FlowPools: Lock-Free Deterministic Concurrent Data-Flow Queues

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Abstract. Implementing correct and deterministic parallel programs is hard (additional motivation sentence after this). We present the design and implementation of a fundamental data structure for deterministic parallel data-flow computation. Aditionally, we provide a proof of correctness, showing that the implementation is linearizable, lock-free, and deterministic. Finally, we provide microbenchmarks which compare our *flow pools* against corresponding operations on other popular concurrent data structures, in addition to performance benchmarks on a real *XYZ* application using real data. (Keep abstract between 70 and 150 words).

Keywords: data-flow, concurrent data-structure, determinism

1 Introduction

1.1 Motivation

- we want a deterministic model - we do not block in the programming model (i.e. there are no operations which cause blocking until a value becomes available) - we want a non-blocking data-structure (i.e. the operations on the data-structures should themselves be non-blocking) - programs run indefinitely = ξ we need to GC parts of the data structure we no longer need - we want to reduce heap allocation and inline the datastructure as much as possible = ξ lower memory consumption, better cache behaviour and fewer GC cycles

Obligatory multicore motivation paragraph.

Lock-free is better, and why.

Introduction and motivation for data-flow programming model.

2 Model of Computation

Producer-consumer parallelism. Description and image of queue/stream of values, producer, and multiple consumers.

3 Programming Model

The FlowPool suite supports the following operations:

- Builder.<<(x: T): Builder
 Inserts an element into the underlying FlowPool.
- Builder.seal(n: Int): Unit
 Seals the underlying FlowPool at n elements. The need for the size argument is explained below. A sealed FlowPool may only contain n elements. This allows for callback cleanup and termination.
- FlowPool.doForAll(f: T => Unit): Future[Int] Instructs the FlowPool to execute the closure f exactly once for each element inserted into the FlowPool (asynchronously). The returned future contains the number of elements in the FlowPool and completes once f has been executed for all elements.
- FlowPool.mappedFold[U, V <: U](acc: V)(cmb: (U,V) => V)(map: T => U): Future[(Int, V)] Reduces the FlowPool to a single value of type V, by first mapping each element to an internal representation using map and then aggregating using cmb. No guarantee is given about synchronization or order. Returns a future containing a tuple with number of elements in the FlowPool and the aggregated value.
- FlowPool.builder
 Returns a builder for this FlowPool.
- Future.map[U](f: T => U)
 Maps this future to another future executing the function f exactly once when the first future completes.
- future[T] (f: () => T): Future[T]
 Asynchronously dispatch execution of f an return a future with its result.

Determinism of seal We will show that the final size of the FlowPool is required as an argument to the seal method in order to satisfy the determinism property of the FlowPool. Look at the following program:

```
val p = new FlowPool[Int]()
val b = p.builder

future {
   for (i <- 1 to 10) { b << i }
    b.seal
}

future { for (i <- 1 to 10) { b << i } }</pre>
```

Depending on which for-loop completes first, this program completes successfully or yields an error. A similar program with b.seal(20) will always succeed.

Generators In the following we'll present a couple of generators for FlowPools based on common generators in the Scala standard library.

```
def iterate[T](start: T, len: Int)(f: (T) \Rightarrow T) = {
  val p = new FlowPool[T]
  val b = p.builder
  future {
    var e = start
    for (i <- 1 to len) \{ b << e; e = f(e) \}
    b.seal(len)
  }; p
}
def tabulate[T](n: Int)(f: (Int) \Rightarrow T) = {
  val p = new FlowPool[T]
  val b = p.builder
  future {
    for (i \leftarrow 0 to (n-1)) {
      b << f(i)
    b.seal(n)
  }; p
}
def fill[T](n: Int)(elem: => T) = {
  val p = new FlowPool[T]
  val b = p.builder
  future {
    for (i <- 1 to n) { b << elem }
    b.seal(n)
  }; p
}
```

Monadic Operations In the following we'll present some monadic operations on top of the basic FlowPool operations. This will also show some use-cases of the futures as result type of doForAll.

```
def map[S](f: T => S) = {
  val fp = new FlowPool[S]
  val b = fp.builder
  doForAll { x =>
     b << f(x)
  } map { b.seal _ }
  fp
}</pre>
```

```
def filter(f: T => Boolean) = {
   val fp = new FlowPool[T]
   val b = fp.builder

   mappedFold(0)(_ + _) { x =>
      if (f(x)) { b << x; 1 } else 0
   } map { case (c,fc) => b.seal(fc) }

   fp
}

def flatMap[S](f: T => FlowPool[S]) = {
   val fp = new FlowPool[S]
   val b = fp.builder

   mappedFold(future(0))(_ <+> _) { x =>
      f(x).doForAll(b << _)
   } map { case (c,cfut) => cfut.map(b.seal _) }

   fp
}
```

where <+> is the future of the sum of two Future[Int].

4 Implementation

5 Proofs

5.1 Abstract Pool Semantics

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5.2 Linearizability

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- 5.3 Lock-Freedom
- 5.4 Determinism
- 6 Experimental Results

7 Related Work

Things to probably cite: Oz, gpars, Java CLQ, our futures writeup.

Things we should probably have a look at: Microsoft TPL, Dataflow Java, FlumeJava...

Forcing a bib, [1], [2], [3], [4], [5], [6]

8 Conclusion

References

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A Proof of Correctness

Definition 1 (Data types). A **Block** b is an object which contains an array b.array, which itself can contain elements, $e \in Elem$, where **Elem** represents the type of e and can be any countable set. A given block b additionally contains an index b.index which represents an index location in b.array, a unique index identifying the array b.blockIndex, and b.next, a reference to a successor block c where c.blockIndex = b.blockIndex + 1. A **Terminal** term is a sentinel object, which contains an integer $term.sealed \in -1 \cup \mathbb{N}$, and term.callbacks, a set of functions $f \in Elem \Rightarrow Unit$.

Definition 2 (FlowPool). A **FlowPool** pool is an object that has a reference pool.start, to the first block b_0 (with $b_0.blockIndex = 0$), as well as a reference pool.current typically pointing to some subsequent block b_n where $b_n = b_0$ or where b_n is reachable from b_0 following next references. Initially, pool.current = pool.start. The pool **state** $\mathbb S$ is defined as the sequence of blocks reachable from pool.start by following next references within blocks. More formally, the relation reachable(b, c) on two blocks b, c holds iff $b = c \lor b.next = c \lor \exists b' : reachable(b, b') \land reachable(b', c)$. A **state changing** instruction is any atomic write or CAS instruction that changes an object that can be accessed from pool.start.

Definition 3 (Abstract state). An **abstract state** \mathbb{A} is a tuple (elems, sealed) such that $\mathbb{A} \in \{(elems, sealed) \mid elems \subset Elem, sealed \in \{-1\} \cup \mathbb{N}\}$. Abstract state operations on some abstract state \mathbb{A} are $append(\mathbb{A}, e) = \mathbb{A}'$ where $\mathbb{A}' = (elems \cup \{e\}, sealed)$ if $\mathbb{A} = (elems, sealed)$, $seal(\mathbb{A}, sealSize) = \mathbb{A}''$ where $\mathbb{A}'' = (elems, sealSize)$: $sealSize \in \mathbb{N}$ if $\mathbb{A} = (elems, sealed)$ and sealed = -1, the unsealed state, or sealed = sealSize already.

Definition 4 (Consistency). A FlowPool state \mathbb{S} of *pool* with starting block *pool.start* is consistent with an abstract state $\mathbb{A} = (elems, sealed)$ iff some element $e \in elems \Leftrightarrow \exists b, i : reachable(pool.start, b) \land b.array(i) = e$, and

 $\exists c, j : c.array(j) \in Terminal \land c.array(j).sealed = sealed \land reachable(pool.start, c).$ A FlowPool operation op is **consistent** with the corresponding abstract state operation op' iff $\mathbb{S}' = op(\mathbb{S})$ is consistent with an abstract state $\mathbb{A}' = op'(\mathbb{A})$. A **consistency change** is a change from state \mathbb{S} to state \mathbb{S}' such that \mathbb{S} is consistent with an abstract state \mathbb{A} and \mathbb{S}' is consistent with an abstract set \mathbb{A}' , where $\mathbb{A} \neq \mathbb{A}'$.

Definition 5 (Lock-freedom). In a scenario where some finite number of threads are executing a concurrent operation, that concurrent operation is *lock-free* if and only if that concurrent operation is completed after a finite number of steps by some thread.

Theorem 1 (Lock-freedom). FlowPool operations append, seal, and doForAll are lock-free.

We begin by first proving that there are a finite number of execution steps before a consistency change occurs.

Lemma 1. After invoking an operation op, if non-consistency changing CAS operations CAS1, CAS3, or CAS4, in the pseudocode fail, they must have already been successfully completed by another thread since op began.

Proof. Trivial inspection of the pseudocode reveals that since CAS1 makes up a check that precedes CAS2, and since CAS2 is the only operation besides CAS1 which can change the expected value of CAS1, in the case of a failure of CAS1, CAS2 (and thus CAS1) must have already successfully completed or CAS1 must have already successfully completed by a different thread since op began executing.

Likewise, by trivial inspection CAS3 is the only CAS which can update the b.next reference, therefore in the case of a failure, some other thread must have already successfully completed CAS3 since the beginning of op.

Like above, CAS4 is the only CAS which can change the *current* reference, therefore in the case of a failure, some other thread must have already successfully completed CAS4 since op began.

Lemma 2. Invoking the expand operation will execute a non-consistency changing instruction after a finite number of steps. Furthermore, given a total number of blocks numBlocks reachable in a FlowPool pool before invoking expand, the number of blocks numBlocks' after some finite number of steps is guaranteed to satisfy numBlocks' > numBlocks.

Proof. From inspection of the pseudocode, it is clear that the only point at which expand(b) can be invoked is under the condition that for some block b, b.index > LASTELEMPOS, where LASTELEMPOS is the maximum size set aside for elements of type Elem in any block. Given this, we will proceed by showing that a new block will be created with all related references b.next and current correctly set.

There are two conditions under which a non-consistency changing CAS instruction will be carried out.

- Case 1: if $b.next = \bot$, a new block nb will be created and CAS3 will be executed. From Lemma 1, we know that CAS3 must complete successfully

on some thread. Afterwards recursively calling expand on the original block b.

− Case 2: if $b.next \neq \bot$, CAS4 will be executed. Lemma 1 guarantees that CAS4 will update current to refer to b.next, which we will show can only be a new block. Likewise, Lemma 1 has shown that CAS3 is the only state changing instruction that can initiate a state change at location b.next, therefore, since CAS3 takes place within Case 1, Case 2 can only be reachable after Case 1 has been executed successfully. Given that Case 1 always creates a new block, therefore, b.next in this case, must always refer to a new block.

Therefore, since from Lemma 1 we know that both CAS3 and CAS4 can only fail if already completed guaranteeing their finite completion, and since CAS3 and CAS4 are the only state changing operations invoked through expand, the expand operation must complete in a finite number of steps.

Finally, since we saw in Case 2 that a new block is always created and related references are always correctly set, that is both b.next and current are correctly updated to refer to the new block, it follows that numBlocks strictly increases after some finite number of steps.

Lemma 3. After invoking append(elem), if CAS2 fails, then some thread has successfully completed CAS2 or CAS5 (or likewise, CAS6) after some finite number of steps.

Proof. First, we show that a thread attempting to complete CAS2 can't fail due to a different thread completing CAS1 so long as seal has not been invoked after completing the read of currobj. We address this exception later on.

Since after check, the only condition under which CAS1, and by extension, CAS2 can be executed is the situation where the current object currobj with index location idx is the Terminal object, it follows that CAS1 can only ever serve to duplicate this Terminal object at location idx + 1, leaving at most two Terminals in block referred to by current momentarily until CAS2 can be executed. By Lemma 1, since CAS1 is a non-consistency changing instruction, it follows that any thread holding any element elem' can execute this instruction without changing the expected value of currobj in CAS2, as no new object is ever created and placed in location idx. Therefore, CAS2 cannot fail due to CAS1, so long as seal has not been invoked by some other thread after the read of currobj.

This leaves only two scenarios in which consistency changing CAS2 can fail:

- Case 1: Another thread has already completed CAS2 with a different element elem'.
- Case 2: Another thread completes an invocation to the seal operation after the current thread completes the read of currobj. In this case, CAS2 can fail because CAS5 (or, likewise CAS6) might have completed before, in which case, it inserts a new Terminal object term into location idx (in the case of a seal invocation, $term.sealed ∈ \mathbb{N}$, or in the case of a doForAll invocation, $\{term.callbacks ∈ \}$).

We omit the proof and detailed discussion of CAS6 because it can be proven using the same steps as were taken for CAS5.

Lemma 4. Each operation executes only a finite number of steps between each state changing instruction.

Proof. We proceed by individually inspecting each operation which contains a state changing instruction.

The advance, check, totalElems, invokeCallbacks, and tryWriteSeal operations have a finite number of execution steps, as they contain no recursive calls, loops, or other possibility to restart.

The **append** operation is restarted in one of three cases:

Case 1: The call to the finite operation check returns false, causing call to
 advance followed by a recursive call to append with the same element elem
 which in turn once again calls check.

We show that after a finite number of steps, the *check* will evaluate to *true*, or some other thread will have completed a consistency changing operation since the initial invocation of *append*. In the case where *check* evaluates to *true*, Lemma 3 applies, as, it guarantees that a consistency changing CAS is completed after a finite number of steps.

When the call to the finite operation check returns false, if the subsequent advance finds that a Terminal object is at the current block index idx, then the next invocation of append will evaluate check to true. Otherwise, it must be the case that another thread has moved the Terminal to a subsequent index since the initial invocation of append, which is only possible using a consistency changing instruction.

Second, as long as advance finds that the element at idx is an Elem, it will increment idx. This can only happen a finite number of times until a Terminal is found in the current block, or some other thread has moved the Terminal to a subsequent index. However, the latter is only possible by successfully completing CAS2 after the initial invocation of append.

- Case 2: CAS1 fails, which we know from Lemma 1 means that it must've already been completed by another thread, triggering a recursive call append(elem) again on the same element elem.
- Case 3: CAS2 fails, which, by Lemma 3, indicates that either some other thread has already completed CAS2 with another element, or another consistency changing instruction, CAS5 or CAS6 has successfully completed. Afterwards, another recursive call to append(elem) is triggered on the same element elem.

Is this it?

Lemma 5. Assume a concurrent operation op is started. After a finite number of state changing instructions, a consistency changing CAS instruction is guaranteed to be successfully completed.

Proof.

Lemma 6. Assume a concurrent operation is started. If a consistency changing CAS instruction completes, some concurrent operation is guaranteed to be completed.

Proof.

 $Lock\mbox{-}freedom.$

A.1 Scratchpad

After invoking append, if check is false, a consistency changing CAS (CAS2, CAS5, or CAS6) is completed after a finite number of steps.

We have to show that we'll update *current* after a finite number of steps. The *expand* operation contains two CAS instructions; *CAS*3 and *CAS*4.

Lemma 1. In each operation there is a finite number of execution steps

between consecutive CAS instructions..

Proof. The append operation is restarted in three cases. Case 1: iff check returns $true \land CAS1$ fails. Case 2: . Case 3:

expand

tryWriteSeal

asyncDoForAll

Then, the operation corresponding to the consistency-changing CAS instruction is guaranteed to be eventually completed

If there's a CAS failing, then some other thread completes the CAS. Consistency change means progress.

OLD: *Proof.* Case 1: The failing CAS4 happens after a successful CAS3. From lemma 1, we know that CAS3, which is a check that precedes CAS4, is guaranteed to be successfully completed by some thread, so we focus on the implications of failure of CAS4. Case 2: CAS5 takes place if nb is null. Therefore, in both cases, CAS4 and CAS5 successfully complete.

 ${\bf Lemma~3.}~~consistency\mbox{-}changing~~CAS~~operations~~...~~will~~successfully~~complete.$

Proof. Uses \mathbb{A} .

Lemma 4. Assume that the FlowPool is consistent with some abstract state \mathbb{A} . If one of the operations advance or expand succeeds, the FlowPool will remain consistent with the abstract state \mathbb{A} following the operation.

Proof. The CAS operations, denoted CAS3, and CAS4 in the pseudo-code, within the expand operation neither affect elems nor sealed, thus by Definition 4, causes no consistency change. Likewise, the advance operation either calls expand once, or it invokes CAS1 it may update the index of the current block, neither of which cause a consistency change.

Lemma 5 (). If a consistency changing CAS completes, then the operation is guaranteed to successfully complete.

Lemma 6 (). append operation is lock-free.

Lemma 7 (). seal operation is lock-free.

Lemma 8 (). doForAll operation is lock-free.