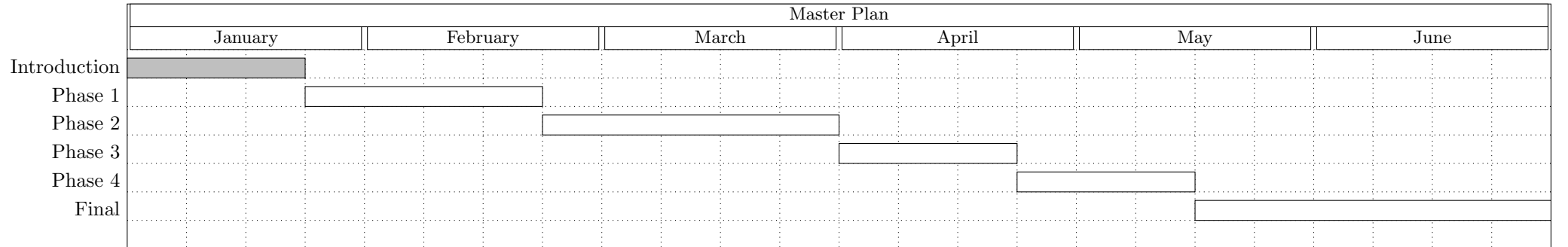


# MASTER PLAN - ISAK HAMMER

## SOLVING CAHN-HILLIARD EQUATION USING CUTCIP

	Phase 1	Phase 2	Phase 3	Phase 4	Report
Estimated time	2-3 Weeks	4-5 Weeks	2 Weeks	3 Weeks	
Problem	CutDG for $-\Delta u = f$	CutCIP for $\Delta^2 u = f$	$\partial_t u + \Delta^2 u = g$	$\partial_t u + \Delta^2 u + f(u) = g$	
Goals	<ul style="list-style-type: none"> <li>• Analysis <ul style="list-style-type: none"> <li><input type="checkbox"/> Coercivity</li> <li><input type="checkbox"/> Boundedness</li> </ul> </li> <li>• Implementation <ul style="list-style-type: none"> <li><input type="checkbox"/> <math>L^2</math> convergence</li> <li><input type="checkbox"/> <math>H^1</math> convergence</li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>• Analysis <ul style="list-style-type: none"> <li><input type="checkbox"/> Coercivity</li> <li><input type="checkbox"/> Boundedness</li> <li><input type="checkbox"/> A priori estimates</li> <li><input type="checkbox"/> Condition number <math>\dagger</math></li> </ul> </li> <li>• Implementation <ul style="list-style-type: none"> <li><input type="checkbox"/> <math>L^2</math> convergence</li> <li><input type="checkbox"/> <math>H^1</math> convergence</li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>• Analysis <ul style="list-style-type: none"> <li><input type="checkbox"/> BDF analysis</li> </ul> </li> <li>• Implementation <ul style="list-style-type: none"> <li><input type="checkbox"/> <math>L^2 L^2</math> convergence</li> <li><input type="checkbox"/> <math>L^2 H^1</math> convergence</li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>• Implementation <ul style="list-style-type: none"> <li><input type="checkbox"/> Fixed point method</li> <li><input type="checkbox"/> <math>L^2 L^2</math> convergence</li> <li><input type="checkbox"/> <math>L^2 H^1</math> convergence</li> </ul> </li> </ul>	<input type="checkbox"/> Introduction <input type="checkbox"/> CutDG $-\Delta u = f$ <ul style="list-style-type: none"> <li><input type="checkbox"/> Formulation</li> <li><input type="checkbox"/> Closed and bounded</li> <li><input type="checkbox"/> Numerical exp.</li> </ul> <input type="checkbox"/> CutCIP for $\Delta^2 u = f$ <ul style="list-style-type: none"> <li><input type="checkbox"/> Formulation</li> <li><input type="checkbox"/> Closed and bounded</li> <li><input type="checkbox"/> A priori Estimates</li> <li><input type="checkbox"/> Numerical exp.</li> </ul> <input type="checkbox"/> CutCIP for $\partial_t u + \Delta^2 u = g$ <ul style="list-style-type: none"> <li><input type="checkbox"/> Time discretization</li> <li><input type="checkbox"/> Numerical Experiments</li> </ul> <input type="checkbox"/> CutCIP for $\partial_t u + \Delta^2 u + f(u) = g$ <ul style="list-style-type: none"> <li><input type="checkbox"/> Fixed point methods</li> <li><input type="checkbox"/> Numerical experiments</li> </ul> <input type="checkbox"/> Conclusion
Comments	Mostly based on (Gürkan and Massing, 2019)	$\dagger$ Not prioritized			
Digression		2nd order mixed formulation	2nd order mixed formulation	2nd order mixed formulation	



## References

Gürkan, Ceren and André Massing (2019). “A stabilized cut discontinuous Galerkin framework for elliptic boundary value and interface problems”. In: *Computer Methods in Applied Mechanics and Engineering* 348, pp. 466–499.