

## Concept Checking Paper 02

1. What is “math” based on all the math you have learned in your life?
2. Let  $f:A \rightarrow B$ ,  $g:B \rightarrow C$ , prove that
  - (i) If  $g \circ f$  is injective, then  $f$  is injective
  - (ii) If  $g \circ f$  is surjective, then  $g$  is surjective
3. Write down the definition of **reflexive**, **in-reflexive**, **total**, **transitive**, **symmetric**, **antisymmetric**, **asymmetric**.
4. For which of the above properties does a **(not-strict) partial order** satisfy? What about a **strict partial order**? **Equivalence relation**? **Total order**?
5. State the two ways to construct real numbers in the slides.
6. Write down the definition of **equinumerous** between two sets and the corresponding notation.
7. Prove Cantor’s Theorem: For every set  $A$ ,  $A \not\approx P(A)$ .

