

Lessons learned from bugs in models of human history

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SG: How to avoid simulating the wrong demographic model

Abstract

Simulation plays a central role in population genomics studies. Recent years have seen rapid improvements in software efficiency that make it possible to simulate large genomic regions for many individuals sampled from large numbers of populations. As the complexity of demographic models we study grows, however, there is an ever-increasing opportunity to introduce bugs in their implementation. Here we describe two errors made in defining population genetic models using the **msprime** coalescent simulator that have found their way into the published record. We discuss how these errors have affected downstream analyses and give recommendations for software developers and users to reduce the risk of such errors.

Introduction

In the effort to build more realistic simulations of genetic diversity, scientific software developers often focus on computational speed and biological realism. Documentation and application programming interface (API), however, also determine whether software is used, and whether it is used correctly.

The **msprime** coalescent simulator (Kelleher et al., 2016; Nelson et al., 2020; Kelleher and Lohse, 2020) is now widely used in genetics studies. Much of its appeal is the large increase in efficiency over the classical **ms** program (Hudson, 2002) which makes it feasible to simulate large samples of whole chromosomes for the first time. Another distinct advantage of **msprime** is the Python API that is its primary interface, greatly increasing the flexibility and ease of use over the standard approach of text-based command line interfaces. In particular, programs like **ms** required users to specify cryptic command line options to describe demographic models. Particularly for the large models we use today, these are not intuitive or comprehensible for humans. The Python API for **msprime** by contrast, allows the user to state models in a more human-readable manner: an example of model specification for the two softwares is provided in the Methods section.

Implementing multi-population models of demographic history for either software is hard and error-prone. In this note we discuss two implementation errors that arose through unfortunate design decisions in **msprime**'s demography API and which then found their way into the scientific record. The first error has relatively mild effects on genetic diversity but was used in many publications, while the second error was used only once but had a large impact on the simulation results. In light of these implementation errors, we discuss improvements to **msprime**'s API motivated by these discoveries and, more generally, best practices for implementing and simulating complex multi-population demography.

Case 1: A misspecified model in msprime’s documentation

To illustrate the demography API, **msprime** included a description of a widely-used three population Out-of-Africa model (Gutenkunst et al., 2009) as part of its tutorial documentation. In this model (Fig. 1A), Eurasian (CEU and CHB) and African (YRI) populations split from each other in the deep past, followed by a more recent split of European and Asian populations, with variable rates of continuous migration between each of the populations. However, the implementation in the **msprime** tutorial was incorrect. Before the time of the split of African and Eurasian populations, when there should have been just a single randomly mating population, migration was allowed to occur between the ancestral population and a second population with size equal to the Eurasian bottleneck size for all time into the past (Fig. 1B). This incorrect model was introduced into the tutorial for **msprime** ver. 0.3.0 and remained in the documentation for around four years.

Fortunately, the effects of this error are subtle. Population sizes and structure since the time of the earliest split are unaffected, so differences in expected F_{ST} are negligible between the intended and incorrect models. However, the ancient structure distorts the distribution of early TMRCA. The extraneous ancient population increases the long-term effective population size, resulting in roughly 4% excess heterozygosity in contemporary populations compared to the intended model (Fig. 1C-F).

Even though the error had a limited effect on simulated data, the tutorial code has been copied many times and used in publications. By searching for some identifying strings from the model definition on GitHub, we found 32 repositories containing either direct copies of the erroneous model code, or code that was obviously derived from it. (We have opened issues on each of these repositories to alert the authors.) In most cases the publications used simulations to test some inference method and were not directly concerned with the details of the demography, and the model was simply used as an example of a complex population history (Kelleher et al., 2019; Albers and McVean, 2020; Tong and Hernandez, 2020). Zhou et al. (2018) used the incorrect model as an example of how their method for visualising demographic models can support **msprime** input. Finally, Pfaffelhuber et al. (2020) used simulations of the incorrect model demography to evaluate their method for choosing ancestry informative markers. Given the very subtle effect of the incorrect model on demography (and the fact the method was evaluated using other simulations and real data), it seems unlikely that the model details had any qualitative effect on their conclusions.

This long-standing error could have been prevented by better API design. To model a population split currently in **msprime**, a user must specify a **MassMigration** event that moves lineages from one population to another and then must also remember to turn off migration between those populations at the same time. The release of **msprime** version 1.0 will introduce a **PopulationSplit** event, which more intuitively links the merger of lineages with appropriate changes in migration rates at the time of the split.

Case 2: Incorrect model parameters in an analysis pipeline

In another publication using this model (Martin et al., 2017), a separate error was introduced: the model itself was defined as suggested in the documentation (using updated parameters from Gravel et al. (2011)) and inspected using the **msprime** debugging tools. After these initial checks were made, however, the simulation was performed without passing the parameter of demographic events, so that the three populations never merged as expected and remained separated with low levels of migration (Fig 2A), leading to a vast overestimate of the divergence across human populations. While the correct model predicts a mean F_{ST} of 0.05 – 0.10 across the three population, the simulated model generated F_{ST} ranging between 0.3 – 0.6, depending on the populations considered. Overall diversity was also strongly affected: heterozygosity was more than doubled in African populations and reduced by more than half in Eurasian populations relative to the intended model.

This simulation was performed to assess the transferability of polygenic risk scores across human populations. In other words, it sought to explore how human demographic history and population structure affect our ability to predict genetic risk in diverse populations given the well-documented unequal representation in medical genetic studies (Popejoy and Fullerton, 2016). The resulting publication has been influential in the discussion of health inequalities and genomics, with over 350 citations since 2017. The large excess in divergence under the incorrect model here exaggerated the role of demography and genetic drift in limiting the transferability of genetic risk scores across populations.

Difficulties in transferability remain in the intended model (Fig. 2), although risk prediction in each population is significantly improved (compare to Fig. 5 in Martin et al. (2017)). The intended simulations indicate that the accuracy of genetic risk scores is still substantially reduced in understudied populations (Fig. 2E-G), supporting the main conclusion of Martin et al. (2017). However, the reduction is much less pronounced than reported. In particular, we do not observe large differences in mean risk prediction across populations (Fig. 2C,D), as presented in Martin et al. (2017). At least for the neutral polygenic architectures considered here, genetic drift alone does not appear to induce large directional biases in mean predicted risk across ethnicities.

Conclusions

The implementation of complex demographic models is error prone, and such errors can have a large impact on downstream analyses and interpretation. The discovery and correction of the demographic models discussed here underscore how API design choice can lead to the propagation of mistakes that are difficult to notice. We therefore recommend the following steps to ensure more robust simulations.

First, the design of user interface and API for scientific software matters, and many bugs can be prevented by using more intuitive interfaces. Whereas the original **msprime** API required the user to pass three separate parameters to specify a demographic model, **msprime** ver. 1.0 will introduce a **Demography** class, which wraps these three parameters. Thus, instead of writing

```
dbg = msprime.DemographyDebugger(
    population_configurations=population_configurations,
    migration_matrix=migration_matrix,
    demographic_events=demographic_events)
dbg.print_history()
ts = msprime.simulate(
    population_configurations=population_configurations,
    migration_matrix=migration_matrix,
    demographic_events=demographic_events)
```

with the error-inducing need to re-enter parameter information, we would now write

```
demography = msprime.Demography(
    population_configurations=population_configurations,
    migration_matrix=migration_matrix,
    demographic_events=demographic_events)
dbg = demography.debug()
dbg.print_history()
ts = msprime.simulate(demography=demography)
```

Second, from a user’s perspective, steps should be taken to validate the implemented demographic model. This could include verification through code review or an independent implementation of the model, which is the approach taken by **stdpopsim** (Adrion et al., 2019) to build a library of quality-controlled models and simulation resources for a growing number of commonly studied species. Such review likely would have caught the error in the **msprime** documentation.

Basic statistical validation should also be performed on any simulated model, and recent progress in computing summary statistics from tree sequence data can make this easier (Ralph et al., 2020). If simulations are so large that statistical validation is burdensome, subsets of the simulated data can be analyzed to ensure general diversity patterns are sound. Such tests likely would have caught the error in Martin et al. (2017).

Graphical inspection of demographic models can also help identify issues, especially if visualization can be automated. **msprime** does contain a demography debugging tool summarizing demographic events occurring over time, and various efforts are underway to facilitate the specification and visualization of population genetics models, such as Zhou et al. (2018) and the **demography** package used in this paper.

Finally, openness is essential to the self-correcting nature of science. We only know about these errors because of open code and open-source development processes. By making their entire pipeline available, Martin et al. (2017) not only enabled other research teams to build upon their findings, but they made it

possible for such errors to be found and corrected. There must be many, many more mistakes out there, and we need both pre- and post-publication vigilance from users and developers to ensure the soundness of the large body of simulation-based analyses.

Methods

We computed the expected allele frequency spectrum using **moments** ver. 1.0.3 (Jouganous et al., 2017), and LD-decay curves using **moments.LD** (Ragsdale and Gravel, 2019). F_{ST} and other diversity statistics were computed from the expected AFS and verified using branch statistics from the tree sequence records of **msprime** simulations using **tskit** ver. 0.2.3 (Ralph et al., 2020). Demographic models were plotted using the **demography** package (<https://github.com/apragsdale/demography>, ver. 0.0.3). We used the original pipeline from Martin et al. (2017) available from https://github.com/armartin/ancestry_pipeline/blob/master/simulate_prs.py. We updated the pipeline to run with the correct demographic parameters and more recent versions of **msprime** and **tskit**, and the updated pipeline is available at <https://github.com/apragsdale/PRS>. Data and python scripts to recreate Figures 1 and 2 can be found at <https://github.com/jeromekelleher/msprime-model-errors>. A full list of the GitHub repositories containing copies of the erroneous model are also given here.

For reference, the Gutenkunst et al. (2009) demographic model, as written in **ms**, is

```
-n 1 1.682020 -n 2 3.736830 -n 3 7.292050
-eg 0 2 116.010723 -eg 0 3 160.246047
-ma x 0.881098 0.561966 0.881098 x 2.797460 0.561966 2.797460 x
-ej 0.028985 3 2 -en 0.028985 2 0.287184
-ema 0.028985 3 x 7.293140 x 7.293140 x x x x x
-ej 0.197963 2 1 -en 0.303501 1 1
```

The equivalent model using **msprime** is more human readable and provided in full at <https://github.com/jeromekelleher/msprime-model-errors>. The demographic events are given as

```
demographic_events = [
    # CEU and CHB merge into B with rate changes at T_EU_AS
    msprime.MassMigration(
        time=T_EU_AS, source=2, destination=1, proportion=1.0),
    msprime.MigrationRateChange(time=T_EU_AS, rate=0),
    msprime.MigrationRateChange(
        time=T_EU_AS, rate=m_AF_B, matrix_index=(0, 1)),
    msprime.MigrationRateChange(
        time=T_EU_AS, rate=m_AF_B, matrix_index=(1, 0)),
    msprime.PopulationParametersChange(
        time=T_EU_AS, initial_size=N_B, growth_rate=0, population_id=1),
    # Population B merges into YRI at T_B
    msprime.MassMigration(
        time=T_B, source=1, destination=0, proportion=1.0),
    msprime.MigrationRateChange(time=T_B, rate=0),
    # Size changes to N_A at T_AF
    msprime.PopulationParametersChange(
        time=T_AF, initial_size=N_A, population_id=0)
]
```

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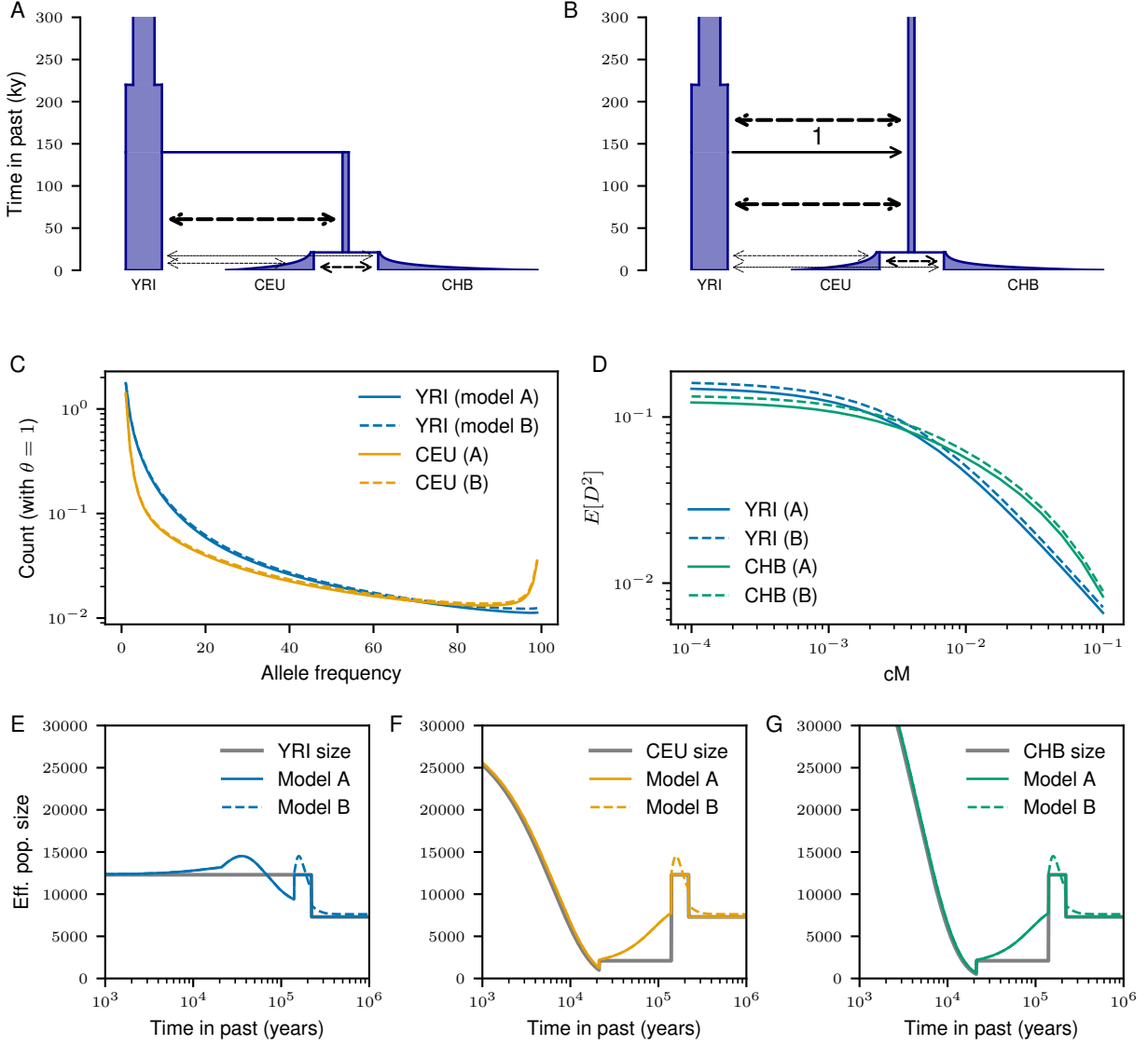


Figure 1: **Expected diversity statistics under the Gutenkunst et al. (2009) model.** (A) The correctly implemented model. Dashed arrows depict continuous migration. (B) The incorrectly implemented model from the `msprime` tutorial, with migration continuing into the past beyond the mass migration event with proportion 1 from the ancestral population to the bottleneck population. (C) Marginal allele frequency spectra under the two models. Heterozygosity in the incorrect model is inflated by 3.5%, though the general shape of the distributions are qualitatively similar. (D) Similarly, the increased heterozygosity leads to excess D^2 , though the LD-decay is qualitatively similar between models. (E-G) True size history for each population plotted against the expected size history from the expected inverse coalescence rates.

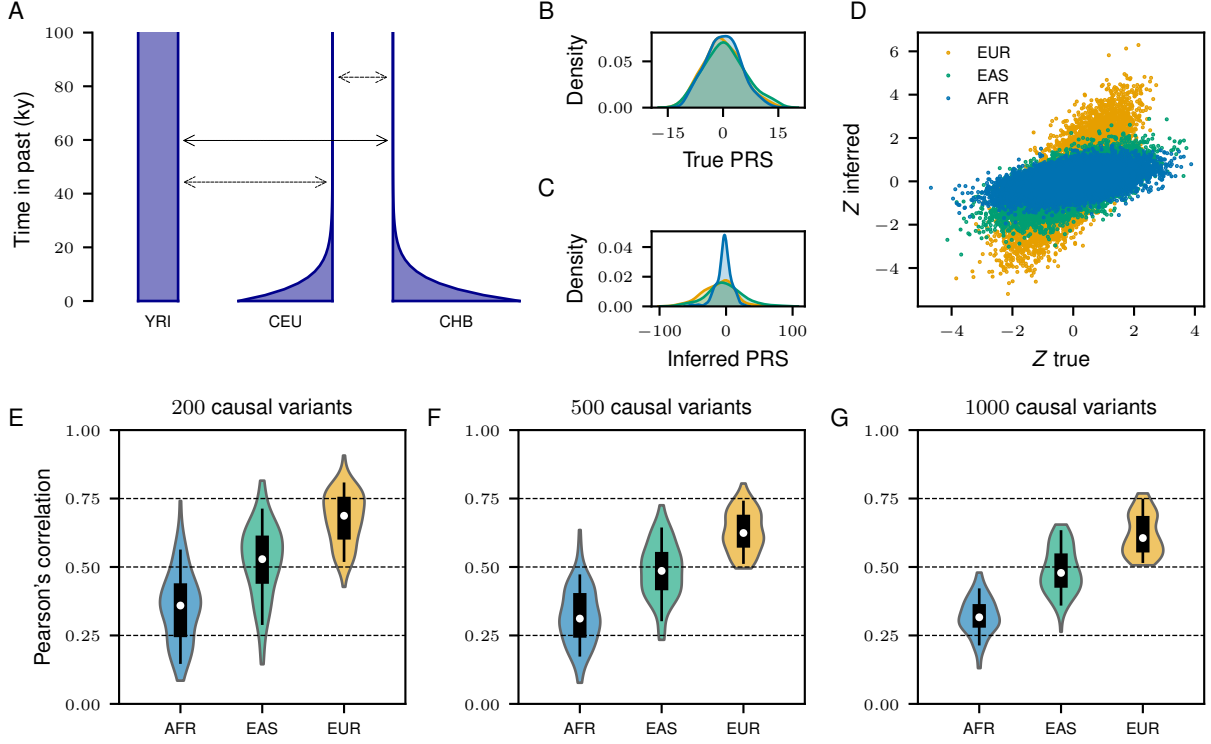


Figure 2: **The transferability of PRS under neutrality.** (A) In Martin et al. (2017), the simulated demographic model did not apply demographic events in the past, so continental populations were simulated as isolated with low levels of migration for all time. The intended model is shown in Figure 1A. (B-G) We repeated the simulation experiment in Martin et al. (2017) using the correct demographic model. While risk prediction in the African and East Asian population is reduced compared to the studied European population, the reduction in prediction accuracy is not as hopeless as originally reported. Notably, under a neutral polygenic architecture, we do not expect significant bias in inferred PRS in any of the populations (C, D). Correlations were computed over 100 simulation replicates. For direct comparison to the original study, see Figure 5 in Martin et al. (2017).