

Data Structures (Abstraction)

- ADT: Abstract Data Type

Arrays

- A type of ADT for storing and accessing data in computer's memory
- Array Data Structure:
 - Homogenous data: Represents a sequence of elements of the same data type
 - Elements can be accessed, retrieved, stored or replaced at given index positions
- Random Access and Contiguous Memory:
 - Array indexing is a random access operation
 - Address of item: base address + offset
 - ◆ Index operation:
 1. Fetch base address of array's memory block
 2. Find target index by adding offset (Index * k) to base address, k is number of memory cells required by an array item
- Advantage:
 - Access element directly (e.g. A[11] accesses 12th element)
 - Supported by many languages
 - Use less memory than linked structure
- Disadvantage:
 - A lot of data movement during operation e.g. adding/ removing elements
 - Static, must declare array size, inflexible when more data is needed
- **One-Dimensional Array**
 - General form:

*mylist = [] * MAXSIZE*

- Index from 1 to MAXSIZE ensuring total number of elements = MAXSIZE
- OR Index from 0 to MAXSIZE-1
 - ◆ Element name: [], e.g. scores[4]

- **for Loop** to read values into array:

- ◆ General form:

```
mylist = [ ]
for i in range(SIZE):
    value = input("enter value")
    mylist.append( value )
```

- **while Loop** to process data more than once:

- ◆ Read list up to X number of elements
- ◆ Using input -999 to end

```
mylist = [ ]
value = input("enter value")
while value is not "-999" or value is not -999:
    mylist.append( value )
```

- **Parallel Arrays:**

- ◆ Two or more arrays with same size and index

```
mylist1 = [ None for i in range(SIZE) ]
mylist2 = [ None for i in range(SIZE) ]

for i in range(SIZE):
    value1 = input("enter value 1: ")
    value2 = input("enter value 2: ")
    mylist1[ i ], mylist2[ i ] = value1, value2
```

- **Two-Dimensional Array (Matrix / Grid)**

- Used for information that fits naturally into a table
- Two subscripts are necessary to specify an element in a matrix
 - ◆ Row subscript
 - ◆ Column subscript
- General form:

```
matrix = [ [ None ] for i in range(COLUMN) ] for j in
range(ROW)                                     # initialise 2D array
matrix[0][0] = value                           # assign value
```

```

for row in matrix:
    for column in row:
        print(column, end = " ")
    print()

```

output in 2D format

Dictionary

- A type of randomly accessed data structure
- Contains a key and a corresponding value associated with it
- Keys are unique in each dictionary, there isn't any duplicate keys
- Values aren't unique, multiple keys can correspond to the same value
- Initialise dictionary:

```

dictionary = { }
dictionary["abc"] = 101      # assign value to key
( dictionary[k] = v )

```

- Dictionary methods (built-in):
 - Get value of specified key (returns value):
 - ◆ `dictionary.get("abc")` *# returns None if key not in dictionary*
 - ◆ `dictionary["abc"]`
 - Get all dictionary keys (returns array):
 - ◆ `dictionary.keys()`
 - Get all dictionary values (returns array):
 - ◆ `dictionary.values()`
 - Get all dictionary items (returns array):
 - ◆ `dictionary.items()`
 - Remove specified key (and value) from dictionary:
 - ◆ `dictionary.pop("abc")` *# error if specified element isn't in dictionary*
 - Check if key / value is in dictionary (returns boolean):
 - ◆ `dictionary.get("abc")` *# returns None if key not in dictionary*
 - ◆ `if k in dictionary.keys():` ...

◆ *if v in dictionary.values() : ...*

● Sorting elements in a dictionary:

- Dictionaries aren't automatically sorted
- Returning values from dictionary may not be in the original/chronological order
- Built-in sorting functions:
 - ◆ By key:

```
sorted_elements = [ ]  
for key in sorted( dictionary.keys( ) ):  
    sorted_elements.append( key, dictionary[key] )
```

◆ By value:

```
sorted_elements = [ ]  
  
for k, v in dictionary.items( ):  
    sorted_elements.append([k, v])  
  
sorted_elements.sort( key = lambda x: x[1] )
```

○ Manually sorting:

```
sorted_elements = [ ]  
  
while len( dictionary.keys( ) ) is not 0:  
# loops if dictionary isn't empty  
    smallest_key, smallest_val = None, None  
  
    for k, v in dictionary.items( ):  
# traverse dictionary to find smallest key / val  
        if ( smallest_key == None ) or ( k < smallest_key):  
# or v < smallest_val if sorting by value  
            smallest_key, smallest_val = k, v  
  
    sorted_elements.append( [smallest_key, smallest_val] )  
    dictionary.pop( smallest_key )  
# remove smallest key from dictionary
```

Linked Structure

- A type of structure that requires traversal, not randomly accessed
- Types:
 - Singly linked: Linking in one direction
 - Doubly linked: Linking in both directions
- Basic unit of representation: Node
 - Singly linked node contains:
 - ◆ Data value
 - ◆ Pointer to the next node
- Methods to set up singly linked array:
 - Two parallel arrays
 - Pointers
 - ◆ Specified value (e.g. None or 0) represents end of structure
 - ◆ Python: "None" can be used as empty link
- Start pointer points to the first node
- End node with "null" as next value to indicate the end of linked list
- Defining singly linked node class:
 - Flexibility and ease of use are critical
 - Node instance variables are usually referenced without method calls
 - Constructors allow user to set a node's link when node is created

```
class Node(object):  
    def __init__(self, data, next = None):  
        self.data = data  
        self.next = next
```

- Using singly linked node class:
 - Node variables are initialised to "None" or a new "Node" object

```
node1 = None    # empty link  
node2 = Node ( "A", None )    #node containing data and  
empty link (End node)  
node3 = Node ( "B", node2 )    # node containing data and a  
link to node2
```

- Operations on singly linked structures:

- Traversal:

- ◆ Visit each node without deleting it
- ◆ Uses a temporary pointer variable

```
curr = head
while curr != None:      # None serves as sentinel to stop
process
    <use or modify curr.data>
    curr = curr.next
```

- Searching:

- Resembles a traversal
- Two possible sentinels;
 1. Empty link
 2. Data item that equals to target item

```
curr = head
while ( curr != None ) and ( curr.data != targetItem ):
    curr = curr.next
if curr != None:
    <target has been found>
else:
    <target is not in linked structure>
```

- Accessing *i*th item is sequential structure:

```
# Assume  $0 \leq i < n$ 
# i is item to be accessed
# n is number of nodes in structure
```

```
curr = head
while i > 0:
    curr = curr.next
    i = i - 1
return curr.data
```

- Traversal to access specified value:

- If target item not present: no replacement occurs, operation returns False
- If target item is present: new item replaces it, operation returns True

```

curr = head
while ( curr != None ) and ( target != curr.data ):
    curr = curr.next
if curr != None:
    return curr.data
else:
    # not found
    return None

```

- Replacing *i*th item:

```

# Assume 0 <= i < n:
# i is item to be processed
# n is number of nodes in structure

```

```

curr = head
while i > 0:
    curr = curr.next
    i = i - 1
curr.data = newItem

```

- Inserting at beginning:

```

newNode = Node(newItem)
newNode.next = head.next
head.next = newNode

```

- Advantage:
 - Little data movement, no shifting of items needed for insertion or removal, only need to change pointer
- Disadvantage:
 - No random access, must traverse list

Binary Search Tree

notes incoming

- A tree of nodes
- Nodes contain 3 types of values:
 - Data value (can be more than 1 data value)
 - Left pointer
 - Right pointer
- Traverse by comparing target to the current data:

- If target < current data: move left
- If target > current data: move right

- **Node:**

```
class Node:
    def __init__(self, data, left, right):
        self.data = data
        self.left, self.right = left, right
```

- **Implementation using array:**

```
class BST_Array:
    def __init__(self, MAXSIZE):
        self.tree = [None] for i in range(MAXSIZE + 1)
        self.root = 0
        self.nextfree = 1

        for i in range(1, MAXSIZE):
            self.tree[i] = Node("", 0, i+1)          #
chaining using right ptr
            self.tree[MAXSIZE] = Node("", 0, 0)

    def AddItemIterative(new):
        if self.nextfree == 0:                      # tree is
full
            print("tree is full!")
            return ""

        target = self.nextfree
        self.tree[target] = new

        if self.root == 0:                          # tree is
empty
            self.nextfree = self.tree[target].right
            self.tree[target].right = 0

        else:                                       #
traverse tree
            curr = self.root
            prev = None
```



```

lastmove = ""

while curr is not 0:
    prev = curr

    if target < self.tree[curr].data:      # move
left
        last = "L"
        curr = self.tree[curr].left

    else:
        last = "R"
        curr = self.tree[curr].right

    if lastmove = "L":                    # adjust
previous node's ptr
        self.tree[prev].left = target
    else:
        self.tree[prev].right = target

    self.nextfree = self.tree[target].right
    self.tree[target].right = 0

def AddItemRecursive(self, value, curr):
    if self.nextfree == 0:                #
tree is full
        print("tree is full!")
        return ""

    else:
        target = self.nextfree

        if self.root == 0:                #
tree is empty
            self.root = target            #
insert at root

        self.tree[target].data = value
        self.nextfree = self.tree[target].right
        self.tree[target].right = 0

    return ""

```

```

else:
    curr_node = self.tree[curr]          #
assign ptr for easy reference

    if value < curr_node.data:          #
compares value

    if curr_node.left != 0:            #
moves left

        self.AddItemRecursive(value,
curr_node.left)

    else:                                #
location found

        curr_node.left = target        #
insert

        self.tree[target].data = value
        self.nextfree =
self.tree[target].right

        self.tree[target].right = 0

    else:                                #
compares value

    if curr_node.right != 0:          #
moves right

        self.AddItemRecursive(value,
curr_node.right)

    else:                                #
location found

        curr_node.right = target      #
insert

        self.tree[target].data = value
        self.nextfree =
self.tree[target].right

        self.tree[target].right = 0

def GetRoot(self):
    return self.root

def InOrderTraversal(self, root):

```

```

if root != 0:
    self.InOrderTraversal(self.tree[root].left)
    print(self.tree[root].data)
    self.InOrderTraversal(self.tree[root].right)

```

- **Implementation using direct pointers (referencing memory space):**

```

class BST_Dir:
    def __init__(self):
        self.root = None

    def AddItemIterative(self, value):
        # check for max size if required

        if self.root == None:                                     #
            tree is empty                                         #
            self.root = Node(value)                             #
            insert                                                #
            return ""

        else:                                                     #
            tree is not empty                                     #
            curr = self.root
            prev = None
            lastmove = ""

            while curr != None:                                    #
                find location to insert                            #
                prev = curr

                if value < curr.data:                              #
                    move left                                     #
                    lastmove = "L"
                    curr = curr.left

                else:                                              #
                    move right                                    #
                    lastmove = "R"
                    curr = curr.right

```

```

                                if lastmove == "L":                                #
insert                                                                   
                                prev.left = Node(value)
                                else:
                                prev.right = Node(value)

                                def AddItemRecursive_M1(self, value, tree):        #
recursive method 1
                                # check for max size if required

                                if tree == None:                                #
location found, insert
                                return Node(value)

                                elif value < tree.data:                          #
compare values
                                if tree.left == None:                            #
location found, insert
                                tree.left = Node(value)

                                else:                                              #
continue traversal
                                self.AddItemRecursive_M1(self, value,
tree.left)

                                else:                                              #
compare values
                                if tree.right == None:                            #
location found, insert
                                tree.right = Node(value)

                                else:                                              #
continue traversal
                                self.AddItemRecursive_M1(self, value
tree.right)

                                def AddItemRecursive_M2(self, value, tree):
                                # check for max size if required

                                if self.root == None:                            #

```

```

tree is empty
        self.root = Node(value)
        return ""

    else:                                     #
tree is not empty
        if tree == None:                     #
location found
            return Node(value)               #
return value back to original function

        elif value < tree.value:             #
compare values
            node = self.AddItemRecursive_M2(self,
value, tree.left)
                                                    #
traverse to find location
            tree.left = node                  #
insert
            return node                      #
return value back to original function

        else:                               #
compare values
            node = self.AddItemRecursive_M2(self,
value, tree.right)
                                                    #
traverse to find locartion
            tree.right = node                 #
insert
            return node                      #
return value back to original function

        # node value is returned to original function to
        establish pointer chain

    def InOrder(self, tree):
        if tree is not None:
            self.InOrder(tree.left)
            print(tree.data)
            self.InOrder(tree.right)

```

Stacks

- FILO (first-in-last-out) / LIFO (last-in-first-out) structure
 - First item to be pushed into the stack is the last to be removed
 - Last item to be pushed into the stack is the first to be removed
- Access is completely restricted to just one end, called the "top"
- Stack methods:
 - *self.push(item)*: inserts item at top of stack
 - *self.pop()*: removes and returns item at the top of stack, if stack is not empty
 - *self.peek()*: returns item at top of stack, if stack is not empty, does not remove item
 - *self.isEmpty()*: returns True if stack is empty, otherwise False
 - *self.__len__()*: returns the number of elements in the stack currently, same as len(s)
 - *self.__str__()*: returns the string representation of the stack, same as str(s)
- Applications of Stacks:
 - Evaluating arithmetic expressions:
 - ◆ Infix form: operator located between operands (A+B)
 - ◆ Sometimes require parentheses
 - ◆ Involves rules of mathematical operation
 - ◆ E.g. $(33 + 22 * 2 = 33 + 44 = 78)$
 - ◆ Postfix form: operator immediately follows operands (A B +)
 - ◆ Does not require parentheses
 - ◆ Evaluation applies operators as soon as they are encountered
 - ◆ E.g. $(34\ 22\ 2\ * \ + = 34\ 44 \ + = 78)$
 - Evaluating Infix to Postfix:
 1. Start with empty postfix expressions and empty stack (stack holds operators and left parentheses)
 2. Scan across infix expressions from left to right
 3. Encounter operand: append to postfix expression
 4. Encounter '(': push into stack
 5. Encounter operator:
 1. Pop all operators from stack with equal or higher precedence

2. Append to postfix expression
 3. Push scanned operator onto stack
 6. Encounter ')': pop all operators from stack to postfix expression until meeting matching '(', discard '('
 7. Encounter end of infix expression: pop remaining operators from stack to postfix expression
- Evaluating Postfix:
 1. Scan across postfix expression from left to right
 2. Encounter operator: apply it to two preceding operands, replace all three expressions with result
 3. Continue scanning until the end of expression has been reached

Create new stack

While postfix expression is not empty:

Get next token

If token is operand:

Push token into stack

Else:

If token is operator:

Pop the top two operands from stack

Apply operator to the two operands

Push resulting value into stack

EndIf

EndWhile

Return final value

- Memory management:
 - ◆ Keeps track of details during programme runtime
 - ◆ When a function calls another function, it interrupts its own execution and needs to be able to resume its excursion in the same state it was in when it was interrupted
 - ◆ LIFO behaviour
 - ◆ When a function is called:
 1. Push a copy of its activation record onto the runtime stack
 2. Copy its arguments into parameter spaces
 3. Transfer control to starting address of the body of function
 - ◆ Top activation record in the runtime stack is always

the function that's currently being executed

- ◆ When a function terminates:

1. Pop activation record or terminated function from runtime stack
2. Use new top activation record to restore environment of interrupted function and resume execution of the interrupted function

- Implementation:

- ◆ Using array:

```
class ArrayStack:
    CAPACITY = 100

    def __init__(self):
        self.items = list( )
        for i in range( ArrayStack.CAPACITY ):
            self.items.append( None )
        self.top = -1
        self.size = 0

    def push(self, newItem):
        if self.isFull( ):
            print("Stack is full")
            return ""
        else:
            self.size += 1
            self.top += 1
            self.items[self.top] = newItem

    def pop(self):
        if self.isEmpty( ):
            print("Stack is empty")
            return ""
        else:
            oldItem = self.items[self.top]
            self.top -= 1
            self.size -= 1
            return oldItem

    def peek(self):
        if self.isEmpty( ):
```



```

        print("Stack is empty")
        return ""
    else:
        return self.items[self.top]

def __len__(self):
    return self.size

def isEmpty(self):
    return self.size == 0

def isFull(self):
    return self.size == ArrayStack.CAPACITY

def __str__(self):
    res = ""
    for i in range( len(self) ):
        res = res + str( self.items[i] ) + " "
    return res

```

◆ Using linked structure:

```

class Node:
    def __init__(self, data, next):
        self.data = data
        self.next = next

class LinkedStack:
    def __init__(self):
        self.top = None
        self.size = 0

    def push(self, newItem):
        newNode = Node( newItem, self.top )
        self.top = newNode
        self.size += 1

    def pop(self):
        if self.isEmpty():
            print("Stack is empty")
            return ""

```

```

        else:
            oldItem = self.top.data
            self.top = self.top.next
            self.size -= 1
            return oldItem

    def peek(self):
        if self.isEmpty():
            print("Stack is empty")
            return ""
        else:
            return self.top.data

    def __len__(self):
        return self.size

    def isEmpty(self):
        return self.size == 0

    def __str__(self):
        res = ""
        curr = self.top
        while curr != None:
            res += str( self.top.data ) + " "
            curr = curr.next
        return res

```

Queue

- Insertion is restricted to the **rear**
 - "enqueue" to add item to rear of queue
- Removal restricted to the **front**
 - "dequeue" to remove item from front of queue
- FIFO (first-in-first-out) structure
- Queue methods:
 - self.enqueue(item): inserts item at rear of queue
 - self.dequeue(): removes and returns item at front of queue (queue must not be empty)
 - self.peak(): returns item at front of queue
 - self.isEmpty(): returns True if queue is empty, otherwise False

- self.__len__(): returns number of items in queue
- self.__str__(): returns string representation of queue
- Implementation:
 - Linked Structure:

```
class Node:
```

```
    def __init__(self, data, next):
        self.data = data
        self.next = next
```

```
class LinkedQueue( object ):
```

```
    def __init__(self):
        self.front = None
        self.size = 0
        self.rear = None
```

```
    def enqueue(self, newItem):
        newNode = Node( newItem, None )
        if self.isEmpty( ):
            self.front = newNode
        else:
            self.rear.next = newNode
        self.rear = newNode
        self.size += 1
```

```
    def dequeue(self):
        if self.isEmpty( ):
            print("Queue is empty")
            return ""
        else:
            oldItem = self.front.data
            self.front = self.front.next
            if self.front == None:          #queue is empty
                self.rear = None
            self.size -= 1
        return oldItem
```

```
    def peek(self):
        if self.isEmpty( ):
            print("Queue is empty")
            return ""
```

```

        else:
            return self.front.data

    def __len__(self):
        return self.size

    def isEmpty(self):
        return self.size == 0

    def __str__(self):
        res = ""
        curr = self.front
        while curr != None:
            res += str( curr.data ) + " "
            curr = curr.next
        return res

```

○ Linear Array:

```

class ArrayQueue(object):
    CAPACITY = 100

    def __init__(self):
        self.items = list( )
        for i in range ArrayQueue.CAPACITY:
            self.items.append( None )
        self.rear = -1
        self.size = 0

    def enqueue(self, newItem):
        if self.isFull( ):
            print("Queue is full")
            return ""
        else:
            self.rear += 1
            self.size += 1
            self.items[self.rear] = newItem

    def dequeue(self):
        if self.isEmpty( ):
            print("Queue is empty")

```

```

        return ""
    else:
        oldItem = self.items[0]
        for i in range ( self.size-1 ):
            self.items[i] = self.items[i+1]
        self.rear -= 1
        self.size -= 1
        return oldItem

def peek(self):
    if self.isEmpty( ):
        print("Queue is empty")
        return ""
    else:
        return self.items[0]

def __len__(self):
    return self.size

def isEmpty(self):
    return self.size == 0

def isFull(self):
    return self.size == ArrayQueue.CAPACITY

def __str__(self):
    res = ""
    if self.isEmpty( ):
        print("Queue is empty")
        return ""
    else:
        for i in range( self.size );
            res += str( self.items[i] ) + " "
        return res

```

○ Cyclic Array:

```

class ArrayQueue:
    CAPACITY = 100

    def __init__(self):

```

```

self.items = list( )
for i in range ArrayQueue.CAPACITY:
    self.items.append(None)
self.size = 0
self.front = 0
self.rear = -1

```

```

def enqueue(self, newItem):
    if self.isFull( ):
        print("Queue is full")
        return ""
    else:
        if self.rear = ArrayQueue.CAPACITY - 1: #end of

```

array

```

        self.rear = 0
    else:
        self.rear += 1
    self.items[self.rear] = newItem
    self.size += 1

```

```

def dequeue(self):
    if self.isEmpty( ):
        print("Queue is empty")
        return ""
    else:
        oldItem = self.items[self.front]
        if self.front = ArrayQueue.CAPACITY - 1: #end

```

of array

```

        self.front = 0
    else:
        self.front += 1
    self.size -= 1
    return oldItem

```

```

def peek(self):
    if self.isEmpty( ):
        print("Queue is empty")
        return ""
    else:
        return self.items[self.front]

```

```
def __len__(self):  
    return self.size  
  
def isEmpty(self):  
    return self.size == 0  
  
def isFull(self):  
    return self.size == ArrayQueue.CAPACITY  
  
def __str__(self):  
    res = ""  
    curr = self.front  
    for i in range(self.size):  
        res += str(self.items[curr]) + " "  
        if curr == ArrayQueue.CAPACITY-1:  
            curr = 0  
        else:  
            curr += 1  
    return res
```