

**Homework 5 – Solutions**

1. [Performance]

**1.6**

- a. Class A:  $10^5$  instr. Class B:  $2 \times 10^5$  instr. Class C:  $5 \times 10^5$  instr.  
Class D:  $2 \times 10^5$  instr.

Time = No. instr.  $\times$  CPI/clock rate

$$\text{Total time P1} = (10^5 + 2 \times 10^5 \times 2 + 5 \times 10^5 \times 3 + 2 \times 10^5 \times 3) / (2.5 \times 10^9) = 10.4 \times 10^{-4} \text{ s}$$

$$\text{Total time P2} = (10^5 \times 2 + 2 \times 10^5 \times 2 + 5 \times 10^5 \times 2 + 2 \times 10^5 \times 2) / (3 \times 10^9) = 6.66 \times 10^{-4} \text{ s}$$

$$\text{CPI(P1)} = 10.4 \times 10^{-4} \times 2.5 \times 10^9 / 10^6 = 2.6$$

$$\text{CPI(P2)} = 6.66 \times 10^{-4} \times 3 \times 10^9 / 10^6 = 2.0$$

- b. clock cycles(P1) =  $10^5 \times 1 + 2 \times 10^5 \times 2 + 5 \times 10^5 \times 3 + 2 \times 10^5 \times 3$   
=  $26 \times 10^5$
- clock cycles(P2) =  $10^5 \times 2 + 2 \times 10^5 \times 2 + 5 \times 10^5 \times 2 + 2 \times 10^5 \times 2$   
=  $20 \times 10^5$

2. [Performance]

**1.7**

- a.  $\text{CPI} = T_{\text{exec}} \times f / \text{No. instr.}$

Compiler A CPI = 1.1

Compiler B CPI = 1.25

- b.  $f_B / f_A = (\text{No. instr.}(B) \times \text{CPI}(B)) / (\text{No. instr.}(A) \times \text{CPI}(A)) = 1.37$

- c.  $T_A / T_{\text{new}} = 1.67$

$$T_B / T_{\text{new}} = 2.27$$

## 3. [Performance]

**1.12**

$$1.12.1 \quad T(P1) = 5 \times 10^9 \times 0.9 / (4 \times 10^9) = 1.125 \text{ s}$$

$$T(P2) = 10^9 \times 0.75 / (3 \times 10^9) = 0.25 \text{ s}$$

clock rate (P1) > clock rate(P2), performance(P1) < performance(P2)

$$1.12.2 \quad T(P1) = \text{No. instr.} \times \text{CPI} / \text{clock rate}$$

$$T(P1) = 2.25 \times 10^{11} / 3 \times 10^9 \text{ s}$$

$$T(P2) = 5 \times 10^8 \times 0.75 / (3 \times 10^9), \text{ then } N = 9 \times 10^8$$

## 4. [Pipelining and Data Hazards]

**4.8****4.8.1**

Pipelined	Single-cycle
350 ps	1250 ps

**4.8.2**

Pipelined	Single-cycle
1750 ps	1250 ps

**4.8.3**

Stage to split	New clock cycle time
ID	300 ps

**4.8.4**

a.	35%
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**4.8.5**

a.	65%
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**4.8.6** We already computed clock cycle times for pipelined and single cycle organizations, and the multi-cycle organization has the same clock cycle time as the pipelined organization. We will compute execution times relative to the pipelined organization. In single-cycle, every instruction takes one (long) clock cycle. In pipelined, a long-running program with no pipeline stalls completes one instruction in every cycle. Finally, a multi-cycle organization completes a LW in 5 cycles, a SW in 4 cycles (no WB), an ALU instruction in 4 cycles (no MEM), and a BEQ in 4 cycles (no WB). So we have the speedup of pipeline

	Multi-cycle execution time is X times pipelined execution time, where X is:	Single-cycle execution time is X times pipelined execution time, where X is:
a.	$0.20 \times 5 + 0.80 \times 4 = 4.20$	$1250 \text{ ps} / 350 \text{ ps} = 3.57$