Data Structures (Abstraction)

- ADT: Abstract Data Type

Arrays

- A type of ADT for storing and accessing data in computer's memory
- Array Data Structure:
    - Homogenous data: Represents a sequence of elements of the same data type
    - Elements can be accessed, retrieved, stored or replaced at given index positions
- Random Access and Contiguous Memory
- Advantage:
    - Access element directly (e.g. A[11] accesses 12th element)
    - Supported by many languages
    - Use less memory than linked structure
- Disadvantage:
    - A lot of data movement during operation e.g. adding/ removing elements
    - Static, must declare array size, inflexible when more data is needed

- **One-Dimensional Array**
    - General form:

      *mylist = [ ] * MAXSIZE*

    - Index from 1 to MAXSIZE ensuring total number of elements = MAXSIZE
    - OR Index from 0 to MAXSIZE-1
        - Element name: [], e.g. scores[4]
    - **for Loop** to read values into array:
        - General form:

```
mylist = [ ]
for i in range(SIZE):
    value = input("enter value")
```

mylist.append(value)

- **while Loop** to process data more than once:
  - Read list up to X number of elements
  - Using input -999 to end

mylist = [ ]
value = input("enter value")
while value is not "-999" or value is not -999:
    mylist.append(value)

- **Parallel Arrays:**
  - Two or more arrays with same size and index

mylist1 = [None for i in range(SIZE)]
mylist2 = [None for i in range(SIZE)]

for i in range(SIZE):
    value1 = input("enter value 1: ")
    value2 = input("enter value 2: ")
    mylist1[i], mylist2[i] = value1, value2

- **Two-Dimensional Array (Matrix / Grid)**
  - Used for information that fits naturally into a table
  - Two subscripts are necessary to specify an element in a matrix
    - Row subscript
    - Column subscript
  - General form:

 # initialise 2D array
matrix = [[None] for i in range(COL)] for j in range(ROW)

 # assign value
matrix[0][0] = value

 # output in 2D format
for row in matrix:
    for column in row:

print(*column*, *end* = " ")
print( )

Dictionary

- A type of randomly accessed data structure
- Contains a key and a corresponding value associated with it
- Keys are unique in each dictionary, there isn't any duplicate keys
- Values aren't unique, multiple keys can correspond to the same value
- Initialise dictionary:

```
dictionary = { }

# assign value to key ( dictionary[k] = v )
dictionary["abc"] = 101
```

- Dictionary methods (built-in):
  - Get value of specified key (returns value):
    - *dictionary.get*("abc")
      - *# returns None if key not in dictionary*
    - *dictionary*["abc"]

  - Get all dictionary keys (returns array):
    - *dictionary.keys*( )

  - Get all dictionary values (returns array):
    - *dictionary.values*( )

  - Get all dictionary items (returns array):
    - *dictionary.items*( )

  - Remove specified key (and value) from dictionary:
    - *dictionary.pop*("abc")*# error if specified element isn't in dictionary*

  - Check if key / value is in dictionary (returns boolean):
    - *dictionary.get*("abc")
      - *# returns None if key not in dictionary*
    - *if k in dictionary.keys*( ): ...

- *if v in dictionary.values( ): …*

- Sorting elements in a dictionary:
  - Dictionaries aren't automatically sorted
  - Returning values from dictionary may not be in the original/chronological order
  - Built-in sorting functions:
    - By key:

```
sorted_elements = [ ]
for key in sorted( dictionary.keys( ) ):
    sorted_elements.append( key, dictionary[key] )
```

    - By value:

```
sorted_elements = [ ]

for k, v in dictionary.items( ):
    sorted_elements.append([k, v])

sorted_elements.sort( key = lambda x: x[1] )
```

  - Manually sorting:

```
sorted_elements = [ ]

# loops if dictionary isn't empty
while len( dictionary.keys( ) ) is not 0:
    smallest_key, smallest_val = None, None

    # traverse dictionary to find smallest key / val
    for k, v in dictionary.items( ):

        # or v < smallest_val if sorting by value
        if ( smallest_key == None ) or ( k < smallest_key):
            smallest_key, smallest_val = k, v

    sorted_elements.append( [smallest_key, smallest_val] )

    # remove smallest key from dictionary
```

dictionary.pop(smallest_key)

Linked Structure

- A type of structure that requires traversal, not randomly accessed
- Types:
    - Singly linked: Linking in one direction
    - Doubly linked: Linking in both directions
- Basic unit of representation: Node
    - Singly linked node contains:
        - Data value
        - Pointer to the next node
- Methods to set up singly linked array:
    - Two parallel arrays
    - Pointers
        - Specified value (e.g. None or 0) represents end of structure
        - Python: "None" can be used as empty link
- Start pointer points to the first node
- End node with "null" as next value to indicate the end of linked list
- Defining singly linked node class:
    - Flexibility and ease of use are critical
    - Node instance variables are usually referenced without method calls
    - Constructors allow user to set a node's link when node is created

```
class Node(object):
    def __init__ (self, data, next = None):
        self.data = data
        self.next = next
```

- Using singly linked node class:
    - Node variables are initialised to "None" or a new "Node" object

```
node1 = None      # empty link

#node containing data and empty link (End node)
```

```
node2 = Node ( "A", None )

# node containing data and a link to node2
node3 = Node ( "B", node2 )
```

- Operations on singly linked structures:
  - Traversal:
    - Visit each node without deleting it
    - Uses a temporary pointer variable

```
curr = head

# None serves as sentinel to stop process
while curr != None:
    <use or modify curr.data>
    curr = curr.next
```

- Searching:
  - Resembles a traversal
  - Two possible sentinels;
    1. Empty link
    2. Data item that equals to target item

```
curr = head
while ( curr != None ) and ( curr.data != targetItem ):
    curr = curr.next
if curr != None:
    <target has been found>
else:
    <target is not in linked structure>
```

- Accessing *i*th item is sequential structure:

```
# Assume  0 <= i < n
# i is item to be accessed
# n is number of nodes in structure

curr = head

while i > 0:
    curr = curr.next
    i = i - 1
```

```
return curr.data
```

- Traversal to access specified value:
  - If target item not present: no replacement occurs, operation returns False
  - If target item is present: new item replaces it, operation returns True

```
curr = head

# traverse to find target
while ( curr != None ) and ( target != curr.data ):
    curr = curr.next

# found
if curr != None:
    return curr.data

# not found
else:
    return None
```

- Replacing *i*th item:

```
# Assume  0 <= i < n:
# i is item to be processed
# n is number of nodes in structure

curr = head

while i >  0:
    curr = curr.next
    i = i - 1

curr.data = newItem
```

- Inserting at beginning:

```
newNode = Node(newItem)
newNode.next = head.next
```

```
head.next = newNode
```

- Advantage:
  - Little data movement, no shifting of items needed for insertion or removal, only need to change pointer
- Disadvantage:
  - No random access, must traverse list

Binary Search Tree

- A tree of nodes
- Nodes contain 3 types of values:
  - Data value (can be more than 1 data value)
  - Left pointer
  - Right pointer
- Traverse by comparing target to the current data:
  - If target < current data: move left
  - If target > current data: move right

- **Node:**

```
class Node:
    def __init__(self, data, left, right):
        self.data = data
        self.left, self.right = left,  right
```

- **Implementation using array:**

```
class BST_Array:
    def __init__(self, MAXSIZE):
        self.tree = [None] for i in range(MAXSIZE + 1)
        self.root = 0
        self.nextfree = 1

        # chaining using right ptr
        for i in range(1, MAXSIZE):
            self.tree[i] = Node("", 0, i+1)
        self.tree[MAXSIZE] = Node("", 0, 0)

    def AddItem_Iter(new):
```

```
        # tree is full
        if self.nextfree == 0:
            print("tree is full!")
            return ""

        target = self.nextfree
        self.tree[target] = new

        # tree is empty
        if self.root == 0:
            self.nextfree = self.tree[target].right
            self.tree[target].right = 0

        # traverse tree to find position to insert
        else:
            curr = self.root
            prev = None
            lastmove = ""

            while curr is not 0:
                prev = curr

                if target < self.tree[curr].data:
                    last = "L"
                    curr = self.tree[curr].left

                else:
                    last = "R"
                    curr = self.tree[curr].right

            # adjust previous node's ptr
            if lastmove = "L":
                self.tree[prev].left = target
            else:
                self.tree[prev].right = target

            self.nextfree = self.tree[target].right
            self.tree[target].right = 0

    def AddItem_Rec(self, value, curr):
```

```
        # tree is full
        if self.nextfree == 0:
            print("tree is full!")
            return ""

        else:
            target = self.nextfree

            # tree is empty, insert at root
            if self.root == 0:
                self.root = target
                self.tree[target].data = value
                self.nextfree = self.tree[target].right
                self.tree[target].right = 0

                return ""

            else:
                curr_node = self.tree[curr]

                if value < curr_node.data:

                    # moves left
                    if curr_node.left != 0:
                        self.AddItem_Rec(value,
curr_node.left)

                    # location found, insert
                    else:
                        curr_node.left = target
                        self.tree[target].data = value
                        self.nextfree =
self.tree[target].right
                        self.tree[target].right = 0

                else:
                    if curr_node.right != 0:
                        self.AddItem_Rec(value,
curr_node.right)
```

```
                    # location found, insert
                    else:
                        curr_node.right = target
                        self.tree[target].data = value
                        self.nextfree =
self.tree[target].right
                        self.tree[target].right = 0

    def  GetRoot(self):
        return self.root

    def InOrderTraversal(self, root):
        if root != 0:
            self.InOrderTraversal(self.tree[root].left)
            print(self.tree[root].data)
            self.InOrderTraversal(self.tree[root].right)
```

- **Implementation using direct pointers (referencing memory space):**

```
class BST_Dir:
    def __init__(self):
        self.root = None

    def AddItem_Iter(self, value):
        # check for max size if required

        # tree is empty, insert
        if self.root == None:
            self.root = Node(value)
            return ""

        else:
            curr = self.root
            prev = None
            lastmove = ""

            # find location to insert
            while curr != None:
```

```
            prev = curr

            # move left
            if value < curr.data:
                lastmove = "L"
                curr = curr.left

            # move right
            else:
                lastmove = "R"
                curr = curr.right

        # insert
        if lastmove == "L":
            prev.left = Node(value)
        else:
            prev.right = Node(value)

# recursive method 1
def AddItem_Rec_M1(self, value, tree):
    # check for max size if required

    # location found, insert
    if tree == None:
        return Node(value)

    elif value < tree.data:
        # location found, insert
        if tree.left  == None:
            tree.left = Node(value)

        else:
            self.AddItem_Rec_M1(self, value, tree.left)

    else:
        # location found, insert
        if tree.right == None:
            tree.right = Node(value)

        else:
            self.AddItem_Rec_M1(self, value tree.right)
```

```
# recursive method 2
def AddItem_Rec_M2(self, value, tree):
    # check for max size if required

    # tree is empty, insert
    if self.root == None:
        self.root = Node(value)
        return ""

    else:
        # location found, return node
        if tree == None:
            return Node(value)

        elif value < tree.value:
            # traverse to find location
            node = self.AddItem_Rec_M2(self, value,
tree.left)

            # location found, insert, return node
            tree.left = node
            return node

        else:
            # traverse to find location
            node = self.AddItem_Rec_M2(self, value,
tree.right)

            # location found, insert, return node
            tree.right = node
            return node

    # node value is returned to original function to
establish pointer chain

def InOrder(self, tree):
    if tree is not None:
        self.InOrder(tree.left)
        print(tree.data)
```

self.InOrder(*tree.right*)

Stacks

- FILO (first-in-last-out) / LIFO (last-in-first-out) structure
  - First item to be pushed into the stack is the last to be removed
  - Last item to be pushed into the stack is the first to be removed
- Access is completely restricted to just one end, called the "top"
- Stack methods:
  - *self.push*(*item*): inserts item at top of stack
  - *self.pop*( ): removes and returns item at the top of stack, if stack is not empty
  - *self.peek*( ): returns item at top of stack, if stack is not empty, does not remove item
  - *self.isEmpty*( ): returns True if stack is empty, otherwise False
  - *self.__len__*( ): returns the number of elements in the stack currently, same as len(s)
  - *self.__str__*( ): returns the string representation of the stack, same as str(s)
- Applications of Stacks:
  - Evaluating arithmetic expressions:
    - Infix form: operator located between operands (A+B)
      - Sometimes require parentheses
      - Involves rules of mathematical operation
      - E.g. (33 + 22 * 2 = 33 + 44 = 78)
    - Postfix form: operator immediately follows operands (A B +)
      - Does not require parentheses
      - Evaluation applies operators as soon as they are encountered
      - E.g. (34 22 2 * + = 34 44 + = 78)
  - Evaluating Infix to Postfix:
    1. Start with empty postfix expressions and empty stack (stack holds operators and left parentheses)
    2. Scan across infix expressions from left to right
    3. Encounter operand: append to postfix expression
    4. Encounter '(': push into stack
    5. Encounter operator:

1. Pop all operators from stack with equal or higher precedence
2. Append to postfix expression
3. Push scanned operator onto stack

6. Encounter ')': pop all operators from stack to postfix expression until meeting matching '(', discard '('
7. Encounter end of infix expression: pop remaining operators from stack to postfix expression

- Evaluating Postfix:
  1. Scan across postfix expression from left to right
  2. Encounter operator: apply it to two preceding operands, replace all three expressions with result
  3. Continue scanning until the end of expression has been reached

```
Create new stack
While postfix expression is not empty:
    Get next token
    If token is operand:
        Push token into stack
    Else:
        If token is operator:
            Pop the top two operands from stack
            Apply operator to the two operands
            Push resulting value into stack
    EndIf
EndWhile
Return final value
```

- Implementation:
  - Using array:

```
class ArrayStack:
    CAPACITY = 100

    def __init__(self):
        self.items = list( )
        for i in range( ArrayStack.CAPACITY ):
            self.items.append( None )
        self.top = -1
        self.size = 0
```

```python
        def push(self, newItem):
            if self.isFull( ):
                print("Stack is full")
                return ""
            else:
                self.size += 1
                self.top += 1
                self.items[self.top] = newItem

        def pop(self):
            if self.isEmpty( ):
                print("Stack is empty")
                return ""
            else:
                oldItem = self.items[self.top]
                self.top -= 1
                self.size -= 1
                return oldItem

        def peek(self):
            if self.isEmpty( ):
                print("Stack is empty")
                return ""
            else:
                return self.items[self.top]

        ~def ( __len__, isEmpty, isFull, __str__)~
```

- Using linked structure:

```python
    class Node:
        def __init__(self, data, next):
            self.data = data
            self.next = next

    class LinkedStack:
        def __init__(self):
            self.top = None
            self.size = 0
```

```
def push(self, newItem):
    newNode = Node( newItem, self.top )
    self.top = newNode
    self.size += 1

def pop(self):
    if self.isEmpty( ):
        print("Stack is empty")
        return ""
    else:
        oldItem = self.top.data
        self.top = self.top.next
        self.size -= 1
        return oldItem

def peek(self):
    if self.isEmpty( ):
        print("Stack is empty")
        return ""
    else:
        return self.top.data

~def ( __len__, isEmpty, __str__)~
```

Queue

- Insertion is restricted to the **rear**
  - "enqueue" to add iem to rear of queue
- Removal restricted to the **front**
  - "dequeue" to remove item from front of queue
- FIFO (first-in-first-out) structure
- Queue methods:
  - self.enqueue(item): inserts item at rear of queue
  - self.dequeue( ): removes and returns item at front of queue (queue must not be empty)
  - self.peak( ): returns item at front of queue
  - self.isEmpty( ): returns True if queue is empty, otherwise False
  - self.__len__( ): returns number of items in queue
  - self.__str__( ): returns string representation of queue

```python
def __str__(self):
    res = ""
    curr = self.front
    while curr != None:
        res += str( curr.data ) + " "
        curr = curr.next
    return res
```

- Implementation:
  - Linked Structure:

```python
class Node:
    def __init__(self, data, next):
        self.data = data
        self.next = next

class LinkedQueue( object ):
    def __init__(self):
        self.front = None
        self.size = 0
        self.rear = None

    def enqueue(self, newItem):
        newNode = Node( newItem, None )

        if self.isEmpty( ):
            self.front = newNode

        else:
            self.rear.next = newNode
        self.rear = newNode
        self.size += 1

    def dequeue(self):
        if self.isEmpty( ):
            print("Queue is empty")
            return ""

        else:
```

```
            oldItem = self.front.data
            self.front = self.front.next

            #queue is empty
            if self.front == None:
                self.rear = None
            self.size -= 1

        return oldItem

    def peek(self):
        if self.isEmpty( ):
            print("Queue is empty")
            return ""

        else:
            return self.front.data

    def __len__(self):
        return self.size

    def isEmpty(self):
        return self.size == 0
```

- Linear Array:

```
class ArrayQueue(object):
    CAPACITY = 100

    def __init__(self):
        self.items = list( )

        for i in range ArrayQueue.CAPACITY:
            self.items.append( None )

        self.rear = -1
        self.size = 0

    def enqueue(self, newItem):
        if self.isFull( ):
```

```
            print("Queue is full")
            return ""

        else:
            self.rear += 1
            self.size += 1
            self.items[self.rear] = newItem

    def dequeue(self):
        if self.isEmpty( ):
            print("Queue is empty")
            return ""

        else:
            oldItem = self.items[0]

            for i in range ( self.size-1 ):
                self.items[i] = self.items[i+1]

            self.rear -= 1
            self.size -= 1
            return oldItem

    def peek(self):
        if self.isEmpty( ):
            print("Queue is empty")
            return ""
        else:
            return self.items[0]

    def isEmpty(self):
        return self.size == 0

    def isFull(self):
        return self.size == ArrayQueue.CAPACITY
```

- Cyclic Array:

```
class ArrayQueue:
```

```
CAPACITY = 100

def __init__(self):
    self.items = list( )

    for i in range ArrayQueue.CAPACITY:
        self.items.append(None)

    self.size = 0
    self.front = 0
    self.rear = -1

def enqueue(self, newItem):
    if self.isFull( ):
        print("Queue is full")
        return ""

    else:
        if self.rear = ArrayQueue.CAPACITY - 1: #end of
array
            self.rear = 0

        else:
            self.rear += 1
        self.items[self.rear] = newItem
        self.size += 1

def dequeue(self):
    if self.isEmpty( ):
        print("Queue is empty")
        return ""

    else:
        oldItem = self.items[self.front]
        if self.front = ArrayQueue.CAPACITY - 1: #end
of array
            self.front = 0
        else:
            self.front += 1
        self.size -= 1
        return oldItem
```