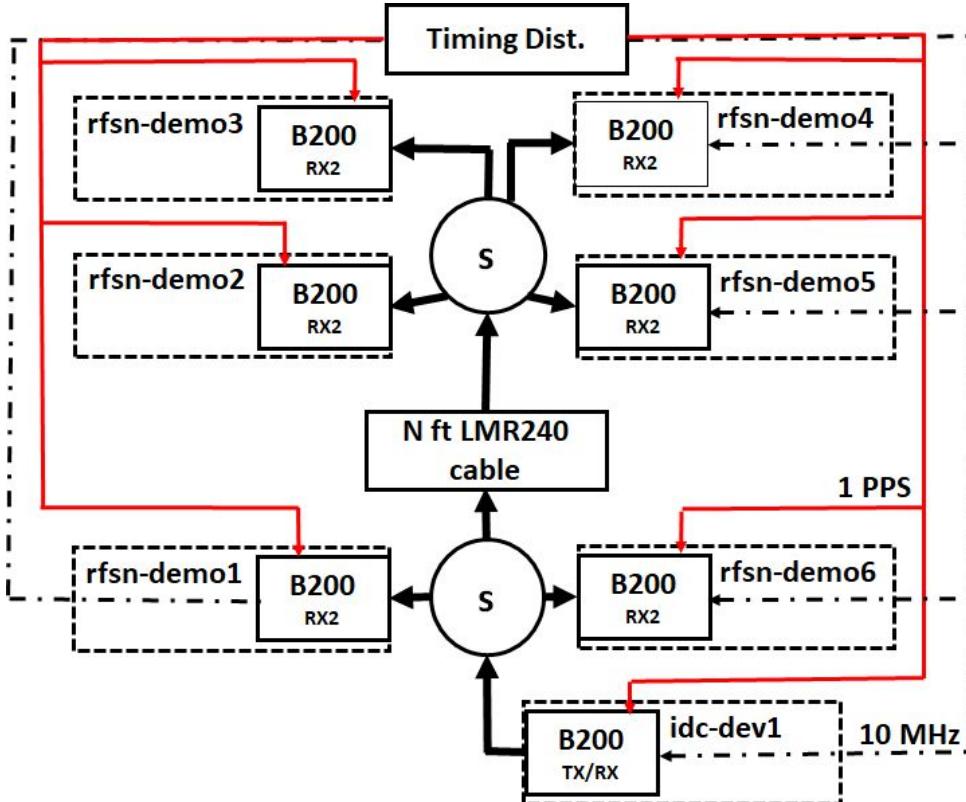
Calibration: Testbed Setup



- Nodes 2, 3, 4, and 5 were passed delayed signal sequence.
- Nodes 1 and 6 received non-delayed signal sequence.

TX: 25 Msps -- RX: 25 Msps, 50 MHz master clock.

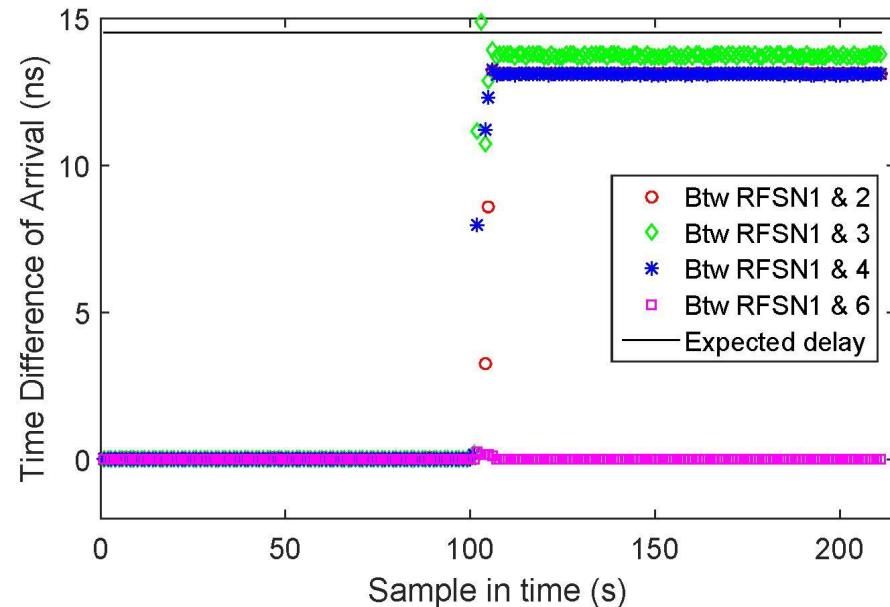
Calibration: Running Experiment



TX: 25 Msps -- RX: 25 Msps, 50 MHz master clock.

- LMR-240 cables of known lengths were attached 110 seconds into each recording session.
- For each node, average ToAs seen during first 100 seconds was subtracted from ToA vector during each recording session.
- Used magnitude interpolation around the cross-correlation peak value to compute ToA estimate.

Time Difference of Arrival over 12 ft LMR240 cable

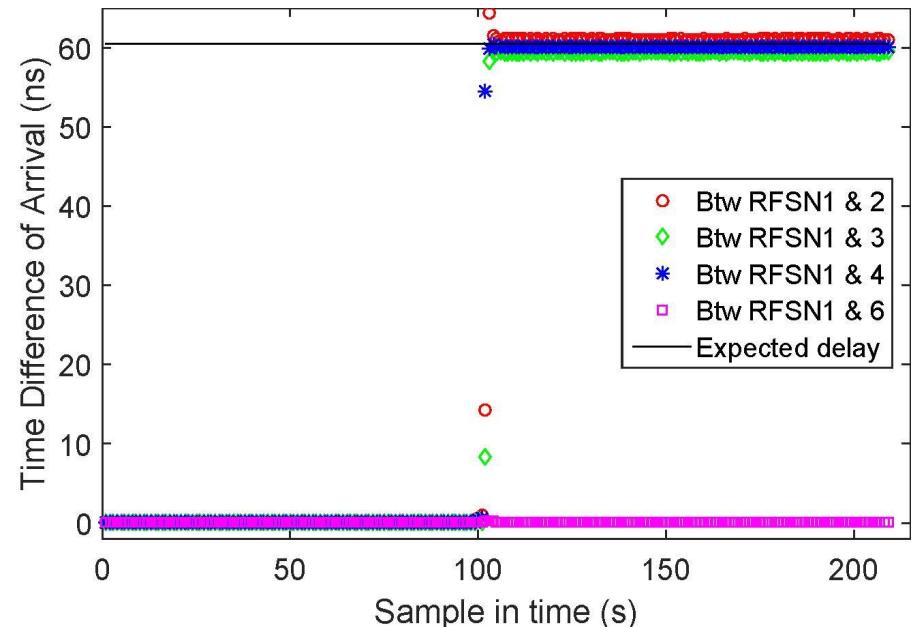


| TDoA -> | Btw 1 & 2 | Btw 1 & 3 | Btw 1 & 4 | Btw 1 & 6 |
|-----------------------------|-----------|-----------|-----------|-----------|
| Mean (ns) | 13.0750 | 13.7267 | 13.1034 | 0.0242 |
| Variance (ns ²) | 1.8990E-1 | 9.5577E-3 | 6.6974E-3 | 3.0686E-4 |
| Std Dev (ns) | 0.4358 | 0.0978 | 0.0818 | 0.0175 |
| MSE (ns ²) | 2.2976E-0 | 6.4481E-1 | 2.0323E-0 | 8.9917E-4 |

Results are of average TDoA vector from four runs

- Expected delay through 12 ft LMR240 cable is: $12 \text{ ft} / 0.8262 \text{ ft/ns} = 14.5243 \text{ ns}$

Time Difference of Arrival over 50 ft LMR240 cable

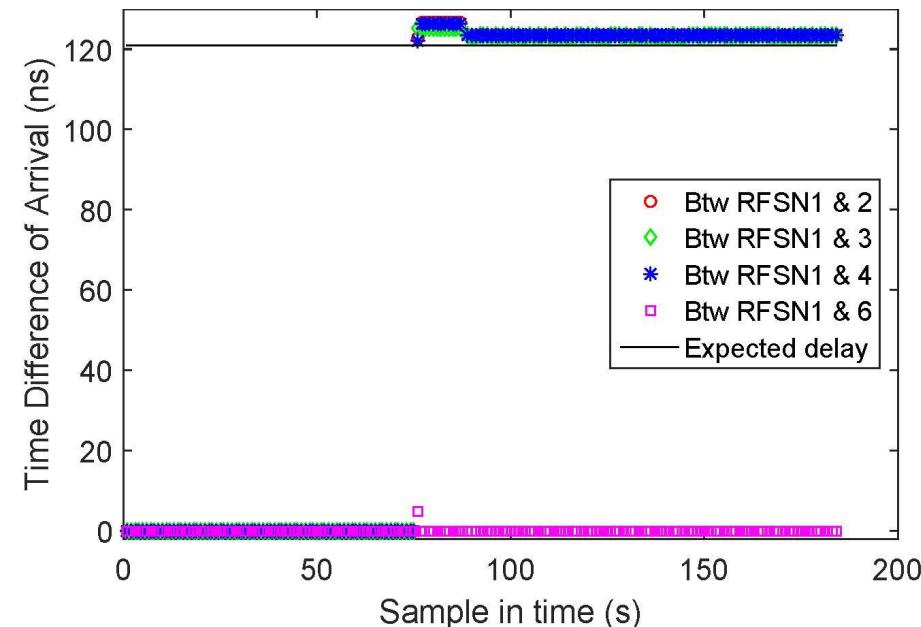


| TDoA -> | Btw 1 & 2 | Btw 1 & 3 | Btw 1 & 4 | Btw 1 & 6 |
|-----------------------------|-----------|-----------|-----------|-----------|
| Mean (ns) | 61.0461 | 59.4250 | 60.1079 | 0.0035 |
| Variance (ns ²) | 1.9459E-4 | 6.0374E-4 | 3.7281E-5 | 4.1453E-6 |
| Std Dev (ns) | 0.0139 | 0.0246 | 0.0061 | 0.0020 |
| MSE (ns ²) | 3.0133E-1 | 1.1676E-0 | 1.5527E-1 | 1.6303E-5 |

Results are of average TDoA vector from four runs

- Expected delay through 12 ft LMR240 cable is: $50 \text{ ft} / 0.8262 \text{ ft/ns} = 60.5181 \text{ ns}$

Time Difference of Arrival over 100 ft LMR240 cable

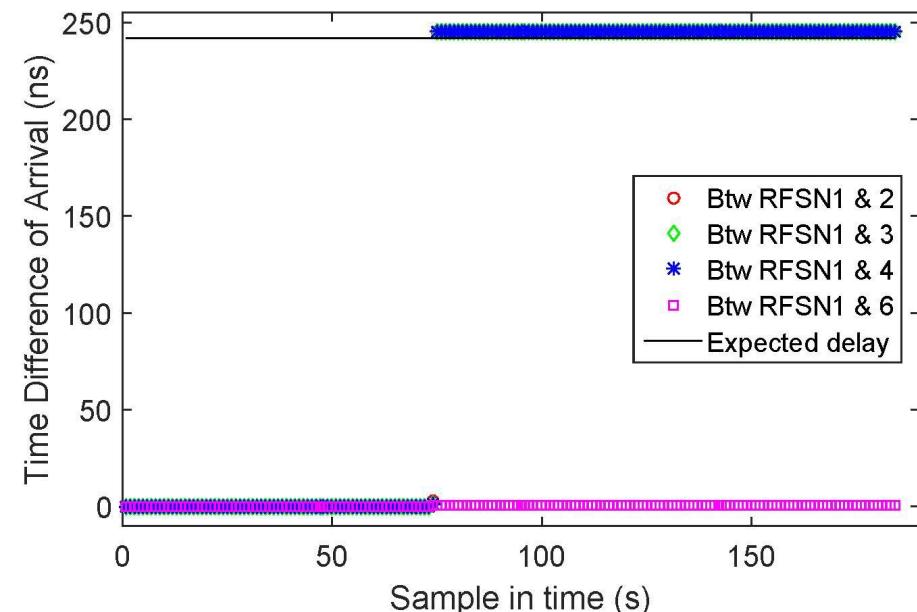


| TDoA -> | Btw 1 & 2 | Btw 1 & 3 | Btw 1 & 4 | Btw 1 & 6 |
|-----------------------------|-----------|-----------|-----------|-----------|
| Mean (ns) | 121.7498 | 123.1022 | 122.7003 | 0.4180 |
| Variance (ns ²) | 5.6723E-4 | 1.0220E-3 | 1.3408E-4 | 9.6546E-5 |
| Std Dev (ns) | 0.0238 | 0.0320 | 0.0116 | 0.0098 |
| MSE (ns ²) | 0.5706 | 4.4814 | 2.9312 | 0.1772 |

Results are of average TDoA vector from four runs

- Expected delay through 100 ft LMR240 cable: $100 \text{ ft} / 0.8262 \text{ ft/ns} = 121.0361 \text{ ns}$

Time Difference of Arrival over 200 ft LMR240 cable



| TDoA -> | Btw 1 & 2 | Btw 1 & 3 | Btw 1 & 4 | Btw 1 & 6 |
|-----------------------------|-----------|-----------|-----------|-----------|
| Mean (ns) | 244.9814 | 245.0107 | 245.1557 | 0.8586 |
| Variance (ns ²) | 1.7674E-4 | 2.5461E-4 | 1.2964E-5 | 9.3918E-6 |
| Std Dev (ns) | 0.0133 | 0.0160 | 0.0036 | 0.0031 |
| MSE (ns ²) | 8.9707 | 9.1476 | 10.0497 | 0.7439 |

Results are of average TDoA vector from four runs

- Expected delay through 200 ft LMR240 cable: $200 \text{ ft} / 0.8262 \text{ ft/ns} = 242.0722 \text{ ns}$

Wrapping Up

- Experiments show our timing variance on 4 different cable lengths (with 4 trials apiece) match expectations
- RFSNCC allows us to schedule and collect data easily
- Already collected relatively large (40TB) dataset from stadium

Contact

Github Repo - <http://bit.ly/2vlgQBQ>

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ToA Calculation

- Simple parabolic interpolation

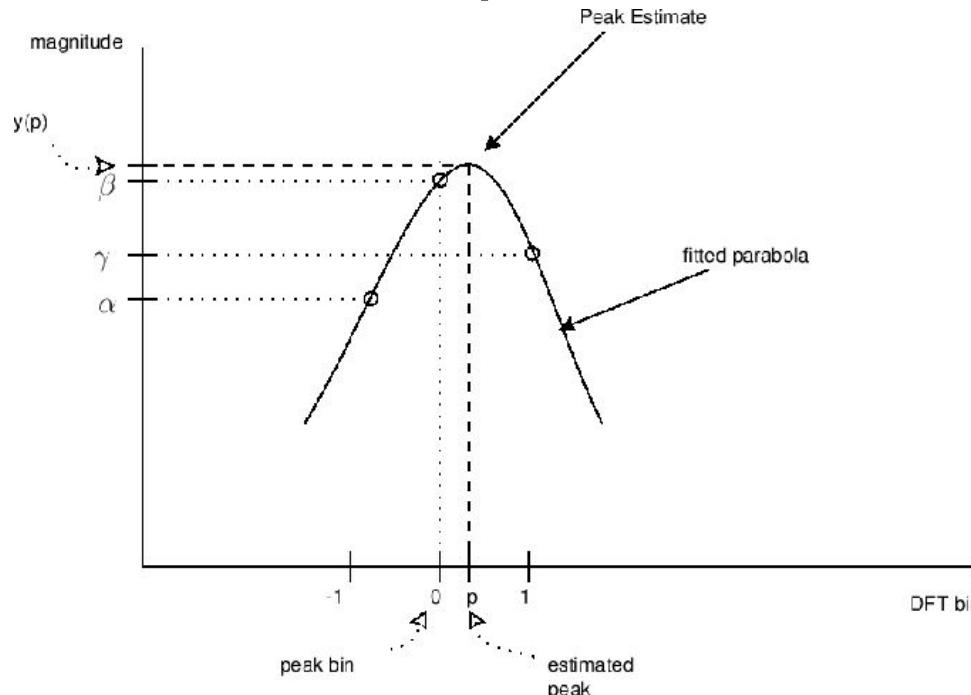


Figure 12.1: Illustration of parabolic peak interpolation using the three samples nearest the peak.