Discrete-Event Simulation of Queueing Systems in Java: The JSimulation and JQueues Libraries

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Release 5

This book is dedicated to Dick Epema, Graham Birtwistle, and Isi Mitrani.

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Chapter 1

Preface

Queueing systems deal with the general notion of waiting for (the completion of) something. They are ubiquitously and often annoyingly present in our everyday lives. If there is anything we do most, it is probably waiting for something to happen (finally winning a non-trivial prize in the State Lottery after paying monthly tickets over the past thirty years), arrive (the breath-taking dress we ordered from that webshop against warnings in the seller's reputation blog), change (the reception of many severely bad hands in the poker game we just happened to ran into), stop (the constant flipping into red of traffic lights while we are just within breaking distance in our urban environment), or resume (the heater that regularly happens to have a mind of its own during winter months).

XXX

Chapter 2 Introduction

Chapter 3

Guided Tour

3.1 Getting Started

3.2 Creating and Running Queueing-System Simulations

A Simple Simulation with a First-Come First-Served Queue

In order to perform a simulation study in jqueues, the following four actions need to be taken:

- The creation of an event list;
- The creation of one or more queues, and their attachment to the event list;
- The selection of the method for listening to the queue(s), and/or the event list;
- The creation of a workload consisting of jobs;
- Running the event list.

Without much further ado, here's an example:

Listing 3.1: A simple simulation with a single FCFS_B queue and ten jobs.

```
final SimEventList el = new DefaultSimEventList ();
final int bufferSize = 2;
final FCFS_B queue = new FCFS_B (el, bufferSize);
queue.registerStdOutSimQueueListener ();
for (int j = 0; j < 10; j++)
{
final double jobServiceTime = (double) 2.2 * j;</pre>
```

```
final double jobArrivalTime = (double) j;
final String jobName = Integer.toString (j);
final SimJob job = new DefaultSimJob (null, jobName, jobServiceTime);
SimEntityEventScheduler.scheduleJobArrival (job, queue, jobArrivalTime);
}
el.run ();
```

In Listing 3.1, we first create a single event list of type DefaultSimEventList and a FCFS_B queue. On the queue, we invoke its default "listener", issuing notification to the standard output. Subsequently, we create ten jobs named "0", "1", "2", ..., scheduled for arrival at the queue at t = 0, t = 1, t = 2, ..., respectively. Finally, we "run" the event list, i.e., let it process the arrivals.

The event list type DefaultSimEventList will suffice for almost all practical cases, but it is essential to note already that a *single* event-list instance is typically used throughout *any* simulation program. Its purpose of the event list is to hold scheduled *events* in non-decreasing order of *schedule time*, and, upon request (in this case through el.run), starts processing the scheduled events in sequence, invoking their associated *actions*. In this case, the use of events remains hidden, because jobs are scheduled through the use of utility method scheduleJobArrival.

The queue of choice is the First-Come First-Served queue with limited buffer size, FCFS_B, described in more detail in Section 6.4.2. The constructor takes two arguments, the event list el and the buffer size. The queueing system consists of a queue with only B places to hold jobs, and a single server that "serves" the jobs in the queue in order of their arrival. If a job arrives at the FCFS_B system while all places in the queue are occupied by other jobs, the arriving job is denied access to the system, and is *dropped*. Once a queue has finished serving the (single) job, the job *departs* from the system.

So how long does it take to serve a job? Well, in jqueues, the default behavior is that a queue requests the job for its required service time, and we set a fixed service time (at any queue) for each job upon creation as the third argument of the constructur. The first argument of the DefaultSimJob is the event list to which it is to be attached. For jobs (well, at least the ones derived from DefaultSimJob), it is often safe to set this to null, although we could have equally well set it to el. However, queues must always be attached to the event list; a null value upon construction will throw an exception.

The (approximate) output of the code fragment of Listing 3.1 is shown in Listing 3.2 below.

Listing 3.2: Example output of Listing 3.1.

```
StdOutSimQueueListener t=0.0, entity=FCFS_B[2]: UPDATE.
StdOutSimQueueListener t=0.0, entity=FCFS_B[2]: STATE CHANGED:

=> ARRIVAL [Arr[0]@FCFS_B[2]]
=> START [Start[0]@FCFS_B[2]]
```

```
> DEPARTURE [Dep[0]@FCFS_B[2]]
=> DEFARTURE [Dep[0]@FCFS.B[2]]
StdOutSimQueueListener t=0.0, queue=FCFS.B[2]: ARRIVAL of job 0.
StdOutSimQueueListener t=0.0, queue=FCFS.B[2]: START of job 0.
StdOutSimQueueListener t=0.0, queue=FCFS.B[2]: DEPARTURE of job 0.
StdOutSimQueueListener t=1.0, entity=FCFS.B[2]: UPDATE.
StdOutSimQueueListener t=1.0, entity=FCFS.B[2]: STATE CHANGED:
        => ARRIVAL [Arr[1]@FCFS_B[2]]
=> START [Start[1]@FCFS_B[2]]
=> STA_FALSE [StartArmed[false]@FCFS_B[2]]
=> STA.FALSE [StartArmed [false]@FCFS.B[2]]
StdOutSimQueueListener t=1.0, queue=FCFS.B[2]: ARRIVAL of job 1.
StdOutSimQueueListener t=1.0, queue=FCFS.B[2]: START of job 1.
StdOutSimQueueListener t=1.0, queue=FCFS.B[2]: START.ARMED -> false.
StdOutSimQueueListener t=2.0, entity=FCFS.B[2]: UPDATE.
StdOutSimQueueListener t=2.0, entity=FCFS.B[2]: STATE CHANGED:
=> ARRIVAL [Arr[2]@FCFS.B[2]]
StdOutSimQueueListener t=2.0, queue=FCFS.B[2]: ARRIVAL of job 2.
StdOutSimQueueListener t=3.0, entity=FCFS.B[2]: UPDATE.
StdOutSimQueueListener t=3.0, entity=FCFS.B[2]: STATE CHANGED:
=> ARRIVAL [Arr[3]@FCFS.B[2]]
StdOutSimQueueListener t=3.0, queue=FCFS.B[2]: ARRIVAL of job 3.
 StdOutSimQueueListener t=3.0, queue=FCFS_B[2]: ARRIVAL of job 3. StdOutSimQueueListener t=3.2, entity=FCFS_B[2]: UPDATE. StdOutSimQueueListener t=3.2, entity=FCFS_B[2]: STATE CHANGED:
 StdOutSimQueueListener t = 3.2, entity=FCFS_B[2]: STATE CHANGED:

=> DEPARTURE [Dep[1]@FCFS_B[2]]

>> START [Start[2]@FCFS_B[2]]

StdOutSimQueueListener t = 3.2, queue=FCFS_B[2]: DEPARTURE of job 1.

StdOutSimQueueListener t = 4.0, entity=FCFS_B[2]: START of job 2.

StdOutSimQueueListener t = 4.0, entity=FCFS_B[2]: STATE CHANGED:

=> ADMINAT [Ass(A)=CCFS_B[2]]
           => ARRIVAL [Arr[4]@FCFS_B[2]]
=> ARRIVAL [AFT [4]@FCFS_B[2]]
StdOutSimQueueListener t=4.0, queue=FCFS_B[2]: ARRIVAL of job 4.
StdOutSimQueueListener t=5.0, entity=FCFS_B[2]: UPDATE.
StdOutSimQueueListener t=5.0, entity=FCFS_B[2]: STATE CHANGED:
=> ARRIVAL [AFT [5]@FCFS_B[2]]
=> DROP [Drop[5]@FCFS_B[2]]
=> CFS_B[2]: ARRIVAL of job 5.
=> DROP [Drop[o] @PCFS.B[2]]
StdOutSimQueueListener t=5.0, queue=FCFS.B[2]: ARRIVAL of job 5.
StdOutSimQueueListener t=5.0, queue=FCFS.B[2]: DROP of job 5.
StdOutSimQueueListener t=6.0, entity=FCFS.B[2]: UPDATE.
StdOutSimQueueListener t=6.0, entity=FCFS.B[2]: STATE CHANGED:
=> ARRIVAL [Arr[6]@FCFS.B[2]]
=> ARRIVAL [AFT [6]@FCFS.B[2]]

=> DROP [Drop[6]@FCFS.B[2]]

StdOutSimQueueListener t=6.0, queue=FCFS.B[2]: ARRIVAL of job 6.

StdOutSimQueueListener t=6.0, queue=FCFS.B[2]: DROP of job 6.

StdOutSimQueueListener t=7.0, entity=FCFS.B[2]: UPDATE.

StdOutSimQueueListener t=7.0, entity=FCFS.B[2]: STATE CHANGED:
StdOutSimQueueListener t=8.0, entity=rc.t==;
=> ARRIVAL [Arr[8]@FCFS_B[2]]
StdOutSimQueueListener t=8.0, queue=FCFS_B[2]: ARRIVAL of job 8.
StdOutSimQueueListener t=9.0, entity=FCFS_B[2]: UPDATE.

StdOutSimQueueListener t=9.0, entity=FCFS_B[2]: STATE CHANGED:
StdOutSimQueueListener t=9.0, entity=FCFS.B[2]: UPDATE.

StdOutSimQueueListener t=9.0, entity=FCFS.B[2]: STATE CHANGED:

>> ARRIVAL [Arr[9]@FCFS.B[2]]

>> DROP [Drop[9]@FCFS.B[2]]

StdOutSimQueueListener t=9.0, queue=FCFS.B[2]: ARRIVAL of job 9.

StdOutSimQueueListener t=9.0, queue=FCFS.B[2]: DROP of job 9.

StdOutSimQueueListener t=14.20000000000001, entity=FCFS.B[2]: UPDATE.

StdOutSimQueueListener t=14.20000000000001, entity=FCFS.B[2]: STATE CHANGED:
StdOutSimQueueListener t = 23.0, entity=FCFS_B[2]: STATE CHANGED:

DEPARTURE [Dep[4]@FCFS_B[2]]

START [Start[8]@FCFS_B[2]]

StdOutSimQueueListener t = 23.0, queue=FCFS_B[2]: DEPARTURE of job 4.

StdOutSimQueueListener t = 23.0, queue=FCFS_B[2]: START of job 8.

StdOutSimQueueListener t = 40.6, entity=FCFS_B[2]: UPDATE.

StdOutSimQueueListener t = 40.6, entity=FCFS_B[2]: STATE CHANGED:
```

```
=> DEPARTURE [Dep[8]@FCFS_B[2]]
=> STA_TRUE [StartArmed[true]@FCFS_B[2]]
StdOutSimQueueListener t=40.6, queue=FCFS_B[2]: DEPARTURE of job 8.
StdOutSimQueueListener t=40.6, queue=FCFS_B[2]: START_ARMED -> true.
```

Apart from the STATE CHANGED, UPDATE and START_ARMED lines in the output, the notifications pretty much speak for themselves. We even get notified when jobs start service (START), and when they are dropped (jobs 5, 6, and 7) by the queue (DROP). The START_ARMED notifications refer to state changes in a special boolean attribute of a queue named its StartArmed property. It is explained in detail in Section 5.3.2 but since you will hardly need it in practical applications, we will not delve into it. Suffice it to say that StartArmed property reveals in some strange way whether the queue would start a hypothetical arriving job if several additional conditions are also met. It is crucial for the implementation of more complex queueing systems.

The remaining two notification types, UPDATE and STATE CHANGED are essential, however, and require special attention. We will however, defer their discussion for now.

Creating and Registering Listeners

In jqueues, monitoring the progress of a running simulation, or perhaps calculating statistiscs on it, starts with chosing the proper *listeners*. During the simulation, queues and jobs, from hereon collectively referred to as *entities*, are obliged to notify registered listeners of (at least) *all* changes to their states. A listener is a Java object implementing the required methods allowing such notifications from the entity.

In the example of Listing 3.1, we used a convenience method registerStdOutSimQueueListener to register a listener at the FCFS_B queue that simply writes the details of such notifications to the standard output, Sytem.out in Java. This is extremely handy for initial testing of a simulation, but in almost all cases, a more sophisticated listener is required; one you have to create yourself. Luckily, jqueues comes with a large collection of listener implementations, each for a specific purpose, that you can modify to suit your needs.

Restricting ourselves for the moment to queue listeners, we can create and register our own listener that reports to System.out in the code in Listing 3.1:

Listing 3.3: Creating and registering a listener.

```
final SimQueueListener listener = new StdOutSimQueueListener ();
queue.registerSimEntityListener (listener);
```

Running the program of ?? again with this modified code fragment will yiel (roughly) the same output, so we have not gained anything so far. However, a

StdOutSimQueueListener allows all (notification) methods to be overridden, so we can, for instance, suppress certain notifications in the output like this:

Listing 3.4: Suppressing specific notifications in a stdOutSimQueueListener. label

```
final SimQueueListener listener = new StdOutSimQueueListener ()
{
    @Override
    public void notifyStateChanged (double time, SimEntity entity, List notifications) {}

    @Override
    public void notifyUpdate (double time, SimEntity entity) {}

    @Override
    public void notifyStartQueueAccessVacation (double time, SimQueue queue) {}

    @Override
    public void notifyStopQueueAccessVacation (double time, SimQueue queue) {}

    @Override
    public void notifyNewStartArmed (double time, SimQueue queue, boolean startArmed) {}

    @Override
    public void notifyOutOfServerAccessCredits (double time, SimQueue queue) {}

    @Override
    public void notifyOutOfServerAccessCredits (double time, SimQueue queue) {}

    @Override
    public void notifyRegainedServerAccessCredits (double time, SimQueue queue) {}

};
queue.registerSimEntityListener (listener);
```

The UPDATE and STATE CHANGED Notifications

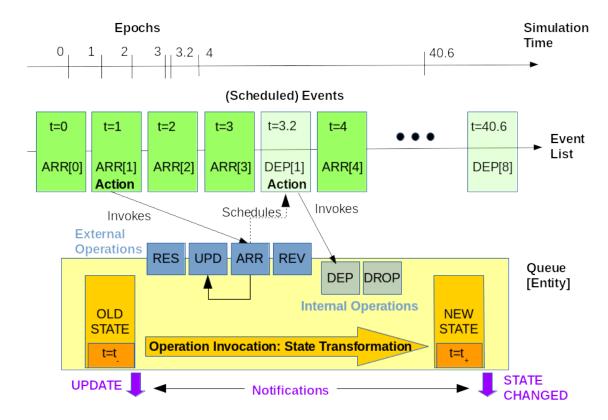
As you may have spotted, events are actually reported twice, once as part of a STATE CHANGED notification, followed by a separate notification specific to the event type (ARRIVAL, DEPARTURE, etc.). As a matter of fact, these separate notifications are merely a courtesy of the queue as it is only required to issue UPDATE, STATE CHANGED and RESET notifications.

In order to understand this, we must realize that in *any* discrete-event simulation, the entities (like queues) involved possess an individual *state* that can only change at discrete moments in time (the *epochs*), and as a result of an *operation* on the entity at that time. This is explained grapically in Figure 3.2.

In the top of the figure, we show the simulation time and some of the epochs from the example. During a simulation run, the simulation time increases monotonically as a function of "real time". What this says is that the simulation time does not "strictly decrease" in real time, but at the same time, that's pretty much the only requirement on the relation between real time and simulation time. For instance, processing the epochs between t = 0 and t = 9 may take several minutes in real time, whereas epochs between t = 9 and t = 100 could be done in a mere second¹

¹This is not to say that is is impossible or even hard to let simulation time progress (roughly) at

Figure 3.1: The relations between simulation time, epochs, the event list, scheduled events, and actions, as well their impact on notifications from and operations on (the state of) an entity.



Below the simulation-time line, we show the event list and some of the scheduled events from the example. The apparent equal distance between the events is actually on pupose. The event list is really not concerned with the simulation-time differences between adjacent events. No matter how large the time interval between an event and its predecessor, in between (basicaly) nothing happened: There were not events, and hence, no state changes. Going back to the figure, we scheduled the arrival events ourselves before processing the event list, but we also see two "departure events" we did not schedule. In fact, these events were scheduled by the queue, in response to previous events. For instance, when job 1 arrives at t = 1 (simulation time), it is taken into service immediately, and after requesting the service time from job 1 (2.2),

the same rate as real time, or at some scaled version of it. However, in discrete-event simulation, the relationship between real time and simulation time is generally considered unimportant.

it schedules a departure event at t=3.2, shown in a somewhat different color because we did not schedule this ourselves (we are not even allowed to do so). This shows an important aspect of the event list while processing it: in general, the actions taken while processing the event list have full freedom to schedule new events, as long as they are not in the past. This, admittedly, is not clear from the figure. What is essential to remember is that a scheduled event await its turn while the event list is being processed, and the event list invokes the event's action when it has processed all preceding events.

Assuming the event's action involves the queue in question, we now turn our attention to the bottom part of the figure, showing our queue from the example, the FCFS_B queue. We assume the arrival event at t=1 is processed by the event list, and the net effect of this (i.e., the action of the event) is the invokation of the arrival operation on the queue (with the job 1 as its argument). As a result of this operation, the state of the queue will transform, and registered listeners to the queue will be informed of the new state upon completion of the operation. This, effectively, is the STATE CHANGED notification. In the figure this is shown with the right-pointing arrow at the bottom from OLD STATE to NEW STATE, and the STATE CHANGED notification below that.

However, before doing anything, the arrival operation invokes the so-called UPDATE operation, which exposes the *old* state to listeners and internally registered "hooks", and, subsequently, increases the most essential state property, the *last update time*. By now, you should realize that as the event list progresses in simulation time, queues (or better, *entities*) that are not affected by the events processed will not be bothered at all. Yet a queue needs to assure that time-stamped operations never lie in the past, so they need to maintain a notion of simulation time themselves. The importance of the UPDATE notification lies in *statistics gathering*, in which it is essential to know exactly during which (non-trivial) intervals the state of a queue did *not* change, and the length of such intervals. As long as you are not involved in statistics-gathering, you can safely ignore these notifications, otherwise, you can find more details in Section 9.

Once the UPDATE operation has been fulfilled, the ARR (job arrival) operation, in this particular case, checks the number of jobs waiting, and drops the arriving job if the number is 2 (=B) by invoking the internal operation DROP. However, for job 1 in the example, it finds an empty waiting area, and, in addition, no job being served at the server. This means that the job is taking into service immediately (the START internal operation), and since the required service time is non-zero, the queue schedules a departure event at t = 3.2. The departur event, in turn, will invoke the internal DEP (job departure) event because of which the job will eventually depart

from the queueing system.

So, what more is there to say. Well, we seem to have so called *external* and *internal* operations, the latter of which we cannot schedule ourselves (departures, drops, ...). In a way, the external operations allow us to subject a queue to some kind of *workload* consisting of arriving jobs (as well as of, yet undescribed, other external operations on the queue). The internal operations, on the other hand, are always involved from within the queue itself, either as a response to a scheduled event, or as a response to an invocation of an external operation in combination with a state condition (e.g., the arrival of a job while 2 jobs are already waiting causes the internal DROP operation to be invoked).

• XXX

- Atomicity of Operations and Notifications and their importance.
- Queue Invariants.
- RESET operation.
- UPDATE operations.
- When does a simulation end?
- Simultaneous events?
- Listeners and Listener Types.
- Remaining Operations (QAV, SAC, REV, AREV).

Chapter 4

Events, Event Lists and Actions

This chapter describes the event and event-list features that are available from the jsimulation package. Note that jsimulation is a dependency of jqueues.

4.1 Creating the Event List and Events

At the very heart of every simulation experiment in jqueues is the so-called event list. The event list obviously holds the events, keeps them ordered, and maintains a notion of "where we are" in a simulation run. Together, an event list and the events it contains define the precise sequence of actions taken in a simulation. The following code snipplet shows how to create an event list and schedule two (empty) events, one at $t_1 = 5.0$ and one at $t_2 = 10$, and print the resulting event list on System.out:

```
final SimEventList el = new DefaultSimEventList ();
final SimEvent e1 = new DefaultSimEvent (5.0);
final SimEvent e2 = new DefaultSimEvent (10.0);
el.add (e1);
el.add (e2);
el.print ();
```

In jsimulation, the event list is of type SimEventList; events are of type SimEvent, respectively. Since both of them are Java *interfaces*, you need implementing classes to instantiate them: DefaultSimEventList for an event list; DefaulSimEvent for an event. Typically, you instantiate a single event list for a simulation experiment, and numerous events.

The double argument in the DefaultSimEvent constructor (of which there are several) is the *schedule time* of the event on the event list. Perhaps surprisingly,

in jsimulation, the schedule time is actually held on the event, *not* on the event list. Also, a SimEventList is inheriting from SortedSet from the Java Collections Framework. These choices have the following consequences:

- Each SimEvent can be present at most once in a SimEventList. You cannot reuse a single event instance (like a job creation and arrival event) by scheduling it multiple times on the event list. Instead, you must either use separate event instances, or reschedule the event the moment it leaves the event list.
- You cannot (more precisely, *should not*) modify the time on the event while it is scheduled on an event list.
- You always have access to the (intended) schedule time of the event, without having to refer to an event list (if the event is scheduled at all) or use a separate variable to keep and maintain that time.
- The events must be equipped with a *total ordering* (imposed by SortedSet) and distinct events should not be equal (imposed by us). This means that for each pair of (distinct) events scheduled on a SimEventList, one of them is always strictly larger than the other (in the ordering, they cannot be "equal").

The output of the code snipplet is something like¹:

```
SimEventList {X}.DefaultSimEventList@{Y}, class=DefaultSimEventList, time=-Infinity: t=5.0, name=No Name, object=null, action=null. t=10.0, name=No Name, object=null, action=null.
```

The output shows the name of the event list (as obtained from its toString method) and the current time $(-\infty)$ in the first row, and then the events in the list in the proper order. By the way, we modified the output; the markers $\{X\}$ and $\{Y\}$ represents strings that most likely deviate on your system.

The output also shows the four properties of an event: its time, name, user object, and action. These will be described in more detail in the next section.

4.2 Event Properties and Event Constructors

A SimEvent has the following properties:

- Time: The (intended) schedule time of the event (default $-\infty$).
- Name: The name of the event, which is only used for logging and output (default "No Name").

¹We may have improved the layout in the meantime.

4.3. ACTIONS 25

• Object: A general-purpose object available for storing information associated with the event (jsimulation nor jqueues uses this field; its default value is null).

• Action: The action to take, a SimEventAction (default null), described in the next section.

Each property has corresponding getter and setter methods:

Properties of SimEvent		
double getTime ()		
void setTime (double)		
String getName ()		
void setName (String)		
T getObject ()		
void setObject (T)		
SimEventAction getEventAction ()		
${\color{red}\mathbf{void}}\ \mathbf{setEventAction}\ (\mathbf{SimEventAction})$		

Note that T refers to the so-called *generic-type argument* of SimEvent (and also of DefaultSimEvent). The prototype is SimEvent<T>, so T can be any object type. The use of generic types is explained in some more details in the "Advanced Topics" section, but for now T can be simply read as a Object.

The next section describes the actions in more detail, but we first provide a list of constructors for DefaultSimEvent:

```
Constructors of DefaultSimEvent

DefaultSimEvent (String, double, T, SimEventAction)

DefaultSimEvent (double, T, SimEventAction)

DefaultSimEvent (double, SimEventAction)

DefaultSimEvent (double)

DefaultSimEvent ()
```

Any non-listed property in a constructor will obtain its default value.

4.3 Actions

A SimEventAction defined what needs to be done by the time an event is *executed* or *processed*. In Java terms, a SimEventAction is an interface with a single abstract method which is invoked when the event is processed. Below we show the declaration of the interface:

```
@FunctionalInterface
public interface SimEventAction<T>
```

There are several ways to create actions for events. The first and most often used way in our own code is to use anonymous inner classes:

```
final SimEventList el = new DefaultSimEventList ();
final SimEvent e =
    new DefaultSimEvent ("My_First_Real_Event", 5.0, null, new SimEventAction ()
    {
        @Override
        public final void action (final SimEvent event)
        {
            System.out.println ("Event=" + event + ", _time=" + event.getTime () + ".");
        }
        @Override
        public String toString ()
        {
            return "My_First_Action";
        }
        });
        el.add (e);
        el.print ();
        el.print ();
```

Note that we are now using the full <code>DefaultSimEvent</code> constructor, passing a name, and supplying a <code>SimEventAction</code> as an anonymous inner class. In the inner class, we define the <code>action</code> method, and in the meantime override the <code>toString</code> method (to be honest, this was merely to keep the generated text within bounds). The generated output is:

```
SimEventList {X}.DefaultSimEventList@{Y}, class=DefaultSimEventList, time=-Infinity: t=5.0, name=My First Real Event, object=null, action=My First Action.

Event=My First Real Event, time=5.0.

SimEventList {X}.DefaultSimEventList@{Y}, class=DefaultSimEventList, time=5.0: EMPTY!
```

Clearly, as expected! However, rote that after "running" the event list, it turns out to be empty, and its time is now t = 5.0, the schedule time of our event. This is as intended, and will be explained in the next section. But first we look at an alternative way of attaching actions to events:

```
final SimEventList el = new DefaultSimEventList ()
{
    @Override
    public final String toString ()
    {
        return "My_Renamed_Event_List";
    }
};
final SimEventAction action = new SimEventAction ()
{
    @Override
    public final void action (final SimEvent event)
{
```

```
System.out.println ("Event=" + event + ",_time=" + event.getTime () + ".");
}
@Override
public final String toString ()
{
   return "A_Shared_Action";
}

for (int i = 1; i <= 10; i++)
{
   final SimEvent e = new DefaultSimEvent ("Our_Event", (double) i, null, action);
   el.add (e);
}
el.print ();
el.print ();
el.print ();</pre>
```

In this example, we created a single action object (again using an anonymous inner class), and reuse it among ten distinct events we schedule (we cannot reuse those). We also took the opportunity give our event list a friendlier name by overriding its toString method. The output is as follows:

```
SimEventList My Renamed Event List, class=, time=-Infinity:
t=1.0, name=Our Event, object=null, action=A Shared Action.
t=2.0, name=Our Event, object=null, action=A Shared Action.
  t=3.0, name=Our Event, object=null, action=A
                                                                 Shared
  t=4.0, name=Our Event, object=null, action=A Shared Action.
  t=5.0, name=Our Event, object=null, action=A Shared Action
  t\!=\!6.0\,, \text{ name=Our Event}\,, \text{ object=} \textbf{null}\,, \text{ action=} A \text{ Shared}
  t=7.0, name=Our Event, object=null, action=A Shared Action.
  \begin{array}{lll} t=8.0, & name=Our & Event, & object=null, & action=A & Shared & Action \\ t=9.0, & name=Our & Event, & object=null, & action=A & Shared & Action. \\ \end{array}
  t = 10.0, name=Our Event, object=null, action=A Shared Action
\label{eq:event}  \text{Event=Our Event, time=2.0.} 
Event=Our Event, time=3.0
Event=Our Event, time=4.0.
Event=Our Event, time=5.0.
Event=Our Event, time=6.0.
Event=Our Event,
                      time = 7.0.
Event=Our Event, time=8.0.
Event=Our Event, time=9.0.
Event=Our Event.
                       time = 10.0
SimEventList My Renamed Event List, class=, time=10.0:
  EMPTY!
```

Again note that the time on the event list after running it is the time of the last event we scheduled on it. In the output, funny enough, the class of the event list is now reported as empty. This is because we used an anonymous class to construct it!

So, there are different ways of attaching a SimEventAction to a DefaultSimEvent. The abundant use of anonymous inner classes as shown here is certainly not to everyone's taste, but it results in relatively compact code (even more through the use of lambda expressions, see XXX).

4.4 Processing the Event List

Once the events of your liking are scheduled on the event list, you can start the simulation by *processing* or *running* the event lists. Processing the event list will cause the

event list to equentially invoke the actions attached to the events in increasing-time order. There are several ways to process a SimEventList:

- You can process the event list until it is empty with the run method.
- You can process the event list until some specified (simulation) time with the runUtil method.
- You can *single-step* through the event list with the runSingleStep method.

You can check whether an event list is being processed through its isRunning method.

While processing, the event list maintains a *clock* holding the (simulation) time of the current event. You can get the time from the event list through **getTime** nethod, although you can obtain it more easily from the event itself. You can insert new events while it is being processed, but these events must not be in the past. Once the event list detects insertion of events in the past, it will throw and exception.

Note that processing the event list is thread-safe in the sense that all methods involved need to obtain a *lock* before being able to process the list. Trying to process an event list that is already being processed from another thread, or from the thread that currently processes the list, will lead to an exception. Note that currently there is no safe, atomic, way to process an event list on the condition that is is not being processed already. Though you can check with <code>isRunning</code> whether the list is being processed or not, the answer from this method has zero validity lifetime.

The example below shows how to schedule new events from event actions; it also shows what happens if you schedule events in the past.

```
else
{
    // Schedule 1 second in the past -> throws exception.
    el.schedule (event.getTime () - 1, this);
    // Never reached.
    System.out.println ("Scheduled_event_in_the_past.");
}
@Override
public final String toString ()
{
    return "Scheduling_Action";
}
};
el.schedule (0, schedulingAction);
el.print ();
el.print ();
el.print ();
```

The code begins to look familiar. First, we create the event list, then a single action. The action is a bit more complicated than before; it has an internal counter in the anynoumous class. Using the counter, it reschedules itself ten times, the first nine times one second in the future, the tenth time at exactly the same time. As mentioned before, this is perfectly legal (and, in fact, often used in our own code). The final attempt to reschedule the action results in an exception, because the event is scheduled in the past. Note that the example also showcases a utility method in SimEventList, viz., schedule (double, SimEventAction), which directly schedules the action on the event list at given time, creating a new SimEvent on the fly. In a later section we will look in more detail at more utility methods on event lists.

The output of the example is shown below².

```
SimEventList The Event List, class=, time=-Infinity:
t=0.0, name=No Name, content=No Name, time=0.0.
                         object=null, action=Scheduling Action.
Event=No Name, time=1.0.
Event=No Name,
                time = 2.0.
Event=No Name.
                time = 3.0.
Event=No Name,
                time = 4.0
Event=No Name,
                time = 5.0.
Event=No Name, time=6.0.
Event=No Name,
                time = 7.0
Event=No Name,
                time = 8.0
Event=No Name, time=9.0.
Scheduled event now.
Event=No Name, time=9.0.
Exception in thread "main"
                              java.lang.Illegal Argument Exception:\\
Schedule time is in the past: 8.0 < 9.0!
```

Note that in this particular case, the exception thrown actually comes with an instructive message as to what caused it (you tried to schedule something on the event list at t=8.0, whereas the current time is beyond that, t=9.0). However, in all honesty, such messages are not present for the majority of exceptions thrown as a result of incorrect arguments from user code. We are currently working on improving this.

²For improved reading, we have left out the full stack-trace of the exception, and rearranged the mixed outputs from System.out and System.err. We will do that without notice in the sequel.

The output also shows the expected result from the first el.print statement: Only a single event is scheduled! The others are created and scheduled while the event list is being processed. It is important to realize that the contents of a SimEventList can always change, as long as these are changes now or in the future. By the way, the second invocation of el.print does not stand a chance; it is unreachable because of the exception thrown in el.run.

4.5 Utility Methods for Scheduling Events

A SimEventList supports various methods for directly scheduling events and actions without the need to generate both the SimEvent and the SimEventAction. In most cases, the availability of one of the object suffices. Below we show the most common utility methods for scheduling on a SimEventList.

Utility methods for scheduling		
void schedule (E)		
Schedules the event at its own time.		
void schedule (double, E)		
Schedules the event at given time.		
reschedule (double, E)		
Reschedules (if present, else schedules) the event at given new time.		
E schedule (double, SimEventAction, String)		
Schedules the action at given time with given event name.		
void scheduleNow (E)		
Schedules the event now.		
E schedule (double, SimEventAction)		
Schedules the action at given time with default event name.		
E scheduleNow (SimEventAction, String)		
Schedules the action now with given event name.		
E scheduleNow (SimEventAction)		
Schedules the action now with default event name.		

Note that E refers to the so-called *generic-type argument* of SimEventList. The prototype is SimEventList<E extends SimEvent>. The use of generic types is explained in some more details in the "Advanced Topics" section, but for now E can be simply read as a SimEvent.

For any of the utilty methods that take a SimEventAction as argument, a new SimEvent is created on the fly, and returned from the method. Upon return from these methods, the newly created event has already been scheduled, and you really

should not schedule it again.

You may wonder how to remove events and actions from the event list. Well, since SimEventList implements the Set interface for SimEvent members, removing an event e from an event list el is as simple as el.remove (e). Currently, there is no support to remove an action from an event list. Because actions can be reused, it would require iterating over all scheduled events, and remove all events with the given action. It is not hard to implement at all, we just did not do it³:

The code fragment silently assumes the absence of null events in the event list, which is indeed guaranteed, and works perfectly for null actions. Note the somewhat unexpected method name on SimEvent to get its action, viz., getEventAction. This name was chosen in order to avoid potential name clashes. At the risk of sounding pedantic, the explicit use of the iterator looks old-fashioned, yet allows for the safe removal of elements from a collection in a loop (contrary to a much fancier for construction).

We conclude with an overview of non-scheduling related utility methods of SimEventList:

Method	Description
void print ()	Prints the event list to System.out.
void print (PrintStream)	Prints the event list to the stream.

4.6 Simultaneous Events

While reading through the previous sections, you may have wondered what would happen if two events are scheduled on exactly the same time. Well, why not just give it a try? First, we create an action class with an index number as argument; when invoked, the action merely prints its index number to System.out:

```
private static class IndexedSimEventAction
implements SimEventAction
{
  final int index;
  public IndexedSimEventAction (final int index)
  {
    this.index = index;
}
```

³This code fragment has not been tested.

```
@Override
public void action (SimEvent event)
{
    System.out.println ("Hello,_I_am_action_number_" + this.index + "!");
}

@Override
public String toString ()
{
    return "Action_" + index;
}
```

So, let us schedule some of these at t=0 in order of increasing index:

```
final SimEventList el = new DefaultSimEventList ();
for (int i = 1; i <= 10; i++)
  el.schedule (0, new IndexedSimEventAction (i), "Event_" + i);
el.print ();
el.run ();</pre>
```

The potential result of this code may be a bit surprising⁴:

```
\begin{array}{lll} \text{SimEventList } \{X\}@\{Y\}, & \textbf{class} = \text{DefaultSimEventList}, & \text{time} = -\text{Infinity}: \\ & t = 0.0, & \text{name} = \text{Event } 3, & \text{object} = \textbf{null}, & \text{action} = \text{Action } 3. \\ & t = 0.0, & \text{name} = \text{Event } 8, & \text{object} = \textbf{null}, & \text{action} = \text{Action } 8. \\ \end{array}
    t=0.0, name=Event 9, object=null, action=Action
t=0.0, name=Event 5, object=null, action=Action
    t=0.0, name=Event 1,
                                              object=null, action=Action
    t\!=\!0.0\,, \text{ name=Event } 4\,, \text{ object=} \textbf{null}\,, \text{ action=} Action
    t=0.0, name=Event 7, object=null, action=Action 7.
t=0.0, name=Event 2, object=null, action=Action 2.
t=0.0, name=Event 6, object=null, action=Action 6.
    t = 0.0, name=Event 10,
                                               object=null, action=Action 10.
Hello, I am action number 3!
Hello, I am action number 8!
Hello, I am action number 9!
Hello, I am action number
Hello, I am action number
Hello,
              I am action
                                     number
Hello,
              I am action number
Hello,
                                     number
              I am action
Hello,
              I am action
                                     number
Hello, I am action number
```

Well, it looks like all our scheduled events were indeed processed, but not in the order we inserted them into the list! It was even clear before processing the event list that there was something "wrong" with the sequence of events. Why? Well, because we explictly instructed the SimEventList not to do process simultaneous events in so-called insertion order, but instead to break ties at random for simultaneously scheduled events. The exact reasoning for doing this is a bit involved, and deferred until the "Advanced Topics" section, but for now it is important to realize that a DefaultSimEventList

• processes its scheduled events in random order should they have equal schedule times;

⁴The probability of you seeing the same result is 1/(10!), which equals the probability of you being *not* surprised at all about your own output.

• will *never* preempt or interrupt the current event it is processing in favor of another event that is scheduled at the same time from within the action of the current event.

Since there is absolutely nothing wrong with maintaining insertion order, you can switch to a different event-list implementation, viz., DefaultEventList_IOEL:

```
final SimEventList el = new DefaultSimEventList_IOEL ();
for (int i = 1; i <= 10; i++)
   el.schedule (0, new IndexedSimEventAction (i), "Event_" + i);
el.print ();
el.run ();</pre>
```

Now the output looks mores structured:

```
SimEventList {X}. DefaultSimEventList_IOEL@{Y}, class=DefaultSimEventList_IOEL,
     \mathtt{time}{=}{-}\,\mathtt{Infinity}:
                              object=null, action=Action
  t = 0.0, name=Event 1,
  t = 0.0, name=Event 2, object=null, action=Action
  t\!=\!0.0\,, \text{ name=Event } 3\,, \text{ object=} \mathbf{null}\,, \text{ action=} Action
  t=0.0, name=Event 4, object=null, action=Action
  t=0.0, name=Event 5, object=null, action=Action
  t=0.0, name=Event 6, object=null, action=Action t=0.0, name=Event 7, object=null, action=Action
  t=0.0, name=Event 8, object=null, action=Action 8.
t=0.0, name=Event 9, object=null, action=Action 9.
t=0.0, name=Event 10, object=null, action=Action 10.
Hello, I am action number 1!
Hello, I am action number 2!
Hello, I am action number 3!
Hello,
        I am action number
                                  4!
Hello, I am action number 5!
Hello, I am action number
Hello,
        I am action number
Hello, I am action number
Hello,
        I am action number
Hello, I am action number
```

Just in case you are curious: we use the abbreviations ROEL for Random-Order Event List and IOEL for Insertion-Order Event List. The DefaultSimEventList is obviously a ROEL; actually it subclasses DefaultSimEventList_ROEL without changes, hence you can also use SimEventList_ROEL as your event-list implementation (perhaps making more explicit the nature of the event list):

```
// Be very careful: this event-list does not respect insertion
// order for simultaneous events!
// ROEL = Random-Order Event List.
final SimEventList el = new DefaultSimEventList_ROEL ();
```

We want to stress that just because our default event-list implementation is a ROEL, it is by no means because ROEL "is just better" than IOEL, or the software in jsimulation and/or jqueues "works better" or even "works only" with a ROEL. Far from it, the current implementations will probably work slightly faster with an IOEL; maintaining insertion order is likely to be faster that drawing random number upon each insertion. So, by all means, use the IOEL implementation if you want to as a replacement to the default ROEL.

4.7 Resetting an Event List

By resetting an event list, through reset, we remove all the events it contains, and set the time to $t = -\infty$, or to a user-specified time through reset (double). Resetting an event list is typically done before repeating a simulation experiment, for instance with a different seed value for random-number generation.

Despite the simplicitly of the concept, we cannot stress enough the importance and consequences of resetting an event list. Although not mandated by jsimulation, the general convention we follow is that an even-list reset puts the event list itself, but also all "entities" (like queues) that use it in a well-known, default, often "empty", state. Partially to that purpose, an event list informs its so-called reset listeners when it is reset. The concept of listeners is described in the next section.

For reasons that will become clear later, in particular when discussing obtaining statistics on queueing systems in **XXX**, it is *highly recommended* to always reset the event list to a *finite* time, even before running it for the first time.

One may wonder why we chose $-\infty$ as the default new time upon a reset, instead of a finite value (zero comes to mind here...). Well, first, we wanted a "fresh" event list to accept all events scheduled at arbitrary time. (Recall that even without running an event list, it will throw an exception if events are scheduled "in the past".) Second, we wanted to avoid the ubiquitous "a simulation starts at t=0" assumption, at least in our own code. For instance, it would be very hard to debug the case in which a statistics-gathering object (e.g., measuring the average number of jobs in a queue) silently assumes that all simulations start at t=0, and the user decides to run a simulation at (for whatever reason) t=+100.

On the other hand, having to remember to pass a finite time upon every reset is, admittedly, far from ideal. The setDefaultResetTime (double) therefore allow for changing the default event-list start time used by reset (). Note though, that this still requires explicit resets of the event list, even before using it for the first time. We are still seeking to improve the reset semantics, in particular related to the new time on the event list and its effect on statistics gathering.

ADD AN EXAMPLE OR TWO HERE!

4.8 Listening to an Event List

You can listen to changes to a SimEventList by registering a *listener* of type SimEventListListener to it. At the present time, there is only support for notifications for an event list reset, and for event-list processing so there is not general "event list changed" notification.

A listener gets notifications for:

- A reset of the event list. This notification is always sent while the list is not begin processed. In fact, if you are only interested in receiving reset notifications, you can use a SimEventListResetListener instead of (the full) SimEventListListener.
- An *update* of the event list. An update is defined as a *strictly positive jump in time during processing*.
- An *empty* event list during processing (this effectively ends processing the event list).
- A *next event* while processing the event list. These notifications, however, are only sent to listeners that implement SimEventListListener.Fine.

The following table summarizes the listener-related methods on a SimEventList.

Method	Description
void addListener (SimEventListResetListener)	Adds a listener.
void removeListener (SimEventListResetListener)	Removes a listener.

The table below list the various notification methods on a listener per listener type; the types are shown in increasing richness.

Method	Description		
${f SimEventListResetListener}$			
void notifyEventListReset (SimEventList)	Reset of given event list.		
SimEventListListener			
void notifyEventListUpdate (SimEventList, double)	Event list update; new time.		
void notifyEventListEmpty (SimEventList, double)	Event list empty at given time.		
SimEventListListener.Fine			
void notifyNextEvent (SimEventList, double)	Process next event; old time.		

4.9 Advanced Topics

In this section we take a closer look at some more advanced topics jsimulation. The sections can be skipped at first reading.

4.9.1	Using	Generic-Type	Arguments
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Interface	Type	Description
SimEvent <t></t>	Т	The type of user object.
SimEventList <e extends="" simevent=""></e>	E	The type of events.
SimEventAction <t></t>	T	The type of user object.

The (partial) implementations in jsimulation follow the same convention as the interface they belong to:

Class
DefaultSimEvent <t></t>
AbstractSimEventList <e extends="" simevent=""></e>
DefaultSimEventList_IOEL <e extends="" simevent=""></e>
DefaultSimEventList_ROEL <e extends="" simevent=""></e>
DefaultSimEventList <e extends="" simevent=""></e>

4.9.2 Event Factories

An *event factory* has a sole purpose: generating new event instances. The use of factories is very common in Java, expecially if one needs to create a "default" instance for a given interface, in our case for SimEvent.

The SimEventFactory interface is as follows:

```
@FunctionalInterface
public interface SimEventFactory<E extends SimEvent>
{
    E newInstance
        (String name, double time, SimEventAction eventAction);
}
```

The generic type argument E is the (base) type of the generated SimEvents. The argument list for newInstance allows for setting all SimEvent properties except the user object (because we believe it is rarely of use).

One particular use for this is to set the event factory on an arbitary SimEventList through its setSimEventFactory method. This is a safe way of using an interface (or event multiple ones) as type argument to SimEventList:

```
interface MySimEvent
extends SimEvent
{
   BigInteger getSeqNumber ();
```

```
static class DefaultMySimEvent
extends DefaultSimEvent
implements MySimEvent
  private static BigInteger
   NEXT_SEQUENCE_NUMBER = BigInteger.ZERO;
 private final BigInteger seqNumber;
  @Override
  public final BigInteger getSeqNumber ()
   return this.seqNumber;
  public DefaultMySimEvent
    (final String name,
     final double time,
     final SimEventAction action)
 {
    super (name, time, null, action);
    this.seqNumber = NEXT_SEQUENCE_NUMBER;
   NEXT_SEQUENCE_NUMBER =
     NEXT_SEQUENCE_NUMBER. add (BigInteger .ONE);
 }
public static void main (final String[] args)
  final SimEventList<MySimEvent> el =
   new DefaultSimEventList (MySimEvent.class);
  el.add (new DefaultMySimEvent
    ("MySimEvent_instance", 5.0, null));
  el.print();
```

In the code fragment, we extended the basic SimEvent interface with a method to maintain a global instance counter of type BigInteger (ignoring the total lack of usefulness), and created a default implementation for it in DefaultMySimEvent. Subsequently, we created an event list, using the generic-type argument and the class argument in the constructor to make sure that the DefaultSimEventList

only accepts MyEventType as events. Note that we use the *interface* here, not the default implementation. The program runs fine and prints the event scheduled on the event list.

However, if we try to schedule an action (null in this case):

```
el.schedule (10.0, (SimEventAction) null);
```

we are treated with an exception:

```
... IllegalStateException: Cannot instantiate MySimEvent!
```

It is more or less immediately clear what the problem is: the event list has to generate a SimEvent in order to schedule the action, but it tries to instantiate MySimEvent, which is an *interface*. (By the way, it also assumes that the event class supports a parameterless constructor!)

We need to tell the event list how to create the events for the various utility methods, and we do that by creating and registering a SimEventFactory for MySimEvent⁵:

```
final SimEventList
new DefaultSimEventList (MySimEvent.class);
el.setSimEventFactory
(
    (final String name,
        final double time,
        final SimEventAction eventAction)
        -> new DefaultMySimEvent (name, time, eventAction)
);
el.add (new DefaultMySimEvent
    ("MySimEvent_instance", 5.0, null));
el.schedule (10.0, (SimEventAction) null);
el.print ();
```

Now we are out of trouble:

```
\begin{array}{c} \dots \\ t = 5.0 \,, \text{ name=MySimEvent instance , object=null , action=null .} \\ t = 10.0 \,, \text{ name=null , object=null , action=null .} \end{array}
```

This section and the previous one on generic-type arguments hopefully showed the maturity of support the generic and runtime type arguments. However, we do not recommend their use unless for very specific use cases that require extending the SimEvent and/or SimEventList interfaces. The problem is that by restricting the allowable compile-time and runtime SimEvent types, the generated objects become

⁵Using a lambda expression this time, see **XXX**.

unusable for libraries using "bare" SimEvents. For instance, the jqueues library will not work with event-lists not supporting "plain" SimEvents.

4.9.3 Simultaneous Events: Random-Order and Insertion-Order Event Lists

In previous sections in this book, we explained that event-list implementations, at least the *non-preemptive* types, come in two natural variants: the ROEL processes simultaneous events in random order, and the IOEL does that in insertion order. We also declared that the default implementation is a ROEL, and that you can easily switch to an IOEL, possibly even gaining some performance. This section is dedicated to motivating the use of, or even the consideration of ROEL as an event list implementation, let alone making it the default! It does not introduce any new software. We already want to stress that ROEL is by no means "better" than IOEL from a user point of view. We do not intend to avocate ROEL over IOEL!

The distinction between ROEL and IOEL is all about *simultaneous* events, and we look at this phenomena from three different viewpoint:

- The *physical* viewpoint: In physics, we are rarely concerned with occurence of simultaneous events, because physical models (to our knowledge) rarely exhibit a strong behavioral dependence on "things happening at the same time".
- The mathematical viewpoint: In mathematical models, we are nearly always dealing with teh possiblity of "things being equal". For instance, it is "undone" two specify an function on two real variables (say, a "maximum indicator") without exactly specifying the result for equal inputs. However, in applications of probability theory, like queueing theory, we often deal with continuous distrubutions and the probability of simulteneous events is often zero. Although simulteneous events still require attention, one can usually get away with noting that "ties are broken at random (with equal probabilities)". Almost always, this solution approach is preferred over trying to impose an additional ordering on the events, as in "Jobs A and B both arrived at t = 0, but job A was first."
- The *software-engineering* viewpoint: In software-engineering, we are not that used to simultaneous events. Sure, there are cases of *concurrency* but the problems that arise are usually fixed by imposing some *order* into which statements, programs, expressions, etc. are to be processed. As a result, software engineering is very much concerned with "doing the right thing given a strict order of

input". A prime example of this are Finite-State Machines supporting state transitions upon external events. Rarely, if ever, does this take into account the possiblity of simultaneous events.

Needless to say, our argument is that the occurrence of simulatenous events is very natural in mathematics, yet the concept of "insertion order" is purely relevant to software-engineering. In other words, there is no equivalence in this context for "insertion order" in mathematics, nor is there is physics.

The reasons for choosing a Random-Order Event List are primarily motivated by its use in jqueues:

- We do not want to *specify* queueing systems with the notion of insertion order, and we probably cannot. Such a specification would be overly complicated, and, as mentioned before, in the mathematical context we rather break ties at random.
- We do not want to *imply* to users the conservation of insertion order in the implementations.
- We do not want to rely on insertion order of events in our tests.

Admittedly, for simple queueing systems like FCFS, it seems simple enough to maintain the order of arrival of jobs in the output process. But as soon as queueing systems become more complicated, especially if multiple queues are involved or feedback, the specification becomes just unnecessarily difficult. To give an example: Suppose we have a feedback FCFS queue with feedback probability 1/4 and two jobs arriving at t=0; jobs A and B having required service times (for each visit) of zero and unity, respectively. Suppose with an insertion-order event list, job A's first arrival is before job B's. So, trusting the conservation of insertion order, the queue starts processing job A, which is fed back to the queue's input immediately with probability 1/4. If so, we are in trouble because we now have to specify whether to first serve job A reappearing at the input or job B. Of course we can find a solution by indeed specifying that a job that is fed back is always inserted after jobs already there, but the real problem is that we have to specify all cases of simultaneus events through insertion-order arguments. And this is just a simple example.

4.9.4 Event Comparators

In order to obtain the required total order on the SimEvents in a SimEventList, the latter uses a Comparator, which by default is an instance of DefaultSimEventComparator, both for ROEL (the default) and IOEL event lists. Its core implementation is

```
@Override
public int compare (E e1, E e2)
{
  int c = Double.compare (e1.getTime (), e2.getTime ());
  if (c == 0)
  {
    c = e1.getSimEventListDeconflictValue ()
        .compareTo
        (e2.getSimEventListDeconflictValue ());
  }
  if ((e1 == e2 && c != 0)
        || (e1 != e2 && c == 0))
        throw new RuntimeException
        ("Error_attempting_to_order_events.");
  return c;
}
```

Not surprisingly, the comparator uses the time property on the events to make a first comparison. In case of a tie, it uses the so-called *deconflict value* on the events, throwing an exception if this still yields a tie. What is interesting to note is that the deconflict value on an event is generated when an event is *added* to an event list by overriding the add and addAll methods from the super class (i.c., TreeSet), e.g., in case of ROEL:

In ROEL, the deconflict value is, as expected drawn from a random-number generator (RNG) rngDeconflict_ROEL. Using this approach has the major advantage that even though events with equal times will be ordered at random, their ordering remains fixed as long as they are in the event list. So, the random ordering in ROEL is *not* implemented by drawing from a RNG the moment it is needed from the event

list (which would, actually, be substantially more difficult), but it is already fixed upon insertion. This, for instance, has the nice feature that consecutive iterators over the (same) event set will always return the events in the same order. By the way, you can set an alternative Comparator by using one of AbstractSimEventList constructors. You cannot change it on the default implementations.

4.9.5 Action is a Functional Interface

Because a SimEventAction is an interface with exactly one abstract method, it can be used in so-called *lambda expressions* in Java 8. So, instead of

```
final SimEventAction action = new SimEventAction ()
{
    @Override
    public final void action (final SimEvent event)
    {
        // Do something with event...
    }
};
```

you can also write:

```
final SimEventAction action =
  (SimEventAction) (final SimEvent event) ->
  {
    // Do something with event...
};
```

or even make it a one-liner.

The SimEventAction interface has been marked a @FunctionalInterface.

4.10 Timers

The abstract AbstractSimTimer class is a small utility class for scheduling a timer on a SimEventList. In view of the classes and methods described before it is not all that useful, but it has been kept in the library for support of legacy code. An AbstractSimTimer features a schedule (double, SimEventList) method that schedules an appropriate event after a delay (the double argument). When the event is processed, the (abstract) method expireAction is invoked, which needs to be defined in a subclass. Also, a pending timer can be (safely) cancelled through its cancel method.

Below is a small, naive example of its use:

```
private static class MyTimer
extends AbstractSimTimer
{
    @Override
    public final void expireAction
        (final double time)
        {
                  System.out.println ("t=" + time + ":_Timer_expired!");
        }
}

public static void main (final String[] args)
{
    final SimEventList el = new DefaultSimEventList ();
    final MyTimer myTimer = new MyTimer ();
        // Progress event list until t=10.
        // Note that AbstractSimTimer does not support t=-\infty.
        el.runUntil (10.0, true, true);
        myTimer.schedule (5, el);
        el.print ();
        el.run ();
}
```

The result of which is:

```
 \begin{array}{lll} SimEventList & \{X\}@\{Y\}\,, & \textbf{class} = DefaultSimEventList\,, & time = 10.0:\\ & t = 15.0\,, & name = \_expire\,, & object = \textbf{null}\,, & action = \{\ldots\}\,.\\ & t = 15.0\colon Timer & expired\,! \end{array}
```

Note that you cannot easily *reschedule* the timer from within the action, because there is no access to the SimEventList, and that you cannot schedule the timer when the time on the event list is infinite (hence the runUntil in the example!).

4.11 Summary and Conclusions

This chapter introduced jsimulation, a small Java library for discrete-event simulation. An overview of the main interfaces and classes is given below:

Interface	Class	Description
SimEvent <t></t>		Event
	DefaultSimEvent <t></t>	Default Event
SimEventList <e></e>		
	AbstractSimEventList <e></e>	Event List (partial)
	DefaultSimEventList_ROEL <e></e>	Random-Order Event List
	DefaultSimEventList_IOEL <e></e>	Insertion-Order Event List
	DefaultSimEventList <e></e>	Default Event List
SimEventAction <t></t>		Action
SimEventListResetListener		Reset Listener
SimEventListListener		Normal Listener
SimEventListResetListener		Detailed Listener
SimEventFactory <e></e>		Event Factory
	DefaultSimEventFactory	Default Event Factory

The remainder of this book is about jqueues, a library for discrete-event simulation of queueing systems. The jqueues library depends on jsimulation for scheduling and processing events and actions.

Chapter 5

Queueing Systems; Entities, Queues, and Jobs

This chapter introduces the concepts behind and implementation of the jqueues package. Together with the underlying jsimulation package, this package allows for discrete-event simulation of a very broad range of queueing systems.

5.1 Introduction and Definitions

Despite the fact that we deal with queueing, waiting, being served (or not), and being denied service on a daily basis, it is, unfortunately, not that easy at all to precisely define a system that captures these "facts of life". In our, admittedly unsatisfactory, definition, a queue or queueing system is an entity that can be visited by other entities called jobs; each visit being initiated by a so-called arrival of a specific job at that queue. A job can only visit only a single queue at a time, yet it can hop to another (or the same) queue once its visit to a particular queue has ended. A queue, on the other hand, can be visited by multiple jobs.

In queueing theory, a branch of mathematics, one attempts to predict the behavior of queues and jobs without being (too) concerned about the particular reasons of a job visit. A very common setting is that jobs visit a queue in order to get a particular service from that queue taking a non-trivial amount of time to complete, the required service time associated with the visit. In other words, visiting jobs have to wait for the completion of their service request. Even worse, the queue is often limited in providing the required services to multiple jobs simultaneously, so jobs have to compete for the service capacity of the server. The outcome of this competition is determined by the so-called service discipline or queue discipline of the queueing

system: the way in which it distributes its limited (finite) service *capacity* among its currently visiting jobs.

Unfortunately, the view of a queueing system as consisting of a waiting area in which jobs wait before being served by one or more servers (i.e., a finite number of them) for a given required service time is too narrow in many interesting applications. For instance, in Medium-Access Control systems, the required "service" to waiting jobs (i.e., frames to be transmitted) is largely determined by external events, viz., the availability of the *medium* for transmissions. In such cases, jobs are not staying in the queue because of an *intrincic* requirement of service from that queue, but merely because they are waiting for an event external to that queue. In other words, the notion of "servers" in a queueing system providing "service" works for many cases, but not for all. And from (theoretical) examples like the Processor-Sharing¹ queueing discipline, it is clear that the notion of servers serving at any time a single job exclusively, needs refinement as well. So, a single server is not constrained, in the general case, to serving only a single job. In Infinite-Server (IS), on the other hand, each job present is served by its own server (of which there are infinitely many), meaning that the "total service capacity" is not a fixed constant, let alone be known in advance. The capacity may not even be finite.

In our conceptual model of a queueing system, we include explicitly the notions of waiting and of being served, but we do not impose *any* structure on the service. In our implementation, queues and jobs are named SimQueues and SimJobs, respectively. Their common features are implemented in an abstract base class SimEntity; for simulation entity.

5.2 Simulation Entities

A SimEntity is an entity relevant to event-list scheduling in a queueing system simulation. Presently, it is either a queue (SimQueue) or a job (SimJob). A queue is an object capable of holding visiting jobs, providing (generic) service to these jobs, and deciding when (or if) they will leave the queue, and end the visit. A SimEntity is the common part of queues and jobs. What they share in common is the event list (SimEventList) they are attached to, the fact that they have a name, and their obligation to propagate state changes (including the currently visited queue of a job, and the jobs currently visiting a queue) to registered listeners. In addition, they must notify such listeners of a reset of the event list. In the table below, we summarize

 $^{^{1}}$ In Processor-Sharing (PS), a server equally distributes its service capacity among jobs present, see **XXX**.

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the SimEntity methods.

Method	Description
SimEventList getEventList ()	Gets the non-null event list.
void registerSimEntityListener	Adds a listener.
(SimEntityListener <j, q=""> listener)</j,>	
void unregisterSimEntityListener	Removes a listener.
(SimEntityListener <j, q=""> listener)</j,>	
Set <simentitylistener<j, q="">></simentitylistener<j,>	Gets a set of current listeners.
getSimEntityListeners ()	
String toStringDefault ()	Returns a default,
	type-specific name of the entity.
setName (String name)	Sets the name of the entity.
void resetEntity ()	Puts the entity in its known initial state.

5.3 Queues

5.3.1 Structure of a SimQueue

A SimQueue consists of two areas, and while a SimJob visits a queue, it is present in either one of them:

- The waiting area: After a successful arrival at the queue, the visiting job always enters the waiting area; in the waiting area, jobs wait before they can be "served", or until they leave the queue otherwise.
- The *service area*: In the service area, jobs receive some sort of (otherwise irrelevant) service from the queue. A job can only enter the service area *from the waiting area*; it cannot directly enter the service area.

Method	Description
Set <j></j>	The current visitor jobs.
getJobs ()	
int	The number of current visitor jobs.
getNumberOfJobs ()	
Set <j></j>	The current visitor jobs in the waiting area.
getJobsInWaitingArea ()	
int	The number of current visitor jobs in the waiting area.
getNumberOfJobsInWaitingArea ()	
Set <j></j>	The current visitor jobs in the service area.
getJobsInServiceArea ()	
int	The number of current visitor jobs in the service area.
getNumberOfJobsInServiceArea ()	

5.3.2 The SimQueue-Visit Lifecycle

Job Arrival

A queue visit starts with the arrival of a job through arrive(double, J). The first argument of arrive is the arrival time; typically an arrival is scheduled as the result of processing a SimEvent on the event list, and the time argument is taken from the event. The second argument is the SimJob that arrives; note the use of the generic type J restricting the type of jobs (at compile time) allowed at the SimQueue.

Method	Description
void	Arrival of a job at the queue.
arrive (double, J)	

Job Drop

At the discretion of the SimQueue, a job can be forced to leave the queue; this is referred to as a job drop. Implementations of the SimQueue interface must specify under which conditions they decide to drop jobs. Typical examples are the unavailability of buffer space, or exceeding a maximum allowed service time. Note that job drops cannot be requested by the user of the queue. A job can be dropped from the waiting area as well as from the service area. (For completeness, we note that a job can also be dropped immediately upon arrival due to queue-access vacations; see next section.)

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Queue-Access Vacation

During a queue-access vacation, access to the SimQueue is prohibited and all jobs are dropped immediately upon arrival. A queue-access vacation affects the queue's behavior only upon arrivals; it has no effects whatsoever on jobs that are already present at the queue. Note that formally, a job arrival at a queue with queue-access vacation is *not* a visit, because the job is never actually present at the queue.

Method	Description
void	Starts or stops a QAV at given time.
setQueueAccessVacation (double, boolean)	
boolean	Checks for an ongoing QAV.
isQueueAccessVacation ()	

Job Start

At the discretion of the SimQueue, a visiting SimJob can be moved from the waiting area to the service area. This is referred to as a *job start*. The start of a job cannot be (directly) controlled by the user. In our interface, it is important to note that 'started jobs' do not necessarily have exclusive access to the server(s). Between arrival and start, a job is said to be *waiting*. After its start, a job is said to be *started*.

Job Revocation

Once a job has been offered, revoke(double, J, boolean) tries to revoke the job, if (still) possible and if supported by the queue discipline at all. The return value indicates if the revocation succeeded. The first argument is the time of the revocation attempt, the second is the job to be revoked. The third argument indicates whether it is allowed to revoke the job from the service area. If false, the revocation attempt will always fail if the job is already in the service area. Note the difference between a revocation (at the caller's discretion) and a drop (at the queue's discretion).

Method	Description
boolean	Revocation attempt of a job at the queue.
revoke (double, J, boolean)	

Server-Access Credits

During a server-access vacation, jobs are prohibited to start, i.e., there is no access to the service area for jobs in the waiting area. It does not affect jobs that have already started. Server-access vacations are actually somewhat more flexible through the notion of server-access credits, denoting the number of jobs still admissible to the service

area, see getServerAccessCredits(). A server-access vacation starts when there are no more server-access credits (due to jobs starting), and ends when credits are explicitly granted to the interface through setServerAccessCredits(double, int). Note that by default, each SimQueue has infinite server-access credits.

Method	Description
void	Sets the remaining SACs at given time.
setServerAccessCredits (double, int)	
int	Gets the actual SACs.
getServerAccessCredits ()	

Note that the value Integer.MAX_VALUE is interpreted as $+\infty$.

Job Departure

At the discretion of the SimQueue, a visiting job may leave the queue because it "got what it came for", i.e., its visit comes to an end according to the queueing discpline in place. This is referred to a *job departure*; and it cannot be enforced by the user. We want to stress that jobs do not necessarily depart from the service area, but can depart from the waiting area as well, or even immediately upon arrival (in which case we formally do not speak of a visit).

The StartArmed Property of a SimQueue

Every SimQueue (implementation) supports the notion of the StartArmed property. The property is a but difficult to grasp at first sight and has little use in simulations, but it is essential in so-called *compressed tandem queues*, see XXX. Nonetheless, since it is part of the SimQueue interface, we state its formal definition: A SimQueue is in StartArmed state, if and only if any (hypothetical) arriving job would start service immediately (i.e., enter the service area upon arrival immediately), if the following conditions would hold:

- the absence of a queue access vacation,
- at least one server-access credit, and
- an empty waiting area.

The actual values of these three state properties is irrelevant, which, admittedly, makes the definition quite hard to understand. If a SimQueue is in StartArmed state, changing its state such that it meets the three conditions above, would lead to the immediate start of a hypothetical arriving job (irrespective of the type and properties of that job).

As an example, consider an instance of the (single-server) FCFS queueing system which has no queue-access vacation, and suppose that it is out of server-access credits, has a single job in the waiting area and no jobs in the service area. In this case, StartArmed == true because an arriving job would be taken into service if we apply the state transformation rules: (1) remove any queue-access vacation (check), (2) give it a single (or more) server-access credit, and (3) remove the job from the waiting area. This leaves a FCFS queueing system without queue-access-vacation, no jobs in the waiting area, and at least one server-access credits, and surely, such a queue would immediately start an arriving job. If initially, however, a job would be in service at the queue, we have StartArmed == false, because the transformed state of the queueing system has a job in service, and FCFS cannot guarantee at all that an arriving job would be taken into service. If on he other side, in the latter case the queue is of type PS, we would have StartArmed == true, because the presence of jobs in the service area in PS, does not inhibit it from immediately starting newly arrived jobs.

Informally, the StartArmed state of a queue reflects the fact as far as the service area is concerned, at least one more job can be added to it.

Method	Description
boolean	Gets the StartArmed property value.
isStartArmed ()	

Copying a SimQueue

Every SimQueue (implementation) supports the creation of a copy of itself.

5.4 The SimJob Interface

Compared to the SimQueue interface, the SimJob interface is remarkably simple. Apart from the internal maintenace of the SimQueue being visited, a SimJob only needs to provide information on the so-called requested service time for a queue visit, through implementation of getServiceTime (Q). This method is used by a @link SimQueue to query the requested service time, and appropriately schedule a departure event for the job, but it can be called anytime. However, the returned value should not change during a visit to a SimQueue, and it is not manipulated by the queue being visited, in other words, it cannot be used to query the remaining service time of a job at a queue. It is safe though to change the return value inbetween queue visits. However, the convention is that the method then returns the required service time at the next visit to the queue. For instance, many test and job-

factory classes depend on this, as they often directly probe a non-visiting job for its required service time at a queue. Obviously, implementations must be prepared for invocations of this method while not visiting a queue. If null, s passed as agrument the service time at the current queue is used, or zero if the job is not currently visiting a queue.

Method	Description
Q	The queue currently visiting.
getQueue ()	
void	Sets the queue currently visiting.
setQueue (Q)	
double	Gets the service time for a visit.
getServiceTime (Q)	

5.5 Invariants and Constraints

Despite the large number of freedom degrees for SimQueues, there is also a number of (obvious) restrictions on the behavior of a queue. For instance,

- a job cannot start, be dropped or be revoked before having arrived;
- a job can start at most once during a queue visit;
- a job can only leave the queueing system through departure (with or without being served), successful revocation or drop;
- a job may not leave the queue at all (a *sticky* job).

Note that with the current interface, a SimJob cannot visit multiple SimQueues simultaneously. The SimQueue currently being visited by a SimJob can be obtained from SimJob.getQueue (); this must be maintained by implementations of arrive (J, double).

5.6 Listening to a SimEntity

One can listen to relevant events at a SimEntity by registering with the entity as a SimEntityListener, the methods of which are summarized in the table below.

Method	Description
void notifyResetEntity	Notification of the reset of an entity
(SimEntity)	
void notifyUpdate	Notification of an update at an entity
(double, SimEntity)	
void notifyStateChanged	Notification of a state change at an entity
(double, SimEntity)	
void notifyArrival	Notification of the arrival
(double, J, Q)	of a job at a queue
void notifyStart	Notification of the start
(double, J, Q)	of a job at a queue
void notifyDrop	Notification of the drop
(double, J, Q)	of a job at a queue
void notifyRevocation	Notification of the successful revocation
(double, J, Q)	of a job at a queue
void notifyDeparture	Notification of the departure
(double, J, Q)	of a job at a queue

It is important to realize that most notifications are fired at the time the SimEntity has processed the corresponding event, and attained its new state. However, there are the following exceptions:

- Update notifications are, by their nature, fired before any state change;
- Arrival notifications are fired *before* the job enters the queue (or before it is dropped);
- Unsuccessful revocations are *not* reported as notification.

Notifications can have tricky semantics, and one should be careful at making assumptions of the SimEntity upon receiving a notification. This is because with notifications, we attempt to achieve two potentially conflicting objectives:

- Each state change is reported as notification;
- Notification listeners always find the SimEntity in a valid state.

So, for instance, one should not assume that during an arrival notification, the job is actually present at the queue, because a queue-access vacation may be active. In that case, the queue will report an arrival of the job, immediately followed by a notification of the job having been dropped. However, upon reception of the arrival notification, the job will not be present at the SimQueue, because that would exhibit an illegal state

of that queue. What we would actually like here, is a notification of a sequence of events at the queue, all happening at the same time, yet in a particular order. In this particular example, a notification of the sequence (ARRIVAL(t,j,q), DROP(t,j,q)) would be required, where t is the time, j is the job and q is the queue. And even though this may not seem important right now, realize that certain queue types depend on maintaining the validity of invariants throughout their lifetime. For instance, the DROP queue drops jobs immediately upon arrival, irrespective of the state of the queue-access vacation. An important sensible invariant for the DROP queue, is that the set of jobs visiting it is always empty. Analogeous invariants exist for other queue types, and we take great care to enforce these invariants to listeners as well as to independently scheduled events.

For SimQueues, one can ontain additional information by registering as a SimQueueListener, the methods of which are summarized in the table below.

Method	Description	
void notifyNewNoWaitArmed	Notification of a change	
(double, Q, boolean)	of the ${\tt noWaitArmed}$ state	
void notifyStartQueueAccessVacation	Notification of the start	
(double, Q)	of a queue-access vacation	
void notifyStopQueueAccessVacation	Notification of the end	
(double, Q)	of a queue-access vacation	
void notifyOutOfServerAccessCredits	Notification that a queue	
(double, Q)	has run out of server-access credits	
void notifyRegainedServerAccessCredits	Notification that a queue	
(double, Q)	has regained server-access credits	

5.7 Formal Treatment of Simulation Entities

Whereas the previous sections introduced SimEntity, SimQueue, and SimJob objects from a use-case perspective, the current section tightens the rope a bit, and treats these objects more formally.

5.7.1 Properties of an Entity

Operational Properties

An *operational* property of an entity is a property that can be changed at any time by the user without effects on the entity's behavior in a simulation. In addition, these properties are never affected by a simulation (i.e., by *operations* on the entity).

Examples include:

- The *name* of an entity;
- The *listeners* to the entity.

Essential Properties

An essential property of an entity is a property that can be only be changed before and after a simulation (i.e., immediately after a reset or construction, but before the start of the simulation). Like operational properties, however, essential properties are never affected by operations on the entity. Essential properties impact the behavior of the queueing system during simulations, but should remain constant while simulating. Examples include:

- The *buffer size* of a FCFS_B queue;
- The *number of servers* of a FCFS_c queue;
- The waiting time of a DELAY queue.

State Properties

Unlike operational and essential properties, *state* properties cannot be directly set by the user; they can only be read. State properties are those properties that change as a result of a simulation running, and the entity being subject to scheduled operations from the event list. State properties can be further subdivided into

- Event properties: State properties that can only change due to an operation (either internal or external) on the entity.
- Continuous properties: State properties that (potentially) change continuously over time, even in the absence of operations on the entity.

Some examples of event properties:

- The set of jobs (in the waiting/service) area) present at a SimQueue;
- The queue-access vacation state of a SimQueue;
- The StartArmed state of a SimQueue.

Some examples of continuous properties:

- The remaining service time of the job in the service area in PS queue;
- The total remaining work in a FCFS queue;
- The elapsed time since the start of the current busy period for a SimQueue.

Note that changes to event properties are always reported to listeners of the entity; whereas changes to continuous properties are *never* reported.

Orthogonal to distinction between state and continuous properties, a state property may be

- Exposed: The property value is accessible to callers.
- **Hidden**: The property value is hidden from callers.
- The State of a Simulation Entity 5.7.2
- 5.7.3 External Operations on a Simulation Entity
- 5.7.4 **Internal Operations on a Simulation Entity**
- Notifications of a Simulation Entity 5.7.5
- 5.7.6 **Extensions**

State Extensions

Operation Extensions

Notification Extensions

Chapter 6

Fundamental Queues

In this chapter we describe implementations of ${\tt SimQueue}$ corresponding to well-knwon queueing disciplines.

6.1 Introduction

6.2 The Generic SimQueue

6.2.1 Introduction

6.2.2 Essential Properties

$\operatorname{Sim}\operatorname{Queue}$			
Essential Properties			
EventList	SimEventList	The event list; non-null.	
AutoRevocationPolicy	AutoRevocationPolicy	The auto-revocation policy.	
RegisteredOperations	Set <simentityoperation></simentityoperation>	The registered operations.	
RegisteredNotificationTypes	Set <member></member>	The registered notification types.	

6.2.3 State Properties

SimQueue			
State Properties			
LastUpdateTime	EE	double	Last update (or reset) time.
QueueAccessVacation	EE	boolean	Queue-Access Vacation state.
StartArmed	EE	boolean	The StartArmed state.
Jobs	EE	Set <j></j>	Jobs present (default: arrival order).
JobsInWaitingArea	EE	Set <j></j>	Jobs waiting (default: arrival order).
JobsInServiceArea EE Set <j> Jobs in service (default: start or</j>		Jobs in service (default: start order).	
ServerAccessCredits $EE int \ge 0$ Number of server-access credits.			

6.2.4 Operations

SimQueue			
Operations			
Update	Е	double	Update at time.
DoOperation	Е	double, Request	Perform operation at time.
SetQueueAccessVacation	Е	double, boolean	Starts/ends a QAV at time.
Arrive	Е	J	Arrival of job at time.
Drop	Ι	J	Drop of job at time.
Revoke	Е	J, boolean	Revocation attempt of job at time.
SetServerAccessCredits	Е	$int \ge 0$	Set the SACs at time.
Start	Ι	J, double	Starts job at time.
Depart	I	J	Lets job depart at time.

6.2.5 State Invariants

SimQueue
State Invariants
${\tt JobsInWaitingArea} \cap {\tt JobsInServiceArea} = \emptyset.$
${ t Jobs} = { t JobsInWaitingArea} \cup { t JobsInServiceArea}.$

6.2.6 Notification Types

SimQueue					
Notification Types					
RESET	double Reset notification with new time.				
UPDATE	DATE double Update notification with				
STATE_CHANGED	<pre>double, Set<notification></notification></pre>	State-changed notification			
		with new time and sub-notifications.			

6.2.7 Internal Schedulable Events

SimQueue		
Internal Schedulable Events		
DepartureEvent	The scheduled departure of a job.	

6.2.8 Operational Properties

SimQueue				
Operational Properties				
Name	String The name,			
default depends on sub-clas				
SimEntityListeners	tityListeners Set <simentitylistener> The registered listeners.</simentitylistener>			

6.3 Serverless Queues

The *serverless* queueing systems in jqueues have no servers and (effectively) no service area. All state operations and state changes concentrate at the waiting area of the queue, and typically upon arrivals. Note that just because the serverless queues have no service area does not mean that visiting jobs cannot depart from it.

6.3.1 The DROP SimQueue

DROP			
Drops jobs	immediately upon arrival.		
Super			
SimQueue	SimQueue See Section 6.2.		
State Invariants			
StartArmed = false.			
${\tt Jobs}=\emptyset.$			
Operational Properties			
Name	The name, default "DROP".		

6.3.2 The SINK SimQueue

SINK			
Lets jobs u	vait indefinitely.		
Super			
SimQueue See Section 6.2.			
State Invariants			
StartArmed = false.			
${ t Jobs} = { t JobInWaitingArea}.$			
Operational Properties			
Name	The name, default "SINK".		

6.3.3 The ZERO SimQueue

ZERO		
Lets jobs d	epart immediately upon arrival.	
Super		
SimQueue	See Section 6.2.	
State Invariants		
StartArmed = false.		
${\tt Jobs}=\emptyset.$		
Operational Properties		
Name	The name, default "ZERO".	

6.3.4 The DELAY SimQueue

DELAY				
Lets jobs d	epart after a fixed wait time.			
Super				
SimQueue	See Section 6.2.			
	Essential Properties			
WaitTime	The wait time, non-negative.			
	State Invariants			
StartArme	d = false.			
	Jobs = JobsInWaitingArea.			
$\texttt{WaitTime} = 0 \Rightarrow \texttt{Jobs} = \emptyset.$				
Operational Properties				
Name	The name, default "DELAY [WaitTime]".			
Equivalences				
$ \begin{split} & \mathtt{DELAY}[0] = \mathtt{ZERO}. \\ & \mathtt{DELAY}[\infty] = \mathtt{SINK}. \end{split} $				

6.3.5 The GATE SimQueue

GATE			
Lets jobs depart in arrival	order	while its	"gate" is open; lets jobs wait otherwise.
Super			
SimQueue	See	Section 6.2	2.
State Properties			
GatePassageCredits	EE	${\tt int} \geq 0$	Remaining allowed departures.
		Operat	tions
SetGatePassageCredits	Е	$\mathtt{int} \geq 0$	Sets the remaining number of GPCs. Integer.MAX_VALUE is treated as $+\infty$.
State Invariants			
$\mathtt{StartArmed} = \mathtt{false}.$			
$\mathtt{GatePassageCredits} > 0 \Rightarrow \mathtt{Jobs} = \emptyset.$			
Operational Properties			
Name The name, default "GATE".			

6.3.6 The ALIMIT SimQueue

ALIMIT			
			Arrival-Rate Limiter
Lets jobs depa	rt immedi	ately but di	rops jobs whose arrival exceeds a given arrival-rate limit.
			Super
SimQueue	See Sect	ion 6.2.	
]	Essential Properties
RateLimit	double	The rate	$\lim_{t \to \infty} 1; t \to \infty.$
			State Properties
RateLimited	HE	boolean	Whether currently (arrival) rate-limited.
		Inter	rnal Schedulable Events
RateLimitExp	RateLimitExpirationEvent The expiration of the rate-limit period.		
Operational Properties			
Name The name, default "ALIMIT[RateLimit]".			
Equivalences			
${ t ALIMIT}[0] = { t DROP}. \ { t ALIMIT}[\infty] = { t ZERO}.$			

6.3.7 The DLIMIT SimQueue

DLIMIT				
		Depart	ture-Rate Limiter	
T , : 1 1	1. 1.	_		
Lets jobs depar	rt immedi	ately but re	espects a given departure-rate limit.	
			Super	
SimQueue	See Sect	ion 6.2.		
		Essen	atial Properties	
RateLimit	double	The rate	$\lim_{t \to \infty} 1_{t} = 0; t = 0.$	
		Stat	te Properties	
RateLimited	HE	boolean	Whether currently (departure) rate-limited.	
		Internal S	Schedulable Events	
RateLimitExp	irationE	vent	The expiration of the rate-limit period.	
	Operational Properties			
Name	Name The name, default "DLIMIT[RateLimit]".			
Equivalences				
$ ext{DLIMIT}[0] = S$ $ ext{DLIMIT}[\infty] = S$				

6.3.8 The LeakyBucket SimQueue

LeakyBucket				
		0	spects a given departure-rate limit, o wait but find the waiting area full.	
			Super	
SimQueue	See Section	on 6.2.		
			Essential Properties	
BufferSize	$int \ge 0$	The buffe	er size; Integer.MAX_VALUE is treated as $+\infty$.	
RateLimit	double	The rate	$\lim_{t \to \infty} 1, t \to 0; t \to \infty.$	
			State Properties	
RateLimited	HE	boolean	Whether currently (departure) rate-limited.	
		Inte	ernal Schedulable Events	
RateLimitExp	irationEv	rent	The expiration of the rate-limit period.	
	Operational Properties			
Name			$\label{thm:continuity} \begin{tabular}{ll} The name, default "LeakyBucket[BufferSize,RateLimit]". \end{tabular}$	
Equivalences				
LeakyBucket[LeakyBucket[-			

6.3.9 The WUR SimQueue

WUR

Wait Until Relieved

Lets arriving jobs wait for their departure until the next arrival.

Super

SimQueue | See Section 6.2.

State Invariants

 $|\mathsf{Jobs}| = 0 \text{ or } 1.$

Operational Properties

Name | The name, default "WUR".

6.4 Nonpreemptive Queues

6.4.1 The FCFS SimQueue

	FCFS				
		First-Come Fir	est-Served		
and infinite buffer.	size.		· ·		
The server can server	ve a	t most one job at a tim	ve.		
	Super				
SimQueue	Se	e Section 6.2.			
		Essential Pro	operties		
BufferSize	F	Integer.MAX_VALUE	The buffer size; Integer.MAX_VALUE is treated as $+\infty$.		
NumberOfServers	F	1	The number of servers.		
	State Invariants				
,	$\begin{aligned} \mathtt{StartArmed} &= (\mathtt{JobsInServiceArea} = \emptyset). \\ \mathtt{JobsInServiceArea} &\leq 1. \end{aligned}$				
$\texttt{ServerAccessCredits} > 0, \ \texttt{JobsInWaitingArea} \neq \emptyset \Rightarrow \texttt{JobsInServiceArea} \neq \emptyset.$					
Operational Properties					
Name	Th	ne name, default "FCFS	5".		

6.4.2 The FCFS_B SimQueue

3	S_{-1}	CF	F
3	S_{-1}	CF	F.

First-Come First-Served with given buffer size

Serves jobs in arrival order until completion with a single server and given (possibly finite) buffer size (BufferSize).

The server can serve at most one job at a time.

Super

SimQueue	See Section	6.2
----------	-------------	-----

Essential Properties

BufferSize	С	$int \ge 0$	The buffer size;
			Integer.MAX_VALUE is treated as $+\infty$.
NumberOfServers	F	1	The number of servers.

State Invariants

 $\mathtt{StartArmed} = (\mathtt{JobsInServiceArea} = \emptyset).$

 $|JobsInWaitingArea| \le BufferSize.$

 $|\mathsf{JobsInServiceArea}| \leq 1.$

 $\texttt{ServerAccessCredits} > 0, \, \texttt{JobsInWaitingArea} \neq \emptyset \Rightarrow \texttt{JobsInServiceArea} \neq \emptyset.$

Operational Properties

Name The name, default "FCFS_B[BufferSize]".

Equivalences

 $FCFS_B[Integer.MAX_VALUE] = FCFS.$

6.4.3 The FCFS_c SimQueue

FCFS_c

First-Come First-Served with given number of servers

Serves jobs in arrival order until completion

with a given number (NumberOfServers) of equal servers and infinite buffer size.

Each server can serve at most one job at a time.

Jobs do not prefer one server over another; there are no server affinities.

Super

SimQueue	See	Section	6.2.

Essential Properties

BufferSize	F	Integer.MAX_VALUE	The buffer size;
			Integer.MAX_VALUE is treated as $+\infty$.
NumberOfServers	С	$\mathtt{int} \geq 0$	The number of servers;
			Integer.MAX_VALUE is treated as $+\infty$.

State Invariants

StartArmed = (|JobsInServiceArea| < NumberOfServers).

 $|JobsInServiceArea| \leq NumberOfServers.$

ServerAccessCredits > 0, JobsInWaitingArea $\neq \emptyset$

 \Rightarrow |JobsInServiceArea| = NumberOfServers.

Operational Properties

Name The name, default "FCFS_NumberOfServers".

Equivalences

 $FCFS_0 = DROP.$

 $FCFS_1 = FCFS$.

6.4.4 The FCFS_B_c SimQueue

FCFS_B_c

First-Come First-Served with given buffer size and number of servers

Serves jobs in arrival order until completion with a given number (NumberOfServers) of equal servers and given (possibly finite) buffer size (BufferSize). Each server can serve at most one job at a time.

Jobs do not prefer one server over another; there are no server affinities.

Super

SimQueue	See Section 6.2.		
	Essen		ntial Properties
BufferSize	С	$int \ge 0$	The buffer size;
			Integer.MAX_VALUE is treated as $+\infty$.
NumberOfServers	С	$\mathtt{int} \geq 0$	The number of servers;
			Integer.MAX_VALUE is treated as $+\infty$.

State Invariants

StartArmed = (|JobsInServiceArea| < NumberOfServers).

 $|{\tt JobsInWaitingArea}| \leq {\tt BufferSize}.$

 $|JobsInServiceArea| \le NumberOfServers.$

ServerAccessCredits > 0, JobsInWaitingArea $\neq \emptyset$

 \Rightarrow |JobsInServiceArea| = NumberOfServers.

Operational Properties

Name The name, default "FCFS_NumberOfServers[BufferSize]".

Equivalences

 $FCFS_1[Integer.MAX_VALUE] = FCFS.$

 $FCFS_1[B] = FCFS_B[B].$

FCFS_c[Integer.MAX_VALUE] = FCFS_c.

 $FCFS_0[0] = DROP.$

FCFS_0[Integer.MAX_VALUE] = SINK.

6.4.5 The IS SimQueue

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ı	١.	`

Infinite Servers

Serves jobs in arrival order until completion with an infinite number of servers and infinite buffer size.

Each server can serve at most one job at a time.

Jobs do not prefer one server over another; there are no server affinities.

Super

SimQueue	See Section 6	.2.

Essential Properties

BufferSize	F	Integer.MAX_VALUE	The buffer size;
			Integer.MAX_VALUE is treated as $+\infty$.
NumberOfServers	F	Integer.MAX_VALUE	The number of servers;
			Integer.MAX_VALUE is treated as $+\infty$.

State Invariants

 $StartArmed = \overline{true}$.

 ${\tt ServerAccessCredits} > 0 \Rightarrow {\tt JobsInWaitingArea} = \emptyset.$

Operational Properties

Name The name, default "IS".

Equivalences

 $IS = FCFS_Integer.MAX_VALUE.$

IS = FCFS_Integer.MAX_VALUE[Integer.MAX_VALUE].

6.4.6 The IS_CST SimQueue

IS_CST

Infinite Servers with Constant Service Time

Serves jobs in arrival order until completion with an infinite number of servers and infinite buffer size.

 $Each\ job\ is\ served\ for\ a\ queue-determined\ fixed\ service\ time\ ({\tt ServiceTime}).$

Each server can serve at most one job at a time.

Jobs do not prefer one server over another; there are no server affinities.

Super

SimQueue	See	See Section 6.2.		
Essential Properties				
BufferSize	F	Integer.MAX_VALUE	The buffer size;	
			Integer.MAX_VALUE is treated as $+\infty$.	
NumberOfServers	F	Integer.MAX_VALUE	The number of servers;	

State Invariants

Integer.MAX_VALUE is treated as $+\infty$.

The service time for each job.

StartArmed = true.

ServiceTime

 $\texttt{ServerAccessCredits} > 0 \Rightarrow \texttt{JobsInWaitingArea} = \emptyset.$

double > 0

ServiceTime = $0 \Rightarrow JobsInServiceArea = \emptyset$.

С

Operational Properties

Name The name, default "IS_CST[ServiceTime]".

6.4.7 The IC SimQueue

T	1	7
ı	l	,

Infinite Capacity

Serves jobs in arrival order until completion

with an infinite number of infinite-capacity servers and infinite buffer size.

Each job is served in zero time.

Each server can serve at most one job at a time.

Jobs do not prefer one server over another; there are no server affinities.

Super

SimQueue	See Section 6	.2.

Essential Properties

BufferSize	F	Integer.MAX_VALUE	The buffer size;
			Integer.MAX_VALUE is treated as $+\infty$.
NumberOfServers	F	Integer.MAX_VALUE	The number of servers;
			Integer.MAX_VALUE is treated as $+\infty$.

State Invariants

StartArmed = true.

ServerAccessCredits $> 0 \Rightarrow \text{Jobs} = \emptyset$.

 $JobsInServiceArea = \emptyset.$

Operational Properties

Name The name, default "IC".

Equivalences

 $IC = IS_CST[0].$

6.4.8 The NoBuffer_c SimQueue

NoBuffer_c

Serves jobs in arrival order until completion

with a given number (NumberOfServers) of equal servers and zero buffer size. Each server can serve at most one job at a time.

Jobs do not prefer one server over another; there are no server affinities.

Super

SimQueue	See	Section	6.2.

Essential Properties

BufferSize	F	0	The buffer size;
NumberOfServers	С	$int \ge 0$	The number of servers;
			Integer.MAX_VALUE is treated as $+\infty$.

State Invariants

StartArmed = (|JobsInServiceArea| < NumberOfServers).

JobsInWaitingArea= \emptyset .

 $| JobsInServiceArea | \le NumberOfServers.$

Operational Properties

Name	The name, default	${ m ``NoBuffer_NumberOfServers''}.$
------	-------------------	---------------------------------------

Equivalences

 $NoBuffer_c = FCFS_c[0].$

 $NoBuffer_1 = FCFS[0].$

 $NoBuffer_0 = DROP.$

6.4.9 The LCFS SimQueue

LCFS				
		Last-Come First-	-Served	
and infinite buffer siz	e.	val order until completion	on with a single server	
The server can serve	at me	ost one joo at a time.		
		Super		
SimQueue	See	Section 6.2.		
		Essential Prop	perties	
BufferSize	F	F Integer.MAX_VALUE The buffer size; Integer.MAX_VALUE is treated as $+\infty$.		
NumberOfServers	F	1	The number of servers.	
		State Proper	rties	
JobsInWaitingArea	EE	Set <j></j>	Jobs waiting	
_			in reverse-arrival order.	
State Invariants				
${ t StartArmed} = ({ t JobsInServiceArea} = \emptyset).$				
$ { t JobsInServiceArea} \leq 1.$				
${\tt ServerAccessCredits} > 0, \ {\tt JobsInWaitingArea} \neq \emptyset \Rightarrow {\tt JobsInServiceArea} \neq \emptyset.$				
Operational Properties				
Name	The	name, default "LCFS"		

6.4.10 The SJF SimQueue

SJF				
		Shortest-Job 1	First	
Serves jobs in increas	ing se	ervice-time order until	completion	
with a single server a		• • • • • • • • • • • • • • • • • • • •		
The server can serve	at me	ost one job at a time.		
		Super		
		Super		
SimQueue	See	Section 6.2.		
		Essential Prop	perties	
		Essentiai i rop	oer tres	
BufferSize	F	Integer.MAX_VALUE	The buffer size;	
			Integer.MAX_VALUE is treated as $+\infty$.	
NumberOfServers	F	1	The number of servers.	
		State Proper	ctios	
		State 1 Tope	lues	
JobsInWaitingArea	EE	Set <j></j>	Jobs waiting	
			in increasing service-time order.	
		C T .		
		State Invaria	ants	
StartArmed = (Jobs)	InSer	$\overline{ ext{viceArea} = \emptyset}$).		
JobsInServiceArea ≤ 1 .				
Operational Properties				
Name The name, default "SJF".				
	I	·		

6.4.11 The LJF SimQueue

LJF				
		Longest-Job I	First	
		Longest-Job 1	1150	
Serves jobs in decreas	sing s	ervice-time order until	completion	
with a single server a		• • • • • • • • • • • • • • • • • • • •		
The server can serve	at mo	ost one job at a time.		
		Super		
		Super		
SimQueue	See	Section 6.2.		
		Essential Prop	perties	
BufferSize	F	Integer.MAX_VALUE	The buffer size;	
			Integer.MAX_VALUE is treated as $+\infty$.	
NumberOfServers	F	1	The number of servers.	
		State Proper	etios	
		State 1 Topel	lites	
JobsInWaitingArea	EE	Set <j></j>	Jobs waiting	
			in decreasing service-time order.	
		State Invaria		
		State Invaria	ants	
StartArmed = (Jobs)	$\texttt{StartArmed} = (\texttt{JobsInServiceArea} = \emptyset).$			
$ JobsInServiceArea \leq 1.$				
${\tt ServerAccessCredits} > 0, \ {\tt JobsInWaitingArea} \neq \emptyset \Rightarrow {\tt JobsInServiceArea} \neq \emptyset.$				
On another all D				
Operational Properties				
Name	ame The name, default "LJF".			

6.4.12 The RANDOM SimQueue

RANDOM				
Serves jobs in random with a single server a The server can serve	nd inj	finite buffer size.		
		Super		
SimQueue	See	Section 6.2.		
		Essential Prop	erties	
BufferSize	F Integer.MAX_VALUE The buffer size; Integer.MAX_VALUE is treated as $+\infty$.			
NumberOfServers	F	1	The number of servers.	
		State Proper	rties	
JobsInWaitingArea	Jobs InWaitingArea EE Set <j></j>			
	State Invariants			
$\begin{aligned} & \mathtt{StartArmed} = (\mathtt{JobsInServiceArea} = \emptyset). \\ & \mathtt{JobsInServiceArea} \leq 1. \\ & \mathtt{ServerAccessCredits} > 0, \ \mathtt{JobsInWaitingArea} \neq \emptyset \Rightarrow \mathtt{JobsInServiceArea} \neq \emptyset. \end{aligned}$				
Operational Properties				
Name	Name The name, default "RANDOM".			

6.4.13 The SUR SimQueue

	SUR			
		Serve Until F	Relieved	
Companie de la comie	1	and an auntil the stant of t	the ment ich	
		order until the start of t d infinite buffer size.	me next 100	
_		t most one job at a tim	,e	
The server can serve	oc an			
		Super	•	
		•		
SimQueue	See	e Section 6.2.		
		Essential Pro	operties	
D CC G:		T . MAY WATTID		
BufferSize	F	Integer.MAX_VALUE	The buffer size;	
NumberOfServers	F	1	Integer.MAX_VALUE is treated as $+\infty$. The number of servers.	
Number Orser vers	T,	1	The humber of servers.	
		State Inva	riants	
		State IIIva	Terros	
StartArmed = true	ə.			
$ JobsInServiceArea \leq 1.$				
${ t ServerAccessCredits} > 0 \Rightarrow { t JobsInWaitingArea} = \emptyset.$				
Operational Properties				
Name	Th	e name, default "SUR'	•	

6.5 Preemptive Queues

In preemptive queues, the service area consists of a countable number of servers, each capable of serving a single job at a time, yet this service to a job can be *preempted* in favor of another job.

6.5.1 Preemption Strategies; the PreemptionStrategy Class

At the moment a job is preempted at a server, one of several things can happen, as determined by the *preemption strategy*. In jqueues, the preemption strategy is implemented in an enum name PreemptionStrategy, and it can take the following values:

- DROP: The preemped job is dropped.
- RESUME: The preempted job is put on hold, after calculating the remaining service time. Future service resumption continues at the point where the previous service was interrupted.
- RESTART: The preempted job is put on hold. Future service resumption requires the job to be served from scratch.
- REDRAW: The preempted job is put on hold. Future service resumption requires the job to be served from scratch with a new required service time.
- DEPART: The preempted job departs, even though it may not have finished its service requirements.
- CUSTOM: A different strategy that those mentioned above is applied to preempted jobs. The strategy needs to be specified in the concrete SimQueue implementation.

Not all preemptive-queue implementations support all preemption strategies. For instance, the REDRAW strategy is not supported by any implementation, because it conflicts with the contract the the service time of a SimJob has to remain constant during a (single) SimQueue visit.

The preemption strategy is a parameter that can be passed upon construction by all implemented preemptive queues in jqueues. Its default value is RESUME. If you pass an unsupported preemption strategy, the queue will throw an UnsupportedOperationException.

6.5.2 The P_LCFS SimQueue

Р	_]	[]	C	F	S

Preemptive Last-Come First-Served

Serves jobs in reverse arrival order until completion or preemption with a single server and infinite buffer size.

A job in service is preempted upon the start of a new job.

The server can execute at most one job at a time,

but an arbitrary number of jobs may be in service.

Super

SimQueue	See	Section	6.2.
----------	-----	---------	------

Essential Properties

BufferSize	F	Integer.MAX_VALUE	The buffer size;	
			Integer.MAX_VALUE is treated as $+\infty$.	
NumberOfServers	F	1	The number of servers.	
PreemptionStrategy	С	PreemptionStrategy	The preemption strategy.	

State Properties

${ t JobsInWaitingArea}$	EE	Set <j></j>	Jobs waiting
			in reverse-arrival order.

Operations

Preempt	I	double, J	Job preemption at time.
StartServiceChunk	I	double, J	Start service chunk for job at time.

State Invariants

StartArmed = true.

 ${\tt ServerAccessCredits} > 0 \Rightarrow {\tt JobsInWaitingArea} = \emptyset.$

Operational Properties

Name	Э	The	e name,	default	″ F	'_LCFS	Pr	reemp	tionS	trat	egy	· •
------	---	-----	---------	---------	------------	--------	----	-------	-------	------	-----	-----

6.5.3 The SRTF SimQueue

SRTF

Shortest Remaining-Time First

Serves jobs in reverse order of remaining service time until completion or preemption with a single server and infinite buffer size.

A job in service is preempted upon the start of a new job

with a strictly smaller remaining service time.

Jobs are started in reverse required service-time order

at the earliest opportunity (i.e., independent of the state of the service area).

The server can execute at most one job at a time,

but an arbitrary number of jobs may be in service.

Super

SimQueue	See Section 6.2.
----------	------------------

Essential Properties

BufferSize	F	Integer.MAX_VALUE	The buffer size;
			Integer.MAX_VALUE is treated as $+\infty$.
NumberOfServers	F	1	The number of servers.
PreemptionStrategy	С	PreemptionStrategy	The preemption strategy.

State Properties

${ t JobsInWaitingArea}$	EE	Set <j></j>	Jobs waiting in (1) service-time
			and (2) arrival order.

Operations

Preempt	I	double, J	Job preemption at time.
StartServiceChunk	I	double, J	Start service chunk for job at time.

State Invariants

StartArmed = true.

ServerAccessCredits $> 0 \Rightarrow \texttt{JobsInWaitingArea} = \emptyset$.

Operational Properties

Name	The name, default "SRTF[PreemptionStrategy]".

6.6 Processor-Sharing Queues

In Processor-Sharing (PS) queues, the service area consists of a countable number of servers, each capable of serving multiple jobs at a time, sharing its capacity among those jobs.

6.6.1 The PS SimQueue

PS					
		Processor S	haring		
Serves all started in	bs	simultaneously at equal	rates until completion		
		d infinite buffer size.	r		
		ival order at the earlies	t opportunity.		
The server can exec	cute	an arbitrary number o	f jobs $simultaneously$.		
			· · ·		
		Super	r		
SimQueue	Se	e Section 6.2.			
		Essential Pro	operties		
BufferSize	F	Integer.MAX_VALUE	The buffer size;		
		0 -	Integer.MAX_VALUE is treated as $+\infty$.		
NumberOfServers	F	1	The number of servers.		
		<u> </u>			
		State Inva	riants		
StartArmed = true	StartArmed = true.				
${\tt ServerAccessCredits} > 0 \Rightarrow {\tt JobsInWaitingArea} = \emptyset.$					
	Operational Properties				
Name	Th	ne name, default "PS".			

6.6.2 The CUPS SimQueue

CUPS

Catch-Up Processor-Sharing

Serves all started jobs with least obtained service times simultaneously at equal rates until (1) completion, or (2) another job starts or

(3) the jobs in execution "catch-up"

in terms of obtained service time with another set of jobs in service, with a single server and infinite buffer size.

Jobs are started in arrival order at the earliest opportunity.

The server can execute an arbitrary number of jobs simultaneously.

Super

Essential Properties

BufferSize	F	Integer.MAX_VALUE	The buffer size;
			Integer.MAX_VALUE is treated as $+\infty$.
NumberOfServers	F	1	The number of servers.

Operations

CatchUp I double CatchUp	tch-up at time.
--------------------------------	-----------------

State Invariants

StartArmed = true.

ServerAccessCredits $> 0 \Rightarrow JobsInWaitingArea = \emptyset$.

Internal Schedulable Events

CatchUpEvent A "catch-up" event.

Operational Properties

Name	The name, default "CUPS".
------	---------------------------

6.6.3 The SocPS SimQueue

SocPS

Social Processor-Sharing

Serves all started jobs simultaneously such that their departures times are equal, distributing its service capacity among those job to that effect, with a single server and infinite buffer size.

The service rate of a job in the service area

is linearly proportional to its remaining service time.

Jobs are started in arrival order at the earliest opportunity.

The server can execute an arbitrary number of jobs simultaneously.

Super

SimQueue	See Section 6.2.
Simplified 1	see section 0.2.

Essential Properties

BufferSize	F	Integer.MAX_VALUE	The buffer size;
			Integer.MAX_VALUE is treated as $+\infty$.
NumberOfServers	F	1	The number of servers.

State Invariants

StartArmed = true.

ServerAccessCredits $> 0 \Rightarrow JobsInWaitingArea = \emptyset$.

Operational Properties

Name	The name, default "SocPS".

Multiclass Queues and Jobs

- 7.1 Introduction
- 7.2 Nonpreemptive Multiclass Queues
- 7.2.1 The HOL SimQueue
- 7.3 Preemptive Multiclass Queues
- 7.3.1 The PQ SimQueue
- 7.4 Processor-Sharing Multiclass Queues
- 7.4.1 The HOL-PS SimQueue

Composite Queues

8.1 Introduction

Composite queues consist of zero or more other queues named subqueues or embedded queues, and a visit of a job to the composite queue is equivalent to a sequence of visits to the subqueues, the order of which is determined by the composite queue. The most prominent example of a composite queue is called a tandem queue, consisting of a finite sequence of (distinct) queues that a job must visit in order before leaving the composite queue. If we number the subqueues $1, 2, \ldots, K$, a job visiting the tandem queue, must first complete a visit to queue 1, and upon departure from queue 1, it immediately arrives at queue 2, and so forth, until it departs from queue K, at which time it leaves the tandem queue. Using the previous chapters, it is actually rather easy to construct a tandem queue, e.g., a tandem queue consisting of two P_LCFS queues, as we have shown in Listing 8.1 below. The output of the program is shown in Listing 8.2.

Listing 8.1: A tandem queue consisting of two P_LCFS queues (using SimJob).

```
private static final class TandemJob
extends DefaultSelfListeningSimJob
{
    final List<SimQueue> queues;
    public TandemJob (final SimEventList eventList,
        final String name,
        final double requestedServiceTime,
        final List<SimQueue> queues)
    {
        super (eventList, name, requestedServiceTime);
        this.queues = queues;
        this.registerSimEntityListener (new StdOutSimEntityListener ());
    }
    @Override
    public void notifyDeparture (final double time,
        final DefaultSelfListeningSimJob job,
```

```
final SimQueue queue)
{
   if (this.queues.indexOf (queue) < this.queues.size () - 1)
      getEventList ().schedule (time, (SimEventAction) (SimEvent event) ->
      {
       queues.get (queues.indexOf (queue) + 1).arrive (time, job);
      });
   }
}

public static void main (final String[] args)
{
   final SimEventList el = new DefaultSimEventList ();
   el.reset (0);
   final P.LCFS lcfs.1 = new P.LCFS (el, null);
   lcfs.1.setName ("Ql");
   final P.LCFS lcfs.2 = new P.LCFS (el, null);
   lcfs.2.setName ("Q2");
   final List<SimQueue> queueSequence = new ArrayList<> ();
   queueSequence.add (lcfs.1);
   queueSequence.add (lcfs.2);
   for (int j = 1; j <= 5; j++)
      lcfs.1.scheduleJobArrival (j, new TandemJob (el, "J" + j, 10 * j, queueSequence));
   el.run ();
}</pre>
```

Listing 8.2: Output of the program in Listing 8.1.

```
 StdOutSimEntityListener \ t=1.0, \ queue=Q1: \ ARRIVAL \ of \ job \ J1. 
StdOutSimEntityListener t=1.0, queue=Q1:
StdOutSimEntityListener t=2.0, queue=Q1:
                                                          START of job J1.
ARRIVAL of job J2
                                                          START of job J2.
ARRIVAL of job J3.
StdOutSimEntityListener
                                  t=2.0, queue=Q1:
StdOutSimEntityListener t=3.0, queue=Q1: StdOutSimEntityListener t=3.0, queue=Q1:
                                                          START of job J3.
                                                          ARRIVAL of job J4.
START of job J4.
ARRIVAL of job J5.
StdOutSimEntityListener t = 4.0,
                                            queue=Q1:
StdOutSimEntityListener\ t=4.0,
                                            queue=Q1:
                                  t=5.0, queue=Q1: START of job J5.
t=55.0, queue=Q1: DEPARTURE of job J5.
t=55.0, queue=Q2: ARRIVAL of ich T5.
t=55.0. queue=Q2: ARRIVAL of ich T5.
StdOutSimEntityListener t=5.0, queue=Q1:
StdOutSimEntityListener
StdOutSimEntityListener
StdOutSimEntityListener
                                                           START of job J5.
DEPARTURE of job J4.
StdOutSimEntityListener
                                  t = 55.0, queue=Q2:
StdOutSimEntityListener \ t=94.0\,,\ queue=Q1:
StdOutSimEntityListener
                                  t=94.0, queue=Q2:
                                                            ARRIVAL of job J4.
StdOutSimEntityListener t=94.0, queue=Q2: START of job J4. StdOutSimEntityListener t=123.0, queue=Q1: DEPARTURE of job J3.
StdOutSimEntityListener \ t = 123.0 \,, \ queue = \!\!Q2 \colon
                                                             ARRIVAL of job J3.
                                               queue=Q2:
StdOutSimEntityListener t = 123.0, queue=Q2: StdOutSimEntityListener t = 142.0, queue=Q1:
                                                             START of job J3.
DEPARTURE of job J2
                                                             ARRIVAL of job J2.
START of job J2.
DEPARTURE of job J1.
StdOutSimEntityListener\ t \!=\! 142.0\,,
StdOutSimEntityListener\ t=142.0,
                                               queue=Q2:
StdOutSimEntityListener t=151.0, queue=Q1:
                                                             ARRIVAL of job J1.
START of job J1.
DEPARTURE of job J1
{\tt StdOutSimEntityListener} \ \ t \! = \! 151.0 \, ,
                                               queue=Q2:
StdOutSimEntityListener t=151.0.
                                               queue=Q2:
StdOutSimEntityListener \ t=161.0 \,, \ queue=\!\!Q2 \colon
                                               queue=Q2:
{\tt StdOutSimEntityListener}
                                  t = 172.0,
                                                             DEPARTURE of job J2.
                                                             DEPARTURE of job J3.
StdOutSimEntityListener t=183.0, queue=Q2:
{\bf StdOutSimEntityListener}
                                  t = 194.0, queue=Q2:
                                                             DEPARTURE of job J4
StdOutSimEntityListener t=205.0, queue=Q2: DEPARTURE of job J5
```

In the example, 5 jobs are scheduled to arrive at a tandem queueing system consisting of the sequence of two P_LCFS queues named Q1 and Q2. The jobs arrive at t = 1, 2, ..., 5, and require service times at each of the P_LCFS queues of 10, 20, ..., 50, respectively. Given the high required service times compared to the interarrival times, the jobs leave Q1, in reverse order of arrival. However, again because of the relatively high required service times, no job can depart from Q2 before the next arrival at that queue. As a result, Q2 again reverses the order of arriving job in its departure process, and jobs depart from Q2 in order of arrival at the first queue (and

at the virtual tandem queue).

Despite the intriguing result that a tandem queue consisting of two P_LCFS queues can behaves like a FCFS queue with modified service-time requirement, and the fact that the tandem queue was so easy to realize, we want to focus at the implementation of the tandem queue, because there are some issues with it. Most important, we explained in the beginning of this section, that a composite queue behaves like the equivalent of its subqueues equipped with some rouing of jobs between these subqueues. However, in the example, there is no notion of a composite SimQueue at all! The job-arrival process "somehow know" that Q1 is the first queue at which jobs must arrive, and the jobs themselves route themselves to the "next queue". In other words, all the "logic" related to routing jobs in a tandem queue is implemented in the arrival process and in the job implementation, whereas we really want these to be part of the tandem queue, the SimQueue. This, for instance, would allow any to properly visit the composite SimQueue without knowledge on its (internal) structure.

Well, allowing *any* SimJob to visit the tandem queue is not that difficult, as is shown in Listing 8.3 below. All we have to do is listen to departure events on Q1 and then schedule an arrival event at Q2.

Listing 8.3: A tandem queue consisting of two P_LCFS queues (using SimQueue).

The result of the program is identical to that shown in 8.2, and the program itself is surprisingly short (we no longer have to create a dedicated SimJob for the tandem queue). This suggests (luckily) that the jqueues package has sufficient means to model composite queues manually. However, we are still faced with the problems that there is not really a notion of a composite queue, and we have not tackled the more generic problem of putting SimQueues is tandem:

- What if any of the subqueues *drops* the job?
- How to revoke a jobs from a composite queue?
- How to obtain statistics on the composite queue?

In other words, what we really want is an implementation of a SimQueue that behaves as the concatenation of visits to its subqueues. In Listing 8.4 we show this approach using a BlackTandemSimQueue described in this chapter, with its output in 8.5.

Listing 8.4: A tandem queue consisting of two P_LCFS queues (using BlackTandem-SimQueue).

```
public static void main (final String[] args)
{
    final SimEventList el = new DefaultSimEventList ();
    el.reset (0);
    final P.LCFS lcfs.1 = new P.LCFS (el, null);
    lcfs.1.setName ("Q1");
    final P.LCFS lcfs.2 = new P.LCFS (el, null);
    lcfs.2.setName ("Q2");
    final Set<SimQueue> subQueues = new LinkedHashSet ();
    subQueues.add (lcfs.1);
    subQueues.add (lcfs.2);
    final BlackTandemSimQueue compositeQueue = new BlackTandemSimQueue (el, subQueues, null);
    for (int j = 1; j <= 5; j++)
    {
        final SimJob job = new DefaultSimJob (el, "J" + j, 10 * j);
        compositeQueue.scheduleJobArrival (j, job);
        job.registerSimEntityListener (new StdOutSimEntityListener ());
    }
    el.run ();
}</pre>
```

Listing 8.5: Output of the program in Listing 8.4.

```
\overline{\texttt{StdOut}} \\ \texttt{SimEntityListener} \quad t = 1.0 \,, \quad \texttt{queue=Tandem} \, [\, Q1 \,, Q2 \,] \, :
                                                                                  ARRIVAL of job J1
StdOutSimEntityListener t=1.0, queue=Tandem [Q1,Q2] StdOutSimEntityListener t=2.0, queue=Tandem [Q1,Q2]
                                                                                 START of job J1.
ARRIVAL of job J2
\label{eq:stdoutSimEntityListener} \begin{array}{lll} StdOutSimEntityListener & t=2.0, & queue=Tandem & [Q1,Q2] \\ StdOutSimEntityListener & t=3.0, & queue=Tandem & [Q1,Q2] \\ StdOutSimEntityListener & t=3.0, & queue=Tandem & [Q1,Q2] \\ \end{array}
                                                                                 START of job J2.
ARRIVAL of job J3.
                                                                                  START of job J3
StdOutSimEntityListener t=4.0, queue=Tandem[Q1,Q2] StdOutSimEntityListener t=4.0, queue=Tandem[Q1,Q2]
                                                                                  ARRIVAL of job J4.
                                                                                  START of job J4.
StdOutSimEntityListener t=5.0, queue=Tandem [Q1,Q2]
                                                                                  ARRIVAL of
{\tt StdOutSimEntityListener} \ \ t=5.0 \,, \ \ {\tt queue=Tandem} \, [\, {\tt Q1} \,, {\tt Q2} \,]
                                                                                  START of job J5.
DEPARTURE of job
                                                                                    DEPARTURE of job
                                                                                    DEPARTURE of job J3.
DEPARTURE of job J4.
StdOutSimEntityListener\ t=205.0, queue=Tandem[Q1,Q2]: DEPARTURE of job J5
```

The latter example shows exactly what we want: The creation of a new SimQueue that behaves exactly like a tandem configuration of two other queues. Admittedly, the code in the example is not particularly smaller than that of the previous examples, and the latter examples can certainly be used as a starting point for the study of tandem (and other composite) queues. However, if, for instance, you want to create a new SimQueue type that is the equivalent of other queues that are somehow interconnected, or if you want to study nested composite queues, then constructing a composite queue is a much faster (and more reliable) approach.

The extensive support for composite queues is one of the most distinguishing features of jqueues. Next to tandem queues, there is support for various types of feedback queues, encapsulated queues and parallel queues. In the next chapter we describe these composite queues in detail. In the remainder of the present chapter, we introduce some important concepts that apply to any composite queue.

8.2 The SimQueueComposite Interface

In the jqueues implementation, composite queues implement the SimQueueComposite interface, which, in turn, inherits from SimQueue.

8.2.1 The 'Queues' Property

The value of the 'Queues' property of a SimQueueComposite is a Set holding the subqueues of the composite queue. The property can only be set upon construction of the composite queue; and cannot be changed thereafter, but the subqueues can be accessed through getQueues (). (Note that the Set returned should not be modified.) Since the order of the subqueues is important to most composite-queue types, the implementation of getQueues () must maintain a deterministic ordering of the subqueues.

8.2.2 The 'StartModel' Property

8.3 Tandem Queues

8.3.1 The Tandem SimQueue

In tandem queues, visiting jobs must visit each subqueue one in a predetermined (and fixed) sequence. The list of (distinct) subqueues is passed upon construction, and cannot be changed afterwards.

	Tandem		
Description	Serves jobs by letting their delegate jobs visit		
	the sequence of subqueues \mathcal{Q} exactly once.		
State			
QAV	Drops arriving jobs during QAVs.		
NoWaitArmed	Always true.		
Waiting Area	Infinite waiting area, FIFO discipine.		
SAC	The remaining number of arriving jobs that can have a delegate job		
	arrive at the tandem queue.		
	If zero, arriving jobs wait in the waiting area.		
	Integer.MAX_VALUE is treated as $+\infty$.		
Service Area	Holds the jobs whose delegate job have arrived anywhere.		
State Operations			
Set QAV	Ends/starts a QAV.		
Arrival	The queue accepts arrivals.		
Drop	Drops arriving jobs during QAVs.		
	Drops a visiting job if its delegate job is dropped on any subqueue.		
Revocation	Jobs can be revoked while waiting and while being served.		
Set SAC	Set SAC Sets/overwrites SAC; Integer.MAX_VALUE == $+\infty$.		
	Starts waiting jobs if $SAC > 0$.		
Start	Starts a job if its delegate job arrives anywhere.		
Departure	Jobs depart if its delegate job departs from the last subqueue.		
State Invariants			
$ J(t) = J_w(t) + \sum_{q \in \mathcal{Q}} J_q(t) .$			
Properties			
EventList	The event list; non-null; RO.		
Name	The name, default "LJF"; non-null; RW.		
Queues	The set (and list) of subqueues Q ; ordered; RO.		

8.3.2 The CTandem2 SimQueue

8.4 Parallel Queues

- 8.4.1 The JSQ SimQueue
- 8.4.2 The JRQ SimQueue
- 8.4.3 The Pattern SimQueue
- 8.4.4 The Parallel SimQueue

8.5 Feedback Queues

- 8.5.1 The FB_v SimQueue
- 8.5.2 The FB_p SimQueue
- 8.5.3 The FB SimQueue

8.6 Jackson Queues

8.6.1 The Jackson SimQueue

8.7 Encapsulator Queues

An encapsulator queue has exactly one subqueue.

- 8.7.1 The Enc SimQueue
- 8.7.2 The EncHS SimQueue
- 8.7.3 The EncTL SimQueue
- 8.7.4 The EncJL SimQueue
- 8.7.5 The EncXM SimQueue
- 8.8 Special Composite Queues
- 8.8.1 The Drop-Collector Queue
- 8.9 Generic Composite Queues
- 8.9.1 The Comp SimQueue

Queue and Job Statistics

9.1 Introduction

If you have read this book linearly up to this point, we hope you are wondering by now how to compute statistics like average job sojourn time at a queue, or average server utilization (just to name a few). Actually, this is somewhat on purpose: None of the interfaces and concrete implementations of jobs and queues provide direct support for maintaining and calculating statistics. This has three important reasons:

- It relieves the concrete SimQueue and SimJob implementations of the tedious and error-prone responsability of maintaining and calculting statistics; their basis functionality in terms of e.g. implementing the proper queueing discipline is complicated enough as it is.
- It forces the implementation of statistics in a generic way, e.g., applicable to any queue type.
- It allows for easy replacement of *all* statistics-gathering and maintenance code with that of a professional third-party statistics package like **XXX**.

Needless to say, jqueues has full support for the implementation of statistics, and actually, provides a few basic, but highly effective and extensible classes for statistics gathering itself. The starting point for gathering statistics of a SimEntity is to register as a suitable SimEntityListener to it, and update statistics upon notifications from the entity, inparticular update notifications and visit-related notifications like arrivals, drops and departures. Recall that a SimEntity is required to notify registered listeners just before it state changes through an update notification, allowing for easy maintenance of "time-average-type" statistics like the average number

of jobs present at a queue. In addition (and often requiring a bit more work) the visit-related notifications allow for maintenance of "visit-related" statistics, like the average job sojourn time at a queue.

In the following section, we will first explain how to obtain statistics for a SimQueue or SimJob manually, following the approach outline above. Subsequently, we will introduce a few statistics-related class that intend to make it easier to obtain such statistics.

9.1.1 Example: The Average Number of Jobs at a Queue

In this statistics-related example, we create a SimQueue and a workload consisting of arriving SimJobs. Our objective is to run the simulation, and calculate the average number of jobs at the queue. To make the example more interesting, we create two queues, a FCFS queue and a Preemptive (Resume) LCFS queue. We equip each with a listener that maintains the number of jobs at the queue over time. As shown in Listing 9.1 below, we use a DefaultSimEntityListener as base classs, making it easier to ignore all the notifications we are not interested in. Note that we are silently assuming that the listener is registered at a SimQueue, and not at some other SimEntity type. In addition, we left out some sanity checking, e.g., on the time parameter (should not be in the past).

Listing 9.1: Simple listener for maintaining and calculating the average number of jobs at a SimQueue.

```
private final static class AvgJStatListener
extends DefaultSimEntityListener
{
    public AvgJStatListener (SimQueue queue)
    {
        notifyResetEntity (queue);
        queue.registerSimEntityListener (this);
    }

    private double tStart = Double.NEGATIVE_INFINITY;
    private double tLast = Double.NEGATIVE_INFINITY;
    private double cumJ = 0;

    @Override
    public void notifyResetEntity (SimEntity entity)
    {
        tStart = entity.getEventList ().getTime ();
        tLast = tStart;
        cumJ = 0;
    }

    @Override
    public void notifyUpdate (double time, SimEntity entity)
    {
        cumJ += ((SimQueue) entity).getNumberOfJobs () * (time - tLast);
        tLast = time;
    }

    public final double getStartTime ()
    {
        return this.tStart;
    }
}
```

```
public final double getEndTime ()
{
   return this.tLast;
}

public final double calculate ()
{
   if (tLast > tStart)
   {
      if (! Double.isInfinite (tLast - tStart))
        return cumJ / (tLast - tStart);
      else
        return 0;
   }
  else
   return 0;
}
```

Note that we are only interested in two notifications from the SimQueue, reset and update notifications. Because the number of jobs at a SimQueue is a simple function, we can easily integrate it over time by considering all points in time at which the function value can change, and cumulating the product of the interval since the last update with the current value. By definition, such points in time are the updates of a SimQueue and the constract of the latter mandates that each update results in a notification at its listeners before any changes have been applied to the queue. Needless to say, this requires substantial discipline for implementations of SimQueue, but we use it here to our advantage. In the end, all we need to do it divide the cumulated value with the total time interval, taking special care of the possibility that the interval is $+\infty$.

For the start of the interval, we use the reset notification from the queue. At each reset, we take the start time from the current time of the event list (note that we cannot take the time from the SimQueue directly), and reset our internal statistics. Note that we call notifyResetEntity directly from the constructor as well, because we cannot rely on receiving a reset between construction of the object and starting the simulation. Also note that we may assume that the number of jobs at a reset, as well as upon construction of a SimQueue is zero, conform the contract of a SimQueue. However, unless the event list or the SimQueue attached to it is reset to a finite time value, we must use Double.NEGATIVE_INFINITY as time value. This explains the default values used in AvgJStatListener.

We list the example program using the AvgJStatListener and its output in Listings 9.2 and 9.3 below. Note the very important el.reset (0) line in the main program. We will later show the effect of leaving out or forgetting this statement. The correctness of the calculated values in the output can be assessed easily as is shown in the comments of the main program. For P_LCFS, the program outputs one of two distinct values for the average, both of which are actually correct, due to

an ambiguity in the event scheduling. (Which we, in all honesty, overlooked while constructing the example.) This is also explained in the comments of the program.

Listing 9.2: Example program for calculating the average number of jobs at two queues.

```
public static void main (final String[] args)
  final SimEventList el = new DefaultSimEventList ();
     reset (0);
'Schedule 5 jobs, 0 through 4 at t = 0, 1, 2, 3, 4
      and service times 0, 1, 2, 3, 4, respectively.
      Departure times with FCFS: 0, 2, 4, 7, 11.
      WITH P_LCFS: AMBIGUITY!
      Departure\ times\ with\ P\_LCFS\ [2\ arrives\ after\ departure\ of\ 1]:\ 0,\ 2,\ 8,\ 10,\ 11.
      cumJ = 0 + 1 + 1 + 2 + 3 + 3 + 3 + 3 + 2 + 2 + 1 = 21 avgJ = 21 \ / \ 11 = 1.9090.
      Departure times with P_LCFS [2 arrives before departure of 1]: 0, 8, 10, 11, 11. cumJ = 0 + 1 + 2 + 3 + 4 + 4 + 4 + 4 + 3 + 3 + 2 = 30. avgJ = 30 / 11 = 2.7272.
  final FCFS fcfs = new FCFS (el);
  final P_LCFS lcfs = new P_LCFS (el, null);
  for (int j = 0; j \le 4; j++)
     e:.run ();
System.out.println ("FCFS:");
System.out.println ("__Start_time:_" + avgJStatListener_fcfs.getStartTime () + ".");
System.out.println ("__End_Time__:_" + avgJStatListener_fcfs.getEndTime () + ".");
System.out.println ("_Average_number_of_jobs:_" + avgJStatListener_fcfs.calculate () + ".");
System.out.println ("PLCFS:");
System.out.println ("PLCFS:");
   el.run ();
  System.out.println ("__Start_time:_" + avgJStatListener_lcfs.getStartTime () + ".");
System.out.println ("__End_Time__:_" + avgJStatListener_lcfs.getEndTime () + ".");
System.out.println ("__Average_number_of_jobs:_" + avgJStatListener_lcfs.calculate () + ".");
```

Listing 9.3: Output from the example program in Listing 9.2.

```
FCFS:
    Start time: 0.0.
    End Time : 11.0.
    Average number of jobs: 1.27272727272727.

P.LCFS:
    Start time: 0.0.
    End Time : 11.0.
    Average number of jobs: 1.909090909090909 [OR 2.7272727272727, see comments].
```

As mentioned earlier, it is essential to reset the event list to a finite time value before use. Below in Listing 9.4 we show the output of the program if we leave out the el.reset (0) statement, essentially starting the simulation and, more importantly, gathering the statistics at $t = -\infty$. The result is zero, because we are taking the average value of a function over an infinite interval, knowing that is is only non-zero over a finite interval. Despite that fact that for this particular case, we seem to get away with the infinite interval, and are able to return a sensible value for the

average, this does not hold for the general case. (For instance, suppose we would have scheduled an arrival at $t = -\infty$, the program would still return the incorrect zero value for the average.) As a rule of thumb, the use of statistics involving infinite values should be avoided at all times, again stressing the importance of resetting the event list to a finite value before its use.

Listing 9.4: Output from the example program in Listing 9.2 without resetting the event list to zero (i.e., starting at $t = -\infty$).

```
FCFS:
Start time: -Infinity.
End Time : 11.0.
Average number of jobs: 0.0.
P.LCFS:
Start time: -Infinity.
End Time : 11.0.
Average number of jobs: 0.0.
```

9.1.2 Example: The Total Sojourn of a Job at Visited Queues

9.2 The AbstractSimQueueStat Base Class

The examples in the previous sections explained how to obtain statistics on SimQueues and SimJobs. The next sections in this chapter introduce a few classes that either directly provide a few of the most basic statistics or allow you to define your own statistics more easily.

The AbstractSimQueueStat is the (abstract) base class for all subsequent classes. Its functionality is comparable to AvgJStatListener introduced in Section 9.1.1, with a few new functions and increased robustness, and delegating the actual maintenance and calulation of the statistic(s) to only a few abstract methods. To illustrate its use, we show in Listings 9.5 and 9.6 the modified listener and main program, respectively, from the example in Section 9.1.1 now using AbstractSimQueueStat.

Listing 9.5: Using AbstractSimQueueStat for a listener for maintaining and calculating the average number of jobs at a SimQueue.

```
private static class AvgJStatListener
extends AbstractSimQueueStat
{
    public AvgJStatListener (SimQueue queue)
    {
        super (queue);
    }
    private double cumJ = 0;
    private double avgJ = 0;
    @Override
    protected void resetStatistics ()
{
```

```
cumJ = 0;
    avgJ = 0;
}

@Override
protected void updateStatistics (double time, double dt)
{
    cumJ += getQueue ().getNumberOfJobs () * dt;
}

@Override
protected void calculateStatistics (double startTime, double endTime)
{
    if (startTime == endTime)
        return;
    if (! Double.isInfinite (endTime - startTime))
        avgJ = cumJ / (endTime - startTime);
    else
        avgJ = 0;
}

public double getAvgJ ()
{
    calculate ();
    return this.avgJ;
}
```

Listing 9.6: Example program for calculating the average number of jobs at two queues using AbstractSimQueueStat.

Compared to the manual approach in Section 9.1.1, we highlight the following

differences:

- In the listener, we only have to implement what to do upon a reset (resetStatistics) and upon an update (updateStatistics), and how to calculate the (internally stored) result (calculateStatistics); the base class takes care of registering at SimQueue and internally storing the times of the last reset (or the time at construction) and of the last update.
- In the concrete listener, we provide a method for access to the internally stored result, but that method automatically invokes the base class' calculate () method first. The base class attempts to avoid unnecessary recalculations of the result in its subclass.
- Users of the concrete subclass have access to the methods getStartTime and getLastUpdateTime at all times. Upon calculation (without a time argument), the time of the last update determines the upper boundary of the measurement interval.
- Users may also invoke calculate (double endTime) which allows the extension of the measurement interval beyond the last update time. This, however, prevents subsequent update before the endTime provided, unless the object (or the queue, or the underlying event list) is reset. Nonetheless, the feature is handy because in many practical cases, one wants to take the time average over a fixed time interval, instead of a time interval of which the upper boundary is determined by the last update. Unfortunately, one cannot chose and endTime smaller than the last update time (at the expense of an exception thrown).
- Users can change the SimQueue from which the statistics are obtained through setQueue (Q). Setting the queue will immediately reset the statistics object. As expected, the base class AbstractSimQueueStat takes care of registering at the new queue (if any) after unregistering at the old queue. The only sensible use for that feature that we can think of is delayed initialization.

9.3 The SimpleSimQueueStat Class

The SimpleSimQueueStat class implements AbstractSimQueueStat described in Section 9.2 for some important statistics on a SimQueue:

• The average number of jobs;

- The average number of jobs in the service area;
- The maximum and minimum number of jobs;
- The maximum and minimum number of jobs in the service area.

Attaching a SimpleSimQueueStat to a SimQueue is a very conventient way of obtaining a first impression of the performance of the queue; we have used it a lot ourselves during testing. Below in Listing 9.7 we illustrate its use for the example in Section 9.1.1; the output (still ambiguous!) is shown in Listing 9.8. Note that the number of updates is also available from SimpleSimQueueStat, which is very handy for detailed update-related debugging on SimQueue implementations.

Listing 9.7: Example program for obtaing basic statistics using SimpleSimQueueStat.

```
public static void main (final String[] args)
    final SimEventList el = new DefaultSimEventList ();
    el.reset (0);

// Schedule 5 jobs, 0 through 4 at t = 0, 1, 2, 3, 4
          and service times 0, 1, 2, 3, 4, respectively.
          WITH P_LCFS: AMBIGUITY!
          Departure times with P_LCFS [2 arrives after departure of 1]: 0, 2, 8, 10, 11.
         Departure times with P_LCFS [2 arrives before departure of 1]: 0, 8, 10, 11, 11. 
 cumJ = 0 + 1 + 2 + 3 + 4 + 4 + 4 + 4 + 4 + 3 + 3 + 2 = 30. 
 avgJ = 30 / 11 = 2.7272.
    final FCFS fcfs = new FCFS (el);
    final P.LCFS lcfs = new P.LCFS (el, null);
for (int j = 0; j <= 4; j++)
        final SimpleSimQueueStat avgJStatListener_fcfs = new SimpleSimQueueStat (fcfs);
final SimpleSimQueueStat avgJStatListener_lcfs = new SimpleSimQueueStat (lcfs);
    el.run ();
    System.out.println ("FCFS:");
   System.out.println ("L-Start_time:_" + avgJStatListener_fcfs.getStartTime () + ".");
System.out.println ("L-End_Time_L:_" + avgJStatListener_fcfs.getLastUpdateTime () + ".");
System.out.println ("L-Number_of_updates____:_"
+ avgJStatListener_fcfs.getNumberOfUpdates () + ".");
  + avgJStatListener_fcfs.getNumberOfUpdates () + ".");
System.out.println ("__Average_number_of_jobs______"
+ avgJStatListener_fcfs.getAvgNrOfJobs () + ".");
System.out.println ("__Average_number_of_jobs__in_service_area:_"
+ avgJStatListener_fcfs.getAvgNrOfJobsInServiceArea () + ".");
System.out.println ("__Maximum_number_of_jobs______"
+ avgJStatListener_fcfs.getMaxNrOfJobs () + ".");
System.out.println ("P_LCFS:");
System.out.println ("__Start_time:_" + avgJStatListener_lcfs.getStartTime () + ".");
System.out.println ("__End_Time__:_" + avgJStatListener_lcfs.getLastUpdateTime () + ".");
System.out.println ("__Number_of_updates_____:"
+ avgJStatListener_fcfs.getNumberOfUpdates () + ".");
System.out.println ("__Average_number_of_jobs_____:"
   System.out.println ("_Average_number_of_jobs______"");
+ avgJStatListener_lcfs.getAvgNrOfJobs () + ".");
System.out.println ("_Average_number_of_jobs_in_service_area:_"
+ avgJStatListener_lcfs.getAvgNrOfJobsInServiceArea ()+ ".");
System.out.println ("_Maximum_number_of_jobs_____"");
+ avgJStatListener_lcfs.getMaxNrOfJobs () + ".");
```

Listing 9.8: Output from the example program in Listing 9.7.

Note the remarkable difference in the average number of jobs in the service area between FCFS and P_LCFS. In the former, jobs waiting are only admitted to the service area if the previously arrived job has departed, whereas in the latter, jobs are admitted immediately to the service area upon arrival (because their service starts immediately), and preempted jobs are *not* transferred back into the waiting area. This illustrates the (surprising) distinction between the number of jobs *in service* (a concept not directly supported by SimQueue) and the number of jobs *in the service area* (in which service is allowed, but not guaranteed).

9.4 The AutoSimQueueStat Class

9.4.1 Introduction

The SimpleSimQueueStat class described in Section 9.3 provides a convenient way of obtaining some important statistics related to the number of jobs at a queue or at its service area. Although it is fairly easy to extend SimpleSimQueueStat, or even AbstractSimQueueStat for that matter, for other time-dependent performance measures, we quickly realize that the resulting code would only differ in which statistic we take from the queue upon updates. The AutoSimQueueStat class introduced in this section honors this observation, and relies on a so-called SimQueueProbe to obtain the momentary value of a specific performance measure at a SimQueue. It then automatically maintains the average, maximum and minimum values for all registered probes.

9.4.2 The SimQueueProbe Interface

As described in the previous section, the SimQueueProbe interface features obtaining the momentary value of a specific performance measure at a queue (the queue is actually a parameter, so probes can be reused). Its interface definition is shown in Listing 9.9. Note that only double values (or values that can be cast to double) are supported.

Listing 9.9: The SimQueueProbe interface.

```
public interface SimQueueProbe<Q extends SimQueue>
{
   public double get (Q queue);
}
```

9.4.3 The AutoSimQueueStatEntry Class

The AutoSimQueueStatEntry class connects a SimQueueProbe with a name, and adds statistics maintenance for the values the probe provides. Unfortunately, unlike a SimQueueProbe, you cannot reuse a AutoSimQueueStatEntry among different queues.

9.4.4 Example

Below in Listing 9.10 we illustrate the use of AutoSimQueueStat for the example in Section 9.1.1; the output (still ambiguous!) is shown in Listing 9.11. Note that two probes are created, one for the number of jobs at a queue, and one for the number of jobs in the service area at a queue. For each queue, FCFS and P_LCFS, an array of entries is created, holding unique entries for the statistics required. Finally, note that AutoSimQueueStat features a method report () (optionally, with an integer indentation parameter) for quickly reporting the calculated statistics for all registered probes.

Listing 9.10: Example program for obtaing statistics using AutoSimQueueStat.

```
for (int j = 0; j <= 4; j++)
{
    fcfs.scheduleJobArrival (j, new DefaultSimJob (el, "JobF_" + j, j));
    lcfs.scheduleJobArrival (j, new DefaultSimJob (el, "JobL_" + j, j));
}
final SimQueueProbe probeJ =
    (SimQueueProbe) (SimQueue queue) -> queue.getNumberOfJobs ();
final SimQueueProbe probeJX =
    (SimQueueProbe) (SimQueue queue) -> queue.getNumberOfJobsInServiceArea ();
final List<AutoSimQueueStatEntry> entries_fcfs = new ArrayList >> ();
final List<AutoSimQueueStatEntry> entries_lcfs = new ArrayList >> ();
entries_fcfs.add (new AutoSimQueueStatEntry ("J", probeJ));
entries_fcfs.add (new AutoSimQueueStatEntry ("JX", probeJX));
entries_lcfs.add (new AutoSimQueueStatEntry ("J", probeJX));
entries_lcfs.add (new AutoSimQueueStatEntry ("JX", probeJX));
final AutoSimQueueStat stat_fcfs = new AutoSimQueueStat (fcfs, entries_fcfs);
final AutoSimQueueStat stat_lcfs = new AutoSimQueueStat (lcfs, entries_lcfs);
el.run ();
System.out.println ("FCFS:");
stat_fcfs.report (2);
System.out.println ("PLCFS:");
stat_lcfs.report (2);
System.out.println ("PLCFS:");
stat_lcfs.report (2);
```

Listing 9.11: Output from the example program in Listing 9.7.

9.5 The SimpleSimQueueVisitsStat Class

The SimpleSimQueueVisitsStat maintains and calculates some important visits-related statistics on the queue it is registered at:

- The number of arrivals, of jobs that started and the number of departures;
- The number of dropped and (successfully) revoked jobs;
- The average waiting time (averaged over jobs that started);
- The average sojourn time (averaged over jobs that departed);
- The maximum and minimum waiting time (averaged over jobs that started);
- The maximum and minimum sojourn time (averaged over jobs that departed).

In Listing 9.12 below we provide an example of its use, again using the scheduling example from YYY; its corresponding output is shown in Listing 9.13.

Listing 9.12: Example program for obtaing basic statistics using SimpleSimQueue-VisitsStat.

```
public static void main (final String[] args)
   final SimEventList el = new DefaultSimEventList ();
   el. reset (0);

// Schedule 5 jobs, 0 through 4 at t = 0, 1, 2, 3, 4
         and service times 0, 1, 2, 3, 4, respectively.
        WITH P_LCFS: AMBIGUITY!
        Departure times with P-LCFS [2 arrives after departure of 1]: 0, 2, 8, 10, 11.   
    cumJ = 0 + 1 + 1 + 2 + 3 + 3 + 3 + 3 + 2 + 2 + 1 = 21.   
    avgJ = 21 / 11 = 1.9090.   
    avgWaitJ = 0.   
    avgSojJ = 0 + 1 + 9 + 7 + 4 / 5 = 21 / 5 = 4.2.
         Departure times with P_LCFS [2 arrives before departure of 1]: 0, 8, 10, 11, 11.
        Departure times with P-LCFS [2 arrives before departure cum J = 0 + 1 + 2 + 3 + 4 + 4 + 4 + 4 + 4 + 3 + 3 + 2 = 30. avg J = 30 / 11 = 2.7272. avg Wait J = 0. avg Soj J = 0 + 10 + 9 + 7 + 4 / 5 = 30 / 5 = 6.0.
    final FCFS fcfs = new FCFS (el);
   final PLCFS lcfs = new PLCFS (el, null);
for (int j = 0; j <= 4; j++)
       final SimpleSimQueueVisitsStat visitsStatListener_fcfs = new SimpleSimQueueVisitsStat (fcfs); final SimpleSimQueueVisitsStat visitsStatListener_lcfs = new SimpleSimQueueVisitsStat (lcfs);
    el.run ();
   System.out.println ("FCFS:");
System.out.println ("__Start_Time__
          visitsStatListener_fcfs.getStartTime ()
                                                                                                               + ".");
   + visitsStatListener_fcfs.getStattTime ()
System.out.println ("__End_Time___:_"
+ visitsStatListener_fcfs.getLastUpdateTime ()
System.out.println ("__Number_of_Arrivals___:_"
+ visitsStatListener_fcfs.getNumberOfArrivals ()
System.out.println ("_Number_of_Started_Lisbs."
                                                                                                               + ".");
                                                                                                               + ".");
   System.out.println ("__Number_of_Started_Jobs:_
            visitsStatListener_fcfs.getNumberOfStartedJobs () + ".");
   + VisitsStatListener_fcis.getNumberOfStatecasous () + . ,,
System.out.println ("__Number_of_Departures__:_"
+ visitsStatListener_fcfs.getNumberOfDepartures () + ".");
System.out.println ("__Minimum_Waiting_Time__:_"
+ visitsStatListener_fcfs.getMinWaitingTime () + ".");
System.out.println ("__Maximum_Waiting_Time__:_"
+ ":"itsStatListener_fcfs.getMaxWaitingTime () + ".");
   + visitsStatListener_fcfs.getMaxWaitingTime ()
System.out.println ("__Average_Waiting_Time__:_"
+ visitsStatListener_fcfs.getAvgWaitingTime ()
                                                                                                              + ".");
                                                                                                              + ".");
   + visitsStatListener_icis.gethig.urn_Time__:_"

System.out.println ("__Minimum_Sojourn_Time__:_"

+ visitsStatListener_fcfs.getMinSojournTime ()
                                                                                                              + ".");
   System.out.println ("__Maximum_Sojourn_Time__:.
   + visitsStatListener.fcfs.getMaxSojournTime ()
System.out.println ("__Average_Sojourn_Time__:_"
+ visitsStatListener.fcfs.getAvgSojournTime ()
System.out.println ("P_LCFS:");
System.out.println ("__Start_Time___:_"
                                                                                                              + ".");
                                                                                                               + ".");
   + visitsStatListener_lcfs.getLastUpdateTime ()

+ visitsStatListener_lcfs.getLastUpdateTime ()
                                                                                                               + ".");
                                                                                                               + ".");
   System.out.println ("__Number_of_Arrivals____:_"
+ visitsStatListener_lcfs.getNumberOfArrivals ()
                                                                                                              + ".");
   System.out.println ("__Number_of_Started_Jobs:_" + visitsStatListener_lcfs.getNumberOfStartedJobs () + ".");
System.out.println ("__Number_of_Departures__:_"
```

Listing 9.13: Output from the example program in Listing 9.12.

```
FCFS:
    Start Time
   End Time
   Number of Arrivals :
Number of Started Jobs:
   Number of Departures
Minimum Waiting Time
Maximum Waiting Time
                                             0.0.
                                             3.0.
    Average Waiting
                               Time
                                             0.8.
   Minimum Sojourn Time
Maximum Sojourn Time
                                          : 0.0.
: 7.0.
Average Sojourn Time P_LCFS:
    Start Time
   Start Time :
End Time :
Number of Arrivals :
Number of Started Jobs:
Number of Departures :
Minimum Waiting Time :
                                          : 11.0.
                                             5.0.0.
   Maximum Waiting Time
                                             0.0.
   Average Waiting Time
Minimum Sojourn Time
                                             0.0. \\ 0.0.
   Maximum Sojourn
                               _{\mathrm{Time}}
                                                       [OR 10.0, see comments].
   Average Sojourn
                               Time
                                                      OR 6.0, see comments
```

9.6 Conclusions

Visualization

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Standardized Workload Patterns

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Conclusions