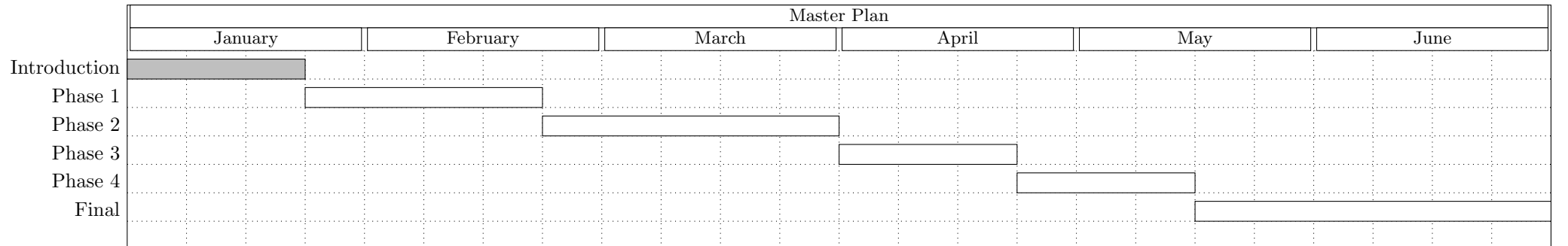


MASTER PLAN - ISAK HAMMER -

SOLVING CAHN-HILLIARD EQUATION USING CUTCIP

Version: January 22, 2023

	Phase 1	Phase 2	Phase 3	Phase 4	Report
Estimated time	2-3 Weeks	4-5 Weeks	2 Weeks	3 Weeks	
Problem	CutDG for $-\Delta u = f$	CutCIP for $\Delta^2 u = f$	$\partial_t u + \Delta^2 u = g$	$\partial_t u + \Delta^2 u + f(u) = g$	
Goals	<ul style="list-style-type: none"> • Analysis <ul style="list-style-type: none"> <input type="checkbox"/> Coercivity <input type="checkbox"/> Boundedness • Implementation <ul style="list-style-type: none"> <input type="checkbox"/> L^2 convergence <input type="checkbox"/> H^1 convergence 	<ul style="list-style-type: none"> • Analysis <ul style="list-style-type: none"> <input type="checkbox"/> Coercivity <input type="checkbox"/> Boundedness <input type="checkbox"/> A priori estimates <input type="checkbox"/> Condition number \dagger • Implementation <ul style="list-style-type: none"> <input type="checkbox"/> L^2 convergence <input type="checkbox"/> H^1 convergence 	<ul style="list-style-type: none"> • Analysis <ul style="list-style-type: none"> <input type="checkbox"/> BDF analysis • Implementation <ul style="list-style-type: none"> <input type="checkbox"/> $L^2 L^2$ convergence <input type="checkbox"/> $L^2 H^1$ convergence 	<ul style="list-style-type: none"> • Implementation <ul style="list-style-type: none"> <input type="checkbox"/> Fixed point method <input type="checkbox"/> $L^2 L^2$ convergence <input type="checkbox"/> $L^2 H^1$ convergence 	<input type="checkbox"/> Introduction <input type="checkbox"/> CutDG $-\Delta u = f$ <ul style="list-style-type: none"> <input type="checkbox"/> Formulation <input type="checkbox"/> Closed and bounded <input type="checkbox"/> Numerical exp. <input type="checkbox"/> CutCIP for $\Delta^2 u = f$ <ul style="list-style-type: none"> <input type="checkbox"/> Formulation <input type="checkbox"/> Closed and bounded <input type="checkbox"/> A priori Estimates <input type="checkbox"/> Numerical experiments <input type="checkbox"/> CutCIP for $\partial_t u + \Delta^2 u = g$ <ul style="list-style-type: none"> <input type="checkbox"/> Time discretization <input type="checkbox"/> Numerical experiments <input type="checkbox"/> CutCIP for $\partial_t u + \Delta^2 u + f(u) = g$ <ul style="list-style-type: none"> <input type="checkbox"/> Fixed point methods <input type="checkbox"/> Numerical experiments <input type="checkbox"/> Conclusion
Comments	Mostly based on (Gürkan and Massing, 2019)	\dagger Not prioritized			
Digression		2nd order mixed formulation	2nd order mixed formulation	2nd order mixed formulation	



References

Gürkan, Ceren and André Massing (2019). “A stabilized cut discontinuous Galerkin framework for elliptic boundary value and interface problems”. In: *Computer Methods in Applied Mechanics and Engineering* 348, pp. 466–499.