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Article

# Constructing artificial features with Grammatical Evolution for the motor symptoms of Parkinson's Disease

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Abstract: This study introduces a set of features designed to capture the motor symptoms of Parkinson's Disease (PD) through detailed motion analysis, with a specific focus on how these symptoms change before and after medication. The features reflect key aspects of patient movement, such as tremor intensity, slowness, rigidity, instability, and irregularity in motion patterns. By quantifying how consistently and smoothly a patient performs specific tasks, the features provide insight into motor control quality and neurological function. Crucially, they are labeled according to the patient's state—before and after receiving medication—allowing for a clear comparison of treatment effects. This enables not only objective tracking of symptom severity, but also evaluation of medication responsiveness. These features address a fundamental clinical need: moving beyond subjective observation toward continuous, data-driven monitoring of disease progression and therapeutic effectiveness in Parkinson's Disease. In the current work the impact of feature construction using Grammatical Evolution on previously mentioned features in evaluated. We compare traditional neural architectures (MLP with ADAM, MLP with Genetic Algorithm, and RBF networks) against models trained on artificially constructed features. The results demonstrate a substantial reduction in classification error when 2 to 5 constructed features are used, achieving the lowest error rate (14.33%) with four generated features (FC4GEN), compared to 38.65% for the best baseline model (RBF). These findings highlight the effectiveness of evolutionary feature construction in enhancing classification accuracy.

**Keywords:** Machine learning; Evolutionary algorithms; Genetic Programming; Grammatical Evolution

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### 1. Introduction

Global health systems face a significant and growing challenge in the form of neurode-generative diseases. These conditions cause severe motor and cognitive impairment and are characterized by a progressive disruption of the structure and function of neurons. As the world's population ages, neurodegenerative diseases like Parkinson's and Alzheimer's disease are becoming more common. These conditions have a significant negative impact on patients' quality of life and are becoming more and more expensive. Innovative methods of early detection, assessment, and treatment are required for these difficult disorders.

A common neurodegenerative disease that primarily affects the motor system is Parkinson's disease (PD). Tremor, bradykinesia (slow movement), rigidity, and postural instability are classic clinical presentations. Non-motor symptoms like mood disorders,

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sleep disorders, and cognitive impairment are frequently present as well. Since there are no particular biological tests that can result in an early diagnosis, PD diagnosis primarily depends on clinical evaluation, despite the fact that the condition's symptom profile is complex. As a result, slow symptom progression leads to misdiagnosis or delay, which leads to ineffective treatment, poor patient outcomes, and a lower quality of life [1].

The early detection and monitoring of Parkinson's disease (PD) could be greatly aided by recent technological advancements, particularly in the fields of machine learning (ML) and the internet of things (IoT). IoT sensors such as smartwatches, wearable health monitors, and others allow continuous and non-intrusive monitoring of motor activities, tremor frequencies, and gait abnormalities in real-time. These tools enable an evaluation of a patient's health while they are engaging in their regular activities and continue to gather large amounts of data outside of the typical clinical settings. One can more accurately identify early indicators of Parkinson's disease and enable early interventions by using machine learning techniques on this data [2,3]. For example, ML algorithms can analyze speech patterns, motor skills, and other non-motor symptoms and differentiate subtle patterns that could foretell the full-blown expression of the disease.

The pursuit of accurate, quantitative, and real-time measurement of Parkinson's disease (PD) motor symptoms has been the prime interest of computational neurology. It is rich in the current state-of-the-art research that utilizes diverse sensor modalities and machine learning (ML) methodologies. Pioneering work has validated the potential of smartphone sensor-derived composite scores, like the mobile Parkinson Disease Score (mPDS), that highly correlate to the conventional standards, such as the MDS-UPDRS, and that are capable of tracking intraday symptom variation as well as response to therapy [4]. In the same line, smartphone-enabled active tests as well as passive monitoring during clinical trial protocols have been shown to be realistic, reliable, and highly sensible, usually uncovering abnormalities even among those patients rated as normal on specific items of the UPDRS during the clinic evaluation [5].

In addition to smartphones, specific PD symptoms have been targeted with specialpurpose sensors. Quantification of bradykinesia, the PD hallmark, has been achieved successfully with gyrosensors during tapping tests, demonstrating strong correlations with clinical ratings [6]. Tremor measurement has been automated with body-worn accelerometers combined with Hidden Markov Models, classifying tremor type and severity reliably [7]. Moreover, inertial sensors have been used to detect and classify complex gait disorders such as Freezing of Gait (FOG) reliably [8]. Even speech has been targeted in the remote monitoring paradigm, where off-the-shelf speech tests analyzed with signal analysis combined with regression models are capable of tracking PD progression with clinically helpful accuracy [9]. Notably, incorporation of the resulting objective measures into standard care has been shown to improve significantly the resulting clinical outcomes, including the UPDRS as well as quality-of-life scores [10]. Latest advances still investigate the integration of sensor data and advanced ML. Research has looked into the integration of speech signals along with ensemble classifiers such as AdaBoost [11] as well as the processing of gait as well as tremor data obtained from off-the-shelf wearable devices. Still missing, though, is an integrative, high-fidelity method for tracking the subtle kinematics of hand movement, a key domain for the measurement of bradykinesia as well as tremor—beyond controlled smartphone tasks.

This work contributes to this vibrant body of research through the proposal of a unifying methodology grounded in a bespoke SmartGlove system that would allow indepth analysis of hand movement. Our contribution is tripartite:

• Innovation and pilot use of the SmartGlove, a sensor- rich tool to capture high-accuracy, multi-parameter kinematic output of the hand.

- Construction of a holistic, multiple-component feature selection framework that goes beyond single technologies by integrating statistical significance (t-tests), ensemble learning (Random Forest), and analysis of variance (PCA) to pick the most discriminating, non-redundant biomarkers.
- The recognition of essential attributes—especially non-linear dynamics and spectral traits—that are notably proficient in differentiating motor states in Parkinson's Disease patients both prior to and following medication, offers an enhanced array of digital biomarkers for prospective diagnostic and monitoring applications.

By emphasizing the rich data space of hand kinematics and adopting a rigorous, multifaceted analytical framework, this research hopes to improve the accuracy and completeness of objective PD evaluation. Briefly stated, the key innovation of this work lies in the combination of a specially crafted data-capture device with an upper-level analytical framework. Contrast this with previous work, which has employed repurposed consumer devices or targeted a very limited set of symptoms, and our specially developed SmartGlove presents a previously unmatched, high-fidelity view of hand motion's rich kinematics. Coupled with our multi-modal feature choice methodology, this system doesn't merely replicate clinical scores but uncovers a novel class of physiologically enlightening biomarkers—specifically in the non-linear dynamic range—that are hidden under conventional analysis. This end-to-end machine learning model is a significant advancement toward precise, data-based neurology from correlation against clinical scales to the detection of underlying digital biomarkers for Parkinson's disease.

In this work, extensive use was made of the Grammatical Evolution [12] technique to create artificial features from existing ones in order to significantly reduce the number of required inputs and to detect hidden correlations in the initial features of the patterns. The applications of the Grammatical Evolution includes cases such as function approximation[13,14], economic problems [15], network security issues [16], water quality problems [17], medical problems [18], evolutionary computing [19], temperature prediction in data centers [20], solving trigonometric problems [21], composing music [22], construction of neural networks [23,24], numerical problems [25], video games [26,27], energy issues [28], combinatorial optimization [29], cryptography [30], production of decision trees [31], problems that appear in electronic circuits [32] etc.

The remainder of this paper follows this organization: Section 2 outlines the materials and methods utilized with a detailed description of the system architecture of the Smart-Glove system, the process of data acquisition related to individual exercises of the hands, and the overall feature extraction process. Section 3 details the multi-faceted feature choice strategy and the composite scoring system used to determine the best biomarkers. Finally, Section 4 discusses implications of the research results, points out limitations of the study, and suggests directions of future research.

### 2. Materials and Methods

This section describes the complete methodology developed for the objective measurement of motor symptoms for Parkinson's Disease (PD). The approach integrates a custom-developed data acquisition system with an advanced computational protocol for conveting raw sensor data into highly discriminative biomarkers. The analysis that follows follows this outline: first, the SmartGlove system and data collection protocol used during special motor experiments are described; second, the multi-domain feature extraction approach is outlined; third, the multi-method scoring regimen developed for feature selection is presented; and, last, the keynote technique of Grammatical Evolution for synthesizing virtual features for improved classification performance, dimension reduction, and generalizability is presented.

### 2.1. SmartGlove System and Sources of Data

The system of interest here as a primary data source is the SmartGlove system, a specially developed wearable system that has been created with the intent of telemonitoring motor symptoms of PD patients. It has been created with the support of the Operational Program of the Epirus Region 2014-2020 and ESPA 2014-2020 with a view of increasing innovative health and biotechnology solutions. The system of SmartGlove has three primary subsystems:

- 1. Textile Glove: Made of durable, biocompatible materials, the glove has conductive areas on the palm and fingers that aid movement recognition. It is sweat-resistant and can be washed. It is also expected to last longer than 10 years.
- 2. System on Chip (SoC): The central processing unit encompasses a low-energy microcontroller that incorporates a Bluetooth 5.0 module, facilitating wireless data communication while utilizing minimal energy resources (with a typical operational range of 10-100 meters, contingent upon the surrounding environment).
- 3. Sensors: The glove contains a multi-modal sensor suite:
- 4. Flex sensors to measure finger bending.
- 5. Contact sensors to detect finger-to-palm interaction.
- 6. A 9-axis Inertial Measurement Unit (IMU), composed of a 3-axis accelerometer, 3-axis gyroscope, and 3-axis magnetometer, to identify hands' orientation and movement. IMU has outputs of up to a sampling rate of 100 Hz and a resolution of 16 bits.

The system is supplemented with a power management circuitry developed for lithium-polymer batteries, as well as with flash memory used for transient storage of data. The SmartGlove complies with the IEC 60601-1 medical electrical apparatus safety standard, thus ensuring reliability for medical applications. The SmartGlove sends data via Bluetooth to the mobPark mobile app supporting Android 6.0+ as well as iOS 11+. The app acts as an intermediary providing the possibility of managing the profile of the users, providing screen-level cues of exercises, as well as capturing sensor data at a sampling rate of 100 Hz. Then the captured data gets securely sent via an encrypted HTTPS connection to a centralized cloud platform like AWS or Azure for storage, processing, and analyzing purposes with a consideration of the General Data Protection Regulation (GDPR).

### 2.2. Data Collection Exercises

The data recording at 100 Hz sampling frequency was selected for efficient tremor frequency (4-6 Hz) and bradykinesia capture. Prior to and after the administration of medicines, measurements were recorded, in order for this therapeutic effect of medicines. to be investigated. Four motor activities, according to standardized clinical examination, were performed:

- Exercise 0 (**Resting Tremor Observation**)): The patient was asked to sit with hands on their thighs, palms facing upwards, counting from 1 to 10. This evaluates postural stability, rest tremor. An example of this exercise is shown in Figure 1.
- Exercise 1 (**Test for Postural Tremor and Coordination**): The patient as shown in Figure 2 held hands at shoulder height with fingers interlocked and attempted touching their index fingers together on counting to ten. This evaluates postural tremor and coordination.
- Exercise 2 (**Finger Tapping Speed Test**): Lifting the palm, the subject made ten fast, repeated taps using the index finger on the thumb as shown in Figure 3. This is a routine measure for assessing motor speed and bradykinesia.
- Exercise 3 (**Hand Opening-Closing Test**): The patient did ten fast, sustained cycles of full fist then reopening the hand from a fully stretched palm position. This exercise

evaluates hand rigidity and bradykinesia and an example of this exercise is shown in Figure 4.



Figure 1. Resting Tremor Observation

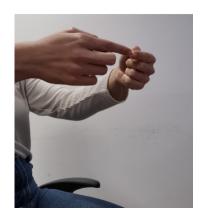


Figure 2. Test for Postural Tremor and Coordination



Figure 3. Finger Tapping Speed Test



Figure 4. Hand Opening-Closing Test

# 2.3. Feature extraction

Numerous features were taken from the raw sensor data (accelerometer, gyroscope, magnetometer) for each exercise in order to quantitatively describe the motor symptoms of Parkinson's disease. These features were computed using 50% overlap (50 samples, 0.5

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seconds) and sliding windows of 100 samples (1 second). These features extracted are as follows:

- Statistical Properties: These characteristics provide a succinct explanation of the signal's variation and distribution. The following properties were calculated: Skewness, Kurtosis, Quartile Deviation, Mean, Standard Deviation, Variance, Minimum, Maximum, Range, Median, and Interquartile Range (IQR).
- Energy Characteristics: These metrics assess the signal's intensity and degree of activity. Signal Magnitude Area (SMA), Root Mean Square (RMS), Total Energy, and Logarithmic Energy are among the features that were extracted.
- Frequency-Domain Features: These are essential for detecting tremors and take into account the signal's spectral characteristics. Included are the following features: Dominant Frequency, Spectral Flatness, Spectral Flux, Spectral Variability, Spectral Entropy, Spectral Centroid, Spectral Spread, and Spectral Roll-on(85%).
- Dynamic and Nonlinear Features: These characteristics specify the signal's temporal fluctuations, complexity, and predictability. The following characteristics are taken into consideration: Mean Absolute Deviation (MAD), Root Mean Square of Successive Differences (RMSSD), Higuchi Fractal Dimension, Lyapunov Exponent, and Sample Entropy.

Since each feature includes specific aspects of motor impairment typical of the disease, such as tremor regularity, movement amplitude, and signal complexity, the selection of features was driven by a large body of literature on PD analysis. The characteristics for Movement Analysis in Parkinson's Disease are outlined in Table 1.

Category	Characteristics	Purpose	Clinical Significance
Central Tendency	Mean, Median	Median Measures the central value	Detection of bradykinesia
,		of the signal	(slowed movements)
Dispersion	Standard deviation,	Quantifies the spread of data	Identifies motion variability
	Variance, IQR, QD	_	(e.g. gravity, tremor)
Range	Minimum/Maximum value,	Records extreme	Assessment of range
	Range	values	of motion reduction
			in patients with Parkinson's disease
Distribution Shape	Skewness, Kurtosis	Describes asymmetry/peakedness	Correlation with irregular
		of distribution	motor patterns
Variability	Coefficient of Variation	Normalized measures	Variability differentiation before
	(CV), MAD, RMSSD	of dispersion	after the treatment
Energy	Total energy,	Measures signal	Correlation with hypokinesia
	Absolute Energy, RMS	intensity	(reduced motor energy)
Logarithmic Energy	Log Energy	Enhances subtle	Detection of small changes
		energy changes	
Spectral	Spectral Entropy, Centroid	Analyzes frequency	Localization of tremor and
		distribution	rhythmic abnormality
Roll-off	85% Roll-off	Frequency band where	Characterization of
		85% of the power is concentrated	tremor bandwidth
Dominant Frequency	Dominant Frequency	Identification of peak	Detection of Parkinson's
		frequency	tremor (4-6Hz)
Spectral Shape	Flatness, Flux,	Quantifies the stability	Unstable tremors vs.
	Variability, Dispersion	of the spectrum	rhythmic movements
Dynamics	Lyapunov Exponent,	Evaluates the chaos/regularity	Degeneration of motor control
	Sampling Entropy	of the system	in Parkinson's
Fractal	Dimension Higuchi	Measures the complexity	Loss of fine
		of the signal	motor control

**Table 1.** Table of Characteristics for Movement Analysis in Parkinson's Disease.

# 2.4. Feature Selection Methodology

Feature selection is a critical step in developing accurate and interpretable machine learning (ML) models for Parkinson's disease (PD) detection. In this study, a multi-method scoring approach was applied to identify the most informative features that differentiate between pre-medication and post-medication states. Instead of relying on a single method, three complementary techniques were employed, and their outputs were combined into a composite score.

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### 2.4.1. Multi-Method Scoring Approach

To accurately evaluate the value of each characteristic for differentiating between preand post-medication states, a multi-angled scoring approach was adopted. For each feature, scores for three different aspects, such as statistical significance, importance based on the model, and variance contribution, were computed.

• Statistical Significance (Paired T-Test): The paired T-Test was then carried out on measurements preceding and succeeding medication on each dimension. To make the significance a number, the  $p_{\text{value}}$  was transformed into a score using the following formula:

$$score_{T_{test}} = -\log_{10}(p_{value} + \epsilon)$$
 (1)

Here,  $e=1\times 10^{-10}$  is a very small constant introduced for avoiding numerical instability arising from a  $p_{\rm value}$  of zero. This mapping makes variables with lower  $p_{\rm value}$  have exponentially large scores, hence indicating more considerable statistical evidence against the null hypothesis ( [41].

• Model-Based Importance (Random Forest): The Random Forest classifier was built such that it could distinguish between the two different states. The importance of a specific feature was computed using the average reduction in Gini impurity across all trees in the ensemble. Gini impurity is a measure of the purity of a node, and the importance is given by the weighted cumulative reduction in node impurity, divided by the probability of the node, and averaged across trees [42]. The evaluation score<sub>RF</sub> for a feature, f is given by:

$$score_{RF} = \frac{1}{N_{trees}} \sum$$
 (2)

where  $N_{\text{trees}}$  is the overall number of trees, T is one tree, and  $\Delta \text{Gini}(n, f)$  decrease in Gini impurity at node n when a split is made along feature f. High-scoring variables have a larger effect on the model predicting (**Breiman**, **2001**).

• Variance Contribution Score (PCA): Principal Component Analysis (PCA) was performed on the standardized data set. The contribution of a individual original feature towards the principal components (PCs) was measured by adding its absolute loadings across all PCs. The loading of a feature onto a PC is its correlation with the specific component [43]. The score score<sub>PCA</sub> was computed as follows:

$$score_{PCA} = \sum_{i} |loading_{i}|$$
 (3)

Here, the loading<sub>i</sub> is the feature weight corresponding to the i-th principal component. This cumulative sum provides the total impact of the feature on the total variance tackled by the Principal Component Analysis (PCA) model (Jolliffe & Cadima, 2016).

### 2.4.2. Composite Score Calculation

To reduce these unrelated measurements into one unified measure of feature prominence, the scores were amalgamated. Each score was first normalized between [0,1] using min-max normalization for comparability across scores. A clear composite score was then calculated as a weighted average of the normalized scores:

Composite Score = 
$$0.4 \times \text{score}_{T_{\text{test}}} + 0.3 \times \text{score}_{RF} + 0.3 \times \text{score}_{PCA}$$
 (4)

This weighting approach was chosen so that features which are highly statistically significant (by the T-test) are given priority, first, while data from model-based learning (Random Forest) and variance-based analysis (PCA) are incorporated cautiously

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### 2.4.3. Selection of best features

Features were ranked according to their composite score, and the top-performing ones were selected for subsequent model development. Representative high-ranking features includes:

- RMSSD from the gyroscope during Exercise 2 (score: 0.663),
- Lyapunov Exponent (score: 0.644),
- Higuchi Fractal Dimension (score: 0.612).

These selected features served as the foundation for later predictive modeling and analysis, aiming to capture the most relevant motor signal characteristics associated with PD symptoms [44,45]. In Table 2 the top 20 features are presented.

Table 2. Top 20 features scored

Exercise	Sensor	Feature	Composite
		Name	Score
2	gyro	rmssd	0.663
2	gyro	lyapunov_exponent	0.644
2	gyro	higuchi_fractal_dimension	0.612
2	gyro	range	0.573
3	acce	higuchi_fractal_dimension	0.469
3	gyro	max	0.452
3	acce	lyapunov_exponent	0.437
2	gyro	spectral_rolloff	0.433
2	acce	sample_entropy	0.422
0	magn	lyapunov_exponent	0.406
0	magn	spectral_variability	0.399
0	magn	higuchi_fractal_dimension	0.399
0	magn	range	0.381
3	magn	rmssd	0.376
0	gyro	rmssd	0.375
2	gyro	std	0.373
3	acce	spectral_flux	0.367
1	gyro	lyapunov_exponent	0.365
1	gyro	rmssd	0.361
1	gyro	max	0.358

### 2.5. Grammatical Evolution preliminaries

Grammatical Evolution procedure can be considered as a genetic algorithm, where the chromosomes are sets of randomly chosen integers. These integers represent production rules of the provided BNF grammar [33]. BNF grammars are usually expressed as sets having the form G = (N, T, S, P), where

- The set *N* contains the non-terminal symbols of the grammar.
- The set *T* includes the terminal symbols of the grammar.
- *S* denotes the start symbol of the grammar, with  $S \in N$ .
- *P* is the set of production rules of the grammar.

The Grammatical Evolution procedure utilizes an extended version of the initial BNF grammar by adding enumeration in the the production rules. As an example of an extended BNF grammar consider the grammar shown in Figure 5. The notation <> is used to enclose the non - terminal symbols of the grammar. The value d denotes the dimension of the input data. The Grammatical Evolution procedure starts from the start symbol of the program and gradually it creates valid programs in the underlying language, using the production rules of the grammar. The general scheme of the production procedure has as follows:

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- **Get** the next element V from the chromosome that is under processing.
- **Select** the next rule using the equation Rule = V mod NR. The symbol NR denotes the number of production rules for the under processing non terminal symbol.

A full working example of the production procedure is the chromosome

$$x = [9, 8, 6, 4, 16, 10, 17, 23, 8, 14]$$

with d = 3. After a series of steps, the function  $f(x) = x_2 + \cos(x_3)$  is produced for the grammar of Figure 5. The production steps are shown in Table 3.

Figure 5. An example of an extended BNF grammar.

```
S::=<expr>
             (0)
<expr> ::=
           (<expr> <op> <expr>)
                                  (0)
           | <func> ( <expr> )
                                   (1)
           <terminal>
                                   (2)
<op> ::=
                    (0)
                    (1)
            *
                    (2)
                    (3)
<func> ::=
             sin
                  (0)
           cos
                  (1)
           exp
                  (2)
           log
                  (3)
<terminal>::=<xlist>
                                     (0)
           <dlist>.<dlist> (1)
<xlist>::=x1
                (0)
           | x2 (1)
           . . . . . . . . .
           | xd (d-1)
<dlist>::=<digit>
                                    (0)
           (1)
           | <digit><digit><digit>
                                        (2)
<digit> ::= 0 (0)
           | 1 (1)
             2 (2)
           3 (3)
           4 (4)
           | 5 (5)
           6 (6)
           | 7 (7)
           8 (8)
           9 (9)
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String	Chromosome	Operation		
<expr></expr>	9,8,6,4,16,10,17,23,8,14	9 mod $3 = 0$		
( <expr><op><expr>)</expr></op></expr>	8,6,4,16,10,17,23,8,14	$8 \mod 3 = 2$		
( <terminal><op><expr>)</expr></op></terminal>	6,4,16,10,17,23,8,14	6 mod $2 = 0$		
( <xlist><op><expr>)</expr></op></xlist>	4,16,10,17,23,8,14	$4 \mod 3 = 1$		
(x2 <op><expr>)</expr></op>	16,10,17,23,8,14	16 mod $4 = 0$		
(x2+ <expr>)</expr>	10,17,23,8,14	$10 \mod 3 = 1$		
(x2+ <func>(<expr>))</expr></func>	17,23,8,14	17 mod $4 = 1$		
(x2+cos( <expr>))</expr>	23,8,14	23 mod $2 = 2$		
(x2+cos( <terminal>))</terminal>	8,14	$8 \mod 2 = 0$		
(x2+cos( <xlist>))</xlist>	14	14 mod $3 = 2$		
$(x2+\cos(x3))$				

**Table 3.** A series of production steps for the example chromosome.

# 2.6. The feature construction method

The technique of feature construction produces artificial features for classification or regression problems as non - linear transformations of the original ones. The new features are evaluated using a machine learning technique, such as artificial neural networks [34,35] or a Radial Basis Function (RBF) networks [47,48]. This method was presented initially in [36]. Also, this method was used in many areas, such as Spam Identification [37], Fetal heart classification [38], signal processing [39,40] etc. The process has the following steps:

### 1. **Initialization** step.

- (a) **Obtain** the train data for the current problem. The train data have M pairs  $(x_i, t_i)$ , i = 1..M. The dimension of each vector  $x_i$  is d. The values  $t_i$  are the expected outputs for each pattern.
- (b) **Define** the parameters of the genetic algorithm:  $N_g$  stands for the the number of allowed generations,  $N_c$  represents the number chromosomes,  $p_s$  defines the selection rate and  $p_m$  the mutation rate.
- (c) **Set** as  $N_f$  the number of features that will construct the Grammatical Evolution procedure.
- (d) **Initialize** the chromosomes in the population. Each chromosome is considered as a set of randomly chosen positive integers.
- (e) Set k = 1, as the generation counter.

### 2. Genetic step

- (a) **For**  $i = 1, ..., N_c$  **do** 
  - i. **Produce** using the Grammatical Evolution procedure a set of  $N_f$  artificial features for the corresponding chromosome  $g_i$ . These features are produced using the grammar of Figure 5.
  - ii. **Transform** the original dataset using the previously constructed features. The new training set is denoted as  $(x_{g_i,j},t_j)$ , j=1,..M
  - iii. **Train** a machine learning model denoted as C using the new training set. The fitness  $f_i$  for the corresponding chromosome is defined as:

$$f_i = \sum_{j=1}^{M} (C(x_{g_i,j}) - t_j)^2$$
 (5)

In the proposed method the RBF network is used as the machine learning model, since the time required for its training is significantly lower than other models, such as neural networks.

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- iv. **Perform** the selection procedure. During this procedure the chromosomes are firstly sorted according to their fitness values and the best  $(1-p_s) \times N_C$  of them are copied intact to the next generation. The rest of the chromosomes will be substituted by new chromosomes produced during the procedures of crossover and mutation.
- v. **Perform** the crossover procedure. During this procedure  $p_s \times N_c$  new chromosomes are produced. For every pair of  $(\tilde{z}, \tilde{w})$  of new chromosomes, two two distinct chromosomes (z, w) are selected from the current population. The selection is performed using the tournament selection. The new chromosomes are produced from the old ones using the one point crossover procedure, which is graphically outlined in Figure 6.
- vi. **Perform** the mutation procedure: for each each element of each chromosome, a random number  $r \in [0,1]$  is selected. The underlying element is altered randomly when  $r \leq p_m$ .

(b) EndFor

- 3. **Set** k = k + 1
- 4. If  $k \le N_G$  goto **Genetic** Step, else terminate the process and obtain the best chromosome  $g^*$  with the lowest fitness value.
- 5. **Transform** the corresponding test set, using the  $N_f$  features obtained for chromosome  $g^*$ .
- 6. **Apply** a machine learning model to the constructed test set and report the associated test error..

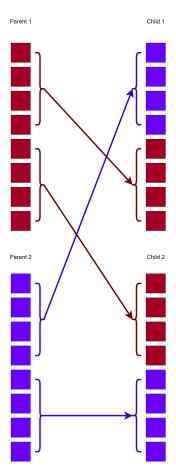


Figure 6. One point crossover method, used in the Grammatical Evolution procedure.

# Initialize data, preprocessing & population Grammar decode & feature build Model training & error Selection, crossover, mutation update

A flowchart of the previous algorithm is shown in Figure 7.

Figure 7. Flowchart of the used genetic algorithm.

3. Results

The code used in the experiments was code in the C++ programming language and for the optimization methods the freely available Optimus programming tool was incorporated [46]. The experiments were conducted on machine with 128GB of ram, running the Debian Linux operating system. Each experiment was executed 30 times and the average classification error was measured and depicted in the related tables and graphs. Also, the 10 - fold cross validation technique was incorporated for the validation of the experimental results. The values for the parameters of the proposed method are depicted in Table 4.

PARAMETER	MEANING	VALUE
$N_g$	Number of maximum allowed generations.	500
$N_c$	Number of chromosomes	500
$p_s$	Selection rate	0.10
$p_m$	Mutation rate	0.05
Н	Number of processing nodes for neural network	10

In the experimental tables the following notation is used:

- 1. The column DATASET represents the performed exercise.
- 2. The column RBF stands for the application of an RBF neural network [47,48] with 10 processing nodes on the corresponding dataset.
- 3. The column GEN represents the application of a genetic algorithm [49] on the training process of a neural network with 10 processing nodes.
- 4. The column PCA stands for the application of the PCA method [50–52] to construct two artificial features from the original ones. Afterwards, a neural network with 10 processing nodes trained using the BFGS method is applied on the new datasets.

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- 5. The column NNC stands for the application of a neural network constructed with Grammatical Evolution [53] on the corresponding dataset.
- 6. The column GENCLASS represents the usage of a method that constructs classification rules using Grammatical Evolution [54].
- 7. The column FC2 is used to represent the application of a genetic algorithm to train a neural network on the dataset produced by the construction of two artificial features using the feature construction method.
- 8. The column FC3 is used to represent the application of a genetic algorithm to train a neural network on the dataset produced by the construction of three artificial features using the feature construction method.
- 9. The column FC4 is used to represent the application of a genetic algorithm to train a neural network on the dataset produced by the construction of four artificial features using the feature construction method.
- 10. The row AVERAGE represents the average classification error for all datasets and the corresponding method.

Table 5 reports classification error per exercise and per feature/model family, where lower values are better. The proposed Feature Construction approach (columns FC2, FC3 and FC4) consistently yields lower errors than classical baselines such as PCA, RBF, NNC, GEN and GENCLASS, indicating that the constructed descriptors capture the discriminative motion patterns more effectively. Based on the overall average, FC3 is the strongest among the proposed variants, achieving the lowest mean error, with FC4 very close behind and FC2 also competitive. In EXERCISE 0 the Feature Construction variants clearly dominate, with FC3 providing the best balance between expressiveness and generalization, FC4 performing nearly as well, and FC2 remaining stable. In EXERCISE 1 the picture is similar: FC2-FC4 retain a lead over classical pipelines and FC3 acts as the "sweet spot," while FC4 is the slightly more aggressive variant and FC2 the conservative yet reliable option. In EXERCISE 2, where separability is more challenging, the FC columns keep the error noticeably lower than the classical models and FC3 generally maintains an edge, although FC4 occasionally approaches or overlaps within small margins. In EXERCISE 3 the same trend holds, with FC2, FC3 and FC4 achieving lower errors and FC3 preserving the overall lead among the proposed methods. Overall, Table 5 underscores that representation quality precedes classifier complexity; when features are properly constructed, even relatively simple decision rules can achieve consistently low error. In practice, orchestrating Feature Construction with linear or RBF-based decision layersor adopting a hybrid design where feature construction is followed by mild dimensionality reduction preserves the information advantage while further controlling noise. The average results for this table are also outlined graphically in Figure 8.

**Table 5.** Experimental results for various exercises.

DATASET	RBF	GEN	PCA	NNC	GENCLASS	FC2	FC3	FC4
EXERCISE 0	40.86%	39.63%	44.70%	32.57%	25.52%	11.39%	11.06%	10.35%
EXERCISE 1	38.65%	47.61%	47.35%	42.07%	29.98%	20.16%	16.08%	14.84%
EXERCISE 2	37.57%	35.33%	40.46%	35.01%	31.34%	22.50%	19.78%	22.10%
EXERCISE 3	41.64%	39.17%	43.46%	35.88%	29.00%	19.79%	17.39%	19.91%

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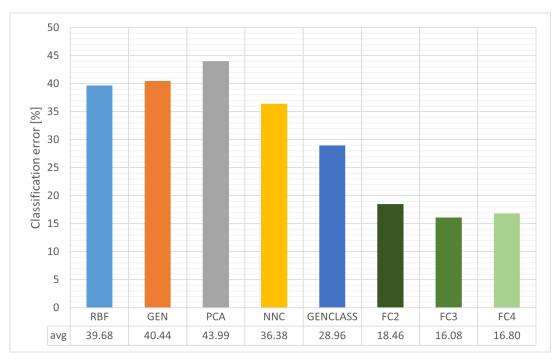


Figure 8. The average classification error for all methods participated in the experiments.

Also the precision values for all exercises and machine learning methods are outlined in Table 6. Similarly, the recall values are depicted in Table 7.

**Table 6.** Precision values for all methods participated in the experiments.

DATASET	RBF	GEN	PCA	NNC	GENCLASS	FC2	FC3	FC4
EXERCISE 0	0.589	0.603	0.559	0.673	0.761	0.885	0.889	0.898
EXERCISE 1	0.62	0.496	0.581	0.595	0.713	0.795	0.837	0.851
EXERCISE 2	0.616	0.726	0.582	0.646	0.69	0.778	0.803	0.78
EXERCISE 3	0.583	0.608	0.566	0.642	0.715	0.803	0.829	0.803

**Table 7.** Recall values for all methods used in the conducted experiments.

DATASET	RBF	GEN	PCA	NNC	GENCLASS	FC2	FC3	FC4
EXERCISE 0	0.588	0.603	0.559	0.689	0.75	0.883	0.885	0.893
EXERCISE 1	0.619	0.766	0.605	0.626	0.711	0.797	0.839	0.854
EXERCISE 2	0.626	0.646	0.589	0.653	0.674	0.771	0.801	0.78
EXERCISE 3	0.583	0.608	0.567	0.652	0.713	0.801	0.827	0.802

4. Conclusions

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