

The missing link: discerning true from false negatives when sampling species interaction networks

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Abstract: Ecosystems are composed of networks of interacting species. These interactions allow communities of species to persist through time through both neutral and adaptive processes. Still a robust understanding of (and ability to predict and forecast) interactions among species remains elusive. This knowledge-gap is largely driven by a shortfall of data—although species occurrence data has rapidly increased in the last decade, species interaction data has not kept pace, largely due to the intrinsic difficulty and effort required to sample interactions. These sampling challenges bias data and hinder inferences about the structure and dynamics of interactions networks. Here, we demonstrate the realized false-negative rate (the percentage of species that actually interact but for which we do not yet have a record) can be quite high, even in thoroughly sampled systems, due to the intrinsic variation in abundances across species in a community. We illustrate how a null model of occurrence detection can be used to estimate the false-negative rate in a given dataset. One hypothesis is that interactions between “rare” species are themselves rare because these species are less likely to encounter one-another than species of higher relative abundance. However, we demonstrate that across several datasets of spatial or temporally replicated networks, there are positive associations that suggest these interactions actually exist but just are not observed. Finally, we assess how false negatives influence various models of network prediction, and recommend directly accounting for observation error in predictive models. We conclude by discussing how the understanding of false-negatives can inform how we design monitoring schemes for species interactions.

1 Introduction

2 Species interactions drive many processes in evolution and ecology. A better understanding of species
3 interactions is an imperative to understand the evolution of life on Earth, to mitigate the impacts of
4 anthropogenic change on biodiversity (Makiola *et al.* 2020), and for predicting zoonotic spillover of
5 disease to prevent future pandemics (Becker *et al.* 2021). At the moment we lack sufficient data to meet
6 these challenges (Poisot *et al.* 2021), largely because species interactions are hard to sample (Jordano
7 2016). Over the past few decades biodiversity data has become increasingly available through remotely
8 collected data and adoption of open data practices (Kenall *et al.* 2014; Stephenson 2020). Still, interaction
9 data remains relatively scarce because sampling typically requires human observation. This induces a
10 constraint on the amount, spatial scale, and temporal frequency of resulting data that it is feasible to
11 collect by humans. Many crowdsourced methods for biodiversity data aggregation (e.g. GBIF, eBird) still
12 relies on automated identification of species, which does not easily generalize to interaction sampling.
13 There is interest in using remote methods for interaction sampling, which primarily detect co-occurrence
14 and derive properties like species avoidance from this data (Niedballa *et al.* 2019). However, this itself is
15 not necessarily indicative of an interaction (Blanchet *et al.* 2020). This is an example of semantic
16 confusion around the word “interaction”—for example one might consider competition a type of species
17 interaction, even though it is marked by a lack of co-occurrence between species, unlike other types of
18 interactions, like trophism or pollination, which require both species to be together at the same place and
19 time. Here we consider interaction in the latter sense, where two species have fitness consequences on
20 one-another if (and only if) they are in the sample place at the same time. In addition, here we only
21 consider direct (not higher-order) interactions.

22 We cannot feasibly observe all (or even most) of the interactions that occur in an ecosystem. This means
23 we can be confident two species actually interact if we have a record of it (given an estimate of species
24 misidentification probability), but not at all confident that a pair of species *do not* interact if we have *no*
25 *record* of those species observed together. In other words, it is difficult to distinguish *true-negatives* (two
26 species never interact) from *false-negatives* (two species interact sometimes, but we do not have a record of
27 it). For a concrete example of a false-negative in a food web, see fig. 1. Because even the most highly
28 sampled systems will still contain missing interactions, there is increasing interest in combining
29 species-level data (e.g. traits, abundance, range, phylogenetic relatedness, etc.) to build models to predict

30 interactions between species we haven't observed together before (Strydom *et al.* 2021). However, the
31 noise of false-negatives could impact the efficacy of our predictive models and have practical
32 consequences for answering questions about interactions (de Aguiar *et al.* 2019). This data constraint is
33 amplified as the interaction data we have is geographically biased toward the usual suspects (Poisot *et al.*
34 2021). We therefore need a statistical approach to assessing these biases in the observation process and
35 their consequences for our understanding of interaction networks.

36 The importance of *sampling effort* and its impact on resulting ecological data has produced a rich body of
37 literature. The recorded number of species in a dataset or sample depends on the total number of
38 observations (Walther *et al.* 1995; Willott 2001), as do estimates of population abundance (Griffiths 1998).
39 This relationship between sampling effort and spatial coverage and species detectability. This has
40 motivated more quantitatively robust approaches to account for error in sampling data in many contexts:
41 to determine if a given species is extinct (Boakes *et al.* 2015), to determine sampling design (Moore &
42 McCarthy 2016), and to measure species richness across large scales (Carlson *et al.* 2020). In the context of
43 interactions, an initial concern was the compounding effects of limited sampling effort combined with the
44 amalgamation of data (across both study sites, time of year, and taxonomic scales) could lead any
45 empirical set of observations to inadequately reflect the reality of how species interact (Paine 1988) or the
46 structure of the network as a whole (Martinez *et al.* 1999; McLeod *et al.* 2021). Martinez *et al.* (1999)
47 showed that in a plant-endophyte trophic network, network connectance is robust to sampling effort, but
48 this was done in the context of a system for which observation of 62,000 total interactions derived from
49 164,000 plant-stems was feasible. In some systems (e.g. megafauna food-webs) this many observations is
50 either impractical or infeasible due to the absolute abundance of the species in question.

51 The intrinsic properties of ecological communities create several challenges for sampling: first, species are
52 not observed with equal probability—we are much more likely to observe a species of high abundance
53 than one of very low abundance (Poisot *et al.* 2015). Canard *et al.* (2012) presents a null model of food-web
54 structure where species encounter one-another in proportion to each species' relative-abundance. This
55 assumes that there are no associations in species co-occurrence due to an interaction (perhaps because
56 this interaction is “important” for both species; Cazelles *et al.* (2016)), but in this paper we later show
57 increasing strength of associations leads to increasing probability of false-negatives in interaction data,
58 and that these positive associations are rampant in existing network data. Second, observed co-occurrence
59 is often equated with meaningful interaction strength, but this is not necessarily the case (Blanchet *et al.*

2020)—a true “non-interaction” would require that neither of two species, regardless of whether they co-occur, ever exhibit any meaningful effect on the fitness of the other. So, although co-occurrence is not directly indicative of an interaction, it is a precondition for an interaction.

Here, we illustrate how our confidence that a pair of species never interacts highly depends on sampling effort. We suggest that surveys of species interactions can benefit from simulation modeling of the sampling process. We demonstrate how the realized false-negative rate of interactions is related to the relative abundance of the species pool, and use simulation to produce a null estimate of the false-negative rate given total sampling effort (the total count of all individuals of all species seen), and to introduce a method for introducing uncertainty into model predictions of interaction probability to account for observation error. We then show that positive associations in co-occurrence data can increase the realized number of false-negatives, and demonstrate these positive associations are rampant in network datasets, and conclude by recommending that the simulation of sampling effort and species occurrence can and should be used to help design surveys of species interaction diversity (Moore & McCarthy 2016), and by advocating use of null models like those presented here as a tool for both guiding design of surveys of species interactions and for modeling detection error in predictive models.

[Figure 1 about here.]

Accounting for false-negatives in species interactions

How many observations of a non-interaction do we need to be confident it's a true negative?

We start with a naive model of interaction detection: we assume that every interacting pair of species is incorrectly observed as not-interacting with an independent and fixed probability, which we denote p_{fn} and subsequently refer to as the False-Negative Rate (FNR). If we observe the same species not-interacting N times, then the probability of a true-negative (denoted p_{tn}) is given by $p_{tn} = 1 - (p_{fn})^N$. This relation (the probability-mass-function of geometric distribution, a special case of the negative-binomial distribution) is shown in fig. 2(A) for varying values of p_{fn} and illustrates a fundamental link between our ability to reliably say an interaction doesn't exist— p_{tn} —and the number of times N we have observed a

86 given species. In addition, note that there is no non-zero p_{fn} for which we can ever *prove* that an
 87 interaction does not exist—no matter how many observations of non-interactions N we have, $p_{tn} < 1$.
 88 From fig. 2(A) it is clear that the more often we see two species co-occurring, but *not interacting*, the more
 89 likely the interaction is a true-negative. This has several practical consequences: first it means negatives
 90 taken outside the overlap of the range of each species aren't informative because co-occurrence was not
 91 possible, and therefore neither was an interaction. Second, we can use this relation to compute the
 92 expected number of total observations needed to obtain a “goal” number of observations of a particular
 93 pair of species (fig. 2(B)). As an example, if we hypothesize that A and B do not interact, and we want to see
 94 species A and B both co-occurring and *not interacting* 10 times to be confident this is a true negative, then
 95 we need an expected 1000 observations of all species if the relative abundances of A and B are both 0.1.
 96 Because the true FNR is latent, we can never actually be sure what the actual number of false negatives in
 97 our data—however, we can use simulation to estimate it for datasets of a given size using neutral models
 98 of observation. If some of the “worst-case” FNRs presented in fig. 2(A) seem unrealistically high, consider
 99 that species are observed in proportion to their relative abundance. In the next section we demonstrate
 100 that the distribution of abundance in ecosystems can lead to very high realized values of FNR (p_{fn}) simply
 101 as an artifact of sampling effort.

102 [Figure 2 about here.]

103 **False-negatives as a product of relative abundance**

104 We now show that the realized FNR changes drastically with sampling effort due to the intrinsic variation
 105 of the abundance of individuals of each species within a community. We do this by simulating the process
 106 of observation of species interactions, applied both to 243 empirical food webs from the Mangal database
 107 (Banville *et al.* 2021) and random food-webs generated using the niche model, a simple generative model
 108 of food-web structure that accounts for allometric scaling (Williams & Martinez 2000). Our neutral model
 109 of observation assumes each observed species is drawn in proportion to each species' abundance at that
 110 place and time. The abundance distribution of a community can be reasonably-well described by a
 111 log-normal distribution (Volkov *et al.* 2003). In addition to the log-normal distribution, we also tested the
 112 case where the abundance distribution is derived from power-law scaling $Z^{(\log(T_i)-1)}$ where T_i is the
 113 trophic level of species i and Z is a scaling coefficient (Savage *et al.* 2004), which yields the same

114 qualitative behavior. The practical consequence of abundance distributions spanning many orders of
115 magnitude of abundance is that observing two “rare” species interacting requires two low probability
116 events: observing two rare species *at the same time*.

117 To simulate the process of observation, for an ecological network M with S species, we sample abundances
118 for each species from a standard-log-normal distribution. For each true interaction in the adjacency
119 matrix M (i.e. $M_{ij} = 1$) we estimate the probability of observing both species i and j at a given place and
120 time by simulating n observations of all individuals of any a species, where the species of the individual
121 observed at the $\{1, 2, \dots, n\}$ -th observation is drawn from the generated log-normal distribution of
122 abundances. For each pair of species (i, j) , if both i and j are observed within the n -observations, the
123 interaction is tallied as a true positive if $M_{ij} = 1$. If only one of i or j are observed—but not both—in these
124 n observations, but $M_{ij} = 1$, this is counted as a false-negative, and a true-negative otherwise. For each
125 pair of species (i, j) , if both i and j are observed within the n -observations, the interaction is tallied as a
126 true positive if $M_{ij} = 1$. If only one of i or j are observed—but not both—in these n observations, but
127 $M_{ij} = 1$, this is counted as a false-negative, and a true-negative otherwise ($M_{ij} = 0$).

128 In fig. 2(C) we see this model of observation applied to niche model networks across varying levels of
129 species richness, and in fig. 2(D) the observation model applied to Mangal food webs. For all niche model
130 simulations in this manuscript, for a given number of species S the number of interactions is drawn from
131 the flexible-links model fit to Mangal data (MacDonald *et al.* 2020), effectively drawing the number of
132 interactions L for a random niche model food-web as

$$L \sim \text{BetaBinomial}(S^2 - S + 1, \mu\phi, 1 - \mu\phi)$$

133 where the MAP estimate of (μ, ϕ) applied to Mangal data from (MacDonald *et al.* 2020) is
134 ($\mu = 0.086$, $\phi = 24.3$). All simulations were done with 500 independent replicates of unique niche model
135 networks per unique number of observations n . All analyses presented here are done in Julia v1.8
136 (Bezanson *et al.* 2015) using both EcologicalNetworks.jl v0.5 and Mangal.jl v0.4 (Banville *et al.* 2021) and
137 are hosted on [Github](#)). Note that the empirical data, for the reasons described above, very likely already
138 contains many false negatives, we’ll revisit this issue in the final section.

139 From fig. 2(C) it is evident that the number of species considered in a study is inseparable from the
140 false-negative rate in that study, and this effect should be taken into account when designing samples of

ecological networks in the future. We see a similar qualitative pattern in fig. 2(D) where the FNR drops off quickly as a function of observation effort, mediated by total richness. The practical consequence of the bottom row of fig. 2 is whether the total number of observations of all species (the x-axis) for the threshold FNR we deem acceptable (the y-axis) is feasible. This raises two points: first, empirical data on interactions are subject to the practical limitations of funding and human-work hours, and therefore existing data tend to fall on the order of hundreds or thousands observations of individuals per site. Clear aggregation of data on sampling effort has proven difficult to find and a meta-analysis of network data and sampling effort seems both pertinent and necessary, in addition to the effects of aggregation of interactions across taxonomic scales (Gauzens *et al.* 2013; Giacomuzzo & Jordán 2021). This inherent limitation on in-situ sampling means we should optimize where we sample across space so that for a given number of samples, we obtain the maximum information possible. Second, what is meant by “acceptable” FNR? This raises the question: does a shifting FNR lead to rapid transitions in our ability inference and predictions about the structure and dynamics of networks, or does it produce a roughly linear decay in model efficacy? We explore this in the next section.

We conclude this section by advocating for the use of neutral models similar to above to generate expectations about the number of false-negatives in a data set of a given size. This could prove fruitful both for designing surveys of interactions but also because we may want to incorporate models of imperfect detection error into predictive interactions models, as Joseph (2020) does for species occurrence modeling. Additionally, we emphasize that one must consider the context for sampling—is the goal to detect a particular species (as in fig. 2(C)), or to get a representative sample of interactions across the species pool? These arguments are well-considered when sampling individual species (Willott 2001), but have not yet been adopted for designing samples of communities.

Including observation-error in interaction predictions

Here we show how to incorporate imperfect observation (both false-negatives and false-positives) into model predictions of interaction probability. Models for interaction prediction typically yield a probability of interaction between each pair of species. When these are considered with uncertainty, it is usually model-uncertainty, e.g. the variance in the interaction probability prediction across several cross-validation folds, where the data is split into training and test sets several times. Here we introduce a method for resampling interaction probabilities (outlined in figure fig. 3) that simulates the observation

process with prior estimates of both false-negative and false-positive probabilities to produce an output distribution of interaction probabilities that accounts for observation error. We implement this in the software package InteractionUncertaintySampler.jl.

[Figure 3 about here.]

We do this by using the process for simulating a distribution of null false-negative rates for a given dataset as described above (fig. 3 (A)). We then consider the output prediction from an arbitrary prediction model, which is the probability p_{ij} that two species i and j interact. To get an estimate of p_{ij} that accounts for observation error, we resample the probability of each interaction p_{ij} by simulating a series of particles. Each particle is the product of the resampling algorithm (“Resampling” within fig. 3 (B)), where the value of a particle is first drawn from a Bernoulli with weight p_{ij} , and if that value is true, the value remains true with probability $1 - p_{fn}$, and if the first draw is false, the value remains false with probability $1 - p_{fp}$. Over many samples of particles, the resulting frequency of ‘true’ outcomes is a single resample of the interaction probability p_{ij}^* . Across many resamples, this forms a distribution of probabilities which are adjusted by the true and false negative rates.

There is also an analytic way to represent this.

Normal approximation to binomial, as the total number of samples from n_p particles approaches infinity, the sum of total successes across all particles approaches a normal distribution with parameters

$$\mathcal{N}\left(n_p p_{ij}, \sqrt{n_p p_{ij}(1 - p_{ij})}\right)$$

Corrected p_{ij} based on p_{fn} and p_{fp} as $p_{ij}^* = p_{ij}(1 + p_{fp})(1 - p_{fn})$

$$\mathcal{N}\left(n_p p_{ij}^*, \sqrt{n_p p_{ij}^*(1 - p_{ij}^*)}\right)$$

and then by normalizing back to (0, 1).

$$\mathcal{N}\left(p_{ij}^*, \sqrt{\frac{p_{ij}^*(1 - p_{ij}^*)}{n_p}}\right)$$

We can then further truncate this, although in practice probability mass outside (0,1) is extremely loss.

190 Number of particles n_p as a uncertainty width. Nautral analogue to number of observations of
191 co-occurrence.

192 As an example case study, we use a boosted-regresssion-tree to predict interactions in a host-parasite
193 network (Hadfield *et al.* 2014) (with features derived in the same manner as Strydom *et al.* (2021) derives
194 features on this data) to produce a set of interaction predictions. We then applied this method to a set of a
195 few resampled interaction probabilities between mammals and parasite species shown in figure fig. 3 (C).
196 Here we implement a simple resampling algorithm, but this could be extended, for example by adjusting
197 the expected FNR for each pair of species by the relative abundance of each species. We have implemented
198 a general framework for this resampling methodology in the Julia package
199 InteractionUncertaintySampler.jl, which enables flexible choices for priors on false-negative and
200 false-positive rates.

201 This method allows us to more effectively represent our uncertainty about observation error in predictions
202 of species interactions. This also has implications for what we mean by ‘uncertainty’ in interaction
203 predictions. A model’s prediction can be ‘uncertain’ in two different ways: the model’s predictions may
204 have high variance, or the model’s predictions may be centered around a probability of interaction of 0.5,
205 where we are the most unsure about whether this interaction exists. Improving the incorporation of
206 different forms of uncertainty in probabilistic interaction predictions seems a necessary next step toward
207 understanding what pairs of species we know the least about, in order to prioritize sampling to provide the
208 most new information possible.

209 **Positive associations in co-occurrence increase the false-negative rate**

210 The model above doesn’t consider the possibility that there are positive or negative associations which
211 shift the probability of species cooccurrence together due to their interaction (Cazelles *et al.* 2016).
212 However, here we demonstrate that the probability of observing a false negative can be higher if there is
213 some positive association in the occurrence of species A and B . If we denote the probability that we
214 observe the co-occurrence of two species A and B as $P(AB)$ and if there is no association between the
215 marginal probabilities of observing A and observing B , denoted $P(A)$ and $P(B)$ respectively, then the
216 probability of observing their co-occurrence is the product of the marginal probabilities for each species,
217 $P(AB) = P(A)P(B)$. In the other case where there is some positive strength of association between

218 observing both A and B because this interaction is “important” for each species, then the probability of
 219 observation both A and B , $P(AB)$, is greater than $P(A)P(B)$ as $P(A)$ and $P(B)$ are not independent and
 220 instead are positively correlated, i.e. $P(AB) > P(A)P(B)$. In this case, the probability of observing a single
 221 false-negative in our naive model from fig. 2(A) is $p_{fn} = 1 - P(AB)$, which due to the above inequality
 222 implies $p_{fn} > 1 - P(A)P(B)$. This indicates an increasingly greater probability of a false negative as the
 223 strength of association gets stronger, $P(AB) \rightarrow P(AB) \gg P(A)P(B)$. However, this still does not consider
 224 variation in species abundance in space and time (Poisot *et al.* 2015). If positive or negative associations
 225 between species structure variation in the distribution of $P(AB)$ across space/time, then the
 226 spatial/temporal biases induced by data collection would further impact the realized false negative rate, as
 227 the probability of false negative would not be constant for each pair of species across sites.

228 To test for these positive associations in data we scoured Mangal for datasets with many spatial or
 229 temporal replicates of the same system. For each dataset, we compute the marginal probability $P(A)$ of
 230 occurrence of each species A across all networks in the dataset. For each pair of interacting species A and
 231 B , we then compute and compare the probability of co-occurrence if each species occurs independently,
 232 $P(A)P(B)$, to the empirical joint probability of co-occurrence, $P(AB)$. Following our analysis above, if
 233 $P(AB)$ is greater than $P(A)P(B)$, then we expect our neutral estimates of the FNR above to underestimate
 234 the realized FNR. In fig. 4, we see the difference between $P(AB)$ and $P(A)P(B)$ for the seven suitable
 235 datasets with enough spatio-temporal replicates and a shared taxonomic backbone (meaning all
 236 individual networks use common species identifiers) found on Mangal to perform this analysis. Further
 237 details about each dataset are reported in tbl. 1.

238 In each of these datasets, the joint probability of co-occurrence $P(AB)$ is decisively greater than our
 239 expectation if species co-occur in proportion to their relative abundance $P(A)P(B)$. This suggests that
 240 there may not be as many “neutrally forbidden links” (Canard *et al.* 2012) as we might think, and that the
 241 reason we do not have records of interactions between rare species is probably due to observation error.
 242 This has serious ramifications for the widely observed property of nestedness seen in bipartite networks
 243 (Bascompte & Jordano 2007)—perhaps the reason we have lots of observations between generalists is
 244 because they are more abundant, and this is particularly relevant as we have strong evidence that
 245 generalism drives abundance (Song *et al.* 2022a), not vice-versa.

246 [Figure 4 about here.]

Table 1: This table describes the datasets used in the above analysis (Fig 2). The table reports the type of each dataset, the total number of networks in each dataset (N), the total species richness in each dataset (S), the connectance of each metaweb (all interactions across the entire spatial-temporal extent) (C), the mean species richness across each local network \bar{S} , the mean connectance of each local network \bar{C} , the mean β -diversity among overlapping species across all pairs of network species ($\bar{\beta}_{OS}$), and the mean β -diversity among all species in the metaweb ($\bar{\beta}_{WN}$). Both metrics are computed using KGL β -diversity (Koleff *et al.* 2003)

Network	Type	N	S	C	\bar{S}	\bar{C}	$\bar{\beta}_{OS}$	$\bar{\beta}_{WN}$
Kopelke <i>et al.</i> (2017)	Food Web	100	98	0.037	7.87	0.142	1.383	1.972
Thompson & Townsend (2000)	Food Web	18	566	0.014	80.67	0.049	1.617	1.594
Havens (1992)	Food Web	50	188	0.065	33.58	0.099	1.468	1.881
Ponisio <i>et al.</i> (2017)	Pollinator	100	226	0.079	23.0	0.056	1.436	1.870
Hadfield <i>et al.</i> (2014)	Host-Parasite	51	327	0.085	32.71	0.337	1.477	1.952
Closs & Lake (1994)	Food Web	12	61	0.14	29.09	0.080	1.736	1.864
CaraDonna <i>et al.</i> (2017)	Pollinator	86	122	0.18	21.42	0.312	1.527	1.907

The impact of false-negatives on network properties and prediction

Here, we assess the effect of false negatives on our ability to make predictions about interactions, as well as their effect on network structure. The prevalence of false-negatives in data is the catalyst for interaction prediction in the first place, and as a result methods have been proposed to counteract this bias (Stock *et al.* 2017; Poisot *et al.* 2022). However, it is feasible that the FNR in a given dataset is so high that it could induce too much noise for an interaction prediction model to detect the signal of possible interaction between species.

To test this we use the dataset from Hadfield *et al.* (2014) that describes host-parasite interaction networks sampled across 51 sites, and the same method as Strydom *et al.* (2021) to extract latent features for each species in this dataset based on applying PCA to the co-occurrence matrix. We then predict a metaweb (equivalent to predicting true or false for an interaction between each species pair, effectively a binary classification problem) from these species-level features using four candidate models for binary classification—three often used machine-learning (ML) methods (Boosted Regression Tree (BRT), Random Forest (RF), Decision Tree (DT)), and one naive model from classic statistics (Logistic Regression

(LR)). Each of the ML models are bootstrap aggregated (or bagged) with 100 replicates each. We partition the data into 80-20 training-test split, and then seed the training data with false negatives at varying rates, but crucially do nothing to the test data. We fit all of these models using MLJ.jl, a high-level Julia framework for a wide-variety of ML models (Blaom *et al.* 2020). We evaluate the efficacy of these models using two common measures of binary classifier performance: the area under the receiver-operator curve (ROC-AUC) and the area under the precision-recall curve (PR-AUC), for more details see Poisot (2022). Here, PR-AUC is slightly more relevant as it is a better indicator of prediction of false-negatives. The results of these simulations are shown in fig. 5(A&B).

[Figure 5 about here.]

One interesting result seen in fig. 5(A&B) is that the ROC-AUC value does not approach random in the same way the PR-AUC curve does as we increase the added FNR. The reason for this is that ROC-AUC is fundamentally not as useful a metric in assessing predictive capacity as PR-AUC. As we keep adding more false-negatives, the network eventually becomes a zeros matrix, and these models can still learn to predict “no-interaction” for all possible species pairs, which does far better than random guessing (ROC-AUC = 0.5) in terms the false positive rate (one of the components of ROC-AUC). This highlights a more broad issue of label class imbalance, meaning there are far more non-interactions than interactions in data. A full treatment of the importance of class-balance is outside the scope of this paper, but is explored in-depth in Poisot (2022).

Although these ML models are surprisingly performant at link prediction given their simplicity, there have been several major developments in applying deep-learning methods to many tasks in network inference and prediction—namely graph-representation learning (GRL, Khoshraftar & An (2022)) and graph convolutional networks (Zhang *et al.* 2019). At this time, these advances can not yet be applied to ecological networks because they require far more data than we currently have. We already have lots of features that could be used as inputs into these models (i.e. species level data about occurrence, genomes, abundance, etc.), but our network datasets barely get into the hundreds of local networks sampled across space and time (tbl. 1). Once we start to get into the thousands, these models will become more useful, but this can only be done with systematic monitoring of interactions. This again highlights the need to optimize our sampling effort to maximize the amount of information contained in our data given the expensive nature of sampling interactions.

290 We also consider how the FNR affects network properties. In fig. 5(C) we see the mean trophic level across
291 networks simulated using the niche model (as above), across a spectrum of FNR values. In addition to the
292 clear dependence on richness, we see that mean trophic level, despite varying widely between niche model
293 simulations, tends to be relatively robust to false negatives and does not deviate widely from the true value
294 until very large FNRs, i.e. $p_{fn} > 0.7$. This is not entirely unsurprising. Removing links randomly from a
295 food-web is effectively the inverse problem of the emergence of a giant component (more than half of the
296 nodes are in a connected network) in random graphs (see Li *et al.* (2021) for a thorough review). The
297 primary difference being that we are removing edges, not adding them, and thus we are witnessing the
298 dissolution of a giant component, rather than the emergence of one. Further applications of percolation
299 theory to the topology of ecological networks could improve our understanding of how false-negatives
300 impact the inferences about the structure and dynamics on these networks.

301 Discussion

302 Species interactions enable the persistence and functioning of ecosystems, but our understanding of
303 interactions is limited due to the intrinsic difficulty of sampling. Here we have provided a null model for
304 the expected number of false-negatives in an interaction dataset. We demonstrated that we expect many
305 false-negatives in species interaction datasets purely due to the intrinsic variation of abundances within a
306 community. We also, for the first time to our knowledge, measured the strength of association between
307 co-occurrence and interactions (Cazelles *et al.* 2016) across many empirical systems, and found that these
308 positive associations are both very common, and showed algebraically that they increase the realized FNR.
309 We have also shown that false-negatives could further impact our ability to both predict interactions and
310 infer properties of the networks, which highlights the need for further research into methods for
311 correcting this bias in existing data.

312 A better understanding of how false-negatives impact species interaction data is a practical
313 necessity—both for inference of network structure and dynamics, but also for prediction of interactions by
314 using species level information. False-negatives could pose a problem for many forms of inference in
315 network ecology. For example, inferring the dynamic stability of a network could be prone to error if the
316 observed network is not sampled “enough.” What exactly “enough” means is then specific to the
317 application, and should be assessed via methods like those here when designing samples. Further,

318 predictions about network rewiring (Thompson & Gonzalez 2017) due to range shifts in response to
319 climate change could be error-prone without accounting for interactions that have not been observed but
320 that still may become climatically infeasible. As is evident from fig. 2(A), we can never guarantee there are
321 no false-negatives in data. In recent years, there has been interest toward explicitly accounting for
322 false-negatives in models (Stock *et al.* 2017; Young *et al.* 2021), and a predictive approach to
323 networks—rather than expecting our samples to fully capture all interactions (Strydom *et al.* 2021). As a
324 result, better models for predicting interactions are needed for interaction networks. This includes
325 explicitly accounting for observation error (Johnson & Larremore 2021)—certain classes of models have
326 been used to reflect hidden states which account for detection error in occupancy modeling (Joseph 2020),
327 and could be integrated in the predictive models of interactions in the future.

328 This work has several practical consequences for the design of interaction samples. Simulating the process
329 of observation could be a powerful tool for estimating the sampling effort required by a study that takes
330 relative abundance into account, and provides a null baseline for expected FNR. It is necessary to take the
331 size of the species pool into account when deciding how many total samples is sufficient for an
332 “acceptable” FNR (fig. 2(C & D)). Further the spatial and temporal turnover of interactions means any
333 approach to sampling prioritization must be spatiotemporal. We demonstrated earlier that observed
334 negatives outside of the range of both species aren’t informative, and therefore using species distribution
335 models could aid in this spatial prioritization of sampling sites.

336 We also should address the impact of false-negatives on the inference of process and causality in
337 community ecology. We demonstrated that in model food webs, false-negatives do not impact the measure
338 of total trophic levels until very high FNR (figure fig. 5(C)), although we cannot generalize this further to
339 other properties. This has immediate practical concern for how we design what taxa to sample—does it
340 matter if the sampled network is fully connected? It has been shown that the stability of subnetworks can
341 be used to infer the stability of the metaweb paper beyond a threshold of samples (Song *et al.* 2022b). But
342 does this extend to other network properties? And how can we be sure we are at the threshold at which we
343 can be confident our sample characterizes the whole system? We suggest that modeling observation error
344 like we have done here can address these questions and aid in the design of samples of species
345 interactions. To try and sample to avoid all false-negatives is a fool’s errand. Species ranges overlap to form
346 mosaics, which themselves are often changing in time. Communities and networks don’t end in space,
347 and the interactions that connect species on the ‘periphery’ of a given network to species outside the

348 spatial extent of a given sample will inevitably appear as false-negatives in practical samples. The goal
349 should instead be to sample a system enough to have a statistically robust estimate of the current state and
350 empirical change over time of an ecological community at a given spatial extent and temporal resolution,
351 and to determine what the sampling effort required prior to sampling.

352 Our work highlights the need for a quantitatively robust approach to sampling design, both for
353 interactions (Jordano 2016) and all other aspects of biodiversity (Carlson *et al.* 2020). As anthropogenic
354 forces create rapid shifts in our planet's climate and biosphere, this is an imperative to maximize the
355 amount of ecological information we get in our finite samples, and make our inferences and decisions
356 based on this data as robust as possible. Where we choose to sample, and how often we choose to sample
357 there, has strong impacts on the inferences we make from data. Incorporating a better understanding of
358 sampling effort and bias to the design of biodiversity monitoring systems, and the inference and predictive
359 models we apply to this data, is imperative in understanding how biodiversity is changing, and making
360 actionable forecasts about the future of ecological interactions on our planet.

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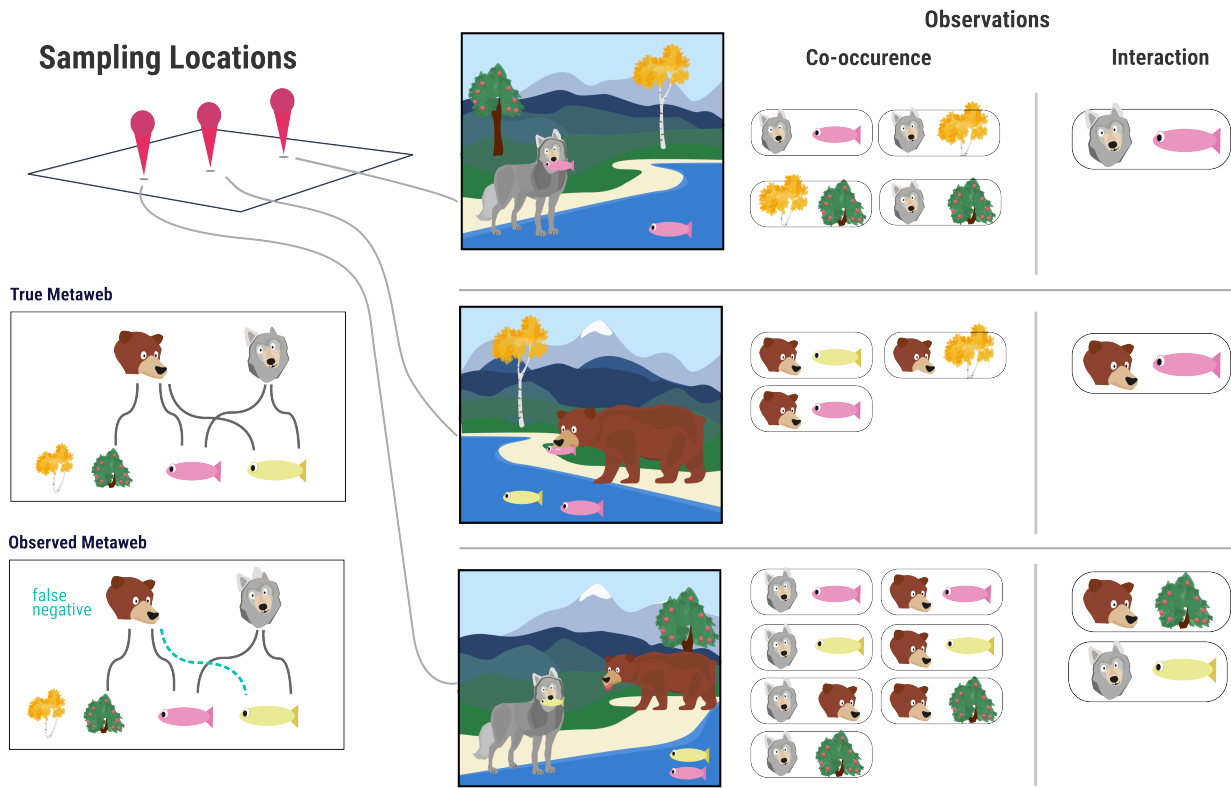


Figure 1: This conceptual example considers a sample of the trophic community of bears, wolves, salmon (pink fish), pike (yellow fish), berry trees, and aspen trees. The true metaweb (all realized interactions across the entire spatial extent) is shown on the left. In the center is what a hypothetical ecologist samples at each site. Notice that although bears are observed co-occurring with both salmon and pike, there was never a direct observation of bears eating pike, even though they actually do. Therefore, this interaction between bears and pike is a false negative.

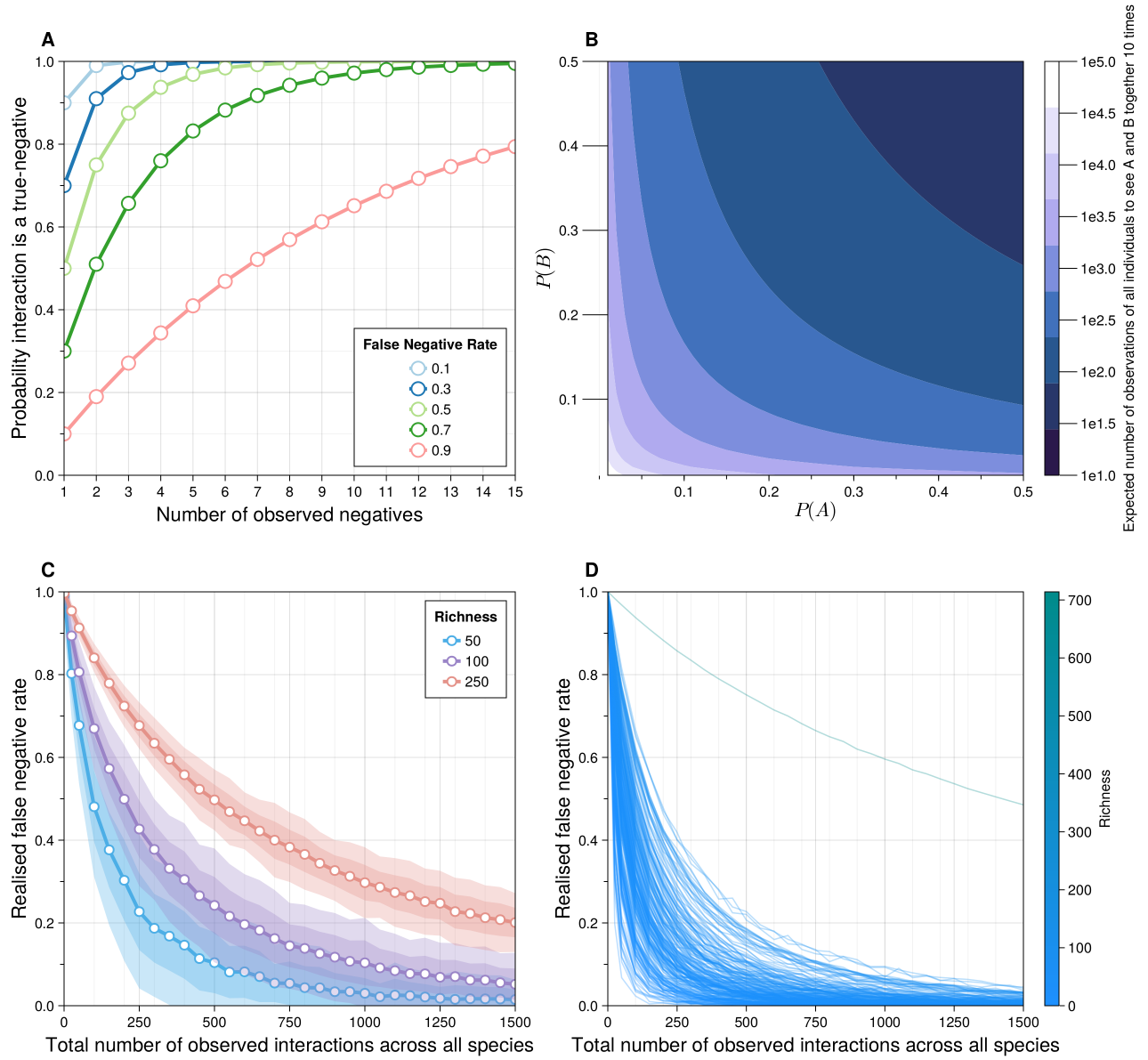


Figure 2: **(A)** The probability that an observed interaction is a true negative (y-axis) given how many times it has been sampled as a non-interaction (x-axis). Each color reflects a different value of p_{fn} , the false-negative rate (FNR)—this is effectively the cdf of the geometric distribution. **(B)** The expected number of total observations needed (colors) to observe 10 co-occurrences between a species with relative abundance $P(A)$ (x-axis) and a second species with relative abundance $P(Y)$. **(C)**: False negative rate (y-axis) as a function of total sampling effort (x-axis) and network size, computed using the method described above. For 500 independent draws from the niche model (Williams & Martinez (2000)) at varying levels of species richness (colors) with connectance drawn according to the flexible-links model (MacDonald *et al.* (2020)) as described in the main text. For each draw from the niche model, 200 sets of 1500 observations are simulated, for which each the mean false negative rate at each observation-step is computed. Means denoted with points, with 1 in the first shade and 2 in the second. **(D)**: Same as **(C)**, except using empirical food webs from Mangal database, where richness. The outlier on **(D)** is a 714 species food-web.

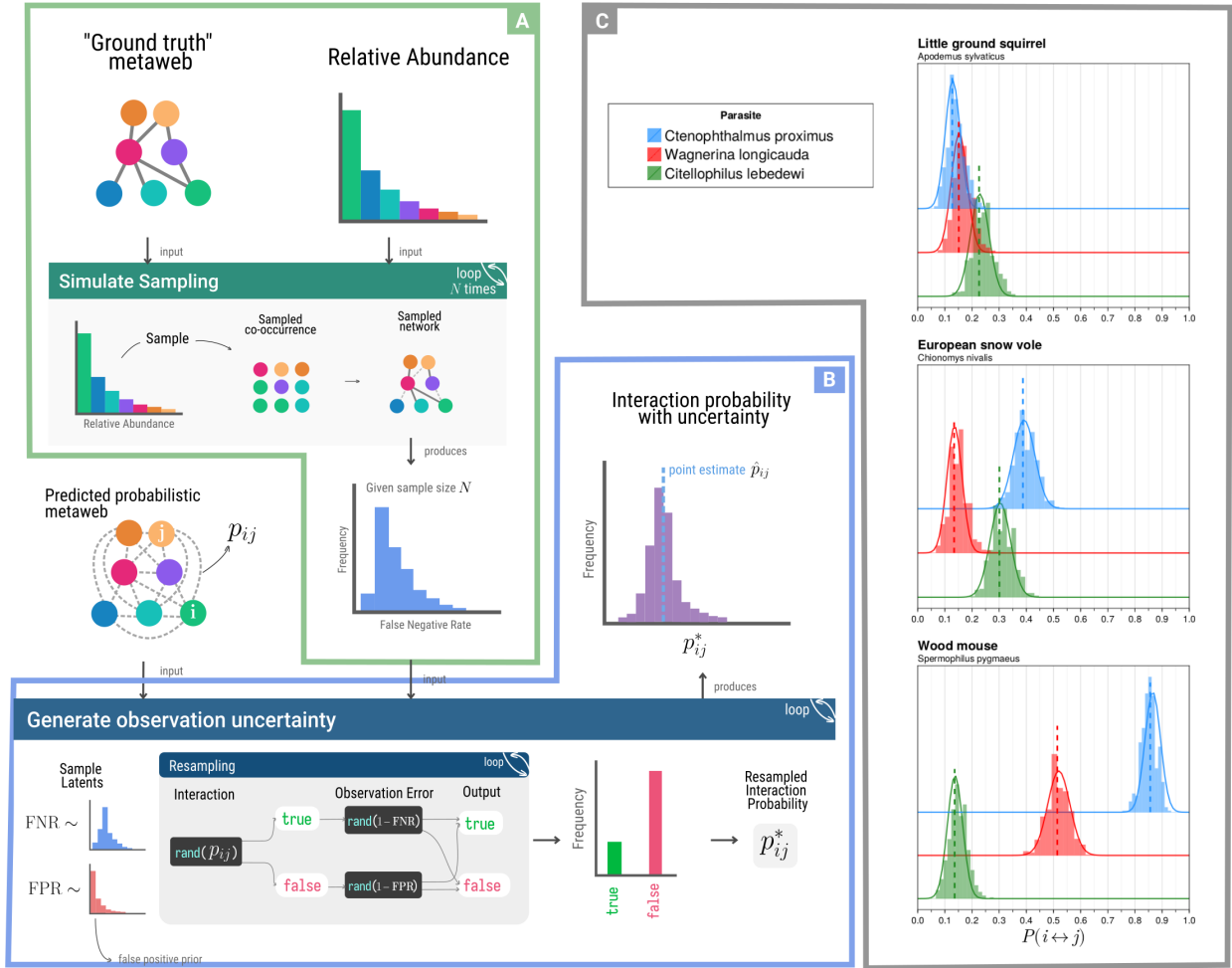


Figure 3: (A) The process for estimating the false-negative rate (FNR) for an interaction dataset consisting of N total observed interactions. (B) The method for resampling interaction probability based on estimates of false-negative and false-positive rates. (C) The method for interaction probability resampling applied to three mammals and three parasites from the Hadfield *et al.* (2014) dataset.

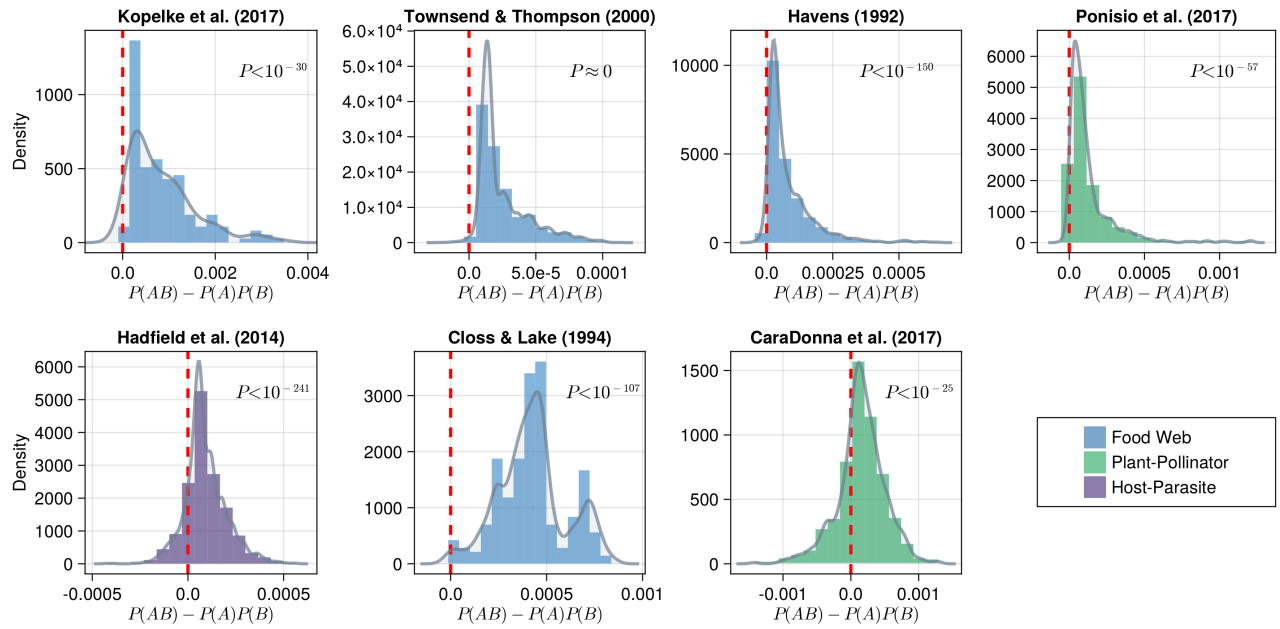


Figure 4: The difference between joint-probability of co-occurrence ($P(AB)$) and expected probability of co-occurrence under independence ($P(A)P(B)$) for interacting species for each dataset. The red-dashed line indicates 0 (no association). Each histogram represents a density, meaning the area of the entire curve sums to 1. The continuous density estimate (computed using local smoothing) is shown in grey. The p-value on each plot is the result of a one-sided t-test comparing the mean of each distribution to 0.



Figure 5: **(A)** The area-under the receiver-operator curve (ROC-AUC) and **(B)** The area-under the precision-recall curve (PR-AUC; right) for each different predictive model (colors/shapes) across a spectrum of the proportion of added false negatives (x-axis). **(C)** The mean trophic-level of all species in a network generated with the niche model across different species richnesses (colors). For each value of the FNR, the mean trophic level was computed across 50 replicates. The shaded region for each line is one standard-deviation across those replicates.