

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

ML Expressions and Variable Bindings

# *Mindset*

- “Let go” of all programming languages you already know
- For now, treat ML as a “totally new thing”
  - Time later to compare/contrast to what you know
  - For now, “oh that seems kind of like this thing in [Java]” will confuse you, slow you down, and you will learn less
- Start from a blank file...

# *A very simple ML program*

[The same program we just wrote in Emacs; here for convenience if reviewing the slides]

```
(* My first ML program *)

val x = 34;

val y = 17;

val z = (x + y) + (y + 2);

val q = z + 1;

val abs_of_z = if z < 0 then 0 - z else z;

val abs_of_z_simpler = abs z
```

# *A variable binding*

```
val z = (x + y) + (y + 2) ; (* comment *)
```

*More generally:*

```
val x = e;
```

- *Syntax:*
  - *Keyword* **val** and *punctuation* = and ;
  - *Variable* **x**
  - *Expression* **e**
    - Many forms of these, most containing *subexpressions*

# *The semantics*

- **Syntax** is just how you write something
- **Semantics** is what that something means
  - **Type-checking** (before program runs)
  - **Evaluation** (as program runs)
- For variable bindings:
  - Type-check expression and extend **static environment**
  - Evaluate expression and extend **dynamic environment**

So what is the precise syntax, type-checking rules, and evaluation rules for various expressions? Good question!

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

ML Rules for Expressions (Seen So Far)

# *A very simple ML program*

This program has integers, variables, addition, if-expressions, less-than, subtraction, and calling a pre-defined function

```
(* My first ML program *)

val x = 34;

val y = 17;

val z = (x + y) + (y + 2);

val q = z + 1;

val abs_of_z = if z < 0 then 0 - z else z;

val abs_of_z_simpler = abs z
```

# Expressions

- We have seen many kinds of expressions:

**34    true    false    x     $e1+e2$      $e1<e2$   
if  $e1$  then  $e2$  else  $e3$**

- Can get arbitrarily large since any subexpression can contain subsubexpressions, etc.
- Every kind of expression has
  1. Syntax
  2. Type-checking rules
    - Produces a type or fails (with a bad error message ☹)
    - Types so far: **int   bool   unit**
  3. Evaluation rules (used only on things that type-check)
    - Produces a value (or exception or infinite-loop)



# *Variables*

- Syntax:  
sequence of letters, digits, \_, not starting with digit
- Type-checking:  
Look up type in current static environment
  - If not there, fail
- Evaluation:  
Look up value in current dynamic environment

# *Addition*

- Syntax:  
 $e1 + e2$  where  $e1$  and  $e2$  are expressions
- Type-checking:  
If  $e1$  and  $e2$  have type `int`,  
then  $e1 + e2$  has type `int`
- Evaluation:  
If  $e1$  evaluates to  $v1$  and  $e2$  evaluates to  $v2$ ,  
then  $e1 + e2$  evaluates to sum of  $v1$  and  $v2$

# *Values*

- All values are expressions
- Not all expressions are values
- Every value “evaluates to itself” in “zero steps”
- Examples:
  - **34, 17, 42** have type **int**
  - **true, false** have type **bool**
  - **()** has type **unit**

# *A slightly tougher one*

*What are the syntax, typing rules, and evaluation rules for conditional expressions?*

Let's write it out...

*Now you try one*

Syntax, type-checking rules, and evaluation rules for less-than comparisons?

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

The REPL and Error Messages

# *Pragmatics*

Last two segments have built up key conceptual foundation

But you also need some pragmatics:

- How do we run programs using the REPL?
- What happens when we make mistakes?

Work on developing resilience to mistakes

- Slow down
- Don't panic
- Read what you wrote very carefully

*use*

`use "foo.sml"` is an unusual expression

It enters bindings from the file `foo.sml`

Result is `()` bound to variable `it`

– Ignorable



# *The REPL*

- Read-Eval-Print-Loop is well named
- Can just treat it as a strange/convenient way to run programs
  - But more convenient for quick try-something-out
  - Then move things over to a testing file for easy reuse
- For reasons discussed in next segment, do *not* use `use` without restarting the REPL session
  - (But using it for multiple files at beginning of session is okay)

# *Errors*

Your mistake could be:

- Syntax: What you wrote means nothing or not the construct you intended
- Type-checking: What you wrote does not type-check
- Evaluation: It runs but produces wrong answer, or an exception, or an infinite loop

Keep these straight when debugging even if sometimes one kind of mistake appears to be another

# *Play around*

Best way to learn something: Try lots of things and don't be afraid of errors

Maybe watching me make a few mistakes will help...

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

Shadowing

# *Multiple bindings of same variable*

Multiple variable bindings of the same variable is often poor style

- Often confusing

But it's an instructive exercise

- Helps explain how the environment “works”
- Helps explain how a variable binding “works”

(Emphasize this now to lay the foundation for first-class functions)

## *Our example*

```
val a = 10
```

```
val b = a * 2
```

```
val a = 5
```

```
val c = b
```

```
val d = a
```

```
val a = a + 1
```

```
(* val g = f - 3 *) (* does not type-check *)
```

```
val f = a * 2
```

## *Two reasons (either one sufficient)*

```
val a = 1
val b = a (* b is bound to 1 *)
val a = 2
```

1. Expressions in variable bindings are evaluated “eagerly”
  - Before the variable binding “finishes”
  - Afterwards, the expression producing the value is irrelevant
2. There is no way to “assign to” a variable in ML
  - Can only shadow it in a later environment

# *use*

This is why I am so insistent about not reusing **use** on a file without restarting the REPL

Else you are introducing some of the same bindings again

- May make it seem like wrong code is correct
- May make it seem like correct code is wrong
- (It's all well-defined, but we humans get confused)



```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

Functions (Informally)

# Function definitions

Functions: the most important building block in the whole course

- Like Java methods, have arguments and result
- But no classes, **this**, **return**, etc.

Example *function binding*:

```
(* Note: correct only if y>=0 *)  
  
fun pow (x : int, y : int) =  
  if y=0  
  then 1  
  else x * pow(x,y-1)
```

Note: The *body* includes a (recursive) *function call*: **pow(x,y-1)**

## *Example, extended*

```
fun pow (x : int, y : int) =  
  if y=0  
  then 1  
  else x * pow(x,y-1)
```

```
fun cube (x : int) =  
  pow (x,3)
```

```
val sixtyfour = cube 4
```

```
val fortytwo = pow(2,2+2) + pow(4,2) + cube(2) + 2
```

# *Some gotchas*

Three common “gotchas”

- Bad error messages if you mess up function-argument syntax
- The use of `*` in type syntax is not multiplication
  - Example: `int * int -> int`
  - In expressions, `*` is multiplication: `x * pow(x, y-1)`
- Cannot refer to later function bindings
  - That’s simply ML’s rule
  - Helper functions must come before their uses
  - Need special construct for *mutual recursion* (later)

# *Recursion*

- If you're not yet comfortable with recursion, you will be soon 😊
  - Will use for most functions taking or returning lists
- “Makes sense” because calls to same function solve “simpler” problems
- Recursion more powerful than loops
  - We won't use a single loop in ML
  - Loops often (not always) obscure simple, elegant solutions

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

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Functions (Formally)

# Function bindings: 3 questions

- Syntax: `fun x0 (x1 : t1, ... , xn : tn) = e`
  - (Will generalize in later lecture)
- Evaluation: **A function is a value!** (No evaluation yet)
  - Adds **x0** to environment so *later* expressions can *call* it
  - (Function-call semantics will also allow recursion)
- Type-checking:
  - Adds binding **x0 : (t1 \* ... \* tn) -> t** if:
  - Can type-check body **e** to have type **t** in the static environment containing:
    - “Enclosing” static environment (earlier bindings)
    - **x1 : t1, ..., xn : tn** (arguments with their types)
    - **x0 : (t1 \* ... \* tn) -> t** (for recursion)

# More on type-checking

```
fun x0 (x1 : t1, ... , xn : tn) = e
```

- New kind of type:  $(t_1 * \dots * t_n) \rightarrow t$ 
  - Result type on right
  - The overall type-checking result is to give  $x_0$  this type in rest of program (unlike Java, not for earlier bindings)
  - Arguments can be used only in  $e$  (unsurprising)
- Because evaluation of a call to  $x_0$  will return result of evaluating  $e$ , the return type of  $x_0$  is the type of  $e$
- The type-checker “magically” figures out  $t$  if such a  $t$  exists
  - Later lecture: Requires some cleverness due to recursion
  - More magic after hw1: Later can omit argument types too



# Function Calls

A new kind of expression: 3 questions

Syntax: **`e0 (e1, ..., en)`**

- (Will generalize later)
- Parentheses optional if there is exactly one argument

Type-checking:

If:

- **`e0`** has some type **`(t1 * ... * tn) -> t`**
- **`e1`** has type **`t1`**, ..., **`en`** has type **`tn`**

Then:

- **`e0 (e1, ..., en)`** has type **`t`**

Example: **`pow(x, y-1)`** in previous example has type **`int`**

# Function-calls continued

$e_0(e_1, \dots, e_n)$

Evaluation:

1. (Under current dynamic environment,) evaluate  $e_0$  to a function **fun**  $x_0$  ( $x_1 : t_1, \dots, x_n : t_n$ ) =  $e$ 
  - Since call type-checked, result *will be* a function
2. (Under current dynamic environment,) evaluate arguments to values  $v_1, \dots, v_n$
3. Result is evaluation of  $e$  in an environment extended to map  $x_1$  to  $v_1, \dots, x_n$  to  $v_n$ 
  - (“An environment” is actually the environment where the function was defined, and includes  $x_0$  for recursion)

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

Pairs and Other Tuples

# *Tuples and lists*

So far: numbers, booleans, conditionals, variables, functions

- Now ways to build up data with multiple parts
- This is essential
- Java examples: classes with fields, arrays

Now:

- *Tuples*: fixed “number of pieces” that may have different types

Coming soon:

- *Lists*: any “number of pieces” that all have the same type

Later:

- Other more general ways to create compound data

# *Pairs (2-tuples)*

Need a way to *build* pairs and a way to *access* the pieces

*Build:*

- Syntax: **(e1, e2)**
- Evaluation: Evaluate **e1** to **v1** and **e2** to **v2**; result is **(v1, v2)**
  - A pair of values is a value
- Type-checking: If **e1** has type **ta** and **e2** has type **tb**, then the pair expression has type **ta \* tb**
  - A new kind of type

# *Pairs (2-tuples)*

Need a way to *build* pairs and a way to *access* the pieces

Access:

- Syntax: **#1 e** and **#2 e**
- Evaluation: Evaluate **e** to a pair of values and return first or second piece
  - Example: If **e** is a variable **x**, then look up **x** in environment
- Type-checking: If **e** has type **ta \* tb**, then **#1 e** has type **ta** and **#2 e** has type **tb**

# Examples

Functions can take and return pairs

```
fun swap (pr : int*bool) =  
  (#2 pr, #1 pr)
```

```
fun sum_two_pairs (pr1 : int*int, pr2 : int*int) =  
  (#1 pr1) + (#2 pr1) + (#1 pr2) + (#2 pr2)
```

```
fun div_mod (x : int, y : int) =  
  (x div y, x mod y)
```

```
fun sort_pair (pr : int*int) =  
  if (#1 pr) < (#2 pr)  
  then pr  
  else (#2 pr, #1 pr)
```

# *Tuples*

Actually, you can have *tuples* with more than two parts

– A new feature: a generalization of pairs

- $(e_1, e_2, \dots, e_n)$
- `ta * tb * ... * tn`
- `#1 e, #2 e, #3 e, ...`

Homework 1 uses triples of type `int*int*int` a lot



# *Nesting*

Pairs and tuples can be nested however you want

- Not a new feature: implied by the syntax and semantics

```
val x1 = (7, (true, 9)) (* int * (bool*int) *)
```

```
val x2 = #1 (#2 x1)      (* bool *)
```

```
val x3 = (#2 x1)         (* bool*int *)
```

```
val x4 = ((3, 5), ((4, 8), (0, 0)))  
          (* (int*int)*((int*int)*(int*int)) *)
```

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

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Introducing Lists

# *Lists*

- Despite nested tuples, the type of a variable still “commits” to a particular “amount” of data

In contrast, a list:

- Can have any number of elements
- But all list elements have the same type

Need ways to *build* lists and *access* the pieces...

# *Building Lists*

- The empty list is a value:

`[]`

- In general, a list of values is a value; elements separated by commas:

`[v1, v2, ..., vn]`

- If  $e1$  evaluates to  $v$  and  $e2$  evaluates to a list  $[v1, \dots, vn]$ , then  $e1 :: e2$  evaluates to  $[v, \dots, vn]$

`e1 :: e2` (\* pronounced "cons" \*)

# Accessing Lists

Until we learn pattern-matching, we will use three standard-library functions

- `null e` evaluates to `true` if and only if `e` evaluates to `[]`
- If `e` evaluates to `[v1, v2, ..., vn]` then `hd e` evaluates to `v1`
  - (raise exception if `e` evaluates to `[]`)
- If `e` evaluates to `[v1, v2, ..., vn]` then `tl e` evaluates to `[v2, ..., vn]`
  - (raise exception if `e` evaluates to `[]`)
  - Notice result is a list

# Type-checking list operations

Lots of new types: For any type `t`, the type `t list` describes lists where all elements have type `t`

– Examples: `int list`   `bool list`   `int list list`  
              `(int * int) list`   `(int list * int) list`

- So `[]` can have type `t list` for *any* type
  - SML uses type `'a list` to indicate this (“quote a” or “alpha”)
- For `e1::e2` to type-check, we need a `t` such that `e1` has type `t` and `e2` has type `t list`. Then the result type is `t list`
- `null : 'a list -> bool`
- `hd : 'a list -> 'a`
- `tl : 'a list -> 'a list`

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

List Functions

# *Functions over lists*

Gain experience with lists and recursion by writing several functions that process and/or produce lists...



## *Example list functions*

```
fun sum_list (xs : int list) =  
  if null xs  
  then 0  
  else hd(xs) + sum_list(tl(xs))
```

```
fun countdown (x : int) =  
  if x=0  
  then []  
  else x :: countdown (x-1)
```

```
fun append (xs : int list, ys : int list) =  
  if null xs  
  then ys  
  else hd (xs) :: append (tl(xs), ys)
```

# *Recursion again*

Functions over lists are usually recursive

- Only way to “get to all the elements”
- What should the answer be for the empty list?
- What should the answer be for a non-empty list?
  - Typically in terms of the answer for the tail of the list!

Similarly, functions that produce lists of potentially any size will be recursive

- You create a list out of smaller lists

# *Lists of pairs*

Processing lists of pairs requires no new features. Examples:

```
fun sum_pair_list (xs : (int*int) list) =  
  if null xs  
  then 0  
  else #1(hd xs) + #2(hd xs) + sum_pair_list(tl xs)  
  
fun firsts (xs : (int*int) list) =  
  if null xs  
  then []  
  else #1(hd xs) :: firsts(tl xs)  
  
fun seconds (xs : (int*int) list) =  
  if null xs  
  then []  
  else #2(hd xs) :: seconds(tl xs)  
  
fun sum_pair_list2 (xs : (int*int) list) =  
  (sum_list (firsts xs)) + (sum_list (seconds xs))
```

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

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Let Expressions

# Review

Huge progress already on the core pieces of ML:

- Types: `int bool unit t1*...*tn t list t1*...*tn->t`
  - Types “nest” (each `t` above can be itself a compound type)
- Variables, environments, and basic expressions
- Functions
  - Build: `fun x0 (x1:t1, ..., xn:tn) = e`
  - Use: `e0 (e1, ..., en)`
- Tuples
  - Build: `(e1, ..., en)`
  - Use: `#1 e, #2 e, ...`
- Lists
  - Build: `[] e1::e2`
  - Use: `null e hd e tl e`

# Now...

The big thing we need: local bindings

- For style and convenience

This segment:

- Basic let-expressions

Next segments:

- A big but natural idea: nested function bindings
- For efficiency (**not** “just a little faster”)

The construct to introduce local bindings is ***just an expression***, so we can use it anywhere an expression can go

# Let-expressions

3 questions:

- Syntax: `let b1 b2 ... bn in e end`
  - Each ***b<sub>i</sub>*** is any *binding* and ***e*** is any *expression*
- Type-checking: Type-check each ***b<sub>i</sub>*** and ***e*** in a static environment that includes the previous bindings.  
Type of whole let-expression is the type of ***e***.
- Evaluation: Evaluate each ***b<sub>i</sub>*** and ***e*** in a dynamic environment that includes the previous bindings.  
Result of whole let-expression is result of evaluating ***e***.

# Silly examples

```
fun silly1 (z : int) =  
  let val x = if z > 0 then z else 34  
    val y = x+z+9  
  in  
    if x > y then x*2 else y*y  
  end  
fun silly2 () =  
  let val x = 1  
  in  
    (let val x = 2 in x+1 end) +  
    (let val y = x+2 in y+1 end)  
  end
```

`silly2` is poor style but shows let-expressions are expressions

- Can also use them in function-call arguments, if branches, etc.
- Also notice shadowing



# *What's new*

- What's new is **scope**: where a binding is in the environment
  - *In* later bindings and body of the let-expression
    - (Unless a later or nested binding shadows it)
  - *Only in* later bindings and body of the let-expression
- *Nothing else is new:*
  - Can put any binding we want, even function bindings
  - Type-check and evaluate just like at “top-level”

# Programming Languages

Dan Grossman

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Nested Functions

# *Any binding*

According to our rules for let-expressions, we can define functions inside any let-expression

```
let  b1 b2 ... bn  in  e  end
```

This is a natural idea, and often good style

## *(Inferior) Example*

```
fun countup_from1 (x : int) =  
  let fun count (from : int, to : int) =  
        if from = to  
        then to :: []  
        else from :: count(from+1,to)  
      in  
        count (1,x)  
      end
```

- This shows how to use a local function binding, but:
  - Better version on next slide
  - **count** might be useful elsewhere

*Better:*

```
fun countup_from1_better (x : int) =  
  let fun count (from : int) =  
        if from = x  
        then x :: []  
        else from :: count(from+1)  
      in  
        count 1  
      end
```

- Functions can use bindings in the environment where they are defined:
  - Bindings from “outer” environments
    - Such as parameters to the outer function
  - Earlier bindings in the let-expression
- Unnecessary parameters are usually bad style
  - Like `to` in previous example

## *Nested functions: style*

- Good style to define helper functions inside the functions they help if they are:
  - Unlikely to be useful elsewhere
  - Likely to be misused if available elsewhere
  - Likely to be changed or removed later
- A fundamental trade-off in code design: reusing code saves effort and avoids bugs, but makes the reused code harder to change later

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

Let Expressions to Avoid Repeated Computation

# *Avoid repeated recursion*

Consider this code and the recursive calls it makes

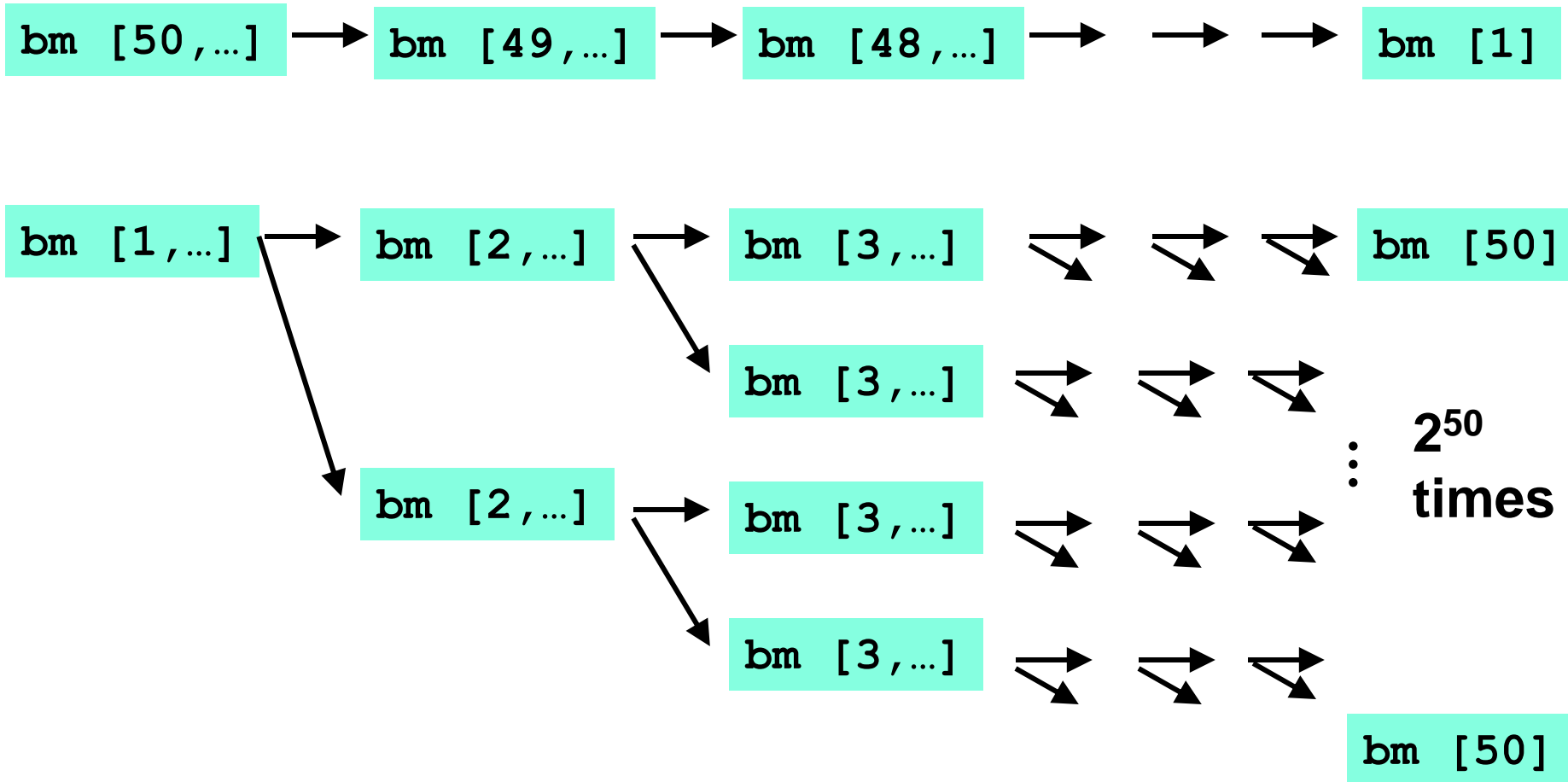
- Don't worry about calls to `null`, `hd`, and `tl` because they do a small constant amount of work

```
fun bad_max (xs : int list) =  
  if null xs  
  then 0 (* horrible style; fix later *)  
  else if null (tl xs)  
  then hd xs  
  else if hd xs > bad_max (tl xs)  
  then hd xs  
  else bad_max (tl xs)  
  
let x = bad_max [50,49,...,1]  
let y = bad_max [1,2,...,50]
```



# *Fast vs. unusable*

```
if hd xs > bad_max (tl xs)
then hd xs
else bad_max (tl xs)
```



# *Math never lies*

Suppose one `bad_max` call's if-then-else logic and calls to `hd`, `null`, `t1` take  $10^{-7}$  seconds

- Then `bad_max [50,49,...,1]` takes  $50 \times 10^{-7}$  seconds
- And `bad_max [1,2,...,50]` takes  $1.12 \times 10^8$  seconds
  - (over 3.5 years)
  - `bad_max [1,2,...,55]` takes over 1 century
  - Buying a faster computer won't help much ☺

The key is not to do repeated work that might do repeated work that might do...

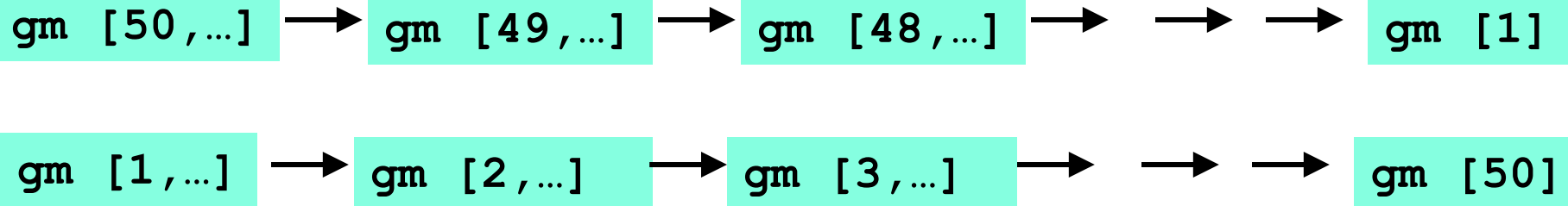
- Saving recursive results in local bindings is essential...

## *Efficient max*

```
fun good_max (xs : int list) =  
  if null xs  
  then 0 (* horrible style; fix later *)  
  else if null (tl xs)  
       then hd xs  
       else  
         let val tl_ans = good_max(tl xs)  
         in  
           if hd xs > tl_ans  
           then hd xs  
           else tl_ans  
         end
```

# *Fast vs. fast*

```
let val tl_ans = good_max(tl xs)
in
  if hd xs > tl_ans
  then hd xs
  else tl_ans
end
```



```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

Options

# *Motivating Options*

Having **max** return 0 for the empty list is really awful

- Could raise an *exception* (future topic)
- Could return a zero-element or one-element list
  - That works but is poor style because the built-in support for *options* expresses this situation directly

# Options

- `t option` is a type for any type `t`
  - (much like `t list`, but a different type, not a list)

Building:

- `NONE` has type `'a option` (much like `[]` has type `'a list`)
- `SOME e` has type `t option` if `e` has type `t` (much like `e :: []`)

Accessing:

- `isSome` has type `'a option -> bool`
- `valOf` has type `'a option -> 'a` (exception if given `NONE`)

## Example

```
fun better_max (xs : int list) =  
  if null xs  
  then NONE  
  else  
    let val tl_ans = better_max(tl xs)  
    in  
      if isSome tl_ans  
        andalso valOf tl_ans > hd xs  
      then tl_ans  
      else SOME (hd xs)  
    end  
  end
```

```
val better_max = fn : int list -> int option
```

- Nothing wrong with this, but as a matter of style might prefer not to do so much useless “`valOf`” in the recursion



## *Example variation*

```
fun better_max2 (xs : int list) =  
  if null xs  
  then NONE  
  else let (* ok to assume xs nonempty b/c local *)  
        fun max_nonempty (xs : int list) =  
          if null (tl xs)  
          then hd xs  
          else  
            let val tl_ans = max_nonempty (tl xs)  
            in  
              if hd xs > tl_ans  
              then hd xs  
              else tl_ans  
            end  
        in  
          SOME (max_nonempty xs)  
        end
```

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

More Boolean and Comparison Expressions

# *Some More Expressions*

Some “odds and ends” that haven’t come up much yet:

- Combining Boolean expressions (and, or, not)
- Comparison operations

# *Boolean operations*

**`e1 andalso e2`**

- Type-checking: **`e1`** and **`e2`** must have type **`bool`**
- Evaluation: If result of **`e1`** is **`false`** then **`false`** else result of **`e2`**

**`e1 orelse e2`**

**`not e1`**

- Syntax in many languages is **`e1 && e2`**, **`e1 || e2`**, **`!e`**
  - **`&&`** and **`||`** don't exist in ML and **`!`** means something different
- “Short-circuiting” evaluation means **`andalso`** and **`orelse`** are not functions, but **`not`** is just a pre-defined function

# Style with Booleans

Language does not *need* `andalso` , `orelse` , `not`

```
(* e1 andalso e2 *)  
if e1  
then e2  
else false
```

```
(* e1 orelse e2 *)  
if e1  
then true  
else e2
```

```
(* not e1 *)  
if e1  
then false  
else true
```

Using more concise forms generally much better style

And definitely please do not do this:

```
(* just say e (!!!) *)  
if e  
then true  
else false
```

# Comparisons

For comparing `int` values:

`=` `<>` `>` `<` `>=` `<=`

You might see weird error messages because comparators can be used with some other types too:

- `>` `<` `>=` `<=` can be used with `real`, but not 1 `int` and 1 `real`
- `=` `<>` can be used with any “equality type” but not with `real`
  - Let’s not discuss equality types yet

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman

A Key Benefit of Immutable Data

# *A valuable non-feature: no mutation*

Have now covered all the features you need (and should use) on hw1

Now learn a very important **non-feature**

- Huh?? How could the *lack* of a feature be important?
- When it lets you know things *other* code will *not* do with your code and the results your code produces

A major aspect and contribution of functional programming:

Not being able to assign to (a.k.a. *mutate*) variables  
or parts of tuples and lists

(This is a “Big Deal”)



# *Cannot tell if you copy*

```
fun sort_pair (pr : int * int) =  
  if #1 pr < #2 pr  
  then pr  
  else (#2 pr, #1 pr)  
  
fun sort_pair (pr : int * int) =  
  if #1 pr < #2 pr  
  then (#1 pr, #2 pr)  
  else (#2 pr, #1 pr)
```

In ML, these two implementations of `sort_pair` are **indistinguishable**

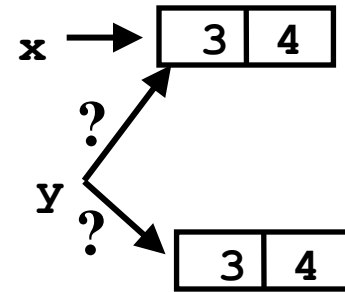
- But only because tuples are immutable
- The first is better style: simpler and avoids making a new pair in the then-branch
- In languages with mutable compound data, these are different!

# Suppose we had mutation...

```
val x = (3,4)
val y = sort_pair x
```

*somehow mutate #1 x to hold 5*

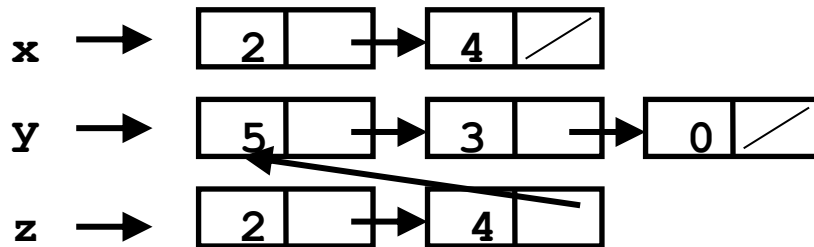
```
val z = #1 y
```



- What is `z`?
  - Would depend on how we implemented `sort_pair`
    - Would have to decide carefully and document `sort_pair`
  - But without mutation, we can implement “either way”
    - No code can ever distinguish aliasing vs. identical copies
    - No need to think about aliasing: focus on other things
    - Can use aliasing, which saves space, without danger

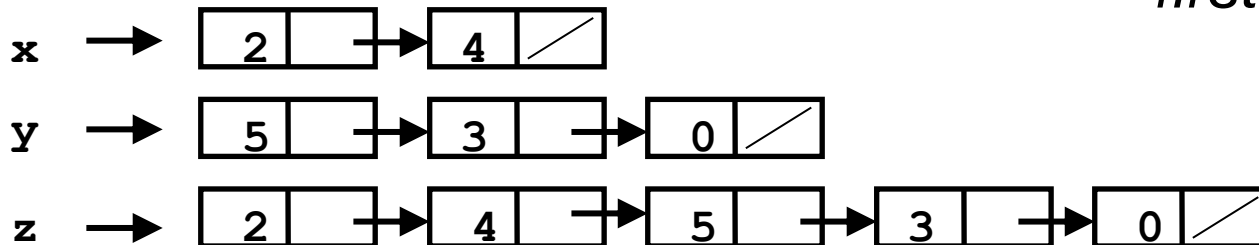
## An even better example

```
fun append (xs : int list, ys : int list) =  
  if null xs  
  then ys  
  else hd (xs) :: append (tl(xs), ys)  
val x = [2,4]  
val y = [5,3,0]  
val z = append(x,y)
```



*(can't tell,  
but it's the  
first one)*

**or**



# *ML vs. Imperative Languages*

- In ML, we create aliases all the time without thinking about it because it is *impossible* to tell where there is aliasing
  - Example: `tl` is constant time; does not copy rest of the list
  - So don't worry and focus on your algorithm
- In languages with mutable data (e.g., Java), programmers are *obsessed* with aliasing and object identity
  - They have to be (!) so that subsequent assignments affect the right parts of the program
  - Often crucial to make copies in just the right places
    - **Optional** Java example in next segment

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
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val a = map (increment, [4,8,12,16])  
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```

# Programming Languages

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Optional: Java Mutation Bug

# *ML vs. Imperative Languages*

- In ML, we create aliases all the time without thinking about it because it is *impossible* to tell where there is aliasing
  - Example: `tl` is constant time; does not copy rest of the list
  - So don't worry and focus on your algorithm
- In languages with mutable data (e.g., Java), programmers are *obsessed* with aliasing and object identity
  - They have to be (!) so that subsequent assignments affect the right parts of the program
  - Often crucial to make copies in just the right places
    - **Optional** Java example...

# *Java security nightmare (bad code)*

```
class ProtectedResource {
    private Resource theResource = ...;
    private String[] allowedUsers = ...;
    public String[] getAllowedUsers() {
        return allowedUsers;
    }
    public String currentUser() { ... }
    public void useTheResource() {
        for(int i=0; i < allowedUsers.length; i++) {
            if(currentUser().equals(allowedUsers[i])) {
                ... // access allowed: use it
                return;
            }
        }
        throw new IllegalAccessException();
    }
}
```

# *Have to make copies*

The problem:

```
p.getAllowedUsers()[0] = p.currentUser();  
p.useTheResource();
```

The fix:

```
public String[] getAllowedUsers() {  
    ... return a copy of allowedUsers ...  
}
```

Reference (alias) vs. copy doesn't matter if code is immutable!



```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
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val a = map (increment, [4,8,12,16])  
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```

# Programming Languages

Dan Grossman

The Pieces of Learning a Language

# *Five different things*

1. **Syntax:** How do you write language constructs?
2. **Semantics:** What do programs mean? (Evaluation rules)
3. **Idioms:** What are typical patterns for using language features to express your computation?
4. **Libraries:** What facilities does the language (or a well-known project) provide “standard”? (E.g., file access, data structures)
5. **Tools:** What do language implementations provide to make your job easier? (E.g., REPL, debugger, code formatter, ...)
  - Not actually part of the language

These are 5 separate issues

- In practice, all are essential for good programmers
- Many people confuse them, but shouldn't

# *Our Focus*

This course focuses on semantics and idioms

- Syntax is usually uninteresting
  - A fact to learn, like “The American Civil War ended in 1865”
  - People obsess over subjective preferences
- Libraries and tools crucial, but often learn new ones “on the job”
  - We are learning semantics and how to use that knowledge to understand all software and employ appropriate idioms
  - By avoiding most libraries/tools, our languages may look “silly” but so would *any* language used this way