

# Data Structures (Abstraction)

- ADT: Abstract Data Type

## Arrays

- A type of ADT for storing and accessing data in computer's memory
- Array Data Structure:
  - Homogenous data: Represents a sequence of elements of the same data type
  - Elements can be accessed, retrieved, stored or replaced at given index positions
- Random Access and Contiguous Memory:
  - Array indexing is a random access operation
  - Address of item: base address + offset
    - ◆ Index operation:
      1. Fetch base address of array's memory block
      2. Find target index by adding offset ( Index \* k ) to base address, k is number of memory cells required by an array item
- Advantage:
  - Access element directly (e.g. A[11] accesses 12th element)
  - Supported by many languages
  - Use less memory than linked structure
- Disadvantage:
  - A lot of data movement during operation e.g. adding/removing elements
  - Static, must declare array size, inflexible when more data is needed
- **One-Dimensional Array**
  - General form:

*mylist = [ ] \* MAXSIZE*

- Index from 1 to MAXSIZE ensuring total number of elements = MAXSIZE
- OR Index from 0 to MAXSIZE-1
  - ◆ Element name: [], e.g. scores[4]

- **for Loop** to read values into array:

- ◆ General form:

```
mylist = [ ]
for i in range(SIZE):
    value = input("enter value")
    mylist.append( value )
```

- **while Loop** to process data more than once:

- ◆ Read list up to X number of elements
- ◆ Using input -999 to end

```
mylist = [ ]
value = input("enter value")
while value is not "-999" or value is not -999:
    mylist.append( value )
```

- **Parallel Arrays:**

- ◆ Two or more arrays with same size and index

```
mylist1 = [ None for i in range(SIZE) ]
mylist2 = [ None for i in range(SIZE) ]

for i in range(SIZE):
    value1 = input("enter value 1: ")
    value2 = input("enter value 2: ")
    mylist1[ i ], mylist2[ i ] = value1, value2
```

- **Two-Dimensional Array (Matrix / Grid)**

- Used for information that fits naturally into a table
- Two subscripts are necessary to specify an element in a matrix
  - ◆ Row subscript
  - ◆ Column subscript
- General form:

```
matrix = [ [ None ] for i in range(COLUMN) ] for j in
range(ROW)                                     # initialise 2D array
matrix[0][0] = value                           # assign value
```

```

for row in matrix:                                # output in 2D format
    for column in row:
        print(column, end = " ")
    print()

```

## Dictionary

- A type of randomly accessed data structure
- Contains a key and a corresponding value associated with it
- Keys are unique in each dictionary, there isn't any duplicate keys
- Values aren't unique, multiple keys can correspond to the same value
- Initialise dictionary:

```

dictionary = { }
dictionary["abc"] = 101          # assign value to key
( dictionary[k] = v )

```

- Dictionary methods (built-in):
  - Get value of specified key (returns value):
 

```
dictionary.get("abc")
dictionary["abc"]
```
  - Get all dictionary keys (returns array):
 

```
dictionary.keys( )
```
  - Get all dictionary values (returns array):
 

```
dictionary.values( )
```
  - Get all dictionary items (returns array):
 

```
dictionary.items( )
```
  - Remove specified key (and value) from dictionary:
 

```
dictionary.pop("abc")    # error if specified element
                           isn't in dictionary
```
  - Check if key / value is in dictionary (returns boolean):
 

```
if k in dict.keys( ): ...
if v in dict.values( ): ...
```
- Sorting elements in a dictionary:

- Dictionaries aren't automatically sorted
- Returning values from dictionary may not be in the original/chronological order
- Built-in sorting functions:
  - ◆ By key:

```
sorted_elements = [ ]
for key in sorted( dictionary.keys( ) ):
    sorted_elements.append( key, dictionary[key] )
```

- ◆ By value:

```
sorted_elements = [ ]

for k, v in dictionary.items( ):
    sorted_elements.append([k, v])

sorted_elements.sort( key = lambda x: x[1] )
```

- Manually sorting:

```
sorted_elements = [ ]

while len( dictionary.keys( ) ) is not 0:
    # loops if dictionary isn't empty
    smallest_key, smallest_val = None, None

    for k, v in dictionary.items( ):
        # traverse dictionary to find smallest key / val
        if ( smallest_key == None ) or ( k < smallest_key ):
            # or v < smallest_val if sorting by value
            smallest_key, smallest_val = k, v

    sorted_elements.append( [smallest_key, smallest_val] )
    dictionary.pop( smallest_key )
    # remove smallest key from dictionary
```

## Linked Structure

- A type of structure that requires traversal, not randomly accessed

- Types:
  - Singly linked: Linking in one direction
  - Doubly linked: Linking in both directions
- Basic unit of representation: Node
  - Singly linked node contains:
    - ◆ Data value
    - ◆ Pointer to the next node
- Methods to set up singly linked array:
  - Two parallel arrays
  - Pointers
    - ◆ Specified value (e.g. None or 0) represents end of structure
    - ◆ Python: "None" can be used as empty link
- Start pointer points to the first node
- End node with "null" as next value to indicate the end of linked list
- Defining singly linked node class:
  - Flexibility and ease of use are critical
  - Node instance variables are usually referenced without method calls
  - Constructors allow user to set a node's link when node is created

```
class Node(object):
    def __init__(self, data, next = None):
        self.data = data
        self.next = next
```

- Using singly linked node class:
  - Node variables are initialised to "None" or a new "Node" object

```
node1 = None    # empty link
node2 = Node ( "A", None )    #node containing data and
empty link (End node)
node3 = Node ( "B", node2 )    # node containing data and a
link to node2
```

- Operations on singly linked structures:
  - Traversal:
    - ◆ Visit each node without deleting it

- ◆ Uses a temporary pointer variable

```

curr = head
while curr != None:      # None serves as sentinel to stop
process
    <use or modify curr.data>
    curr = curr.next

```

- Searching:

- Resembles a traversal
- Two possible sentinels;
  1. Empty link
  2. Data item that equals to target item

```

curr = head
while ( curr != None ) and ( curr.data != targetItem ):
    curr = curr.next
if curr != None:
    <target has been found>
else:
    <target is not in linked structure>

```

- Accessing *i*th item is sequential structure:

```

# Assume 0 <= i < n
# i is item to be accessed
# n is number of nodes in structure

```

```

curr = head
while i > 0:
    curr = curr.next
    i = i - 1
return curr.data

```

- Traversal to access specified value:

- If target item not present: no replacement occurs, operation returns False
- If target item is present: new item replaces it, operation returns True

```

curr = head
while ( curr != None ) and ( target != curr.data ):

```

```

    curr = curr.next
    if curr != None:
        return curr.data
    else:
        # not found
        return None

```

- Replacing *i*th item:

```

# Assume 0 <= i < n:
# i is item to be processed
# n is number of nodes in structure

```

```

curr = head
while i > 0:
    curr = curr.next
    i = i - 1
curr.data = newItem

```

- Inserting at beginning:

```

newNode = Node(newItem)
newNode.next = head.next
head.next = newNode

```

- Advantage:
  - Little data movement, no shifting of items needed for insertion or removal, only need to change pointer
- Disadvantage:
  - No random access, must traverse list

## Binary Search Tree

## # notes incoming

- A tree of nodes
- Nodes contain 3 types of values:
  - Data value (can be more than 1 data value)
  - Left pointer
  - Right pointer
- Traverse by comparing target to the current data:
  - If target < current data: move left
  - If target > current data: move right

- **Node:**

```
class Node:
    def __init__(self, data, left, right):
        self.data = data
        self.left, self.right = left, right
```

- **Implementation using array:**

```
class BST_Array:
    def __init__(self, MAXSIZE):
        self.tree = [None] for i in range(MAXSIZE + 1)
        self.root = 0
        self.nextfree = 1

        for i in range(1, MAXSIZE):
            self.tree[i] = Node("", 0, i+1)          #
chaining using right ptr
            self.tree[MAXSIZE] = Node("", 0, 0)

    def AddItemIterative(new):
        if self.nextfree == 0:                      # tree is
full
            print("tree is full!")
            return ""

        target = self.nextfree
        self.tree[target] = new

        if self.root == 0:                          # tree is
empty
            self.nextfree = self.tree[target].right
            self.tree[target].right = 0

        else:                                        #
traverse tree
            curr = self.root
            prev = None
            lastmove = ""

            while curr is not 0:
```



```

prev = curr

if target < self.tree[curr].data:    # move
left
    last = "L"
    curr = self.tree[curr].left

else:
    last = "R"
    curr = self.tree[curr].right

if lastmove = "L":                # adjust
previous node's ptr
    self.tree[prev].left = target
else:
    self.tree[prev].right = target

self.nextfree = self.tree[target].right
self.tree[target].right = 0

def AddItemRecursive(self, value, curr):
    if self.nextfree == 0:          #
tree is full
        print("tree is full!")
        return ""

    else:
        target = self.nextfree

        if self.root == 0:          #
tree is empty
            self.root = target      #
insert at root

            self.tree[target].data = value
            self.nextfree = self.tree[target].right
            self.tree[target].right = 0

            return ""

    else:
        curr_node = self.tree[curr]    #

```

*assign ptr for easy reference*

```

                                if value < curr_node.data:           #
compares value
                                if curr_node.left != 0:           #
moves left
                                self.AddItemRecursive(value,
curr_node.left)

                                else:                             #
location found
                                curr_node.left = target           #
insert
                                self.tree[target].data = value
                                self.nextfree =
self.tree[target].right
                                self.tree[target].right = 0

                                else:                             #
compares value
                                if curr_node.right != 0:           #
moves right
                                self.AddItemRecursive(value,
curr_node.right)

                                else:                             #
location found
                                curr_node.right = target           #
insert
                                self.tree[target].data = value
                                self.nextfree =
self.tree[target].right
                                self.tree[target].right = 0

def GetRoot(self):
    return self.root

def InOrderTraversal(self, root):
    if root != 0:
        self.InOrderTraversal(self.tree[root].left)
        print(self.tree[root].data)
```

*self.InOrderTraversal(self.tree[root].right)*

- **Implementation using direct pointers (referencing memory space):**

```
class BST_Dir:
    def __init__(self):
        self.root = None

    def AddItemIterative(self, value):
        # check for max size if required

        if self.root == None:                                     #
tree is empty                                                self.root = Node(value)      #
insert                                                         return ""

        else:                                                    #
tree is not empty

            curr = self.root
            prev = None
            lastmove = ""

            while curr != None:                                   #
find location to insert

                prev = curr

                if value < curr.data:                             #
move left

                    lastmove = "L"
                    curr = curr.left

                else:                                             #
move right

                    lastmove = "R"
                    curr = curr.right

            if lastmove == "L":                                   #
insert
```

```

        prev.left = Node(value)
    else:
        prev.right = Node(value)

    def AddItemRecursive_M1(self, value, tree):          #
recursive method 1
        # check for max size if required

        if tree == None:                                #
location found, insert
            return Node(value)

        elif value < tree.data:                          #
compare values
            if tree.left == None:                        #
location found, insert
                tree.left = Node(value)

            else:                                         #
continue traversal
                self.AddItemRecursive_M1(self, value,
tree.left)

        else:                                           #
compare values
            if tree.right == None:                      #
location found, insert
                tree.right = Node(value)

            else:                                         #
continue traversal
                self.AddItemRecursive_M1(self, value
tree.right)

    def AddItemRecursive_M2(self, value, tree):
        # check for max size if required

        if self.root == None:                          #
tree is empty
            self.root = Node(value)
            return ""

```

```

        else:                                     #
tree is not empty
        if tree == None:                         #
location found
            return Node(value)                   #
return value back to original function

        elif value < tree.value:                 #
compare values
            node = self.AddItemRecursive_M2(self,
value, tree.left)
                                                    #
traverse to find location
            tree.left = node                     #
insert
            return node                          #
return value back to original function

        else:                                    #
compare values
            node = self.AddItemRecursive_M2(self,
value, tree.right)
                                                    #
traverse to find locartion
            tree.right = node                    #
insert
            return node                          #
return value back to original function

        # node value is returned to original function to
establish pointer chain

def InOrder(self, tree):
    if tree is not None:
        self.InOrder(tree.left)
        print(tree.data)
        self.InOrder(tree.right)

```

## Stacks

- FILO (first-in-last-out) / LIFO (last-in-first-out) structure
  - First item to be pushed into the stack is the last to be removed
  - Last item to be pushed into the stack is the first to be removed
- Access is completely restricted to just one end, called the "top"
- Stack methods:
  - *self.push(item)*: inserts item at top of stack
  - *self.pop()*: removes and returns item at the top of stack, if stack is not empty
  - *self.peek()*: returns item at top of stack, if stack is not empty, does not remove item
  - *self.isEmpty()*: returns True if stack is empty, otherwise False
  - *self.\_\_len\_\_()*: returns the number of elements in the stack currently, same as len(s)
  - *self.\_\_str\_\_()*: returns the string representation of the stack, same as str(s)
- Applications of Stacks:
  - Evaluating arithmetic expressions:
    - ◆ Infix form: operator located between operands (A+B)
      - ◆ Sometimes require parentheses
      - ◆ Involves rules of mathematical operation
      - ◆ E.g.  $(33 + 22 * 2 = 33 + 44 = 78)$
    - ◆ Postfix form: operator immediately follows operands (A B +)
      - ◆ Does not require parentheses
      - ◆ Evaluation applies operators as soon as they are encountered
      - ◆ E.g.  $(34\ 22\ 2\ *\ + = 34\ 44\ + = 78)$
  - Evaluating Infix to Postfix:
    1. Start with empty postfix expressions and empty stack (stack holds operators and left parentheses)
    2. Scan across infix expressions from left to right
    3. Encounter operand: append to postfix expression
    4. Encounter '(': push into stack
    5. Encounter operator:
      1. Pop all operators from stack with equal or higher precedence
      2. Append to postfix expression
      3. Push scanned operator onto stack
    6. Encounter ')': pop all operators from stack to postfix

expression until meeting matching '(', discard '('

7. Encounter end of infix expression: pop remaining operators from stack to postfix expression

○ Evaluating Postfix:

1. Scan across postfix expression from left to right
2. Encounter operator: apply it to two preceding operands, replace all three expressions with result
3. Continue scanning until the end of expression has been reached

*Create new stack*

*While postfix expression is not empty:*

*Get next token*

*If token is operand:*

*Push token into stack*

*Else:*

*If token is operator:*

*Pop the top two operands from stack*

*Apply operator to the two operands*

*Push resulting value into stack*

*EndIf*

*EndWhile*

*Return final value*

○ Memory management:

- ◆ Keeps track of details during programme runtime
  - ◆ When a function calls another function, it interrupts its own execution and needs to be able to resume its excursion in the same state it was in when it was interrupted
  - ◆ LIFO behaviour
- ◆ When a function is called:
  1. Push a copy of its activation record onto the runtime stack
  2. Copy its arguments into parameter spaces
  3. Transfer control to starting address of the body of function
- ◆ Top activation record in the runtime stack is always the function that's currently being executed
- ◆ When a function terminates:
  1. Pop activation record or terminated function from

runtime stack

2. Use new top activation record to restore environment of interrupted function and resume execution of the interrupted function

○ Implementation:

◆ Using array:

```
class ArrayStack:
    CAPACITY = 100

    def __init__(self):
        self.items = list( )
        for i in range( ArrayStack.CAPACITY ):
            self.items.append( None )
        self.top = -1
        self.size = 0

    def push(self, newItem):
        if self.isFull( ):
            print("Stack is full")
            return ""
        else:
            self.size += 1
            self.top += 1
            self.items[self.top] = newItem

    def pop(self):
        if self.isEmpty( ):
            print("Stack is empty")
            return ""
        else:
            oldItem = self.items[self.top]
            self.top -= 1
            self.size -= 1
            return oldItem

    def peek(self):
        if self.isEmpty( ):
            print("Stack is empty")
            return ""
        else:
```



```

        return self.items[self.top]

def __len__(self):
    return self.size

def isEmpty(self):
    return self.size == 0

def isFull(self):
    return self.size == ArrayStack.CAPACITY

def __str__(self):
    res = ""
    for i in range( len(self) ):
        res = res + str( self.items[i] ) + " "
    return res

```

◆ Using linked structure:

```

class Node:
    def __init__(self, data, next):
        self.data = data
        self.next = next

class LinkedStack:
    def __init__(self):
        self.top = None
        self.size = 0

    def push(self, newItem):
        newNode = Node( newItem, self.top )
        self.top = newNode
        self.size += 1

    def pop(self):
        if self.isEmpty():
            print("Stack is empty")
            return ""
        else:
            oldItem = self.top.data
            self.top = self.top.next

```

```

        self.size -= 1
        return oldItem

    def peek(self):
        if self.isEmpty():
            print("Stack is empty")
            return ""
        else:
            return self.top.data

    def __len__(self):
        return self.size

    def isEmpty(self):
        return self.size == 0

    def __str__(self):
        res = ""
        curr = self.top
        while curr != None:
            res += str( self.top.data ) + " "
            curr = curr.next
        return res

```

## Queue

- Insertion is restricted to the **rear**
  - "enqueue" to add item to rear of queue
- Removal restricted to the **front**
  - "dequeue" to remove item from front of queue
- FIFO (first-in-first-out) structure
- Queue methods:
  - self.enqueue(item): inserts item at rear of queue
  - self.dequeue(): removes and returns item at front of queue (queue must not be empty)
  - self.peak(): returns item at front of queue
  - self.isEmpty(): returns True if queue is empty, otherwise False
  - self.\_\_len\_\_(): returns number of items in queue
  - self.\_\_str\_\_(): returns string representation of queue
- Implementation:

- Linked Structure:

```
class Node:
```

```
    def __init__(self, data, next):  
        self.data = data  
        self.next = next
```

```
class LinkedQueue( object ):
```

```
    def __init__(self):  
        self.front = None  
        self.size = 0  
        self.rear = None
```

```
    def enqueue(self, newItem):  
        newNode = Node( newItem, None )  
        if self.isEmpty( ):  
            self.front = newNode  
        else:  
            self.rear.next = newNode  
        self.rear = newNode  
        self.size += 1
```

```
    def dequeue(self):  
        if self.isEmpty( ):  
            print("Queue is empty")  
            return ""  
        else:  
            oldItem = self.front.data  
            self.front = self.front.next  
            if self.front == None:          #queue is empty  
                self.rear = None  
            self.size -= 1  
            return oldItem
```

```
    def peek(self):  
        if self.isEmpty( ):  
            print("Queue is empty")  
            return ""  
        else:  
            return self.front.data
```

```

def __len__(self):
    return self.size

def isEmpty(self):
    return self.size == 0

def __str__(self):
    res = ""
    curr = self.front
    while curr != None:
        res += str( curr.data ) + " "
        curr = curr.next
    return res

```

○ Linear Array:

```

class ArrayQueue(object):
    CAPACITY = 100

    def __init__(self):
        self.items = list( )
        for i in range ArrayQueue.CAPACITY:
            self.items.append( None )
        self.rear = -1
        self.size = 0

    def enqueue(self, newItem):
        if self.isFull( ):
            print("Queue is full")
            return ""
        else:
            self.rear += 1
            self.size += 1
            self.items[self.rear] = newItem

    def dequeue(self):
        if self.isEmpty( ):
            print("Queue is empty")
            return ""
        else:
            oldItem = self.items[0]

```

```

        for i in range ( self.size-1 ):
            self.items[i] = self.items[i+1]
        self.rear -= 1
        self.size -= 1
        return oldItem

def peek(self):
    if self.isEmpty( ):
        print("Queue is empty")
        return ""
    else:
        return self.items[0]

def __len__(self):
    return self.size

def isEmpty(self):
    return self.size == 0

def isFull(self):
    return self.size == ArrayQueue.CAPACITY

def __str__(self):
    res = ""
    if self.isEmpty( ):
        print("Queue is empty")
        return ""
    else:
        for i in range( self.size );
            res += str( self.items[i] ) + " "
        return res

```

○ Cyclic Array:

```

class ArrayQueue:
    CAPACITY = 100

    def __init__(self):
        self.items = list( )
        for i in range ArrayQueue.CAPACITY:
            self.items.append(None)

```

```
self.size = 0
self.front = 0
self.rear = -1
```

```
def enqueue(self, newItem):
    if self.isFull():
        print("Queue is full")
        return ""
    else:
        if self.rear == ArrayQueue.CAPACITY - 1: #end of
```

array

```
        self.rear = 0
    else:
        self.rear += 1
    self.items[self.rear] = newItem
    self.size += 1
```

```
def dequeue(self):
    if self.isEmpty():
        print("Queue is empty")
        return ""
    else:
        oldItem = self.items[self.front]
        if self.front == ArrayQueue.CAPACITY - 1: #end
```

of array

```
        self.front = 0
    else:
        self.front += 1
    self.size -= 1
    return oldItem
```

```
def peek(self):
    if self.isEmpty():
        print("Queue is empty")
        return ""
    else:
        return self.items[self.front]
```

```
def __len__(self):
    return self.size
```

```
def isEmpty(self):
    return self.size == 0

def isFull(self):
    return self.size == ArrayQueue.CAPACITY

def __str__(self):
    res = ""
    curr = self.front
    for i in range(self.size):
        res += str(self.items[curr]) + " "
        if curr == ArrayQueue.CAPACITY-1:
            curr = 0
        else:
            curr += 1
    return res
```