

Example of Banker's Algorithm

To illustrate the use of Banker's Algorithm, consider a system with five processes P_0 through P_5 and three resource types A, B and C. Resource type A has ten instances, resource type B has five instances and resource type C has seven instances.

Suppose that, at time T_0 , the following snapshot of the system has been taken: $A=10, B=5$ & $C=7$

Process	Allocation A B C	Max Need A B C	Available A B C	Remaining Need A B C
P_1	0 1 0	7 5 3	<u>3</u> <u>3</u> <u>2</u>	7 4 3
P_2	<u>2</u> <u>0</u> <u>0</u>	3 2 2	<u>5</u> <u>3</u> <u>2</u>	1 2 2
P_3	3 0 2	9 0 2	<u>2</u> <u>1</u> <u>1</u>	6 0 0
P_4	2 1 1	4 2 2	7 4 3	2 1 1
P_5	0 0 2	5 3 3	<u>0</u> <u>0</u> <u>2</u>	5 3 1
	7 2 5		7 4 5	

Calculate available resource i.e. Total resources - No. of resources allocated to all processes.

Available resources A = $10 - 7 = 3$

Available resources B = $5 - 2 = 3$

Available resources C = $7 - 5 = 2$

Calculate Remaining need of resources = ~~Maximum~~ Maximum Need of resources - allocated resources

for eg. for process P_1 , Remaining need of resource A = $7 - 0 = 7$

Remaining need of resource $B = 5 - 1 = 4$

Remaining need of resource $C = 3 - 0 = 3$

- ① Now we will check that whether we can fulfill the remaining need of any process with the help of available number of resources A, B and C.
- ② For process P_1 , we require 7 ~~no~~ instance of resource A but we have only 3 instance available for resource A. Similarly we require 4 instances of resource B but we have only 3. We also require 3 instances of resource C but have 2 instances of resource C available with us. So I can fulfill remaining need of only resource C means process P_1 will not be executed.
- ③ Now check for process P_2 . Here, process P_2 remaining need for resources A, B and C is less than respective available instances of resources A, B and C. Means need of process P_2 is fulfilled. So process P_2 will get executed and resources allocated to process P_2 will be released and added to current available resources.
Now available resources $A = 5$, $B = 3$ & $C = 2$
- ④ Now check for process P_3 , remaining need for resource A can not be fulfilled with current available ^{instances of} resources A, so we have to check for process P_4 .

safe | sequence of processes | safe
 $P_2 \rightarrow P_4 \rightarrow P_5 \rightarrow P_1 \rightarrow P_3$ sequence

⑤ For process P_4 , remaining need for resources A, B and C can be fulfilled by current available instances of resources A, B and C. Now process P_4 can be executed and release the resources allocated to process P_4 . So now available resources $A=7$, $B=4$ & $C=3$

⑥ Now check for process P_5 , remaining need for resource A, B & C can be fulfilled by current available instances of resource A, B and C. So process P_5 will be executed and release the resources allocated to process P_5 . Now available resources $A=7$, $B=4$ and $C=5$.

⑦ Now we can check for process P_1 or P_3 . Only sequence will change. If we consider process P_1 , then we can fulfill the remaining need of resources A, B & C. So process P_1 will be executed and release allocated resources. Now available resources $A=7+0=7$, $B=4+1=5$ and $C=5+0=5$.

⑧ For process P_3 , we can fulfill remaining need so process P_3 will be executed and it will release allocated resources. Now current available resources $A=7+3=10$, $B=5+0=5$ and $C=5+2=7$

⑨ When all processes executed total no. of resource $A=10$, $B=5$ and $C=7$ are available. As all processes executed there is no deadlock condition.

Banker's Algorithm Example Solutions

Assume that there are 5 processes, P_0 through P_4 and 4 types of resources. At To we have the following system state:

Max Instances of Resource Type A = 3 [2 allocated + 1 Available]

Max Instances of Resource Type B = 17 [12 allocated + 5 Available]

Max Instances of Resource Type C = 16 [14 allocated + 2 available]

Max Instances of Resource Type D = 12 [12 allocated + 0 Available]

	Given Matrices												Need Matrix =			
	Allocation				Max Matrix								Max Matrix - Allocation			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P_0	0	1	1	0	0	2	1	0	1	5	2	0	0	1	0	0
P_1	1	2	3	1	1	6	5	2	1	6	3	0	0	4	2	1
P_2	1	3	6	5	2	3	6	6	1	12	6	2	1	0	0	1
P_3	0	6	3	2	0	6	5	2	1	12	7	6	0	0	2	0
P_4	0	0	1	4	0	6	5	6	2	14	10	7	0	6	4	2
Total	2	12	14	12					3	17	16	12				

1. Create the need Matrix (Max allocation)

$$\text{Need}(i) = \text{Max}(i) - \text{Allocated}(i)$$

$$(i=0) \Rightarrow (0, 2, 1, 0) - (0, 1, 1, 0) = (0, 1, 0, 0)$$

$$(i=1) \Rightarrow (1, 6, 5, 2) - (1, 2, 3, 1) = (0, 4, 2, 1)$$

$$(i=2) \Rightarrow (2, 3, 6, 6) - (1, 3, 6, 5) = (1, 0, 0, 1)$$

$$(i=3) \Rightarrow (0, 6, 5, 2) - (0, 6, 3, 2) = (0, 0, 2, 0)$$

$$(i=4) \Rightarrow (0, 6, 5, 6) - (0, 0, 1, 4) = (0, 6, 4, 2)$$

2) Use the safety algorithm to test if the system is in a safe state or not

(a) We will first define work & finish:

Initially work = available = (1, 5, 2, 0)
Finish = False for all processes

Finish	Matrix
P ₀	False
P ₁	False
P ₂	False
P ₃	False
P ₄	False

work vector
1 5 2 0

(b) Check the needs of each process $[needs(p_i) \leq Max(p_i)]$, if this condition is true: (i) Execute the process, change Finish [i] = True.

(ii) Release the allocated resources by this process
(iii) Change the work variable = Allocated (P_i) + work

$$need_0(0, 1, 0, 0) \leq work(1, 5, 2, 0)$$

P₀ will be executed because

$$need(P_0) < work \Rightarrow P_0 \text{ will be True}$$

Finish Matrix	P ₀ will release the allocated resources (0, 1, 1, 0)
P ₀ - True	work = work (1, 5, 2, 0) + Allocated (0, 1, 1, 0)
P ₁ - False	Vector = (1, 5, 2, 0) + (0, 1, 1, 0)
P ₂ - False	
P ₃ - False	
P ₄ - False	Work Vector 1 6 3 0

Need₁ (0, 4, 2, 1) \leq work (1, 6, 3, 0) condition is false so P₁ will not be executed.

Need₂ (1, 0, 0, 1) \leq work (1, 6, 3, 0) condition is false so P₂ will not be executed.

Need₃ (0, 0, 2, 0) \leq work (1, 6, 3, 0) condition is True so P₃ will be executed

Finish Matrix	
P ₀₋₁	True
P ₁	False
P ₂	False
P ₃₋₂	P₃ True
P ₄	False

P₃ will release the allocated resources (0, 0, 3, 2)

$$\begin{aligned} \text{work vector} &= \text{work} (1, 6, 3, 0) + \text{Allocated } P_3 \\ &= (1, 6, 3, 0) + (0, 0, 3, 2) \\ &= (1, 12, 6, 2) \end{aligned}$$

work vector

1	12	6	2
---	----	---	---

$$\text{Need}_4 (0, 0, 4, 2) \leq \text{work} (1, 12, 6, 2)$$

condition is true so P₄ executed

P₄ will release the allocated resources (0, 0, 1, 4)

$$\begin{aligned} \text{work vector} &= \text{work} (1, 12, 6, 2) + \text{Allocated } P_4 \\ &= (1, 12, 6, 2) + (0, 0, 1, 4) \\ &= 1, 12, 7, 6 \end{aligned}$$

work vector

1	12	7	6
---	----	---	---

Finish Matrix	
P ₀ -1	True
P ₁	False
P ₂	False
P ₃ -2	True
P ₄ -3	True

$$\text{Need}_1(0,4,2,1) \leq \text{work}(1,12,7,6)$$

condition is True so P₁ will be executed.
P₁ will release the allocated resources
(1,2,3,1)

$$\begin{aligned} \therefore \text{Work vector} &= \text{work}(1,12,7,6) + \text{Allocated } P_1 \\ &= (1,12,7,6) + (1,2,3,1) \\ &= (2,14,10,7) \end{aligned}$$

work vector

2	14	10	7
---	----	----	---

Finish Matrix	
P ₀ -1	True
P ₁ -4	True
P ₂	False
P ₃ -2	True
P ₄ -3	True

Date _____
Page _____

Need $2(1, 0, 0, 1) \leq \text{work}(2, 14, 10, 7)$
 condition is true, so P_2 will be executed.
 P_2 will release the allocated resources
 $(1, 3, 6, 5)$

$$\begin{aligned} \therefore \text{work vector} &= \text{work}(2, 14, 10, 7) + \text{allocated } P_2 \\ &= (2, 14, 10, 7) + (1, 3, 6, 5) \\ &= (3, 17, 16, 12) \end{aligned}$$

work vector

3	17	16	12
---	----	----	----

Finish Matrix	
$P_0 - 1$	True
$P_1 - 4$	True
$P_2 - 5$	True
$P_3 - 2$	True
$P_4 - 3$	True

The system is in a safe state and the processes will be executed in the following order

P_0, P_3, P_4, P_1, P_2 called as Safe sequence.