

Analyzing Summary Variables in the Presence of Partially Missing Longitudinal Data

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bit.ly/jlt-jsm2018

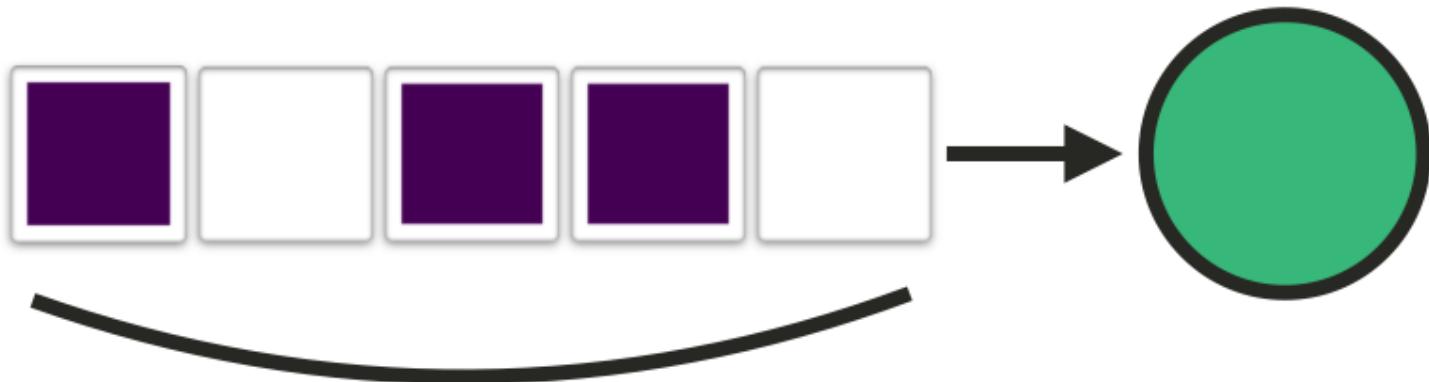
 [jenniferthompson/MissSumVars](https://github.com/jenniferthompson/MissSumVars)

 [@jent103](https://twitter.com/jent103)

Our Motivation



Our Motivation



Our Motivation



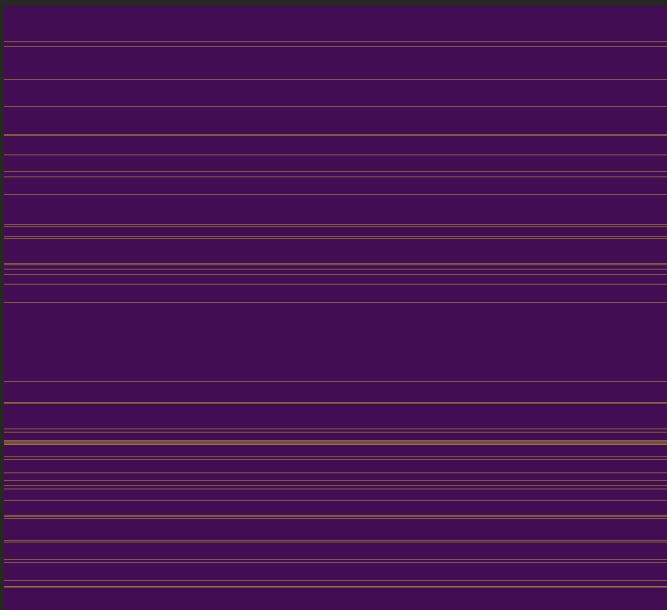
Is more delirium (*in-hospital brain dysfunction*) associated with scores on a cognitive test after hospital discharge?



The Problem

Prospective cohort

status (2.88%)

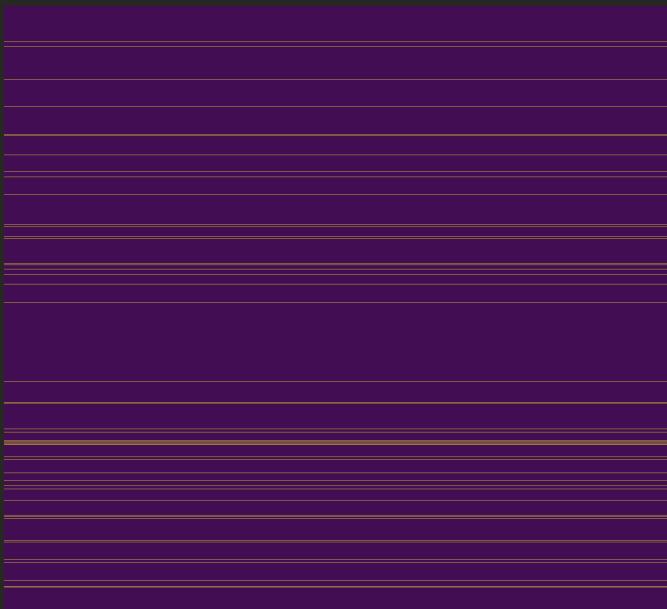


The Problem

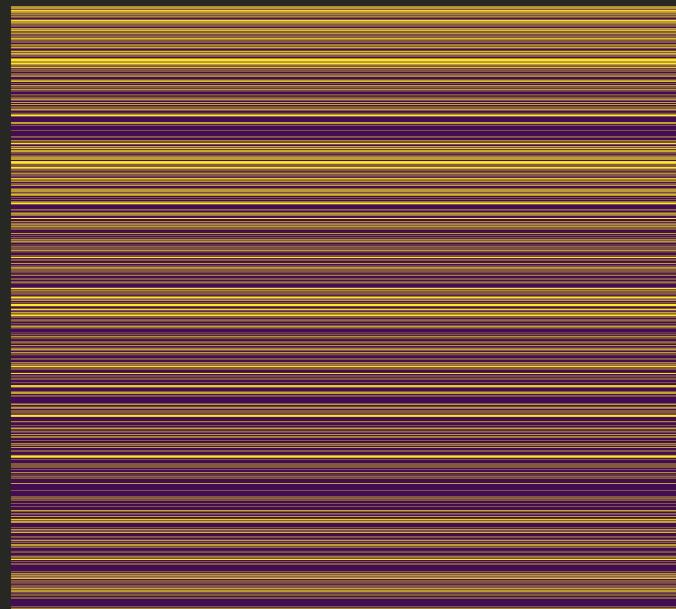
Prospective cohort

Retrospective EMR

status (2.88%)



status (32.19%)

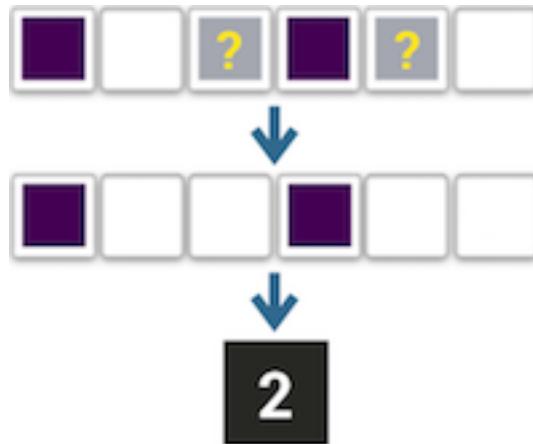


Strategies: Simple

Assume the "best"

NA = unexposed:

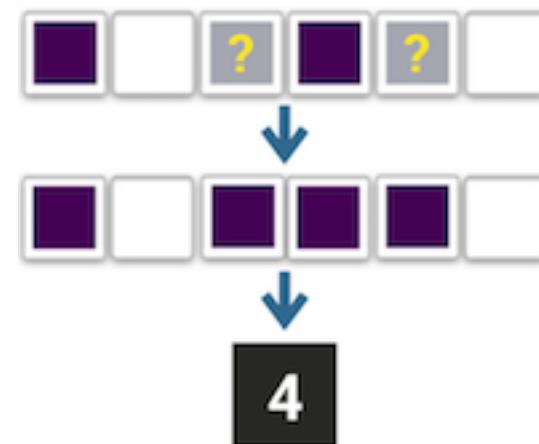
Only count the exposure we know about



Assume the "worst"

NA = exposed:

All missing time points get exposure



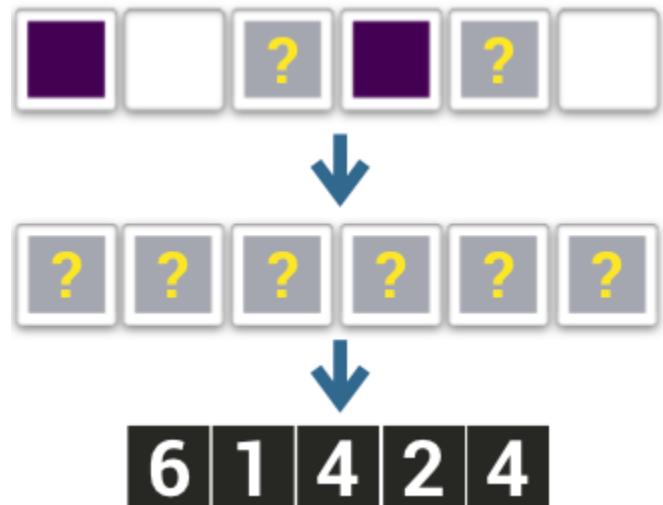
Pros: Straightforward to implement; plausible, if we know a lot about data collection

Cons: Prone to bias

Strategies: Imputation

Assume nothing

1. If subject missing any time point,
entire summary value = NA
2. Multiply impute missing *summary values*
before modeling



Pros:

- Fairly simple to implement
- Acknowledges uncertainty

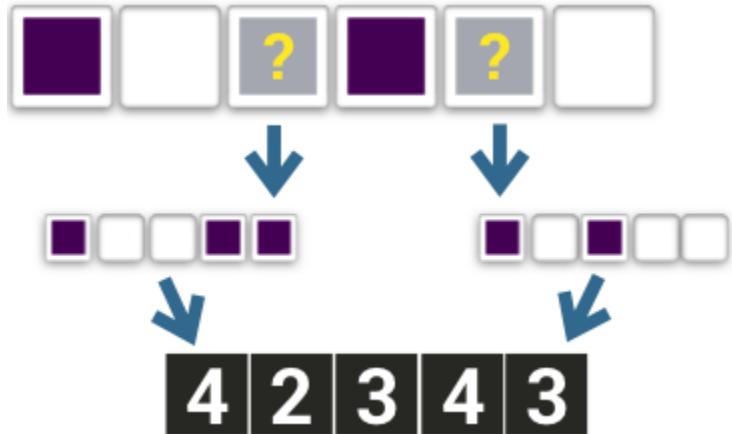
Cons:

- Ignores the data we *do* have
- Likely to *overestimate* uncertainty

Strategies: Imputation

Assume the minimum

1. Multiply impute missing *time points*
2. Summarize each imputed dataset
3. Use these imputed summary datasets when modeling



Pros:

- Maximizes use of data we have, including available covariate information

Cons:

- Computation time
- Data wrangling

Simulations

- 5%, 20%, 35%, 50% of patient-days missing exposure value
- Types of missingness:
 - MCAR
 - MAR
 - Missingness in exposure weakly, moderately, strongly associated with daily severity of illness
 - MNAR
 - Missingness in exposure weakly, moderately, strongly associated with true exposure value
- True relationship with outcome: ranges from 0 to -5
- Imputation methods incorporate severity of illness

STANDARD ERROR

NA = unexposed NA = exposed Impute summary Impute daily

MCAR

MAR
Weak

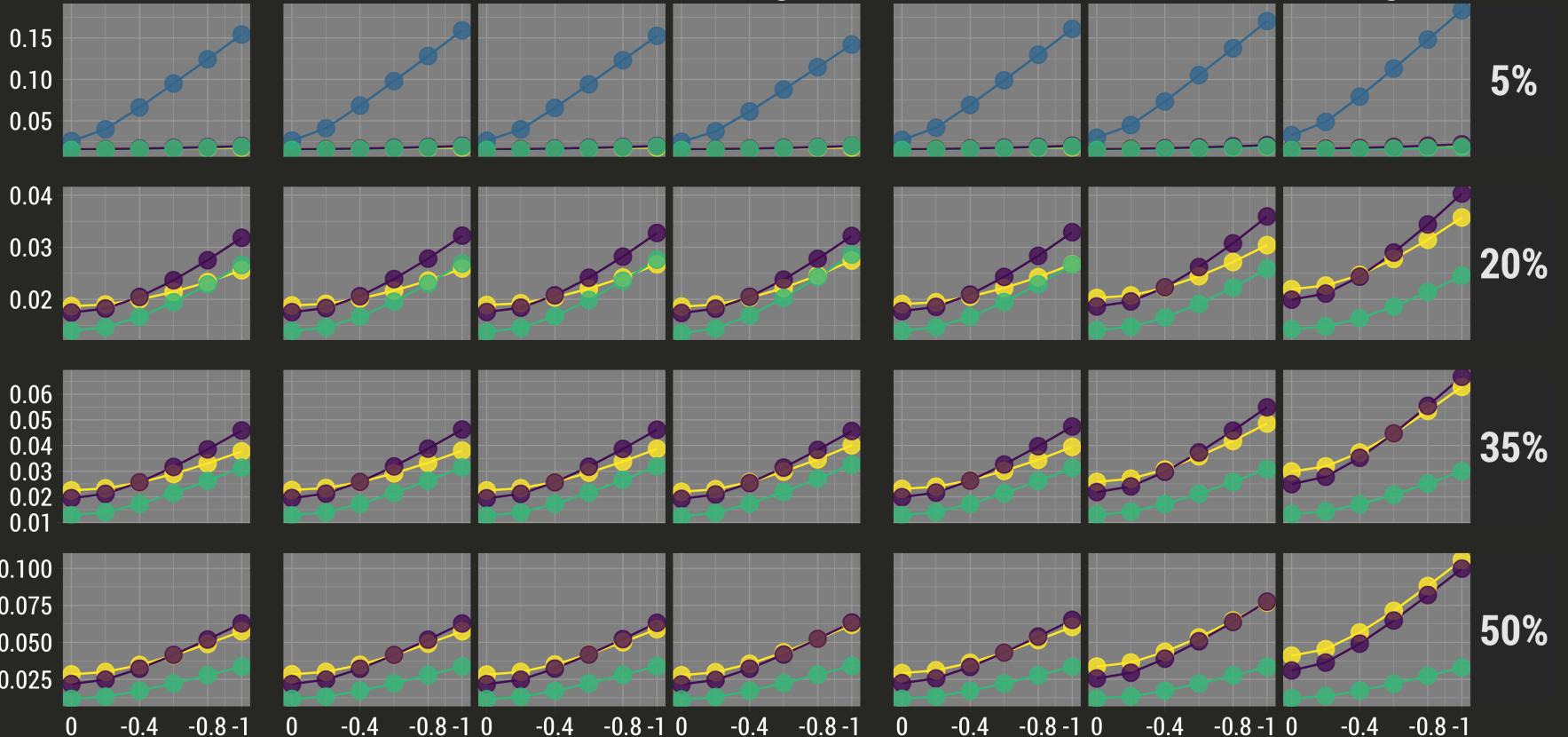
MAR
Moderate

MAR
Strong

MNAR
Weak

MNAR
Moderate

MNAR
Strong

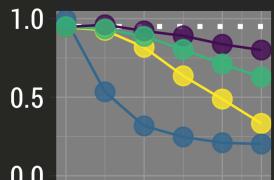


True Effect Size

COVERAGE

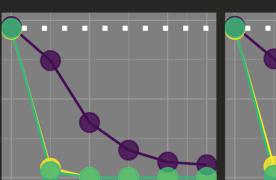
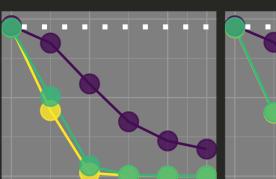
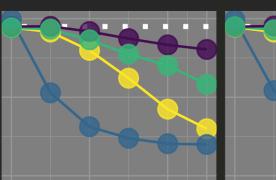
NA = unexposed NA = exposed Impute summary Impute daily

MCAR



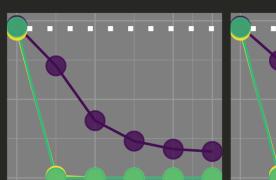
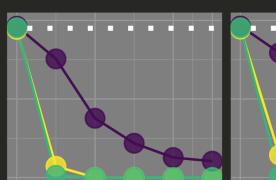
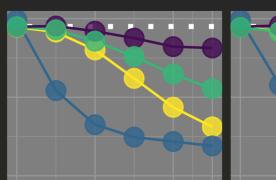
0 -0.4 -0.8 -1

MAR
Weak



0 -0.4 -0.8 -1

MAR
Moderate



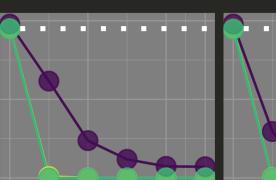
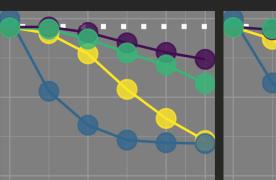
0 -0.4 -0.8 -1

MAR
Strong



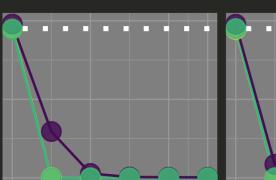
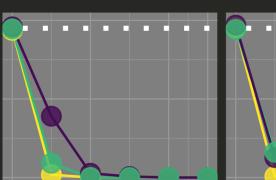
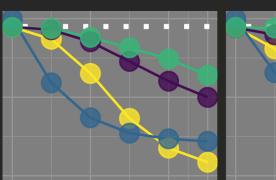
0 -0.4 -0.8 -1

MNAR
Weak



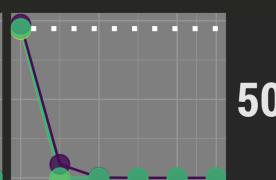
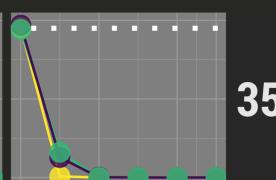
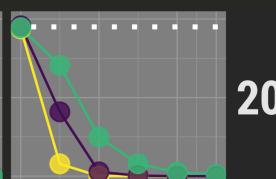
0 -0.4 -0.8 -1

MNAR
Moderate



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MNAR
Strong



0 -0.4 -0.8 -1

True Effect Size

POWER

NA = unexposed NA = exposed Impute summary Impute daily

MCAR

MAR
Weak

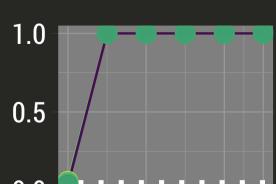
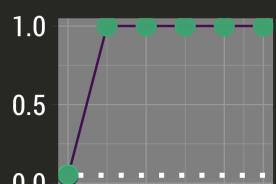
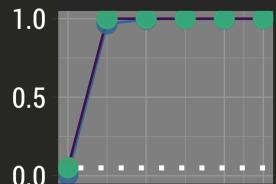
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Moderate

MAR
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MNAR
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5%

20%

35%

50%

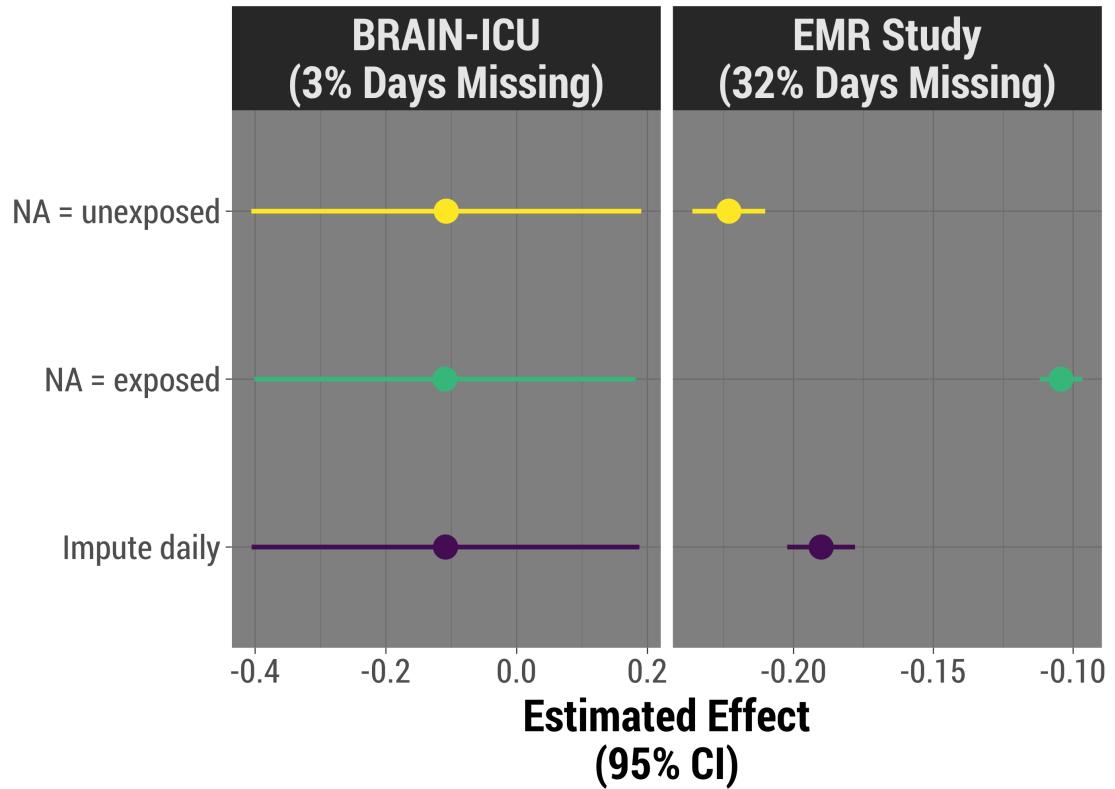
True Effect Size

Examples with Motivating Data

- Duration of exposure vs outcome in two real-world studies, adjusting for one covariate
- Three strategies to summarize duration of exposure

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- Duration of exposure vs outcome in two real-world studies, adjusting for one covariate
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Takeaways

- Understand your data and its missingness
- Don't ignore your missingness
- Don't throw out your data
- Better safe than sorry: imputing at the lowest level is usually worth it

Future Exploration

- Continuous exposure
- Complex relationships between covariates/exposure, missingness

Acknowledgements

- Stef van Buuren for mice
- Davis Vaughn, Henrik Bengtsson for furrr and future
- Brooke Watson for BRRR
- VUMC CIBS Center principal investigators

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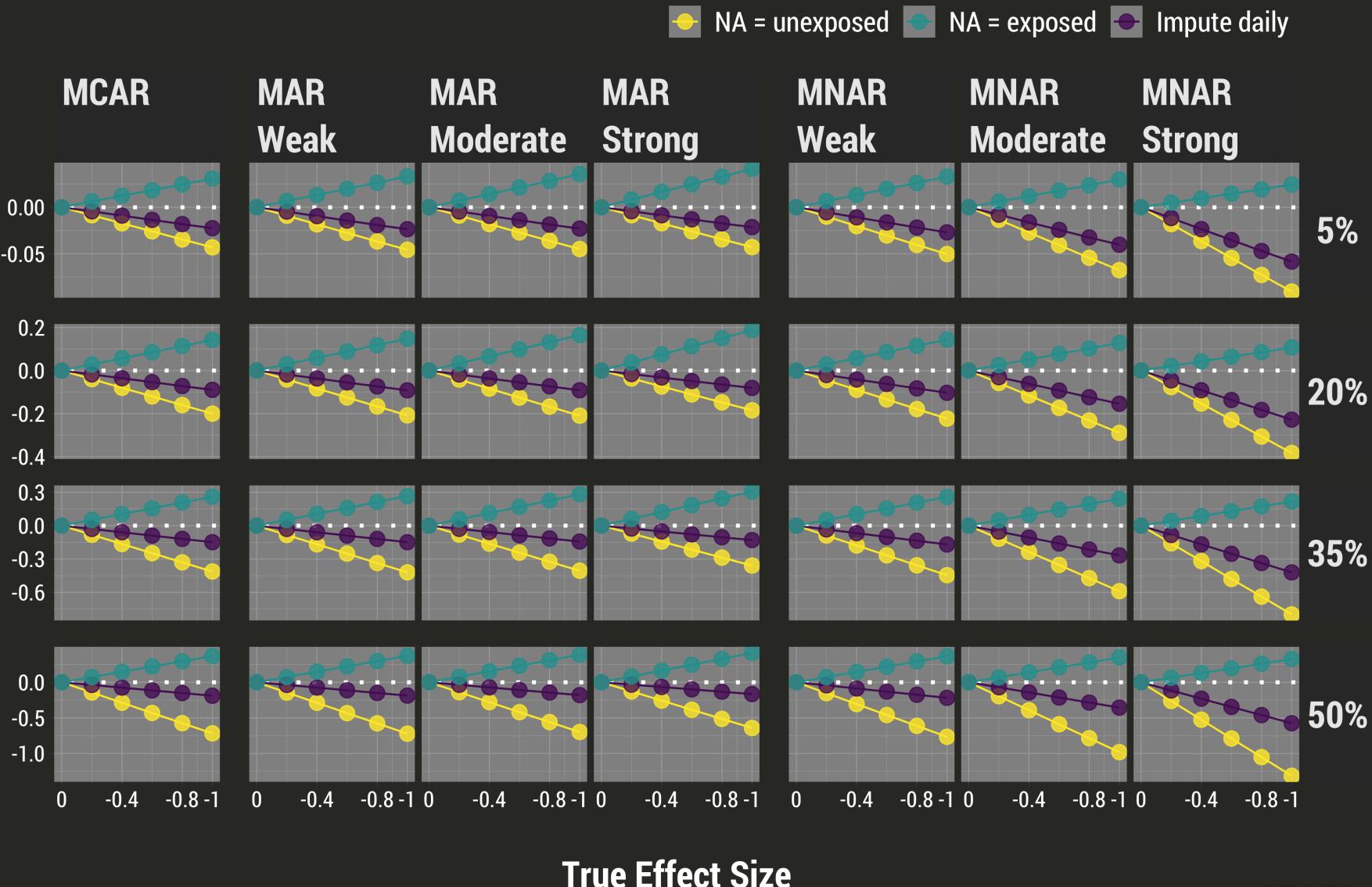
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 [@jenniferthompson](https://orcid.org/0000-0002-169X-103X)

 j.thompson@vumc.org

 jenthompson.me

BIAS



STANDARD ERROR

NA = unexposed NA = exposed Impute daily

MCAR

MAR
Weak

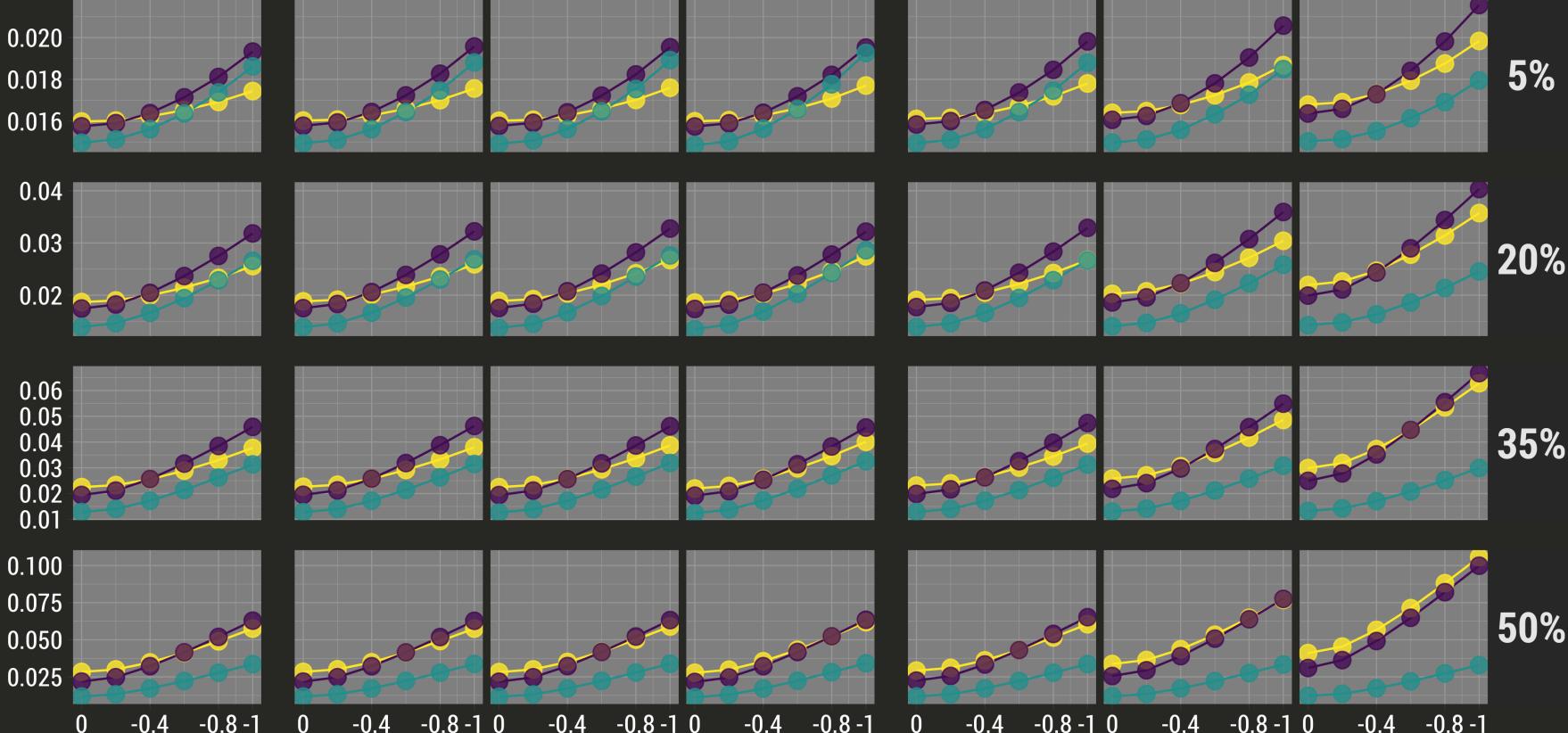
MAR
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True Effect Size

CI WIDTH

NA = unexposed NA = exposed Impute daily

MCAR

MAR
Weak

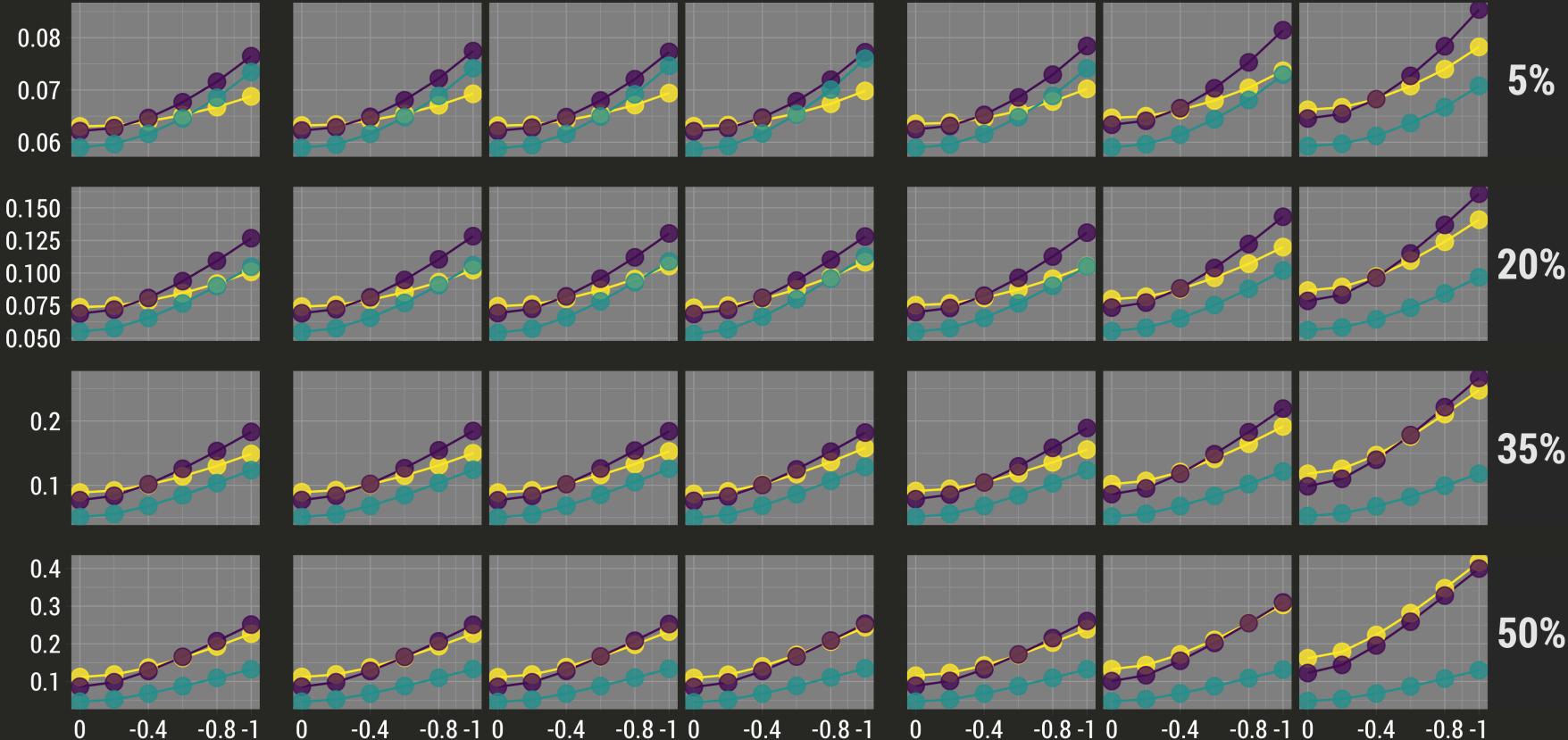
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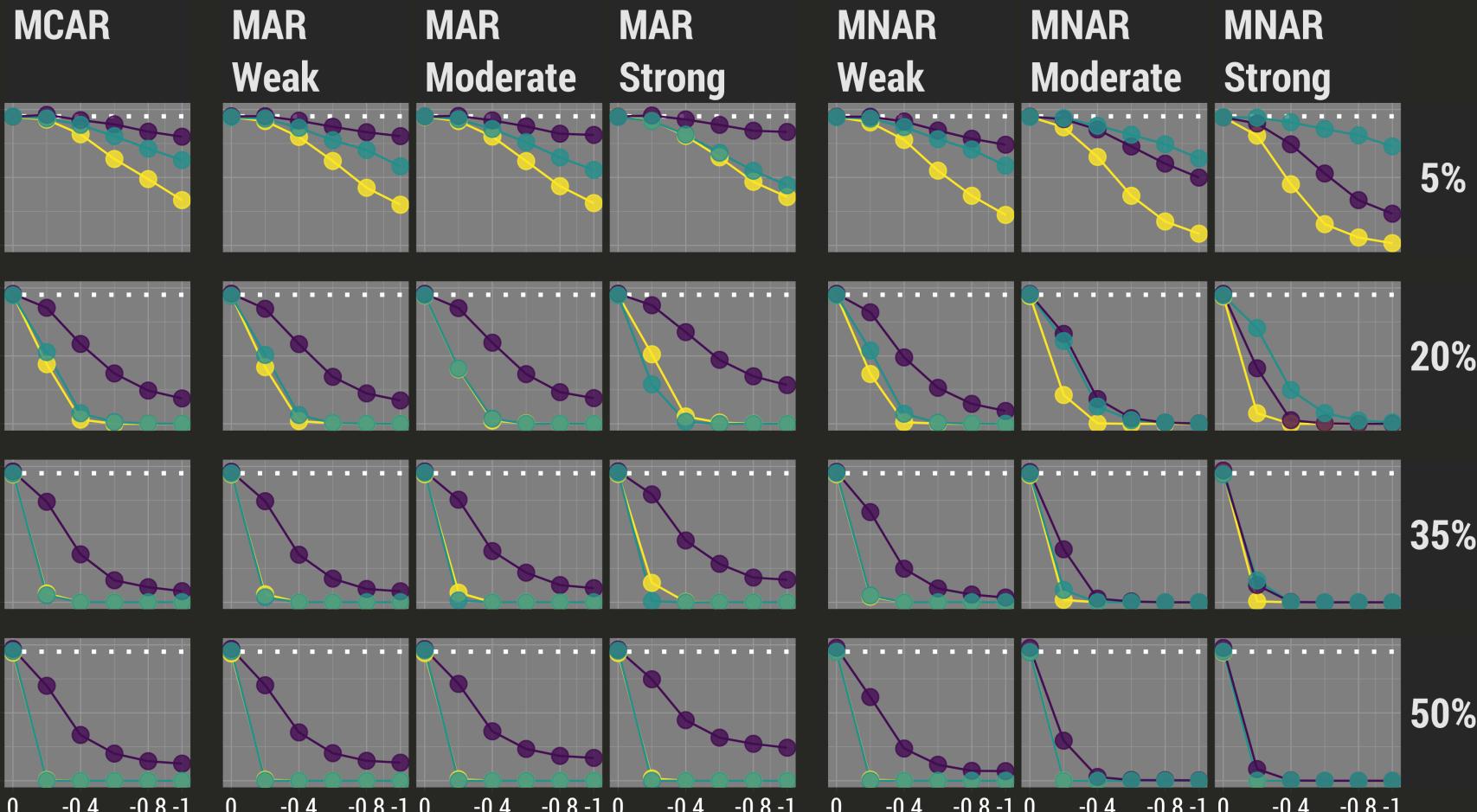
MNAR
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True Effect Size

COVERAGE

 NA = unexposed  NA = exposed  Impute daily

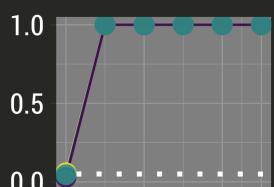
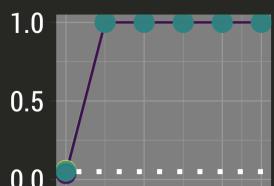
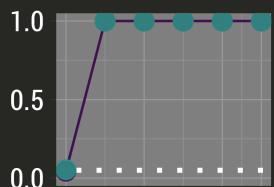
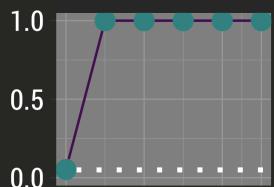


True Effect Size

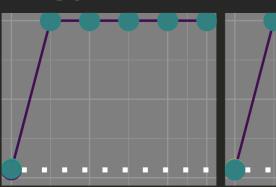
POWER

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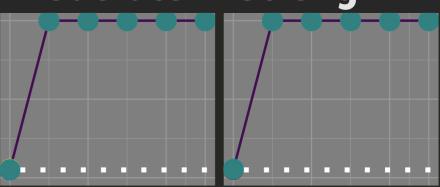
MCAR



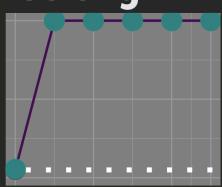
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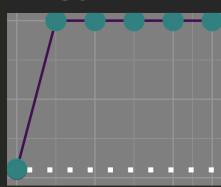
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Moderate



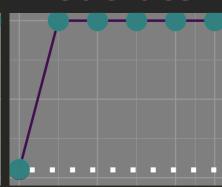
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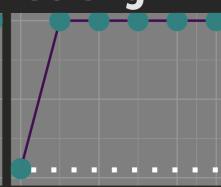
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