UNIVERSITY OF SYDNEY STAT2011 Statistical Models

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Semester 1 2012 Lecturer: Michael Stewart

Tutorial Week 7

- 1. Complete any unfinished work from the week 6 tutorial.
- 2. If gene frequencies are in Hardy-Weinberg equilibrium, the genotypes AA, Aa and aa occur with $Bin(2, \theta)$ probabilities. Suppose that genotypes are determined for a sample of 190 people, with observed frequencies of each as shown below:

$$\begin{array}{c|cccc} AA & Aa & aa \\ \hline 10 & 68 & 112 \\ \end{array}$$

Letting x_i equal the number of a's in the genotype of individual i, we model the original data x_1, x_2, \ldots, x_n as values taken by n = 190 independent $Bin(2, \theta)$ random variables. The table above is a summary of the original data.

- (a) Compute three estimates of θ , based on the counts above:
 - i. $\hat{\theta}_1 = \frac{1}{2}\bar{x}$ where \bar{x} is the mean of the original data;
 - ii. $\hat{\theta}_0 = 1 \sqrt{n_0/n}$ where n_0 is the observed number of zeroes (i.e. of AA's);
 - iii. $\hat{\theta}_2 = \sqrt{n_2/n}$ where n_2 is the observed number of twos (i.e. of aa's).
- (b) Obtain standard errors for each estimate obtained above (see Lecture 20).