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$$\{["1"]\} \{["0","i"]\}$$

1 Interpretation

	N
0	$\{i,1\}$
i	$\{0,1\}$
1	$\{0,i\}$

\wedge	0	i	1
0	$\{0\}$	$\{i\}$	$\{i\}$
i	$\{i\}$	$\{i\}$	$\{i\}$
1	$\{i\}$	$\{i\}$	$\{1\}$

\vee	0	i	1
0	$\{0\}$	$\{i\}$	$\{1\}$
i	$\{i\}$	$\{i\}$	$\{1\}$
1	$\{1\}$	$\{1\}$	$\{1\}$

	\neg
0	$\{1\}$
i	$\{i\}$
1	$\{0\}$

2 Schemas of Σ_N

Size: 3

$$\begin{array}{c}
\text{r1} \\
\frac{N\varphi, \varphi}{} \\
\text{r2} \\
\hline
N\varphi, \neg N\varphi, \neg\varphi, \varphi \\
\text{r3} \\
\frac{\neg N\varphi, \neg\varphi}{} \\
N\varphi, \varphi
\end{array}$$

3 Schemas of Σ_{and}

$$\begin{array}{c}
\text{Size: 8} \\
\text{r4} \\
\frac{\neg((\varphi \wedge \psi)), \varphi}{} \\
\varphi \wedge \psi \\
\text{r5} \\
\frac{\neg((\varphi \wedge \psi)), \psi}{} \\
\varphi \wedge \psi \\
\text{r6} \\
\frac{\varphi, \psi}{} \\
\varphi \wedge \psi \\
\text{r7} \\
\frac{\neg\varphi, \neg\psi}{} \\
\varphi \wedge \psi, \neg((\varphi \wedge \psi)), \varphi, \psi \\
\text{r8} \\
\frac{\neg((\varphi \wedge \psi))}{} \\
\varphi \wedge \psi, \neg\varphi, \varphi \\
\text{r9} \\
\frac{\neg((\varphi \wedge \psi))}{} \\
\varphi \wedge \psi, \neg\psi, \psi \\
\text{r10} \\
\frac{\varphi \wedge \psi}{} \\
\varphi \\
\text{r11} \\
\frac{\varphi \wedge \psi}{} \\
\psi
\end{array}$$

4 Schemas of Σ_{neg}

Size: 3

r12

$$\frac{\neg\varphi, \varphi}{}$$

r13

$$\frac{\varphi}{}$$

$$\frac{}{\neg\neg\varphi, \neg\varphi}$$

r14

$$\frac{\neg\neg\varphi}{}$$

$$\frac{}{\neg\varphi, \varphi}$$

5 Schemas of Σ_{or}

Size: 6

r15

$$\frac{\neg\varphi, \neg\psi}{}$$

$$\frac{}{\neg((\varphi \vee \psi)), \varphi \vee \psi, \varphi, \psi}$$

r16

$$\frac{\neg((\varphi \vee \psi))}{}$$

$$\frac{}{\neg\varphi, \varphi \vee \psi, \varphi}$$

r17

$$\frac{\neg((\varphi \vee \psi))}{}$$

$$\frac{}{\neg\psi, \varphi \vee \psi, \psi}$$

r18

$$\frac{\varphi}{}$$

$$\frac{}{\varphi \vee \psi}$$

r19

$$\frac{\psi}{}$$

$$\frac{}{\varphi \vee \psi}$$

r20

$$\frac{\varphi \vee \psi}{}$$

$$\frac{}{\varphi, \psi}$$