

TYPE CHECKING

motivation:

approximate the set $VAL^* \cup DIV/O^*$
statically.

i.e., without simplifying the expression.

for such "well-typed" expressions,

no argument type checking is needed

but is denominator = 0? (EFFICIENCY)
check is still needed.

a well-typed expression will not get
stuck with an argument type mismatch
during simplification.

(SAFETY).

TYPE SYSTEM

$$\frac{}{n \text{ NUM}} \text{ NUM}$$

$$\frac{}{b \text{ BOOL}} \text{ BOOL}$$

$$\frac{e_1 \text{ NUM} \quad e_2 \text{ NUM}}{e_1 \text{ (op) } e_2 \text{ NUM}} \text{ OP}$$

$$\frac{e_1 \text{ BOOL} \quad e_2 \tau \quad e_3 \tau}{\text{(if) } e_1 \quad e_2 \quad e_3 \quad \tau} \text{ IF}$$

$$\boxed{e \tau}$$

e is well-typed if

$$\vdash e \tau \quad \text{for some } \tau$$

otherwise, e is ill typed.

ex $e = 2/0 + 5 \text{ NUM}$

① $0 \text{ NUM} \quad (\text{NUM})$

② $2 \text{ NUM} \quad (\text{NUM})$

③ $2 \text{ (1) } 0 \text{ NUM} \quad (\text{OP})$

④ $5 \text{ NUM} \quad (\text{NUM})$

⑤ $2/0 + 5 \text{ NUM} \quad (\text{OP})$

e is well-typed

but gives a DIV/0 at runtime

ex $e = \text{if true } 5 \text{ false } \rightarrow 5$

but $\nVdash_w e \tau$ for any τ

e is ILL-TYPED,

but simplifies to a value, not an ATM?

$\therefore \Vdash_w$ is NOT complete, there exist e , st.
 $\nVdash_w e$, but $e \text{ VAL}$.