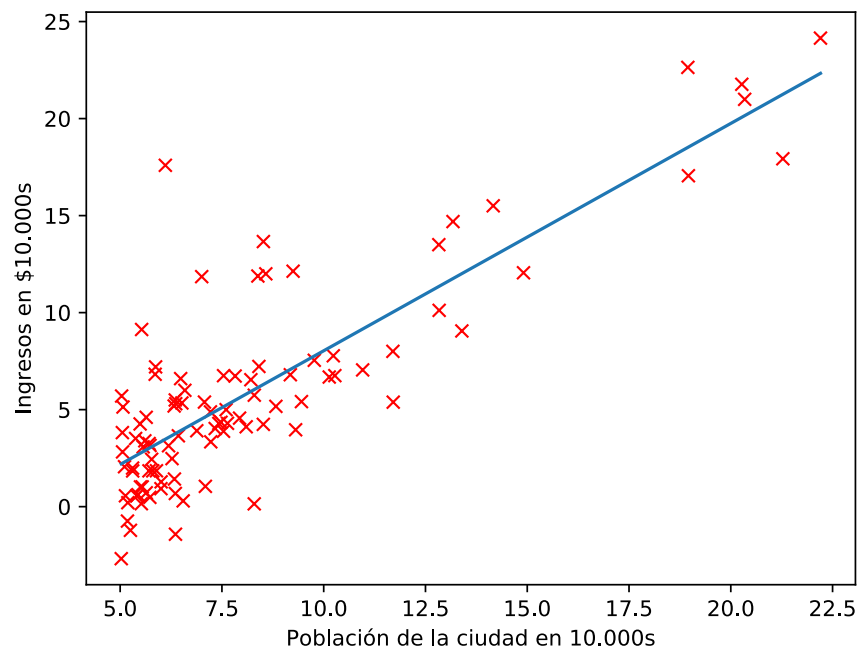
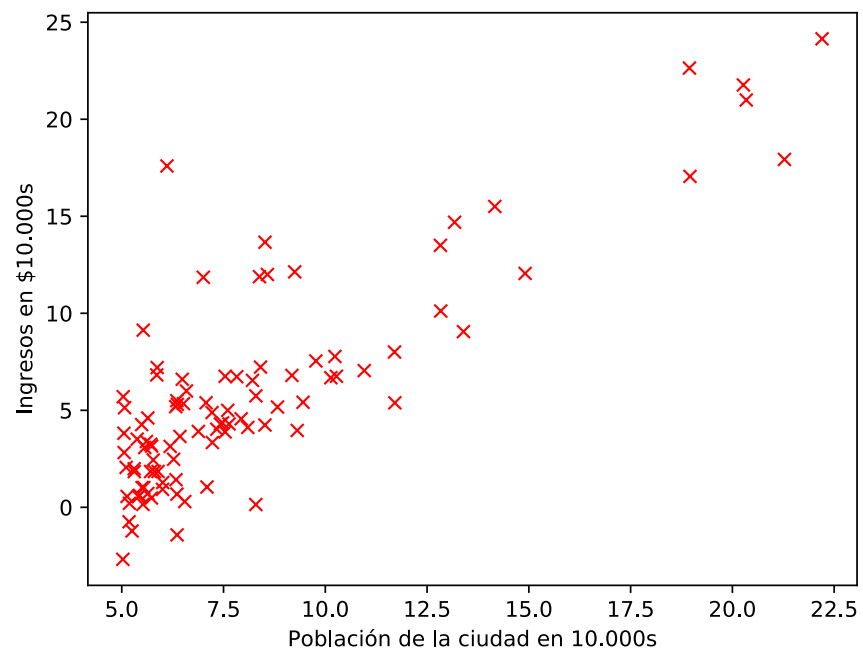


Práctica 1:

regresión lineal



```

import numpy as np
from pandas.io.parsers import read_csv

def carga_csv(file_name):
    """carga el fichero csv especificado y lo
       devuelve en un array de numpy
    """
    valores = read_csv(file_name, header=None).to_numpy()
    # suponemos que siempre trabajaremos con float
    return valores.astype(float)

```

```

array([[ 6.1101 , 17.592  ],
       [ 5.5277 ,  9.1302 ],
       [ 8.5186 , 13.662  ],
       [ 7.0032 , 11.854  ],
       ...,
       [ 5.3054 ,  1.9869 ],
       [ 8.2934 ,  0.14454],
       [13.394  ,  9.0551 ],
       [ 5.4369 ,  0.61705]])

```

Práctica 1: regresión lineal

solución de la primera parte

repeat until convergence {

$$\left. \begin{aligned} \theta_0 &:= \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) \\ \theta_1 &:= \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) \cdot x^{(i)} \end{aligned} \right\} \begin{array}{l} \text{update} \\ \theta_0 \text{ and } \theta_1 \\ \text{simultaneously} \end{array}$$

}

```
datos = carga_csv('ex1data1.csv')
```

```
X = datos[:, 0]
```

```
Y = datos[:, 1]
```

```
m = len(X)
```

```
alpha = 0.01
```

```
theta_0 = theta_1 = 0
```

```
for _ in range(1500):
```

```
    sum_0 = sum_1 = 0
```

```
    for i in range(m):
```

```
        sum_0 += (theta_0 + theta_1 * X[i]) - Y[i]
```

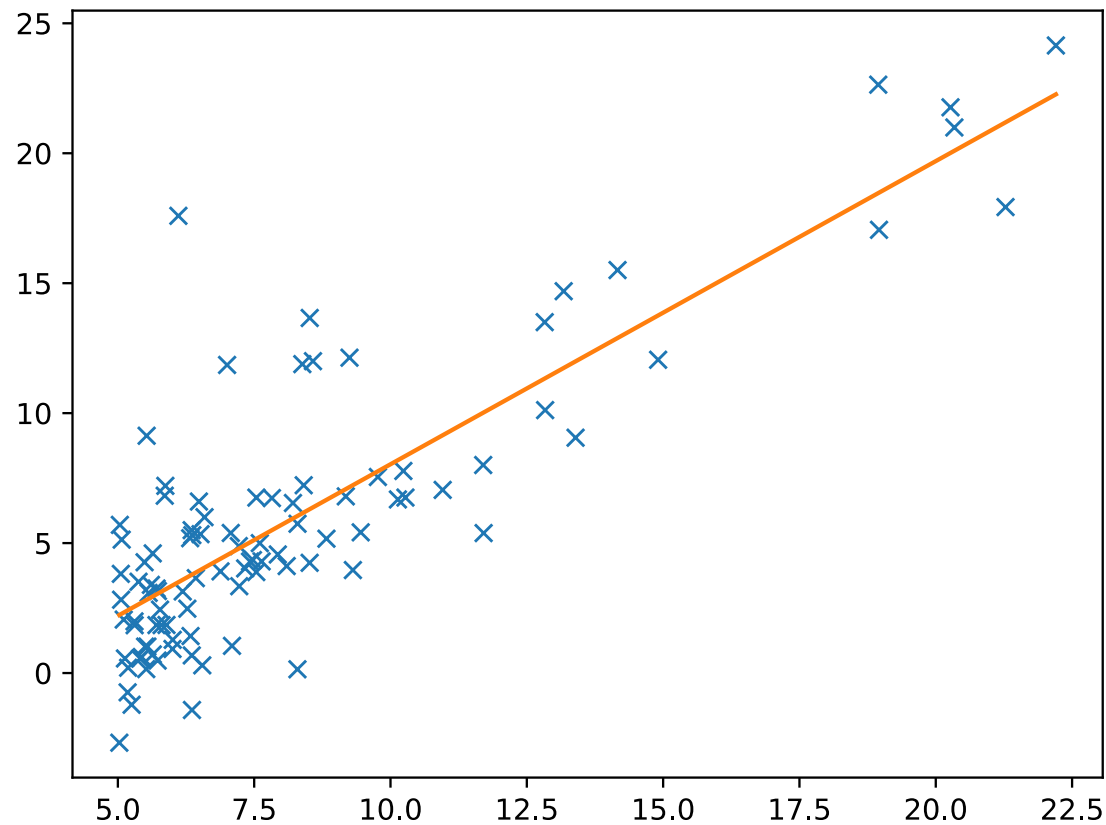
```
        sum_1 += ((theta_0 + theta_1 * X[i]) - Y[i]) * X[i]
```

```
    theta_0 = theta_0 - (alpha / m) * sum_0
```

```
    theta_1 = theta_1 - (alpha / m) * sum_1
```

```
array([[ 6.1101 , 17.592  ],
       [ 5.5277 ,  9.1302 ],
       [ 8.5186 , 13.662  ],
       [ 7.0032 , 11.854  ],
       ...,
       [ 5.3054 ,  1.9869 ],
       [ 8.2934 ,  0.14454],
       [13.394  ,  9.0551 ],
       [ 5.4369 ,  0.61705]])
```

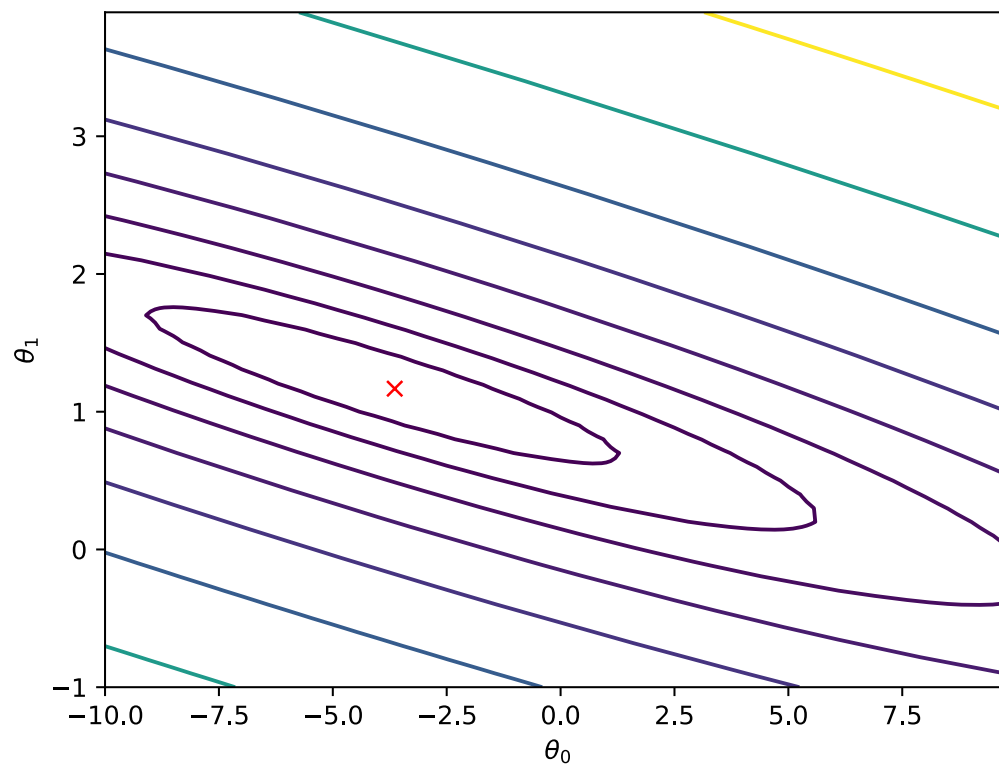
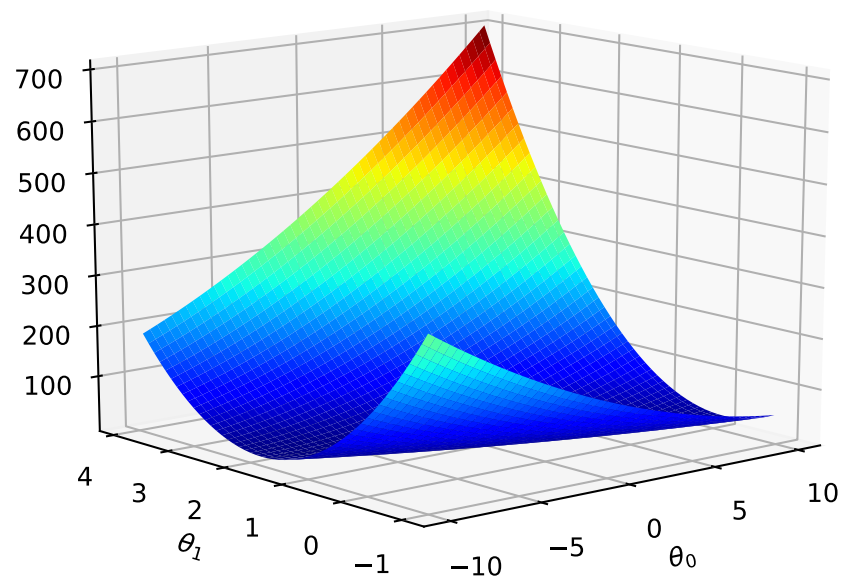
```
plt.plot(X, Y, "x")  
min_x = min(X)  
max_x = max(X)  
min_y = theta_0 + theta_1 * min_x  
max_y = theta_0 + theta_1 * max_x  
plt.plot([min_x, max_x], [min_y, max_y])  
plt.savefig("resultado.pdf")
```



Práctica 1:

regresión lineal

gráficas en 3D




```
import numpy as np
```

```
In [3]: x = np.array([1,2,3])
```

```
In [4]: y = np.array([4,5,6])
```

```
In [5]: xx, yy = np.meshgrid(x,y)
```

```
In [6]: xx
```

```
Out[6]:
```

```
array([[1, 2, 3],  
       [1, 2, 3],  
       [1, 2, 3]])
```

```
In [7]: yy
```

```
Out[7]:
```

```
array([[4, 4, 4],  
       [5, 5, 5],  
       [6, 6, 6]])
```

```
from mpl_toolkits.mplot3d import Axes3D
import matplotlib.pyplot as plt
from matplotlib import cm
from matplotlib.ticker import LinearLocator, FormatStrFormatter
import numpy as np
```

```
fig = plt.figure()
ax = fig.gca(projection='3d')    # ax = Axes3D(fig)
```

```
# Make data.
```

```
X = np.arange(-5, 5, 0.25)
Y = np.arange(-5, 5, 0.25)
X, Y = np.meshgrid(X, Y)
R = np.sqrt(X**2 + Y**2)
Z = np.sin(R)
```

```
# Plot the surface.
```

```
surf = ax.plot_surface(X, Y, Z, cmap=cm.coolwarm,
                       linewidth=0, antialiased=False)
```

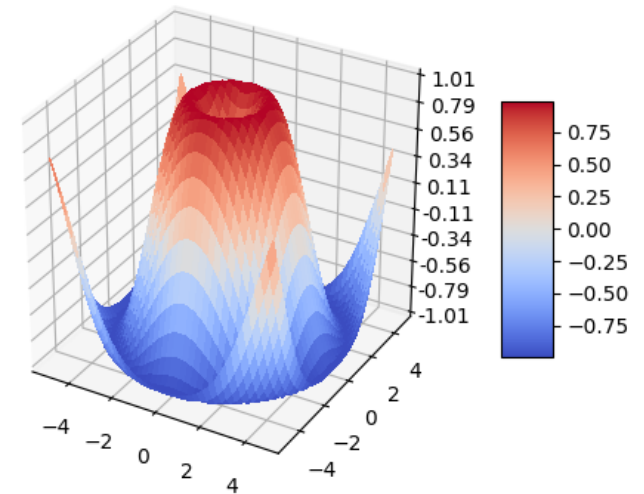
```
# Customize the z axis.
```

```
ax.set_zlim(-1.01, 1.01)
ax.zaxis.set_major_locator(LinearLocator(10))
ax.zaxis.set_major_formatter(FormatStrFormatter('%.02f'))
```

```
# Add a color bar which maps values to colors.
```

```
fig.colorbar(surf, shrink=0.5, aspect=5)
```

```
plt.show()
```

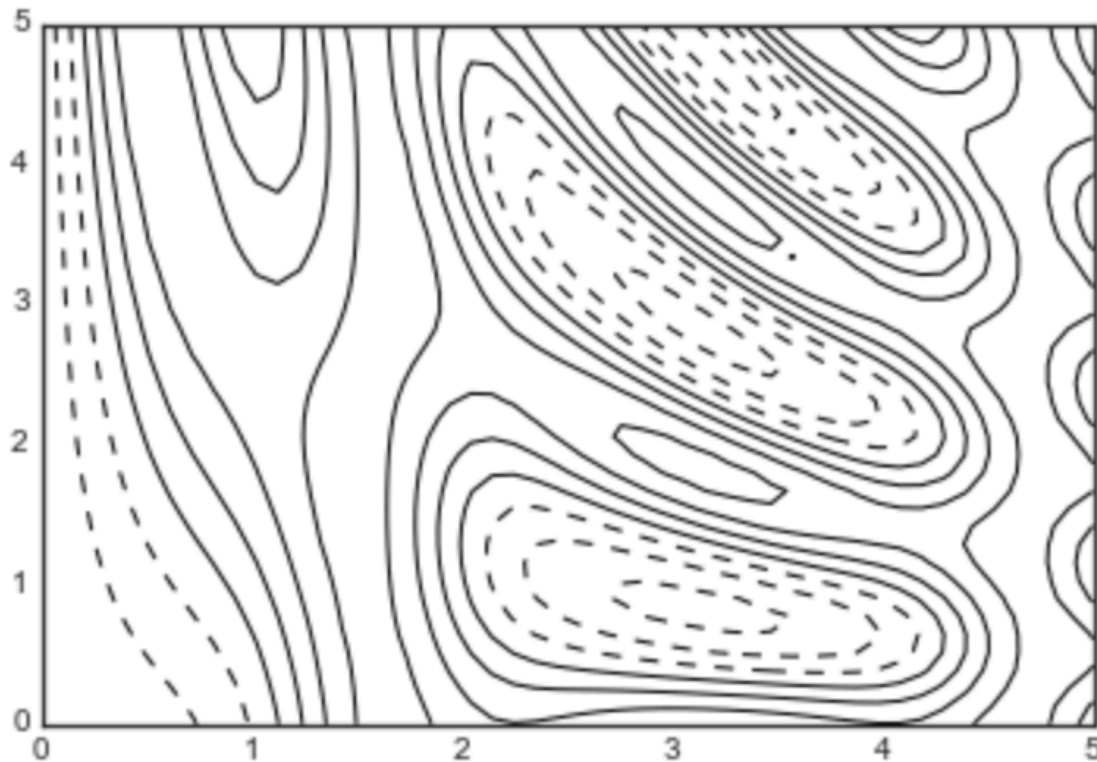


```
def f(x, y):  
    return np.sin(x) ** 10 + np.cos(10 + y * x) * np.cos(x)
```

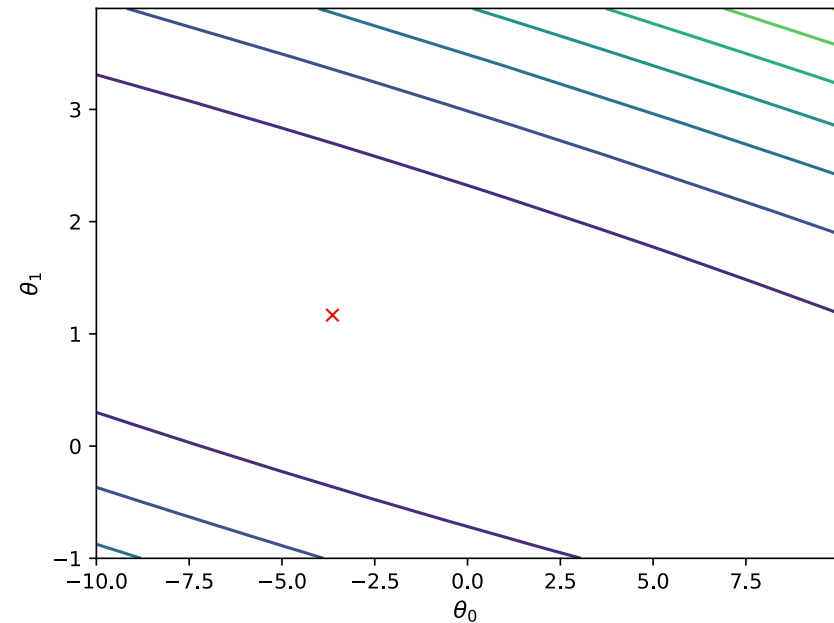
```
x = np.linspace(0, 5, 50)  
y = np.linspace(0, 5, 40)
```

```
X, Y = np.meshgrid(x, y)  
Z = f(X, Y)
```

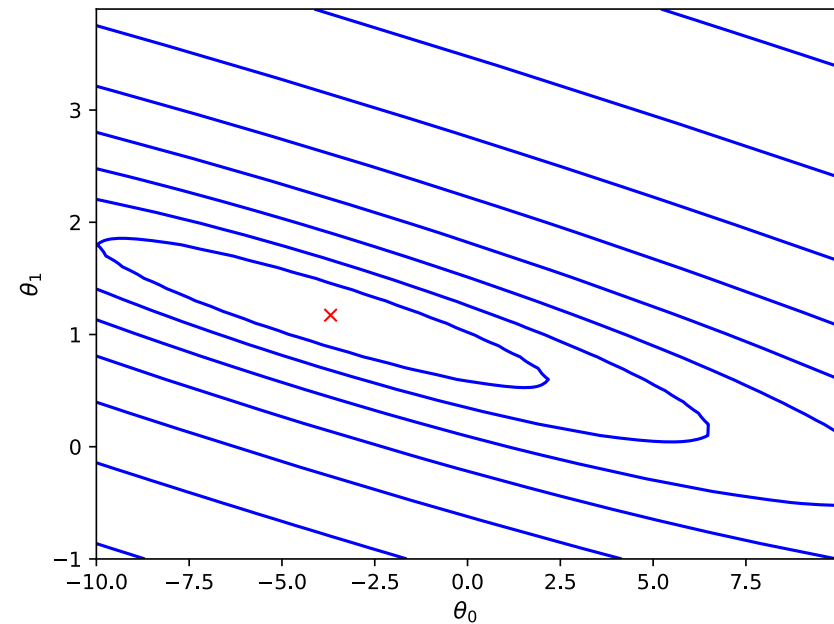
```
plt.contour(X, Y, Z, colors='black');
```



```
plt.contour(Theta0, Theta1, Coste)
```



```
plt.contour(Theta0, Theta1, Coste,  
            np.logspace(-2, 3, 20), colors='blue')
```



```
def make_data(t0_range, t1_range, X, Y):  
    """Genera las matrices X,Y,Z para generar un plot en 3D  
    """  
  
    step = 0.1  
    Theta0 = np.arange(t0_range[0], t0_range[1], step)  
    Theta1 = np.arange(t1_range[0], t1_range[1], step)  
  
    Theta0, Theta1 = np.meshgrid(Theta0, Theta1)  
    # Theta0 y Theta1 tienen las mismas dimensiones, de forma que  
    # cogiendo un elemento de cada uno se generan las coordenadas x,y  
    # de todos los puntos de la rejilla  
  
    Coste = np.empty_like(Theta0)  
    for ix, iy in np.ndindex(Theta0.shape):  
        Coste[ix, iy] = coste(X, Y, [Theta0[ix, iy], Theta1[ix, iy]])  
  
    return [Theta0, Theta1, Coste]
```

Práctica 1:

regresión lineal

solución vectorizada

Gradient descent algorithm

$$\left. \begin{array}{l} \text{repeat until convergence } \{ \\ \theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) \\ \theta_1 := \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) \cdot x^{(i)} \end{array} \right\} \begin{array}{l} \text{update} \\ \theta_0 \text{ and } \theta_1 \\ \text{simultaneously} \end{array}$$

$$\text{Repeat } \left\{ \begin{array}{l} \theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \dots, \theta_n) \end{array} \right\} \quad (\text{simultaneously update for every } j = 0, \dots, n)$$

$$\theta_j := \theta_j - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}$$

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

$$h_{\theta}(x) = \theta^T x$$

```
datos = carga_csv('ex1data1.csv')
```

```
X = datos[:, :-1]  
np.shape(X)          # (97, 1)  
Y = datos[:, -1]  
np.shape(Y)          # (97,)
```

```
m = np.shape(X)[0]  
n = np.shape(X)[1]
```

```
# añadimos una columna de 1's a la X  
X = np.hstack([np.ones([m, 1]), X])
```

```
alpha = 0.01  
Thetas, costes = descenso_gradiente(X, Y, alpha)
```


$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m \left(h_{\theta}(x^{(i)}) - y^{(i)} \right)^2$$

$$X = \begin{bmatrix} \text{---} & (x^{(1)})^T & \text{---} \\ \text{---} & (x^{(2)})^T & \text{---} \\ & \vdots & \\ \text{---} & (x^{(m)})^T & \text{---} \end{bmatrix} \quad \vec{y} = \begin{bmatrix} y^{(1)} \\ y^{(2)} \\ \vdots \\ y^{(m)} \end{bmatrix}$$

$$X\theta = \begin{bmatrix} (x^{(1)})^T \theta \\ (x^{(2)})^T \theta \\ \vdots \\ (x^{(m)})^T \theta \end{bmatrix} = \begin{bmatrix} \theta^T (x^{(1)}) \\ \theta^T (x^{(2)}) \\ \vdots \\ \theta^T (x^{(m)}) \end{bmatrix}$$

$$J(\theta) = \frac{1}{2m} (X\theta - \vec{y})^T (X\theta - \vec{y})$$

$$J(\theta) = \frac{1}{2m} (X\theta - \vec{y})^T (X\theta - \vec{y})$$

```
def coste(X, Y, Theta):  
    H = np.dot(X, Theta)  
    Aux = (H - Y) ** 2  
    return Aux.sum() / (2 * len(X))
```

$$\frac{\partial J(\theta)}{\partial \theta_j} = \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}$$

$$\begin{aligned} \begin{bmatrix} \frac{\partial J(\theta)}{\partial \theta_0} \\ \frac{\partial J(\theta)}{\partial \theta_1} \\ \vdots \\ \frac{\partial J(\theta)}{\partial \theta_n} \end{bmatrix} &= \frac{1}{m} \begin{bmatrix} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_0^{(i)} \\ \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_1^{(i)} \\ \vdots \\ \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_n^{(i)} \end{bmatrix} & h_{\theta}(x) - y = \begin{bmatrix} h_{\theta}(x^{(1)}) - y^{(1)} \\ h_{\theta}(x^{(2)}) - y^{(2)} \\ \vdots \\ h_{\theta}(x^{(m)}) - y^{(m)} \end{bmatrix} \\ &= \frac{1}{m} \sum_{i=1}^m ((h_{\theta}(x^{(i)}) - y^{(i)}) x^{(i)}) \\ &= \frac{1}{m} X^T (h_{\theta}(x) - y) \end{aligned}$$

$$\frac{\delta J(\theta)}{\delta \theta_j} = \frac{1}{m} X^T (h_{\theta}(x) - y)$$

```
def gradiente(X, Y, Theta, alpha):  
    NuevaTheta = Theta  
    m = np.shape(X)[0]  
    n = np.shape(X)[1]  
    H = np.dot(X, Theta)  
    Aux = (H - Y)  
    for i in range(n):  
        Aux_i = Aux * X[:, i]  
        NuevaTheta -= (alpha / m) * Aux_i.sum()  
    return NuevaTheta
```

