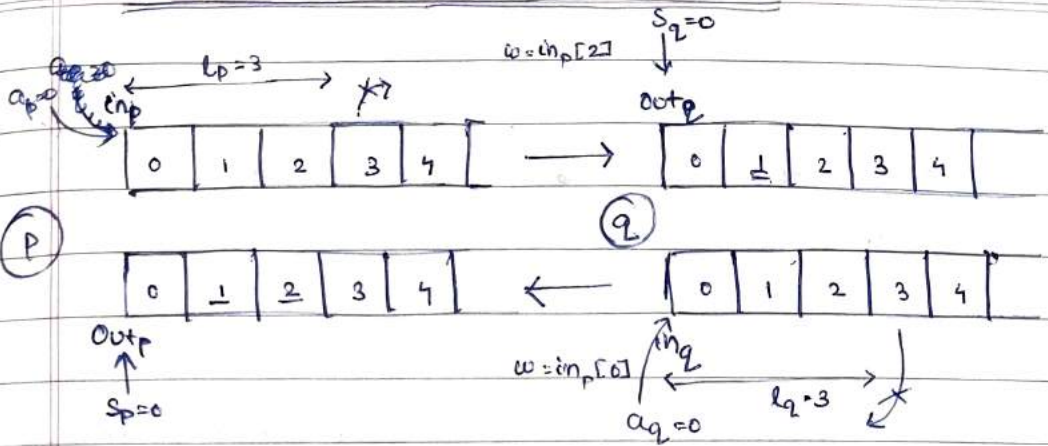


BALANCED SLIDING WINDOW PROTOCOLsafe delivery:

$$out_p[0 \dots s_p - 1] = in_q[0 \dots s_p - 1]$$

$$out_q[0 \dots s_q - 1] = in_p[0 \dots s_q - 1]$$

eventual delivery:

$$s_p \geq K, \quad s_q \geq K, \quad \forall K \geq 0$$

liveness:

$$P \rightarrow s_p - l_q \leq a_p \leq s_q \leq a_q + l_p \leq s_p + l_p$$

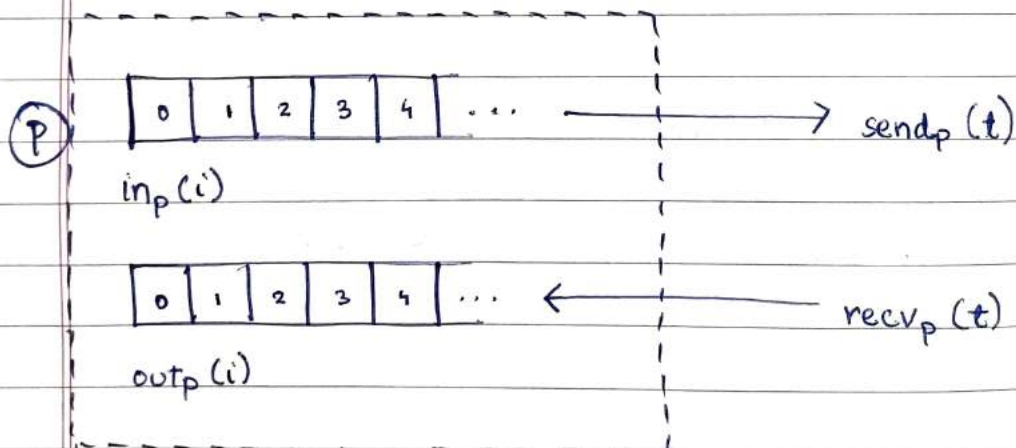
$P \Rightarrow w = in_p[s_q]$ by P $\vee w = in_q[s_p]$ by Q is applic.
(No deadlock is possible).

protocol satisfies requirement of eventual delivery.

SYSTEM1

- a process may send any packet, regardless of what, it has received.
- $$\{ \text{send}_p(i) \} \quad : i \in \mathbb{N}$$
- a channel may choose to send any of the packets it has received at its input?
- $$\therefore C_{out} = \in \{ \text{inp}_p[i] \mid \text{inp}_p[i] \text{ has been sent by } p \}$$

$$\text{or, } \text{out}_c(i) = \{ \text{inp}_c(j) \mid j < i \} \quad \forall i, j \geq 0.$$



non-deterministic:

at $\text{send}_p(t)$ as it can choose which inp to send.

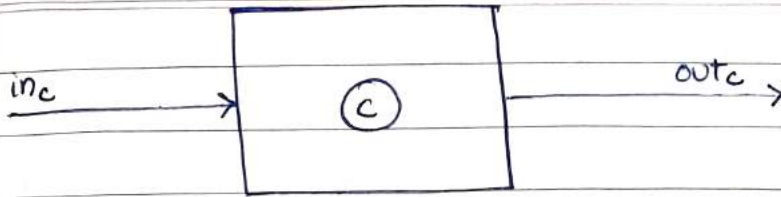
$$\text{i.e., } \text{send}_p(t) = \text{inp}_p(i) \quad : i \in \mathbb{N}$$

↑
choice.

$$\text{but, } \text{recv}_p(t) = \text{out}_p(j) \quad : j \in \mathbb{N}$$

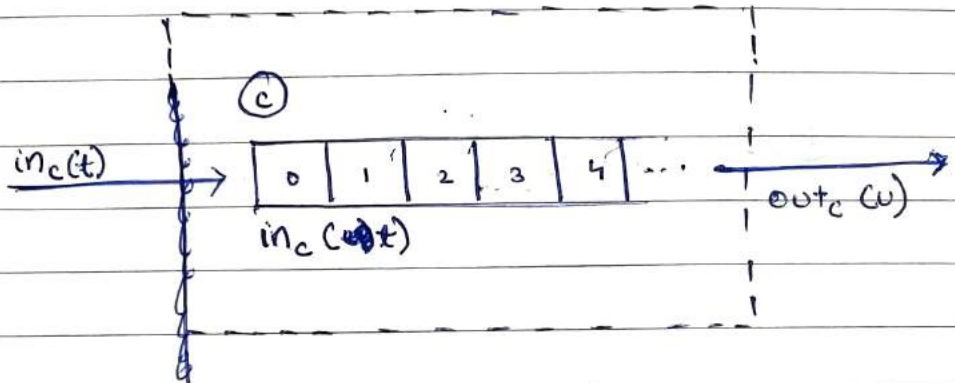
↑
no choice

$$\text{as } \text{out}_p(j) = \text{inp}_q(j) \quad \text{choice}$$



choice (nd.)

$$out_c(t) = in_c(u) \quad \text{st. } u < t \quad t, u \geq 0$$

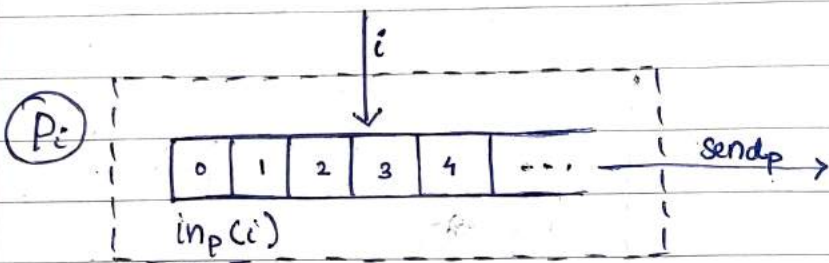


not allowing $out_c(u) = \phi$
as that could lead to no progress.

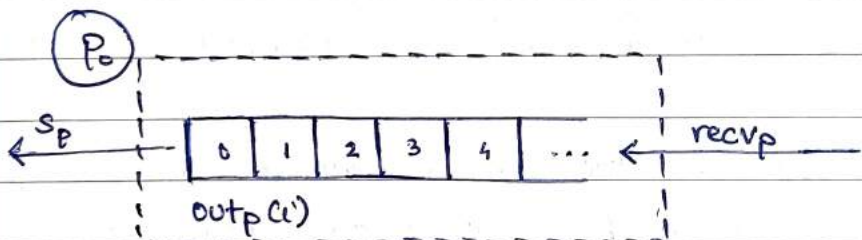
assumption: the channel transmits the message it received, as is, without any modification.

SYSTEM 1 - attempt 2

now i am thinking, it would be (or could be) simpler to subdivide a process (P) into 2 subprocesses (P_i) and (P_o) .



$$\text{send}_p = \langle \text{inp}(i), i \rangle$$



s_p : lowest frame no. not yet received.

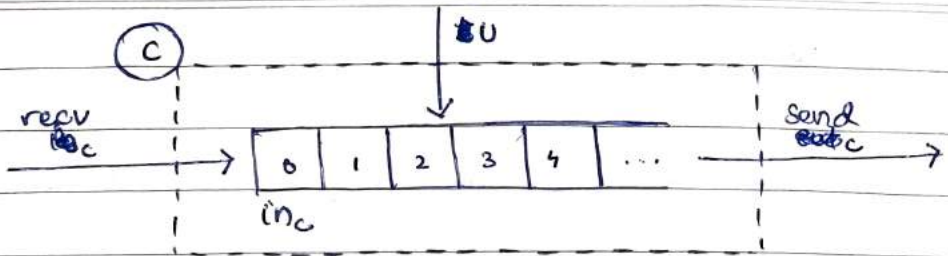
$$\text{out}_p(i) = \text{recv}_p = \langle \text{in}_q(j), i \rangle$$

$$s_p = \min \{ i \mid i \neq \text{undef} \}$$

or

$$s_p(t) = \min \{ i \in \text{recv}_p(t) = \langle -, i \rangle \}$$

$$= j \text{ st. } j \geq i \text{ \& } \text{in } \text{recv}_p(t) = \langle -, i \rangle$$



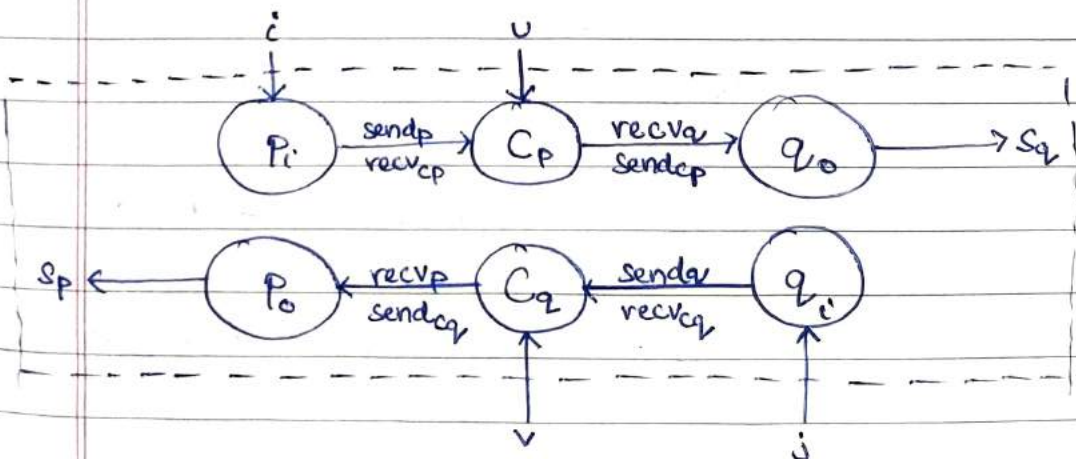
~~$$out_c(t) = recv_c$$~~

$$send_c(t) = recv_c(u) \quad \text{st. } u < t, u, t \geq 0.$$

or

$$in_c(t) = recv_c(t)$$

$$send_c(t) = in_c(u) \quad \text{st. } in_c(u) \neq \text{undef.}$$



4 inputs to interact with,

$$s_0 \langle X_s, X_s^0, U_s, \xrightarrow{s}, Y_s, h_s \rangle$$

$$X_s = \langle in_p, out_p, in_q, out_q, in_{cp}, in_{cq} \rangle$$

$$\text{st. } out_p(i) = in_q(i) \text{ or undef.}$$

$$out_q(i) = in_p(i) \text{ or undef.}$$

$$in_{cp}(t) = in_p(i) \text{ or undef. } i \in \mathbb{N}$$

$$in_{cq}(t) = in_q(i) \text{ or undef. } i \in \mathbb{N}$$

$$X_s^0 = \langle in_p^0, out_p^0, in_q^0, out_q^0, in_{cp}^0, in_{cq}^0 \rangle$$

$$\text{st. } out_p^0(i) = \text{undef. } \forall i \in \mathbb{N}$$

$$out_q^0(i) = \text{undef. } \forall i \in \mathbb{N}$$

$$in_{cp}^0(t) = \text{undef. } \forall t \in \mathbb{N}$$

$$in_{cq}^0(t) = \text{undef. } \forall t \in \mathbb{N}$$

$$U_s = \{ \text{send}_p(i), \text{send}_q(j), \text{send}_p(v), \text{send}_q(v) \}$$

$$\text{st. } \text{inp}(i) \neq \text{undef.}$$

$$\text{in}_q(j) \neq \text{undef.}$$

$$\text{in}_{cp}(v) \neq \text{undef.}$$

$$\text{in}_{cq}(v) \neq \text{undef.}$$

Objective:

$$\text{out}_p(j) = \text{in}_q(j) \quad \forall j \leq K$$

$$\text{out}_q(i) = \text{in}_p(i) \quad \forall i \leq K$$

$$K \in \mathbb{N}$$

inp : frames of process p

K : frames to be transferred.

in_q : frames of process q

out_p : frames received by process p (of q).

out_q : frames received by process q (of p).

{ in_{cp} : frames sent through channel by process p
 in_{cq} : frames sent through channel by process q

(i) $\langle in_p, out_p, in_q, out_q, in_{cp}, \text{out}_{cq} \rangle$

$\downarrow \text{send}_p(i)$

$\langle in_p, out_p, in_q, out_q, in'_{cp}, in_{cq} \rangle$

$$in'_{cp} = \{ t \rightarrow \langle in_p(i), i \rangle \} in_{cp}$$

$$st. in_{cp}(t) = \text{undef.}$$

$$\wedge t \leq x \nexists x \mid in_{cp}(x) = \text{undef.}$$

(ii) $\langle in_p, out_p, in_q, out_q, in_{cp}, \text{out}_{cq} \rangle$

$\downarrow \text{send}_q(j)$

$\langle in_p, out_p, in_q, out_q, in_{cp}, in'_{cq} \rangle$

$$in'_{cq} = \{ t \rightarrow \langle in_q(j), j \rangle \} in_{cq}$$

$$st. in_{cq}(t) = \text{undef.}$$

$$\wedge t \leq x \nexists x \mid in_{cq}(x) = \text{undef.}$$

(iii) $\langle in_p, out_p, in_q, out_q, in_{cp}, out_{cp} \rangle$

↓ $send_{cp}(u)$

$\langle in_p, out_p, in_q, out'_q, in_{cp}, out_{cp} \rangle$

$$out'_q = \{ i \rightarrow F \} out_q$$

$$st. \quad i = i \text{ in } in_{cp}(u) = \langle F, i \rangle$$

$$F = F \text{ in } in_{cp}(u) = \langle F, i \rangle$$

(iv) $\langle in_p, out_p, in_q, out_q, in_{cp}, in_{cq} \rangle$

↓ $send_{cq}(v)$

$\langle in_p, out'_p, in_q, out_q, in_{cp}, out_{cp} \rangle$

$$out'_p = \{ j \rightarrow F \} out_p$$

$$st. \quad j = j \text{ in } in_{cq}(v) = \langle F, j \rangle$$

$$F = F \text{ in } in_{cq}(v) = \langle F, j \rangle$$

Objective:

we want to eliminate the choice of i in $send_p(i)$, and the choice of j in $send_q(j)$. this could make processes p & q deterministic.

$$(2) s_2 \langle X_{s_2}, X_{s_2}^0, U_{s_2}, \xrightarrow{s_2}, \rangle$$

$$X_{s_2} = \langle in_p, out_p, sp, lp, in_q, out_q, in_cp, in_cq \rangle$$

here, sp represents that all frames till $sp-1$ have been received at out_p and that sp is the first frame yet to be sent.

lp represents the frames window for sending, implying that any frames $> sp + lp$ cannot be sent, and process p must ensure first that frames sp is received at out_p , after which it can increment sp , and then will be able to send the frame $sp_{old} + lp$.

(this is a constant)

the above represents additional 2 constraints that apply to the choice of $send_p(c_i)$. c_i is still choosable, but its choice must satisfy above constraints.

$$X_{s_2}^0 = \langle in_p^0, out_p^0, sp^0, lp^0, in_q^0, out_q^0, in_cp^0, in_cq^0 \rangle$$

st. (additional)

$$sp^0 = 0$$

$$sq^0 = 0$$

$$lp^0 = Lp \text{ (say 3)} \quad lq^0 = Lq$$

$$2y^3 + 2x^3y^2 + x^26y$$

$$6 + 6 + 6$$

$$H = \nabla^2 x + \nabla x \nabla y + \nabla^2 y$$

classmate

Date 07.2.2026

Page 211

$$U_{S_2} = U_{S_1}$$

$$= 2xy^3 + 2x$$

$$(i) \langle in_p, out_p, sp, lp, in_q, out_q, sq, lq, in_{cp}, in_{cq} \rangle$$

send_p(i)

$$\langle in_p, out_p, sp, lp, in_q, out_q, sq, lq, in'_{cp}, in_{cq} \rangle$$

$$\text{iff } i \geq sp \wedge i < sp + lp$$

... same as for S₁

$$(ii) \langle in_p, out_p, sp, lp, in_q, out_q, \dots \rangle$$

send_q(j)

$$\langle \dots, in'_{cq} \rangle$$

$$\text{iff } sq \leq i < sq + lq$$

... same as for S₁

$$(iii) \langle \dots \rangle$$

send_{cp}(u)

$$\langle \dots, out'_{cq}, s'_{cq}, \dots \rangle$$

$$s'_{cq} = u \text{ iff } u > sq$$

$$\wedge out'_{cq}(i) \neq \text{undef.} \wedge i < u.$$

... same as for S₁

(iv) $\langle \dots \rangle$ $\downarrow \text{send}_{c_2}(v)$ $\langle \dots, \text{out}'_p, s'_p, \dots \rangle$

$$s'_p = v \quad \text{iff} \quad v > s_p$$

$$\wedge \text{out}'_p(i) \neq \text{undef.} \quad \forall i < v$$

 \dots same as for s_1 .(3) $s_3 \langle X_{s_3}, X_{s_3}^0, U_{s_3}, \xrightarrow{s_3}, \rangle$

$$X_{s_3} = \langle \text{inp}, \text{out}_p, s_p, l_p, t_p, \text{in}_q, \text{out}_q, s_q, l_q, t_q, \text{in}_{cp}, \text{in}_{cq} \rangle$$

 t_p represent the frame that was last sent.

$$X_{s_3}^0: t_{p_0} = -1.$$

$$U_{s_3} = \{ \text{send}_p, \text{send}_q, \text{send}_{cp}(v), \text{send}_{cq}(v) \}$$

channel is still non-deterministic.

(i) $\langle \dots \rangle$ $\downarrow \text{send}_p$ $\langle \dots, t'_p, \dots, \text{in}'_{cp}, \dots \rangle$

$$\text{in}'_{cp} = \text{send}_p(i) \quad \text{where} \quad i = \max(t_p + 1, s_p)$$

$$t'_p = i$$

(ii) similarly for S_{end} .

(iii) (v) same as for S_2 .

RTP:

- ① safety (all frames are received as is, in order).
- ② ~~eventuality~~ (at least k frames can be received by both process with a finite no. of steps).